

# 6d. Useful Functions for Vectors

Martin Alfaro

PhD in Economics

## INTRODUCTION

This section provides an overview of essential functions for manipulating vectors, including sorting, identifying unique elements, counting occurrences, and ranking data. Our ultimate goal is to apply these functions in a practical context, which we'll do in the next section.

## SORTING VECTORS

The `sort` function allows the user to arrange elements in a specific order. By default, it sorts elements in ascending order, but this can be easily reversed to a descending order by setting the keyword argument `rev = true`. The function comes in two variants: `sort`, which returns a new sorted copy, and the in-place version `sort!`, which directly updates the vector.

### **SORT (ASCENDING)**

```
x = [4, 5, 3, 2]
```

```
y = sort(x)
```

```
julia> y
4-element Vector{Int64}:
 2
 3
 4
 5
```

### **SORT (DESCENDING)**

```
x = [4, 5, 3, 2]
```

```
y = sort(x, rev=true)
```

```
julia> y
4-element Vector{Int64}:
 5
 4
 3
 2
```

## SORT!

```
x = [4, 5, 3, 2]
```

```
sort!(x)
```

```
julia> x
4-element Vector{Int64}:
 2
 3
 4
 5
```

Both `sort(x)` and `sort!(x)` allow the sorting order to be dictated by transformations of `x`. Specifically, given a function `foo` and leveraging the keyword argument `by`, the sorted order can be determined by the values of `foo(x)`. We demonstrate this below through the function `sort`.

## SORT - ABSOLUTE

```
x = [4, -5, 3]
```

```
y = sort(x, by = abs) # 'abs' computes the absolute value
```

```
julia> abs.(x)
3-element Vector{Int64}:
 4
 5
 3

julia> y
3-element Vector{Int64}:
 3
 4
-5
```

## SORT - QUADRATIC

```
x = [4, -5, 3]
```

```
foo(a) = a^2
y = sort(x, by = foo) # same as sort(x, by = x -> x^2)
```

```
julia> foo.(x)
3-element Vector{Int64}:
16
25
 9

julia> y
3-element Vector{Int64}:
 3
 4
-5
```

## **SORT - NEGATIVE**

```
x = [4, -5, 3]
```

```
foo(a) = -a
```

```
y = sort(x, by = foo)      # same as sort(x, by = x -> -x)
```

```
julia> foo.(x)
```

```
3-element Vector{Int64}:
```

```
-4
```

```
5
```

```
-3
```

```
julia> y
```

```
3-element Vector{Int64}:
```

```
4
```

```
3
```

```
-5
```

## **RETRIEVING INDICES OF SORTED ELEMENTS**

While `sort` returns the ordered *values* of the vectors, you may also be interested in the *indices* of the sorted elements. This functionality is provided by the function `sortperm`, which returns the indices of `x` that would result in `sort(x)`. In other words, `x[sortperm(x)] == sort(x)` is true. <sup>1</sup>

### **EXAMPLE 1**

```
x = [1, 2, 3, 4]
```

```
sort_index = sortperm(x)
```

```
julia> sort_index
```

```
4-element Vector{Int64}:
```

```
1
```

```
2
```

```
3
```

```
4
```

### **EXAMPLE 2**

```
x = [3, 4, 5, 6]
```

```
sort_index = sortperm(x)
```

```
julia> sort_index
```

```
4-element Vector{Int64}:
```

```
1
```

```
2
```

```
3
```

```
4
```

### EXAMPLE 3

```
x = [1, 3, 4, 2]
```

```
sort_index = sortperm(x)
```

```
julia> sort_index
4-element Vector{Int64}:
 1
 4
 2
 3
```

Analyzing the examples, we can see that the elements in the first two examples are already in ascending order. As a result, `sortperm` returns the trivial permutation `[1, 2, 3, 4]`. In contrast, the last example features an unordered vector `x = [1, 3, 4, 2]`. Thus, the resulting vector `[1, 4, 2, 3]` indicates that the smallest element is at index 1, the second smallest is at index 4, the third smallest is at index 2, and the largest at index 3.

Similar to `sort`, `sortperm` also allows retrieving the indices in descending order. This requires setting the `rev` keyword argument to `true`.

