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What statistical analysis should I use?

Statistical analyses using R

Version info: Code for this page was tested in R 2.15.2.

Introduction

This page shows how to perform a number of statistical tests using R. Each section gives a brief description of the aim of the statistical test, when it is used, an example showing the R commands and R output with a brief interpretation of the output. You can see the page [Choosing the Correct Statistical Test](#) for a table that shows an overview of when each test is appropriate to use. In deciding which test is appropriate to use, it is important to consider the type of variables that you have (i.e., whether your variables are categorical, ordinal or interval and whether they are normally distributed), see [What is the difference between categorical, ordinal and interval variables?](#) for more information on this.

Setup

```
hsb2 <- within(read.csv("http://www.ats.ucla.edu/stat/data/hsb2.csv"), {  
  race <- as.factor(race)  
  schtyp <- as.factor(schtyp)  
  prog <- as.factor(prog)  
})  
  
attach(hsb2)
```

One sample t-test

```
t.test(write, mu = 50)  
  
##  
##      One Sample t-test  
##  
## data:  write  
## t = 4.14, df = 199, p-value = 5.121e-05  
## alternative hypothesis: true mean is not equal to 50  
## 95 percent confidence interval:  
##  51.5 54.1  
## sample estimates:  
## mean of x  
##      52.8
```

One sample median test

```
wilcox.test(write, mu = 50)  
  
##  
##      Wilcoxon signed rank test with continuity correction  
##  
## data:  write  
## V = 13177, p-value = 3.702e-05  
## alternative hypothesis: true location is not equal to 50
```

Binomial test

```
prop.test(sum(female), length(female), p = 0.5)

##
##      1-sample proportions test with continuity correction
##
## data:  sum(female) out of length(female), null probability 0.5
## X-squared = 1.45, df = 1, p-value = 0.2293
## alternative hypothesis: true p is not equal to 0.5
## 95 percent confidence interval:
##  0.473 0.615
## sample estimates:
##      p
## 0.545
```

Chi-square goodness of fit

```
chisq.test(table(race), p = c(10, 10, 10, 70)/100)

##
##      Chi-squared test for given probabilities
##
## data:  table(race)
## X-squared = 5.03, df = 3, p-value = 0.1697
```

Two independent samples t-test

```
t.test(write ~ female)

##
##      Welch Two Sample t-test
##
## data:  write by female
## t = -3.66, df = 170, p-value = 0.0003409
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
##  -7.50 -2.24
## sample estimates:
## mean in group 0 mean in group 1
##      50.1      55.0
```

Wilcoxon-Mann-Whitney test

```
wilcox.test(write ~ female)

##
##      Wilcoxon rank sum test with continuity correction
##
## data:  write by female
## W = 3606, p-value = 0.0008749
## alternative hypothesis: true location shift is not equal to 0
```

Chi-square test

```
chisq.test(table(female, schtyp))

##
##      Pearson's Chi-squared test with Yates' continuity correction
##
```

```
## data: table(female, schtyp)
## X-squared = 5e-04, df = 1, p-value = 0.9815
```

Fisher's exact test

```
fisher.test(table(race, schtyp))

##
##      Fisher's Exact Test for Count Data
##
## data: table(race, schtyp)
## p-value = 0.5975
## alternative hypothesis: two.sided
```

One-way ANOVA

```
summary(aov(write ~ prog))

##              Df Sum Sq Mean Sq F value    Pr(>F)
## prog           2    3176     1588    21.3 4.3e-09 ***
## Residuals    197   14703        75
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Kruskal Wallis test

```
kruskal.test(write, prog)

##
##      Kruskal-Wallis rank sum test
##
## data: write and prog
## Kruskal-Wallis chi-squared = 34, df = 2, p-value = 4.047e-08
```

Paired t-test

```
t.test(write, read, paired = TRUE)

##
##      Paired t-test
##
## data: write and read
## t = 0.867, df = 199, p-value = 0.3868
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## -0.694  1.784
## sample estimates:
## mean of the differences
##              0.545
```

Wilcoxon signed rank sum test

```
wilcox.test(write, read, paired = TRUE)

##
##      Wilcoxon signed rank test with continuity correction
##
```

```
## data: write and read
## V = 9261, p-value = 0.3666
## alternative hypothesis: true location shift is not equal to 0
```

McNemar test

