

Protocol E91

Isabelle Viarouge
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26th of February, 2026

Who are we?

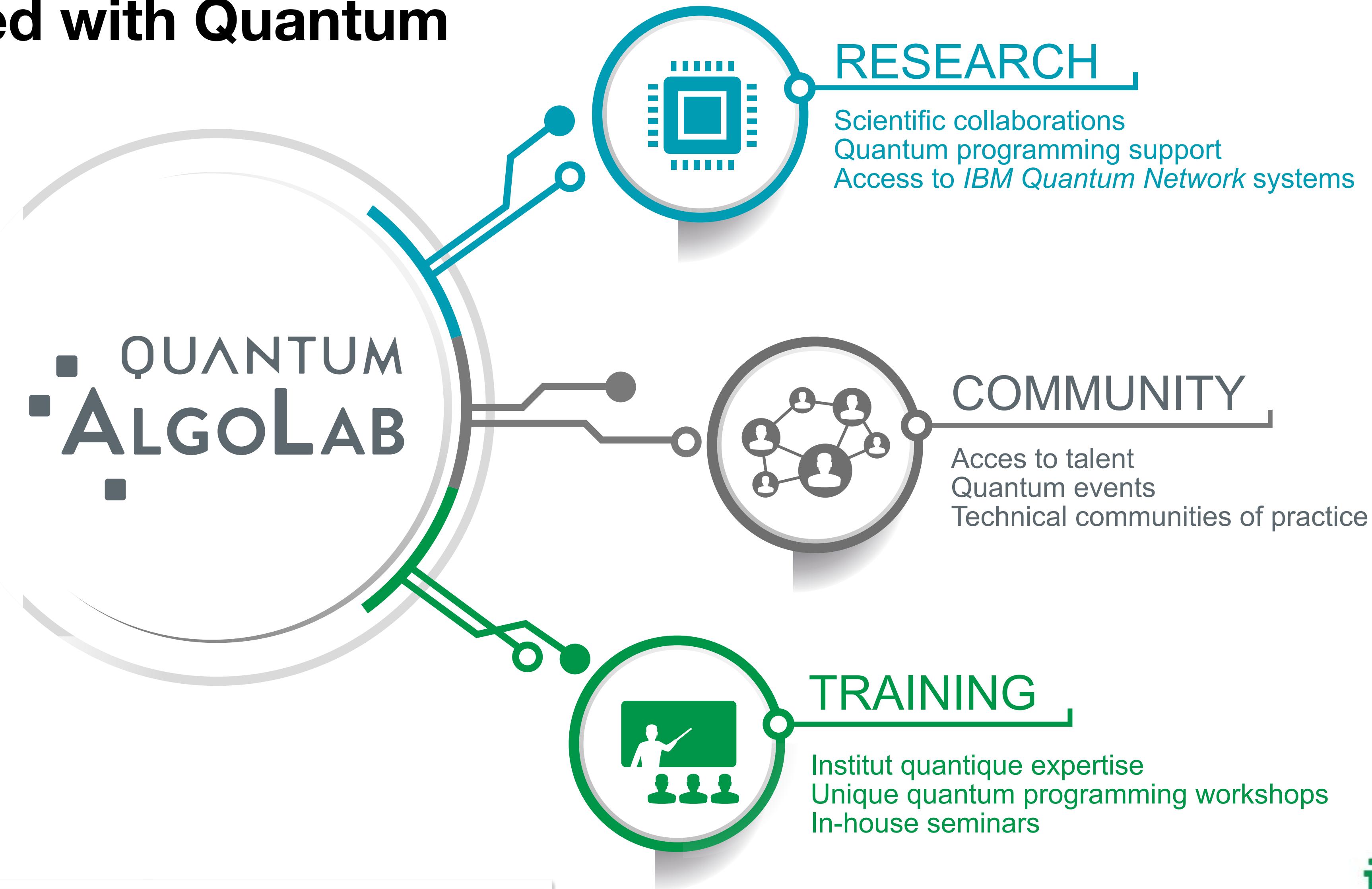
Quantum algorithm laboratory





Quantum AlgoLab

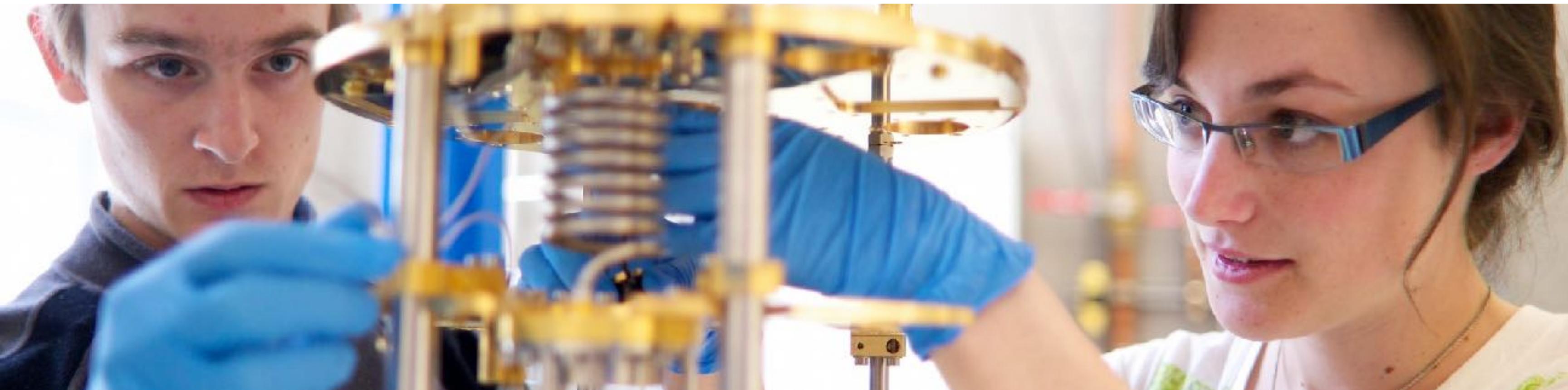
Get started with Quantum



Nous contacter : AlgoLabquantique@usherbrooke.ca

Institut quantique

We place our **250 students and postdocs** at the center of research in an open and collaborative environment to **accelerate** the transition from science to quantum technologies



Our **32 faculty members** come from 4 faculties and 7 departments
\$80M invested in 10 years and a **new building** is now open



Bachelor's degree in Quantum information sciences

Nouvelle cohorte à l'automne 2026

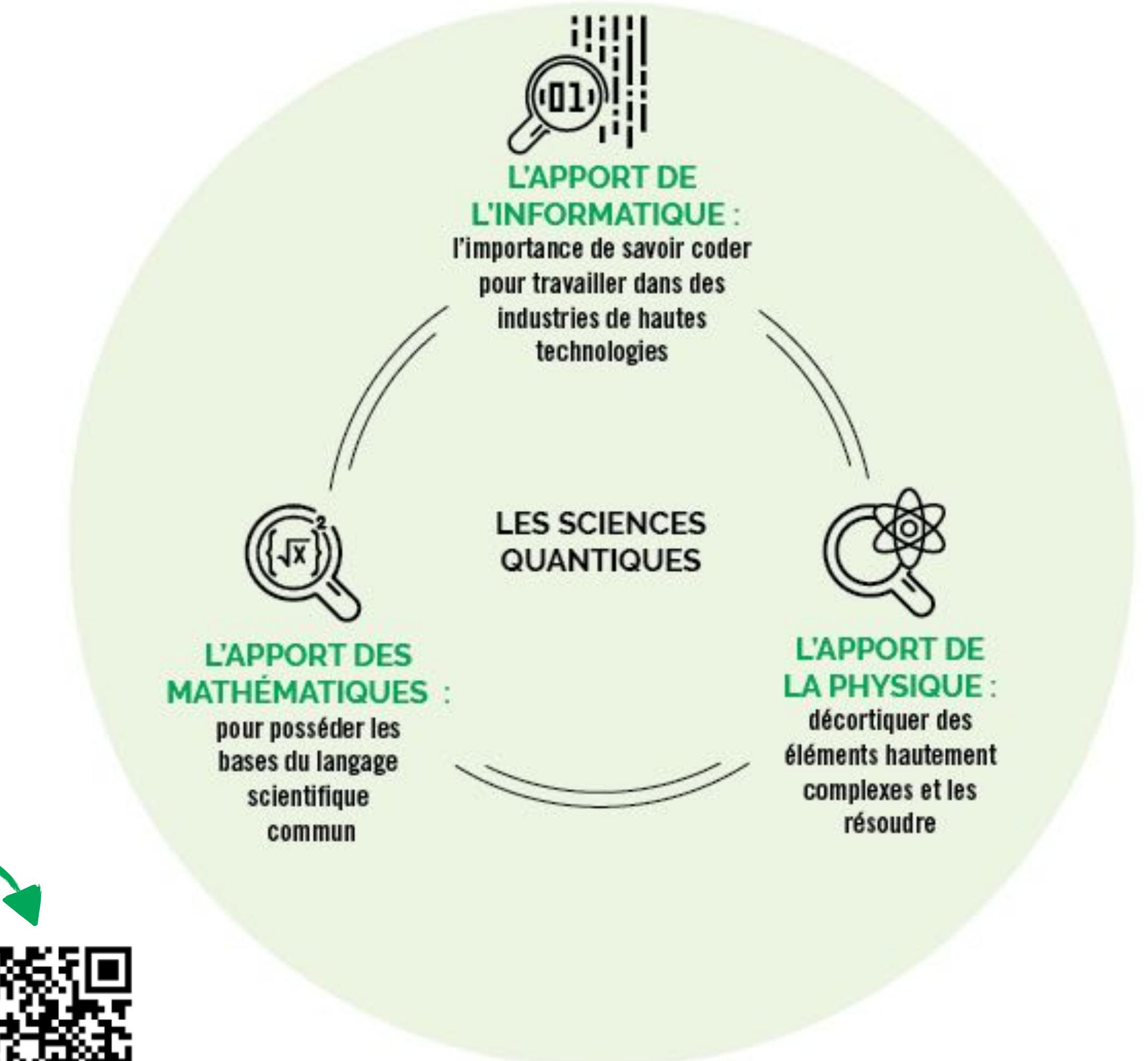
Formation professionnalisante

- Programme interdisciplinaire
- Parcours coop
- Projets intégrateurs

Pour en savoir plus



Université de
Sherbrooke





Institut quantique

Cooperative R&D environment for
Academia and Industry

Quantum tech platforms

Quantum Fab Lab

Quantum computing platform

Plan

- Presentation
- Cryptography
- The qubit
- The photon: messenger of quantum information
- Entanglement and CHSH inequality
- Protocol E91
- Hands-on session

Plan

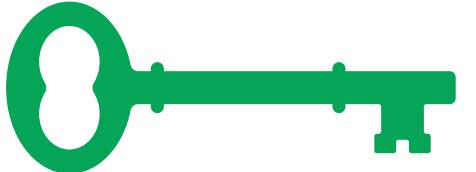
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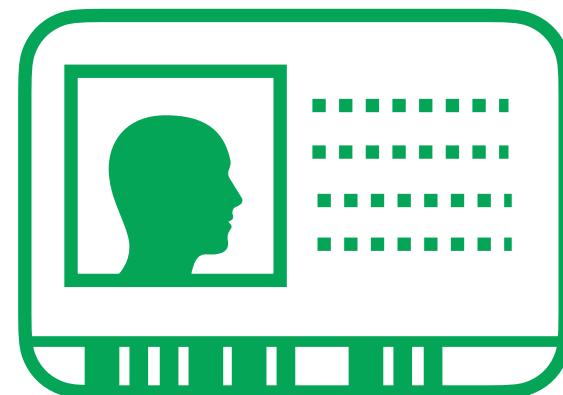
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Cryptography

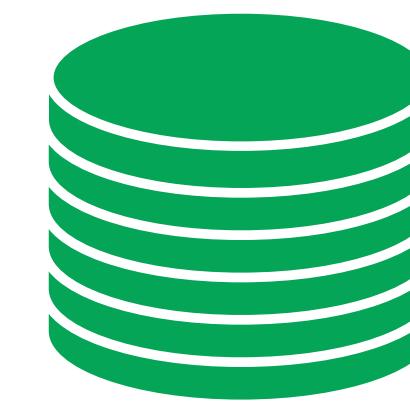
Confidentiality



Authenticity

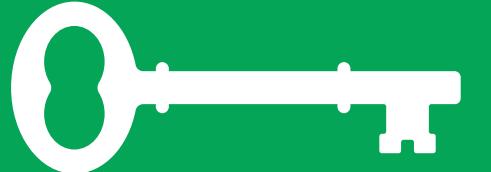


Message integrity

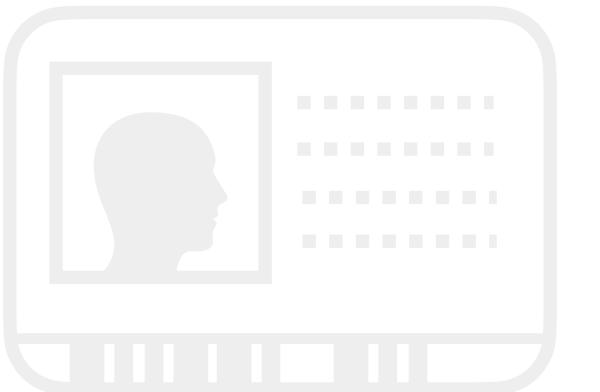


Cryptography

Confidentiality



Authenticity



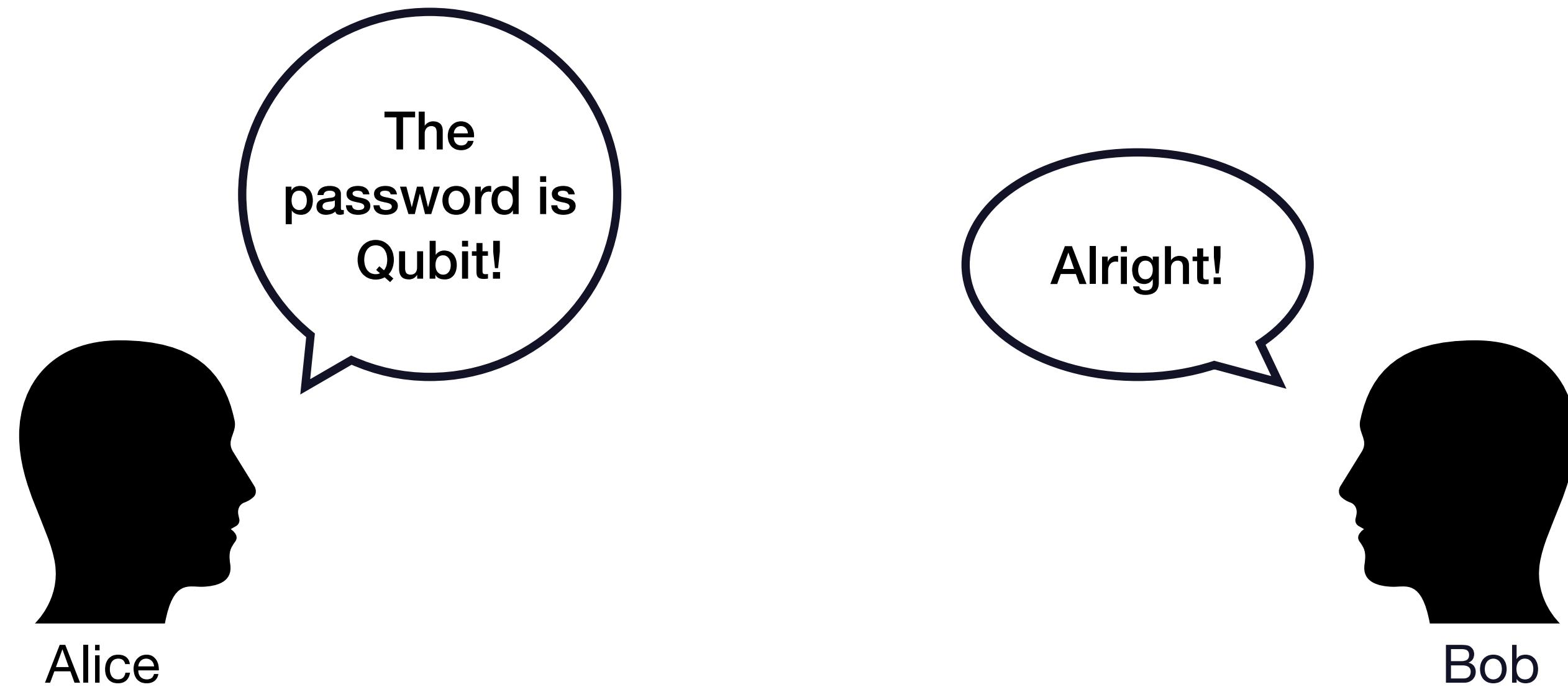
Message integrity



Cryptography

Confidentiality

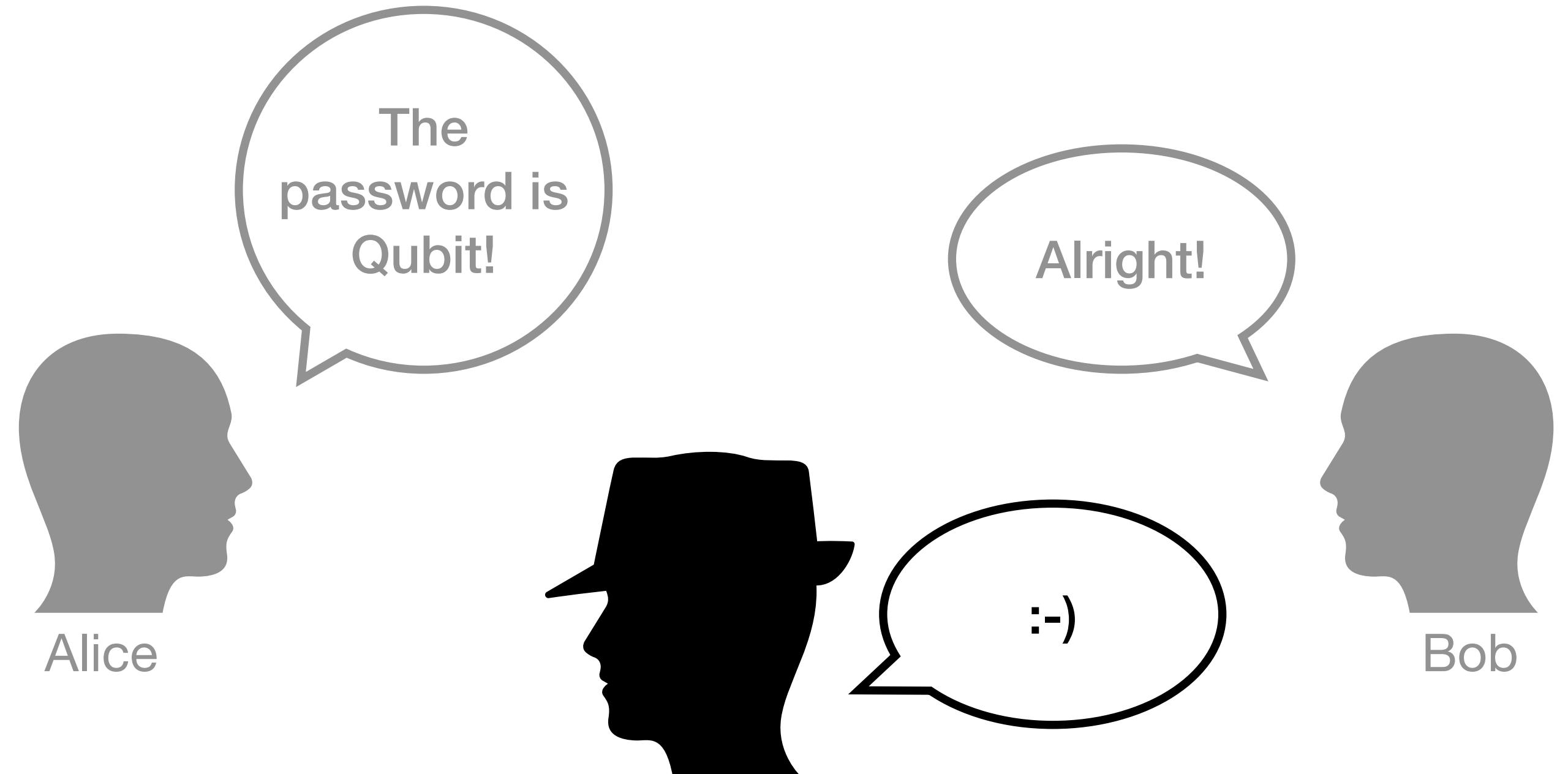
Goal: Ensure that the message is inaccessible to an eavesdropper!



Cryptography

Confidentiality

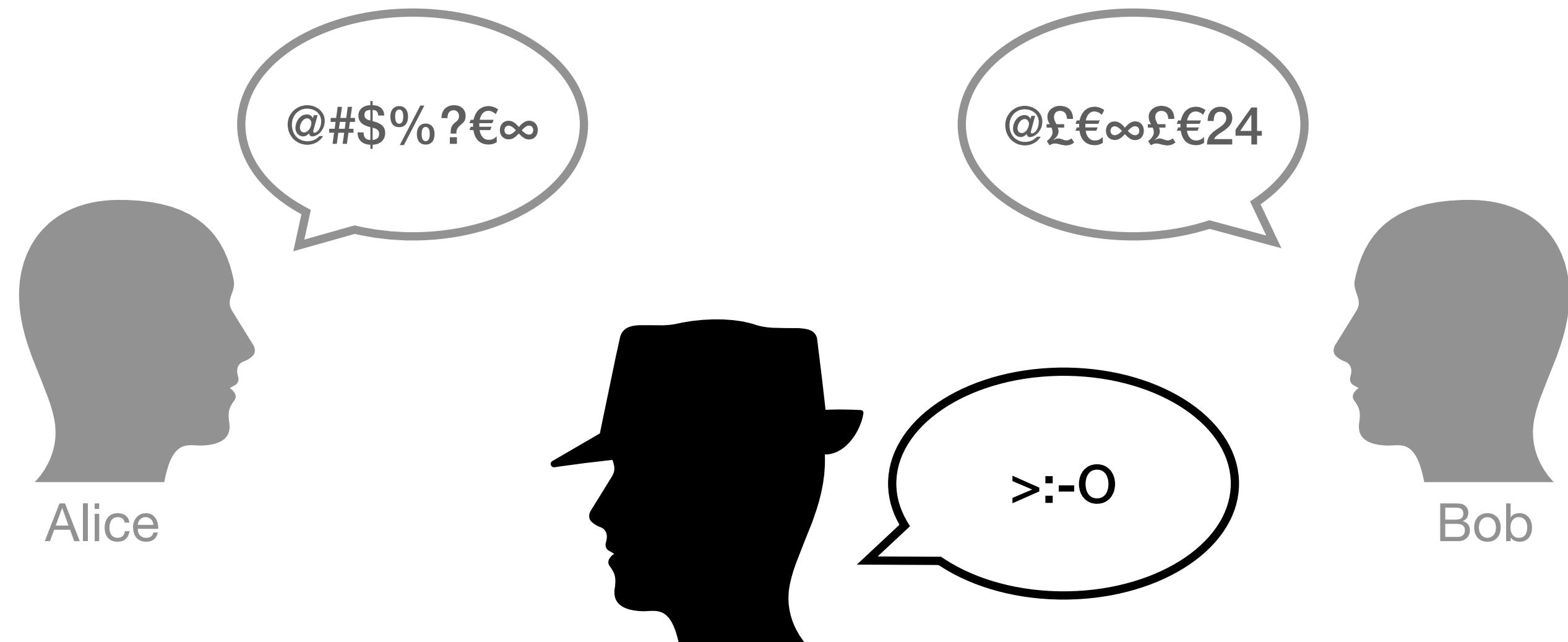
Goal: Ensure that the message is inaccessible to an eavesdropper!



Cryptography

Confidentiality

Goal: Ensure that the message is inaccessible to an eavesdropper!



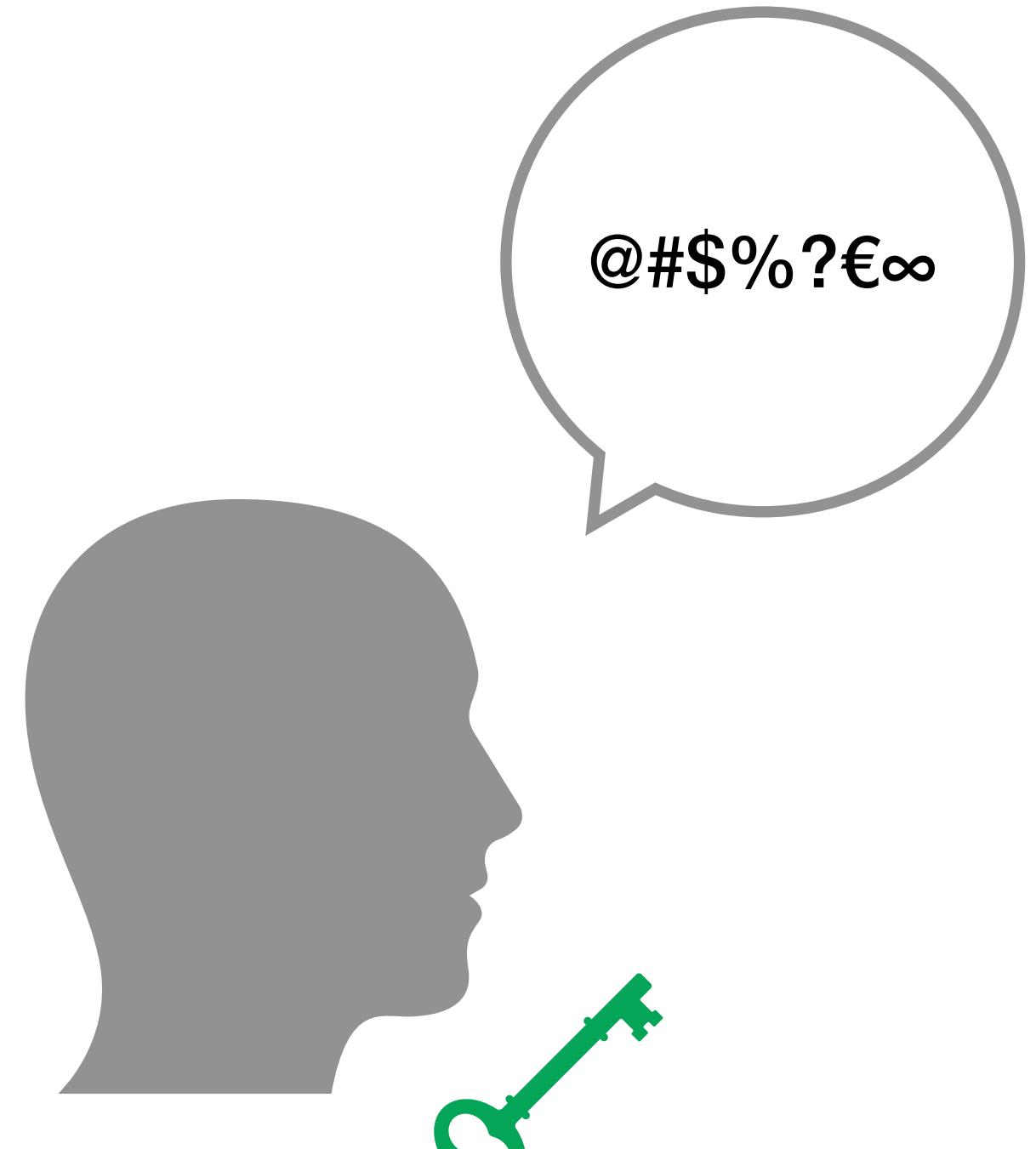
Symmetric Key



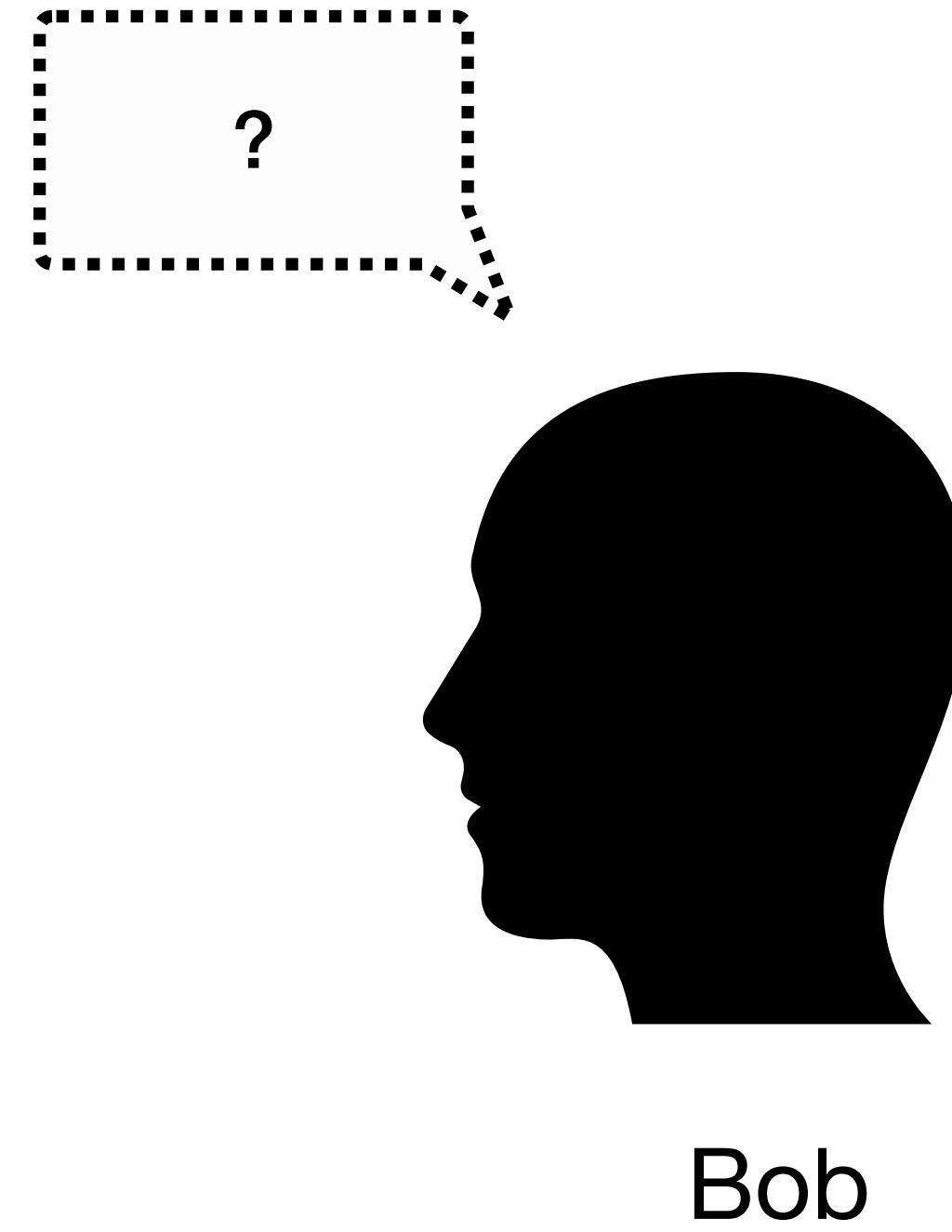
Symmetric Key



Symmetric Key



Alice



Bob

Symmetric Key



Symmetric Key

Property

- One private key for encoding and decoding



Symmetric Key

Property

- One private key for encoding and decoding

Pros

- Low computational resource requirements



Symmetric Key

Property

- One private key for encoding and decoding

Pros

- Low computational resource requirements

Cons

- Key distribution



Symmetric Key

Property

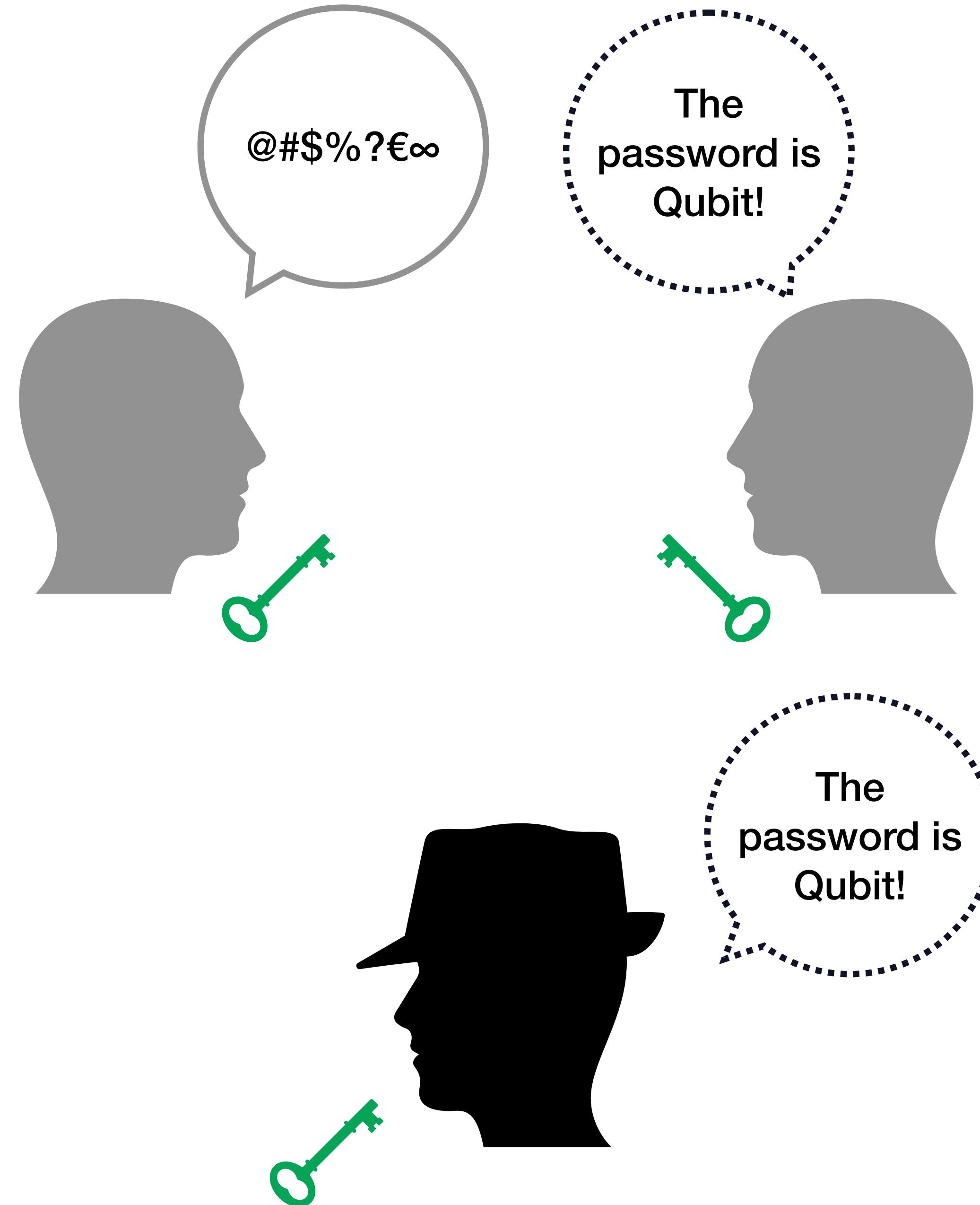
- One private key for encoding and decoding

Pros

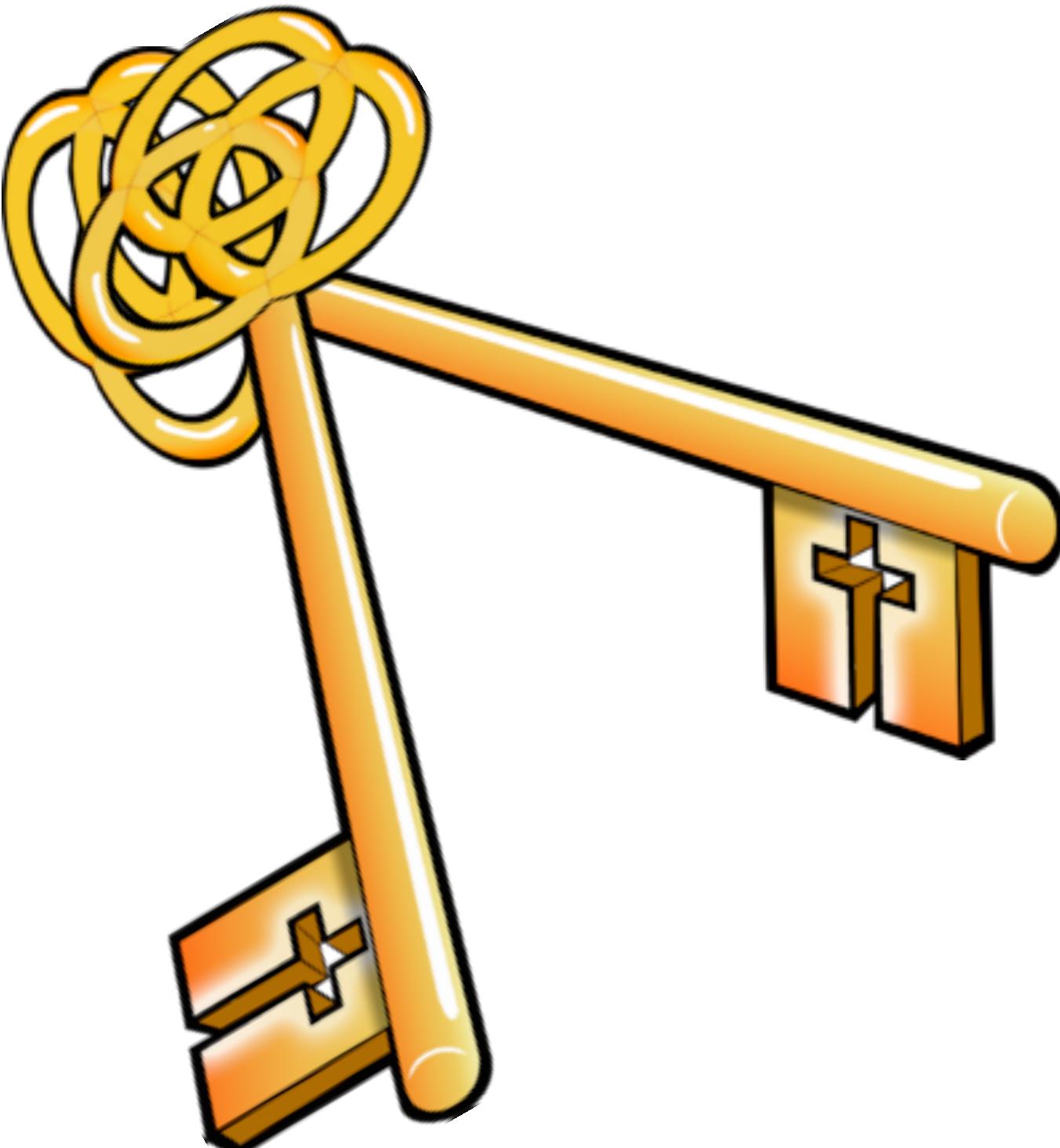
- Low computational resource requirements

Cons

- Key distribution



Asymmetric Key



Properties

- Public key for encryption
- Private key for decryption

Asymmetric Key



Properties

- Public key for encryption
- Private key for decryption

Pros

- Public key distribution

Asymmetric Key



Properties

- Public key for encryption
- Private key for decryption

Pros

- Public key distribution

Cons

- Slow and computationally expensive



Motivation

Quantum cryptography

Motivation

Quantum cryptography



Decrypting messages

- Asymmetric encryption protocols (e.g. RSA with Shor's algorithm)
- Symmetric encryption protocols (e.g. AES with Grover's algorithm)

Motivation

Quantum cryptography



Decrypting messages

- Asymmetric encryption protocols (e.g. RSA with Shor's algorithm)
- Symmetric encryption protocols (e.g. AES with Grover's algorithm)



Quantum cryptography



Quantum Cryptography

Cryptography methods exploiting the properties of quantum mechanics, such as

Superposition

No-cloning theorem

Entanglement



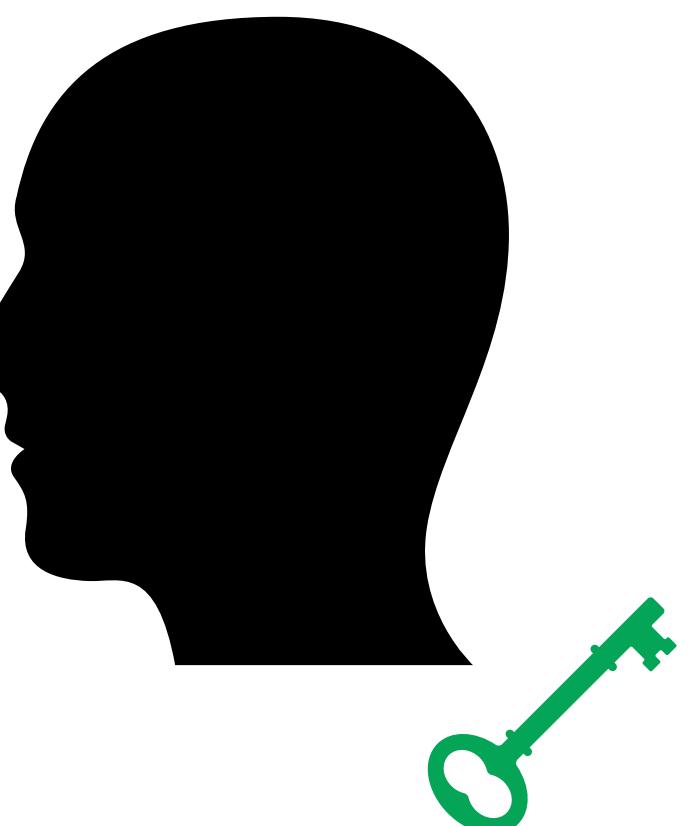
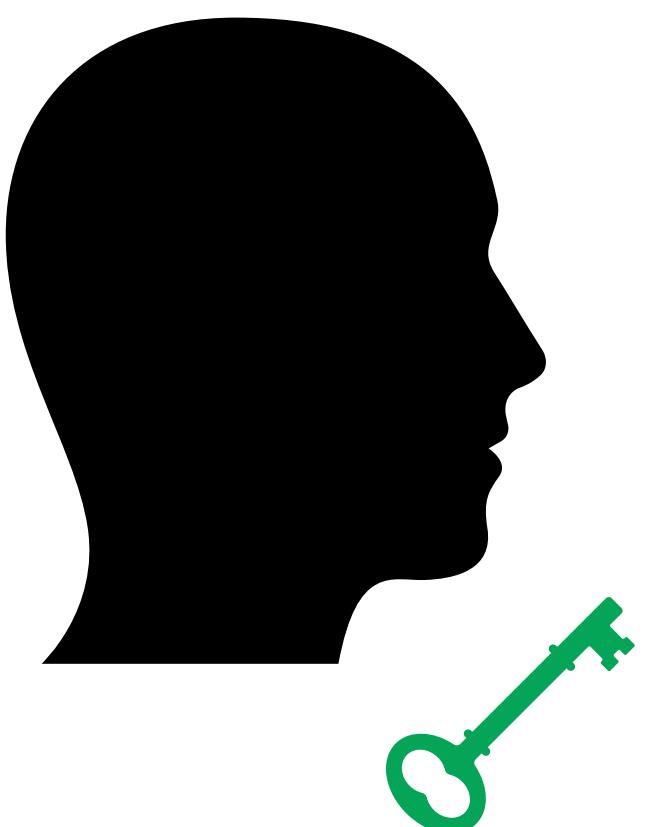
Quantum Key Distribution (QKD)

Quantum Key Distribution

Deploy a symmetric key at Alice's and Bob's using the properties of quantum mechanics

Perfect theoretical security

Spy detection



Protocol E91



All Journals Physics Magazine

Physical Review Letters

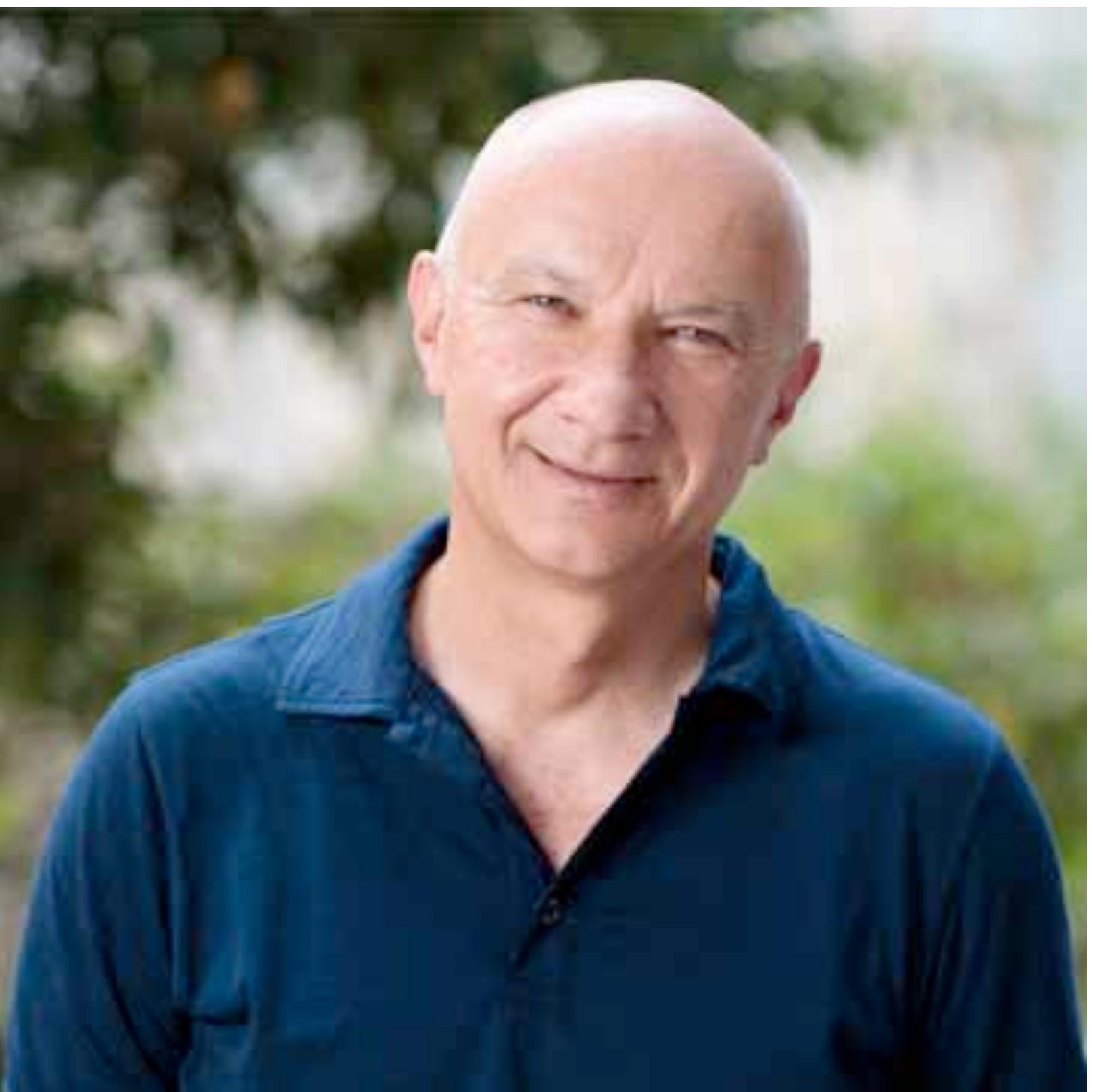
Quantum cryptography based on Bell's theorem

[Artur K. Ekert](#)

Show more ▾

Phys. Rev. Lett. **67**, 661 – Published 5 August, 1991

DOI: <https://doi.org/10.1103/PhysRevLett.67.661>



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The Classical Bit

Classical information

- The bit = the information unit
0 or 1
- Information can be encoded in chains of bits.

