

2020-11/20 GENE CHUNG

#1 $10 \times 8 * m \times n = 8 \times 8$

$\therefore m \times n = 3 \times 1$

$$\rightarrow \begin{matrix} 0 \\ 0 \\ 0 \end{matrix} * \begin{matrix} a \\ b \\ c \end{matrix} = 0 \quad \begin{matrix} 0 \\ 0 \\ 1 \end{matrix} * \begin{matrix} a \\ b \\ c \end{matrix} = -1$$

$$\begin{matrix} 0 \\ 1 \\ 1 \end{matrix} * \begin{matrix} a \\ b \\ c \end{matrix} = 1 \quad \begin{matrix} 1 \\ 1 \\ 1 \end{matrix} * \begin{matrix} a \\ b \\ c \end{matrix} = 0$$

$$\rightarrow \underline{c=-1} \quad \underline{b=2} \quad \underline{a=-1}$$

$$\therefore ? = \begin{bmatrix} -1 \\ 2 \\ -1 \end{bmatrix}$$

and thrs are similar to Δ^2 operator which's

$$Y_{i+2} - 2Y_{i+1} + Y_i \text{ but having different sign.}$$

Thrs operator detects a point changing rapidly

in column direction (Edge Detection)

#2

2-1. When does the zero-crossing occurs?

The answer will be point where laplacean's sign changes. It is usually when intensity of the image changes rapidly, where? Edges!

So usually Edges correspond to zero-crossings,

2-2. bigger sigma makes gaussian filter bigger which makes more of blur and reduces more zero-crossing points and make less points where $h(x,y)$ becomes zero since large σ detects large scale edges & small σ detects fine features

#3

3-1. $\rho = x \sin \theta + y \cos \theta$ for fixed x, y

$$\rightarrow \rho = x \sin \theta + y \cos \theta = \sqrt{x^2 + y^2} \cos(\alpha \sin \theta + \sin \alpha \cos \theta) \\ (\alpha = \arctan(\frac{y}{x}))$$

$$\therefore \rho = \sqrt{x^2 + y^2} \sin(\alpha + \theta)$$

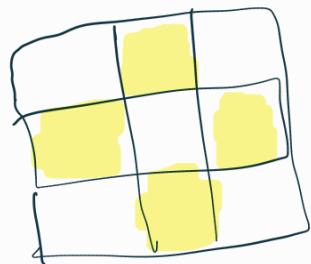
\therefore phase shifted $-\arctan(\frac{y}{x})$ & amplitude

$$\text{be } \sqrt{x^2 + y^2}$$

3-2. period/frequency doesn't varies with the point (x, y) & stay constant as

2π in $\theta \rightarrow \text{axis}$,

#4. Method I used while Implement non maximal Suppression



→ there are total 8 surrounding pixels, we can use only 4 neighboring pixels, but to make more

accurate non-maximal Suppression, I used

all 8 surroundings,

First, I check Gradient

Direction derived by

$\theta = \arctan\left(\frac{S_y}{S_x}\right)$ and selected two neighboring

pixels by such standard below: $-\frac{\pi}{2} < \theta < \frac{\pi}{2}$

$$(\text{i}) -\frac{\pi}{8} < \theta \leq \frac{\pi}{8}$$

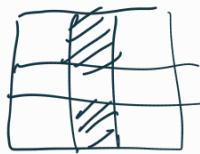


$$(\text{ii}) \frac{\pi}{8} < \theta \leq \frac{3\pi}{8}$$

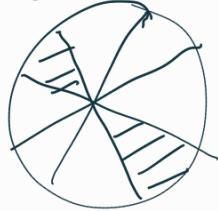
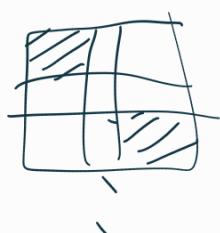


(iii)

$$\frac{3\pi}{8} < \theta \leq \frac{\pi}{2} \text{ or } -\frac{3\pi}{8} > \theta > \frac{\pi}{2}$$



$$(iv) -\frac{3}{8}\pi < \theta < -\frac{\pi}{8}$$



→ Double Thresholding

At weak edge I detected the edge by comparing 4 neighbouring pixels and with high threshold and If all the 4 values were less than high threshold I make the value to 0.