### EXAMPLE 1

```
x = [9, 3, 2, 1]
```

```
sort_index = sortperm(x, rev=true)
```

```
julia> sort_index
4-element Vector{Int64}:
 1
 2
 3
 4
```

### EXAMPLE 2

```
x = [9, 5, 3, 1]
```

```
sort_index = sortperm(x, rev=true)
```

```
julia> sort_index
4-element Vector{Int64}:
 1
 2
 3
 4
```

### EXAMPLE 3

```
x = [9, 3, 5, 1]
```

```
sort_index = sortperm(x, rev=true)
```

```
julia> sort_index
```

```
4-element Vector{Int64}:
```

```
1
3
2
4
```

Finally, `sortperm` also supports the keyword argument `by`. This allows users to define a custom transformation, which serves as the sorting criterion for the indices provided.

### SORT - ABSOLUTE

```
x = [4, -5, 3]
```

```
value = sort(x, by = abs)      # 'abs' computes the absolute value
index = sortperm(x, by = abs)
```

```
julia> abs.(x)
```

```
3-element Vector{Int64}:
```

```
4
5
3
```

```
julia> value
```

```
3-element Vector{Int64}:
```

```
3
4
-5
```

```
julia> index
```

```
3-element Vector{Int64}:
```

```
3
1
2
```

## SORT - QUADRATIC

```
x = [4, -5, 3]
```

```
foo(a) = a^2
```

```
value = sort(x, by = foo) # same as sort(x, by = x -> x^2)
```

```
index = sortperm(x, by = foo)
```

```
julia> foo.(x)
```

```
3-element Vector{Int64}:
```

```
16
```

```
25
```

```
9
```

```
julia> value
```

```
3-element Vector{Int64}:
```

```
3
```

```
4
```

```
-5
```

```
julia> index
```

```
3-element Vector{Int64}:
```

```
3
```

```
1
```

```
2
```

## SORT - NEGATIVE

```
x = [4, -5, 3]
```

```
foo(a) = -a
```

```
value = sort(x, by = foo) # same as sort(x, by = x -> -x)
```

```
index = sortperm(x, by = foo)
```

```
julia> foo.(x)
```

```
3-element Vector{Int64}:
```

```
-4
```

```
5
```

```
-3
```

```
julia> value
```

```
3-element Vector{Int64}:
```

```
4
```

```
3
```

```
-5
```

```
julia> index
```

```
3-element Vector{Int64}:
```

```
1
```

```
3
```

```
2
```

## AN EXAMPLE

One common application of `sortperm` is to reorder a variable based on the values of another variable. For example, suppose we want to assess the daily failures of a machine. Focusing on the first three days of the month, the following code snippet ranks these days by their corresponding failure counts.

## DAYS SORTED BY LOWEST NUMBER OF FAILURES

```
days      = ["one", "two", "three"]  
failures = [8, 2, 4]
```

```
index      = sortperm(failures)  
days_by_failures = days[index]
```

*# days sorted by lowest failures*

```
julia> index
```

```
3-element Vector{Int64}:  
 2  
 3  
 1
```

```
julia> days_by_earnings
```

```
3-element Vector{String}:  
 "two"  
 "three"  
 "one"
```

## REMOVING DUPLICATES

The `unique` function eliminates duplicates from a vector, returning a vector containing each element only once. The function comes in two variants, with `unique` providing a new copy, and the in-place version `unique!` directly updating the original vector.

## UNIQUE

```
x = [2, 2, 3, 4]
```

```
y = unique(x)      # returns a new vector
```

```
julia> x
```

```
4-element Vector{Int64}:  
 2  
 2  
 3  
 4
```

```
julia> y
```

```
3-element Vector{Int64}:  
 2  
 3  
 4
```

## UNIQUE!

```
x = [2, 2, 3, 4]
```

```
unique!(x)           # mutates 'x'
```

```
julia> x
3-element Vector{Int64}:
 2
 3
 4
```

The `StatsBase` package also offers a related function called `countmap`. This enumerates the number of times each element shows up in a vector. Formally, it returns a dictionary, where the unique elements serve as keys, and their corresponding values represent the number of occurrences of that element.

As the keys in the dictionary are unsorted by design, you must apply the `sort` function to the result if you prefer sorted keys. Note that the application of `sort` will automatically transform an ordinary dictionary into an object with type `OrderedDict`.