00000	■■■	01000	■■■	10000	■■■	11000	■■■
00001	■■■	01001	■■■	10001	■■■	11001	■■■
00010	■■■	01010	■■■	10010	■■■	11010	■■■
00011	■■■	01011	■■■	10011	■■■	11011	■■■
00100	■■■	01100	■■■	10100	■■■	11100	■■■
00101	■■■	01101	■■■	10101	■■■	11101	■■■
00110	■■■	01110	■■■	10110	■■■	11110	■■■
00111	■■■	01111	■■■	10111	■■■	11111	■■■

The Classical Bit

Classical information

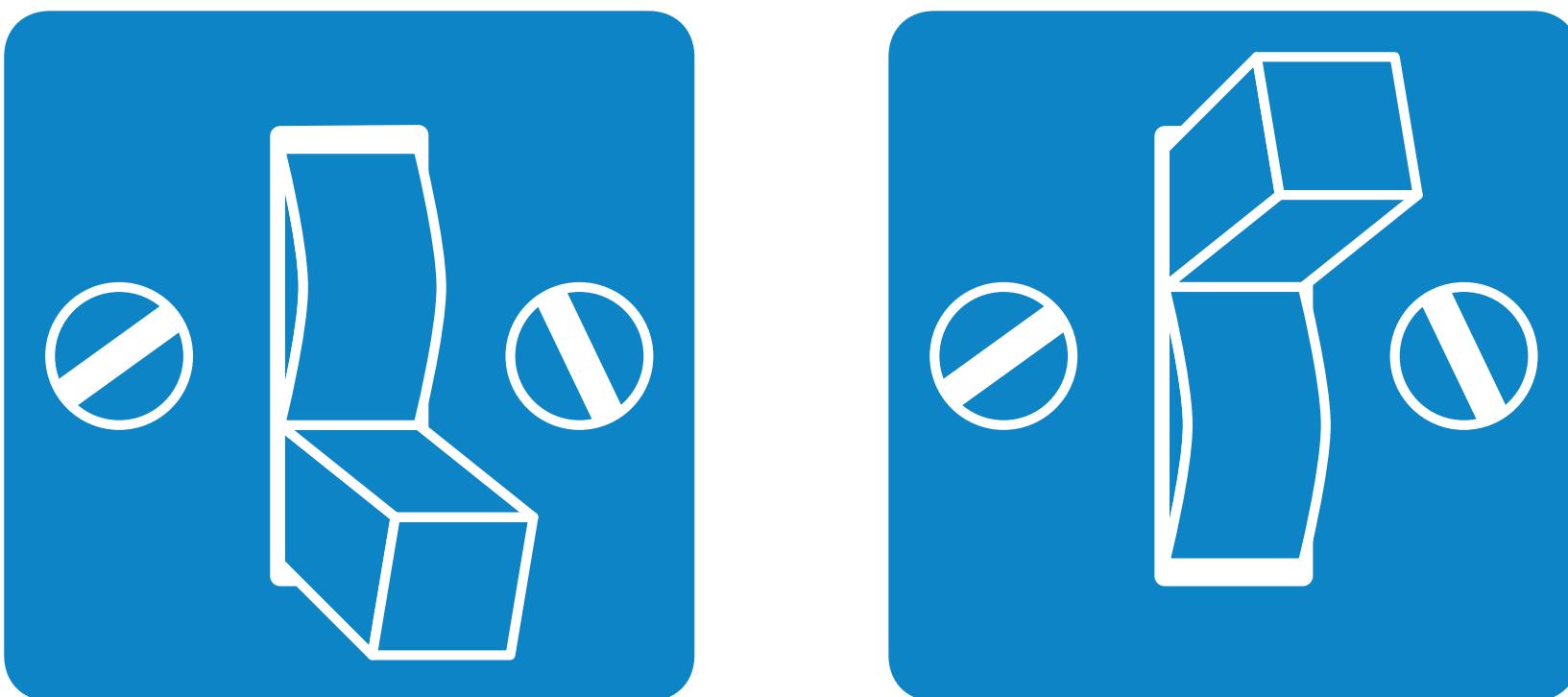
- The bit = the information unit
0 or 1
- Information can be encoded in chains of bits.
- With 5 bits we can encode :
 - Numbers from 0 to 31
 - The alphabet

00000	0	a	01000	8	i	10000	16	q	11000	24	y
00001	1	b	01001	9	j	10001	17	r	11001	25	z
00010	2	c	01010	10	k	10010	18	s	11010	26	
00011	3	d	01011	11	l	10011	19	t	11011	27	
00100	4	e	01100	12	m	10100	20	u	11100	28	
00101	5	f	01101	13	n	10101	21	v	11101	29	
00110	6	g	01110	14	o	10110	22	w	11110	30	
00111	7	h	01111	15	p	10111	23	x	11111	31	

Physical Representation

Classical information

Bit



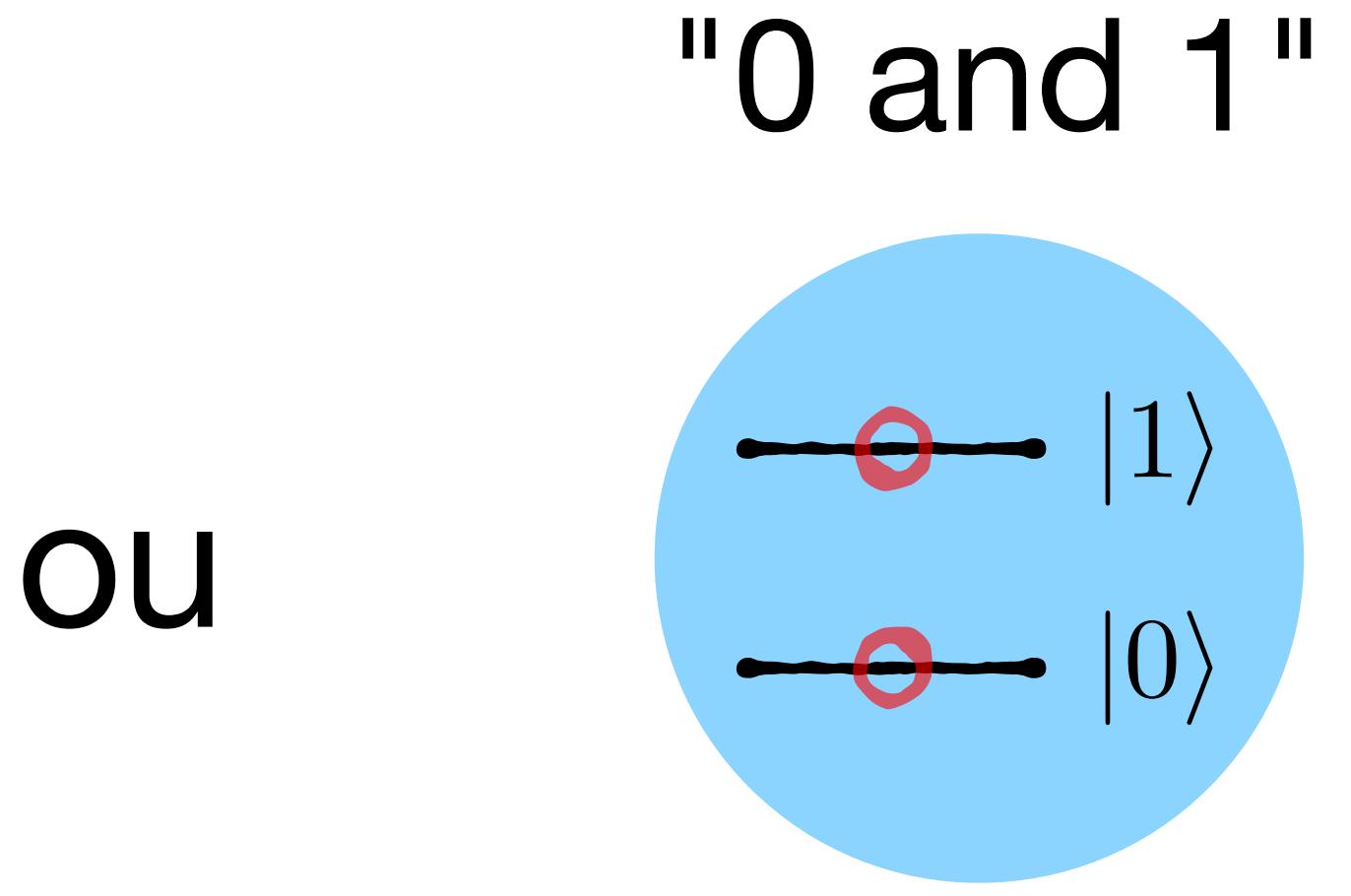
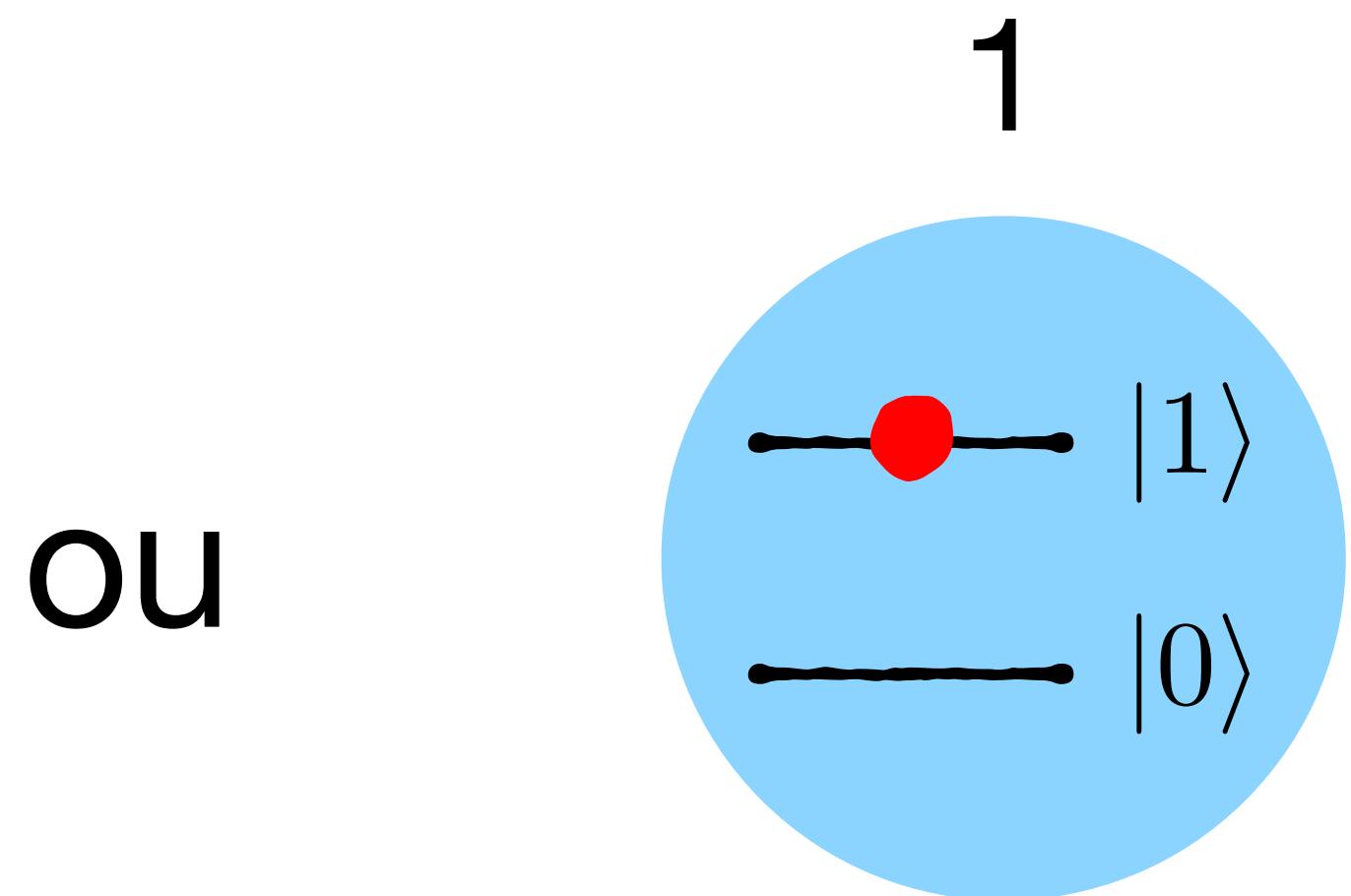
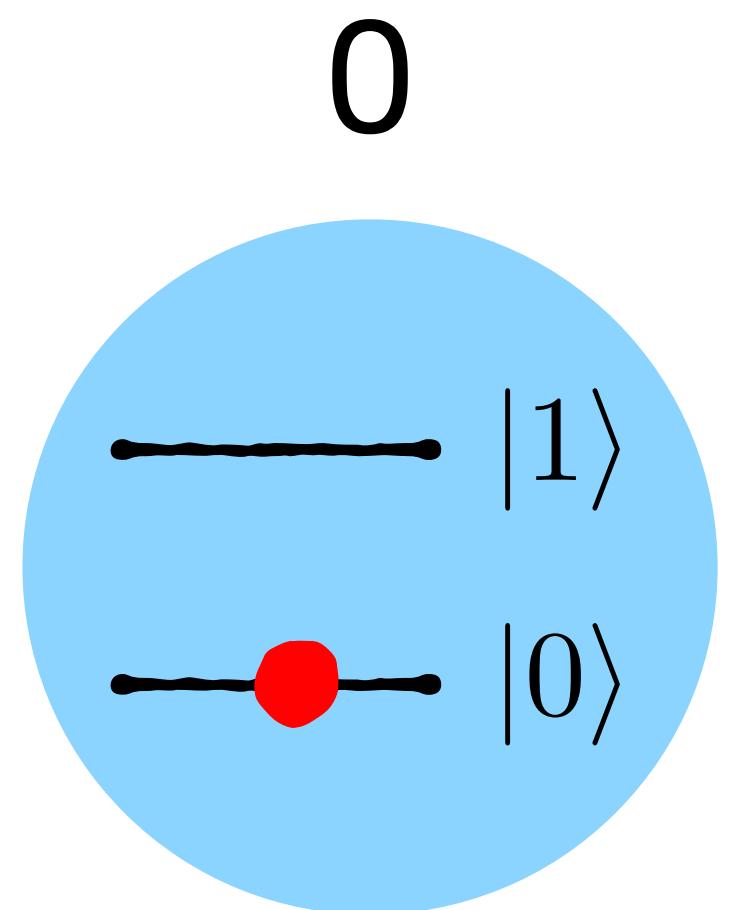
0

1

Quantum Information

The qubit

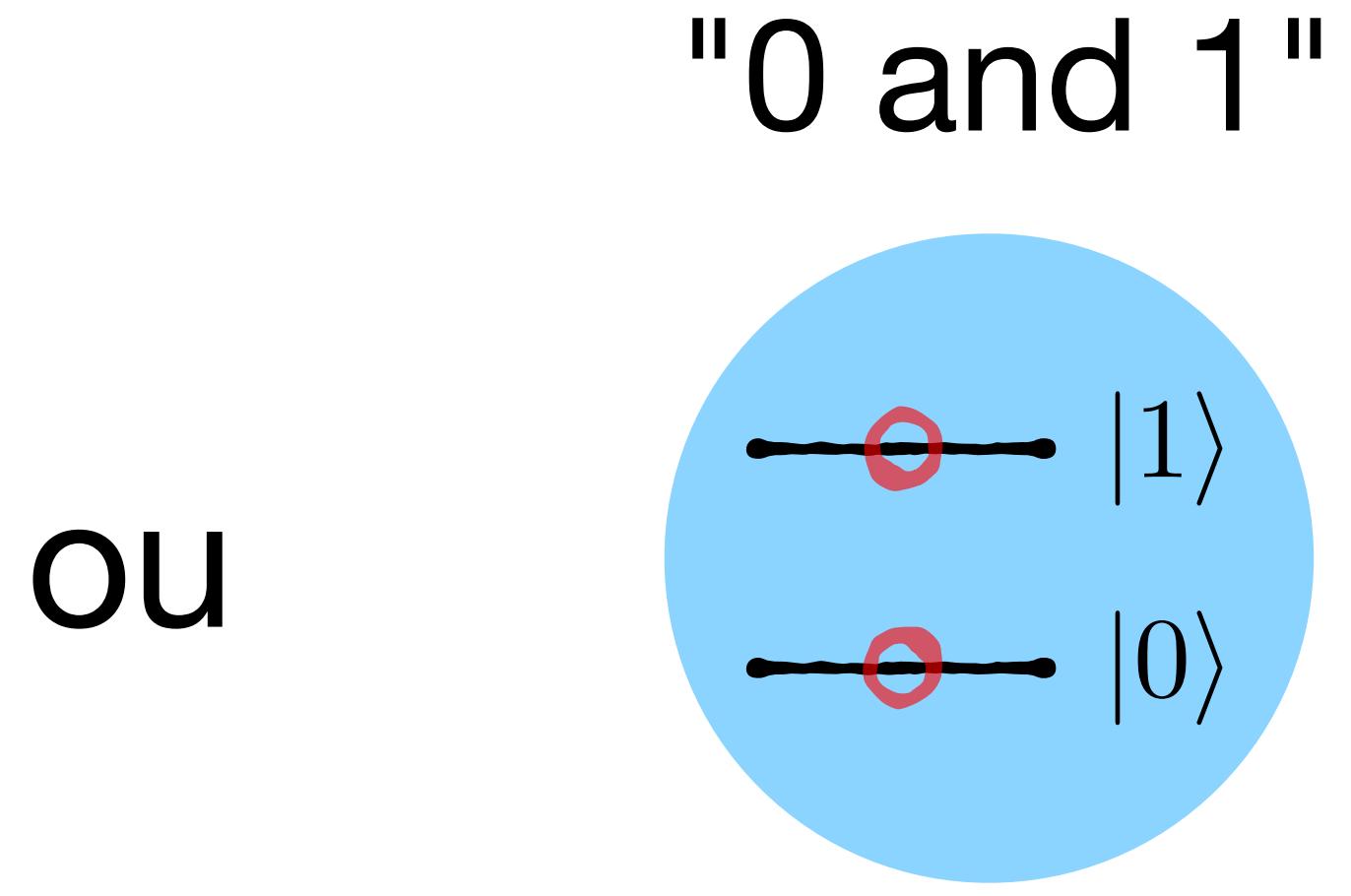
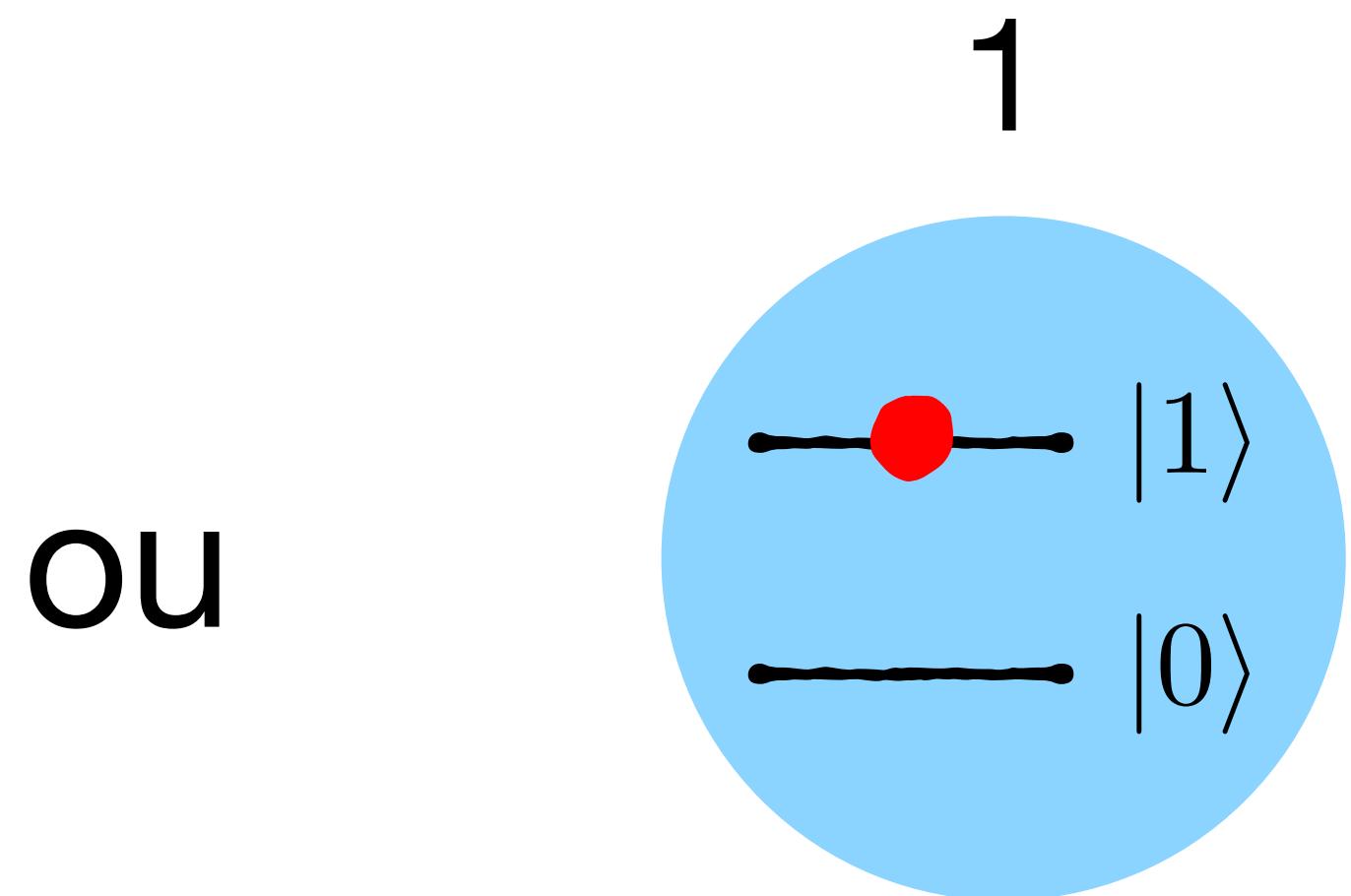
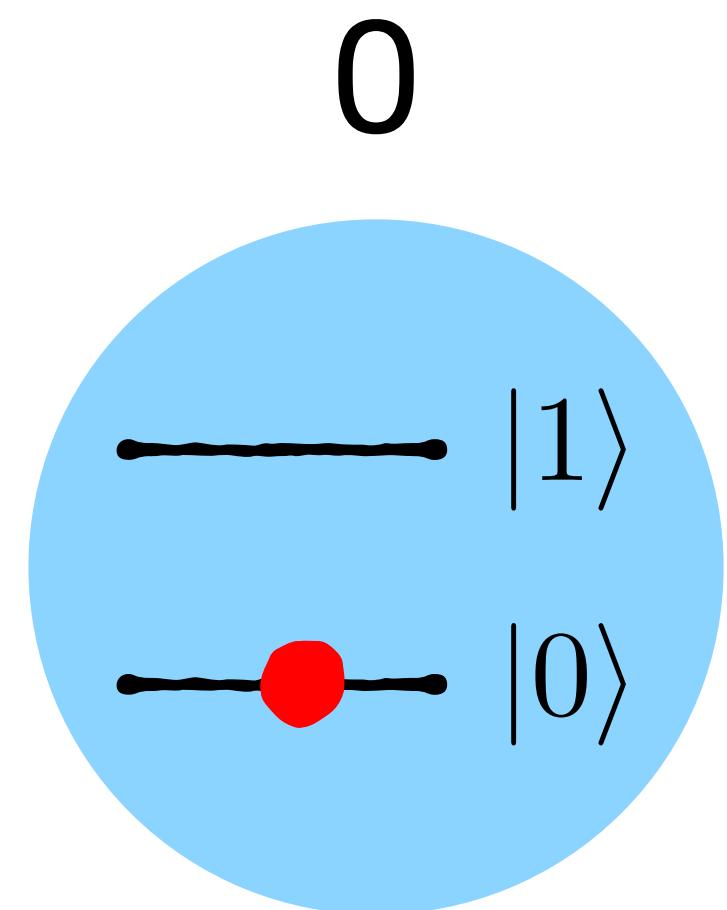
- The qubit = quantum bit
- Takes a continuum of values



Quantum Information

The qubit

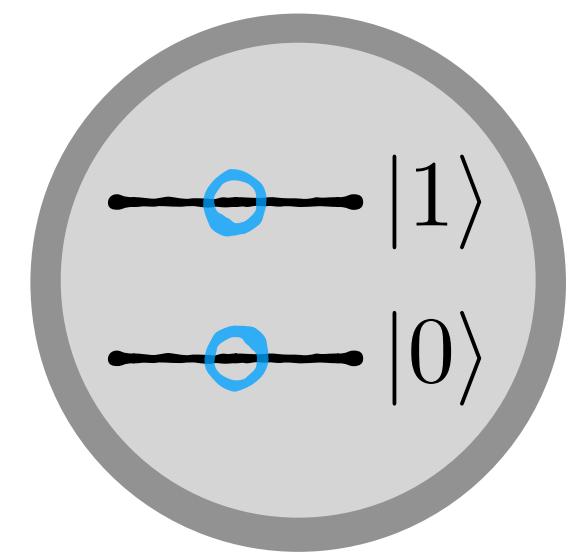
- The qubit = quantum bit
- Takes a continuum of values



Superposition
state

Dirac Notation

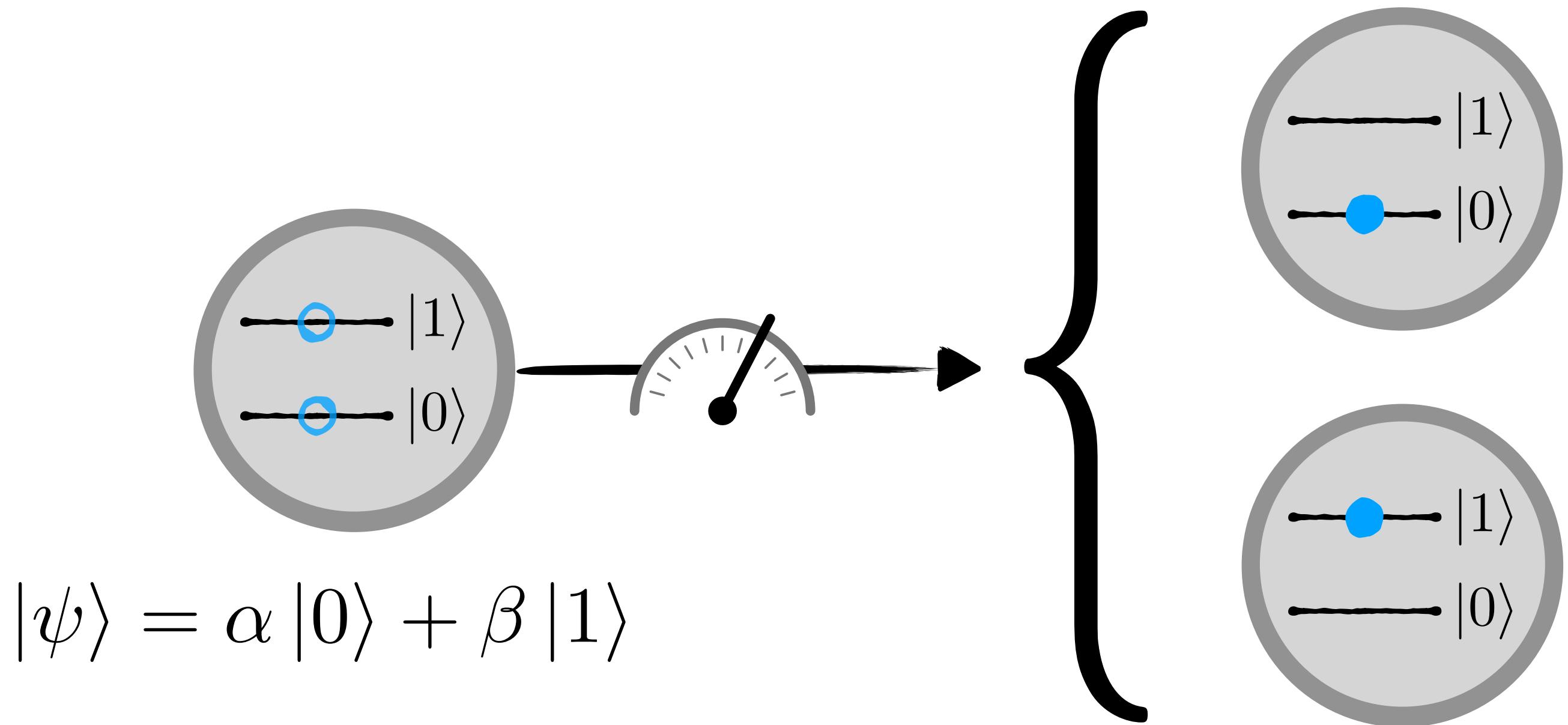
Superposition



$$|\psi\rangle = \alpha|0\rangle + \beta|1\rangle$$

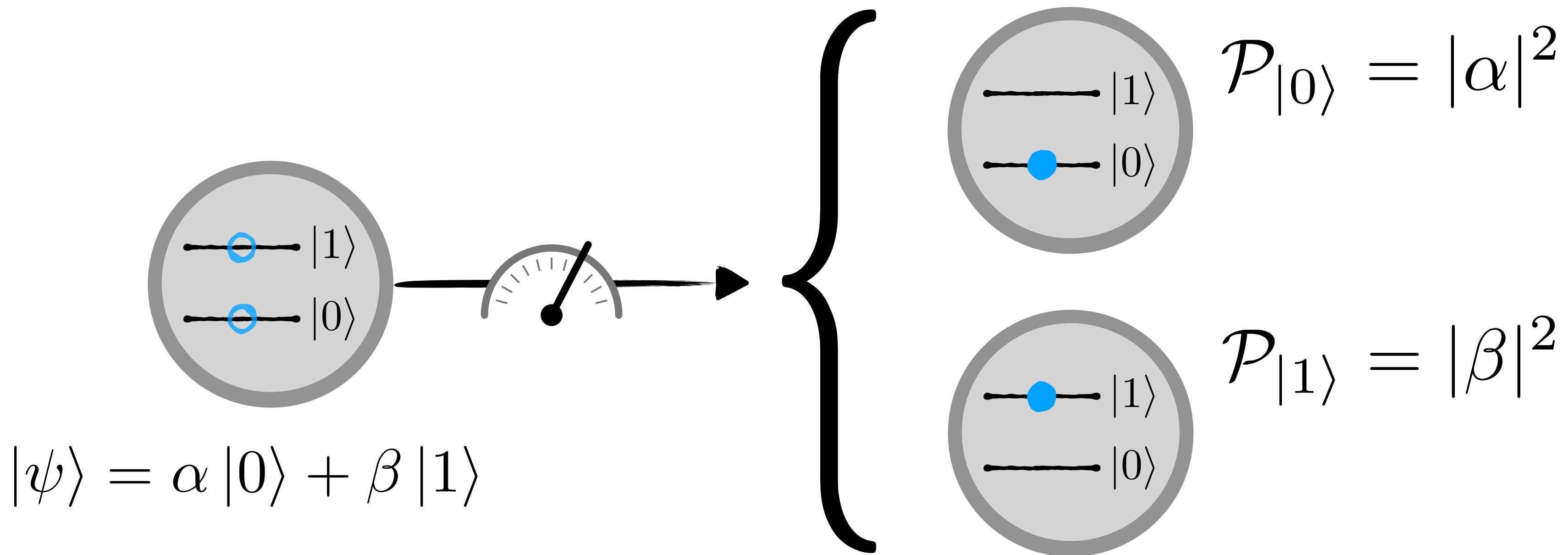
Dirac Notation

Superposition



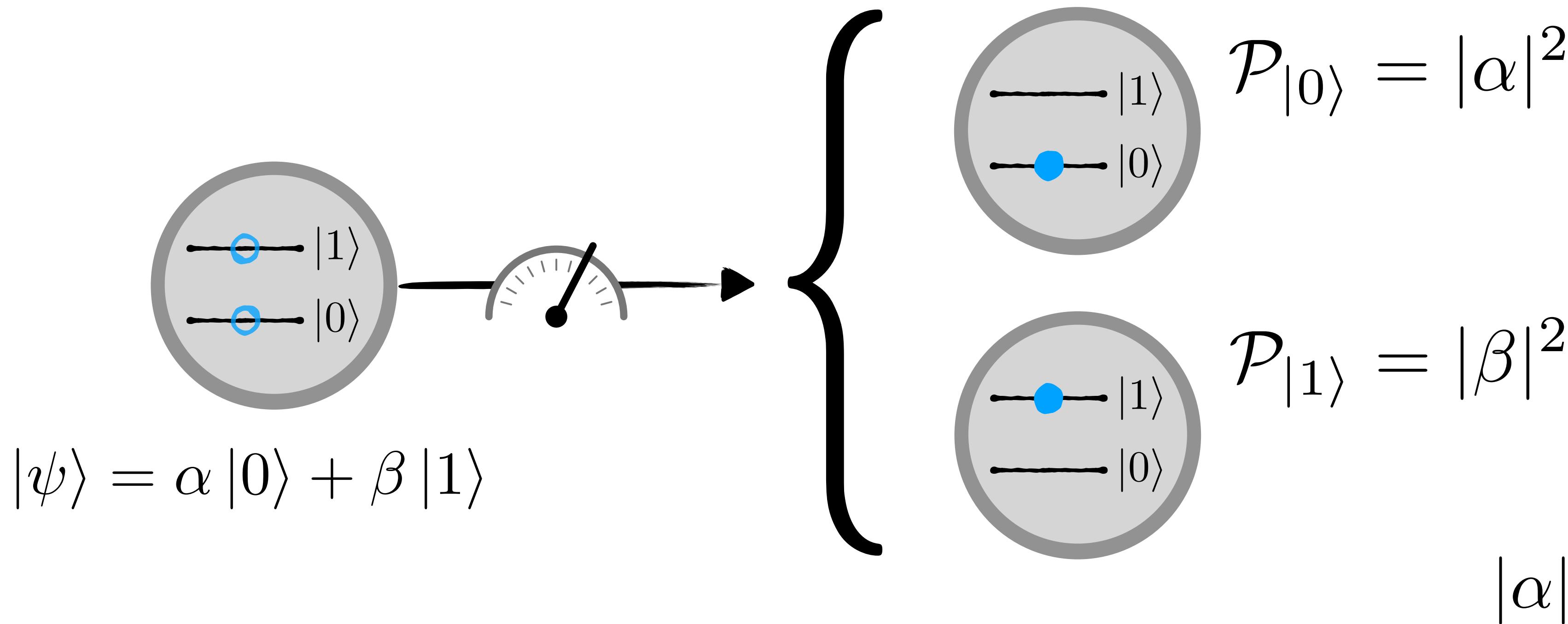
Dirac Notation

Superposition



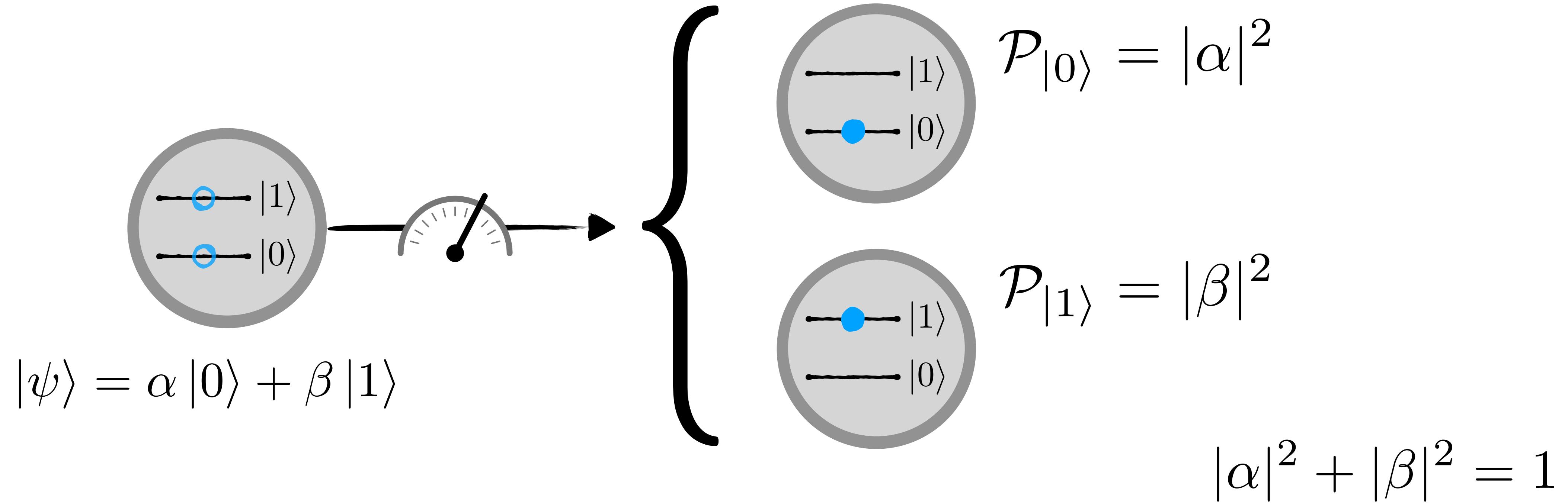
Dirac Notation

Superposition



Dirac Notation

Superposition



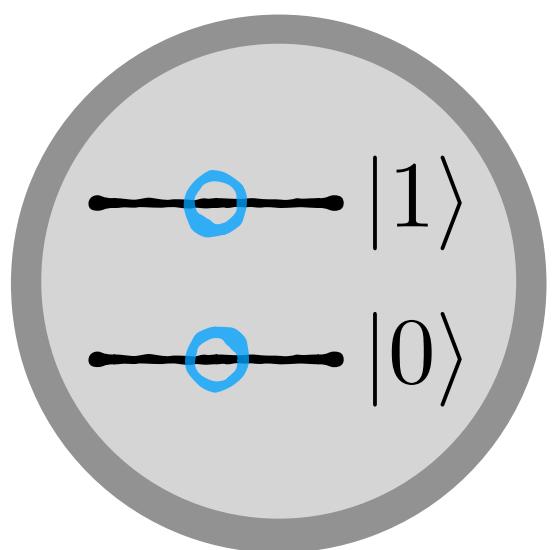
Examples :

$$|\psi\rangle = 1|0\rangle + 0|1\rangle \quad |\psi\rangle = \frac{1}{\sqrt{2}}|0\rangle + \frac{1}{\sqrt{2}}|1\rangle \quad |\psi\rangle = \frac{1}{\sqrt{2}}|0\rangle + \frac{-1}{\sqrt{2}}|1\rangle$$

Physical Representation

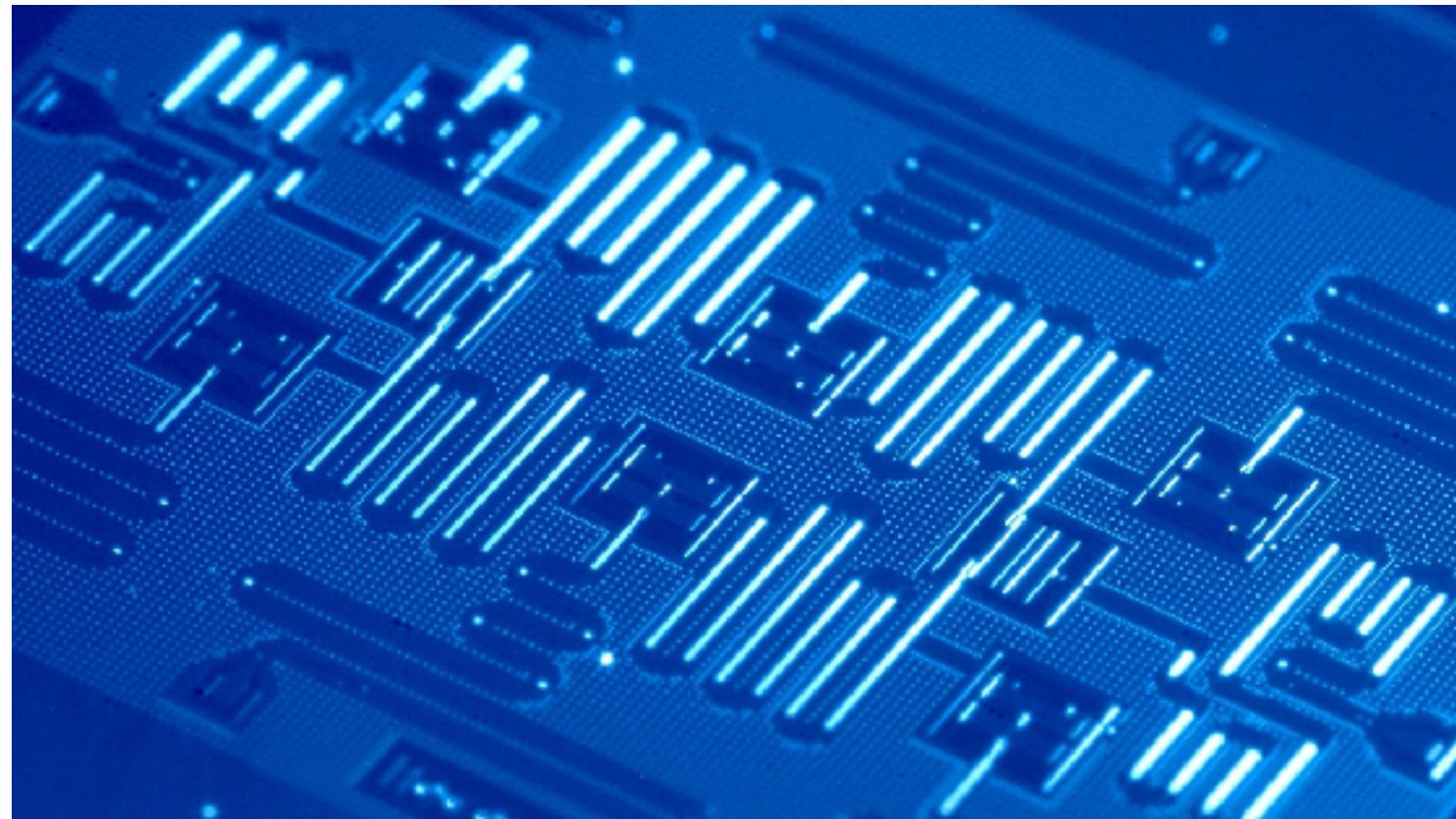
Quantum Information

Qubit

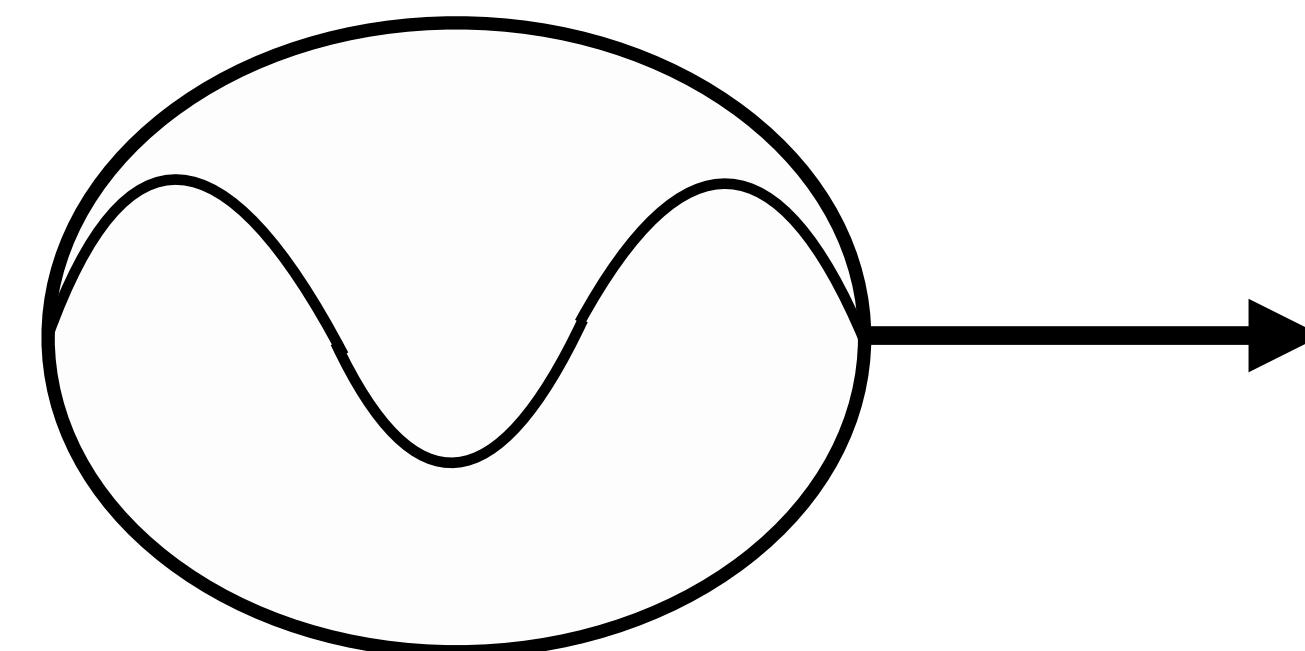


$$|\psi\rangle = \alpha|0\rangle + \beta|1\rangle$$

Supraconducting qubits



IBM



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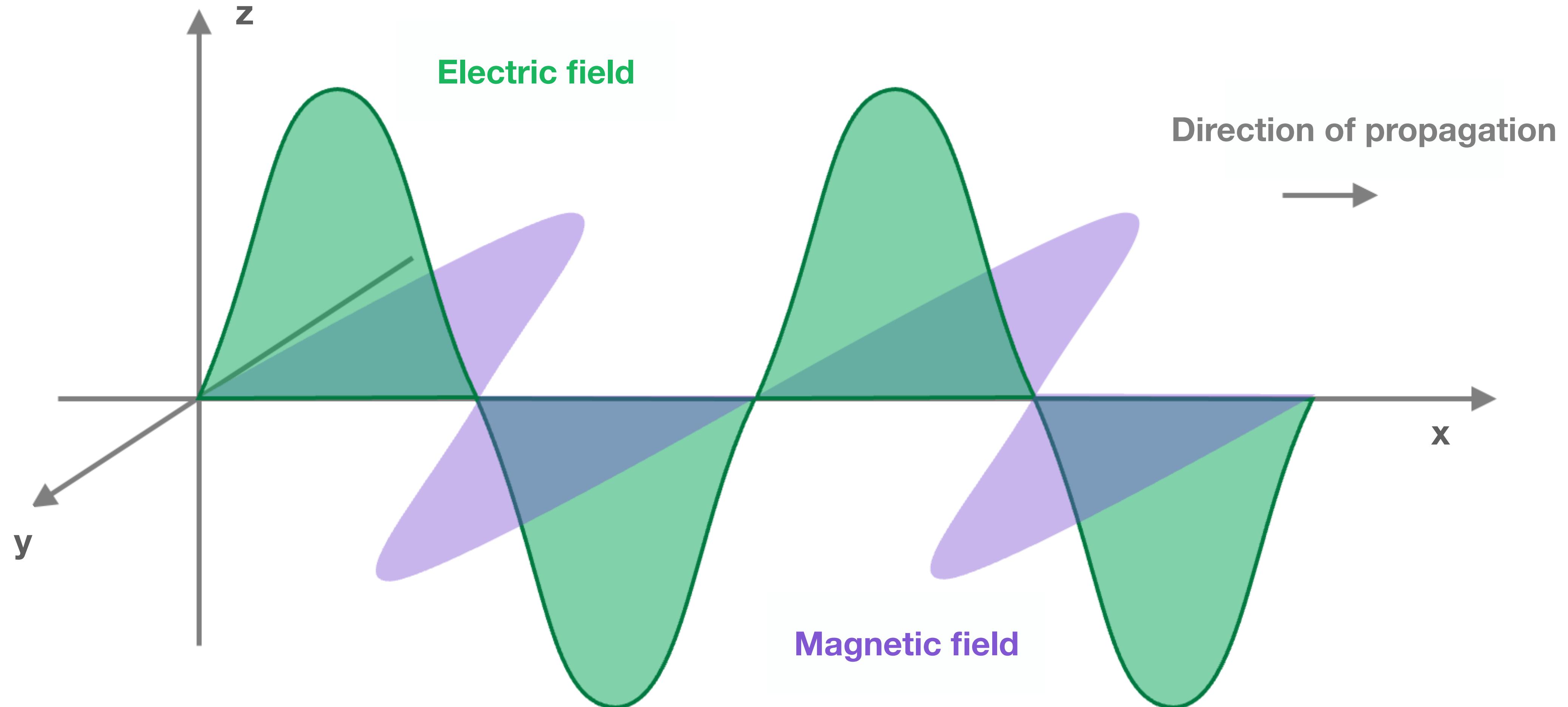
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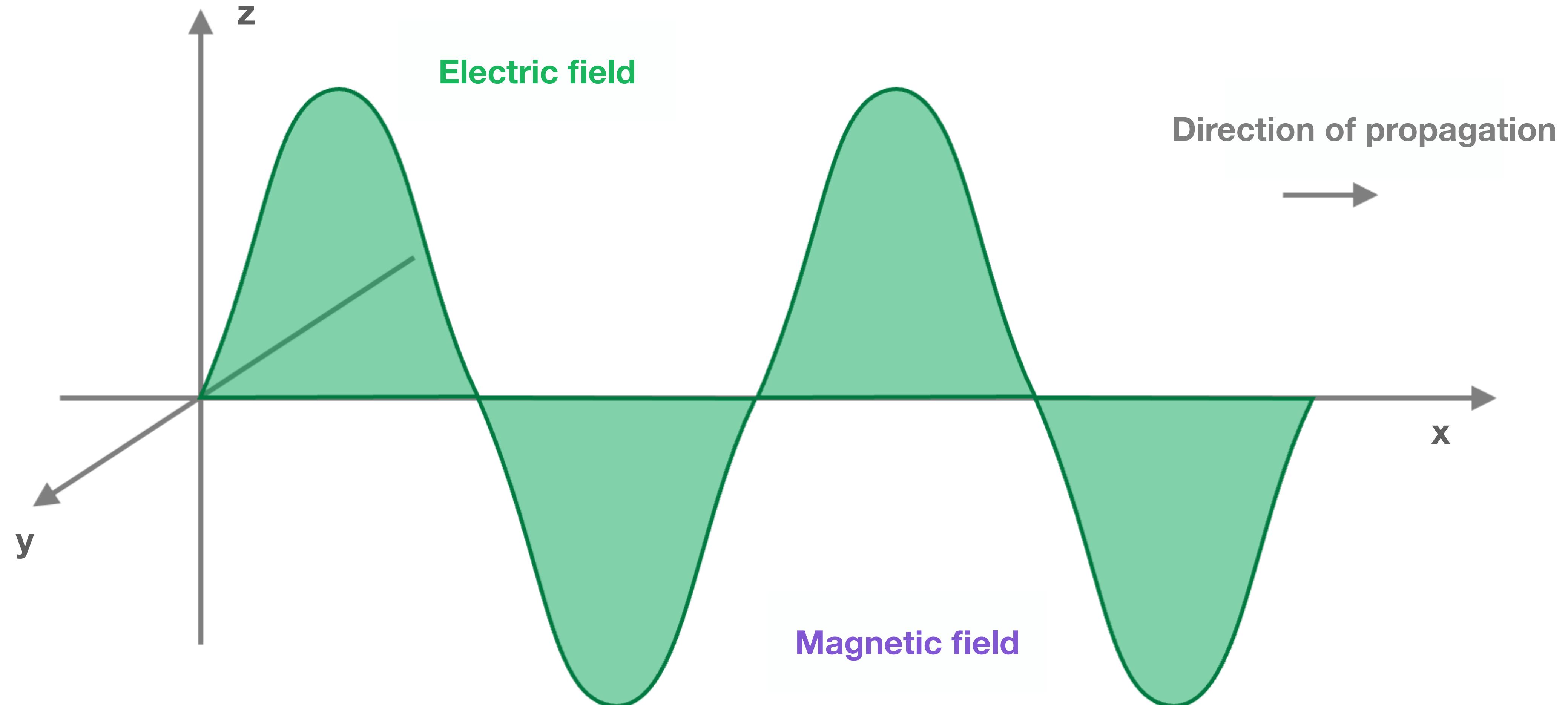
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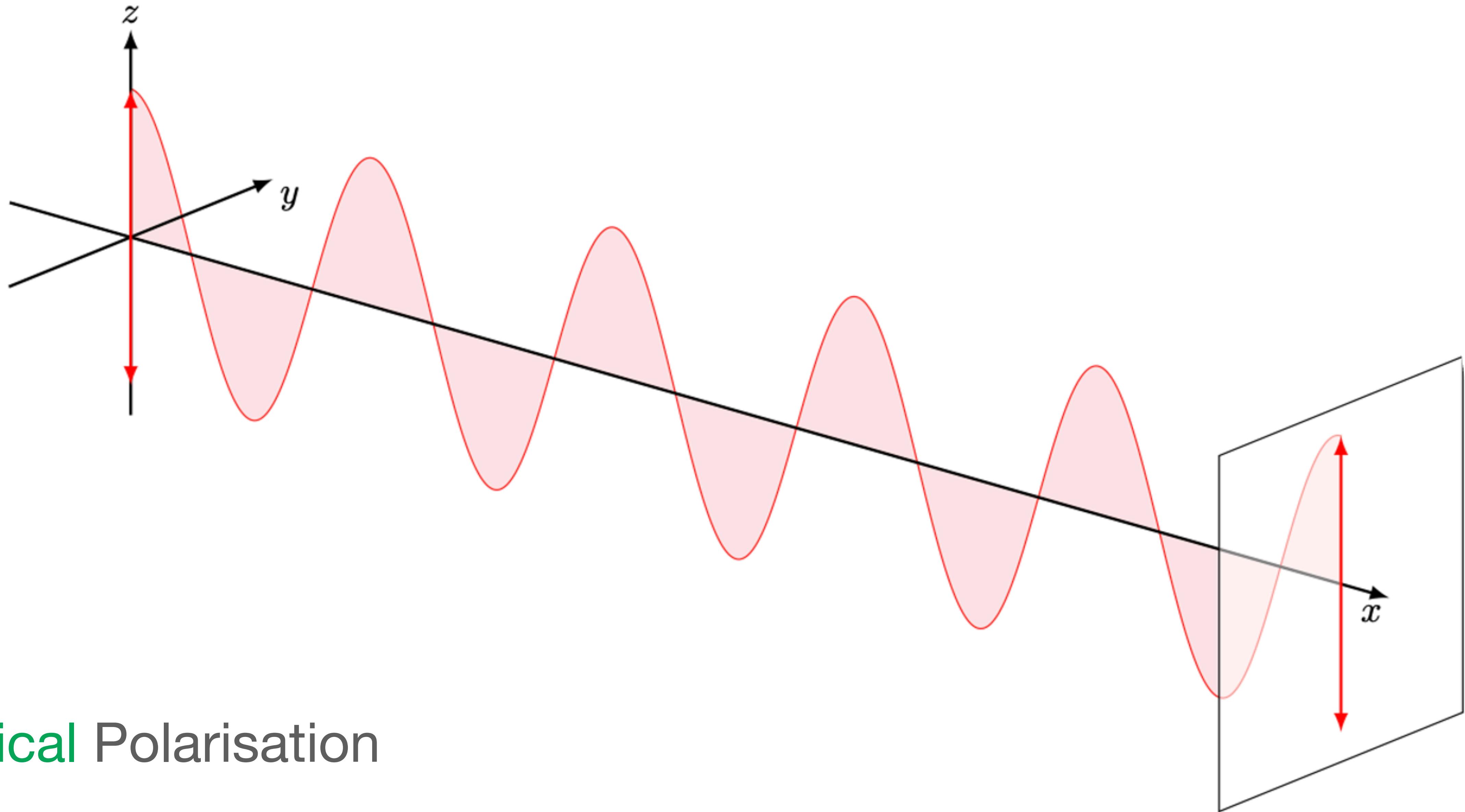
Light



