Randomney

2 SAT (at nost two literals in a clause)

(x, v x2) n (x, v x3) n (x, v x2) n (x, v x3) n (x, v x,)

TFFT X, X, X, X,

Randomired alg, O(n2).

Start with any truth asst.

pit satisfied, done!

if not satisfied, take any unsatisfied clause

flip a cain, flip a variable

repeat until bored

Lo un satisfiable

assume the formula is satisfiable

Sdupon s - truty asst.

current truth asst. A. It matelies between S and A close news

= # of variables - dow!

measure

assurptions change I variable

(YL)

reduce worst can b random walk analy W

2 A of steps b get b n?

T(i) = expected time to get to n

recurrence T(n)=0 T(0) = 1+ T(1)

 $T(i) = \frac{1}{2}T(i-1) + \frac{1}{2}T(i+1) + 1$

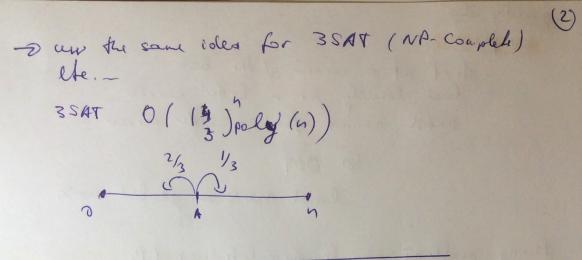
solo T(i) = n2-i2 regardles of start

worst cau. pich an unsatisfied clause to at least one of vary meds to change. maybe both, but in the worst can only on

=) in the worst case, with 1/2 prob. # of matches encreases and with 1/2 prob. It of matches decream

approach: solve propertien, see pallern

```
n=3
                                                   palein
T(0) = T(1) + 1
                                   P= (0) 7
                                                   1(0)= n2
                                   1(1) = 8
T(1) = \frac{1}{2}T(0) + \frac{1}{2}T(2) + 1
                                                   V(1) = n2-1
                                   V(2)=5
                                                   T(2) = ~2 - 4
T(2) = \frac{1}{2}T(1) + \frac{1}{2}.0 + 1
   chech recurrence solution
                                                 T(i)=n2-
     n^{2}-i^{2}=\frac{1}{2}(n^{2}-(i-1)^{2})+\frac{1}{2}(n^{2}-(i+1)^{2})+1
            = n2-12/
Markov's inequality
    non-regalive random quantity X
      X E[X]
   Pr(X > k E(X)) < 1
                                       e.g. h = 2
                                       prob X is 2 Zwice tay
Expected time from i=0
                                         average is < 1
             n 2 fail when solo worth
  Pr (steps to 2 100 n2) 4 100
                                   prob. bound
improve prob. bound (recognize that one solution independence) exists and was not found
 After 2n2 steps
Pr (fail when solution exist) & 1
    restart (alg. con stort any when)
   Pr (foul after new 2 n2 steps, when solution exists) & !
                                     after 100 n2 steps
    Pr (feel after all 242 step trisles) = 2
```



constraints: linear Programming profit 100 € X1: # of product X1, X2, X3 30 600 EX2: # of product 2 X, £ 200 1400 EX3: # of product 3 X2 = 300 X,+x2+X2 = 400 x2 + 3x3 ≤ 600 goal X2 = 300 profit: max 100 x, + 600 x2 + 1400 x3 X3 = 100 350 800 linear program; - linear constrainty X1 = 0 - linear objective function LP's are solvable, provably pely-time algo T not used in practice Simples alg. videly used, but all known "bone" versions are exponential time to algority wally less interesting 100 x, + 600 x2+ 1400 x3 = 4 A plane more powallel veryous to XI max profit to moximum well be at a corner of a box

Simples

- start at a corner of the box

- look locally for a better corner

until council find a better corner

(5 OPT

local max = global max

Many problems can be formulated as (0)

Many problems can be formulated as CPs but CP 05 other not an efficient way to salpe to the often used as bouline and salvability proof

Integer LP: NP-hand would work