## UNSORTED COUNT

```
using StatsBase
x = [6, 6, 0, 5]

y = countmap(x)           # Dict with 'element => occurrences'

elements = collect(keys(y))
occurrences = collect(values(y))
```

```
julia> y
Dict{Int64, Int64} with 3 entries:
 0 => 1
 5 => 1
 6 => 2
```

```
julia> elements
3-element Vector{Int64}:
 0
 5
 6
```

```
julia> occurrences
3-element Vector{Int64}:
 1
 1
 2
```



## SORTED COUNT

```
using StatsBase
x          = [6, 6, 0, 5]

y          = sort(countmap(x))      # OrderedDict with `element => occurrences`

elements   = collect(keys(y))
occurrences = collect(values(y))
```

```
julia> y
OrderedCollections.OrderedDict{Int64, Int64} with 3 entries:
 0 => 1
 5 => 1
 6 => 2

julia> elements
3-element Vector{Int64}:
 0
 5
 6

julia> occurrences
3-element Vector{Int64}:
 1
 1
 2
```

## ROUNDING NUMBERS

Julia provides standard functions to approximate numerical values to a specific precision:

- `round` approximates the number to its nearest integer.
- `floor` approximates the number down to its nearest integer.
- `ceil` approximates the number up to its nearest integer.

Below, we show that these functions are quite flexible. In particular, they allow the user to specify the output's type (e.g., `Int64` or `Float64`), the number of decimals to be included through the keyword argument `digits`, and the significant digits.

## ROUND

```
x = 456.175

round(x)                # 456.0

round(x, digits=1)      # 456.2
round(x, digits=2)      # 456.18

round{Int}(x)           # 456

round(x, sigdigits=1)   # 500.0
round(x, sigdigits=2)   # 460.0
```

## FLOOR

```
x = 456.175

floor(x)                # 456.0

floor(x, digits=1)      # 456.1
floor(x, digits=2)      # 456.17

floor{Int}(x)           # 456

floor(x, sigdigits=1)   # 400.0
floor(x, sigdigits=2)   # 450.0
```

## CEIL

```
x = 456.175

ceil(x)                 # 457.0

ceil(x, digits=1)       # 456.2
ceil(x, digits=2)       # 456.18

ceil{Int}(x)            # 457

ceil(x, sigdigits=1)    # 500.0
ceil(x, sigdigits=2)    # 460.0
```

## RANKINGS

Instead of sorting a vector, you may be interested in determining the rank position of each element. The `StatsBase` package offers two functions for this purpose, `competerank` and `ordinalrank`. The main difference between them lies in how they handle identical elements: `competerank` assigns the same rank to identical elements, while `ordinalrank` assigns different ranks to these elements. Both functions return a rank such that 1 corresponds to the lowest value. If you prefer to invert the ranking, so that the highest value corresponds to a rank of 1, you can add the keyword argument `rev = true`.

### RANK (SAME RANK FOR TIES)

```
using StatsBase
x = [6, 6, 0, 5]

y = competerank(x)
```

```
julia> y
4-element Vector{Int64}:
 3
 3
 1
 2
```

### RANK (SAME RANK FOR TIES)

```
using StatsBase
x = [6, 6, 0, 5]

y = competerank(x, rev=true)
```

```
julia> y
4-element Vector{Int64}:
 1
 1
 4
 3
```

### RANK (UNIQUE POSITIONS)

```
using StatsBase
x = [6, 6, 0, 5]

y = ordinalrank(x)
```

```
julia> y
4-element Vector{Int64}:
 3
 4
 1
 2
```

### RANK (UNIQUE POSITIONS)

```
using StatsBase
x = [6, 6, 0, 5]

y = ordinalrank(x, rev=true)
```

```
julia> y
4-element Vector{Int64}:
 1
 2
 4
 3
```

**Do not confuse** `ordinalrank` **and** `sortperm`

The function `ordinalrank` indicates the position of each value in the *sorted* vector, while `sortperm` indicates the position of each value in the *unsorted* vector.

### 'ORDINALRANK'

```
using StatsBase  
x = [3, 1, 2]  
  
y = ordinalrank(x)
```

```
julia> y  
3-element Vector{Int64}:  
 3  
 1  
 2
```

### 'SORTPERM'

```
using StatsBase  
x = [3, 1, 2]  
  
y = sortperm(x)
```

```
julia> y  
3-element Vector{Int64}:  
 2  
 3  
 1
```

## EXTREMA (MAXIMUM AND MINIMUM)

We conclude by identifying extrema in a vector, along with their corresponding indices. The following examples illustrate the functionality for the maximum, with analogous functions available for the minimum.

### VALUE OF MAXIMUM

```
x = [6, 6, 0, 5]  
  
y = maximum(x)
```

```
julia> y  
6
```

### INDEX OF MAXIMUM

```
x = [6, 6, 0, 5]  
  
y = argmax(x)
```

```
julia> y  
1
```