```
X <- matrix(c(172, 7, 6, 15), 2, 2)
mcnemar.test(X)

##
##      McNemar's Chi-squared test with continuity correction
##
## data: X
## McNemar's chi-squared = 0, df = 1, p-value = 1
```

One-way repeated measures ANOVA

```
require(car)

## Loading required package: car

## Loading required package: MASS

## Loading required package: nnet

## Loading required package: survival

## Loading required package: splines

require(foreign)

## Loading required package: foreign

kirk <- within(read.dta("http://www.ats.ucla.edu/stat/stata/examples/kirk/rb4.dta"),
{
  s <- as.factor(s)
  a <- as.factor(a)
})

model <- lm(y ~ a + s, data = kirk)
analysis <- Anova(model, idata = kirk, idesign = ~s)
print(analysis)

## Anova Table (Type II tests)
##
## Response: y
##           Sum Sq Df F value  Pr(>F)
## a           49.0  3    11.6 0.00011 ***
## s           31.5  7     3.2 0.01802 *
## Residuals    29.5 21
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Repeated measures logistic regression

```
require(lme4)
```

```
## Loading required package: lme4

## Loading required package: Matrix

## Loading required package: lattice

## Attaching package: 'lme4'

## The following object(s) are masked from 'package:stats':
##
## AIC, BIC

exercise <- within(read.dta("http://www.ats.ucla.edu/stat/stata/whatstat/exercise.dta"),
{
  id <- as.factor(id)
  diet <- as.factor(diet)
})
glmer(highpulse ~ diet + (1 | id), data = exercise, family = binomial)

## Generalized linear mixed model fit by the Laplace approximation
## Formula: highpulse ~ diet + (1 | id)
## Data: exercise
## AIC BIC logLik deviance
## 105 113 -49.7 99.5
## Random effects:
## Groups Name Variance Std.Dev.
## id (Intercept) 3.32 1.82
## Number of obs: 90, groups: id, 30
##
## Fixed effects:
## Estimate Std. Error z value Pr(>|z|)
## (Intercept) -2.004 0.663 -3.02 0.0025 **
## diet2 1.145 0.898 1.27 0.2022
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Correlation of Fixed Effects:
## (Intr)
## diet2 -0.738
```

Factorial ANOVA

```
anova(lm(write ~ female * ses, data = hsb2))

## Analysis of Variance Table
##
## Response: write
## Df Sum Sq Mean Sq F value Pr(>F)
## female 1 1176 1176 14.7 0.00017 ***
## ses 1 1042 1042 13.1 0.00039 ***
## female:ses 1 0 0 0.0 0.98276
## Residuals 196 15660 80
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Friedman test

```
friedman.test(cbind(read, write, math))
```

```
##
##      Friedman rank sum test
##
## data:  cbind(read, write, math)
## Friedman chi-squared = 0.645, df = 2, p-value = 0.7244
```

Ordered logistic regression

Factorial logistic regression

```
summary(glm(female ~ prog * schtyp, data = hsb2, family = binomial))

##
## Call:
## glm(formula = female ~ prog * schtyp, family = binomial, data = hsb2)
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -1.89   -1.25    1.06    1.11    1.20
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)   -0.0513     0.3204  -0.16   0.87
## prog2           0.3246     0.3911   0.83   0.41
## prog3           0.2183     0.4319   0.51   0.61
## schtyp2        1.6607     1.1413   1.46   0.15
## prog2:schtyp2  -1.9340     1.2327  -1.57   0.12
## prog3:schtyp2  -1.8278     1.8402  -0.99   0.32
##
## (Dispersion parameter for binomial family taken to be 1)
##
##      Null deviance: 275.64  on 199  degrees of freedom
## Residual deviance: 272.49  on 194  degrees of freedom
## AIC: 284.5
##
## Number of Fisher Scoring iterations: 3
```

Correlation

```
cor(read, write)

## [1] 0.597

cor.test(read, write)

##
##      Pearson's product-moment correlation
##
## data:  read and write
## t = 10.5, df = 198, p-value < 2.2e-16
## alternative hypothesis: true correlation is not equal to 0
## 95 percent confidence interval:
##  0.499 0.679
## sample estimates:
##      cor
## 0.597
```

Simple linear regression

```
lm(write ~ read)
```

```
##
## Call:
## lm(formula = write ~ read)
##
## Coefficients:
## (Intercept)      read
##      23.959      0.552
```

Non-parametric correlation

