# 6d. Useful Functions for Vectors

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### **INTRODUCTION**

This section provides an overview of essential functions for manipulating vectors. We cover in particular common operations like sorting, finding unique elements, counting occurrences, and ranking data. Our ultimate goal is to illustrate the utility of these functions in a practical context, as we'll do in the next section.

### **SORTING VECTORS**

The sort function allows the user to arrange elements in a specific order. Tt sorts elements in ascending order by default, with the possibility of a descending order by setting the keyword argument rev = true.

The function comes in two variants: sort, which returns a new sorted copy, and sort!, the in-place version that directly updates the vector.

```
SORT (ASCENDING)

x = [4, 5, 3, 2]

y = sort(x)

julia> y

4-element Vector{Int64}:
2
3
4
5
```

```
SORT (DESCENDING)

x = [4, 5, 3, 2]

y = sort(x, rev=true)

julia> y

4-element Vector{Int64}:
5
4
3
2
```

Both sort(x) and sort(x) have the option of defining the sorting order based on transformations of x. Specifically, given a function foo, the sorted order can be determined by the values of foo(x). We demonstrate this below through the function sort, whose implementation requires the keyword argument  $footnote{by}$ .

```
SORT - ABSOLUTE

x = [4, -5, 3]

y = sort(x, by = abs)  # 'abs' computes the absolute value

julia> [abs.(x)]
3-element Vector{Int64}:
4
5
3
julia> [y]
3-element Vector{Int64}:
3
4
-5
```

## **RETRIEVING INDICES OF SORTED ELEMENTS**

While sort returns the ordered *values* of the vectors, you may also be interested in the *indices* of the sorted elements. This functionality is provided by the function sortperm, which returns the indices of x that would result in sort(x). In other words, x sortperm(x) == sort(x) returns true.

Note that the elements in the first two examples are already in ascending order. As a result, sortperm returns the trivial permutation  $\begin{bmatrix} 1 & 2 & 3 & 4 \end{bmatrix}$ . In contrast, the last example features an unordered vector  $\begin{bmatrix} x & = & 1 & 3 & 4 & 2 \end{bmatrix}$ . Thus, the resulting vector  $\begin{bmatrix} 1 & 4 & 2 & 3 \end{bmatrix}$  indicates that the smallest element is at index 1, the second smallest is at index 4, the third smallest is at index 2, and the largest at index 3.

Like sort, sortperm also supports retrieving indices in descending order. This requires including the keyword argument rev = true.

Finally, sortperm also accepts the keyword argument by to define a custom transformation.

```
SORT - ABSOLUTE
      = [4, -5, 3]
value = sort(x, by = abs) # 'abs' computes the absolute value
index = sortperm(x, by = abs)
julia> abs.(x)
3-element Vector{Int64}:
5
3
julia> value
3-element Vector{Int64}:
 3
 4
 -5
julia> index
3-element Vector{Int64}:
 3
 1
 2
```

```
SORT - QUADRATIC
      = [4, -5, 3]
foo(a) = a^2
value = sort(x, by = foo) # same as sort(x, by = x -> x^2)
index = sortperm(x, by = foo)
julia> foo.(x)
3-element Vector{Int64}:
 16
 25
  9
julia> | value |
3-element Vector{Int64}:
  4
 -5
julia> index
3-element Vector{Int64}:
 1
 2
```

```
SORT - NEGATIVE
       = [4, -5, 3]
foo(a) = -a
value = sort(x, by = foo) # same as sort(x, by = x \rightarrow -x)
index = sortperm(x, by = foo)
julia> foo.(x)
3-element Vector{Int64}:
 -4
 5
 -3
julia> value
3-element Vector{Int64}:
  4
  3
 -5
julia> index
3-element Vector{Int64}:
 1
 3
 2
```

### **AN EXAMPLE**

One common application of sortperm is to reorder one variable based on the values of another. For example, suppose we want to assess the daily failures of a machine. Focusing on the first three days of the month, the following code snippet ranks these days by their corresponding failure counts.

```
DAYS SORTED BY LOWEST NUMBER OF FAILURES

days = ["one", "two", "three"]
failures = [8, 2, 4]

index = sortperm(failures)
days_by_failures = days[index] # days sorted by lowest failures

julia> index
3-element Vector{Int64}:
2
3
1
julia> days_by_earnings
3-element Vector{String}:
"two"
"three"
"one"
```

### **REMOVING DUPLICATES**

The function <u>unique</u> removes duplicates from a vector, returning a vector that contains each element only once. The function comes in two variants <u>unique</u> provides a new copy, and <u>unique!</u>, the inplace version that directly updates the original vector.

The StatsBase package provides a related function called countmap, which counts the occurrences of each element in a vector. It returns a dictionary where the unique elements act as keys, and their corresponding values represent the number of times each element appears.

