

Model Selection - how to choose model order

60% training set	J_{TRAIN}	training error
20% Cross-Validation set	J_{CV}	Cross-validation error
20% Test Set	J_{TEST}	test error / generalization error

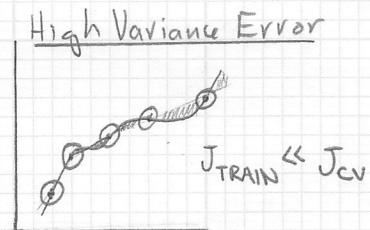
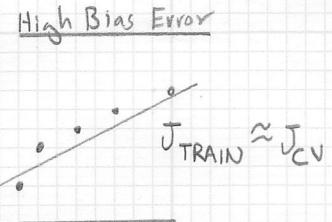
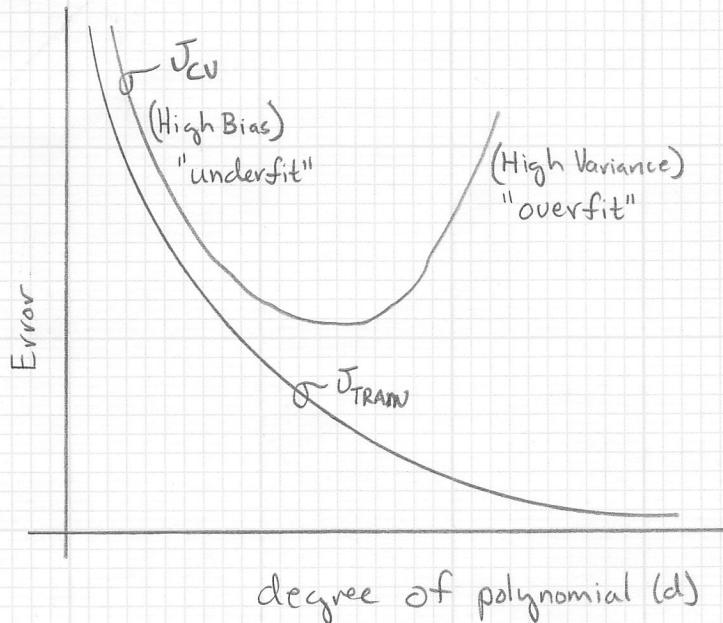
Procedure:

1. Fit several candidate models by minimizing the training error
2. Select candidate that gives the lowest cross-validation error.
3. Estimate generalization error using test set

Notes:

* We should expect $J_{\text{CV}} < J_{\text{TEST}}$ since we have effectively fit a model order parameter to the CV set.

Bias vs. Variance



Bias & Variance - Regularization

* Do not include $\frac{\lambda}{2m} \sum_{j=1}^m \theta_j^2$ in cost functions used for selection purposes. *

$$J_{\text{FIT}}(\theta) = \frac{1}{2} \langle |h_{\theta}(x_{\text{TRAIN}}) - y_{\text{TRAIN}}|^2 \rangle + \frac{1}{2} \lambda (\langle \theta^2 \rangle - \theta_0^2) \quad \text{use to fit params}$$

$$\left. \begin{array}{l} J_{\text{TRAIN}} = \frac{1}{2} \langle |h_{\theta}(x_{\text{TRAIN}}) - y_{\text{TRAIN}}|^2 \rangle \\ J_{\text{CV}} = \frac{1}{2} \langle |h_{\theta}(x_{\text{CV}}) - y_{\text{CV}}|^2 \rangle \\ J_{\text{TEST}} = \frac{1}{2} \langle |h_{\theta}(x_{\text{TEST}}) - y_{\text{TEST}}|^2 \rangle \end{array} \right\} \text{use for model selection}$$

Methods for choosing λ :

- Brute force :

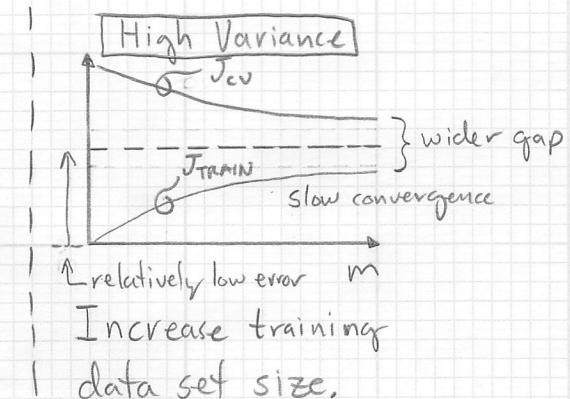
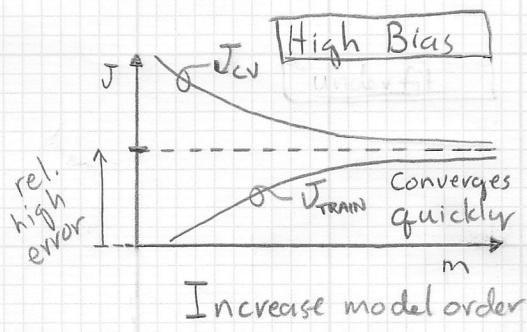
$$\left. \begin{array}{l} \lambda_0 = 0 \\ \lambda_1 \\ \lambda_2 \\ \vdots \\ \lambda_n = \end{array} \right\} \text{run each, choose best } J_{\text{CV}}, \text{ report } J_{\text{TEST}}$$

- Bisection search, terminating when bracket distance falls below some threshold.
- Newton-Raphson?

Learning Curves

J_{TRAIN} vs. m

J_{CV} vs. m



Debugging:

High Bias:

- more features
- more polynomial features
- decrease λ

High Variance:

- less features
- more training examples
- increase λ