```
cor.test(write, read, method = "spearman")
```

```
## Warning: Cannot compute exact p-values with ties
```

```
##
##      Spearman's rank correlation rho
##
## data:  write and read
## S = 510993, p-value < 2.2e-16
## alternative hypothesis: true rho is not equal to 0
## sample estimates:
##      rho
## 0.617
```

Simple logistic regression

```
glm(female ~ read, family = binomial)
```

```
##
## Call:  glm(formula = female ~ read, family = binomial)
##
## Coefficients:
## (Intercept)      read
##      0.7261      -0.0104
##
## Degrees of Freedom: 199 Total (i.e. Null);  198 Residual
## Null Deviance:      276
## Residual Deviance: 275      AIC: 279
```

Multiple regression

```
lm(write ~ female + read + math + science + socst)
```

```
##
## Call:
## lm(formula = write ~ female + read + math + science + socst)
##
## Coefficients:
## (Intercept)      female      read      math      science
##      6.139      5.493      0.125      0.238      0.242
##      socst
##      0.229
```

Analysis of covariance

```
summary(aov(write ~ prog + read))
```

```
##              Df Sum Sq Mean Sq F value    Pr(>F)
## prog           2   3176    1588    28.6 1.2e-11 ***
## read           1   3842    3842    69.3 1.4e-14 ***
## Residuals     196  10861         55
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Multiple logistic regression

```
glm(female ~ read + write, family = binomial)
```

```
##
## Call:  glm(formula = female ~ read + write, family = binomial)
##
## Coefficients:
## (Intercept)          read          write
##      -1.706       -0.071        0.106
##
## Degrees of Freedom: 199 Total (i.e. Null);  197 Residual
## Null Deviance:          276
## Residual Deviance: 248      AIC: 254
```

Discriminant analysis

One-way MANOVA

```
summary(manova(cbind(read, write, math) ~ prog))
```

```
##              Df Pillai approx F num Df den Df    Pr(>F)
## prog           2  0.267      10.1         6    392 2.3e-10 ***
## Residuals     197
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Multivariate multiple regression

```
M1 <- lm(cbind(write, read) ~ female + math + science + socst, data = hsb2)
```

```
require(car)
summary>Anova(M1))
```

```
##
## Type II MANOVA Tests:
##
## Sum of squares and products for error:
##      write read
## write  7259 1091
## read   1091 8700
##
## -----
##
## Term: female
##
## Sum of squares and products for the hypothesis:
##      write  read
## write  1414 -133.5
## read   -133   12.6
##
```