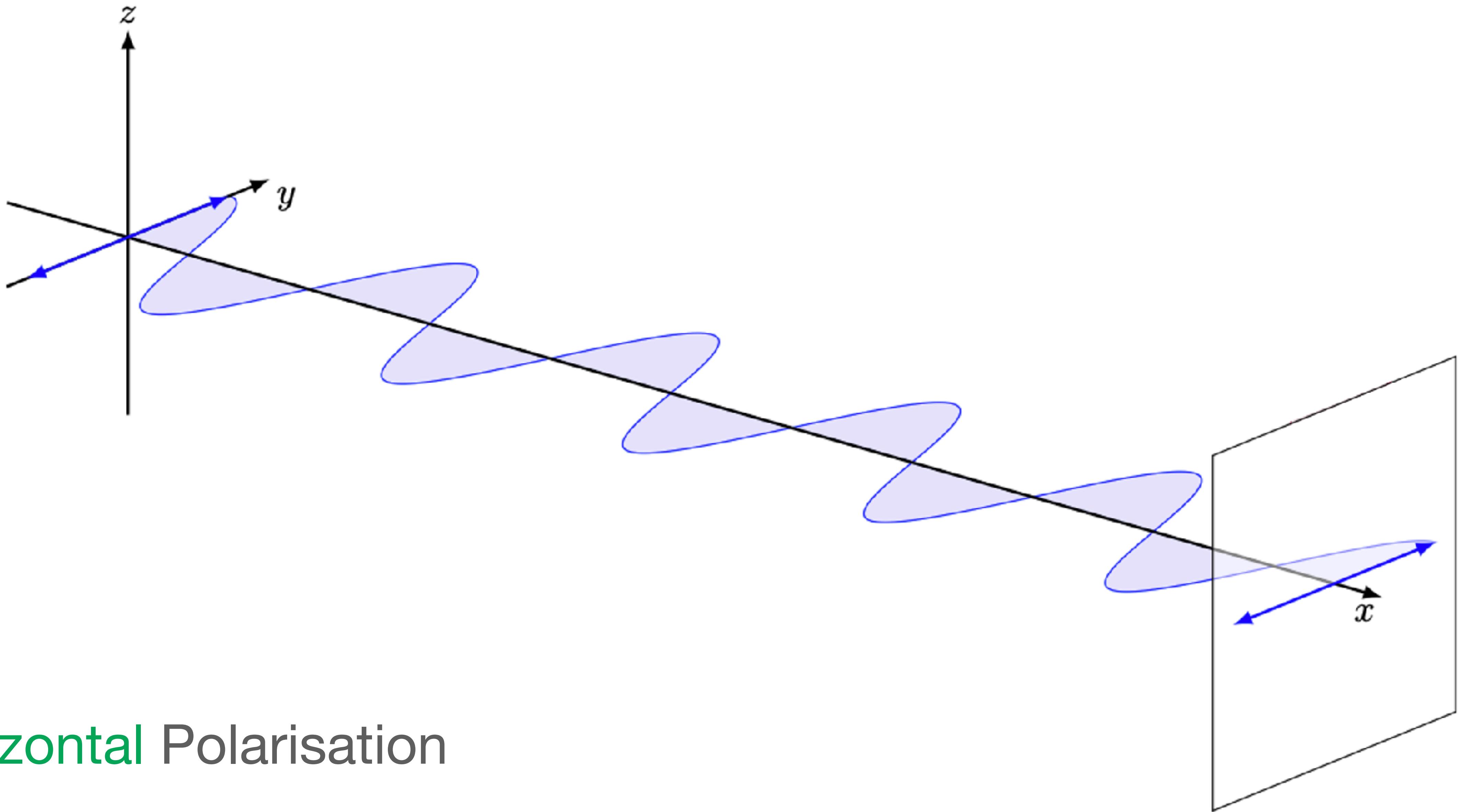
Polarisation: a Quantum Property



Polarisation: a Quantum Property

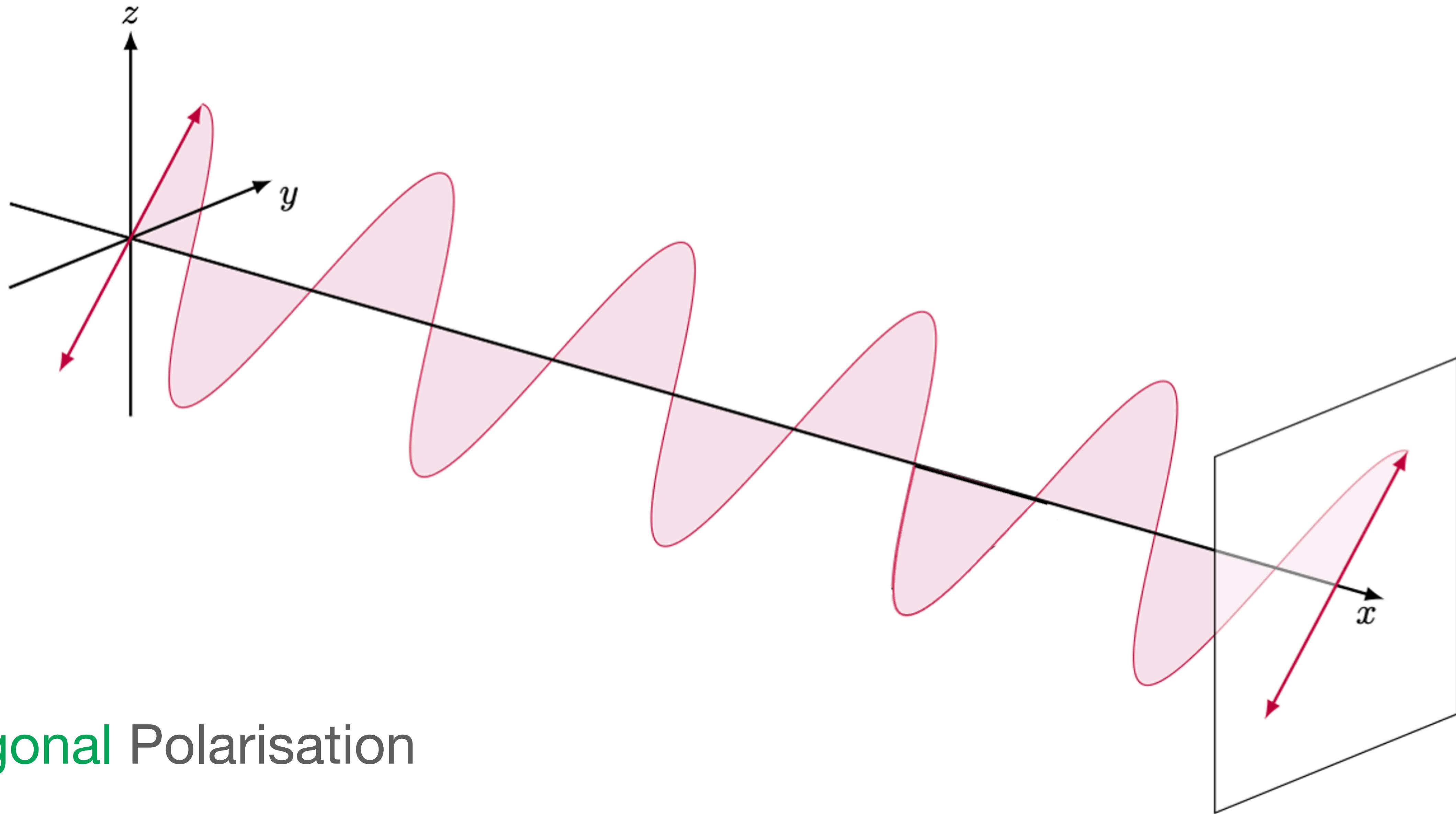


Polarisation: a Quantum Property



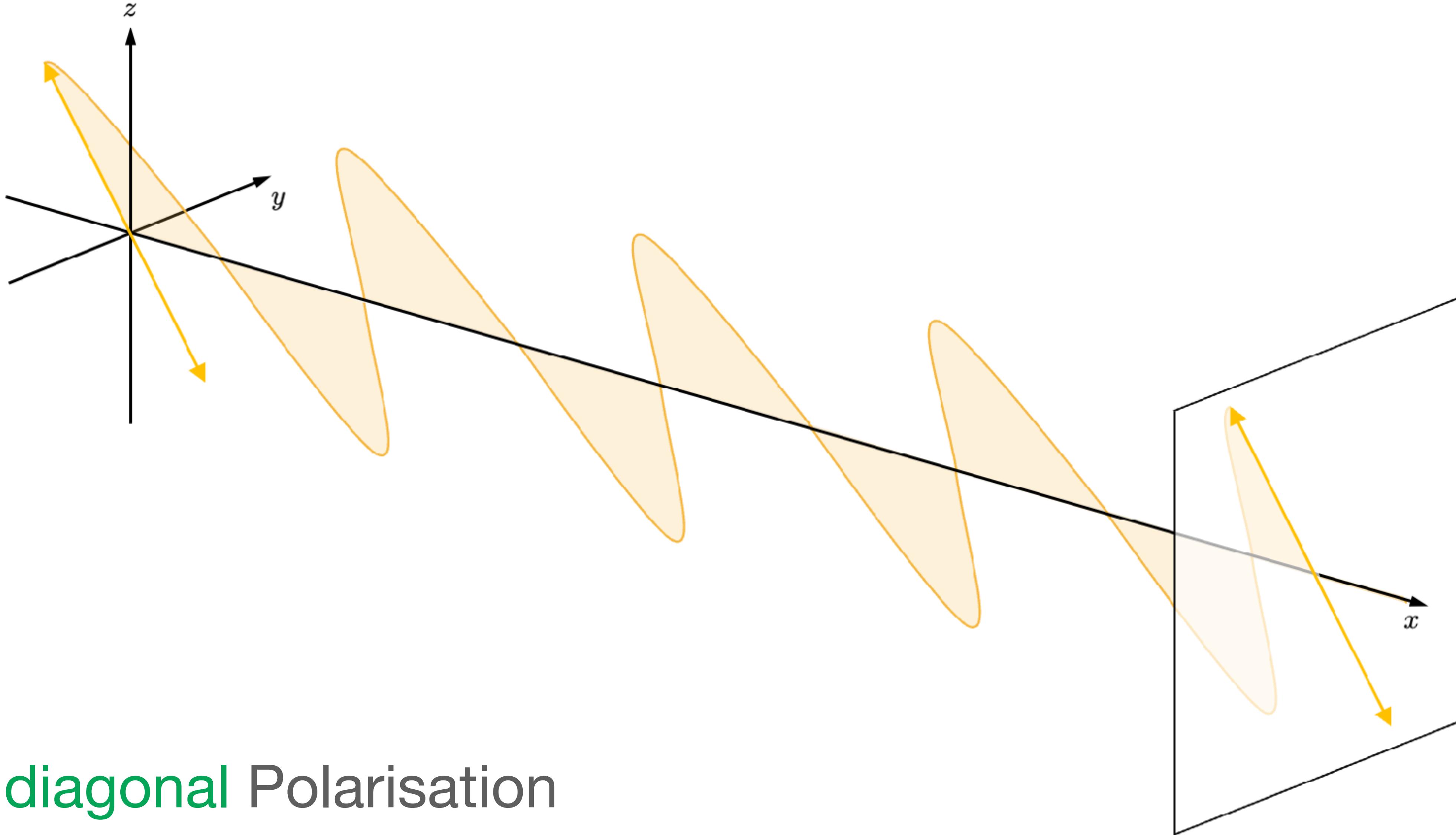
Horizontal Polarisation

Polarisation: a Quantum Property



Diagonal Polarisation

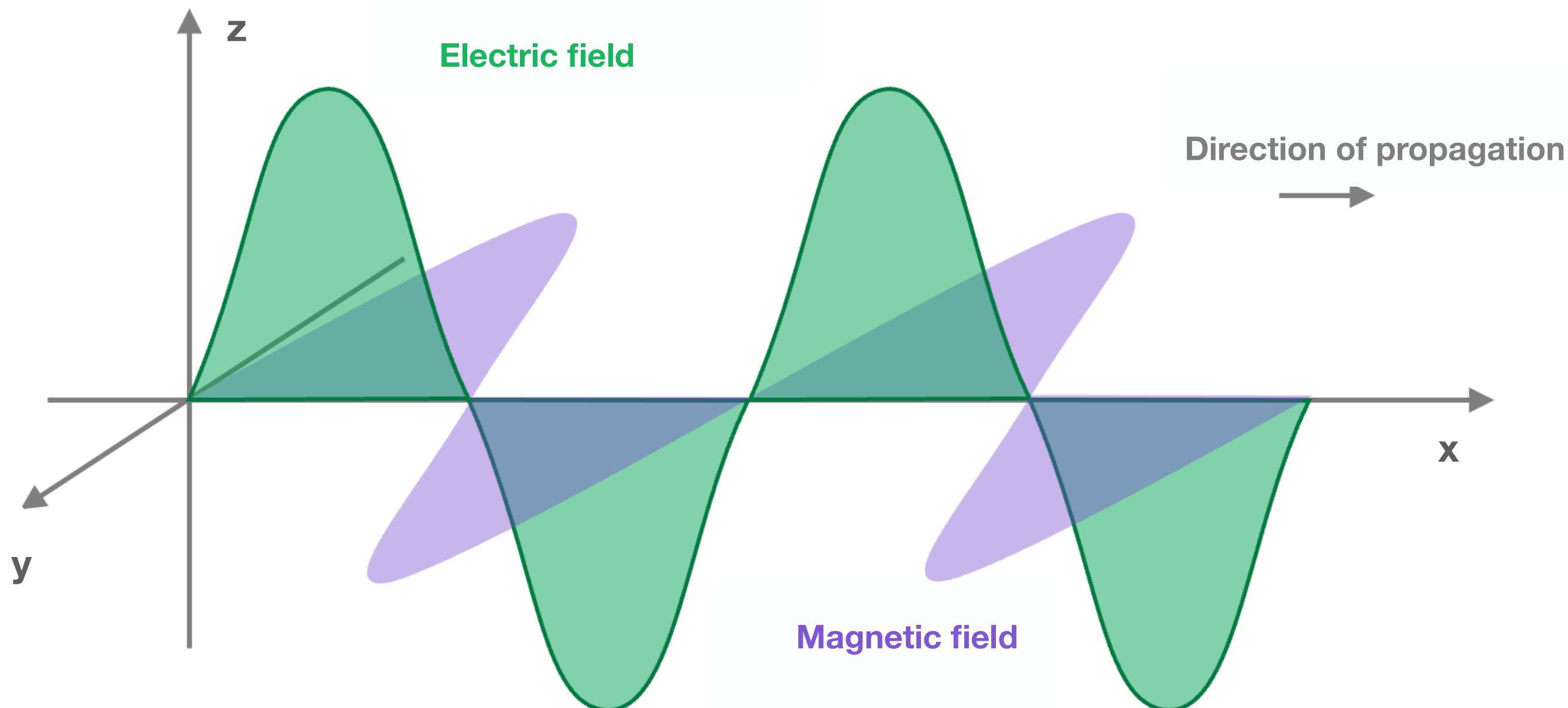
Polarisation: a Quantum Property



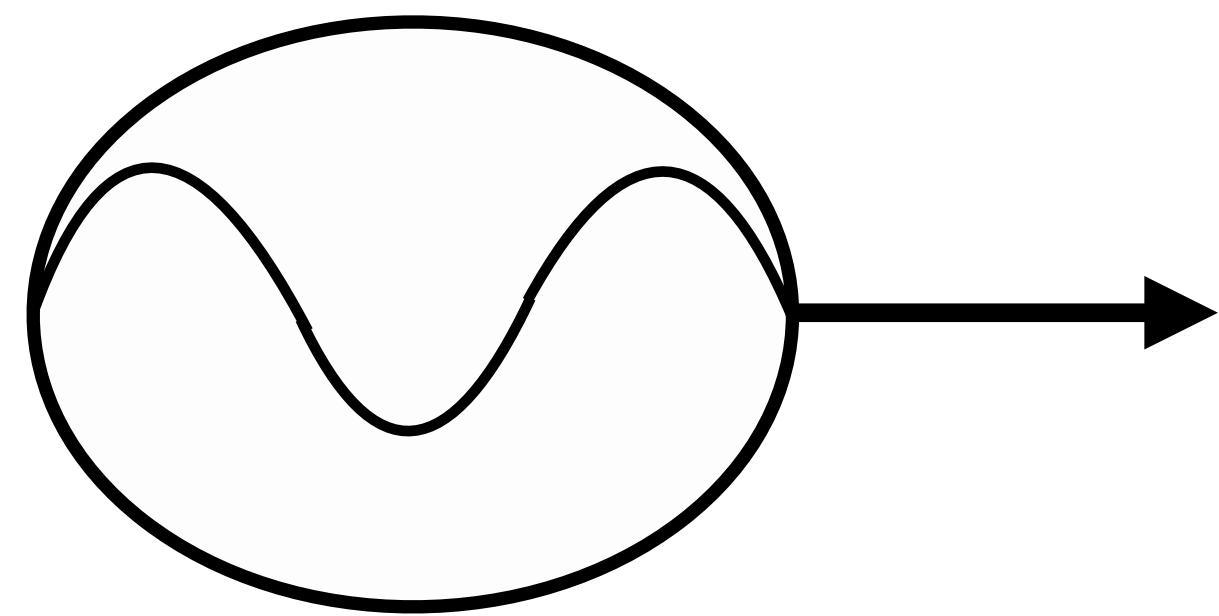
Antidiagonal Polarisation

Wave-Particle Duality of Light

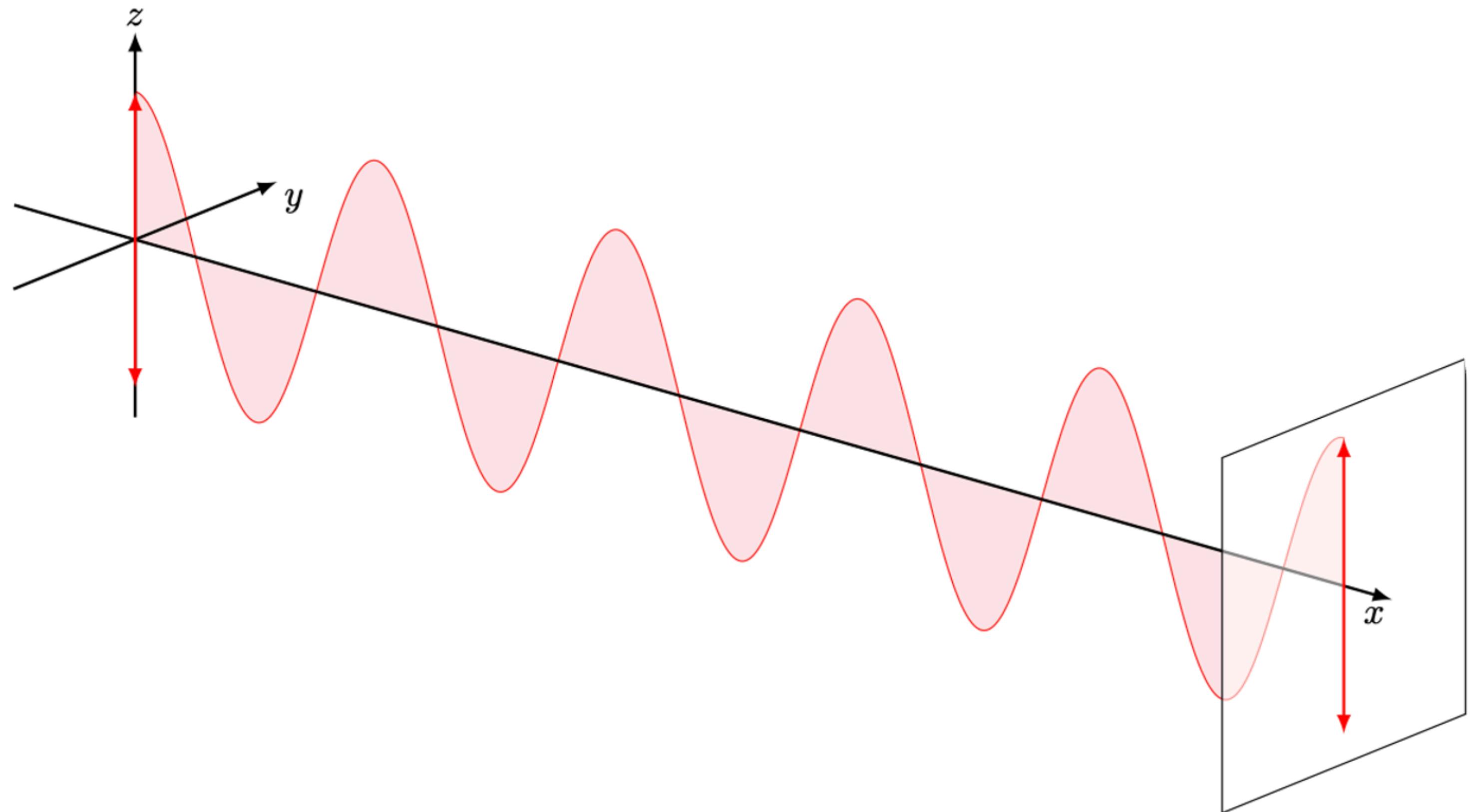
Electromagnetic wave



Photon

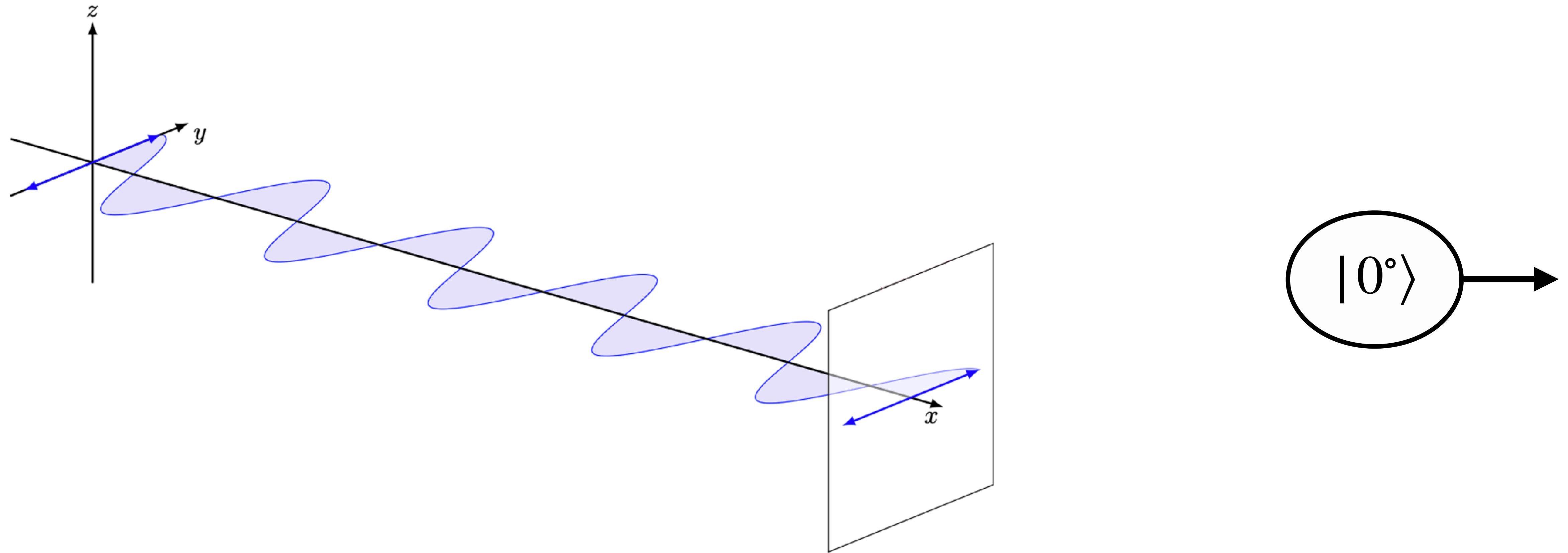


Vertical Polarisation

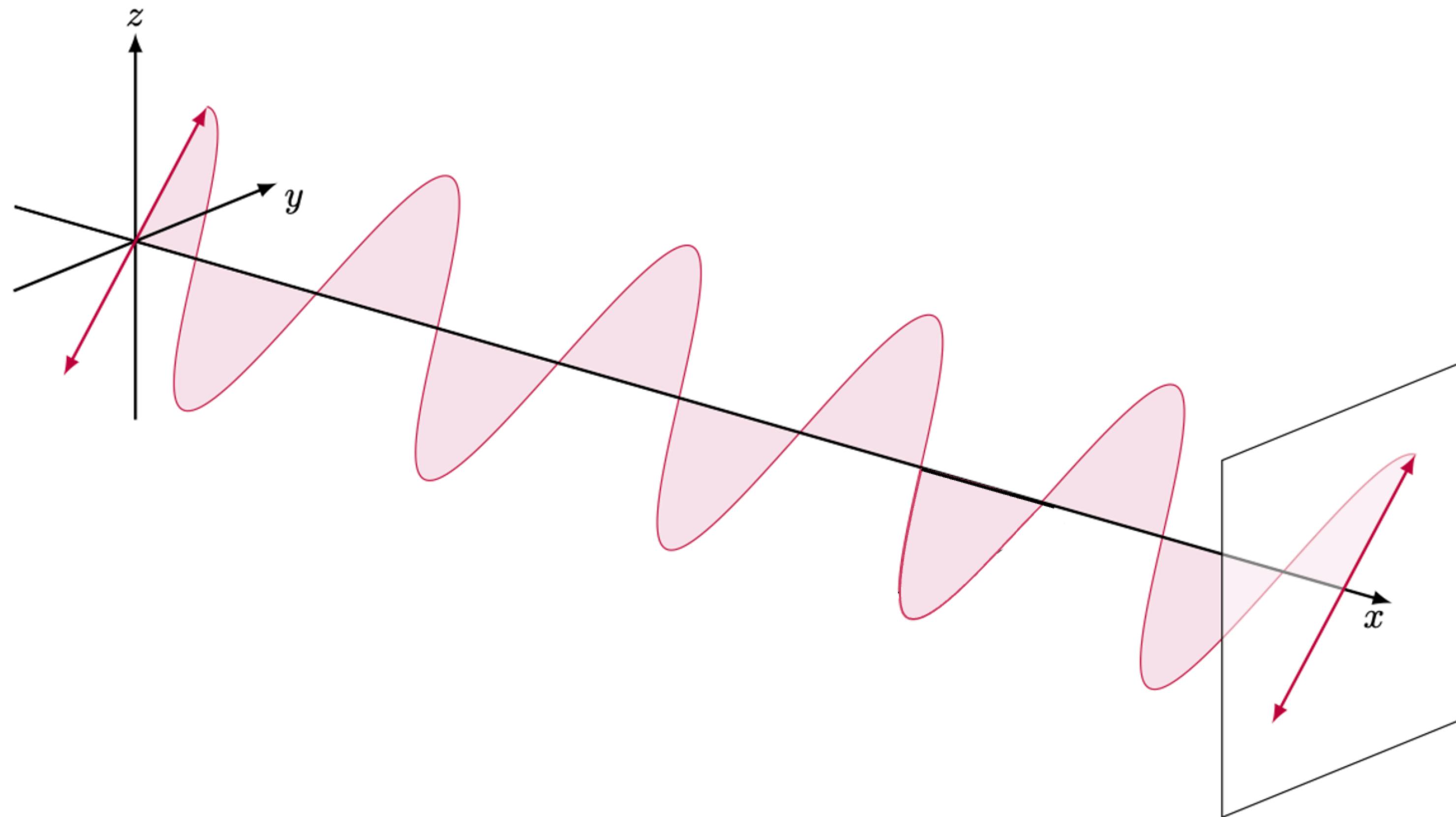


$|90^\circ\rangle$

Horizontal Polarisation

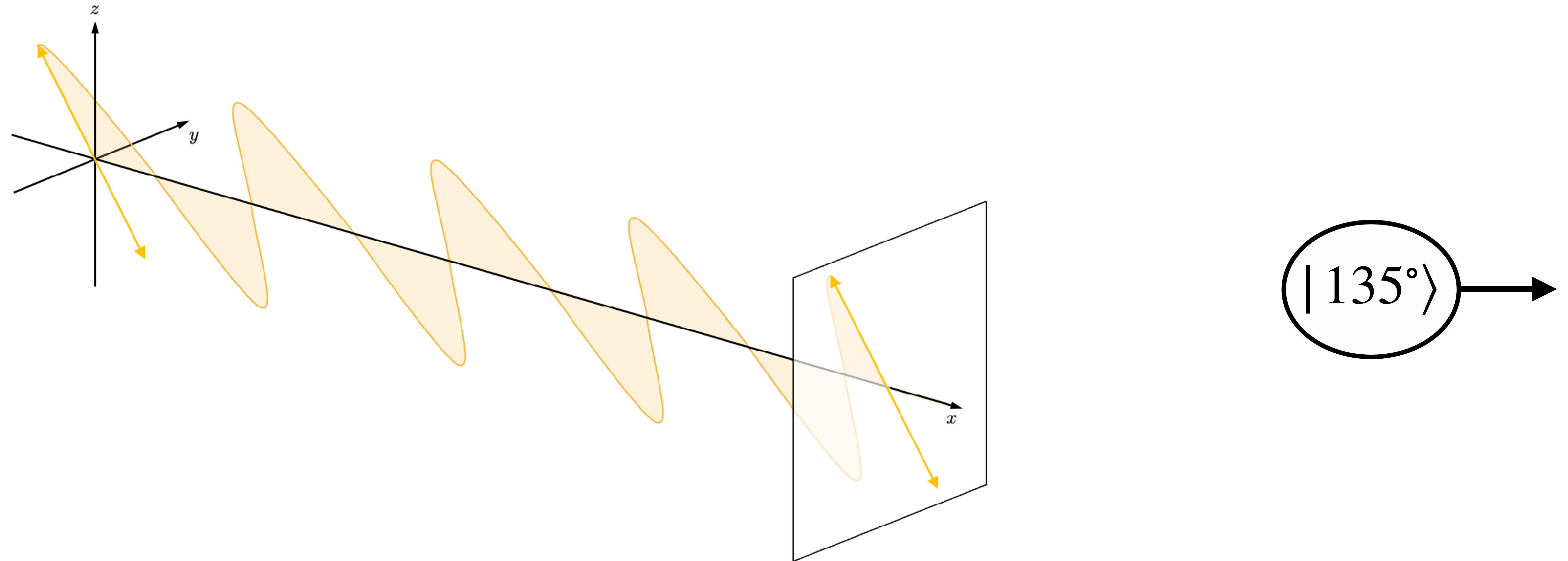


Diagonal Polarisation



$|45^\circ\rangle$

Antidiagonal Polarisation

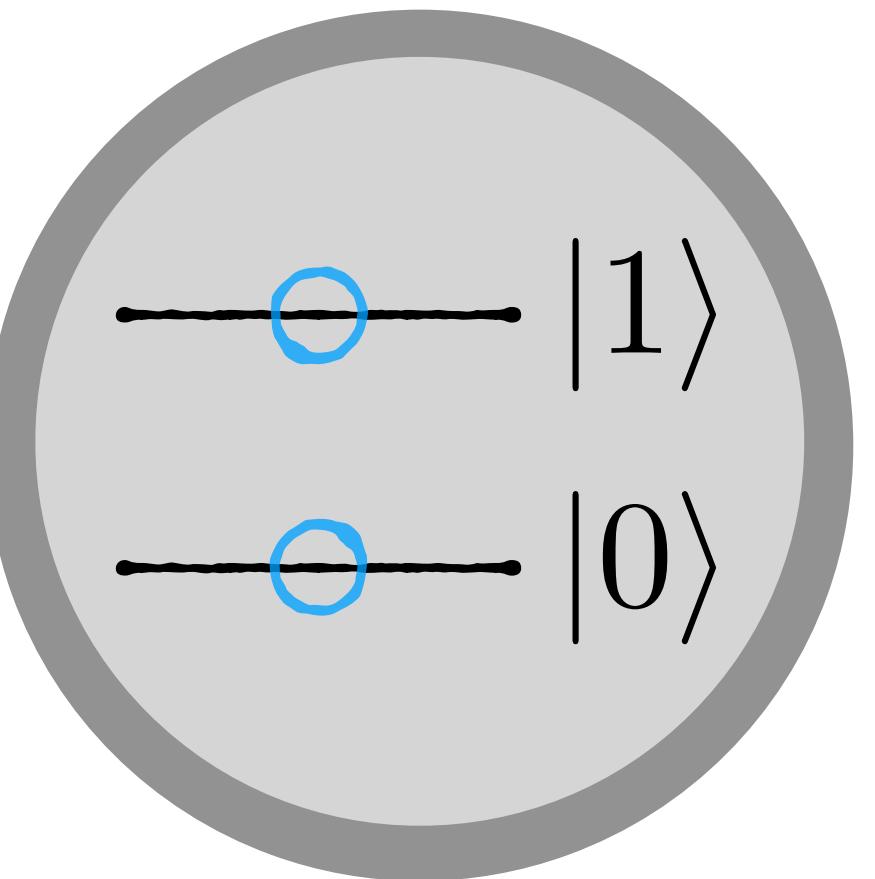


$|135^\circ\rangle$

Basis States

Basis states

$|0\rangle$ et $|1\rangle$



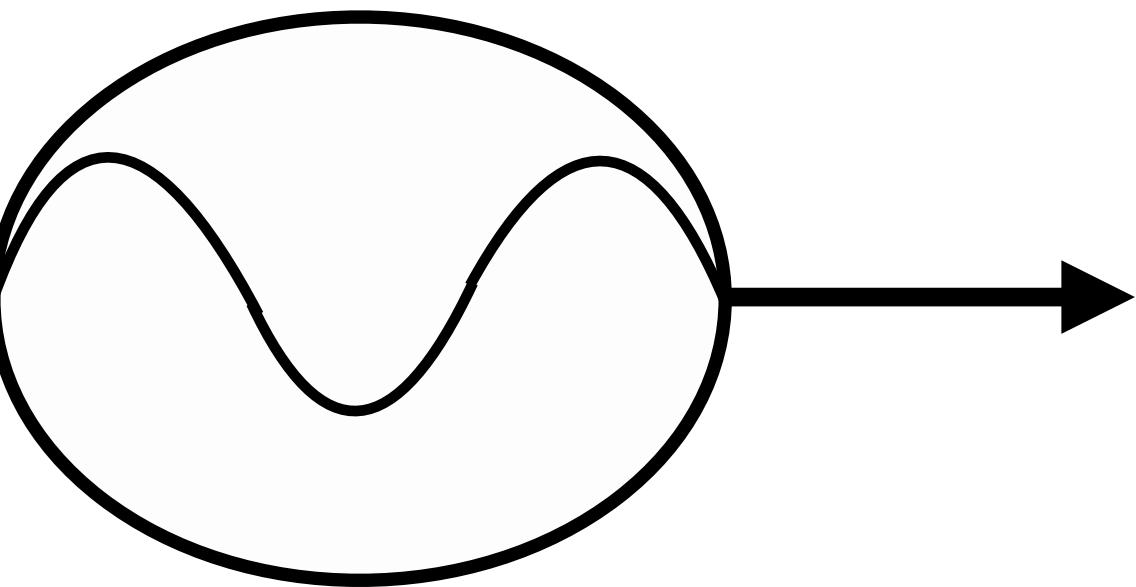
$$|\psi\rangle = \alpha|0\rangle + \beta|1\rangle$$

$$|\alpha|^2 + |\beta|^2 = 1$$

Basis States

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$|0\rangle$ et $|1\rangle$



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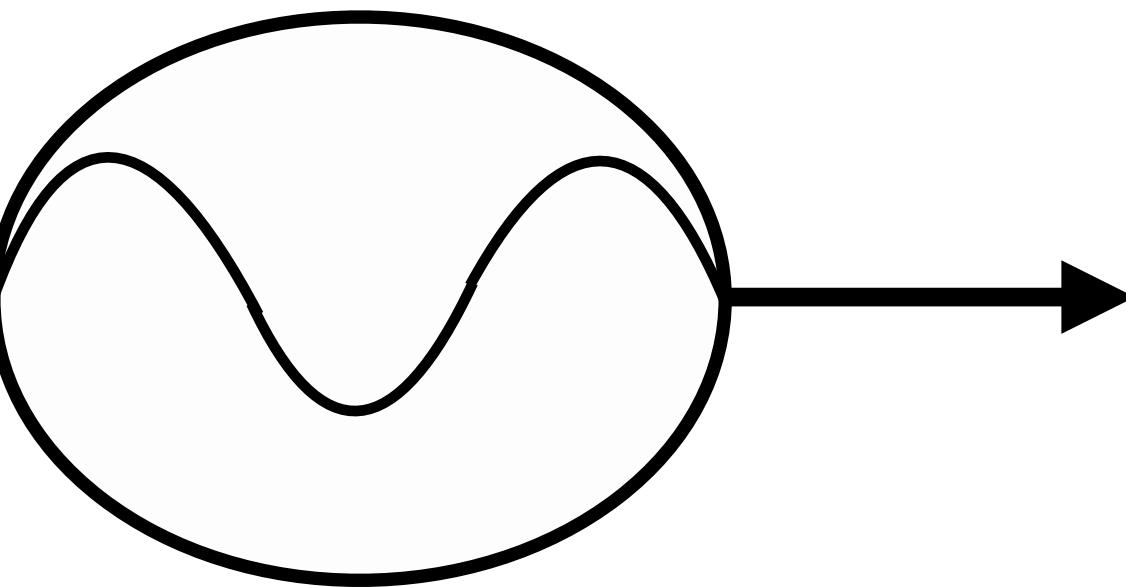
Basis States

Basis states

$|0\rangle$ et $|1\rangle$

$|90^\circ\rangle$ et $|0^\circ\rangle$

$$|\psi\rangle = \alpha|0\rangle + \beta|1\rangle$$



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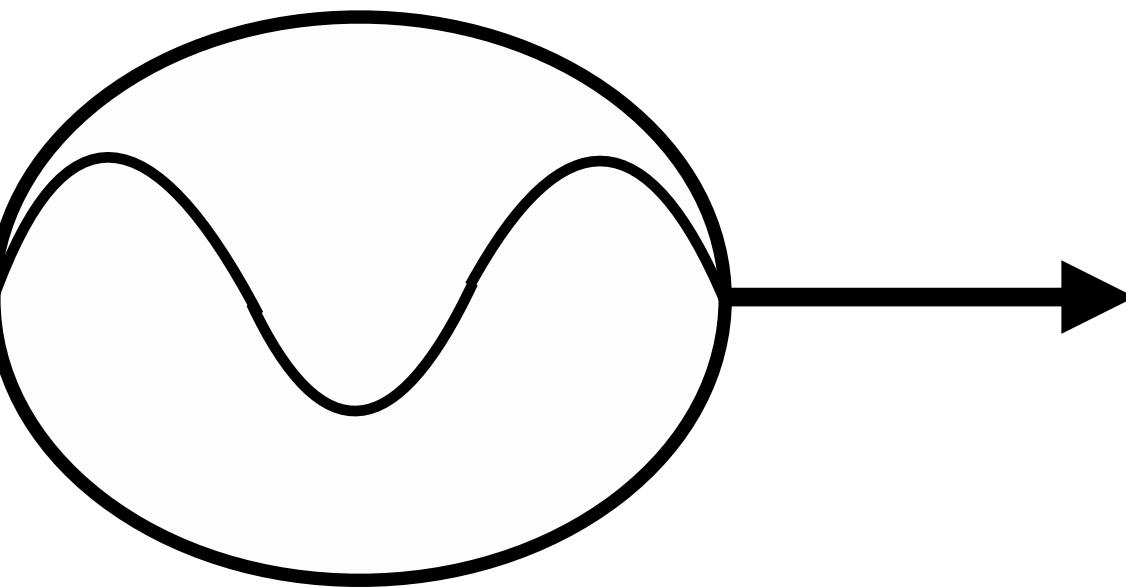
Basis States

Basis states

$|0\rangle$ et $|1\rangle$

$|90^\circ\rangle$ et $|0^\circ\rangle$

$$|\psi\rangle = \alpha|90^\circ\rangle + \beta|0^\circ\rangle$$



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Basis States

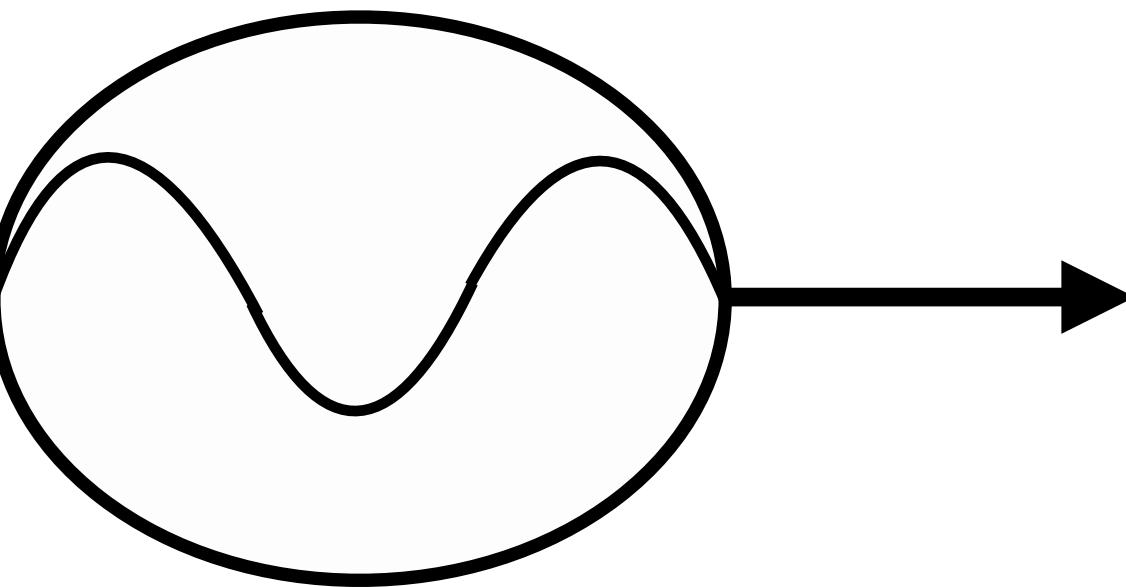
Basis states

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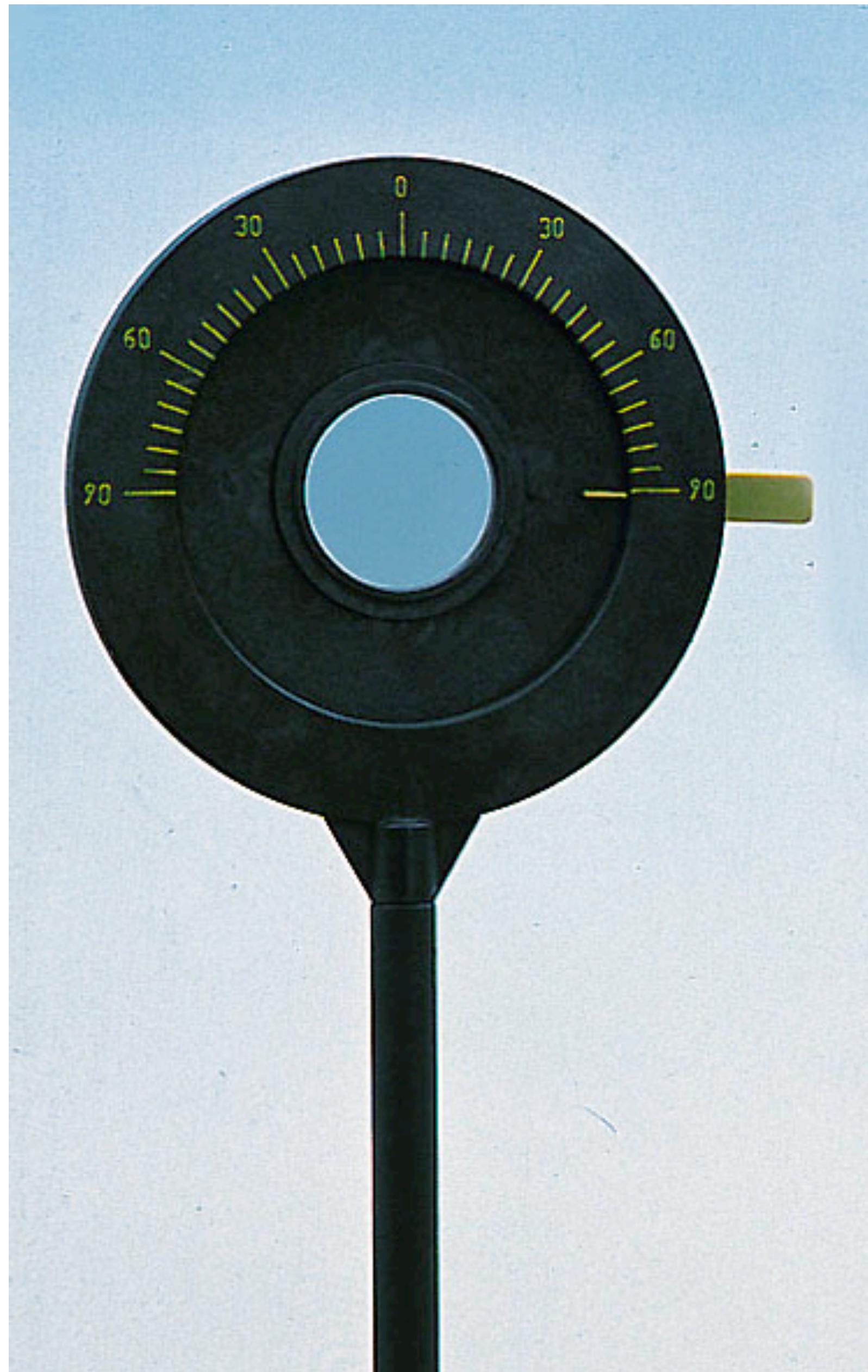
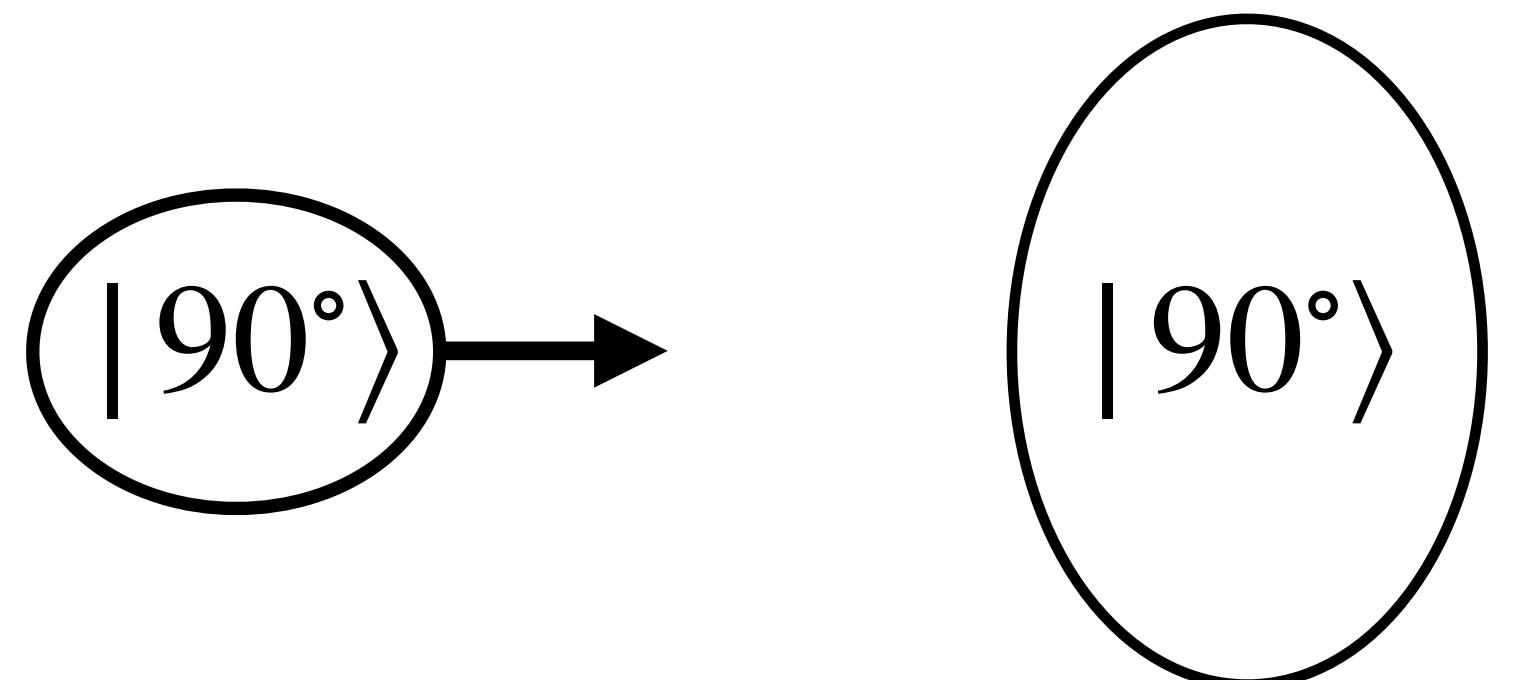
$|45^\circ\rangle$ et $|135^\circ\rangle$

$$|\psi\rangle = \alpha|45^\circ\rangle + \beta|135^\circ\rangle$$

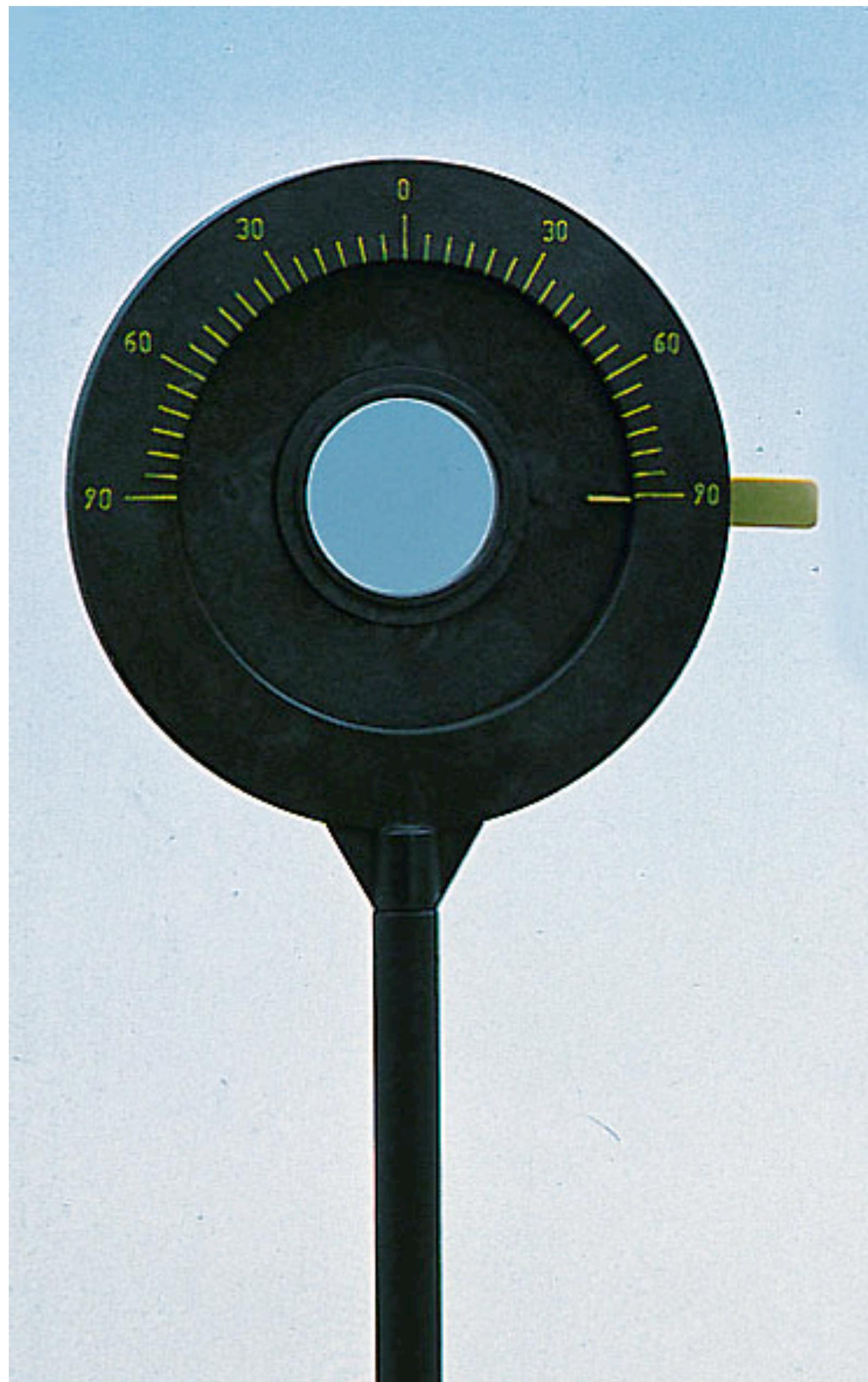
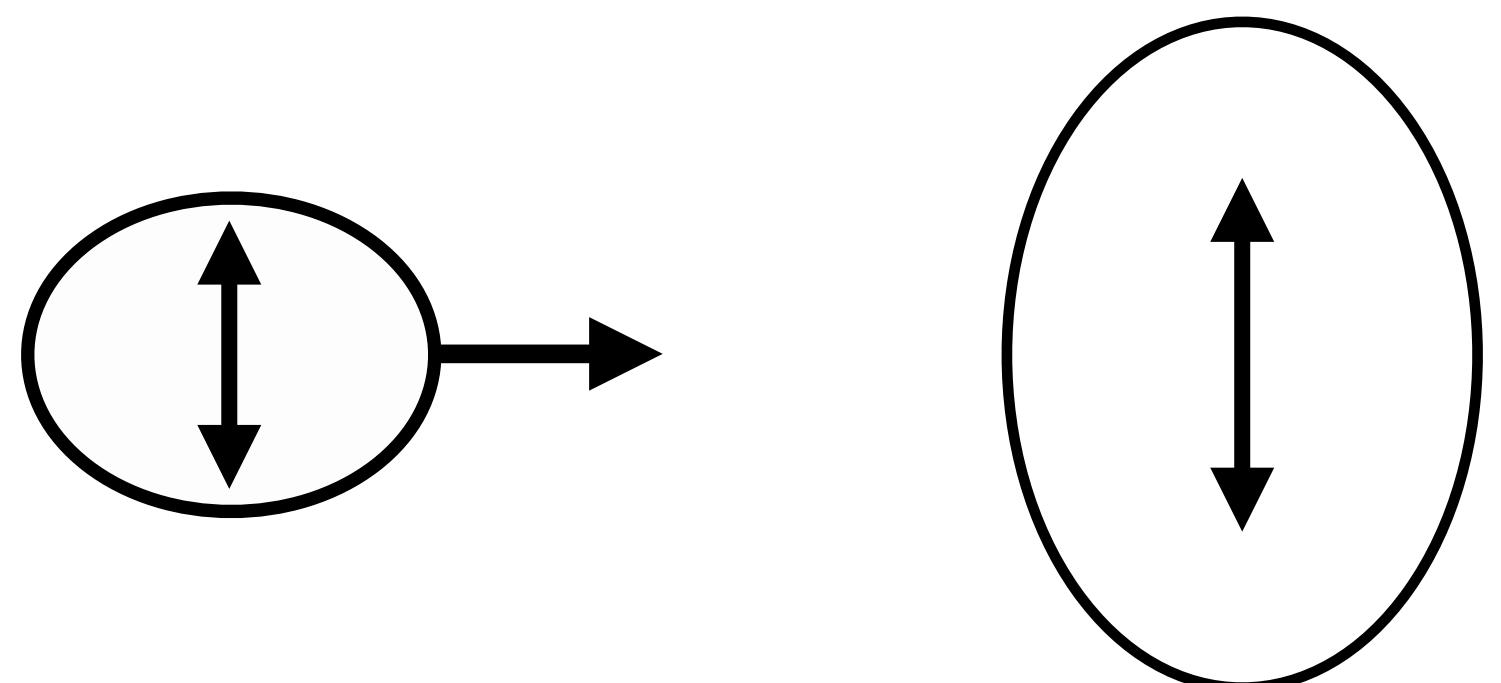


$$|\alpha|^2 + |\beta|^2 = 1$$

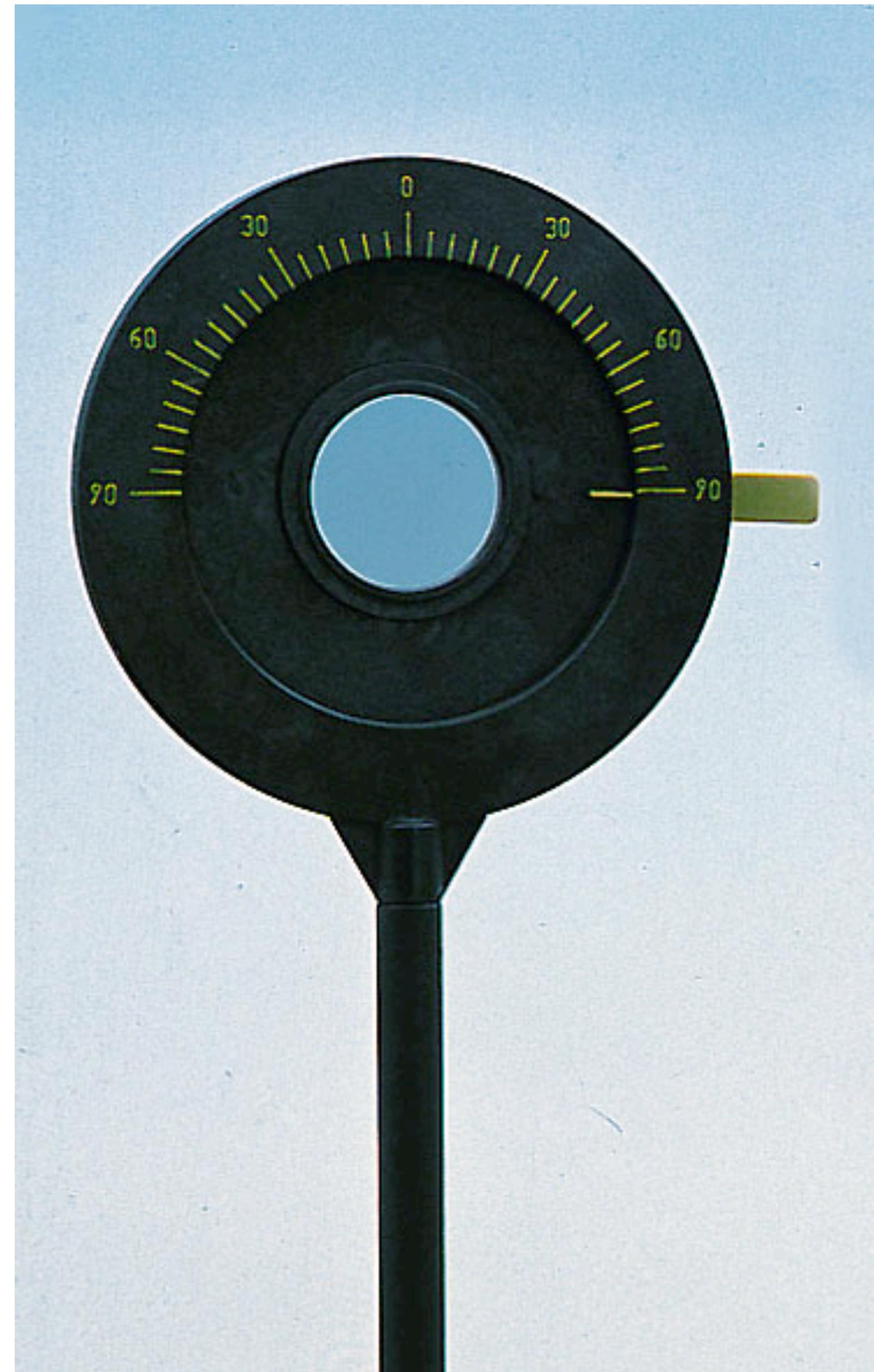
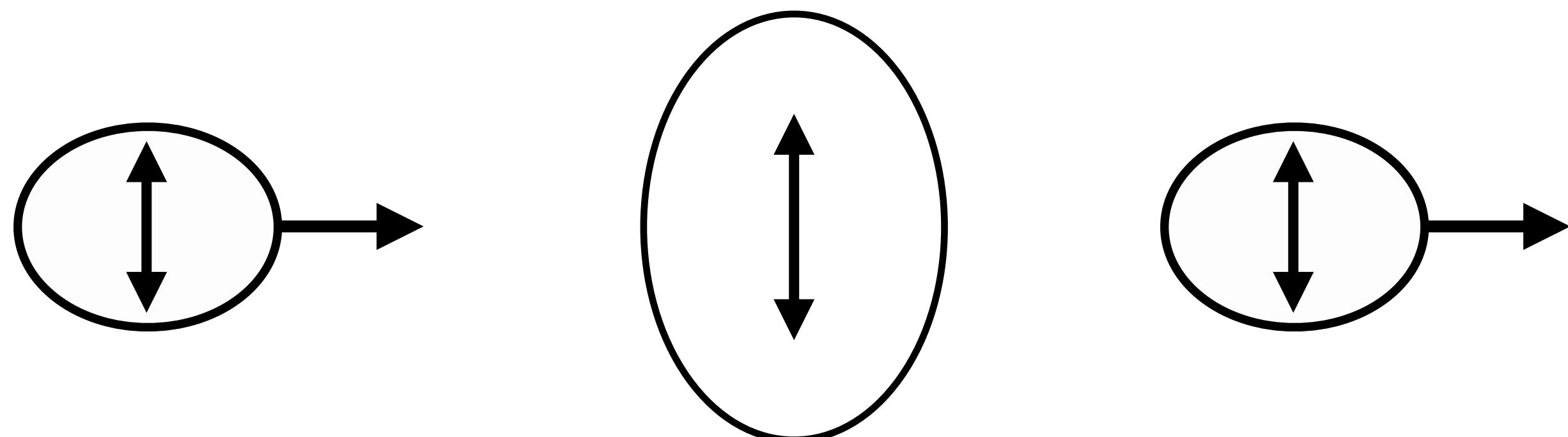
The Polarizer



