

## Lecture 16: October 12

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$A$  = statement on the left is False.  $B$  = statement on the right is True. If  $A$  is true  $\Rightarrow B$  is false  $\Rightarrow A$  is false.

$\{0, 1\}^* = \{\epsilon, 0, 1, 00, 01, \dots\}$  countable

$B = \{0000\dots, 111\dots, 010101\dots\}$

Why not apply diagonalization to  $\{0, 1\}^*$ ?

We need to define  $a_n$ . Each row  $f(n)$  has finite length. If  $f(n)$  has finite length  $\geq n$ , then  $a_n$  is undefined.

$2^{\Sigma^*}$  is uncountably infinite.

There are many TMs

$\Rightarrow$  countably many decidable languages (each decided by some TM)

$\Rightarrow$  countably many recognizable languages (each recognized by some TM)