Latest Submission Grade 100% To pass 80% or higher

1. Compute the projection matrix that allows us to project any vector $\mathbf{x} \in \mathbb{R}^3$ onto the subspace spanned by the basis vector $\mathbf{b} = \begin{bmatrix} 1 \\ 2 \\ 2 \end{bmatrix}$.

2 / 2 points

Do the exercise using pen and paper. You can use the formula slide that comes with the corresponding lecture.

- $O\left[\frac{1}{9}\right]$
- $\bigcirc
 \begin{bmatrix}
 1 & 2 & 2 \\
 2 & 4 & 4 \\
 2 & 4 & 4
 \end{bmatrix}$
 - ✓ Correct Well done!
- 2. Given the projection matrix

2 / 2 points

$$\frac{1}{25} \begin{bmatrix} 9 & 0 & 12 \\ 0 & 0 & 0 \\ 12 & 0 & 16 \end{bmatrix}$$

project $\begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix}$ onto the corresponding subspace, which is spanned by $\mathbf{b} = \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix}$.

Do the exercise using pen and paper.

- $\bigcirc \begin{array}{c} \boxed{21} \\ \frac{1}{25} \\ 0 \\ 28 \end{array}$
- $\begin{bmatrix}
 21 \\
 0 \\
 28
 \end{bmatrix}$
- $\bigcirc \begin{array}{c} \frac{1}{25} \begin{bmatrix} 5 \\ 10 \\ 10 \end{bmatrix}$
- $\begin{bmatrix}
 3 \\
 0 \\
 4
 \end{bmatrix}$
- **3.** Now, we compute the **reconstruction error**, i.e., the distance between the original data point and its projection onto a lower-dimensional subspace.

1 / 1 point

Assume our original data point is $\begin{bmatrix} 1\\1\\1 \end{bmatrix}$ and its projection $\frac{1}{9}\begin{bmatrix} 5\\10\\10 \end{bmatrix}$. What is the reconstruction error?

0.47

✓ Correct Well done!