```
## Multivariate Tests: female
##               Df test stat approx F num Df den Df  Pr(>F)
## Pillai        1    0.170    19.9      2    194 1.4e-08 ***
## Wilks         1    0.830    19.9      2    194 1.4e-08 ***
## Hotelling-Lawley 1    0.205    19.9      2    194 1.4e-08 ***
## Roy           1    0.205    19.9      2    194 1.4e-08 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## -----
##
## Term: math
##
## Sum of squares and products for the hypothesis:
##      write read
## write   715  856
## read    856 1026
##
## Multivariate Tests: math
##               Df test stat approx F num Df den Df  Pr(>F)
## Pillai        1    0.16    18.5      2    194 4.6e-08 ***
## Wilks         1    0.84    18.5      2    194 4.6e-08 ***
## Hotelling-Lawley 1    0.19    18.5      2    194 4.6e-08 ***
## Roy           1    0.19    18.5      2    194 4.6e-08 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## -----
##
## Term: science
##
## Sum of squares and products for the hypothesis:
##      write read
## write   858  901
## read    901  947
##
## Multivariate Tests: science
##               Df test stat approx F num Df den Df  Pr(>F)
## Pillai        1    0.166    19.4      2    194 2.1e-08 ***
## Wilks         1    0.834    19.4      2    194 2.1e-08 ***
## Hotelling-Lawley 1    0.200    19.4      2    194 2.1e-08 ***
## Roy           1    0.200    19.4      2    194 2.1e-08 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## -----
##
## Term: socst
##
## Sum of squares and products for the hypothesis:
##      write read
## write  1106 1277
## read   1277 1476
##
## Multivariate Tests: socst
##               Df test stat approx F num Df den Df  Pr(>F)
## Pillai        1    0.221    27.5      2    194 3.1e-11 ***
## Wilks         1    0.779    27.5      2    194 3.1e-11 ***
## Hotelling-Lawley 1    0.283    27.5      2    194 3.1e-11 ***
## Roy           1    0.283    27.5      2    194 3.1e-11 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Canonical correlation

```
require(CCA)
```

```
## Loading required package: CCA

## Loading required package: fda

## Loading required package: zoo

## Attaching package: 'zoo'

## The following object(s) are masked from 'package:base':
##
## as.Date, as.Date.numeric

## Attaching package: 'fda'

## The following object(s) are masked from 'package:graphics':
##
## matplotlib

## Loading required package: fields

## Loading required package: spam

## Spam version 0.29-3 (2013-04-23) is loaded. Type 'help( Spam)' or 'demo(
## spam)' for a short introduction and overview of this package. Help for
## individual functions is also obtained by adding the suffix '.spam' to the
## function name, e.g. 'help( chol.spam)'.

## Attaching package: 'spam'

## The following object(s) are masked from 'package:base':
##
## backsolve, forwardsolve

## Loading required package: maps

cc(cbind(read, write), cbind(math, science))

## $cor
## [1] 0.7728 0.0235
##
## $names
## $names$Xnames
## [1] "read" "write"
##
## $names$Ynames
## [1] "math" "science"
##
## $names$ind.names
## NULL
##
##
## $xcoef
##      [,1] [,2]
## read -0.0633 -0.104
## write -0.0492 0.122
##
## $ycoef
##      [,1] [,2]
```

```