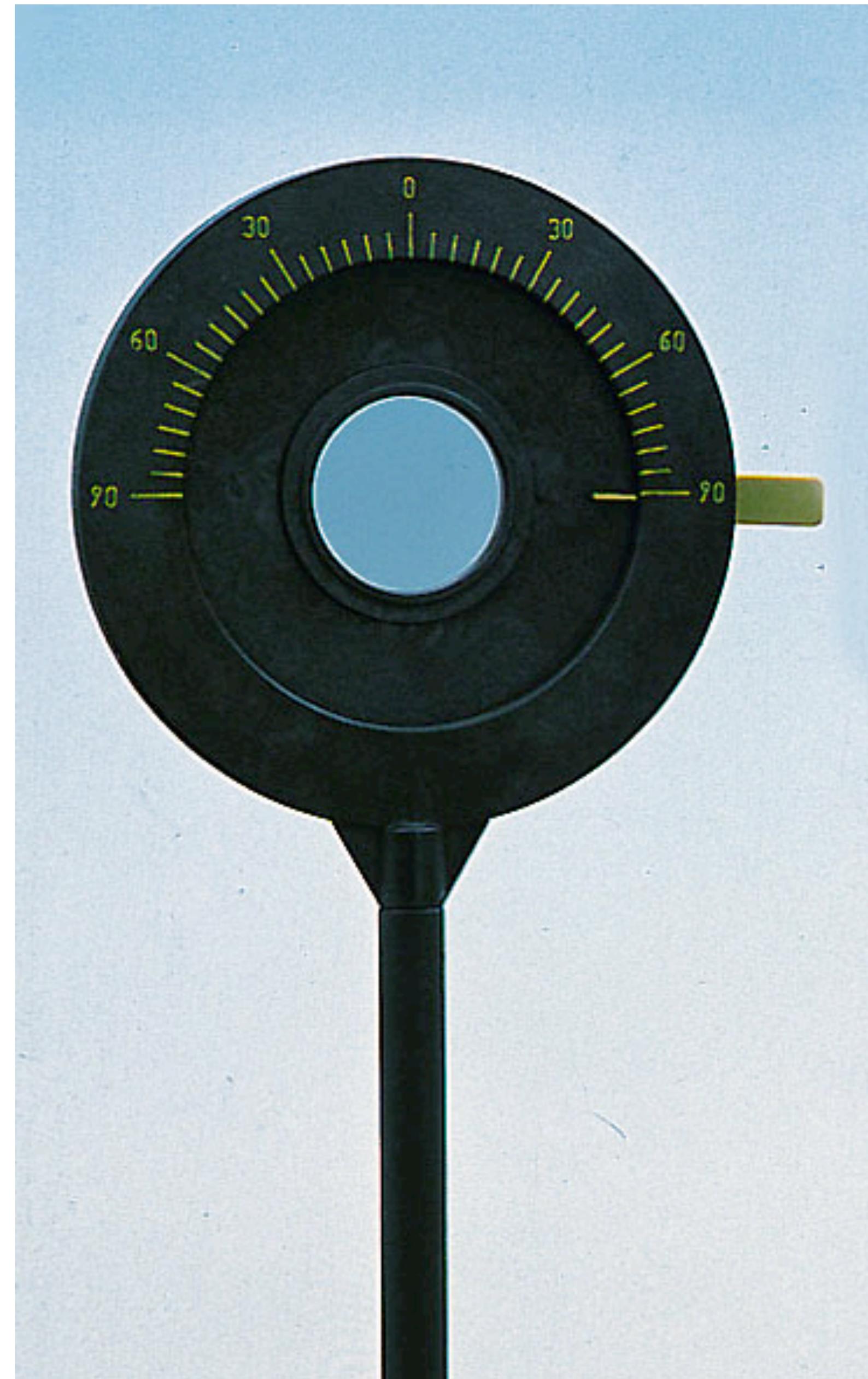
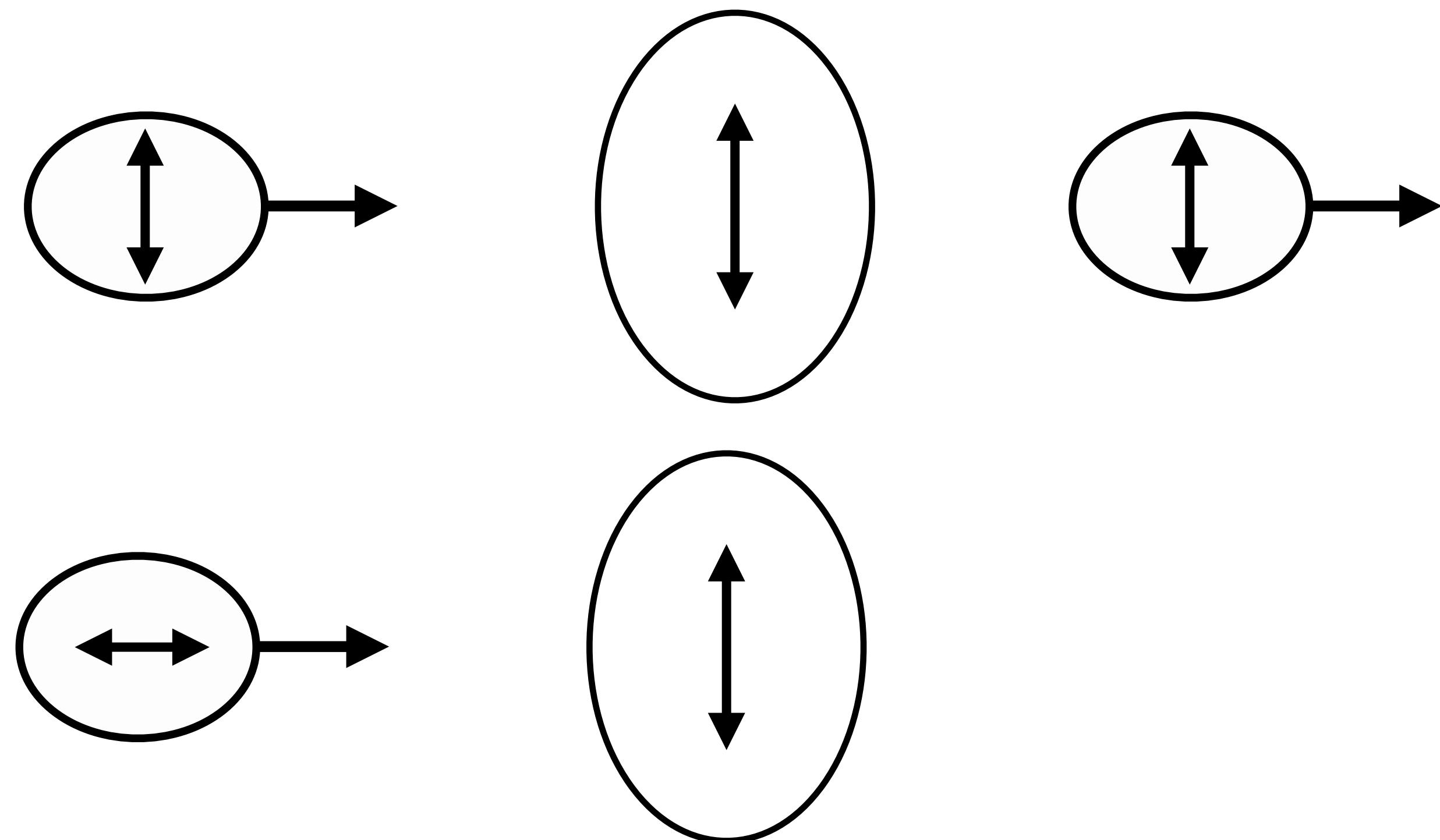
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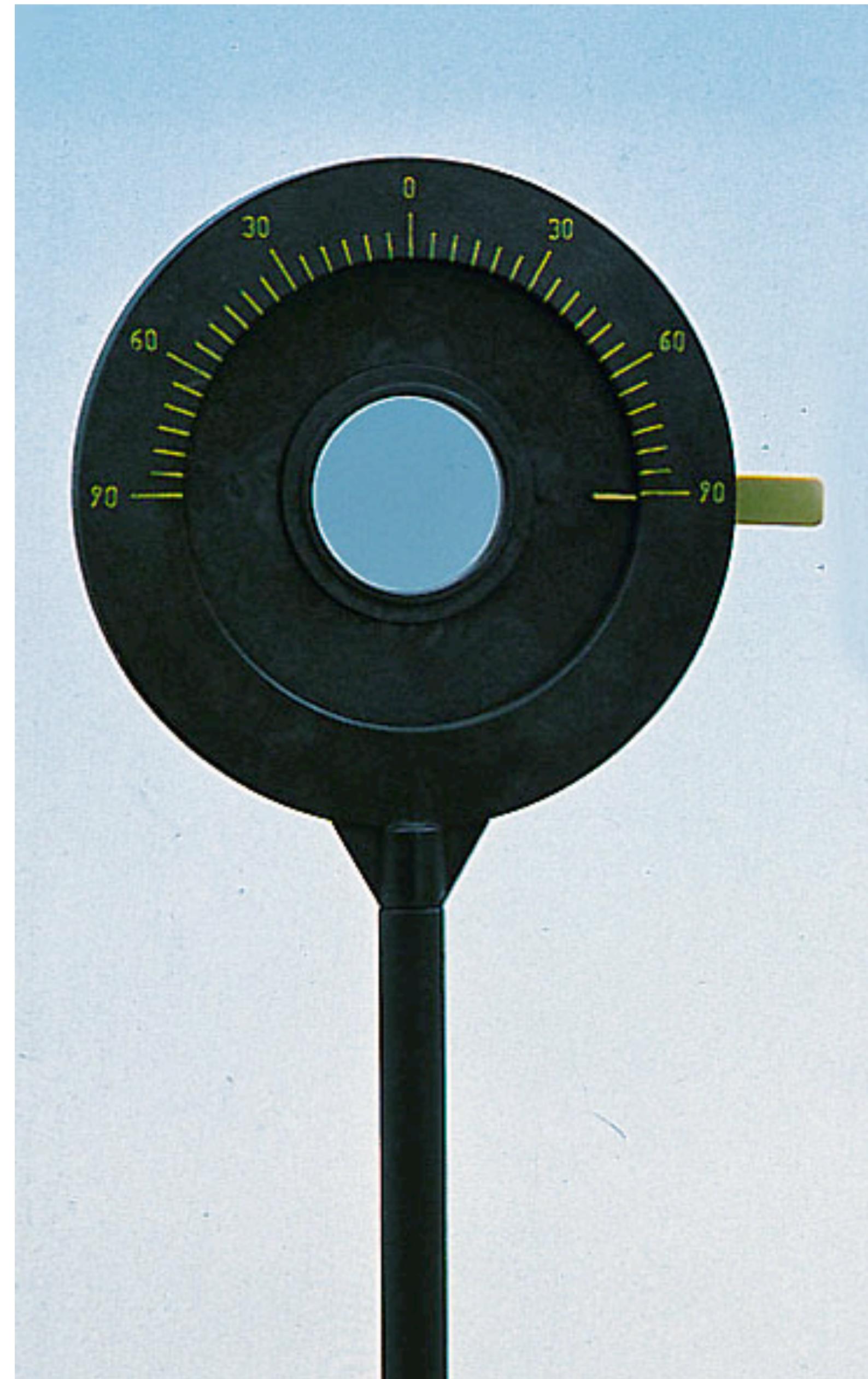
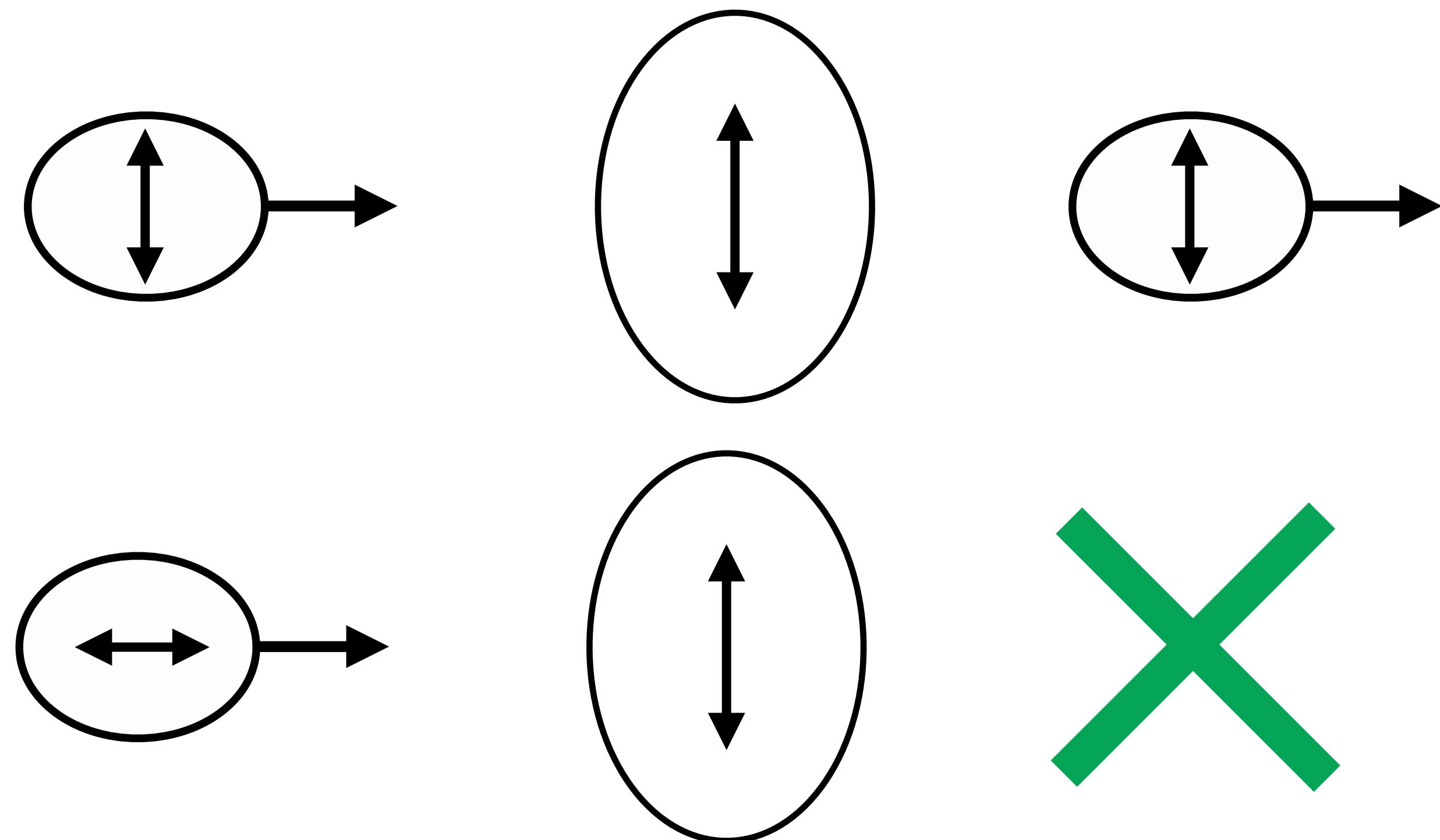
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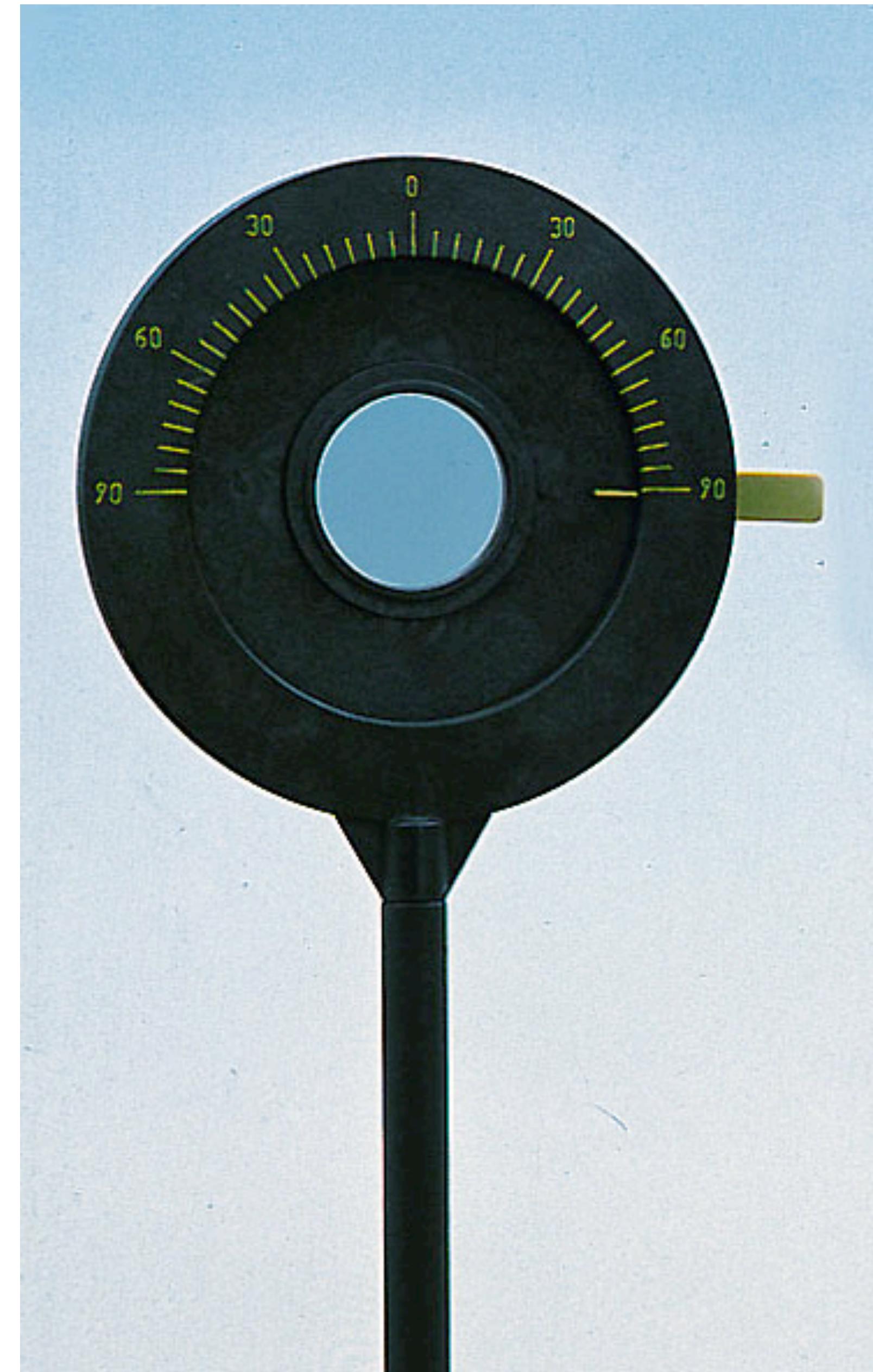
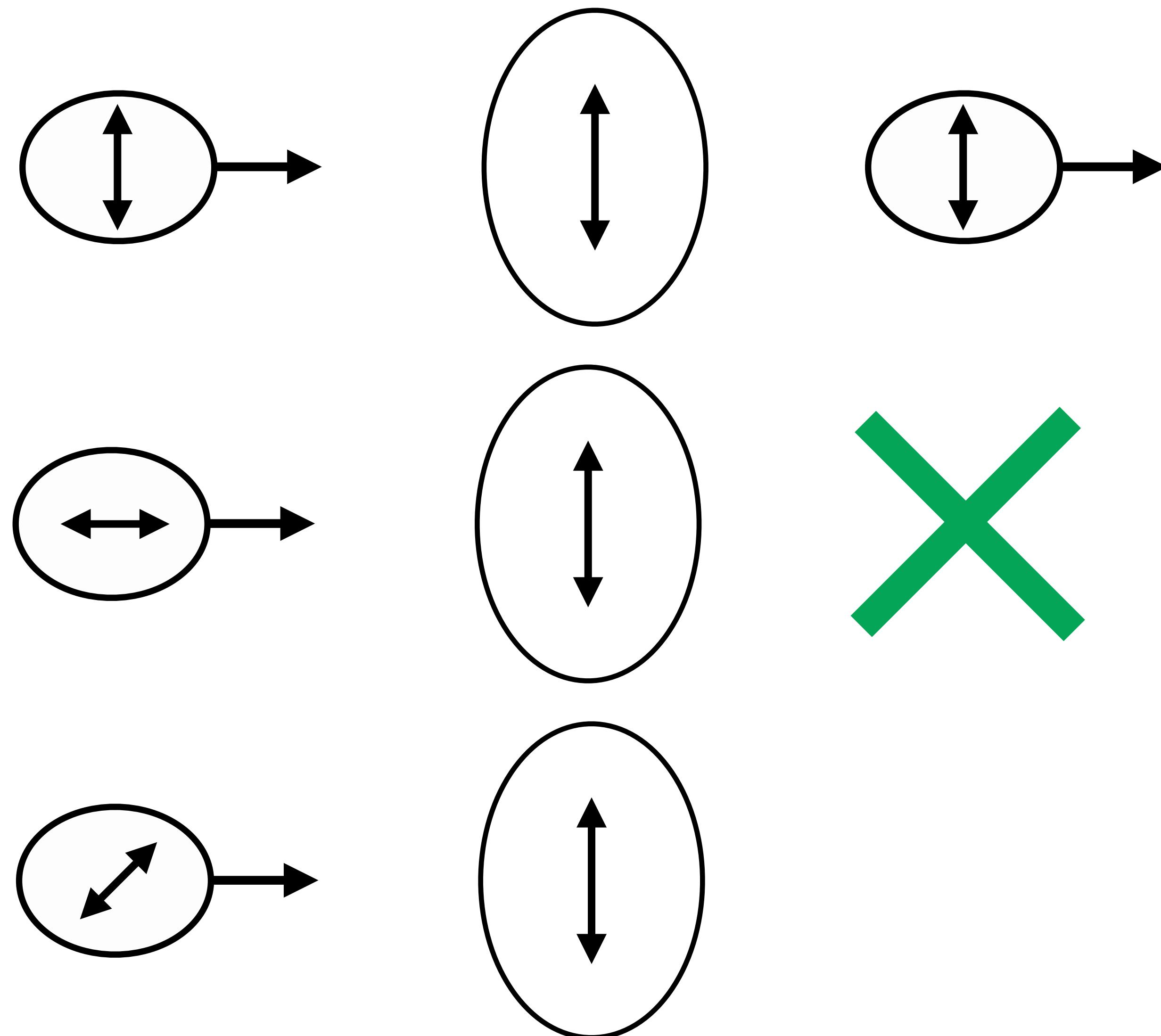
The Polarizer



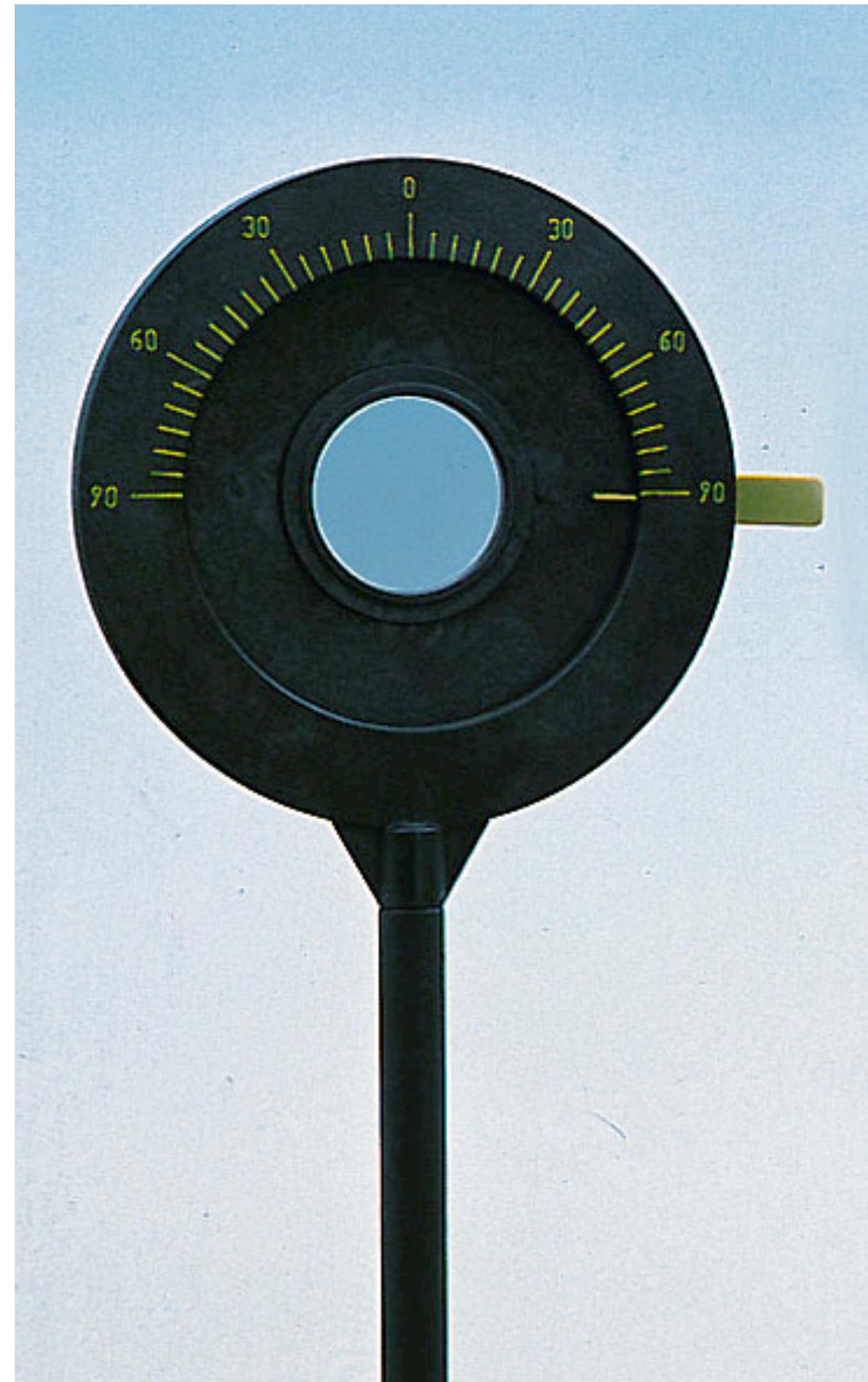
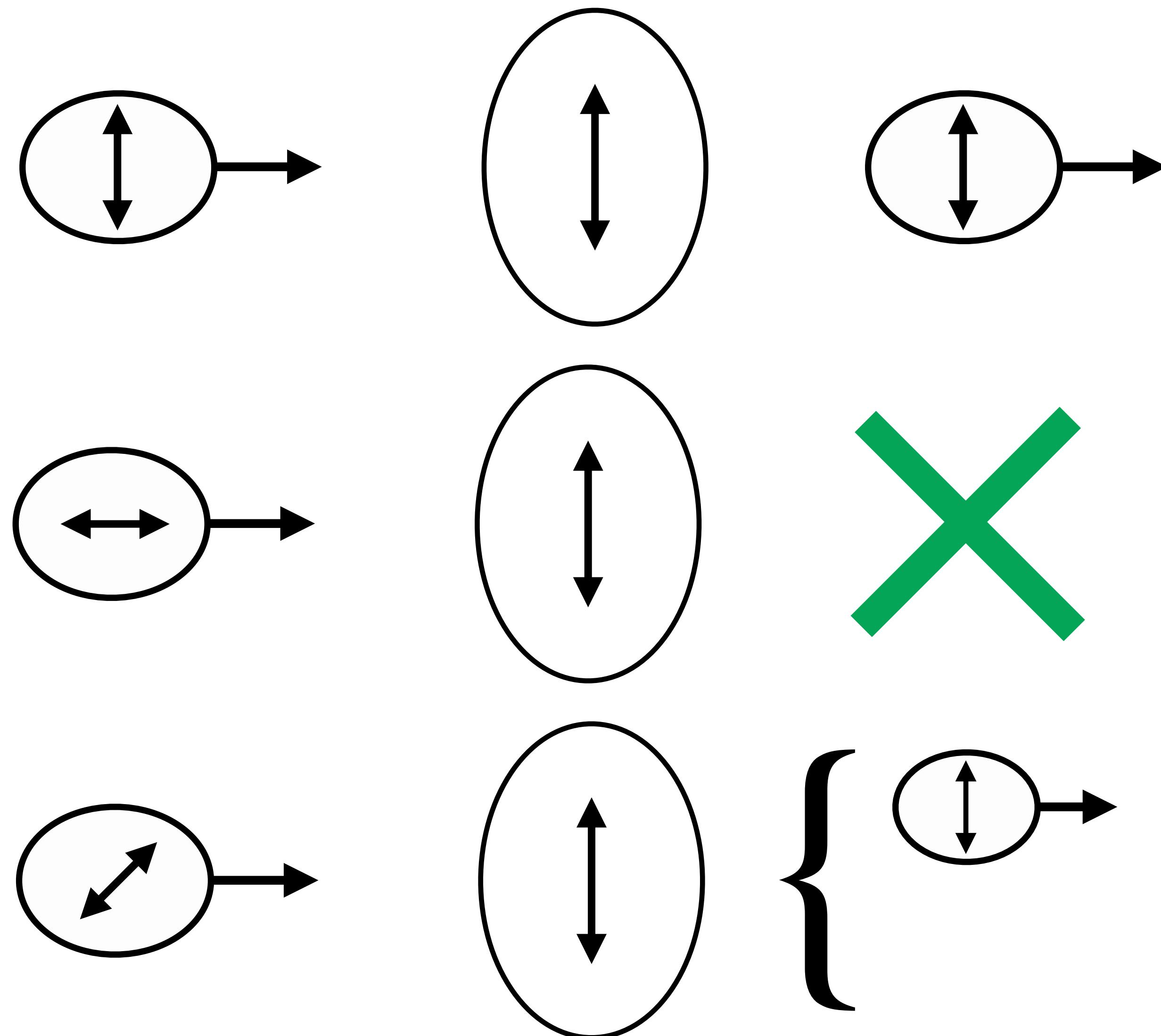
The Polarizer



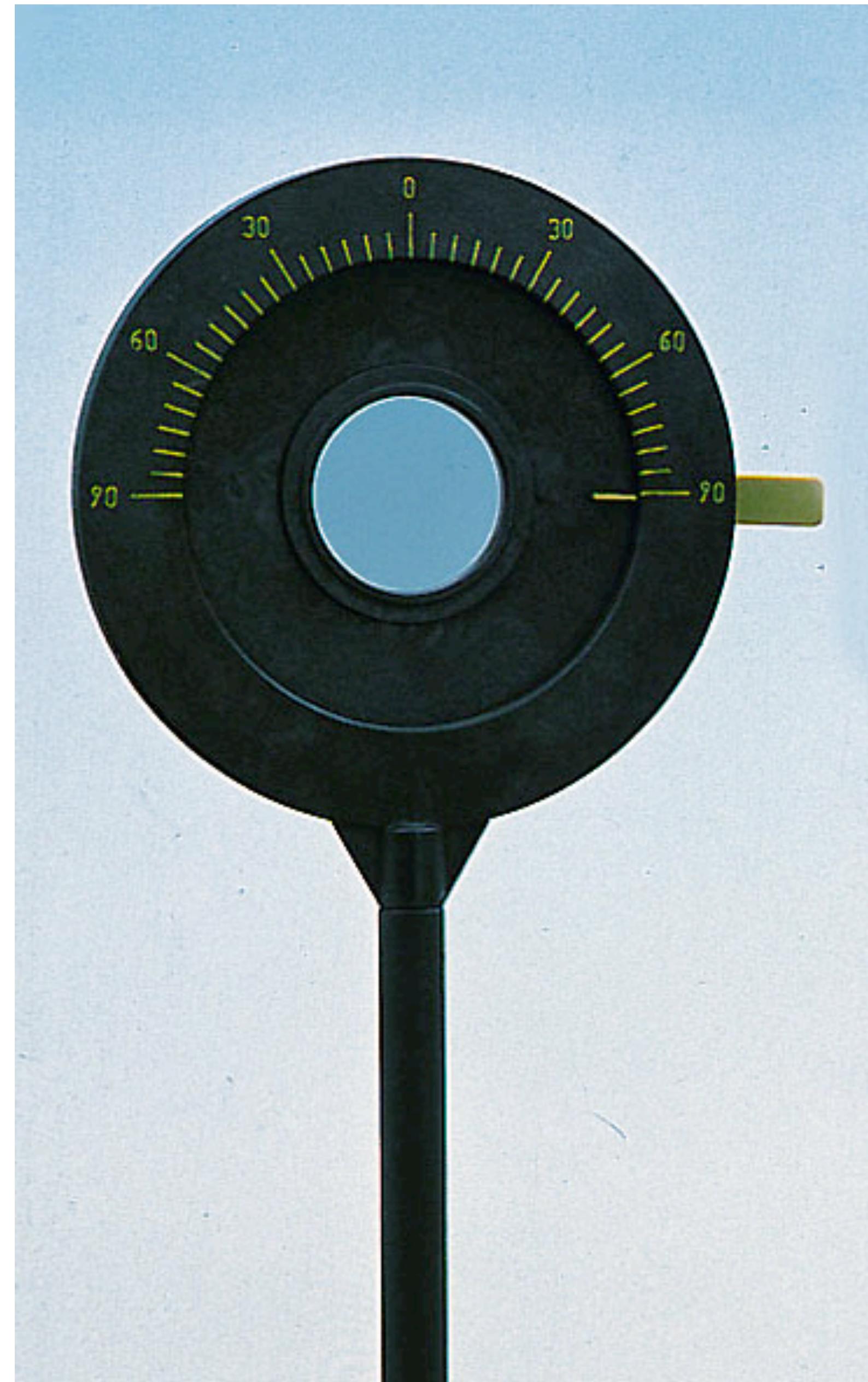
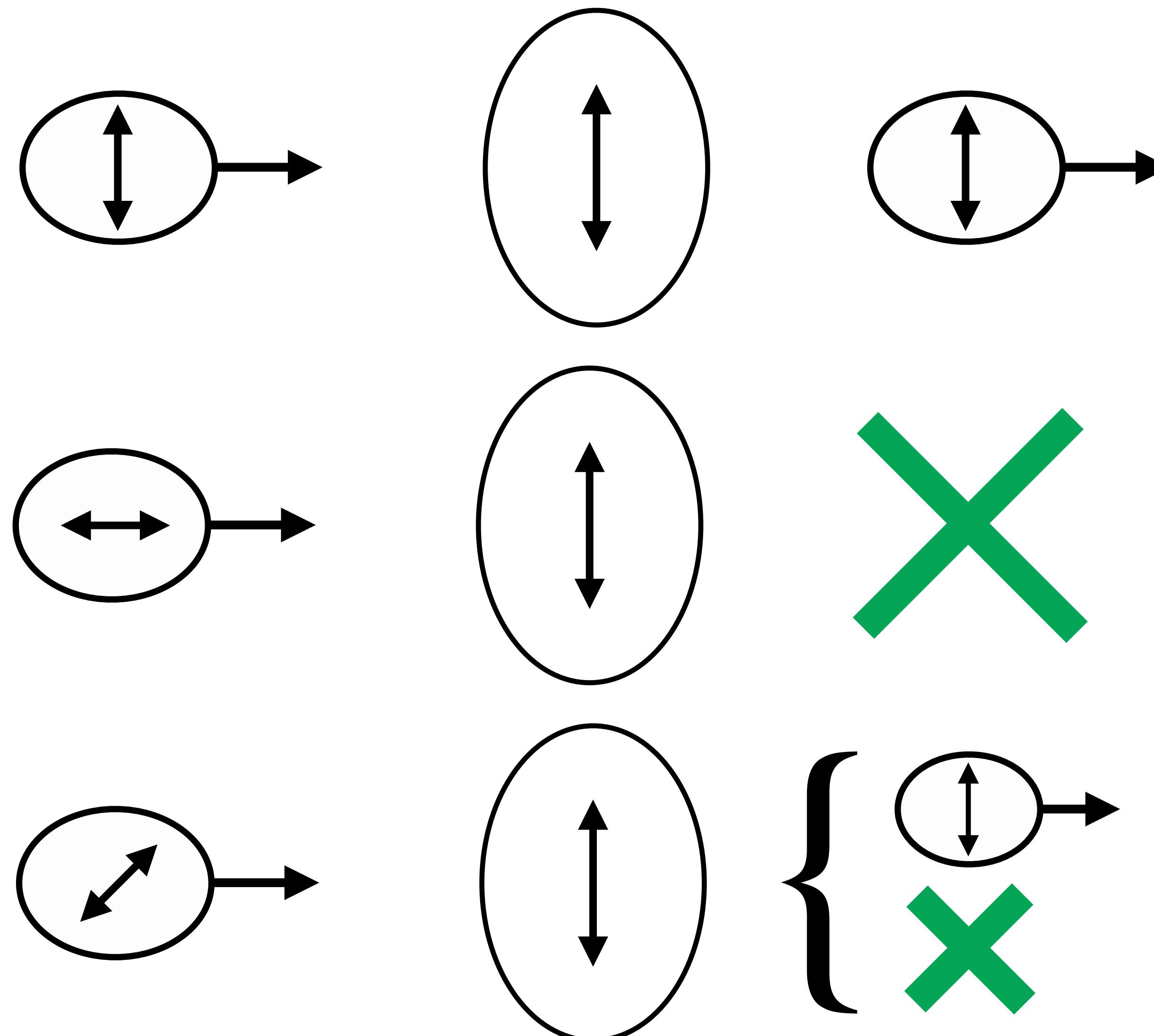
The Polarizer



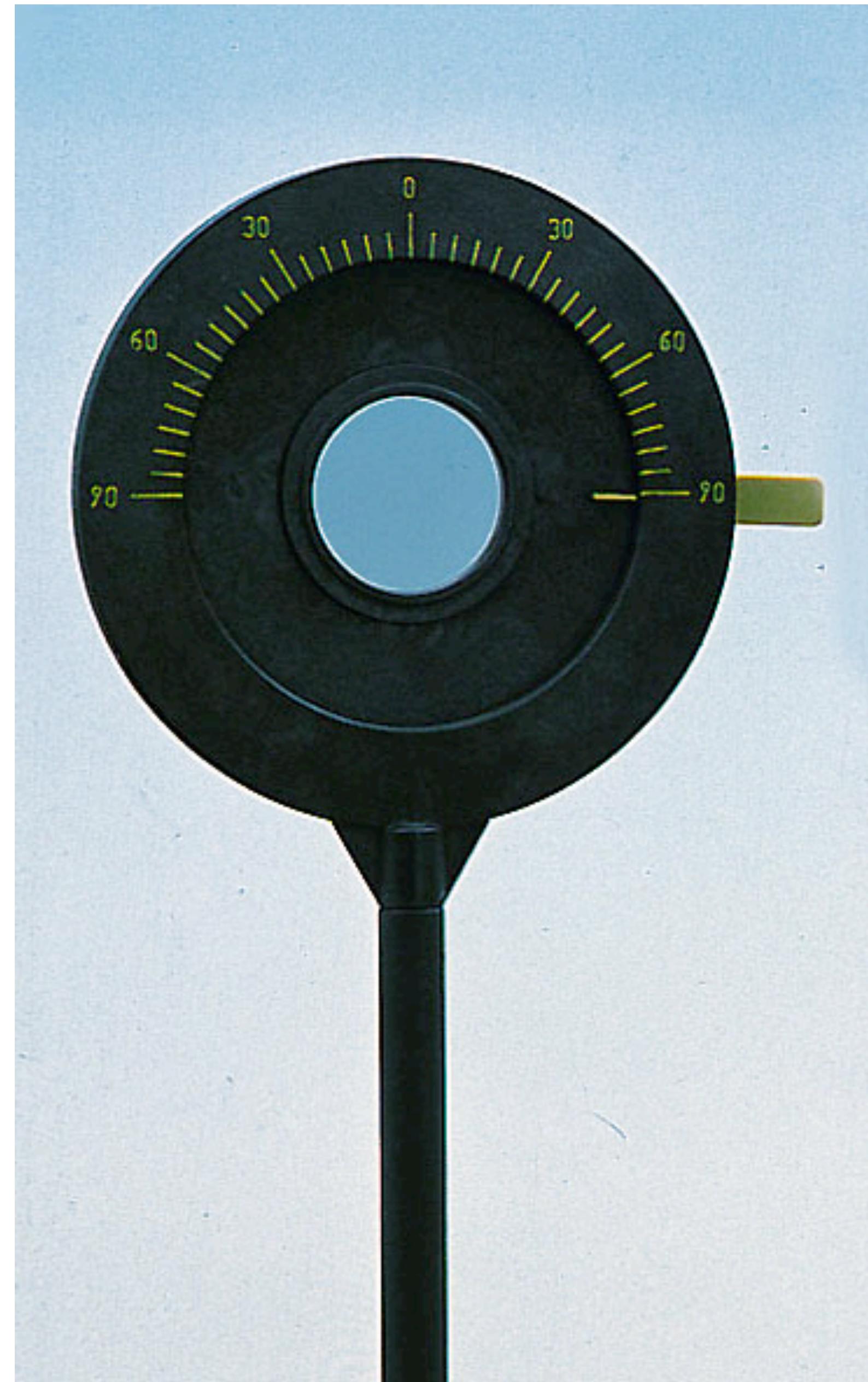
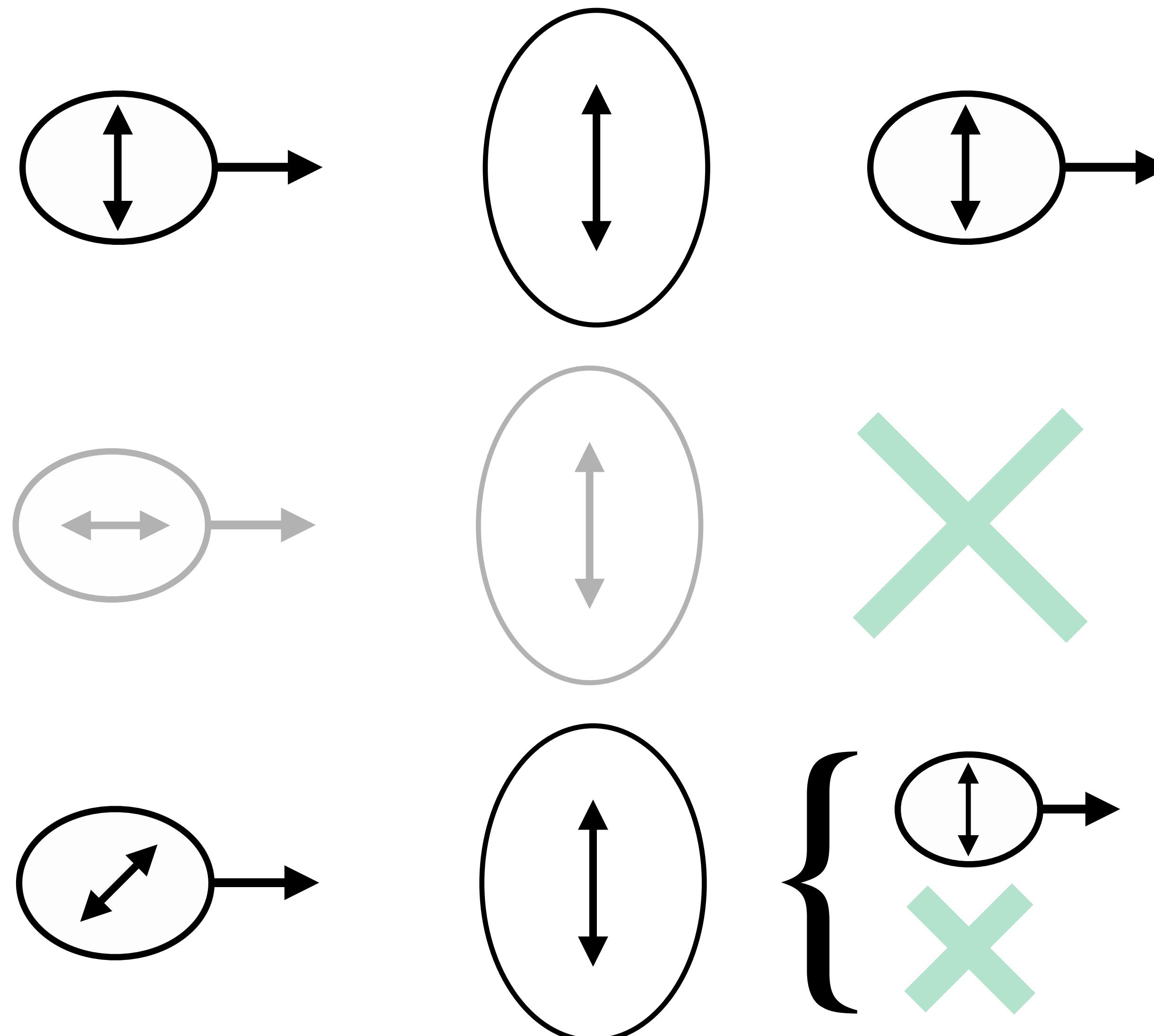
The Polarizer