Note that the keys in the resulting dictionary are unsorted by default. If you prefer sorted keys, you must apply the sort function to the result. This will automatically transform an ordinary dictionary into an object with type OrderedDict.

```
UNSORTED COUNT
using StatsBase
          = [6, 6, 0, 5]
          = countmap(x)
                                    # Dict with `element => occurrences`
elements = collect(keys(y))
occurrences = collect(values(y))
julia> y
Dict{Int64, Int64} with 3 entries:
 0 => 1
 5 => 1
 6 => 2
julia> elements
3-element Vector{Int64}:
5
julia> | occurrences
3-element Vector{Int64}:
1
 2
```

```
SORTED COUNT
using StatsBase
          = [6, 6, 0, 5]
          = sort(countmap(x)) # OrderedDict with 'element => occurrences'
elements = collect(keys(y))
occurrences = collect(values(y))
julia> |y|
OrderedCollections.OrderedDict{Int64, Int64} with 3 entries:
 0 => 1
 5 => 1
 6 => 2
julia> | elements
3-element Vector{Int64}:
5
julia> occurrences
3-element Vector{Int64}:
1
 1
 2
```

### **ROUNDING NUMBERS**

Julia provides standard functions to approximate numerical values to a specific precision:

- round approximates the number to its nearest integer.
- floor approximates the number down to its nearest integer.
- ceil approximates the number up to its nearest integer.

Below, we show that these functions are quite flexible, allowing users to specify the output's type (e.g., Int64) or Float64), the number of decimals places via the keyword argument digits, and the significant digits.

```
FLOOR

x = 456.175

floor(x)  # 456.0

floor(x, digits=1)  # 456.1

floor(x, digits=2)  # 456.17

floor(Int, x)  # 456

floor(x, sigdigits=1)  # 400.0

floor(x, sigdigits=2)  # 450.0
```

```
CEIL

x = 456.175

ceil(x)  # 457.0

ceil(x, digits=1)  # 456.2
 ceil(x, digits=2)  # 456.18

ceil(Int, x)  # 457

ceil(x, sigdigits=1)  # 500.0
 ceil(x, sigdigits=2)  # 460.0
```

# **RANKINGS**

Instead of sorting a vector, you may be interested in determining the rank position of each element. The <code>StatsBase</code> package offers two functions for this purpose: <code>competerank</code> and <code>ordinalrank</code>. The main difference between them lies in how they handle tied elements: <code>competerank</code> assigns the same rank to tied elements, while <code>ordinalrank</code> assigns consecutive ranks. Both functions return ranks where 1 corresponds to the lowest value. The keyword argument <code>rev = true</code> allows you to invert the ranking, so that the highest value corresponds to a rank of 1.

```
RANK (SAME RANK FOR TIES)

using StatsBase
x = [6, 6, 0, 5]

y = competerank(x)

julia> y

4-element Vector{Int64}:
3
3
1
2
```

# DESCENDING RANK (SAME RANK FOR TIES) using StatsBase x = [6, 6, 0, 5] y = competerank(x, rev=true) julia> y 4-element Vector{Int64}: 1 1 4 3

```
RANK (UNIQUE POSITIONS)

using StatsBase
x = [6, 6, 0, 5]

y = ordinalrank(x)

julia> y

4-element Vector{Int64}:
3
4
1
2
```

```
DESCENDING RANK (UNIQUE POSITIONS)

using StatsBase
x = [6, 6, 0, 5]

y = ordinalrank(x, rev=true)

julia> y

4-element Vector{Int64}:

1
2
4
3
```

### Do not confuse ordinalrank and sortperm

The function ordinalrank indicates the position of each value in the sorted vector, while sortperm indicates the position of each value in the unsorted vector.

```
'ORDINALRANK'
using StatsBase
x = [3, 1, 2]
y = ordinalrank(x)

julia> y
3-element Vector{Int64}:
3
1
2

'SORTPERM'
using StatsBase
x = [3, 1, 2]
y = sortperm(x)

julia> y
3-element Vector{Int64}:
```

# **EXTREMA (MAXIMUM AND MINIMUM)**

3

We conclude by presenting a method for finding the indices and values of extrema in collections. The following examples are based on the maximum, with similar functions available for the minimum.

```
VALUE
x = [6, 6, 0, 5]
y = maximum(x)
julia> y
6
```

```
INDEX
x = [6, 6, 0, 5]
y = argmax(x)

julia> y
1
```

```
VALUE AND INDEX

x = [6, 6, 0, 5]

y = findmax(x)

julia> y
  (6, 1)
```

Julia additionally provides the function max and min, which respectively return the maximum and minimum of their *arguments*. These functions will become particularly useful for procedures based on binary operations (e.g., the so-called reductions).

```
'MAX' FUNCTION

x = 3
y = 4

z = max(x,y)

julia> Z
4
```

### **FOOTNOTES**

<sup>&</sup>lt;sup>1.</sup> The name sortperm originates from "sorting permutation". Although the name might seem somewhat opaque, it arises because the operation returns the permutation of indices that would sort the original vector.