## math      -0.0670  0.120
## science -0.0482 -0.121
##
## $scores
## $scores$xscores
##           [,1]      [,2]
## [1,] -0.2636 -0.58956
## [2,] -1.3042 -0.87790
## [3,]  1.4945 -1.55654
## [4,] -0.2492 -2.18757
## [5,]  0.3690  0.44835
## [6,]  0.5588  0.75972
## [7,] -0.1655  0.99033
## [8,]  1.4869  1.06618
## [9,] -0.8894 -0.60276
## [10,] -0.4113 -0.22384
## [11,] -0.1579 -1.63238
## [12,] -0.9038  0.99525
## [13,] -1.6698 -1.27495
## [14,] -0.6155  1.06280
## [15,]  0.2493  1.26547
## [16,]  0.8331  0.60158
## [17,]  0.3690  0.44835
## [18,] -0.5098  0.01998
## [19,] -1.5997 -0.14645
## [20,]  0.5032 -1.96679
## [21,] -0.4954 -1.57803
## [22,] -1.1849  0.12869
## [23,]  0.7702 -1.32593
## [24,] -0.4534 -0.90093
## [25,]  1.3956  0.51099
## [26,]  1.9302 -0.03100
## [27,] -1.4099  0.16492
## [28,]  0.1228  1.05789
## [29,]  1.2483 -0.94700
## [30,]  0.4467 -1.04587
## [31,]  1.7196 -1.59277
## [32,] -1.4656 -2.56159
## [33,] -1.5084  0.40874
## [34,]  1.2271 -0.37369
## [35,] -0.2920  0.78275
## [36,] -1.0936  0.68388
## [37,] -1.0580 -1.48744
## [38,] -1.2622 -0.20080
## [39,]  1.4033 -2.11173
## [40,]  1.9093 -1.28140
## [41,]  0.6153 -0.16119
## [42,] -0.4818  0.47138
## [43,] -0.0458  0.17321
## [44,]  1.2271 -0.37369
## [45,] -1.4099  0.16492
## [46,] -0.4818  0.47138
## [47,]  0.7702 -1.32593
## [48,] -1.1144 -0.56653
## [49,]  0.0243  1.30171
## [50,] -0.3621 -0.34574
## [51,] -0.4538  0.92278
## [52,]  1.8108 -1.03759
## [53,]  0.9528 -0.21555
## [54,] -0.9879 -0.35895
## [55,] -1.7683 -1.03113
## [56,]  1.5154 -0.30614
## [57,]  1.7404 -0.34237
## [58,]  1.3256 -0.61751
## [59,] -0.8894 -0.60276
## [60,]  0.4535 -0.02117
## [61,]  0.4747 -0.59448
## [62,] -0.1235  1.66743
## [63,]  0.9528 -0.21555
```

```
## [64,] 2.1272 -0.51863
## [65,] 0.6717 -1.08211
## [66,] 1.1005 -0.58127
## [67,] -0.5519 -0.65712
## [68,] 1.0093 -1.13646
## [69,] -0.1999 -2.30948
## [70,] 1.1150 -2.17928
## [71,] 0.9528 -0.21555
## [72,] -0.5519 -0.65712
## [73,] -2.0145 -0.42159
## [74,] -1.3042 -0.87790
## [75,] 0.2077 -1.23534
## [76,] 0.9600 -1.01455
## [77,] -0.5803 0.71520
## [78,] -1.3042 -0.87790
## [79,] 2.1692 0.15847
## [80,] 0.9108 -0.89265
## [81,] -0.9879 -0.35895
## [82,] 1.2126 1.22432
## [83,] -1.3042 -0.87790
## [84,] -1.2834 0.37250
## [85,] 0.4047 -1.72297
## [86,] -0.6296 0.83710
## [87,] 0.5945 -1.41160
## [88,] 1.3392 1.43190
## [89,] 1.2135 -2.42310
## [90,] 0.0107 -0.74770
## [91,] -0.4398 1.14848
## [92,] -0.4954 -1.57803
## [93,] -1.4520 -0.51218
## [94,] 1.2691 0.30341
## [95,] 0.9528 -0.21555
## [96,] -0.3133 1.35606
## [97,] -1.7895 -0.45782
## [98,] -1.2834 0.37250
## [99,] 1.5854 0.82236
## [100,] -1.1849 0.12869
## [101,] -1.3535 -0.75599
## [102,] 0.0243 1.30171
## [103,] 0.6645 -0.28310
## [104,] -0.6432 -1.21231
## [105,] -0.2920 0.78275
## [106,] -0.2356 -0.13816
## [107,] -0.9459 0.31815
## [108,] 1.9654 -0.37861
## [109,] 0.2705 0.69216
## [110,] -1.7895 -0.45782
## [111,] -0.2636 -0.58956
## [112,] 0.6573 0.51590
## [113,] -1.1144 -0.56653
## [114,] -1.5997 -0.14645
## [115,] -1.7190 -1.15304
## [116,] 1.4589 0.61478
## [117,] 0.5236 1.10733
## [118,] -2.0145 -0.42159
## [119,] -0.1935 0.53893
## [120,] 0.9948 0.46155
## [121,] -0.5519 -0.65712
## [122,] 0.1792 0.13697
## [123,] 0.1792 0.13697
## [124,] 0.6645 -0.28310
## [125,] -0.1235 1.66743
## [126,] -0.3833 0.22756
## [127,] 0.7210 -1.20402
## [128,] 0.8259 1.40058
## [129,] 0.3270 -0.22875
## [130,] 2.0287 -0.27481
## [131,] -0.6083 0.26380
## [132,] -0.9038 0.99525
```

```