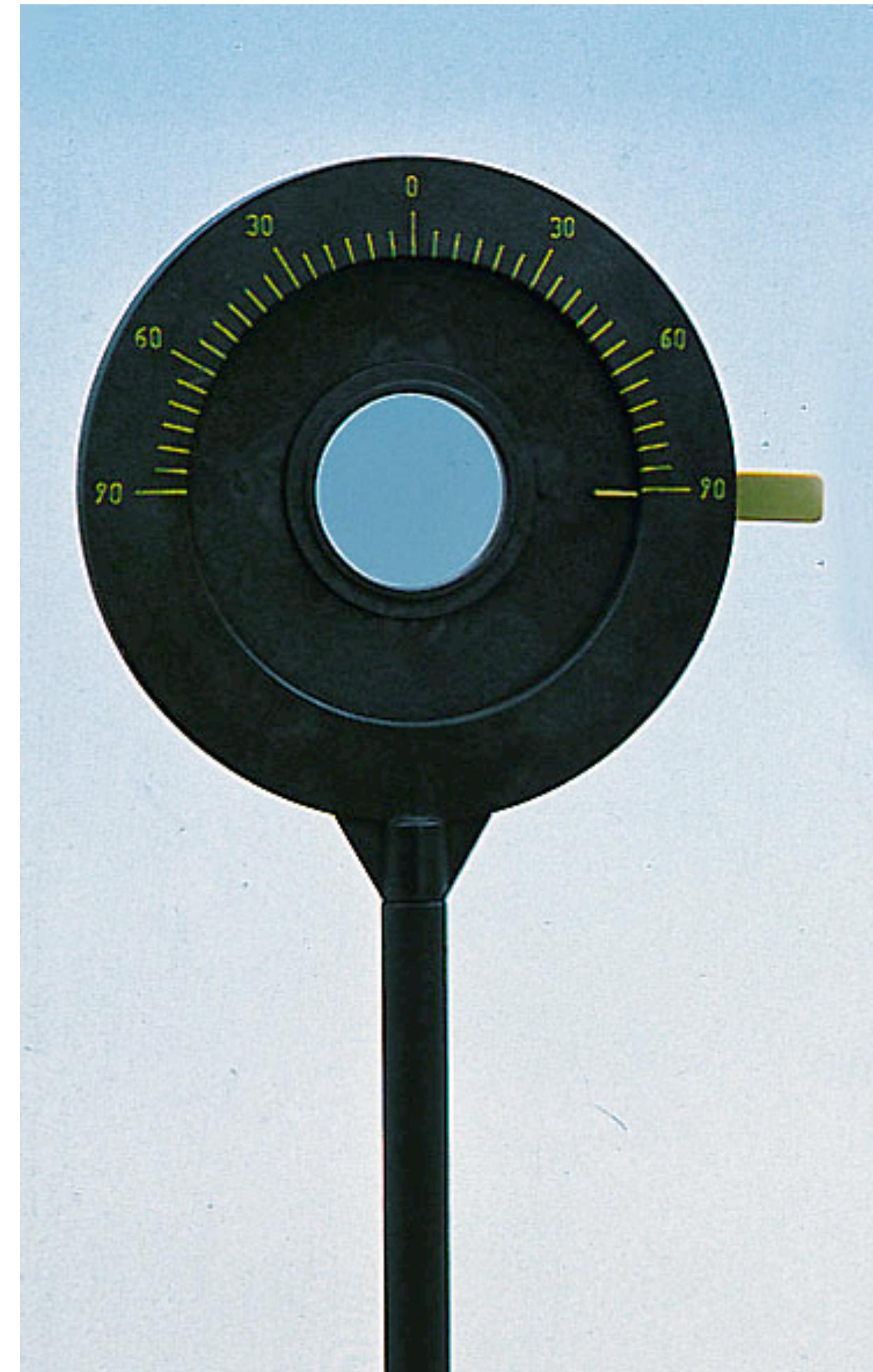
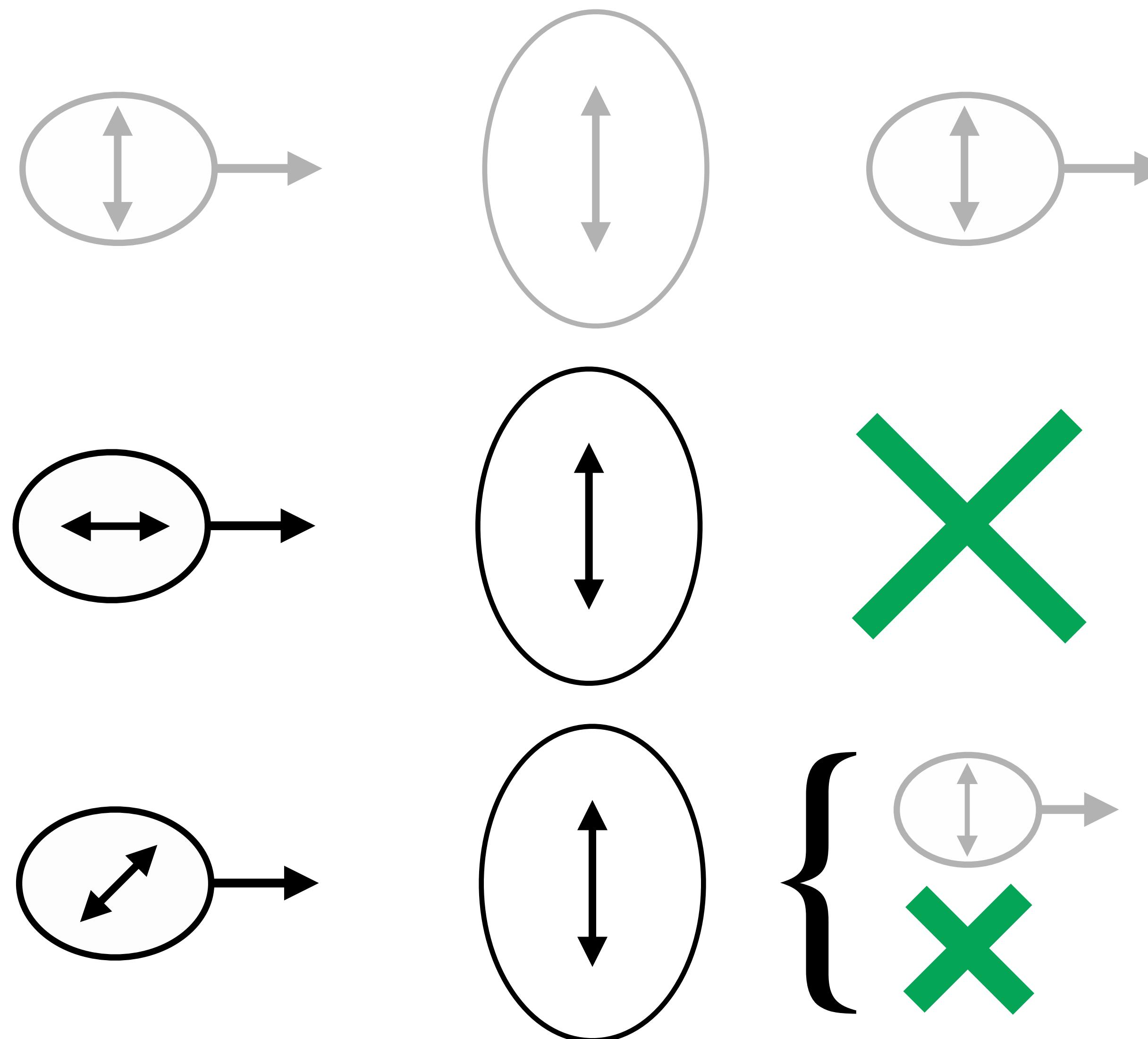
The Polarizer



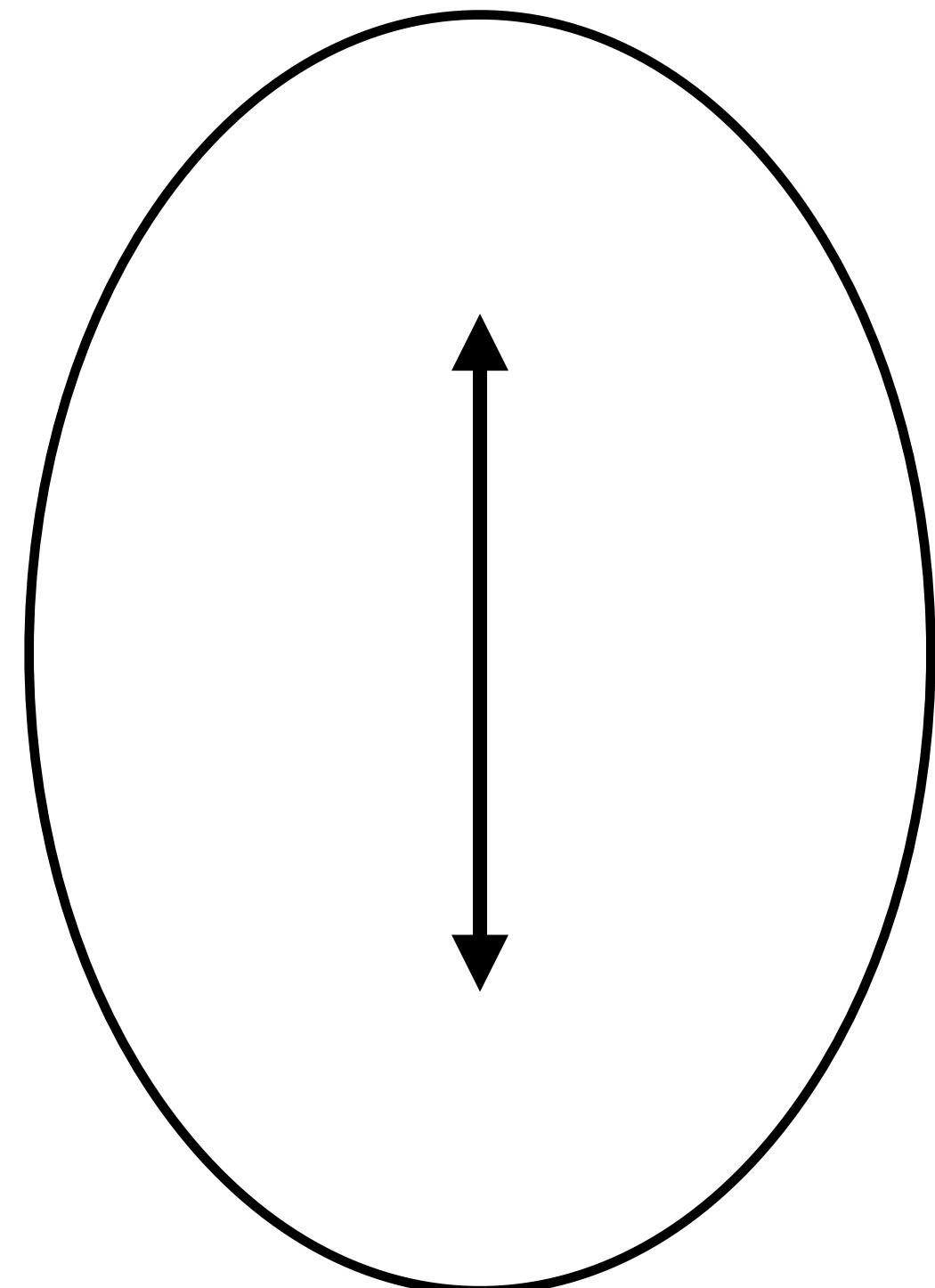
The Polarizer



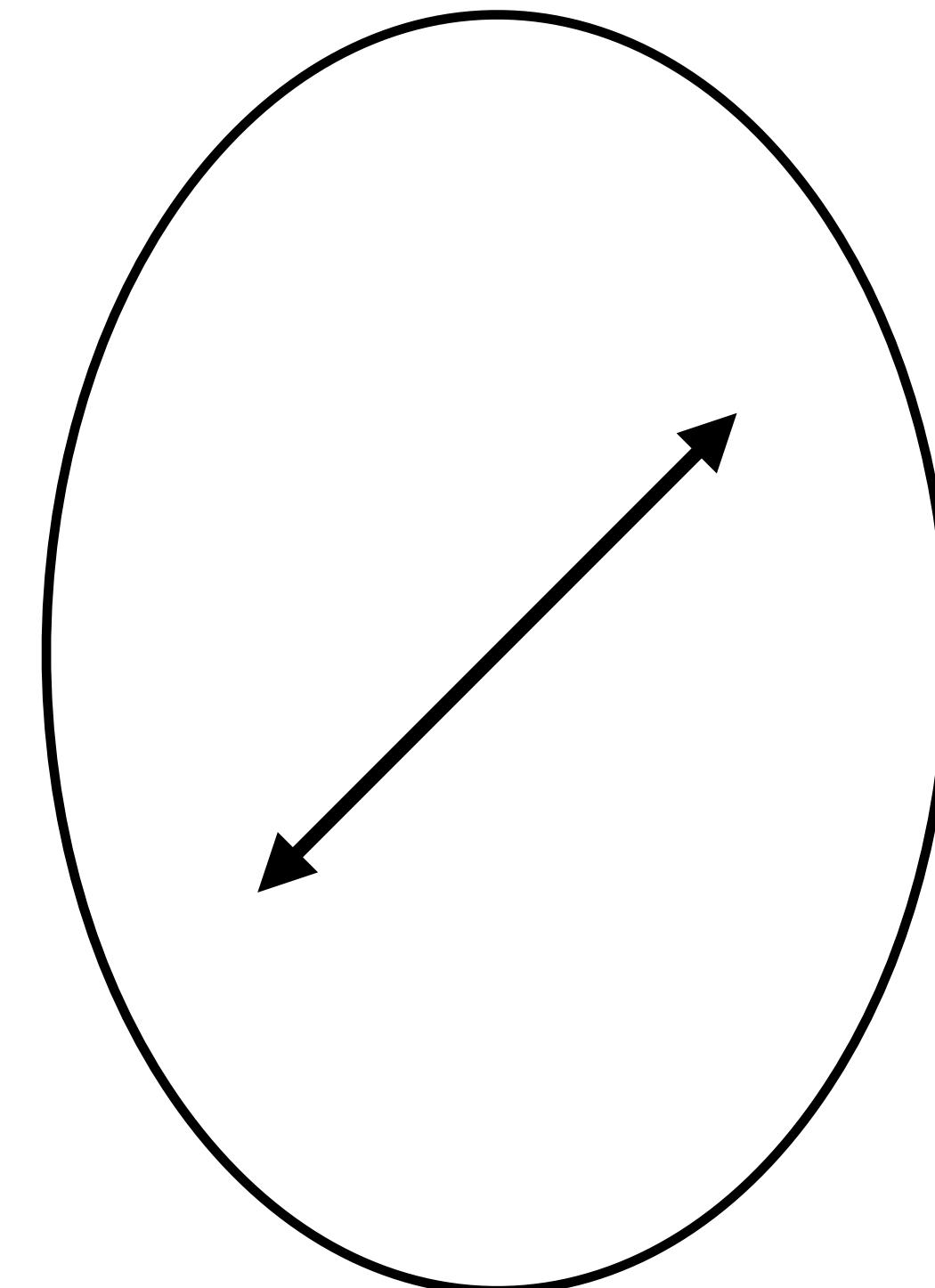
The Polarizer



Measurement Basis

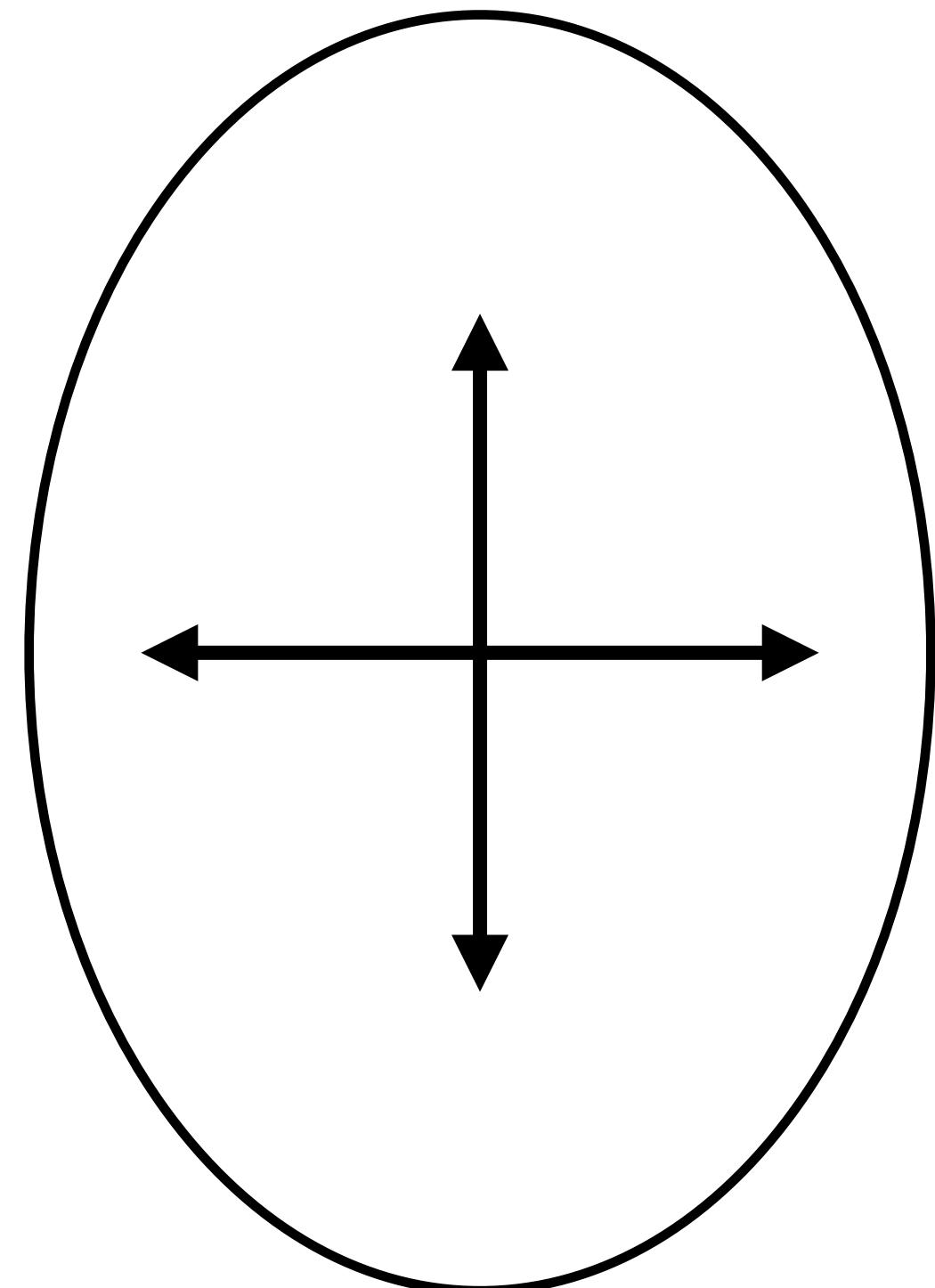


Vertical Basis

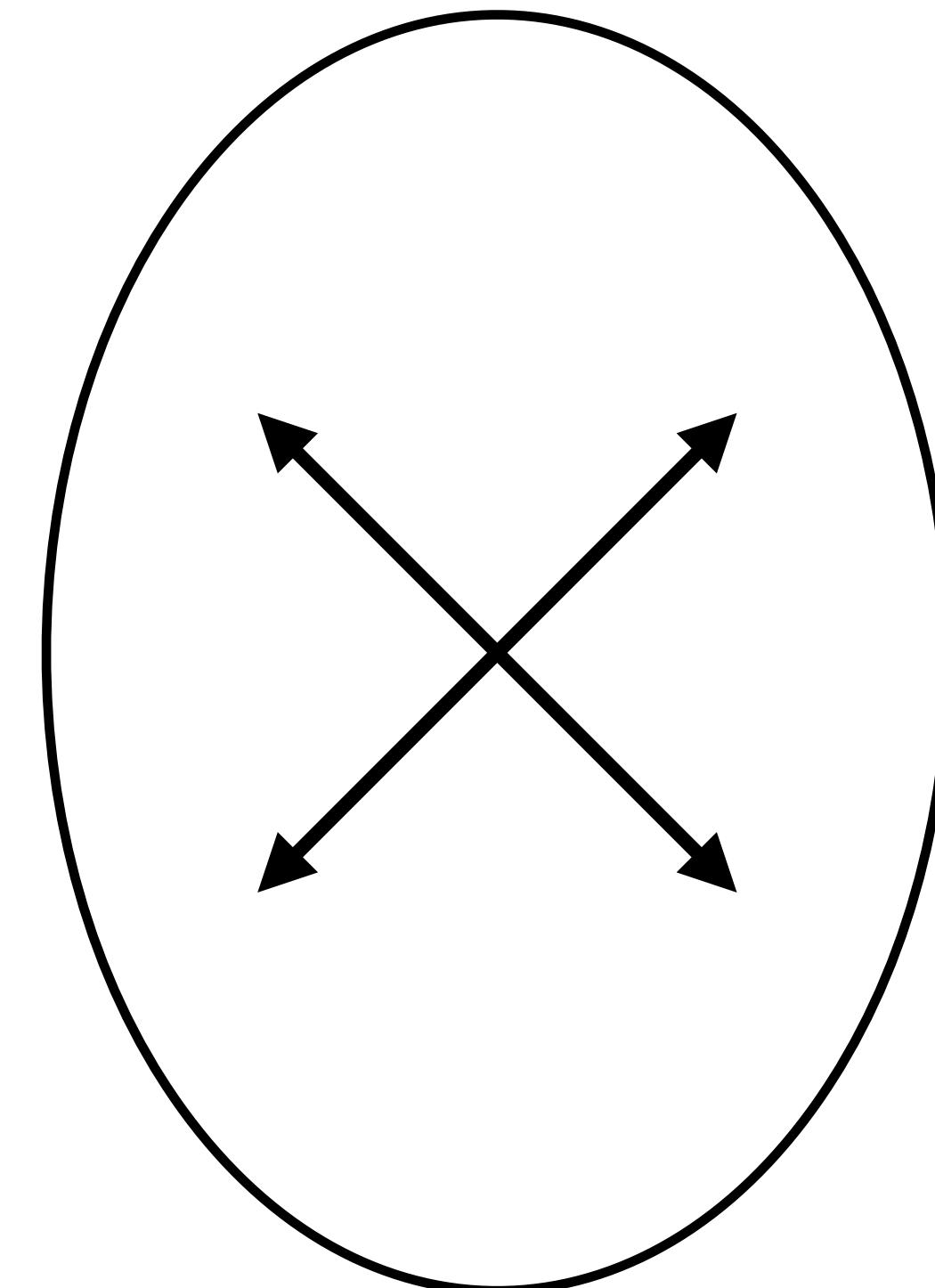


Diagonal Basis

Measurement Basis

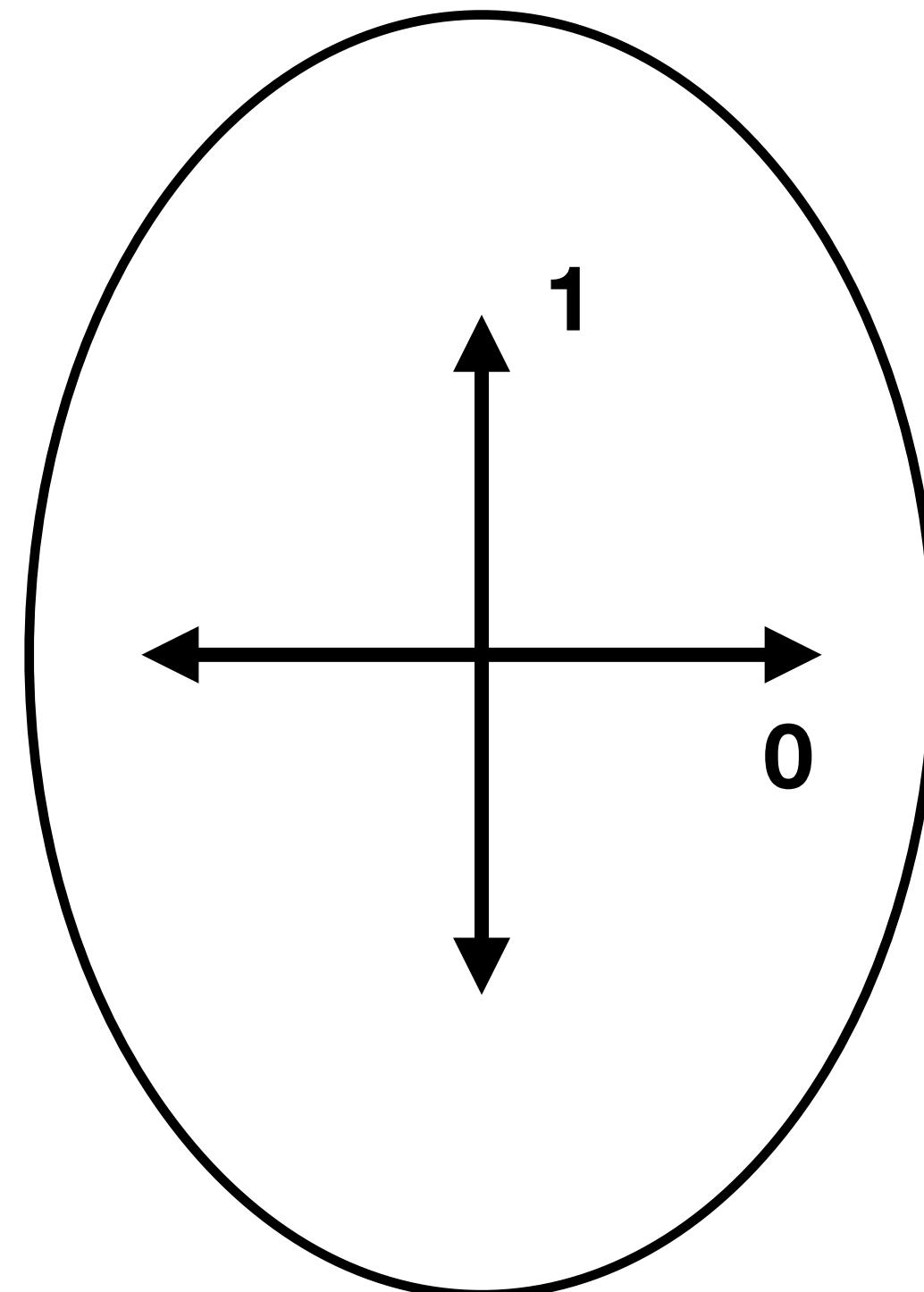


Vertical Basis

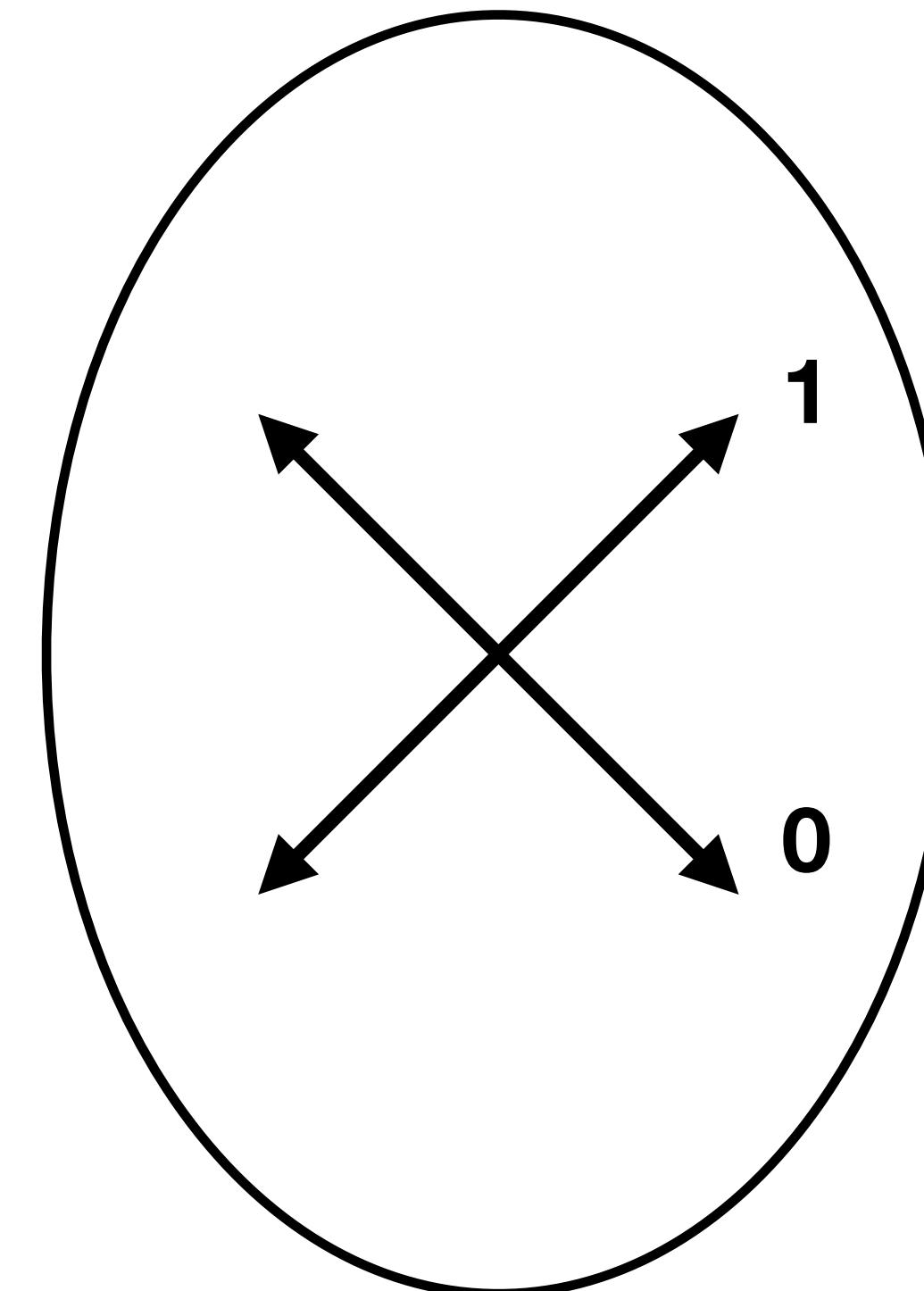


Diagonal Basis

Measurement Basis

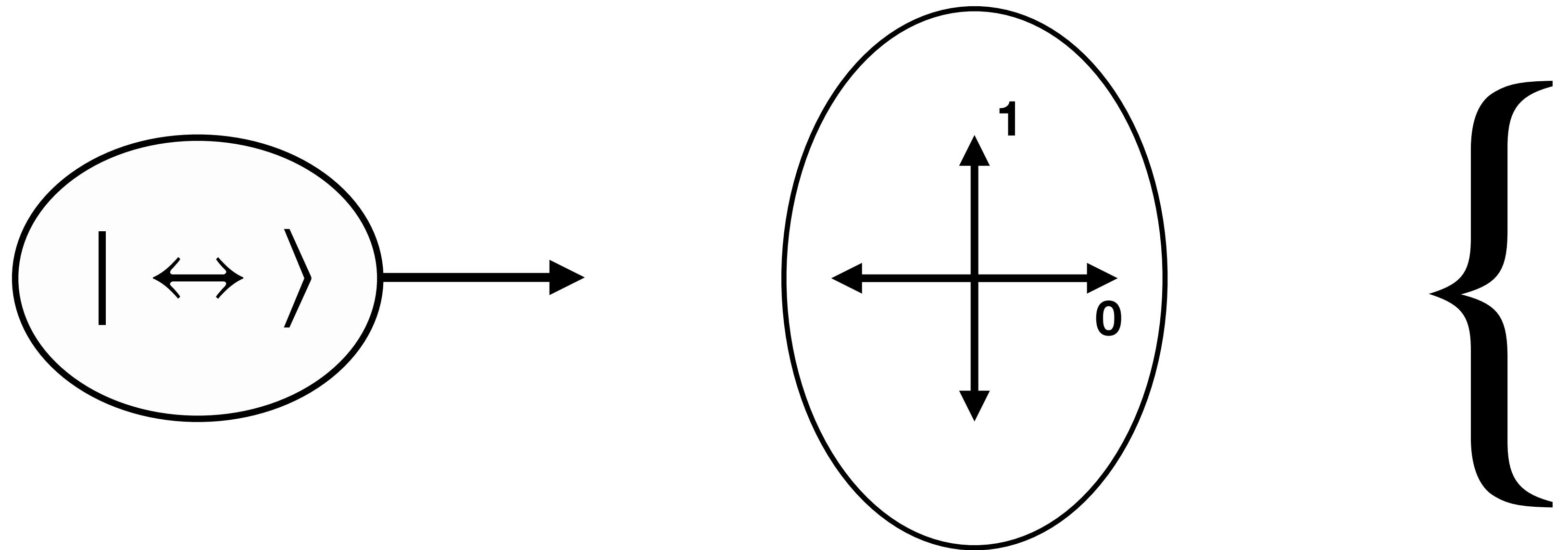


Vertical Basis



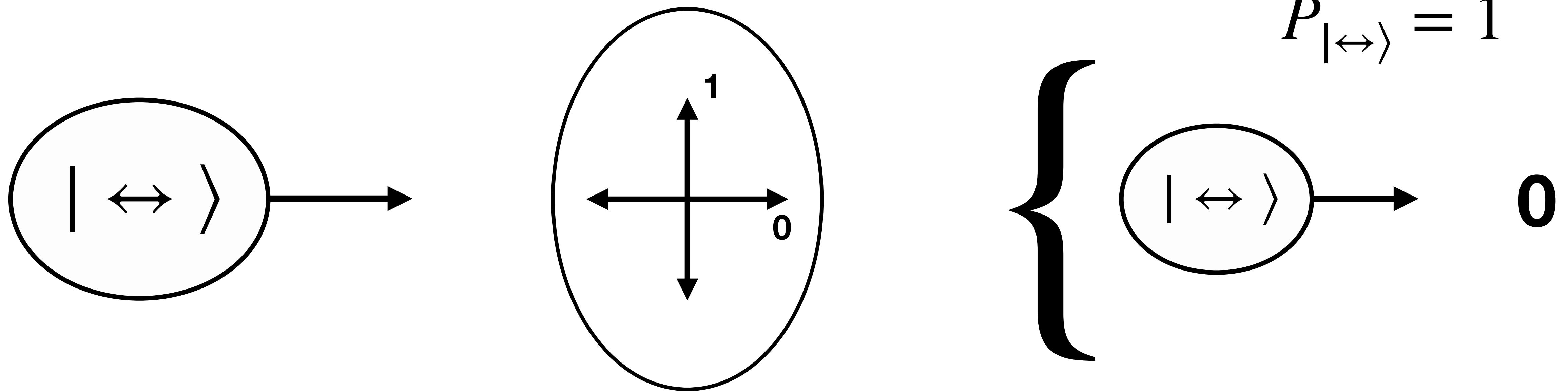
Diagonal Basis

Measurement



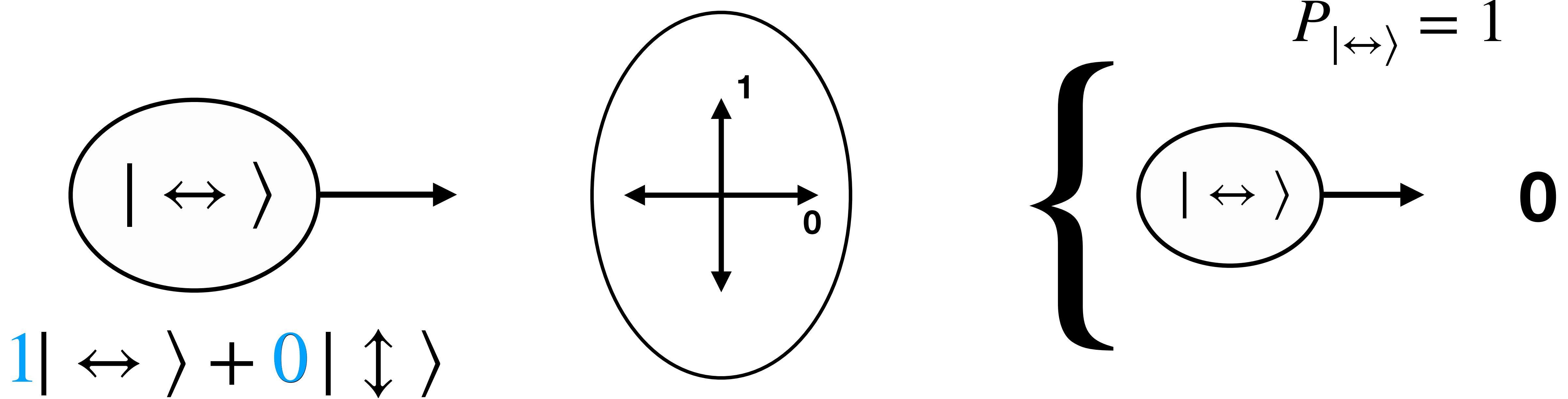
$$|90^\circ\rangle \equiv |\uparrow\downarrow\rangle$$
$$|0^\circ\rangle \equiv |\leftrightarrow\rangle$$

Measurement



$$|90^\circ\rangle \equiv | \uparrow \rangle$$
$$|0^\circ\rangle \equiv | \leftrightarrow \rangle$$

Measurement

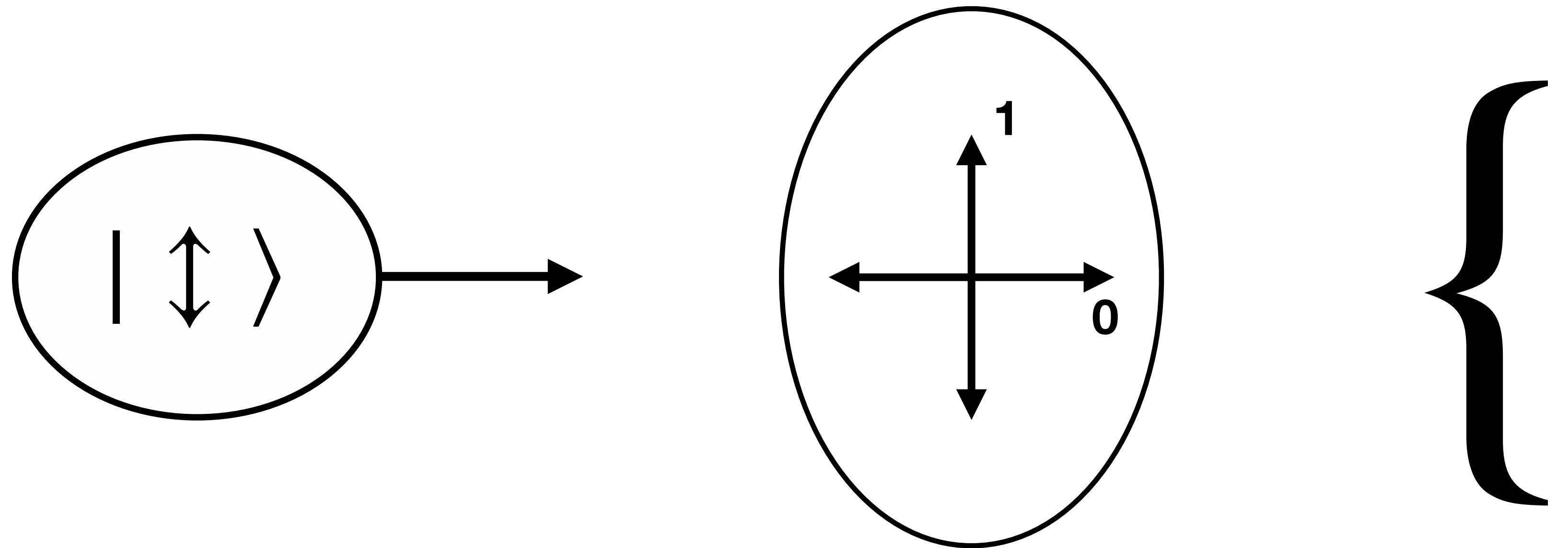


$$\begin{aligned}|90^\circ\rangle &\equiv |\uparrow\rangle \\|0^\circ\rangle &\equiv |\leftrightarrow\rangle\end{aligned}$$

$$P_{|\leftrightarrow\rangle} = |1|^2$$

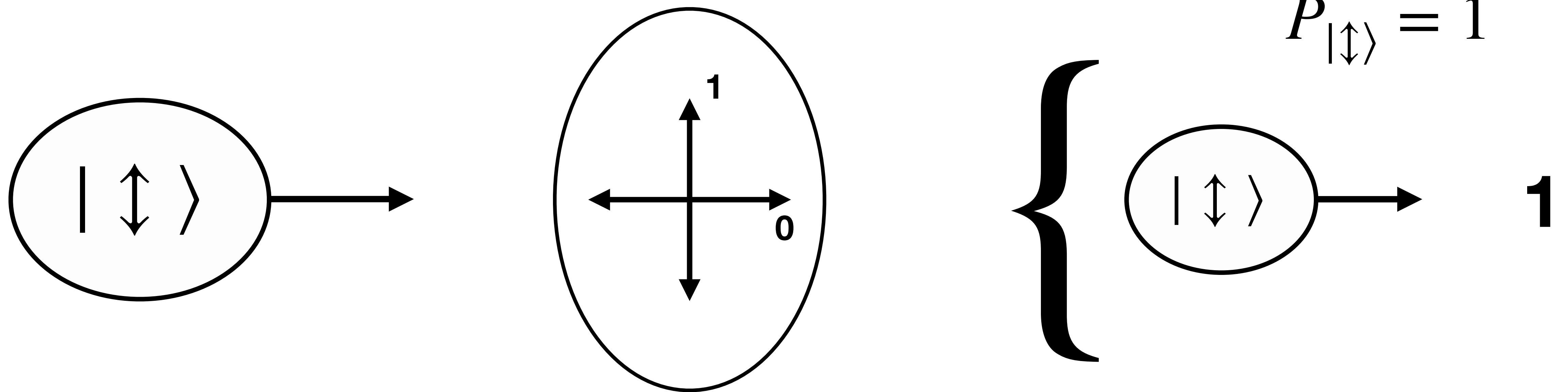
$$P_{|\uparrow\downarrow\rangle} = |0|^2$$

Measurement



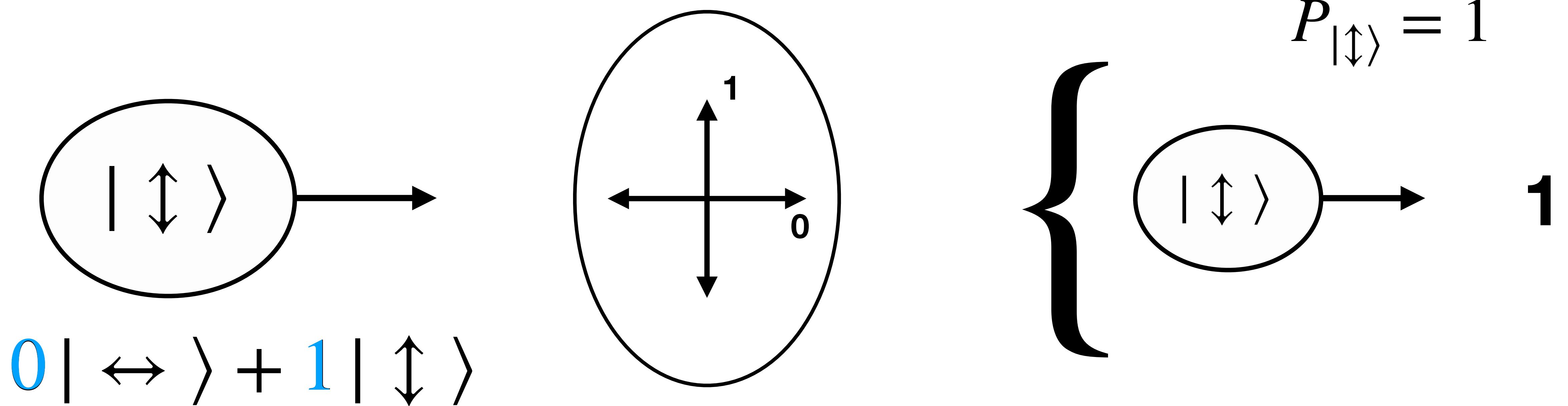
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Measurement



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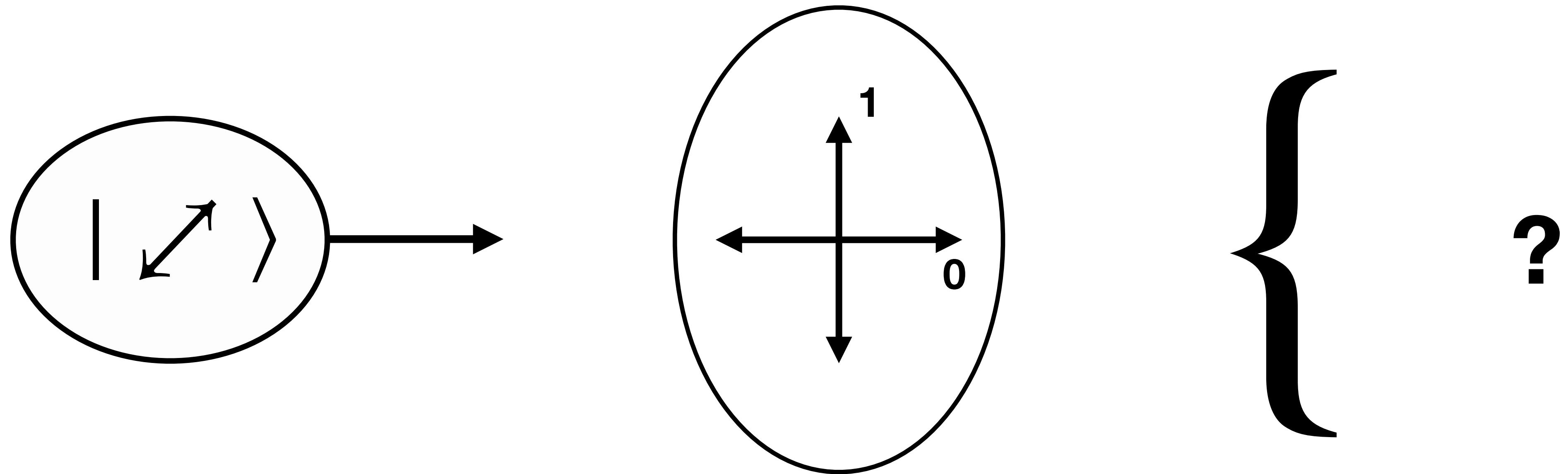
Measurement



$$\begin{aligned}|90^\circ\rangle &\equiv |\leftrightarrow\rangle \\|0^\circ\rangle &\equiv |\leftrightarrow\rangle\end{aligned}$$

$$P_{|\leftrightarrow\rangle} = |0|^2 \quad P_{|\uparrow\rangle} = |1|^2$$

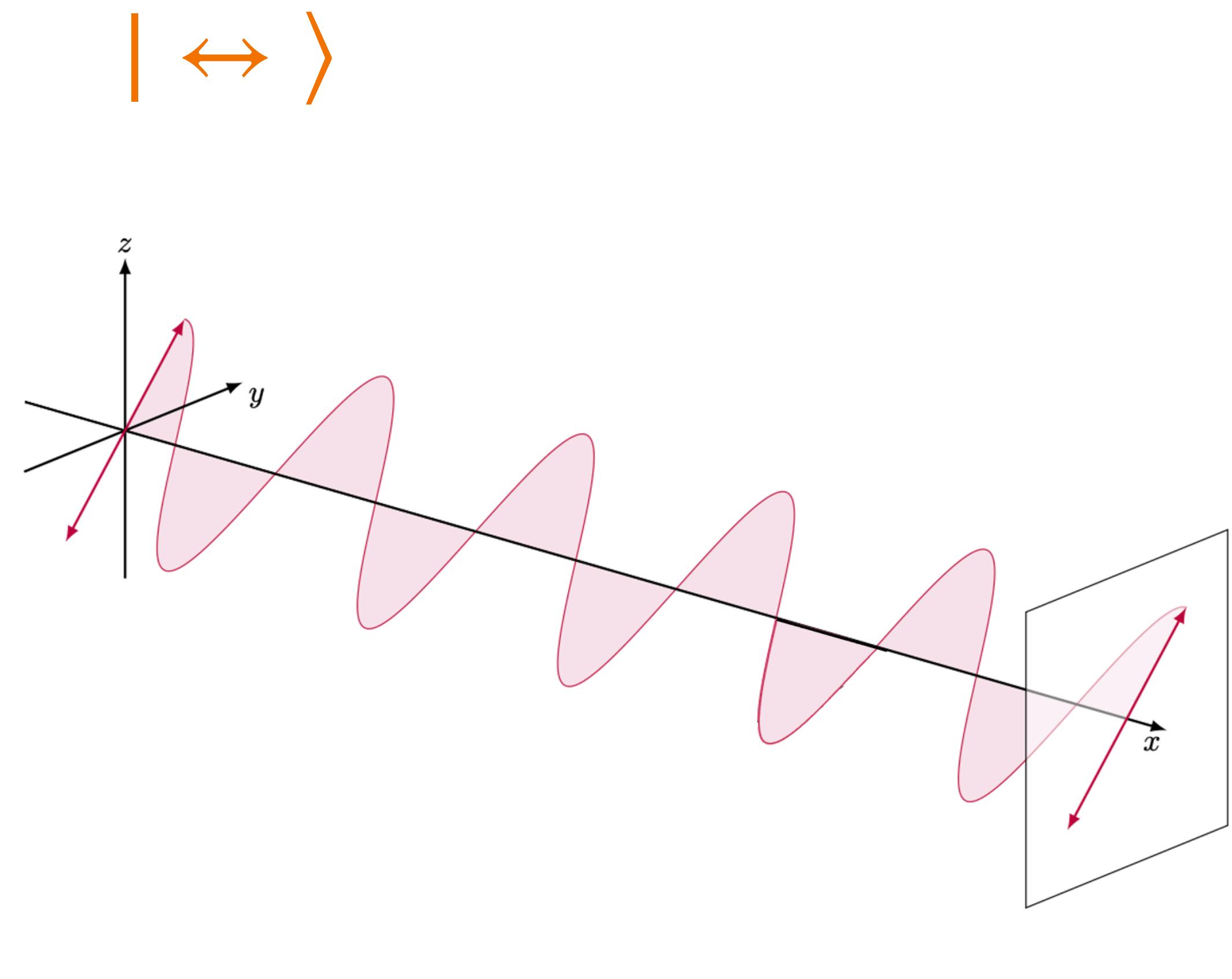
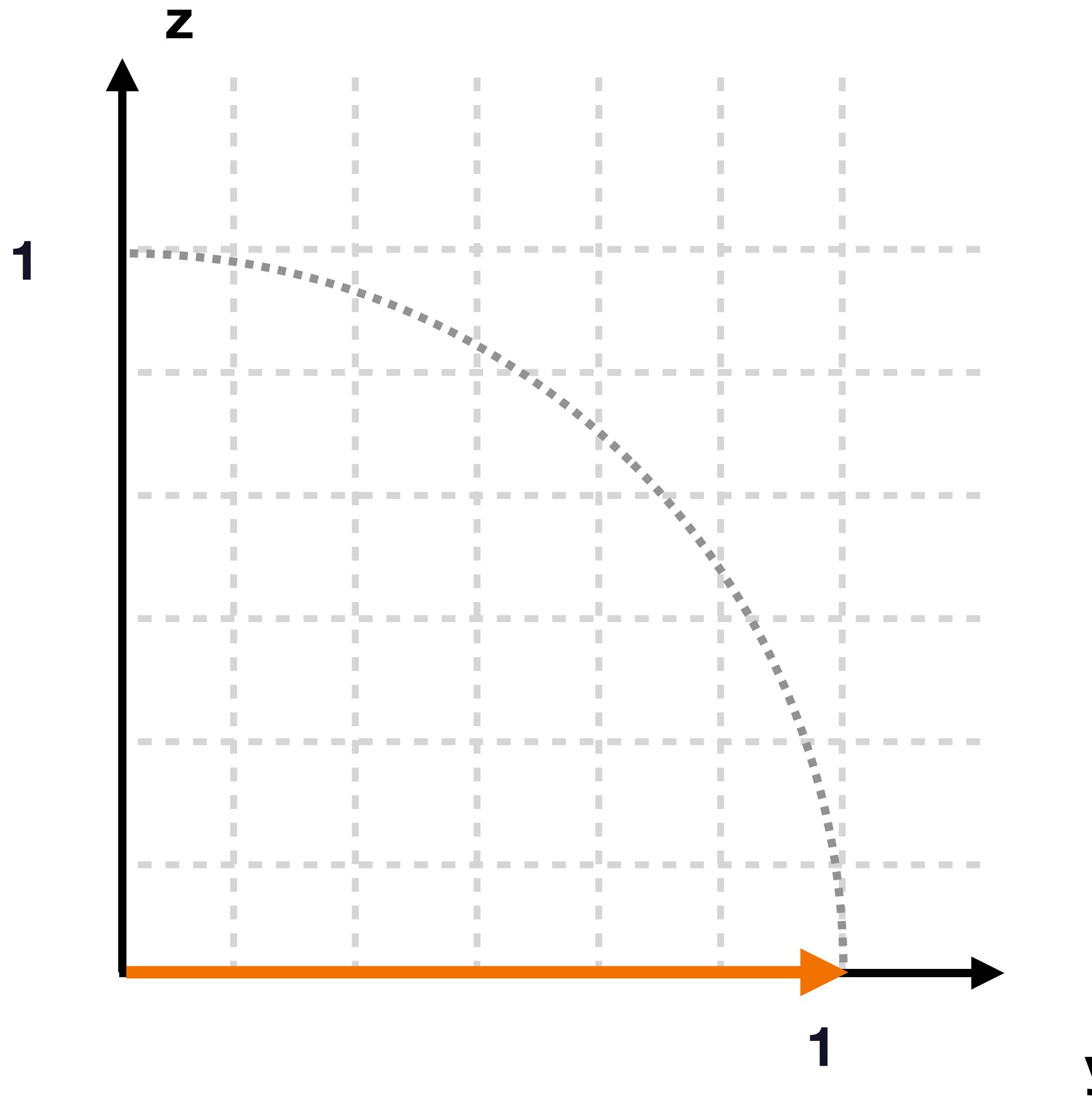
Measurement