By changing Parameter we could obtain 4 different pictures fig 1.c has lots of noise since I use low sigma 2 So I changed Sigma to 3 and obtained Fig a,b,d → Fig a used

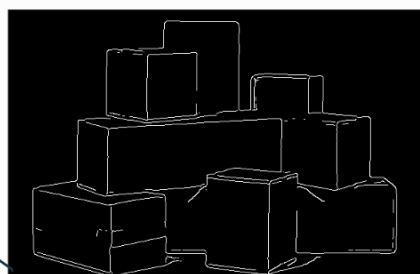


Fig 1.a



Fig 1.b

high threshold 0.14
low threshold 0.04

b used high 0.14
low 0.02

d used high 0.05
low 0.02

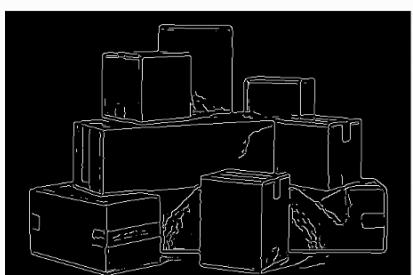


Fig 1.c

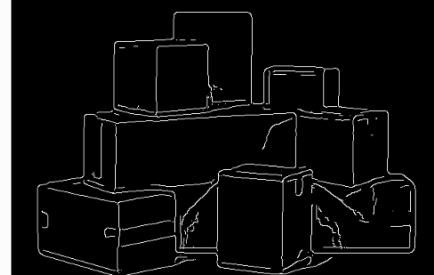


Fig 1.d

There was no dramatic change by low threshold but changing gaussian kernel helped reducing noise.

4.3 Hough transform.



Fig 2.9

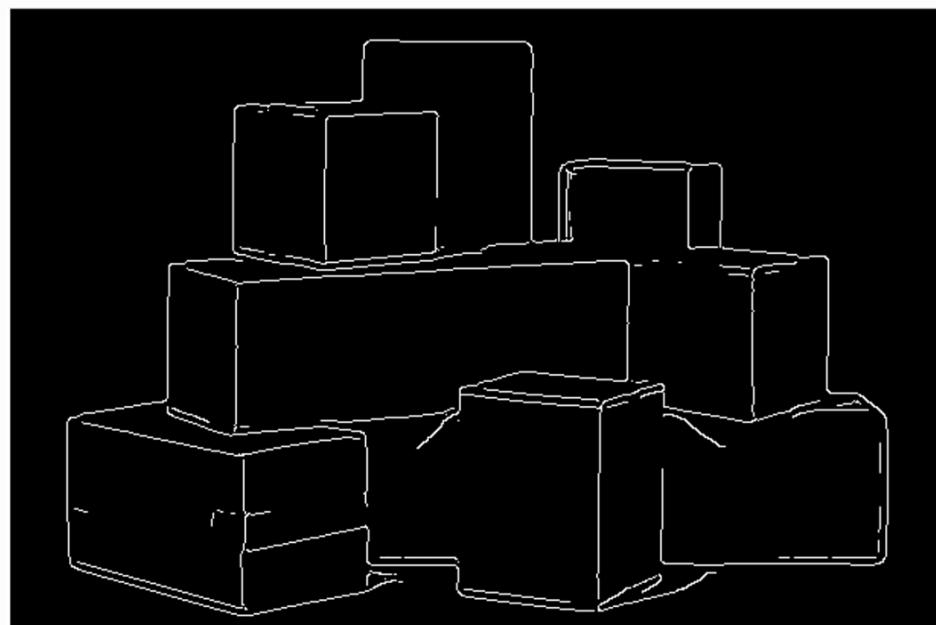


Fig 2.6

Fig 2.9 shows hough transform stored functions in coordinate (ρ, θ) & Fig 2.6 shows the image. I used parameter

$$\text{rhoRes} = 1.8$$

$$\text{thetaRes} = \text{math.pi} / 200$$

& $\text{rhoMaxNum} = 1200$ which indicates maximum # of coordinate "rho",

4. r_p & r_θ are also needed here since returning R_{hb} , Θ_{theta} should be the real ' ρ ' & ' θ ' value, not the int value divided by resolution. So we need each resolution values.