## [133,] -1.4520 -0.51218
## [134,]  0.5868  1.21112
## [135,] -0.8614 -0.15137
## [136,] -2.0073 -1.22059
## [137,]  0.0243  1.30171
## [138,]  0.4323  0.55214
## [139,]  1.4169 -0.06232
## [140,]  0.2005 -0.43633
## [141,]  1.8665  1.68892
## [142,]  0.5868  1.21112
## [143,]  0.8615 -0.77074
## [144,]  0.1228  1.05789
## [145,] -0.2920  0.78275
## [146,]  0.3690  0.44835
## [147,] -0.3133  1.35606
## [148,]  0.5588  0.75972
## [149,]  0.9108 -0.89265
## [150,]  0.3478  1.02165
## [151,]  1.1078 -1.38028
## [152,] -0.8682 -1.17607
## [153,]  0.3758  1.47305
## [154,]  0.2705  0.69216
## [155,] -0.7561  0.62952
## [156,] -1.3042 -0.87790
## [157,] -0.0950  0.29512
## [158,]  0.4391  1.57684
## [159,]  1.3256 -0.61751
## [160,] -1.5717  0.30495
## [161,] -0.1235  1.66743
## [162,] -0.1651 -0.83338
## [163,] -0.0742  1.54552
## [164,] -0.7561  0.62952
## [165,] -0.2920  0.78275
## [166,]  0.9528 -0.21555
## [167,] -0.1655  0.99033
## [168,]  0.7766  1.52249
## [169,] -0.7561  0.62952
## [170,] -0.6576  0.38571
## [171,]  0.4391  1.57684
## [172,]  0.6645 -0.28310
## [173,]  1.4733 -0.98323
## [174,] -0.7981 -0.04757
## [175,]  0.7066  0.39399
## [176,] -1.0371 -0.23704
## [177,] -1.5084  0.40874
## [178,]  0.7766  1.52249
## [179,]  0.1792  0.13697
## [180,] -0.5875  1.51420
## [181,] -0.9459  0.31815
## [182,]  0.7066  0.39399
## [183,] -0.6860  1.75802
## [184,] -0.7773  1.20283
## [185,] -0.5595  1.96560
## [186,] -1.4099  0.16492
## [187,] -0.0458  0.17321
## [188,]  0.7630 -0.52692
## [189,] -1.1356  0.00678
## [190,]  0.4747 -0.59448
## [191,]  0.5868  1.21112
## [192,]  0.8187  2.19959
## [193,]  0.1792  0.13697
## [194,]  0.4038  1.92445
## [195,] -0.2712  2.03316
## [196,] -0.4818  0.47138
## [197,]  0.9808  0.23585
## [198,]  0.2782 -1.93055
## [199,] -0.6296  0.83710
## [200,] -1.2834  0.37250
##
```

```
## $scores$scores
##      [,1]      [,2]
## [1,]  1.01398 -0.8128
## [2,] -0.56166 -1.3052
## [3,] -0.38744 -0.5807
## [4,]  0.32264 -0.8172
## [5,] -0.34719  0.3842
## [6,] -0.42770 -1.5455
## [7,]  0.65755 -1.4179
## [8,]  1.13197  0.6349
## [9,] -0.38744 -0.5807
## [10,] 0.13245  0.1461
## [11,] 0.05471 -0.3367
## [12,] -0.42770 -1.5455
## [13,] -1.67087  1.0991
## [14,] -0.44367  0.1424
## [15,]  1.18299  2.2027
## [16,]  0.73529 -0.9351
## [17,]  0.19943  0.0260
## [18,] -0.78934  0.1402
## [19,] -0.77858  0.7431
## [20,] -0.34719  0.3842
## [21,]  0.49930 -3.8305
## [22,] -2.46945  0.2499
## [23,]  0.36012 -1.2993
## [24,] -0.73311 -0.5829
## [25,]  1.13197  0.6349
## [26,]  1.06499  0.7550
## [27,] -1.33596  0.4984
## [28,] -0.58839 -0.2202
## [29,]  0.86404  1.1155
## [30,]  0.09219 -0.8187
## [31,] -0.05774  1.1095
## [32,] -1.34671 -0.1045
## [33,] -1.37621 -0.4665
## [34,] -1.26376 -1.9126
## [35,] -0.26423 -1.4239
## [36,] -0.80009 -0.4627
## [37,] -2.18000  0.9752
## [38,] -1.71112  0.1343
## [39,]  1.34368  0.8774
## [40,]  1.46689  0.0342
## [41,]  1.25518 -0.2083
## [42,] -0.92330  0.3805
## [43,] -0.44367  0.1424
## [44,]  0.73529 -0.9351
## [45,] -0.22675 -1.9059
## [46,] -1.52093 -0.8291
## [47,]  1.05146 -1.2948
## [48,] -1.70037  0.7372
## [49,] -0.74908  1.1051
## [50,] -0.19171  1.3498
## [51,] -0.80808  0.3812
## [52,]  1.21493 -1.1732
## [53,] -0.47040  1.2274
## [54,]  0.09219 -0.8187
## [55,] -2.19076  0.3723
## [56,]  1.82609  2.0863
## [57,]  1.62237  0.9998
## [58,]  0.71378 -2.1410
## [59,] -0.45442 -0.4605
## [60,]  0.42189  0.8715
## [61,]  0.21540 -1.6619
## [62,] -1.38697 -1.0694
## [63,]  1.77507  0.5185
## [64,]  1.54463  0.5170
## [65,]  0.94178  1.5983
## [66,]  0.93624 -1.2956
## [67,] -0.64462  0.5029
```

```
