1 / 1 point

1 / 1 point

1. The function

 $\beta(\mathbf{x}, \mathbf{y}) = \mathbf{x}^T \begin{bmatrix} 2 & -1 \\ -1 & 1 \end{bmatrix} \mathbf{y}$ 

is

✓ symmetric

**⊘** Correct

Yes:  $eta(\mathbf{x},\mathbf{y}) = eta(\mathbf{y},\mathbf{x})$ 

- not symmetric
- positive definite
- **⊘** Correct

Yes, the matrix has only positive eigenvalues and  $eta(\mathbf{x},\mathbf{x})>0$  for all  $\mathbf{x}\neq\mathbf{0}$  and  $eta(\mathbf{x},\mathbf{x})=0\iff\mathbf{x}=\mathbf{0}$ 

- **✓** bilinear
- **⊘** Correct

## **⊘** Correct

Yes:

- $\beta$  is symmetric. Therefore, we only need to show linearity in one argument.
- For any  $\lambda \in \mathbb{R}$  it holds that  $\beta(\mathbf{x} + \lambda \mathbf{z}, \mathbf{y}) = \beta(\mathbf{x}, \mathbf{y}) + \lambda \beta(\mathbf{z}, \mathbf{y})$ . This holds because of the rules for vector-matrix multiplication and addition.
- not positive definite
- not an inner product
- an inner product
- ✓ Correct

It's symmetric, bilinear and positive definite. Therefore, it is a valid inner product.

- not bilinear
- 2. The function

[1 1]

$$\beta(\mathbf{x}, \mathbf{y}) = \mathbf{x}^T \begin{bmatrix} 1 & -1 \\ -1 & 1 \end{bmatrix} \mathbf{y}$$

is

- not positive definite
- $\bigcirc$  Correct With  $x=[1,1]^T$  we get  $\beta(\mathbf{x},\mathbf{x})=0$ . Therefore  $\beta$  is not positive definite.
- not an inner product

Correct: Since  $\boldsymbol{\beta}$  is not positive definite, it cannot be an inner product.

- **✓** bilinear
- **⊘** Correct

Correct:

- $\beta$  is symmetric. Therefore, we only need to show linearity in one argument.
- $\beta(\mathbf{x} + \lambda \mathbf{z}, \mathbf{y}) = \beta(\mathbf{x}, \mathbf{y}) + \lambda \beta(\mathbf{z}, \mathbf{y})$ . This holds because of the rules for vector-matrix multiplication and addition.
- ✓ symmetric
- **⊘** Correct

Correct:  $eta(\mathbf{x},\mathbf{y}) = eta(\mathbf{y},\mathbf{x})$ 

	positive definite not bilinear not symmetric an inner product		
i 	The function $\beta(\mathbf{x},\mathbf{y}) = \mathbf{x}^T \begin{bmatrix} 2 & 1 \\ -1 & 1 \end{bmatrix} \mathbf{y}$ is $\square \text{ symmetric}$	1/1 poin	ıt.
	<ul> <li>✓ Correct         <ul> <li>Correct.</li> </ul> </li> <li>not bilinear</li> <li>an inner product</li> <li>✓ not an inner product</li> <li>✓ Correct         <ul> <li>Correct</li> <li>Correct: Symmetry is violated.</li> </ul> </li> </ul>		
	The function $\beta(\mathbf{x},\mathbf{y}) = \mathbf{x}^T \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \mathbf{y}$ is	1/1 point	
	<ul> <li>not positive definite</li> <li>not bilinear</li> <li>symmetric</li> <li>✓ Correct         It is the dot product, which we know already. Therefore, it is symmetric.     </li> <li>an inner product</li> <li>✓ Correct         It is the dot product, which we know already. Therefore, it is also an inner product.     </li> </ul>		
5.	For any two vectors $\mathbf{x}, \mathbf{y} \in \mathbb{R}^2$ write a short piece of code that defines a valid inner product.  1 import numpy as np 2 3 def dot(a, b): 4 """Compute dot product between a and b. 5 Args: 6   a, b: (2,) ndarray as R^2 vectors 7 8 Returns: 9   a number which is the dot product between a, b 10 """ 11 12 dot_product = np.dot(a, b) 13 14 return dot_product 15 16 # Test your code before you submit. 17 a = np.array([1,0]) 18 b = np.array([0,1]) 19 print(dot(a,b))	Run	1/1 point

**⊘** Correct

3.

Good job!