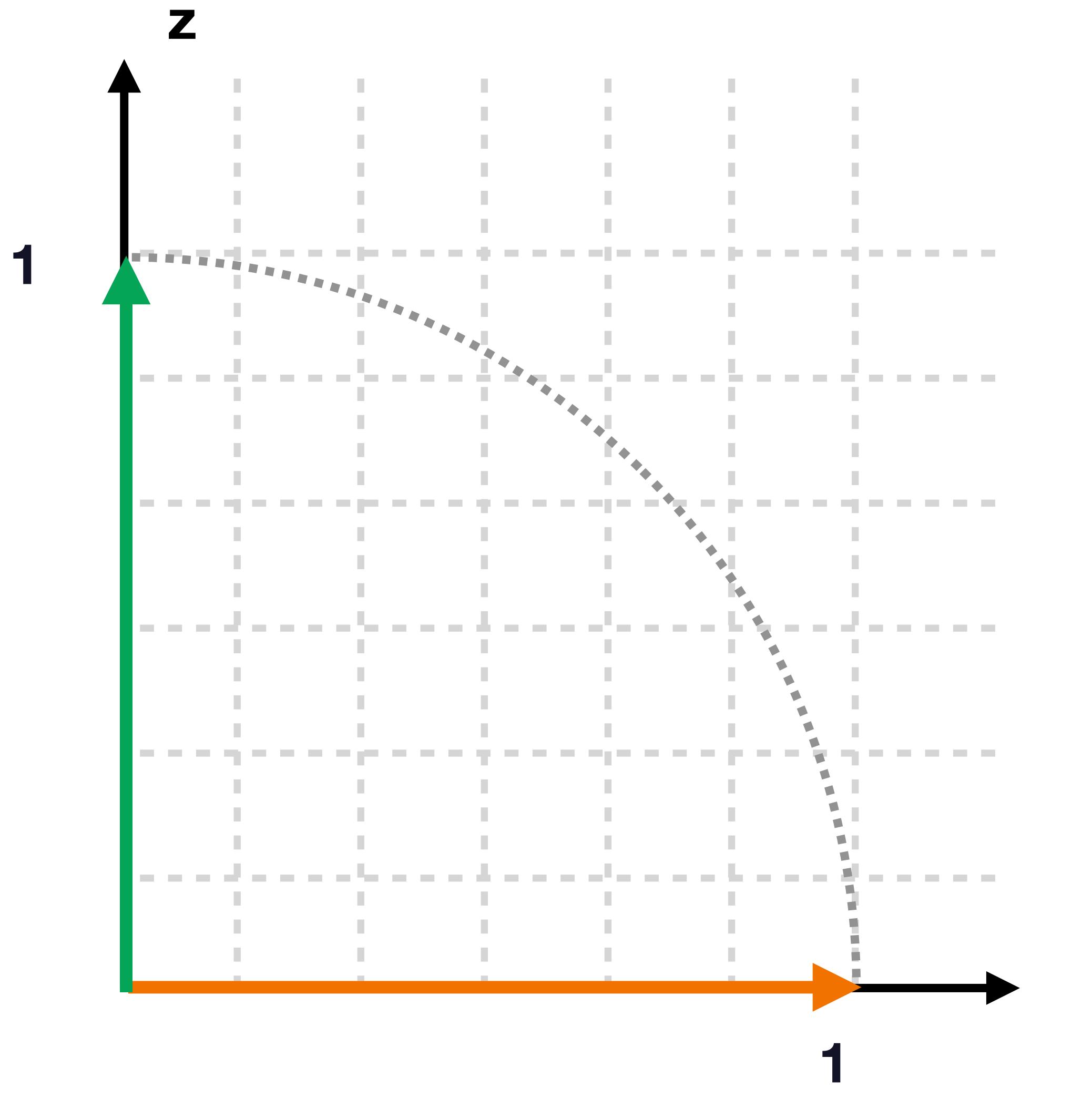
$$|45^\circ\rangle \equiv |\leftrightarrow\rangle$$

$$|135^\circ\rangle \equiv |\nwarrow\rangle$$

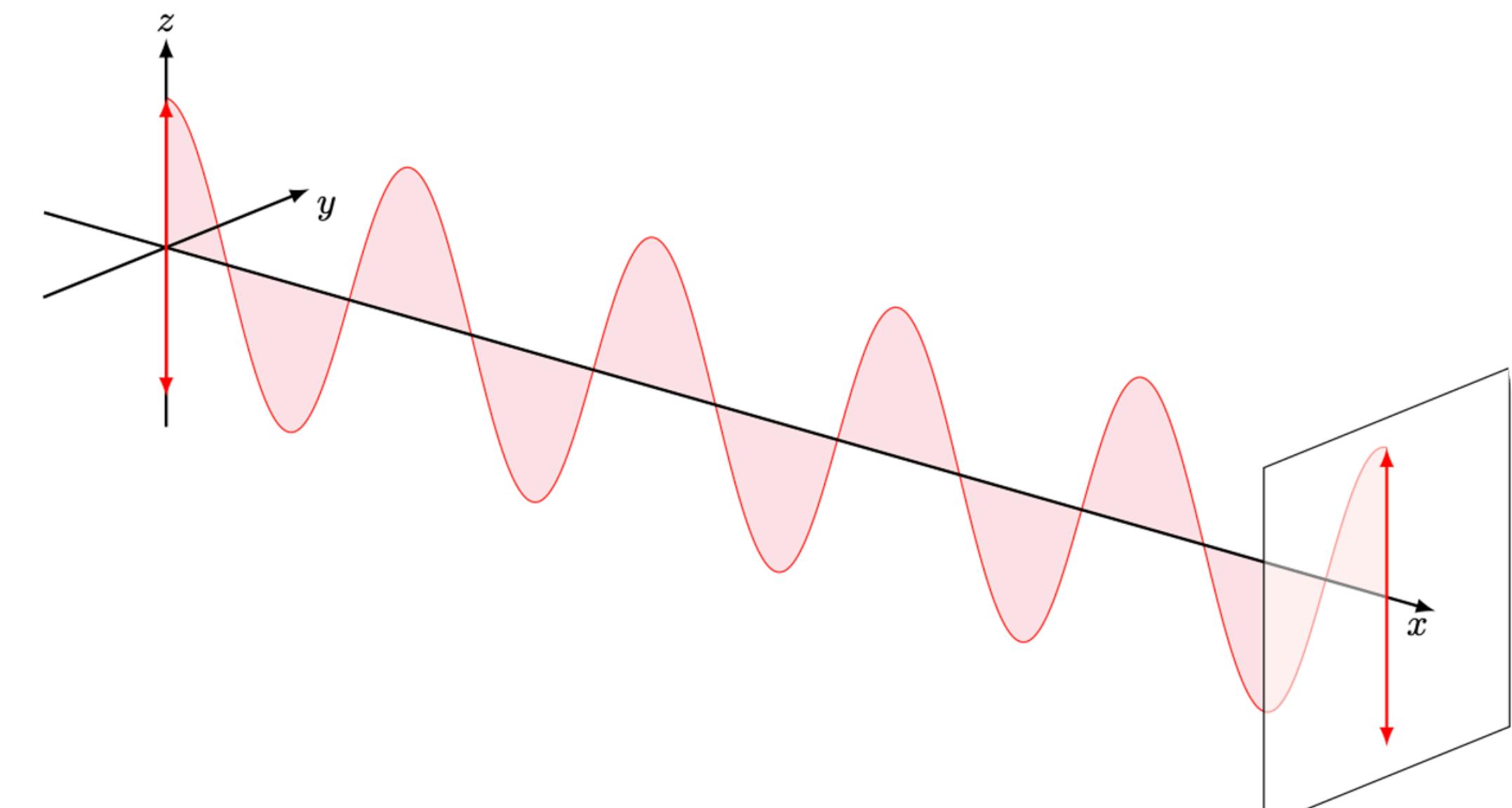
Measurement



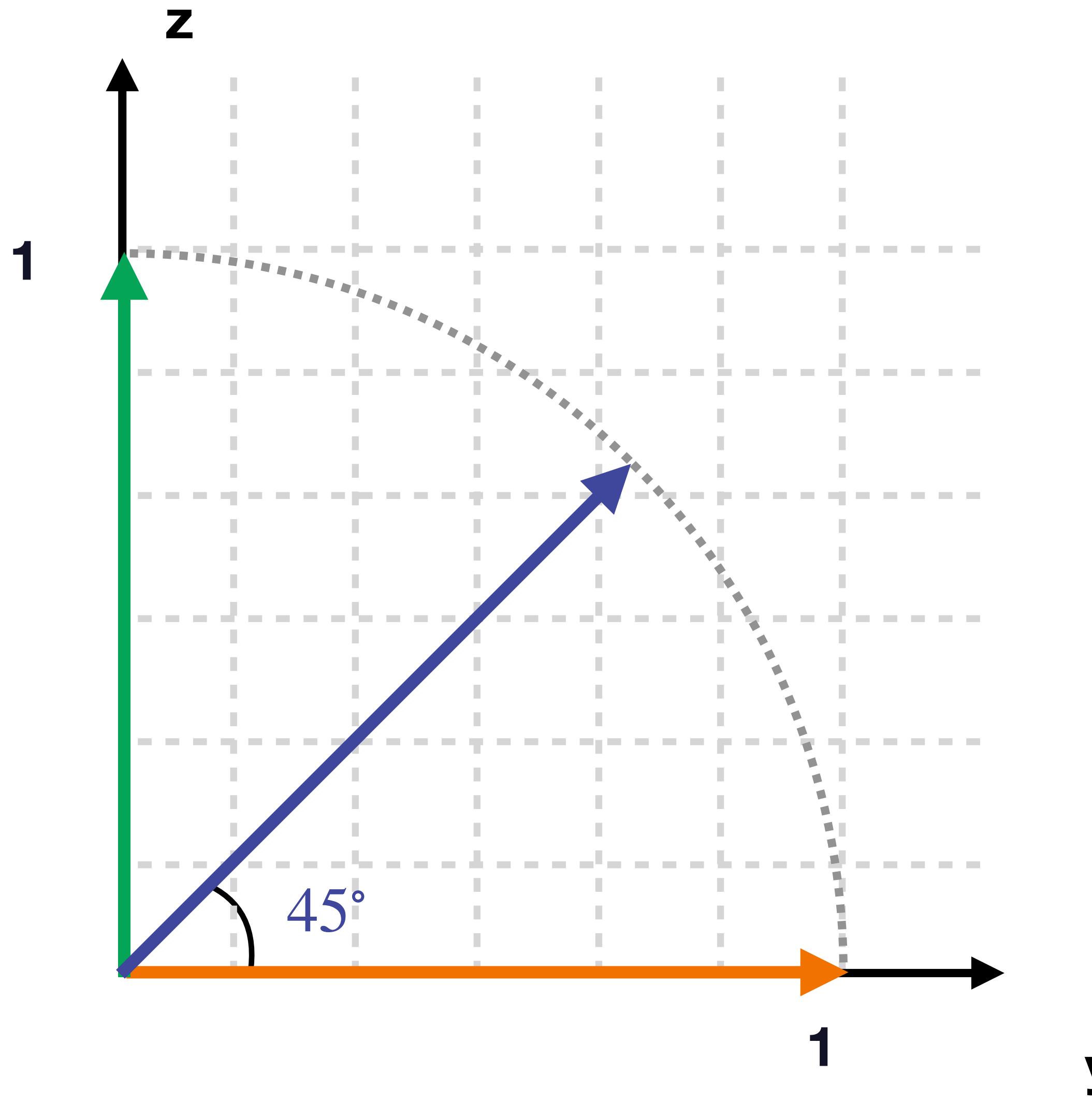
Measurement



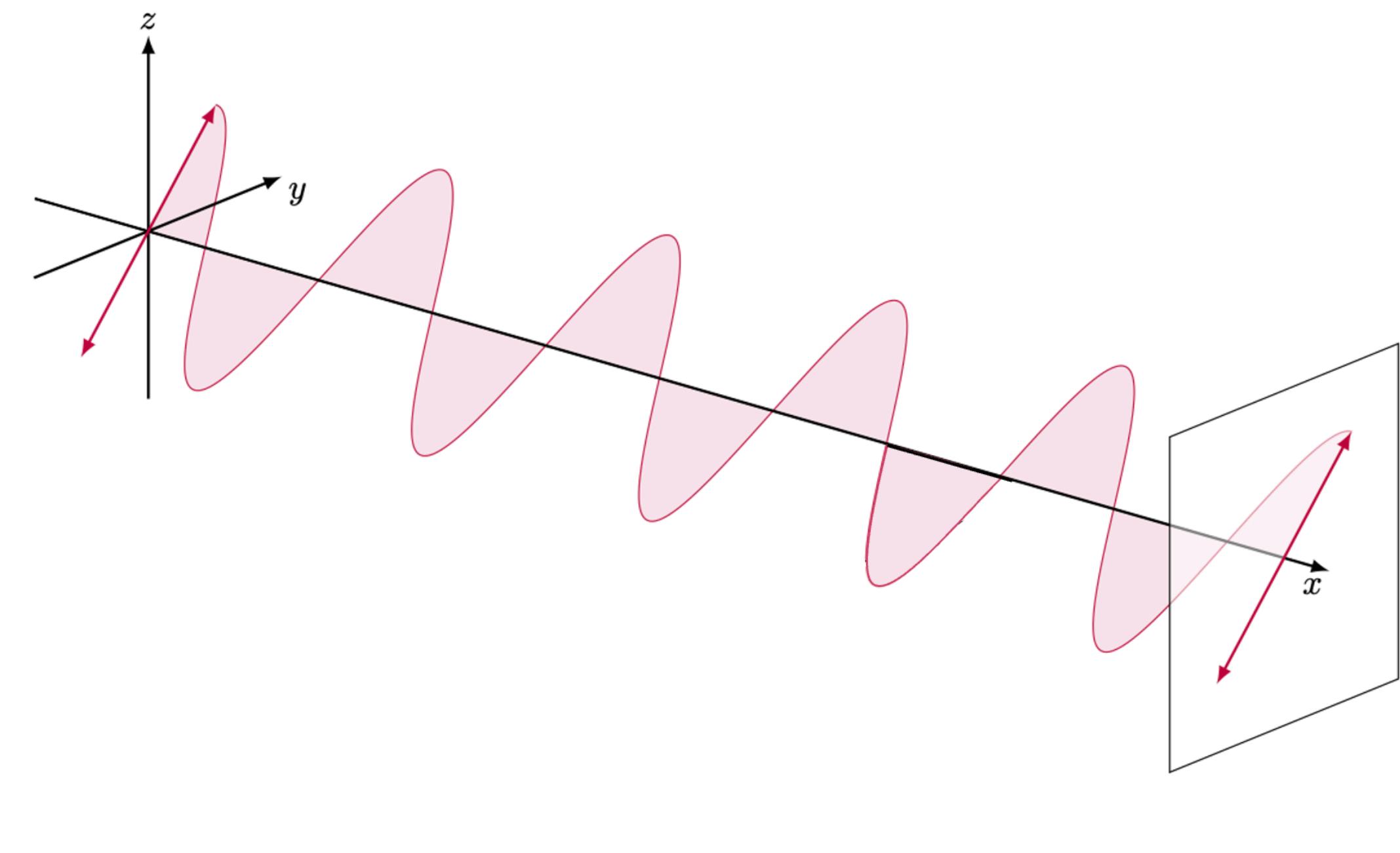
$| \leftrightarrow \rangle$ $| \updownarrow \rangle$



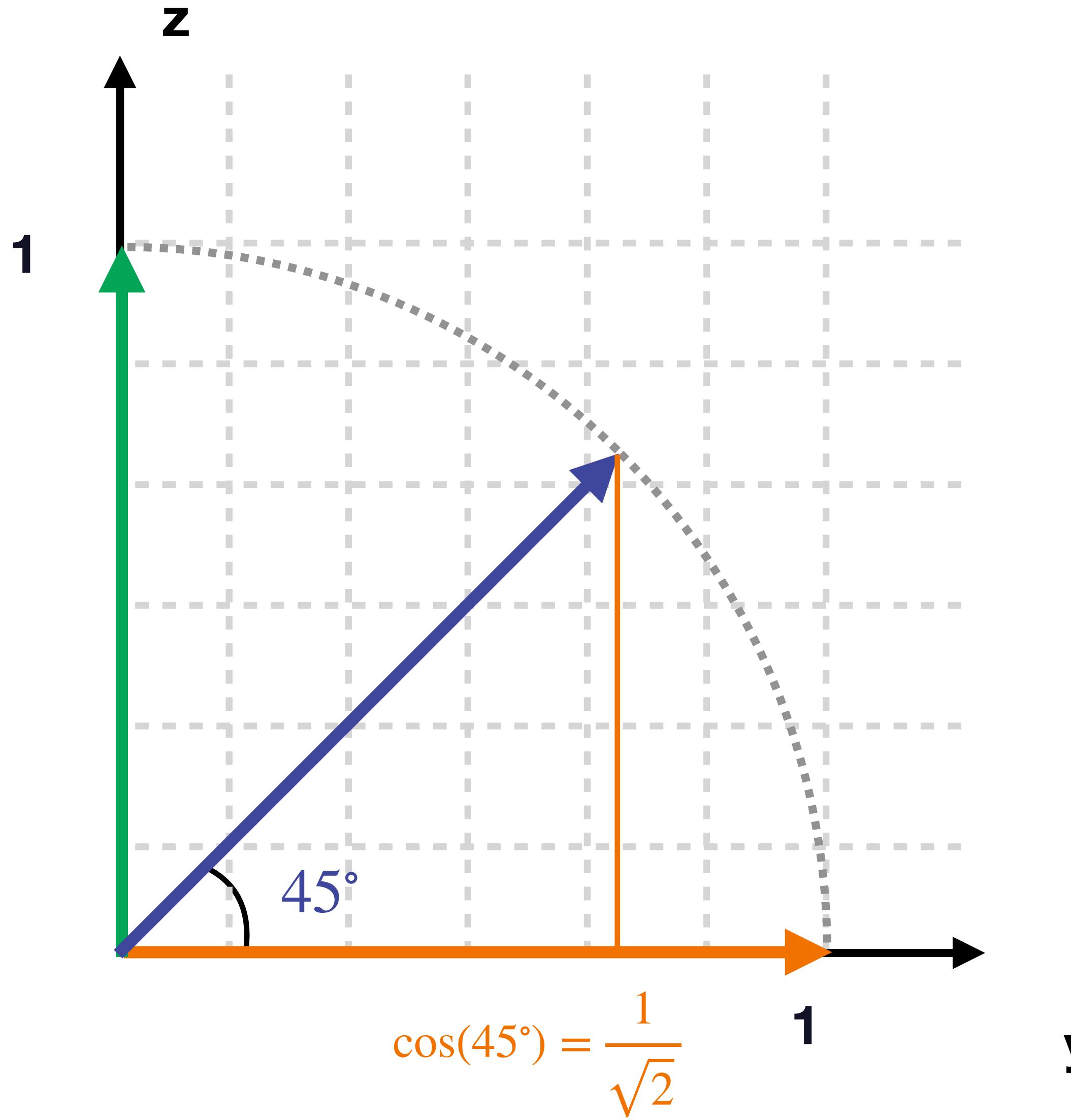
Measurement



$| \leftrightarrow \rangle$ $| \updownarrow \rangle$ $| \swarrow \rangle$



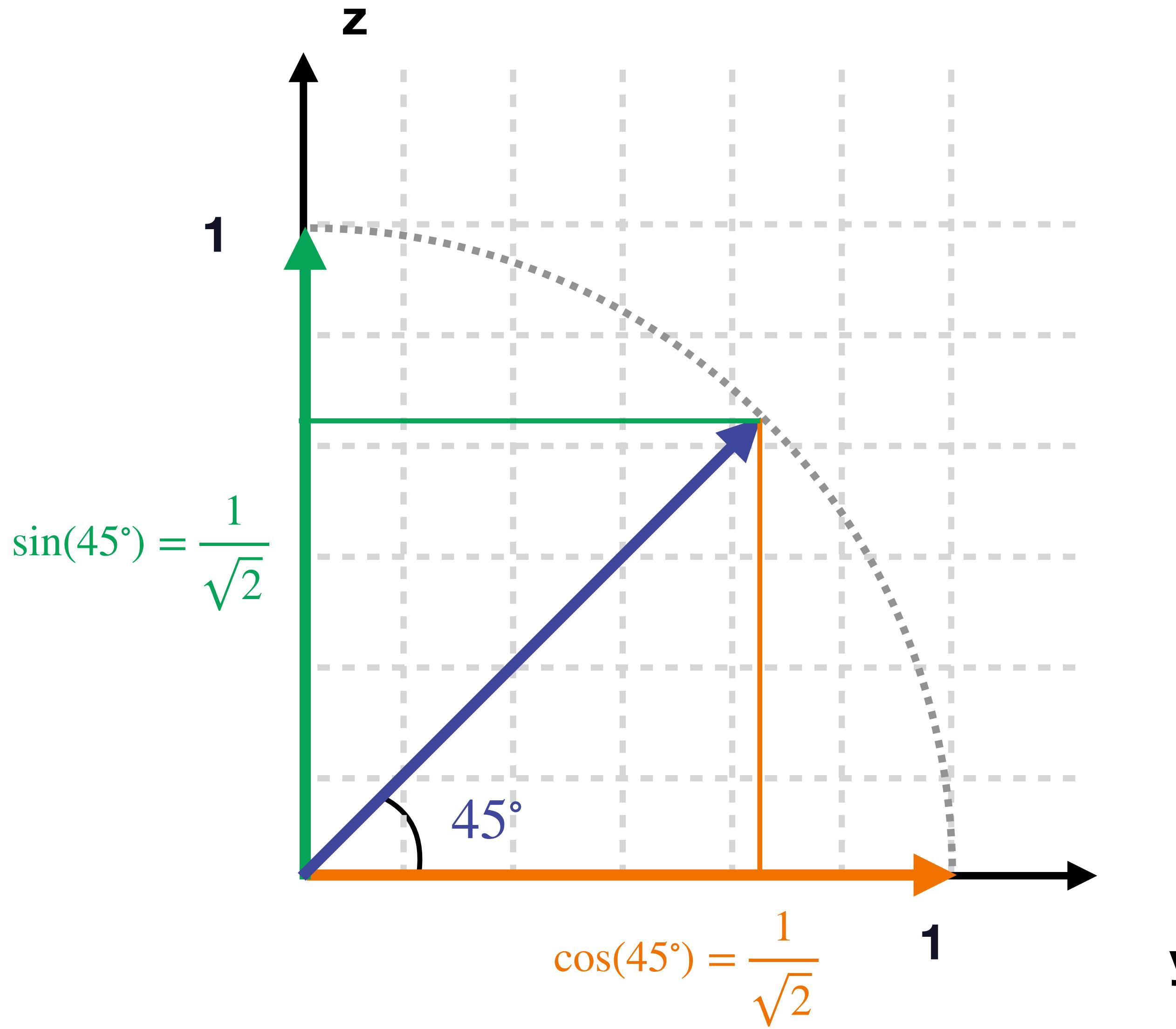
Measurement



$| \leftrightarrow \rangle$ $| \updownarrow \rangle$ $| \swarrow \rangle$

$$| \swarrow \rangle = \frac{1}{\sqrt{2}} | \leftrightarrow \rangle +$$

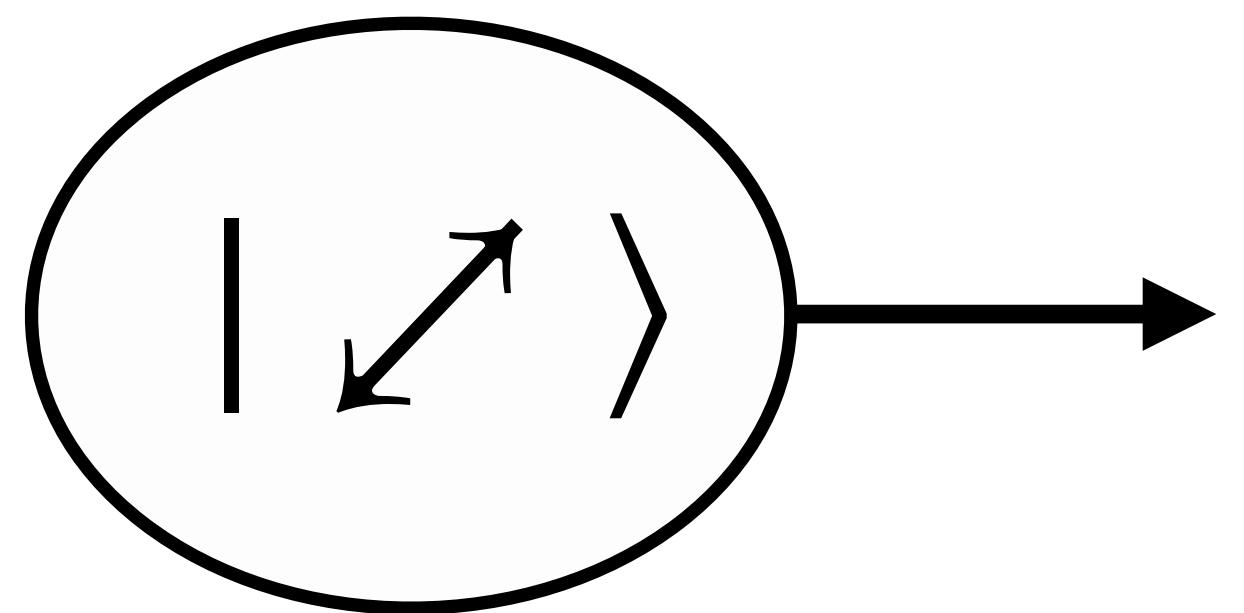
Measurement



$| \leftrightarrow \rangle$ $| \uparrow \downarrow \rangle$ $| \downarrow \uparrow \rangle$

$$| \downarrow \uparrow \rangle = \frac{1}{\sqrt{2}} | \leftrightarrow \rangle + \frac{1}{\sqrt{2}} | \uparrow \downarrow \rangle$$

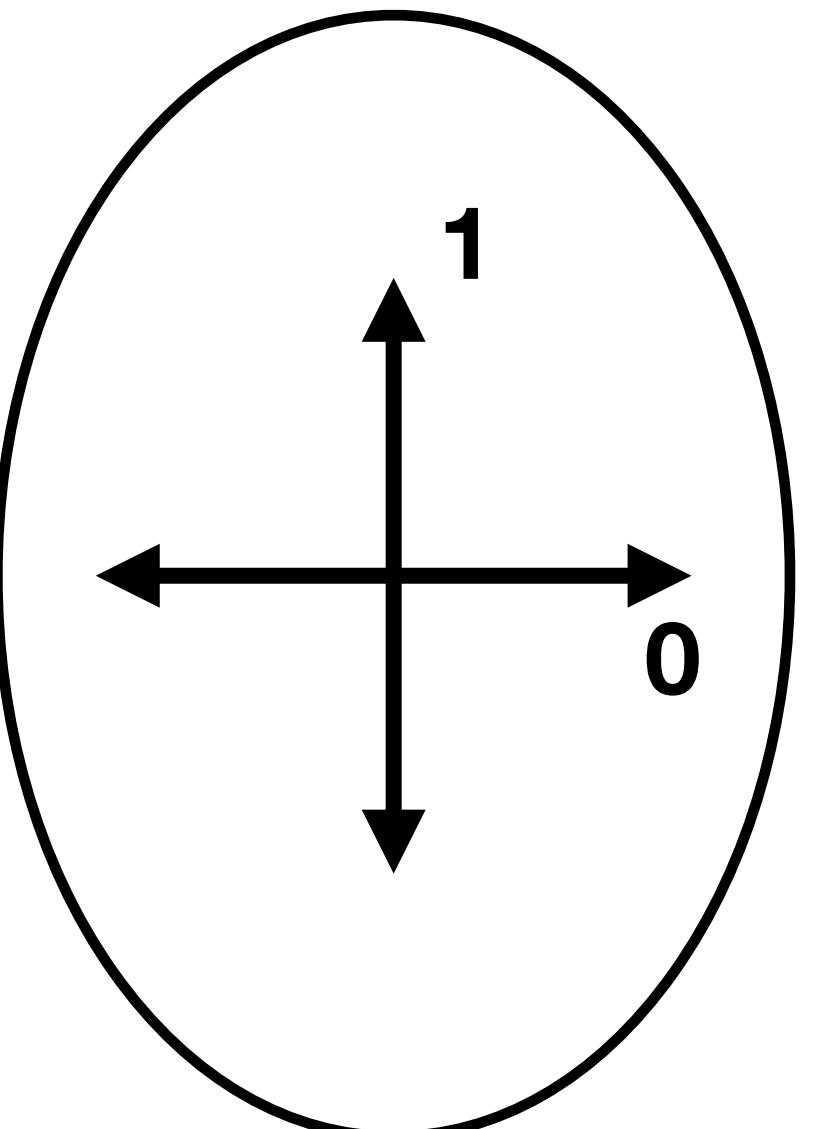
Measurement



$$\frac{1}{\sqrt{2}} |\leftrightarrow\rangle + \frac{1}{\sqrt{2}} |\uparrow\downarrow\rangle$$

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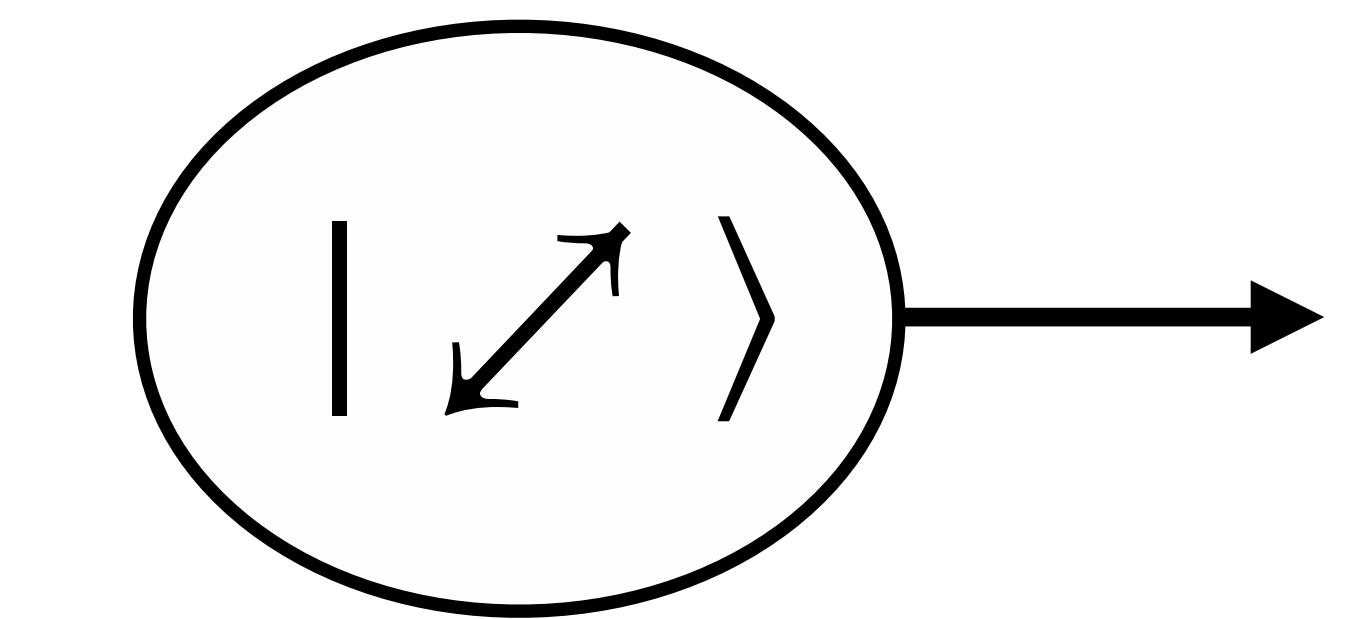
$$|135^\circ\rangle \equiv |\uparrow\downarrow\rangle$$



{ ?

$$|\alpha|^2 + |\beta|^2 = 1$$

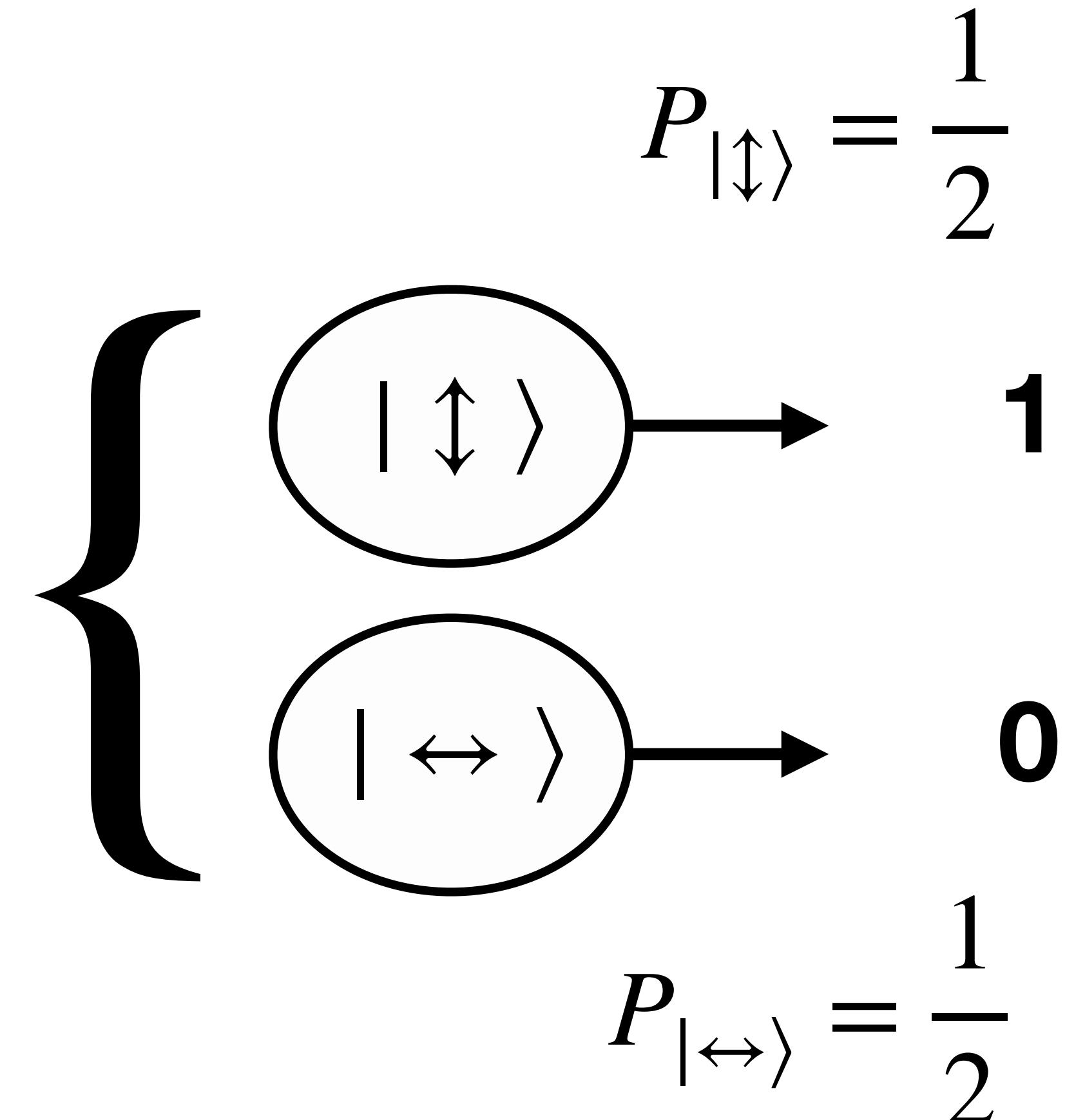
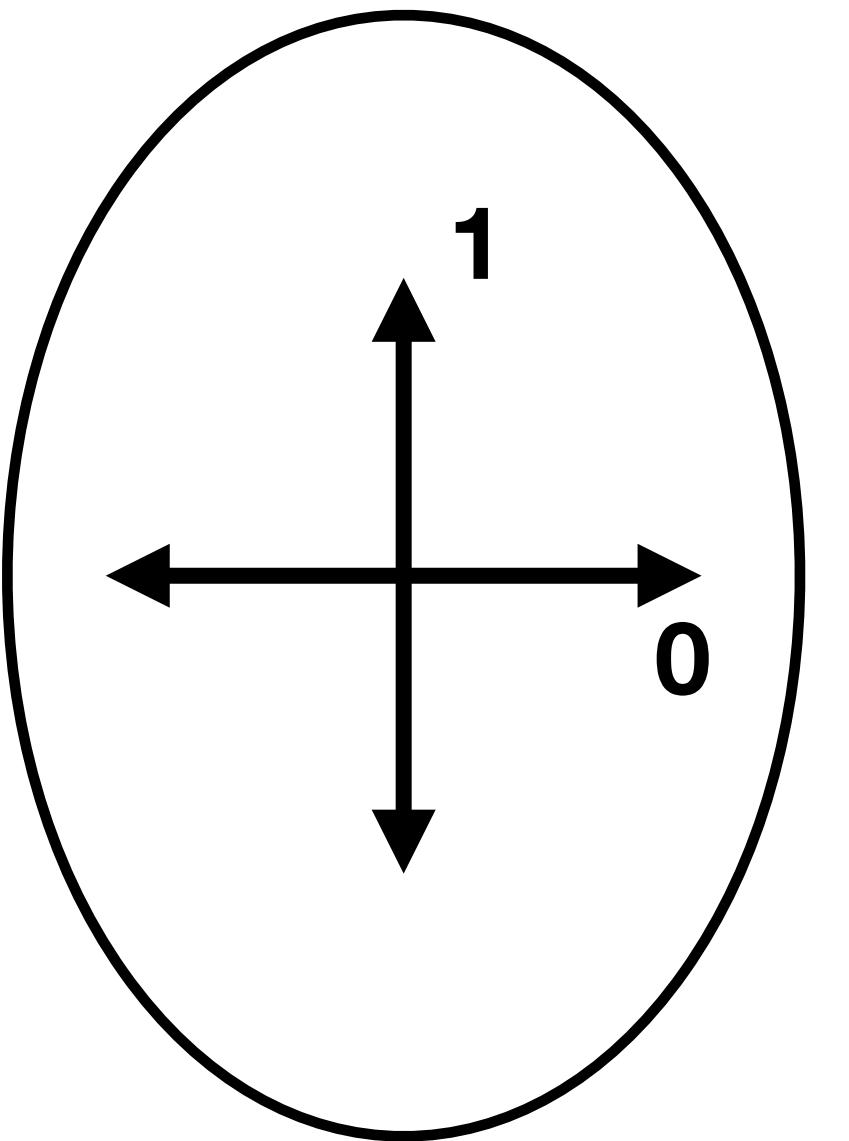
Measurement



$$\frac{1}{\sqrt{2}} | \leftrightarrow \rangle + \frac{1}{\sqrt{2}} | \uparrow \downarrow \rangle$$

$$| 45^\circ \rangle \equiv | \leftrightarrow \rangle$$

$$| 135^\circ \rangle \equiv | \uparrow \downarrow \rangle$$

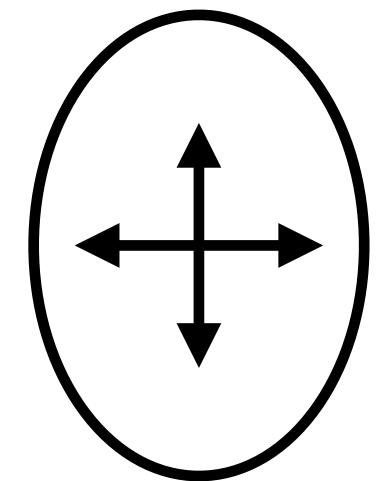


$$|\alpha|^2 + |\beta|^2 = 1$$

Superposition & Quantum Measurement

Key points

- Quantum measurement collapses the polarization into one of the basis states of the measurement basis.

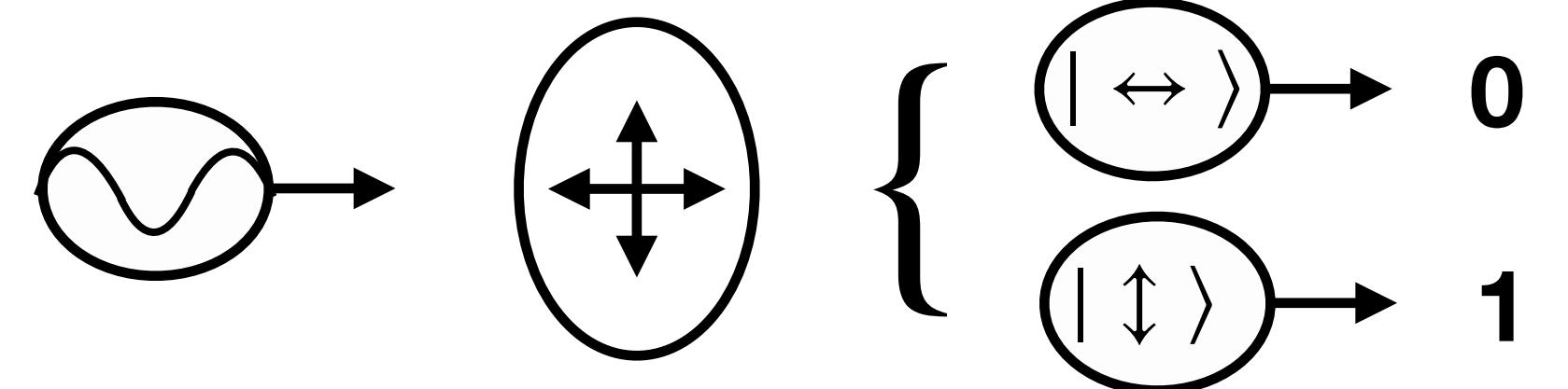


$| \uparrow \downarrow \rangle$ ou $| \leftrightarrow \rangle$

Superposition & Quantum Measurement

Key points

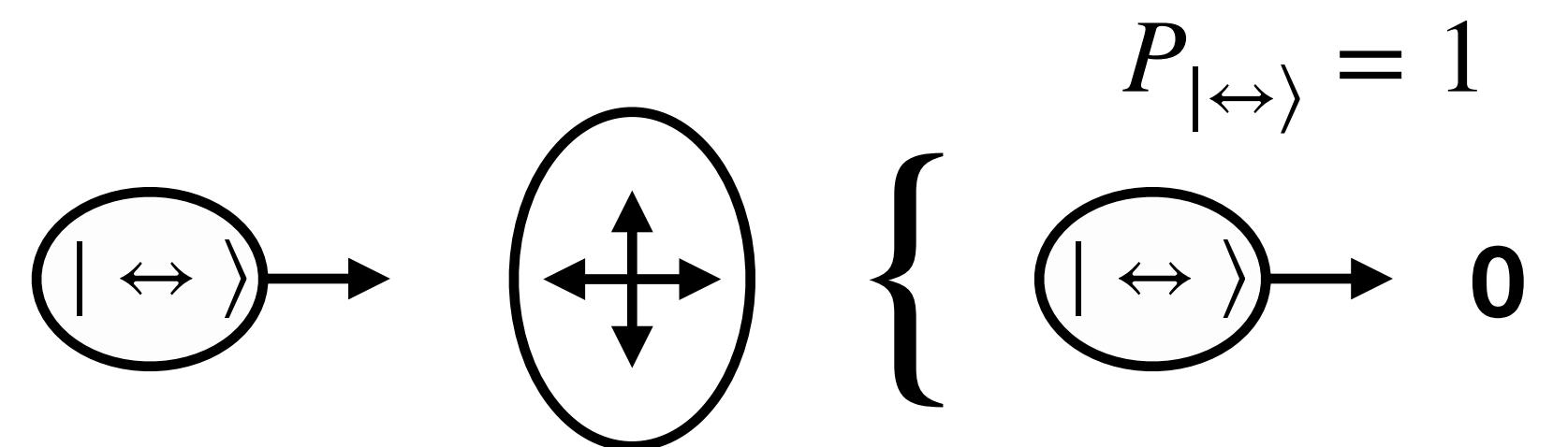
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- If the incident photon is in a superposition state, the measurement result is random.



Superposition & Quantum Measurement

Key points

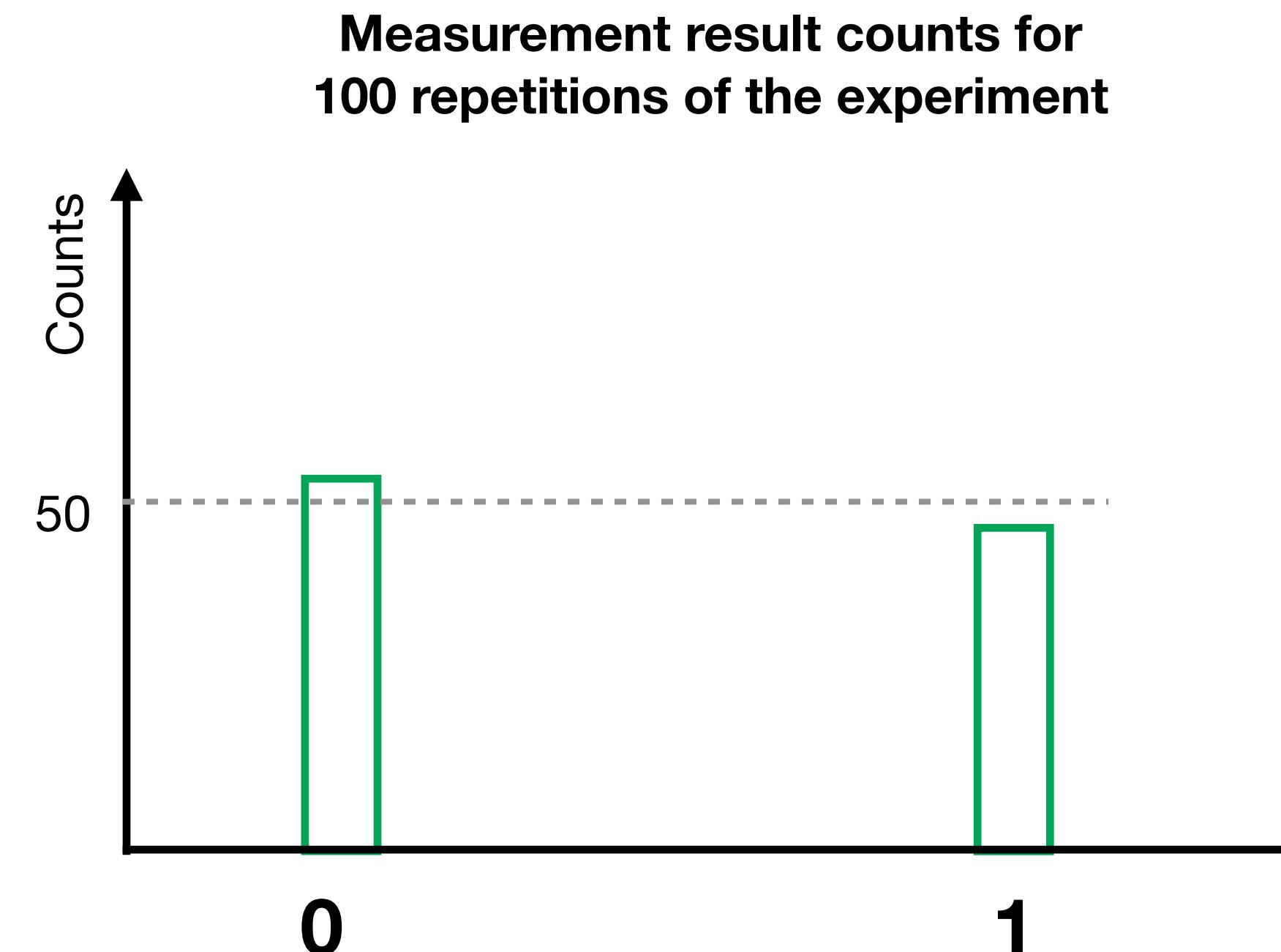
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- If the incident photon is in a basis state of the measurement basis, the result will always be the same.



Superposition & Quantum Measurement

Key points

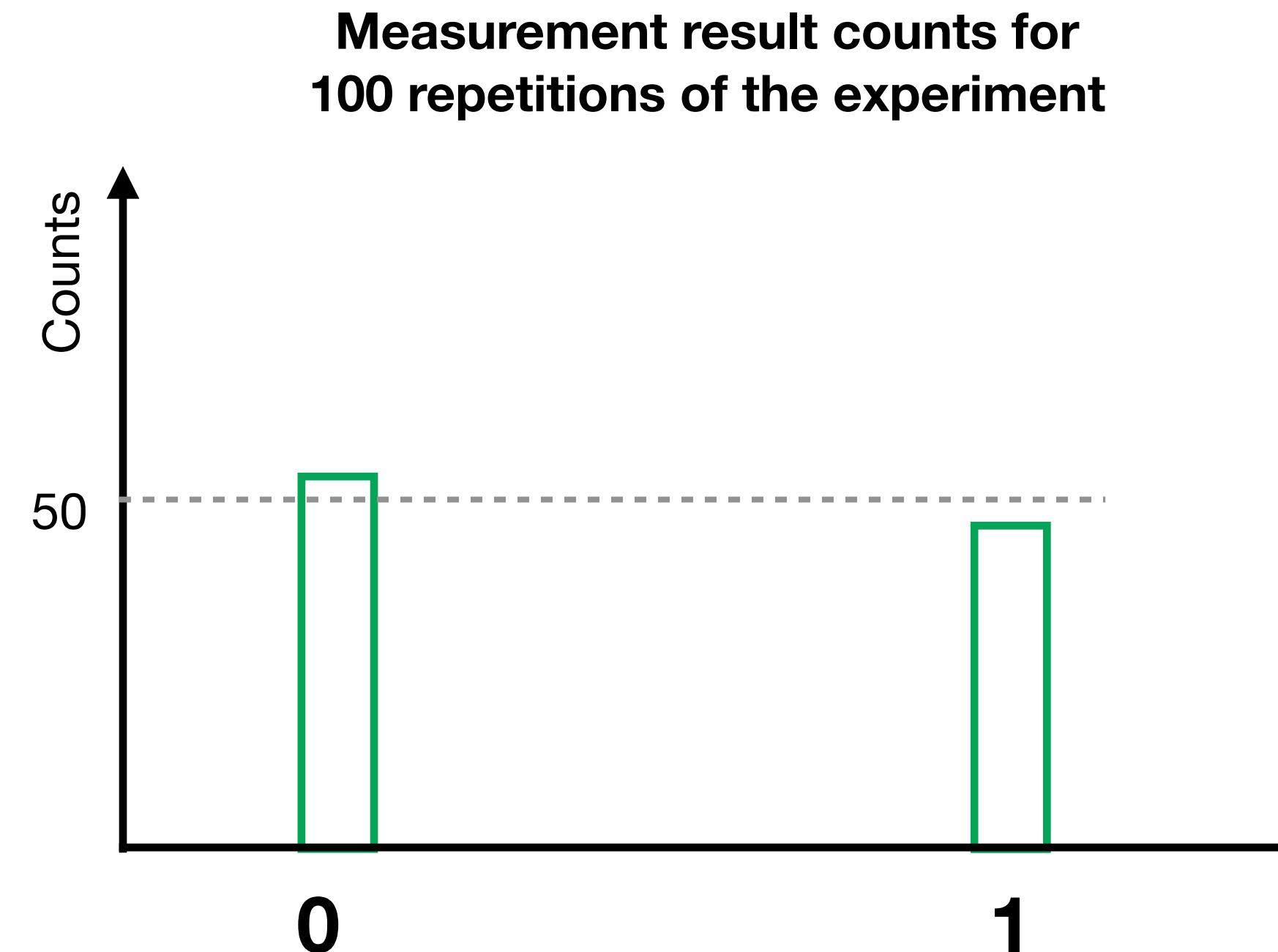
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Superposition & Quantum Measurement

Key points

- Quantum measurement collapses the polarization into one of the basis states of the measurement basis.
- If the incident photon is in a superposition state, the measurement result is random.
- If the incident photon is in a basis state of the measurement basis, the result will always be the same.
- To describe the quantum state of an incident photon, the measurement experiment must be repeated multiple times and the results compiled to build statistics.
- Otherwise, we cannot say anything.