I used all 8 neighbour pixels for

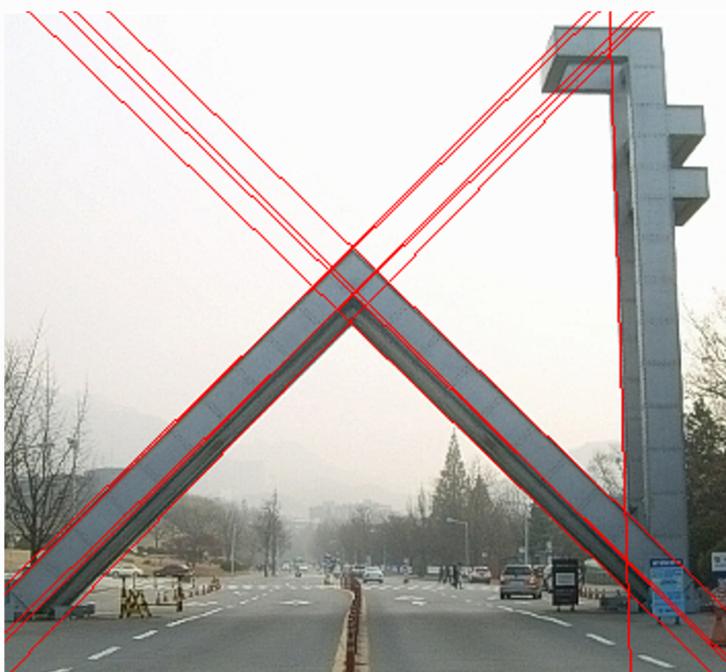


Fig 3. a

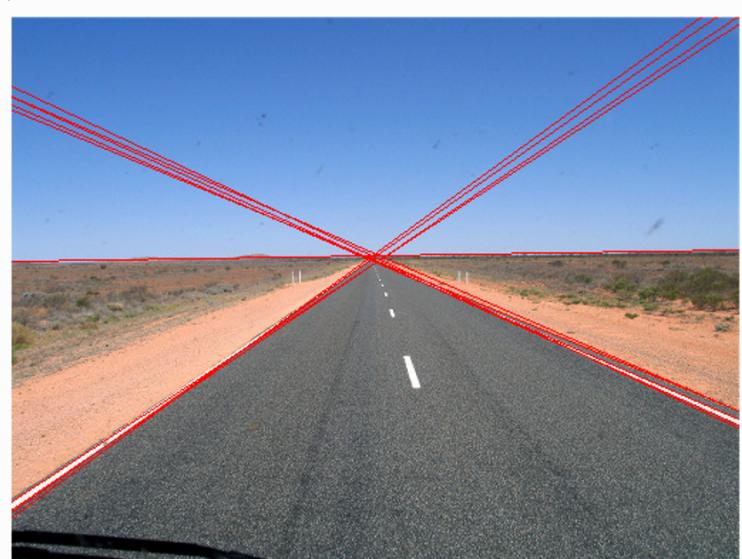


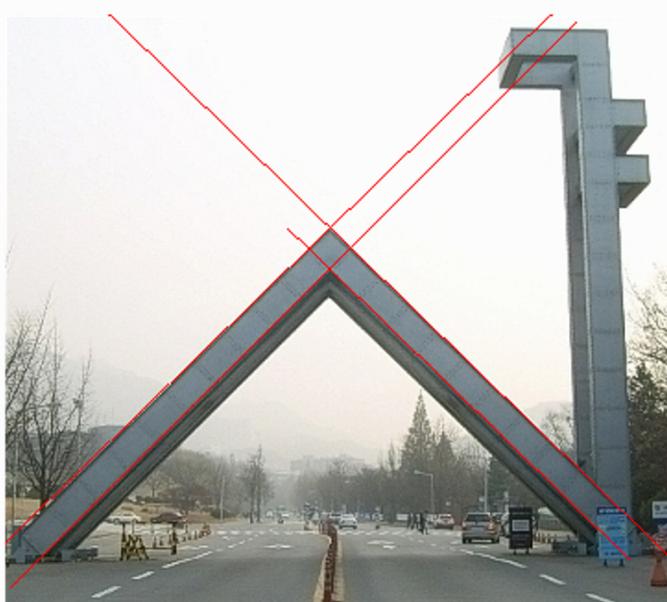
Fig 3. b

Fig 3.a & 3.b is both hough line with

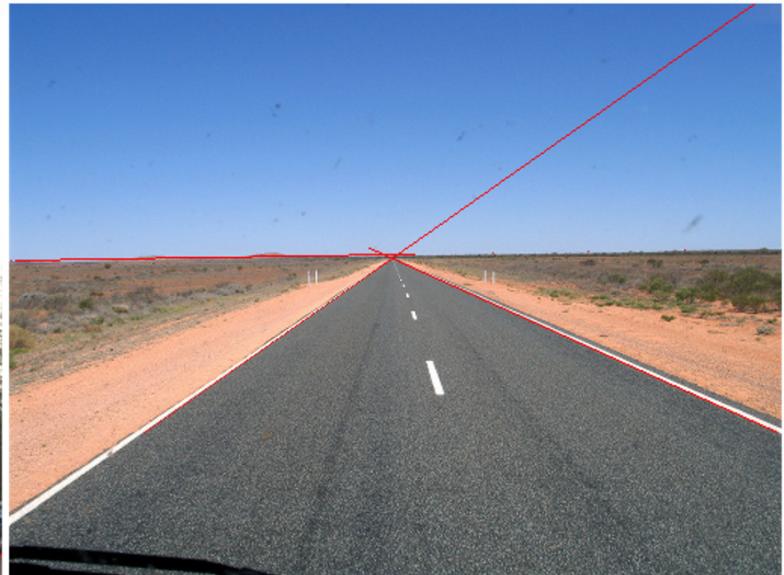
original picture

#5

The main algorithm used to detect the line segments was by detecting the point on the line and see if its out of the edge or It's the edge. I used algorithm of offset and seek of pixels around in boundary of offset has a point $H[i][j] = 1$. Then I used to get segments line.



Frg 4.a



Frg 4.b