5f. Array Indexing

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INTRODUCTION

In order to mutate vectors, you first need to identify the elements you wish to modify. This process is known as **vector indexing**. We've already covered several basic methods for indexing, including vectors and ranges (e.g., $\times[1,2,3]$ or $\times[1:3]$). While these approaches are effective for simple selections, they fall short for more complex scenarios, precluding for example selections based on conditions.

This section expands our toolkit by introducing some additional forms of indexing. The techniques presented primarily build on broadcasting Boolean operations.

LOGICAL INDEXING

Logical indexing (also known as *Boolean indexing* or *masking*) allows you to select elements based on conditions. Considering a vector \boxed{x} , this is achieved using a Boolean vector \boxed{y} of the same length as \boxed{x} , which acts as a filter: $\boxed{x[y]}$ retains elements where \boxed{y} is \boxed{true} and excludes those where \boxed{y} is \boxed{false} .

```
LOGICAL INDEXING

x = [1,2,3]
y = [true, false, true]

julia> [x[y]]
2-element Vector{Int64}:
1
3
```

OPERATORS AND FUNCTIONS FOR LOGICAL INDEXING

Logical indexing becomes a powerful tool when we leverage broadcasting operations, allowing you to easily specify conditions via Boolean vectors. For instance, to select all the elements of \boxed{x} lower than 10, you can broadcast a comparison operator or a custom function.

When dealing with multiple conditions, the conditions must be combined using the logical operators and []. ¹ The following example illustrates the syntax for doing this. Note that *all* operators must be broadcasted, since logical operators only work with scalar values.

```
INDEXING VIA BROADCASTING FUNCTION

x = [3, 6, 7, 8, 100]

# numbers greater than 5, lower than 10, but not including 8
condition(a) = (a > 5) && (a < 10) && (a ≠ 8) #function to eventually broadcast
y = x[condition.(x)]

julia> y

1-element Vector{Int64}:
6
```

The example reveals that directly broadcasting *operators* may result in verbose code, due to the repeated use of dots in the expression. In contrast, approaches based on functions or the macro @. keep the syntax simple, reducing boilerplate code.

LOGICAL INDEXING VIA IN AND E

Remark

The symbols \in and \notin used in this section can be inserted via tab completion:

- € by \in
- ∉ by \notin

Another approach to selecting elements through logical indexing involves in and e. Each of these symbols is available as a function and an operator, and they check whether a *scalar* a belongs to a given collection in so a function in as a function and e as an operator.

The function in(a, list) evaluates whether the scalar a matches any element in the vector list, yielding the same result as $a \in list$. For example, both in(2, [1, 2, 3]) and $a \in [1, 2, 3]$ return true, as $a \in [1, 2, 3]$.

By replacing the scalar a with a collection x, in and e can define Boolean vectors via broadcasting. Recall, though, that broadcasting defaults to iterating over pairs of elements. This means that executing in.(x, list) or $extbox{$x$} . extbox{$x$} . extbo$

As an illustration, below we create a vector y that contains the minimum and maximum of the vector x.

```
FUNCTION 'IN' AND '€'
            = [-100, 2, 4, 100]
list = [minimum(x), maximum(x)]
# logical indexing (both versions are equivalent)
bool_indices = in.(x, Ref(list)) #'Ref(list)' can be replaced by '(list,)'
bool_indices = (\epsilon).(x,Ref(list))
             = x[bool_indices]
julia> | bool_indices |
4-element BitVector:
 0
 0
 1
julia> y
2-element Vector{Int64}:
 - 100
  100
```

Remark

The in function has an alternative curried version, allowing the user to directly broadcast in while treating list as a single element. The syntax for doing this in(list).(x), as shown in the example below.

Remark

The functions and operators in and in allow for negated versions in and in (equivalent to in), which select elements *not* belonging to a set.

Below, we apply them to retain the elements of \boxed{x} that are not its minimum or its maximum.

```
FUNCTION '!IN' AND '∉'
            = [-100, 2, 4, 100]
list = [minimum(x), maximum(x)]
#identical vectors for logical indexing
bool_indices = (!in).(x, Ref(list))
bool_indices = (\notin).(x, Ref(list))
                                         #or `(!∈).(x,
Ref(list)) `
julia> bool_indices
4-element BitVector:
1
 1
julia> [x[bool_indices]]
2-element Vector{Int64}:
 2
 4
```

THE FUNCTIONS 'FINDALL' AND 'FILTER'

We close this section by presenting two additional methods for element selection. They're provided by the functions filter and findall.

The function filter returns the *elements* of a vector x satisfying a given condition. Despite what the name may suggest, filter retains elements rather than discard them. The condition is specified by a function that returns a Boolean scalar.

```
'FILTER'

x = [5, 6, 7, 8, 9]

y = filter(a -> a < 7, x)

julia> y

2-element Vector{Int64}:
    5
    6
```

The function $\boxed{\text{findall}}$ does the same as $\boxed{\text{filter}}$, but returns the *indices* of $\boxed{\times}$. With $\boxed{\text{findall}}$, the condition can be stated in two ways: either via a Boolean scalar function or a Boolean vector.

FOOTNOTES

^{1.} The logical operators & and | | | were introduced in the section about conditional statements.