## [68,] 0.85329 0.5125
## [69,] -1.06004 -0.8261
## [70,] 0.62284 0.5110
## [71,] 1.06499 0.7550
## [72,] -0.65537 -0.1001
## [73,] -1.76735 0.8573
## [74,] -1.42722 -2.0343
## [75,] 0.14842 -1.5418
## [76,] 0.97650 -0.3307
## [77,] 0.04672 0.5073
## [78,] -0.76261 -0.9448
## [79,] 1.06499 0.7550
## [80,] 0.38441 1.3535
## [81,] -0.44367 0.1424
## [82,] -0.53216 -0.9433
## [83,] -1.91207 0.4947
## [84,] -0.22675 -1.9059
## [85,] 1.22568 -0.5702
## [86,] -1.29847 0.0163
## [87,] 0.05471 -0.3367
## [88,] 1.38915 -0.4486
## [89,] 1.70809 0.6386
## [90,] -1.00104 -0.1023
## [91,] -0.66059 2.1908
## [92,] -0.43845 -2.1485
## [93,] -1.65490 -0.5888
## [94,] 0.42189 0.8715
## [95,] 0.67907 -0.2120
## [96,] -1.09752 -0.3441
## [97,] -1.97905 0.6148
## [98,] -2.05679 0.1320
## [99,] 1.46689 0.0342
## [100,] -1.53690 0.8588
## [101,] -1.58792 -0.7090
## [102,] -0.90733 -1.3075
## [103,] 1.15349 1.8408
## [104,] -0.00152 0.3864
## [105,] -0.46518 -1.0635
## [106,] -0.41938 2.7952
## [107,] -0.87229 1.9483
## [108,] 0.88800 -1.4164
## [109,] 0.53435 -0.5747
## [110,] -1.39218 1.2215
## [111,] 0.40559 -2.6253
## [112,] 1.39991 0.1543
## [113,] -0.00950 1.2304
## [114,] -0.70361 -0.2210
## [115,] -0.44367 0.1424
## [116,] 1.52311 -0.6889
## [117,] -0.30970 -0.0979
## [118,] -0.92330 0.3805
## [119,] -1.05727 0.6208
## [120,] 1.46689 0.0342
## [121,] 0.26641 -0.0941
## [122,] 0.53435 -0.5747
## [123,] 0.59611 1.5960
## [124,] 0.22893 0.3879
## [125,] 1.37318 1.2393
## [126,] -0.52141 -0.3404
## [127,] 0.89077 0.0305
## [128,] -0.00152 0.3864
## [129,] 0.00924 0.9894
## [130,] 1.88231 1.3632
## [131,] -0.00152 0.3864
## [132,] -1.40017 2.0655
## [133,] -0.13548 0.6267
## [134,] 0.61208 -0.0919
## [135,] 0.62284 0.5110
## [136,] -1.22350 -0.9478
```

```
## [137,] -0.38744 -0.5807
## [138,]  0.22094  1.2319
## [139,]  1.79104 -1.1695
## [140,]  0.62284  0.5110
## [141,]  1.02474 -0.2098
## [142,]  0.26641 -0.0941
## [143,]  0.66310  1.4759
## [144,]  0.68982  0.3909
## [145,] -0.41417  0.5043
## [146,]  0.83177 -0.6934
## [147,]  0.62806 -1.7798
## [148,]  1.02474 -0.2098
## [149,]  1.01675  0.6342
## [150,]  1.44016  1.1192
## [151,]  1.12122  0.0320
## [152,] -0.85632  0.2603
## [153,]  0.93624 -1.2956
## [154,]  0.18868 -0.5769
## [155,] -0.52141 -0.3404
## [156,] -0.71160  0.6230
## [157,]  0.07345 -0.5777
## [158,]  0.34415  0.3887
## [159,]  1.18820 -0.0882
## [160,] -1.40294  0.6185
## [161,] -0.07926 -0.0964
## [162,]  0.21817 -0.2150
## [163,] -0.42770 -1.5455
## [164,] -1.73785  1.2193
## [165,]  0.15918 -0.9389
## [166,]  1.41865 -0.0867
## [167,] -0.46518 -1.0635
## [168,]  1.14795 -1.0530
## [169,] -0.84556  0.8633
## [170,]  0.05471 -0.3367
## [171,]  0.60133 -0.6948
## [172,]  1.14795 -1.0530
## [173,]  1.71885  1.2416
## [174,] -1.06802  0.0178
## [175,]  1.39192  0.9983
## [176,] -0.93129  1.2245
## [177,] -0.84556  0.8633
## [178,] -0.14624  0.0238
## [179,]  0.21540 -1.6619
## [180,] -0.69286  0.3820
## [181,]  0.33340 -0.2143
## [182,]  0.93103  0.9953
## [183,] -0.82959 -0.8247
## [184,] -0.06850  0.5066
## [185,] -1.57716 -0.1060
## [186,] -1.05727  0.6208
## [187,] -0.21322  0.1439
## [188,]  1.18820 -0.0882
## [189,] -0.37668  0.0223
## [190,] -0.07926 -0.0964
## [191,]  1.25518 -0.2083
## [192,]  0.80228 -1.0553
## [193,] -0.17574 -0.3381
## [194,]  1.57413  0.8789
## [195,] -0.40341  1.1073
## [196,]  0.51837  1.1132
## [197,]  1.74558  0.1566
## [198,] -0.44367  0.1424
## [199,] -0.65537 -0.1001
## [200,] -0.88305  1.3453
##
## $scores$corr.X.xscores
##      [,1] [,2]
## read -0.927 -0.375
## write -0.854  0.520
```



```
##
## $scores$corr.Y.xscores
##      [,1]      [,2]
## math   -0.718   0.0087
## science -0.675  -0.0114
##
## $scores$corr.X.yscores
##      [,1]      [,2]
## read  -0.717  -0.00879
## write -0.660   0.01222
##
## $scores$corr.Y.yscores
##      [,1]      [,2]
## math   -0.929   0.371
## science -0.873  -0.487
```