Encoding Information

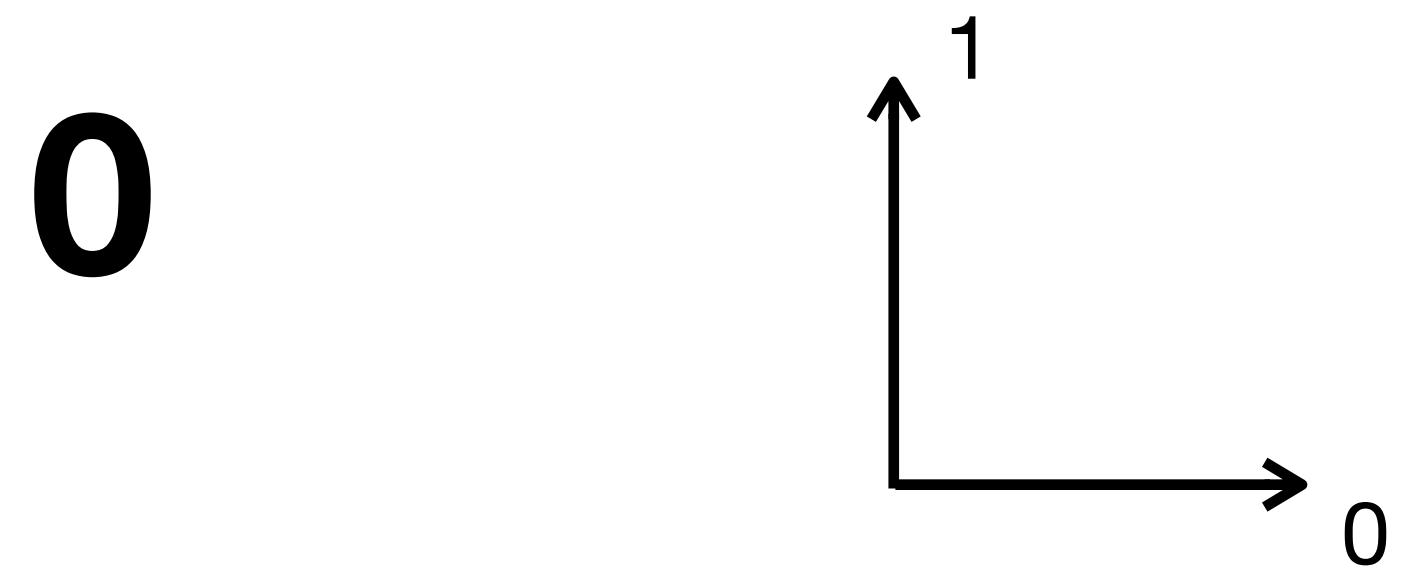
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Encoding Information

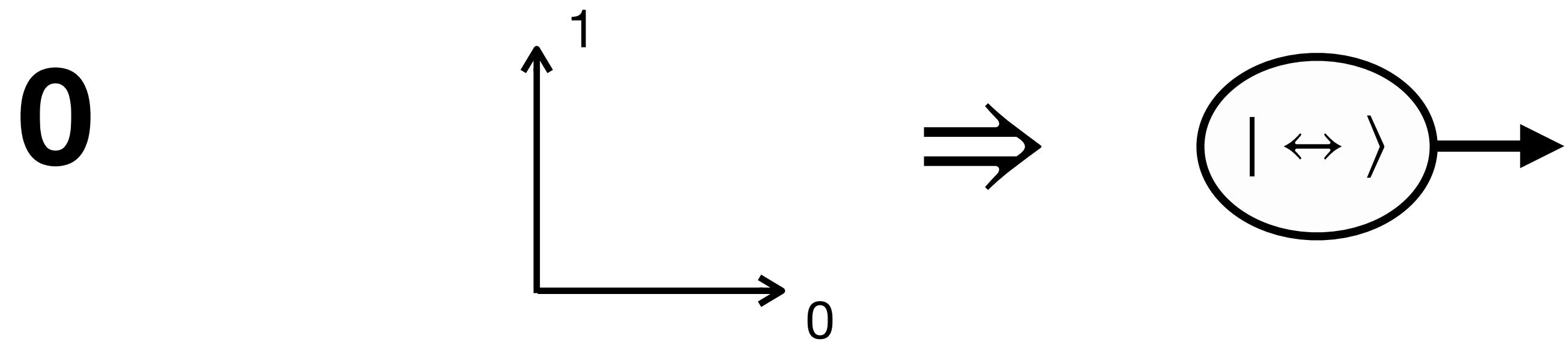
Bit to transmit Measurement
 basis



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Encoding Information

Bit to transmit Measurement basis

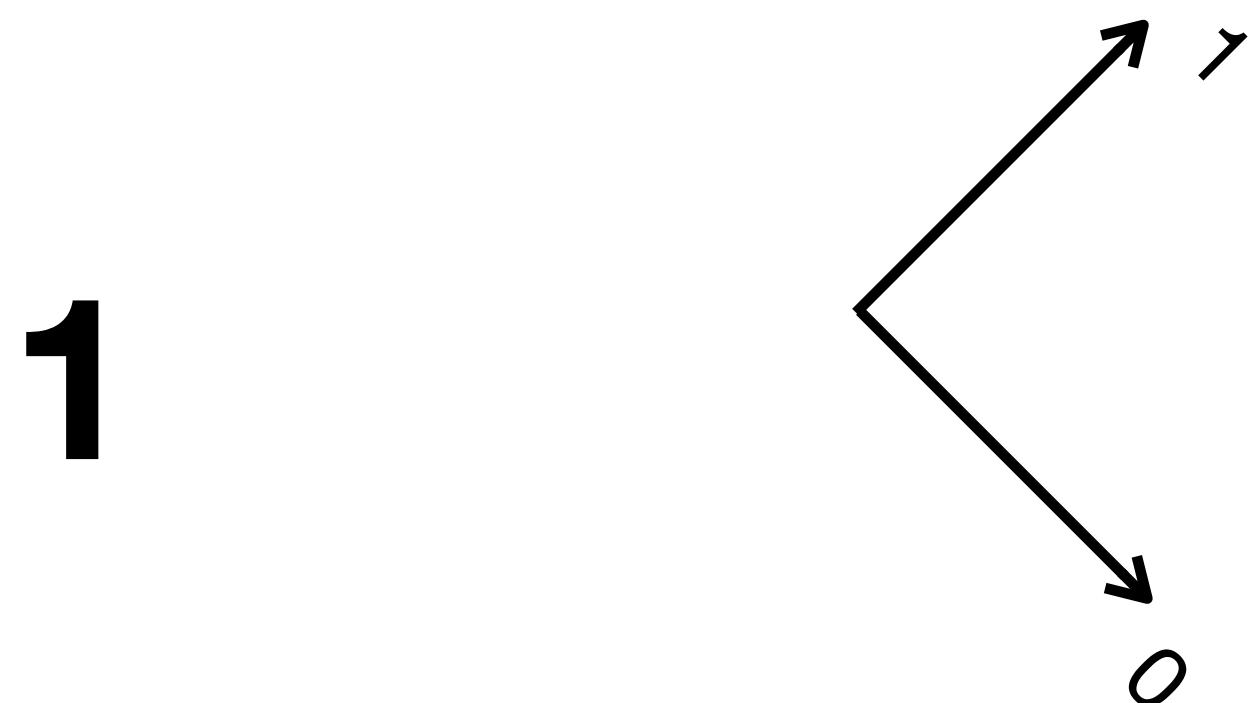


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Encoding Information

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Encoded photon

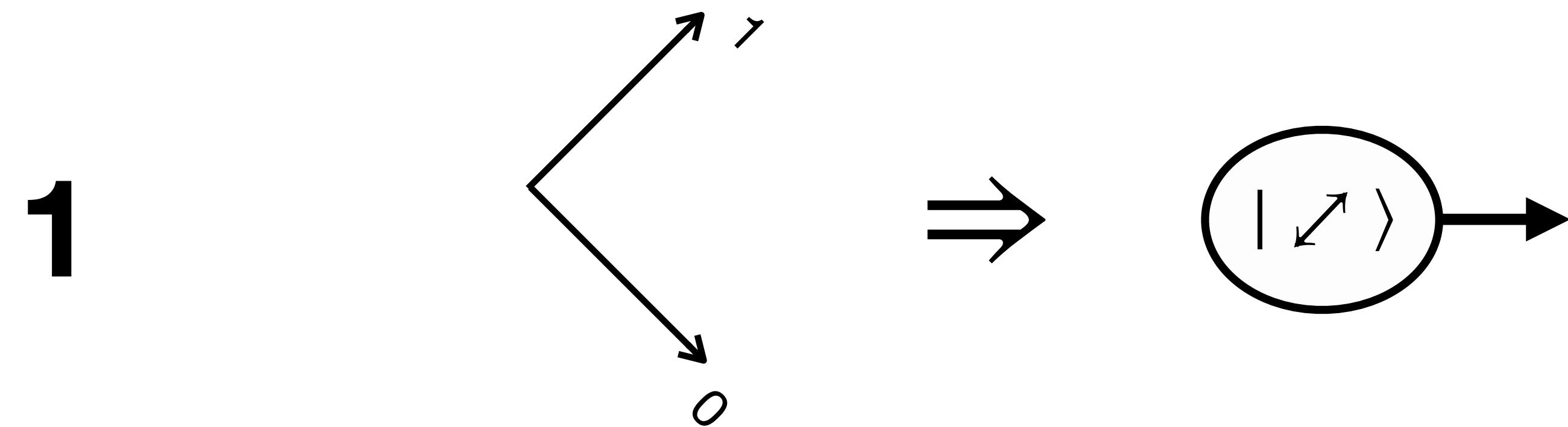


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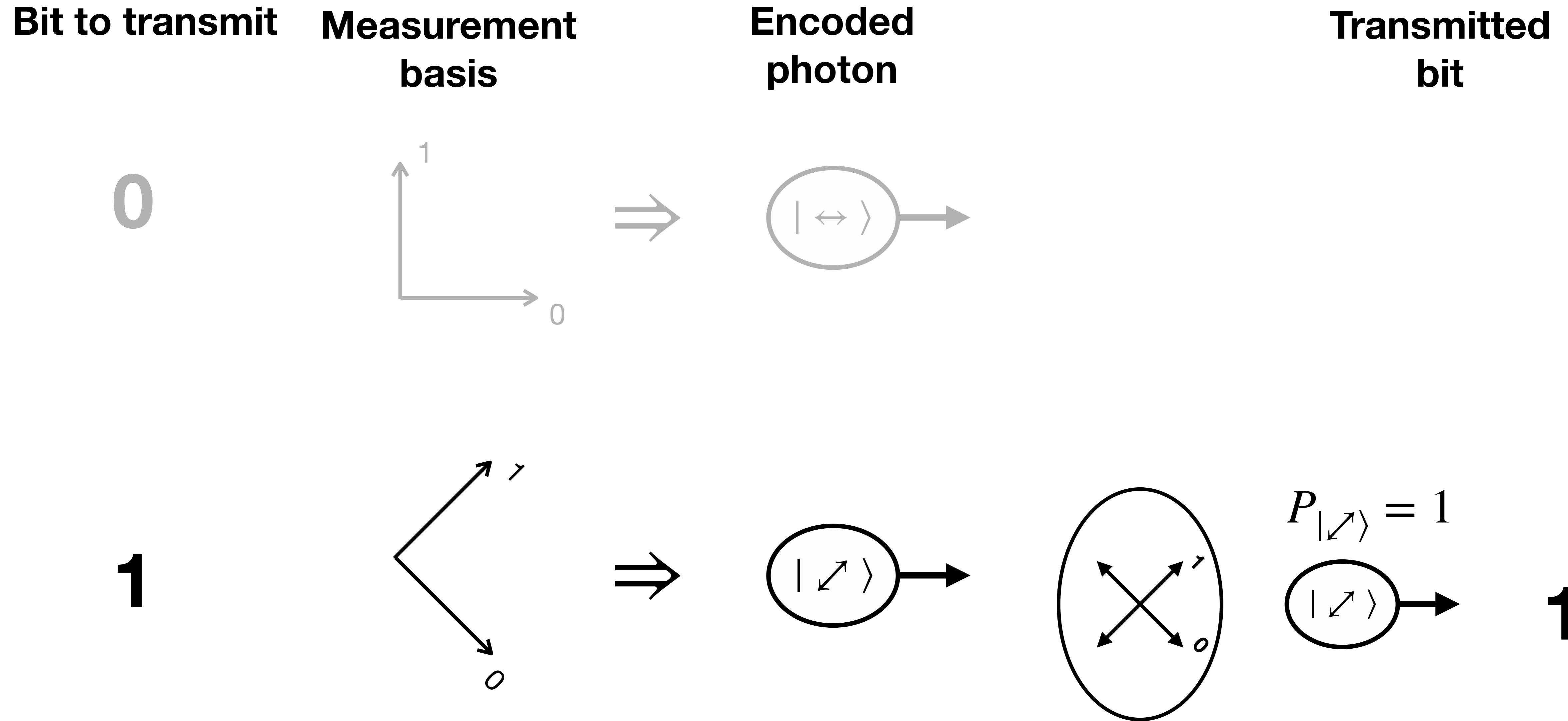
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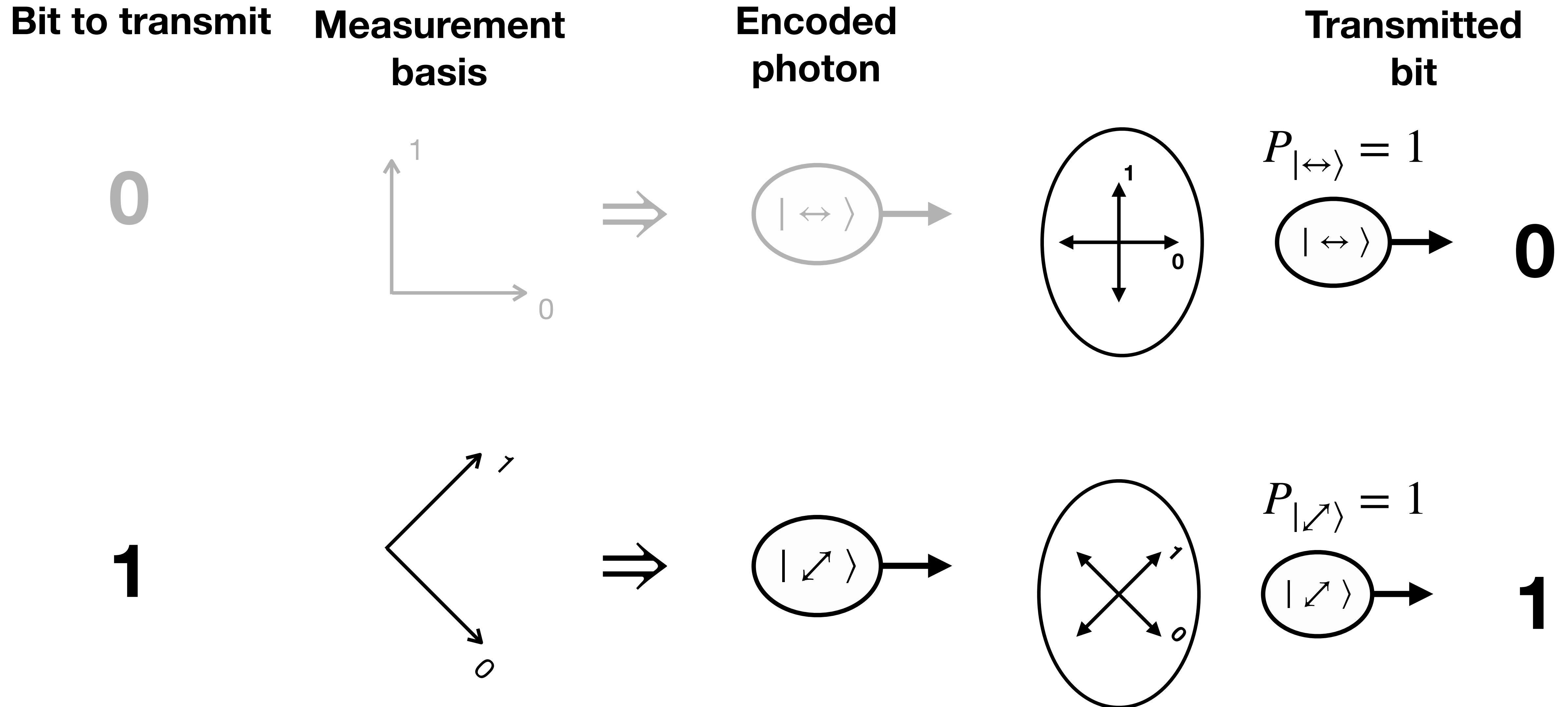
Encoded photon



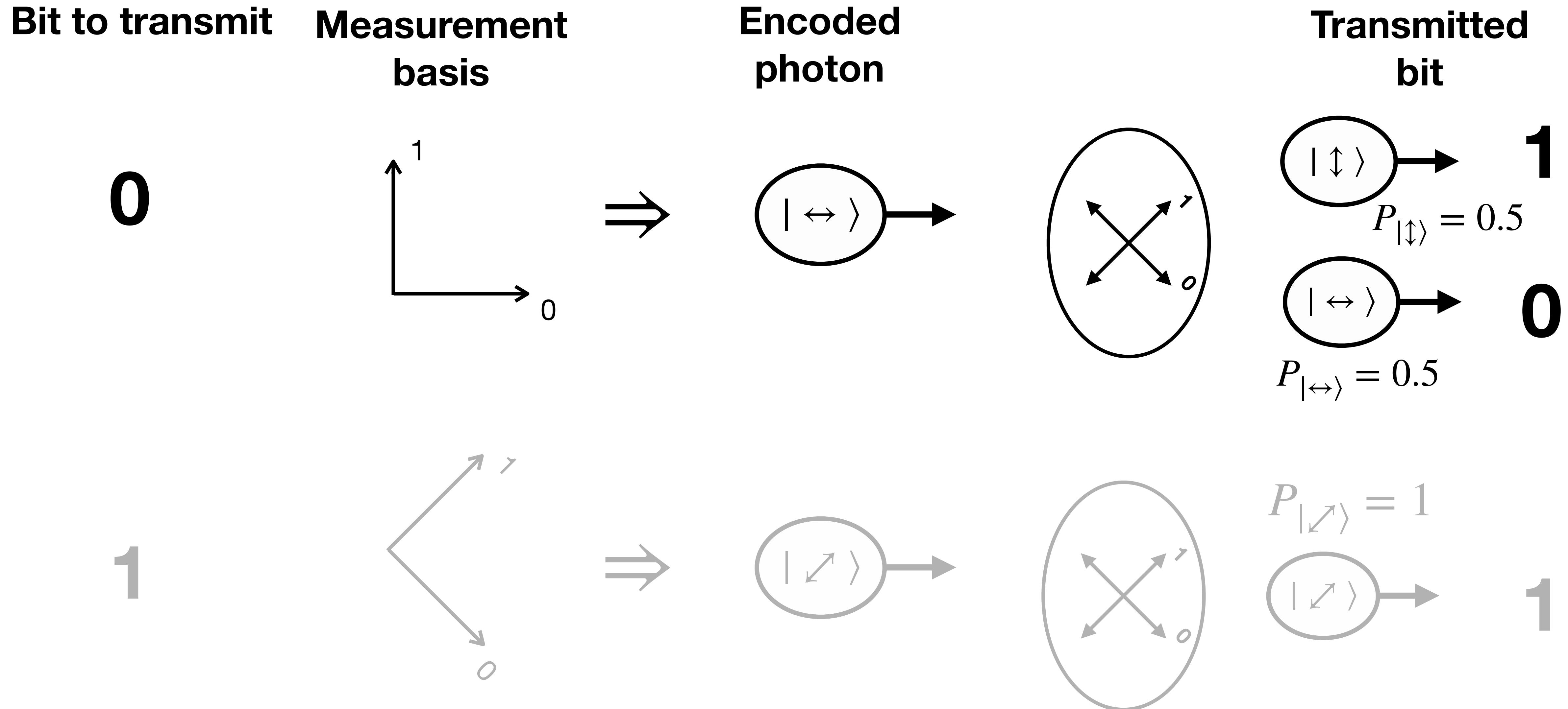
Encoding Information



Encoding Information

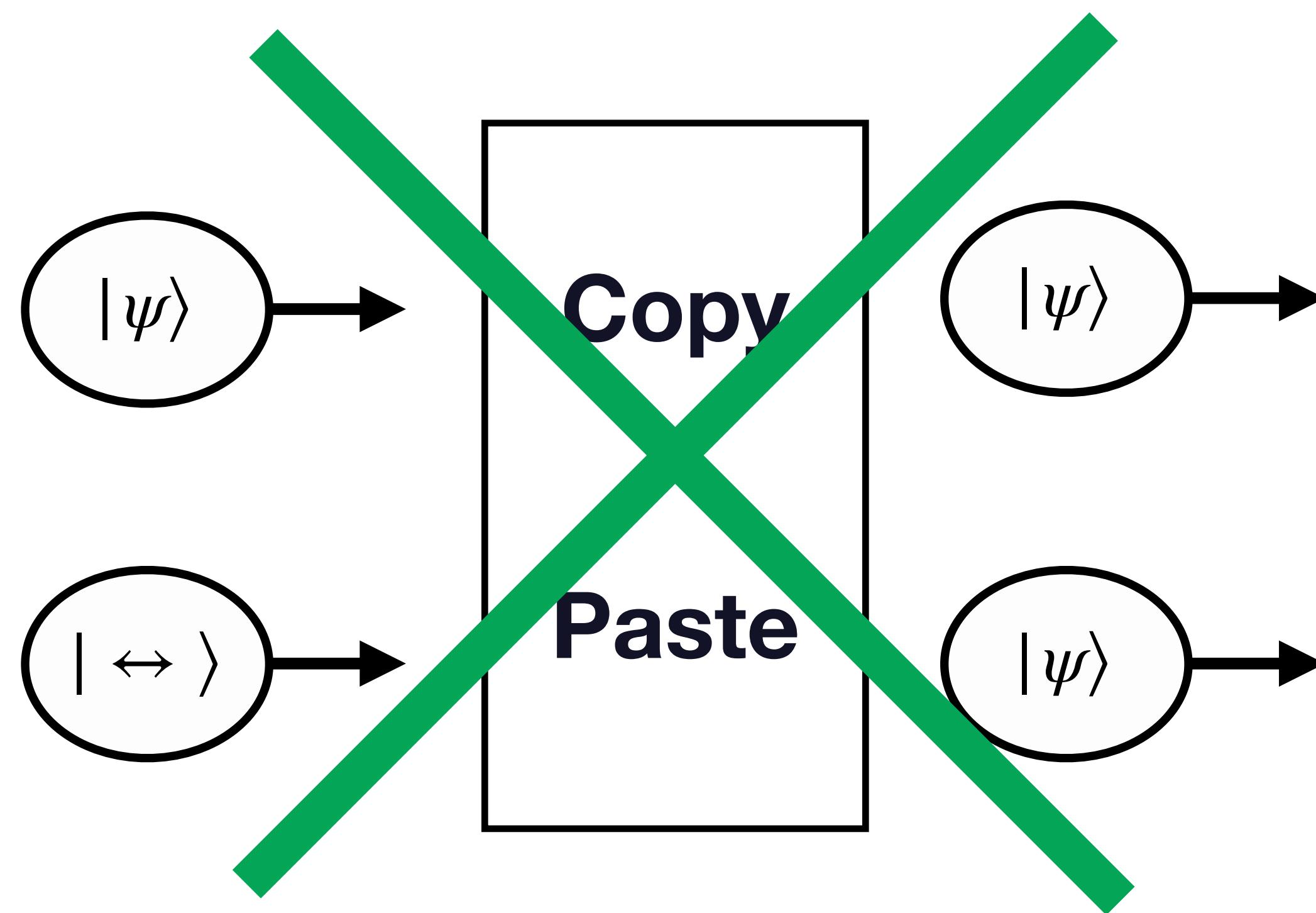


Encoding Information



No-Cloning Theorem

"It is impossible to copy the quantum state of one photon into the quantum state of a second one."



Plan

- ➊ Presentation
- ➋ Cryptography
- ➌ The qubit
- ➍ The photon: messenger of quantum information
- ➎ Entanglement and CHSH inequality
- ➏ Protocol E91
- ➐ Hands-on session

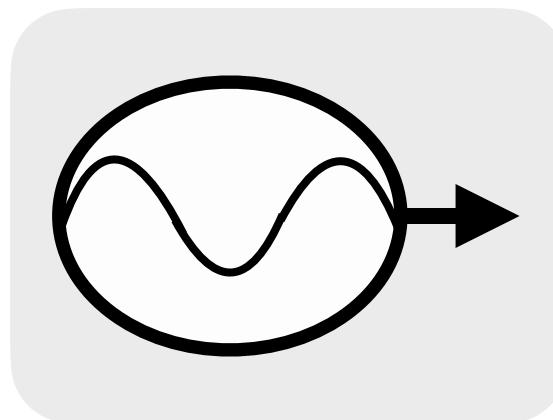
Plan

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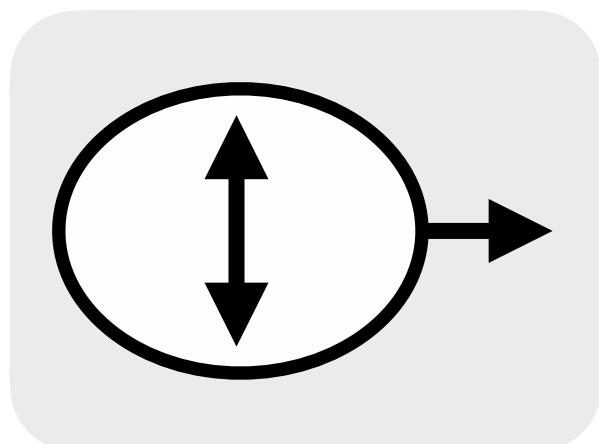
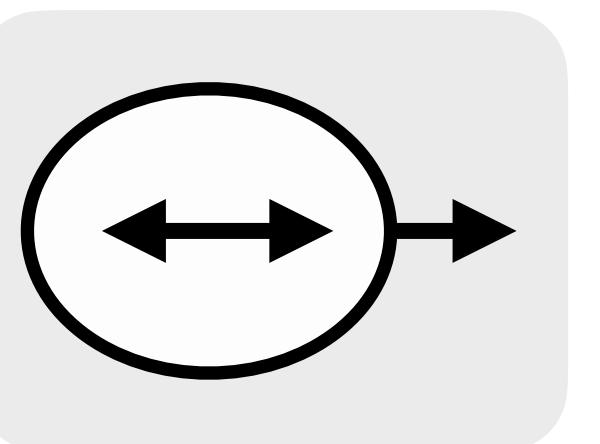
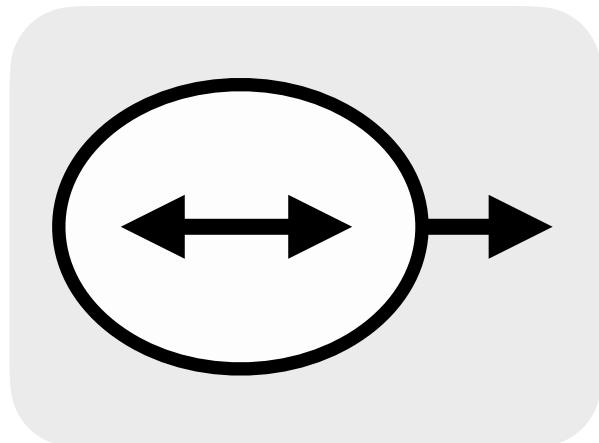
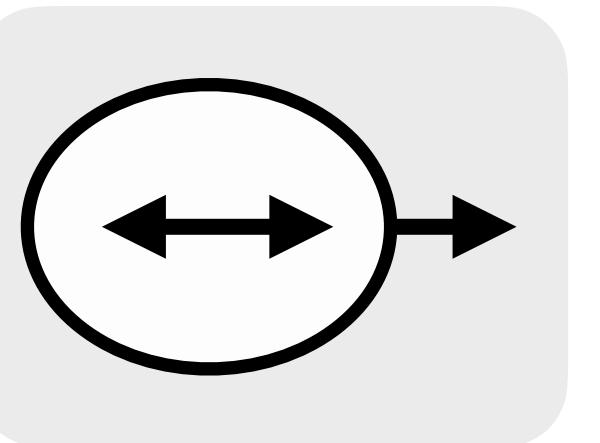
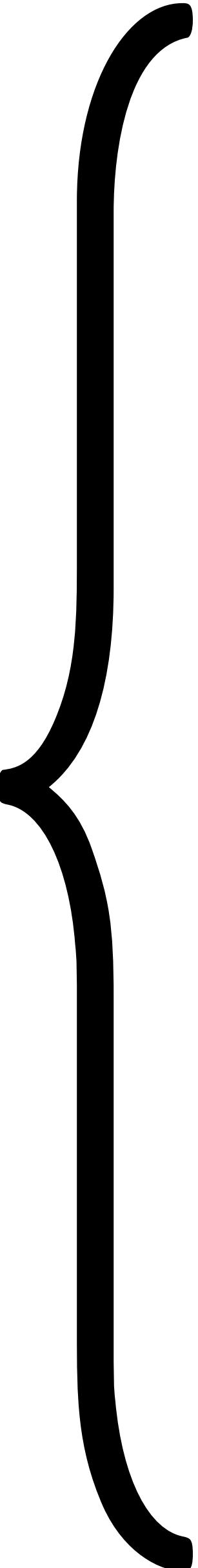
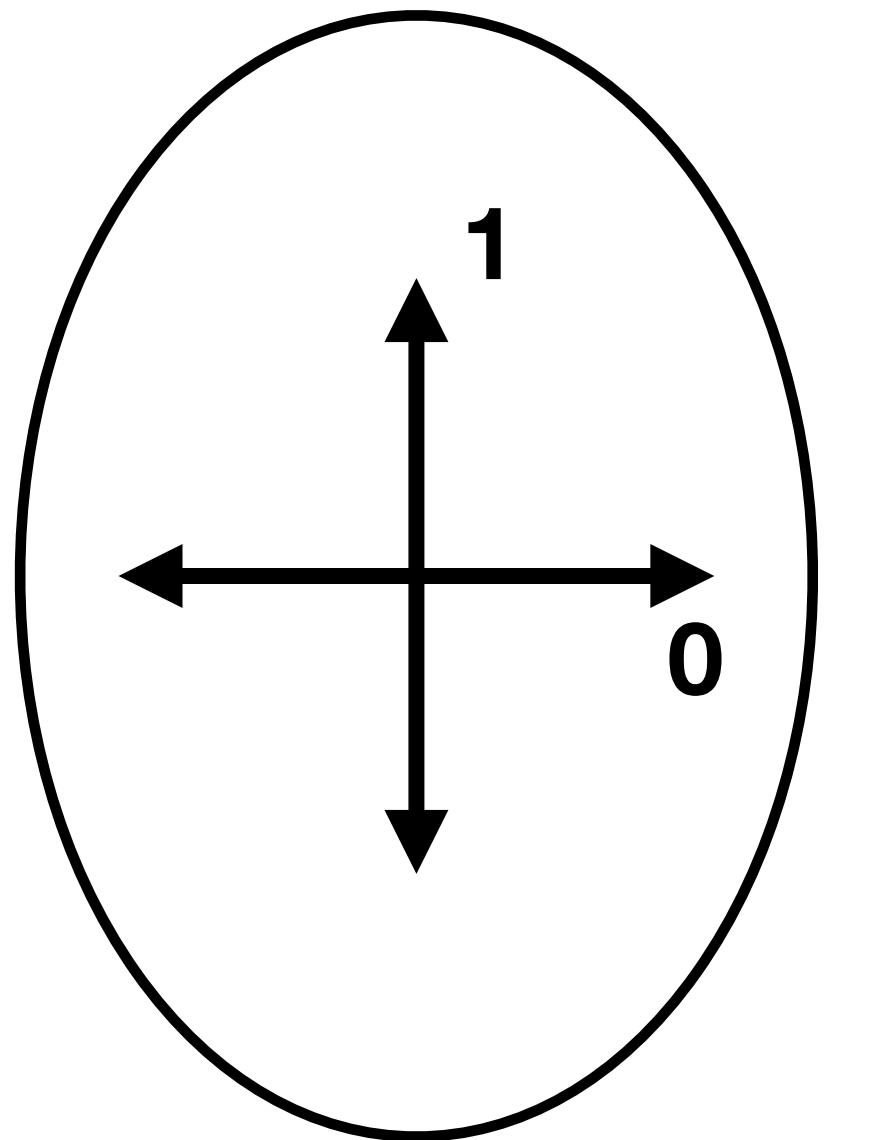
Plan

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Entanglement



$$\alpha | \leftrightarrow \leftrightarrow \rangle + \beta | \leftrightarrow \uparrow \downarrow \rangle \\ + \delta | \uparrow \leftrightarrow \rangle + \gamma | \uparrow \uparrow \downarrow \downarrow \rangle$$



$$P_{|\leftrightarrow\leftrightarrow\rangle} = |\alpha|^2$$

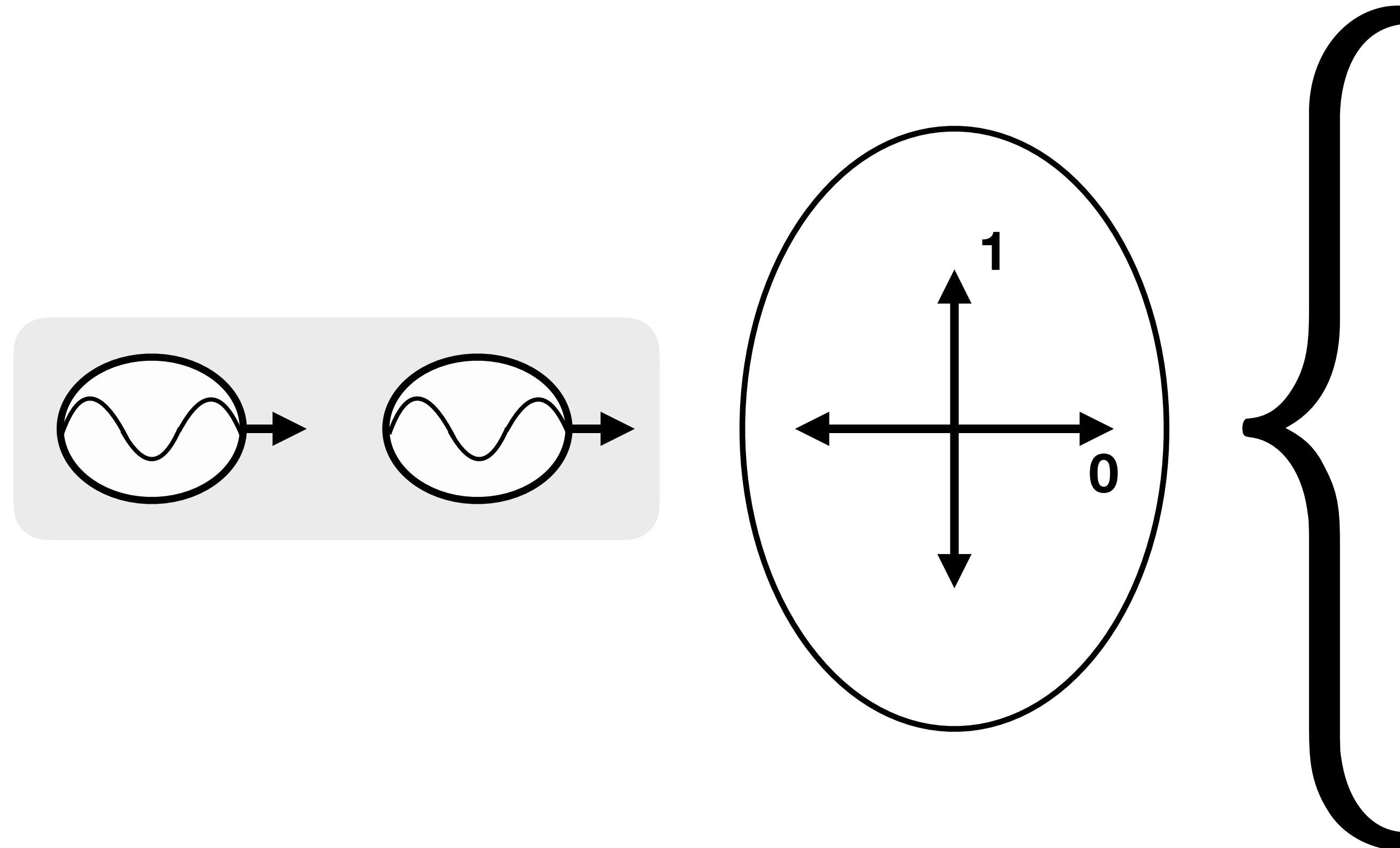
$$P_{|\leftrightarrow\uparrow\downarrow\rangle} = |\beta|^2$$

$$P_{|\uparrow\leftrightarrow\rangle} = |\delta|^2$$

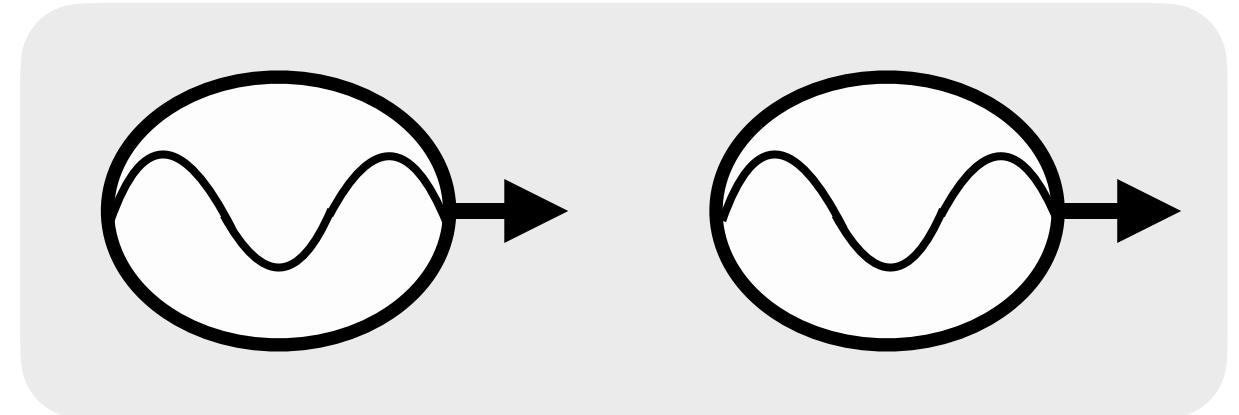
$$P_{|\uparrow\uparrow\downarrow\downarrow\rangle} = |\gamma|^2$$

$$|\alpha|^2 + |\beta|^2 + |\delta|^2 + |\gamma|^2 = 1$$

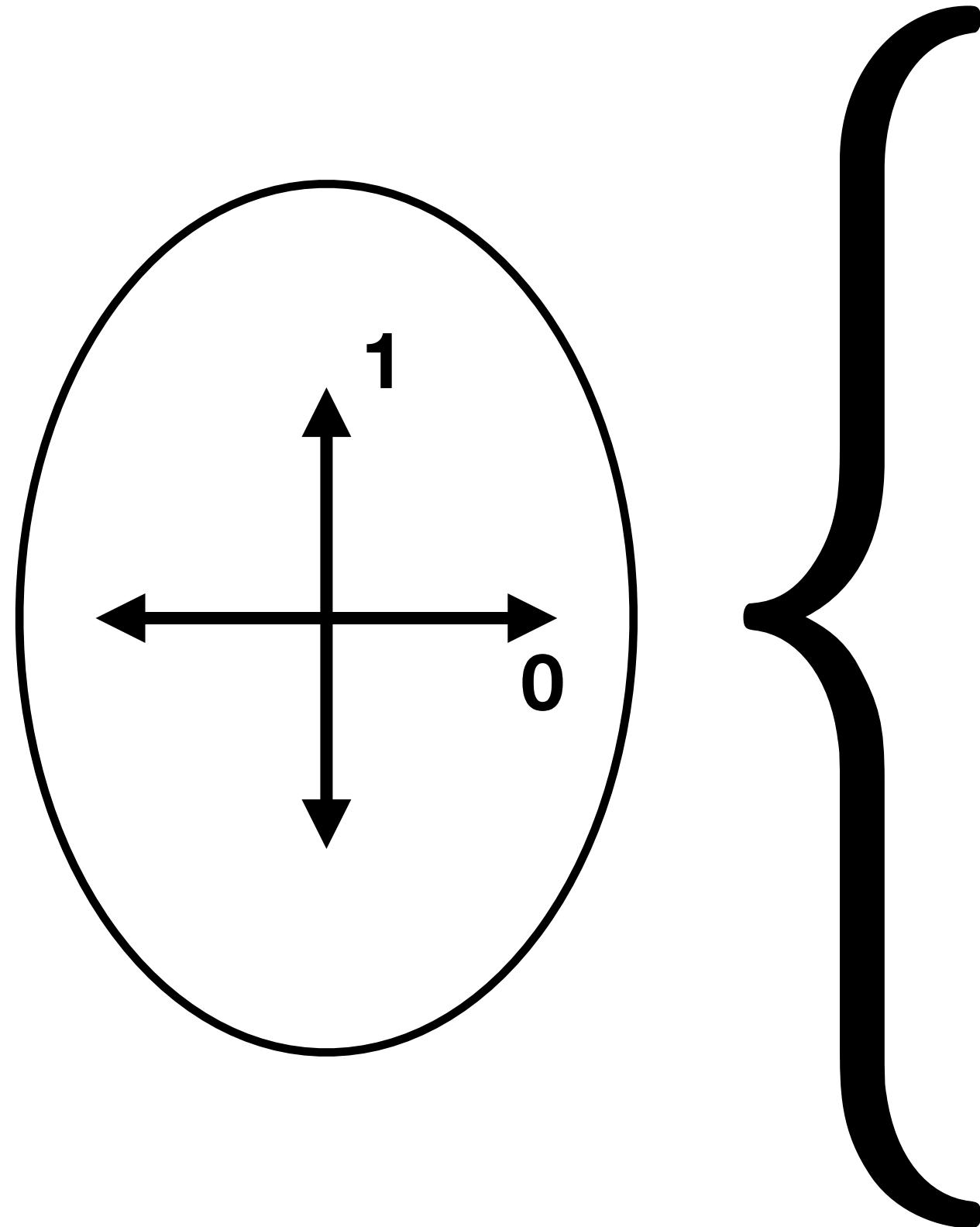
Entanglement



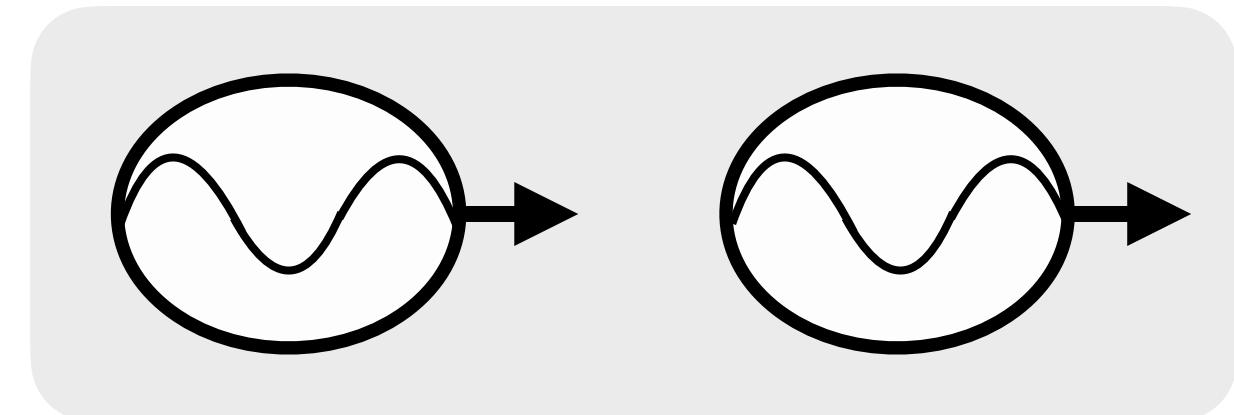
Entanglement



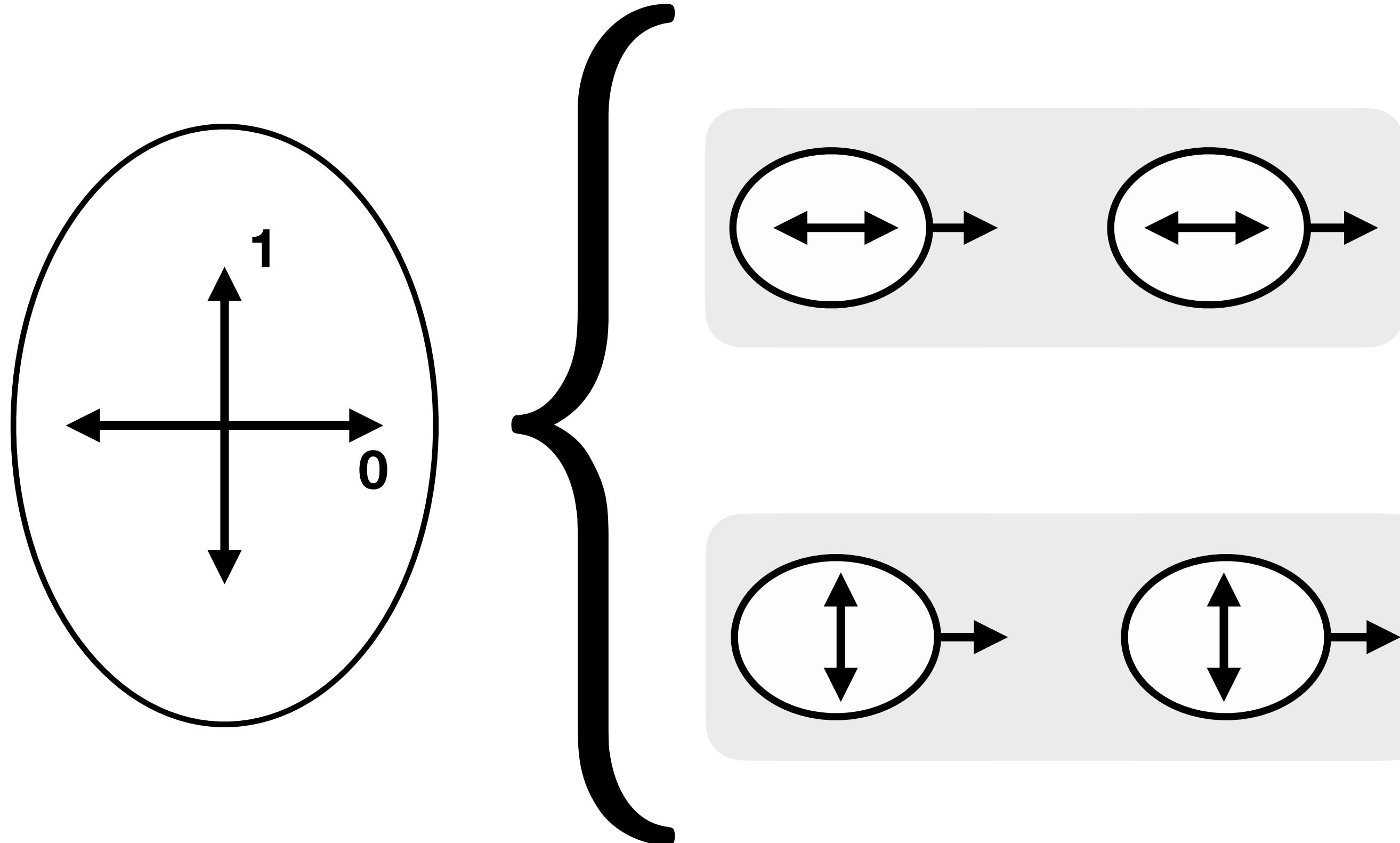
$$\frac{1}{\sqrt{2}} |\leftrightarrow\leftrightarrow\rangle + \frac{1}{\sqrt{2}} |\uparrow\downarrow\rangle$$



Entanglement



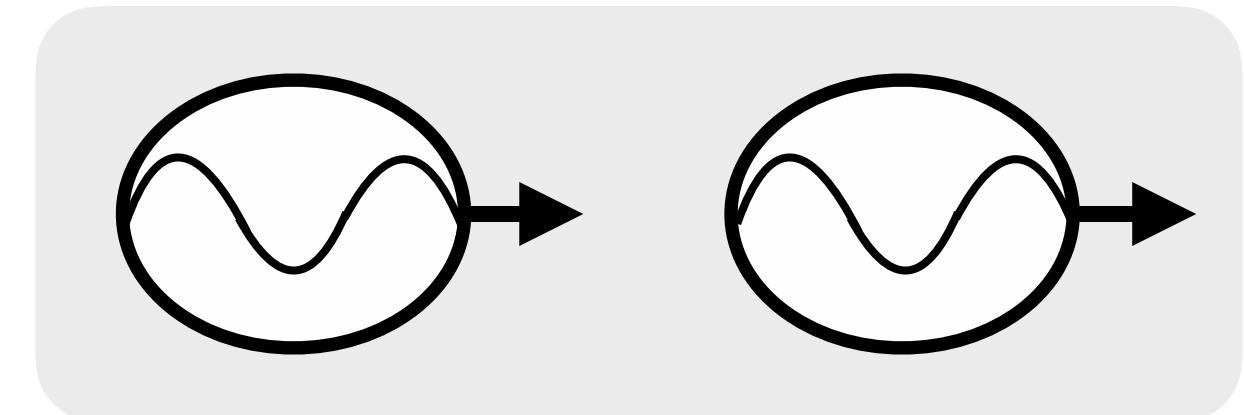
$$\frac{1}{\sqrt{2}} |\leftrightarrow \leftrightarrow\rangle + \frac{1}{\sqrt{2}} |\uparrow \downarrow \uparrow \downarrow\rangle$$



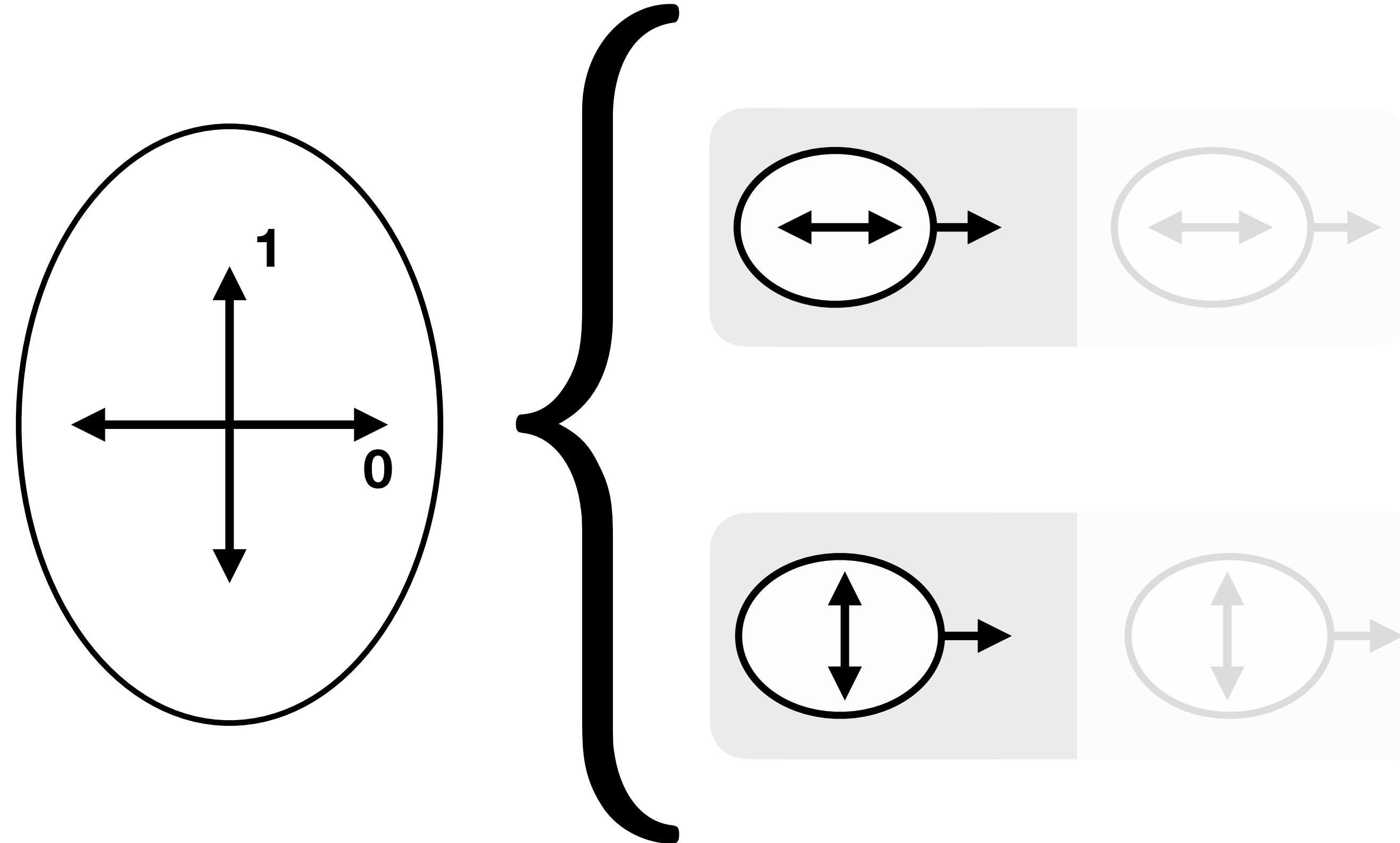
$$P_{|\leftrightarrow \leftrightarrow\rangle} = \frac{1}{2}$$

$$P_{|\uparrow \downarrow \uparrow \downarrow\rangle} = \frac{1}{2}$$

Entanglement



$$\frac{1}{\sqrt{2}} |\leftrightarrow\leftrightarrow\rangle + \frac{1}{\sqrt{2}} |\uparrow\downarrow\rangle$$



$$P_{|\leftrightarrow\leftrightarrow\rangle} = \frac{1}{2}$$

$$P_{|\uparrow\downarrow\rangle} = \frac{1}{2}$$

Bell Pairs

Φ^+

$$\frac{1}{\sqrt{2}} |\leftrightarrow\leftrightarrow\rangle + \frac{1}{\sqrt{2}} |\uparrow\downarrow\uparrow\downarrow\rangle$$