Factor analysis

```
require(psych)

## Loading required package: psych

## Attaching package: 'psych'

## The following object(s) are masked from 'package:fields':
##
## describe

## The following object(s) are masked from 'package:car':
##
## logit

fa(r = cor(model.matrix(~read + write + math + science + socst - 1, data = hsb2)),
  rotate = "none", fm = "pa", 5)

## In fa, too many factors requested for this number of variables to use SMC
## for communality estimates, ls are used instead

## Factor Analysis using method = pa
## Call: fa(r = cor(model.matrix(~read + write + math + science + socst -
##      1, data = hsb2)), nfactors = 5, rotate = "none", fm = "pa")
## Standardized loadings (pattern matrix) based upon correlation matrix
##      PA1  PA2  PA3  PA4  PA5 h2      u2
## read   0.86 -0.02 -0.34 -0.01 -0.39 1 -8.9e-16
## write   0.82  0.15  0.51  0.03 -0.17 1  5.6e-16
## math    0.84 -0.19  0.00 -0.47  0.18 1  1.1e-16
## science 0.80 -0.46  0.00  0.35  0.16 1  0.0e+00
## socst   0.78  0.54 -0.17  0.12  0.24 1  3.3e-16
##
##
##      PA1  PA2  PA3  PA4  PA5
## SS loadings      3.38 0.56 0.41 0.36 0.30
## Proportion Var    0.68 0.11 0.08 0.07 0.06
## Cumulative Var    0.68 0.79 0.87 0.94 1.00
## Proportion Explained 0.68 0.11 0.08 0.07 0.06
## Cumulative Proportion 0.68 0.79 0.87 0.94 1.00
##
## Test of the hypothesis that 5 factors are sufficient.
##
## The degrees of freedom for the null model are 10 and the objective function was 2.51
## The degrees of freedom for the model are -5 and the objective function was 0
##
## The root mean square of the residuals (RMSR) is 0
```

```
## The df corrected root mean square of the residuals is NA
##
## Fit based upon off diagonal values = 1
## Measures of factor score adequacy
##
## Correlation of scores with factors
## Multiple R square of scores with factors
## Minimum correlation of possible factor scores
```

	PA1	PA2	PA3	PA4	PA5
Correlation of scores with factors	1	1	1	1	1
Multiple R square of scores with factors	1	1	1	1	1
Minimum correlation of possible factor scores	1	1	1	1	1

```

princomp(~read + write + math + science + socst, data = hsb2)

## Call:
## princomp(formula = ~read + write + math + science + socst, data = hsb2)
##
## Standard deviations:
## Comp.1 Comp.2 Comp.3 Comp.4 Comp.5
## 18.25  7.68  6.21  5.77  5.43
##
## 5 variables and 200 observations.
```

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