Φ^-

$$\frac{1}{\sqrt{2}} |\leftrightarrow\leftrightarrow\rangle - \frac{1}{\sqrt{2}} |\uparrow\downarrow\uparrow\downarrow\rangle$$

Ψ^+

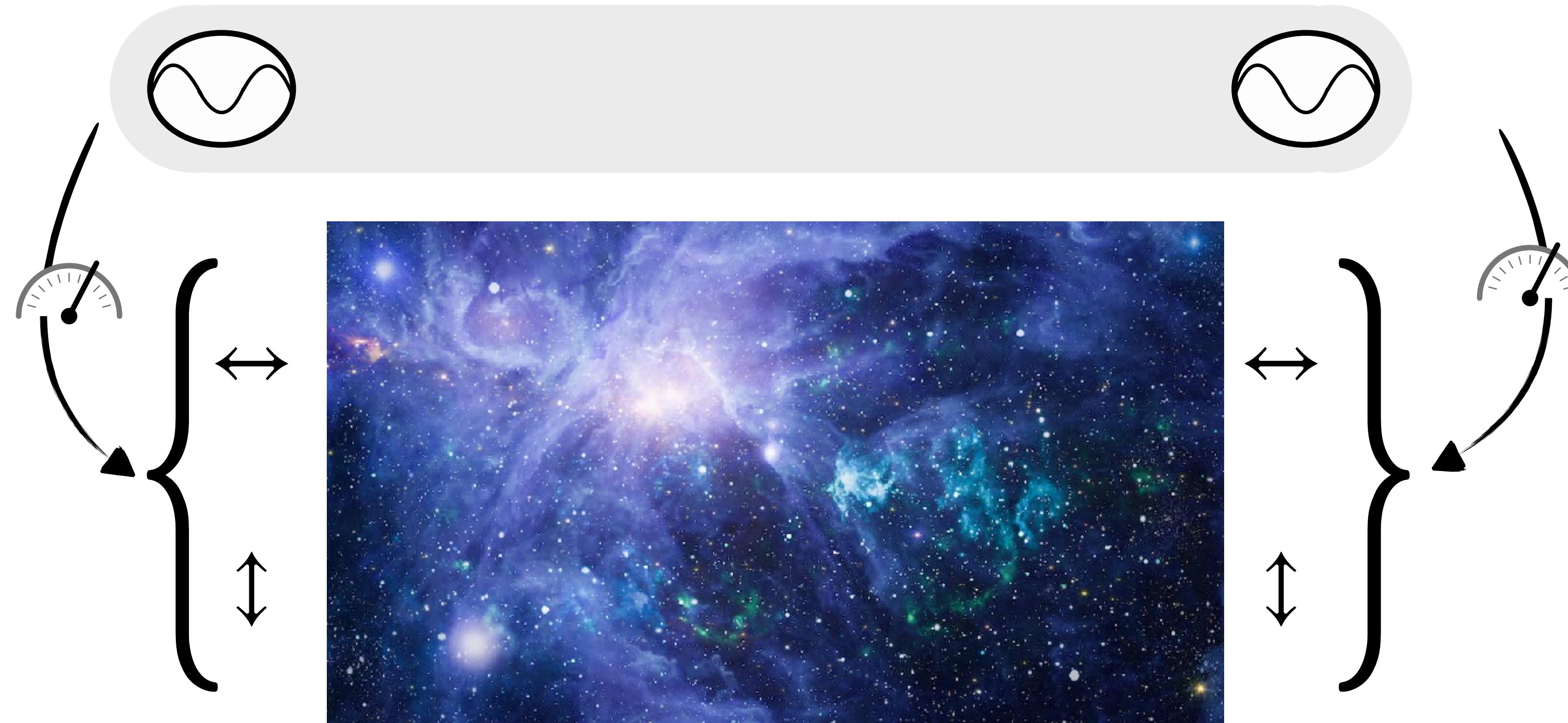
$$\frac{1}{\sqrt{2}} |\leftrightarrow\uparrow\downarrow\rangle + \frac{1}{\sqrt{2}} |\uparrow\downarrow\leftrightarrow\uparrow\downarrow\rangle$$

Ψ^-

$$\frac{1}{\sqrt{2}} |\leftrightarrow\uparrow\downarrow\rangle - \frac{1}{\sqrt{2}} |\uparrow\downarrow\leftrightarrow\uparrow\downarrow\rangle$$

Distance-independent correlations

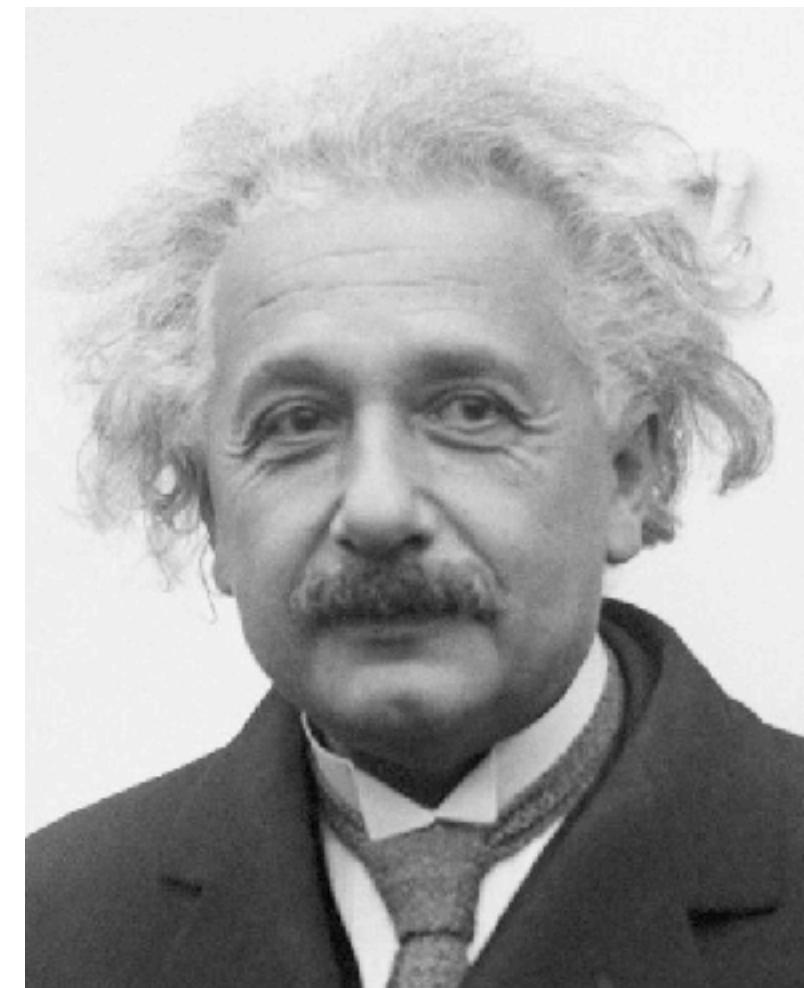
$$\frac{1}{\sqrt{2}} |\leftrightarrow\leftrightarrow\rangle + \frac{1}{\sqrt{2}} |\uparrow\downarrow\uparrow\rangle$$



Interpreting Entanglement



[AB Lægrelius & Westphal](#)



(Image credit: Bettmann / Contributor via Getty Images)

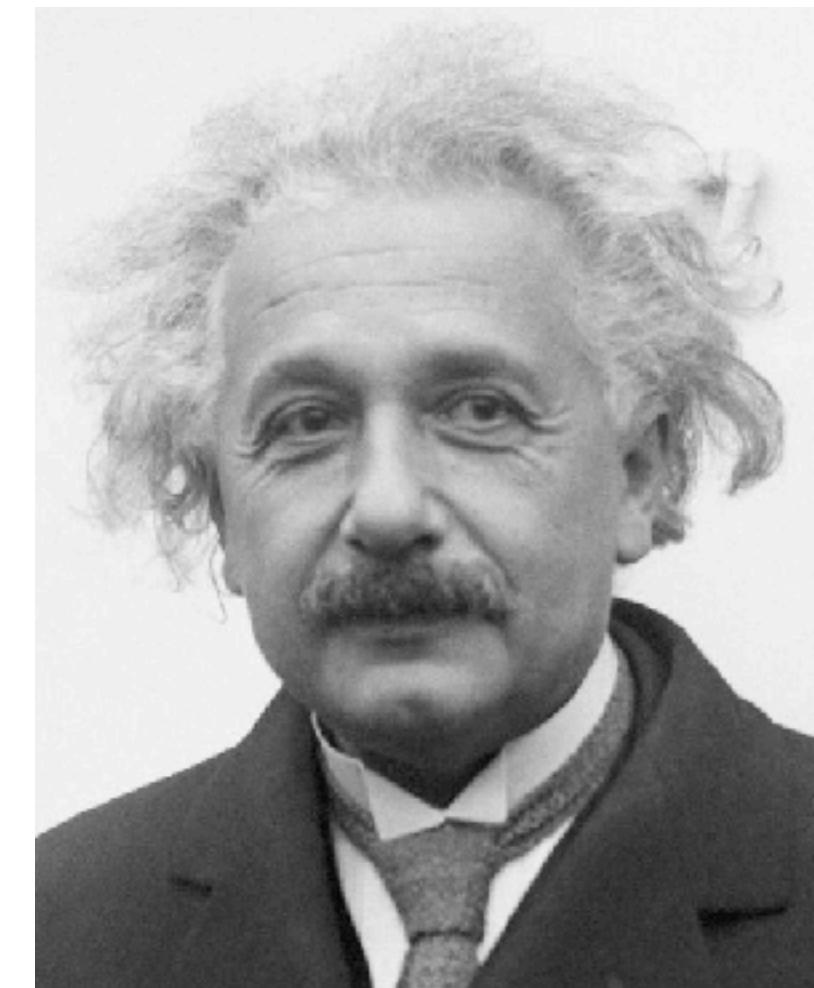
The measurement of the first entangled photon instantly determines the state of the second, regardless of the distance!

Interpreting Entanglement



[AB Lægrelius & Westphal](#)

The measurement of the first entangled photon instantly determines the state of the second, regardless of the distance!



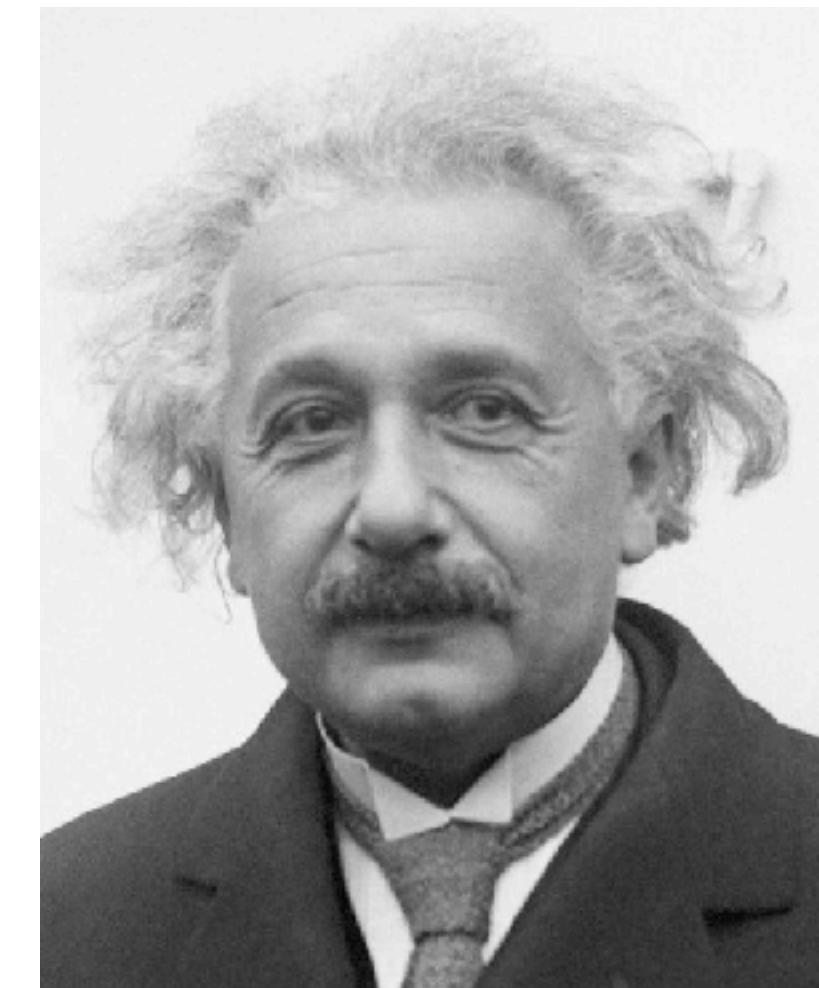
(Image credit: Bettmann / Contributor via Getty Images)

Impossible!
The choice of the state must be determined before the measurement!
There must be hidden variables!

Interpreting Entanglement



[AB Lægrelius & Westphal](#)



(Image credit: Bettmann / Contributor via Getty Images)

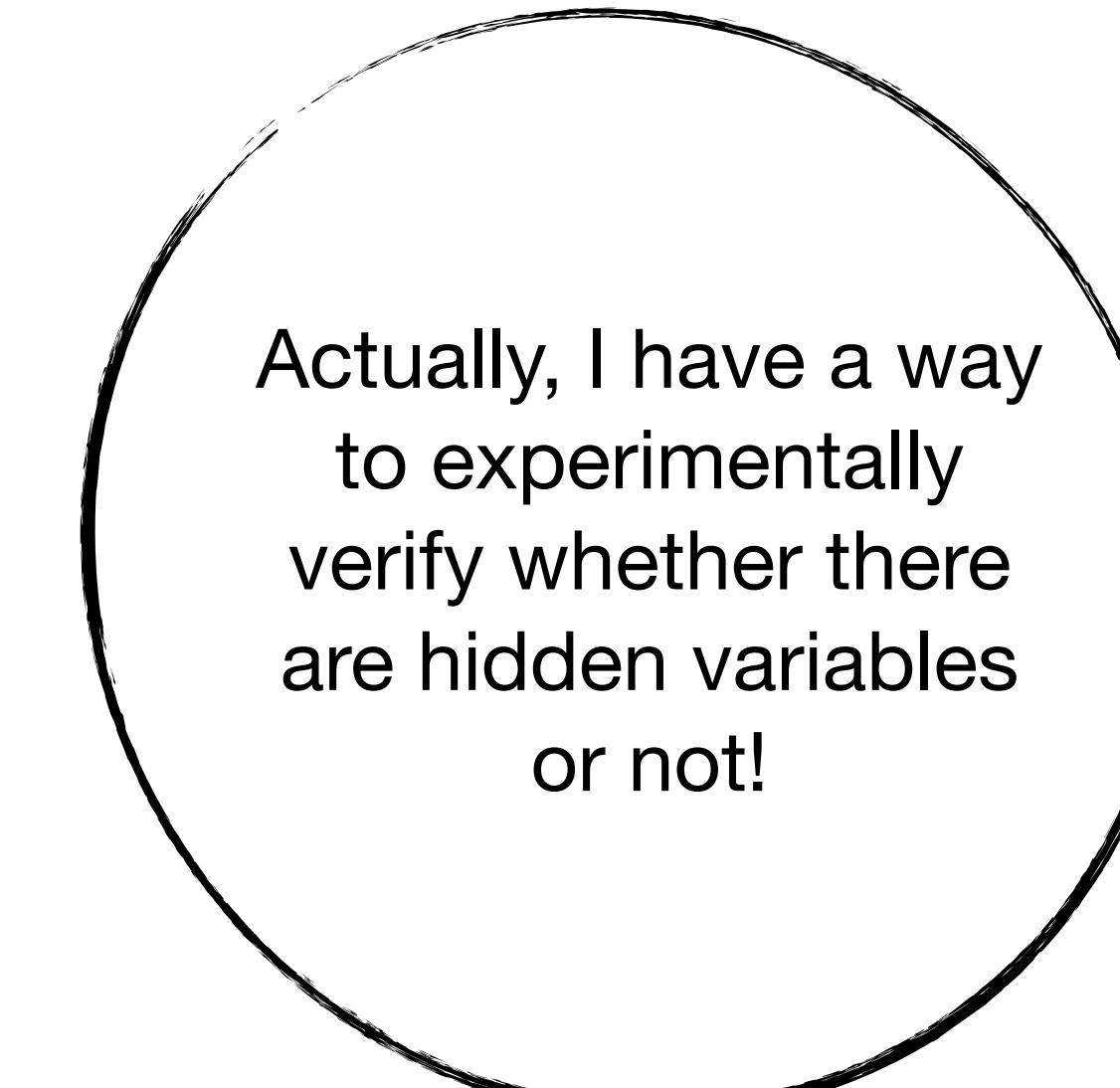
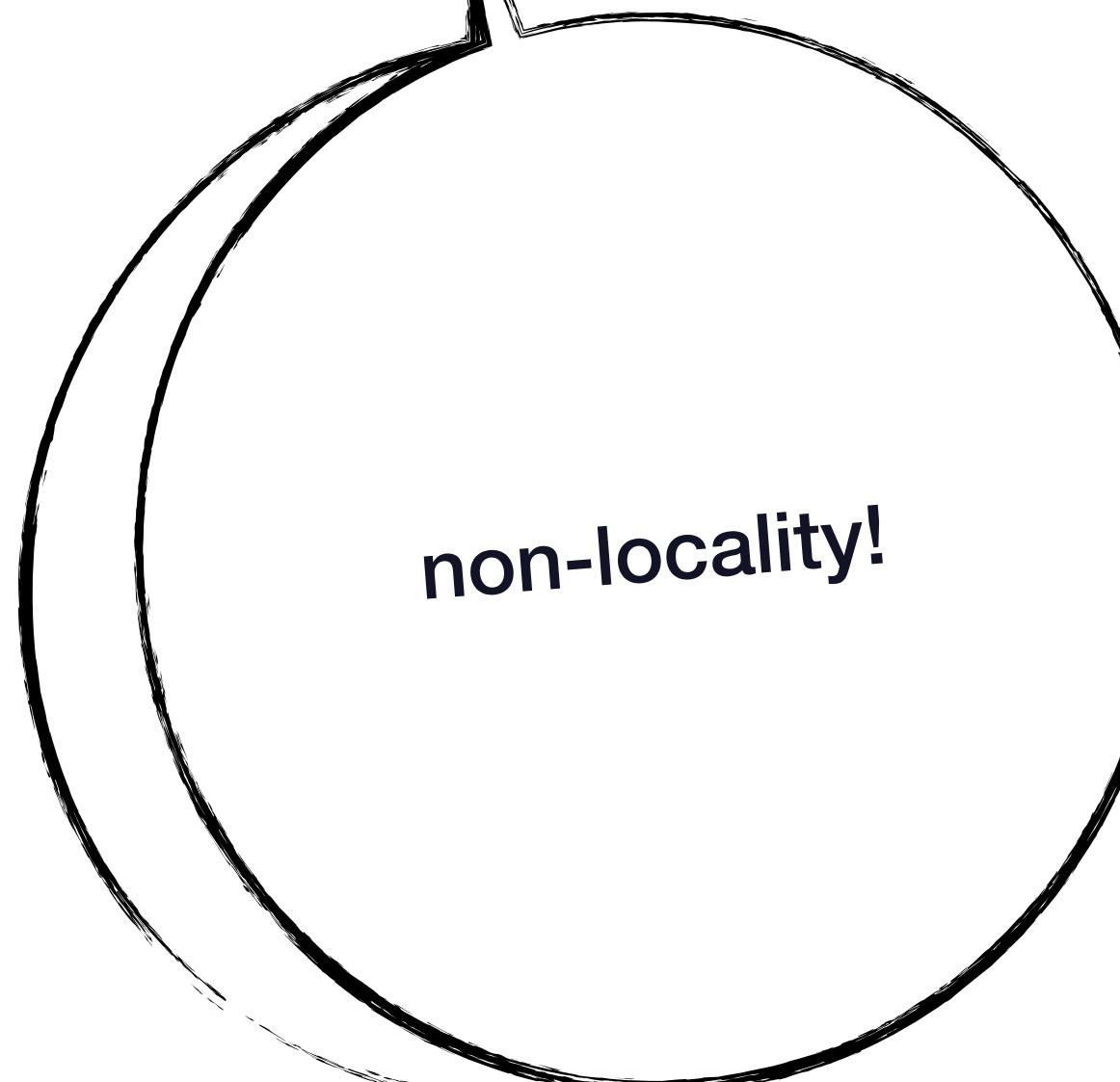
non-locality!

Impossible!
The choice of the
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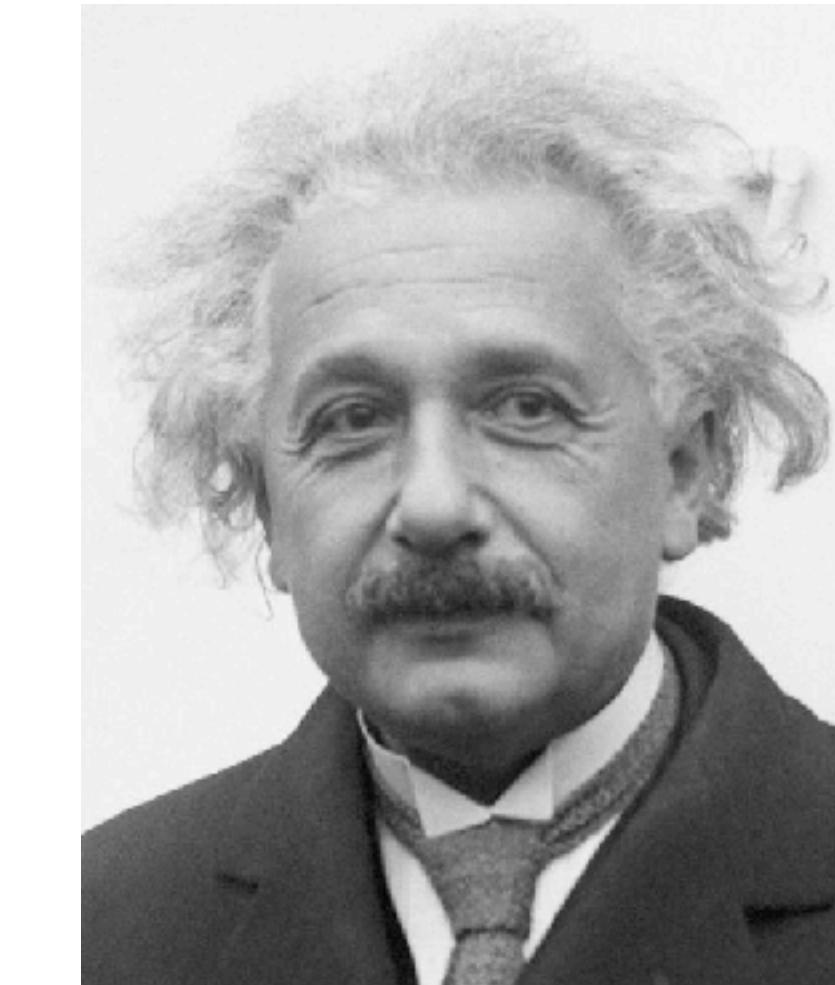
Interpreting Entanglement



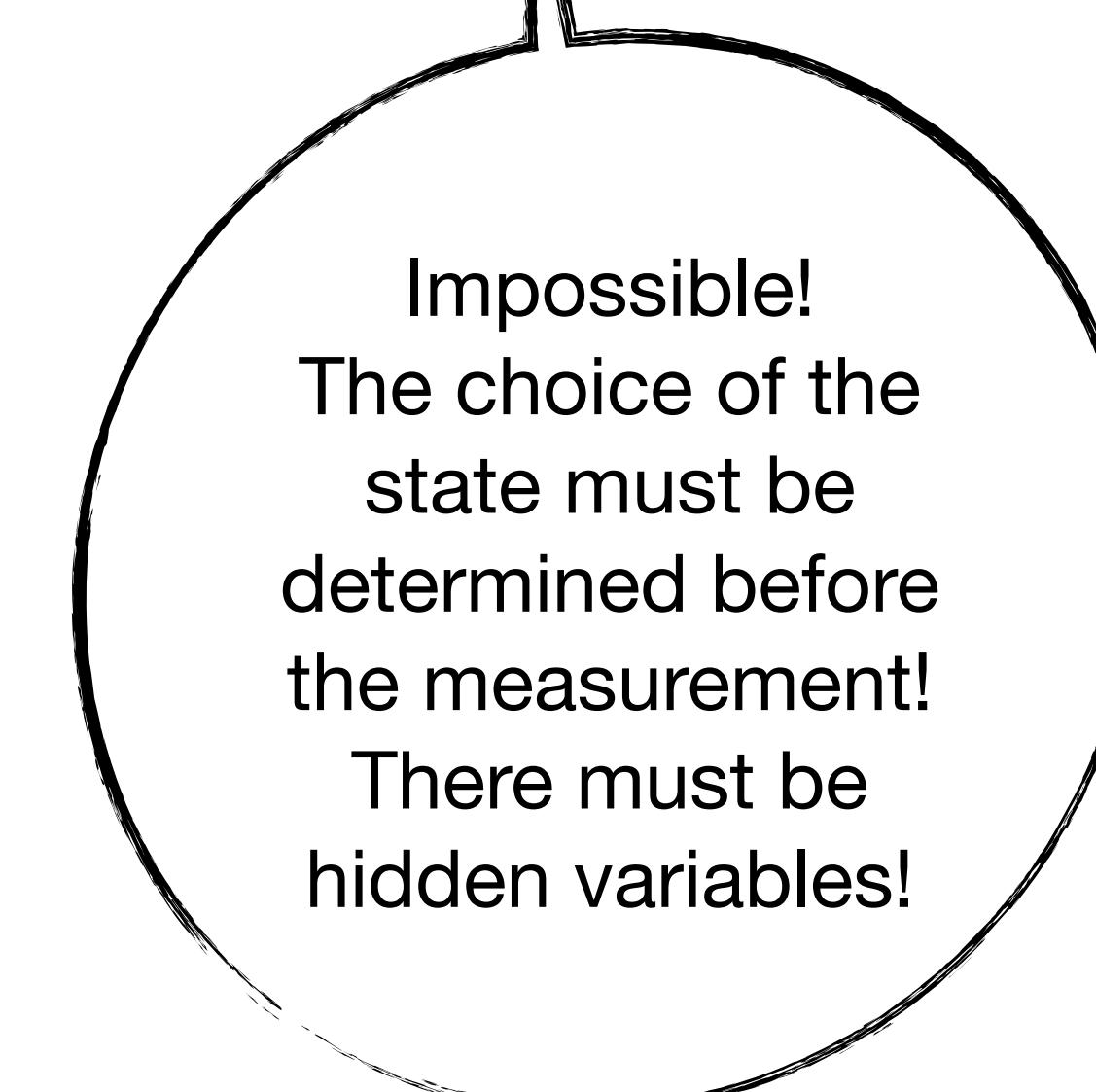
[AB Lagerlöf & Westphal](#)



1974, CERN



(Image credit: Bettmann / Contributor via Getty Images)



Interpreting Entanglement



Bell's Inequality

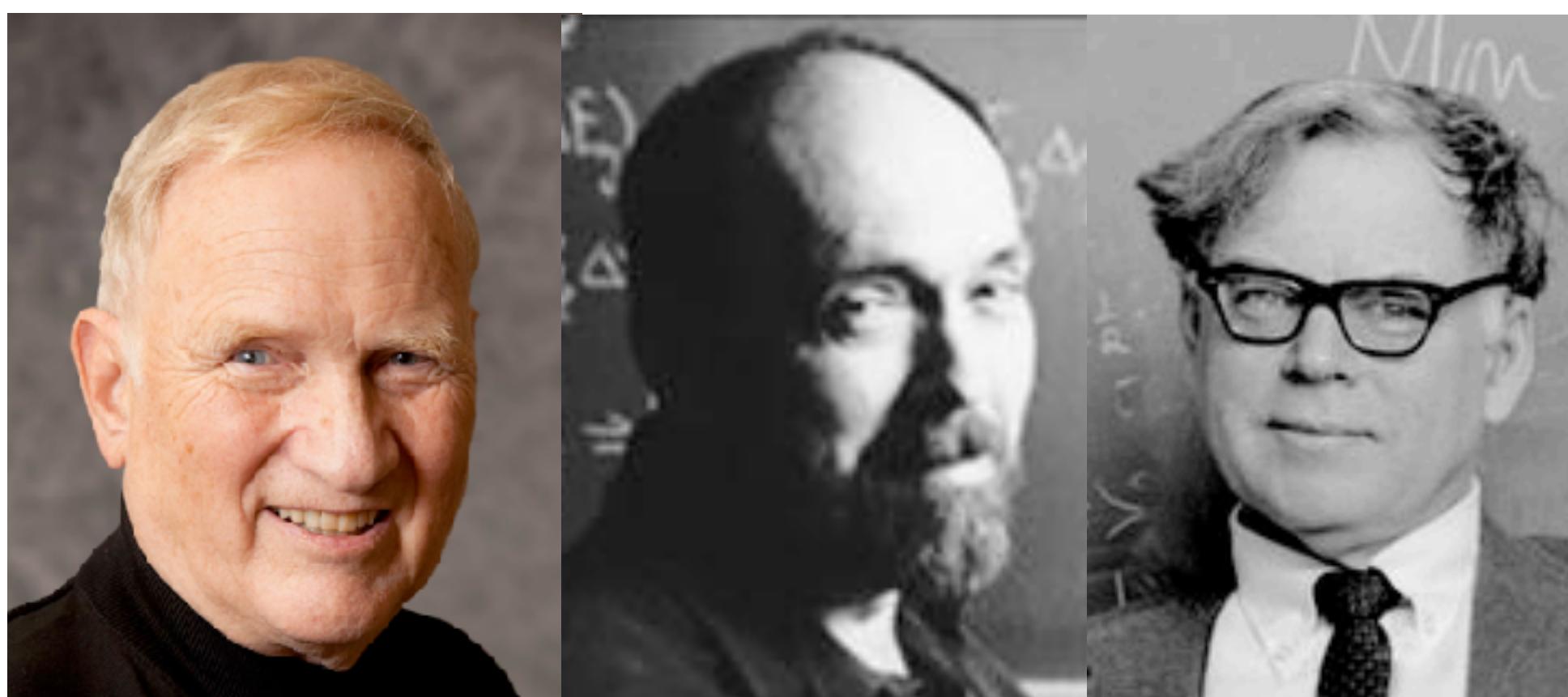
1974, CERN

Interpreting Entanglement



1964

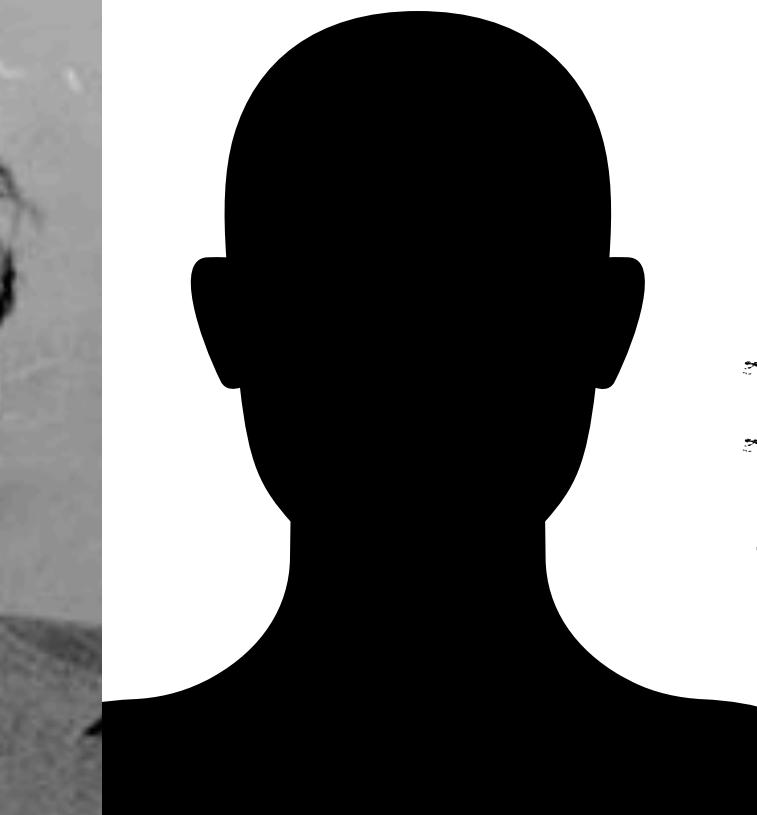
Bell's Inequality



John Clauser

Michael Horne

Abner Shimony



Richard Holt

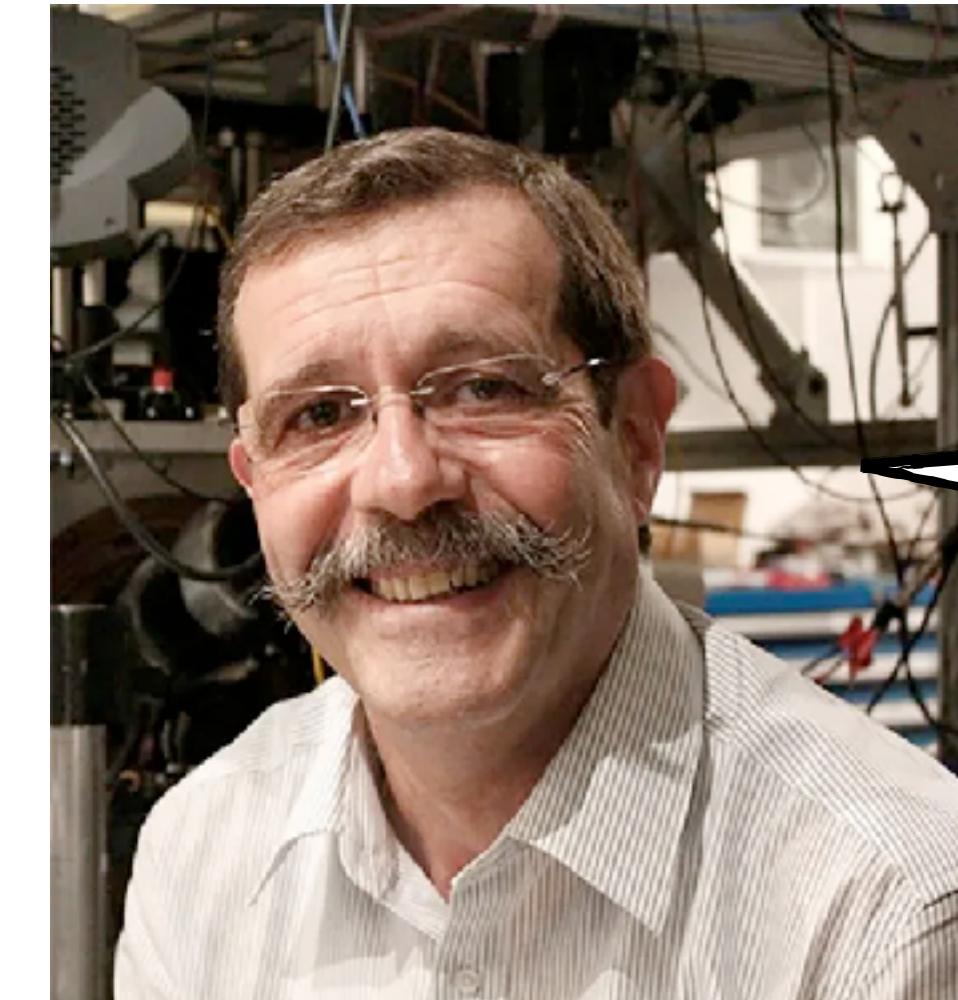
1969

CHSH Inequality

Interpreting Entanglement

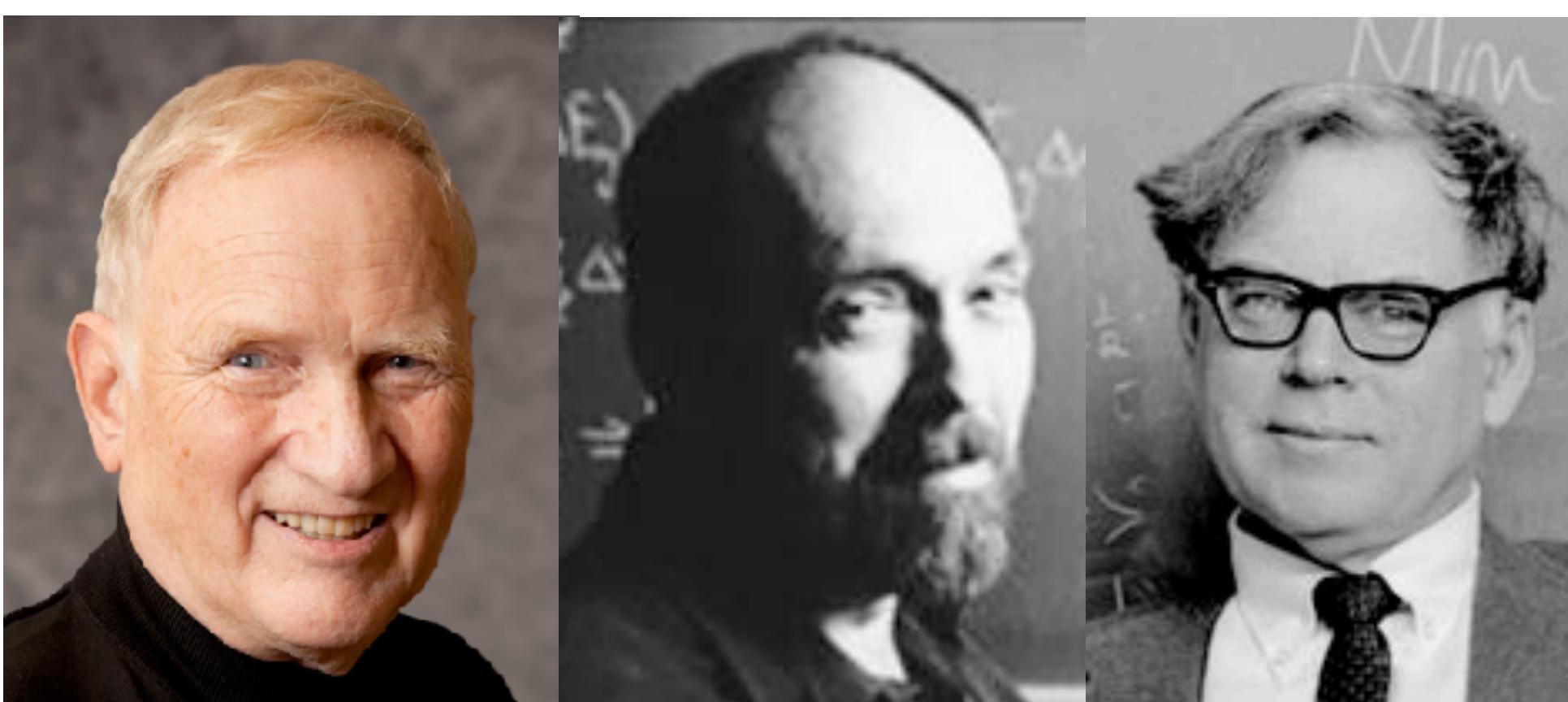


Bell's Inequality

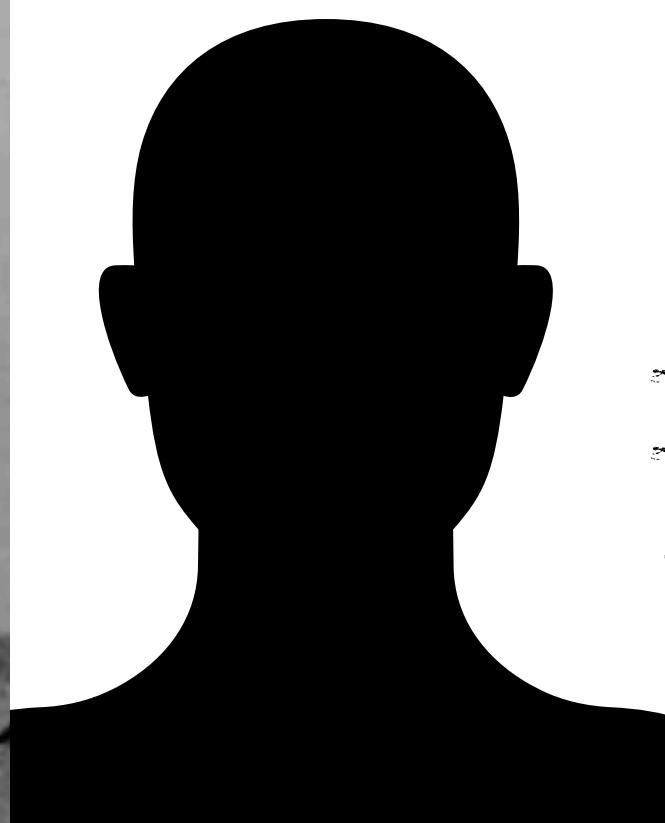


Entanglement
cannot be explained
by a hidden variable
theory!

**EXPERIMENTALLY
VERIFIED**

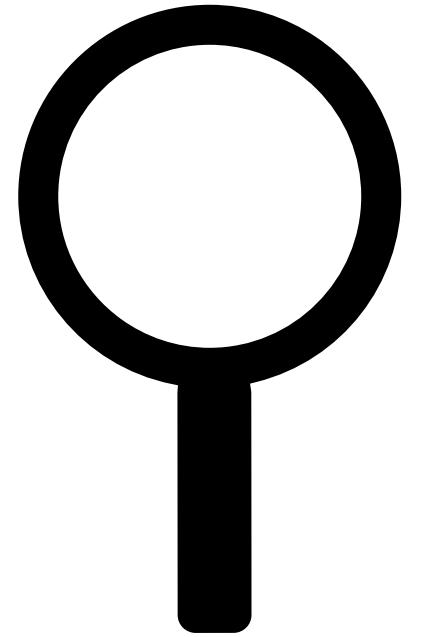


1969

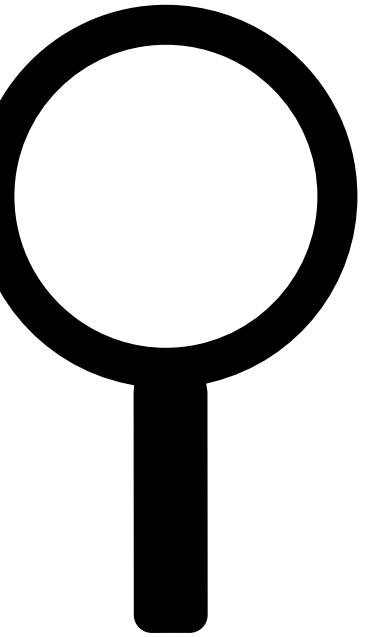
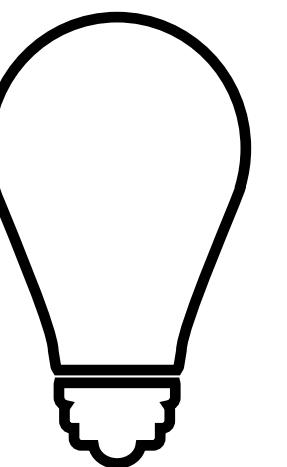


CHSH Inequality

Bell Test



A



B

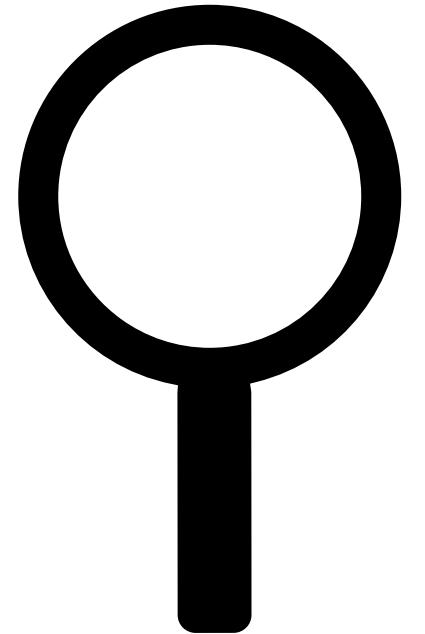
Bases: a_1, a_2

Results: {0, 1}

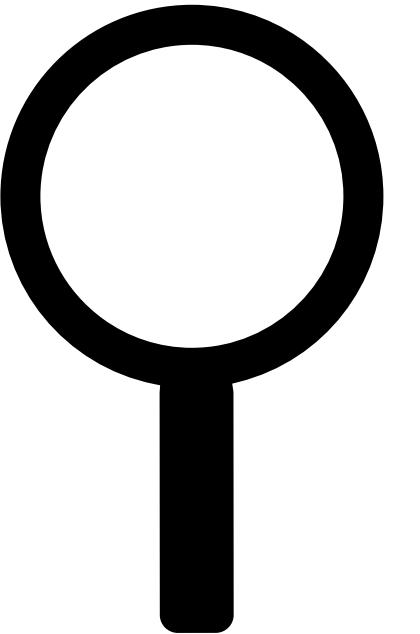
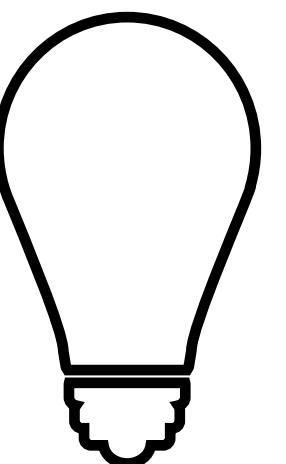
Bases: b_1, b_2

Results: {0, 1}

Bell Test



A



B

Bases: a_1, a_2

Results: ~~{0, 1}~~

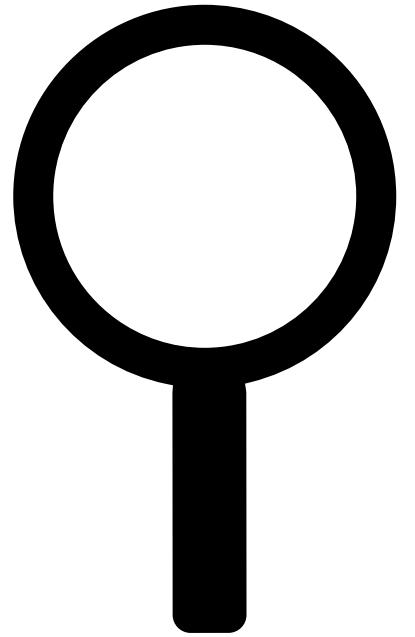
{+1, -1}

Bases: b_1, b_2

Results: ~~{0, 1}~~

{+1, -1}

Bell Test

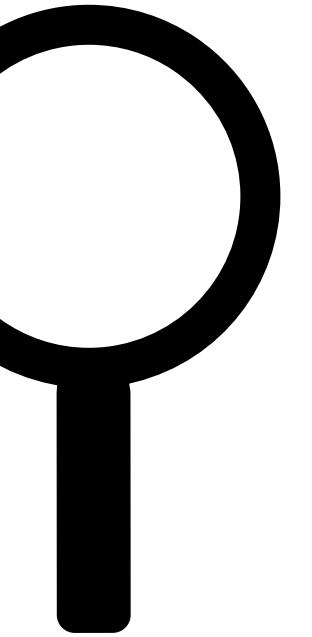
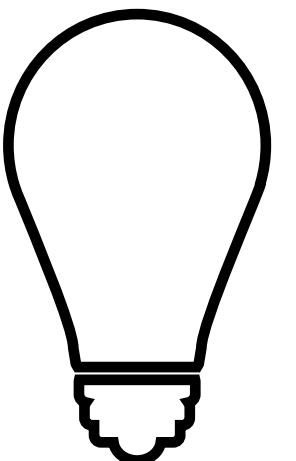


A

Bases: a_1, a_2

Results: ~~$\{0, 1\}$~~

$\{+1, -1\}$



B

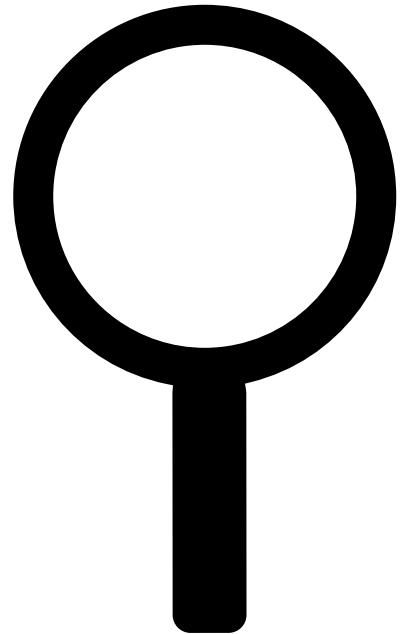
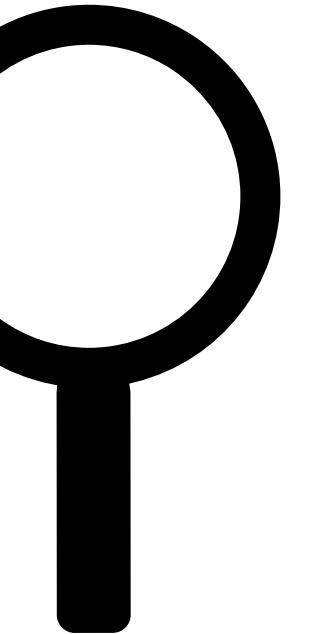
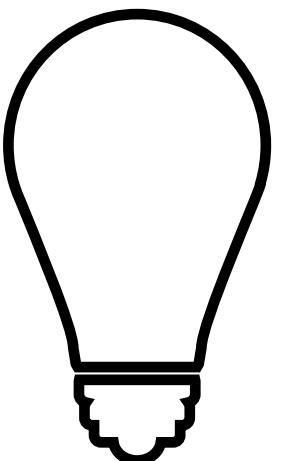
Bases: b_1, b_2

Results: ~~$\{0, 1\}$~~

$\{+1, -1\}$

a_i	b_j	$a_i b_j$
+1	+1	+1
+1	-1	-1
-1	+1	-1
-1	-1	+1

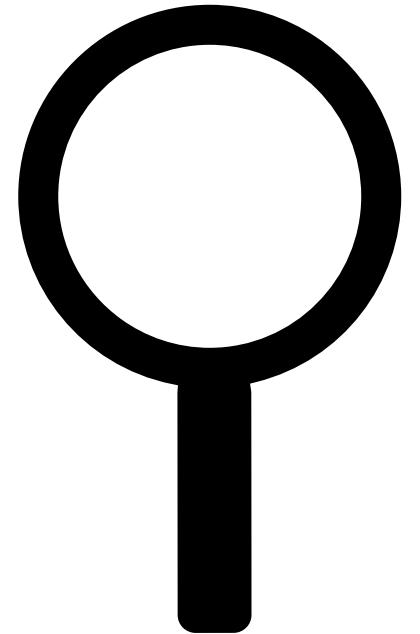
Bell Test

**A****Bases:** a_1, a_2 **Results:** ~~$\{0, 1\}$~~ $\{+1, -1\}$ **B****Bases:** b_1, b_2 **Results:** ~~$\{0, 1\}$~~ $\{+1, -1\}$

a_i	b_j	$a_i b_j$
+1	+1	+1
+1	-1	-1
-1	+1	-1
-1	-1	+1

Same values detected
at A and B

Bell Test

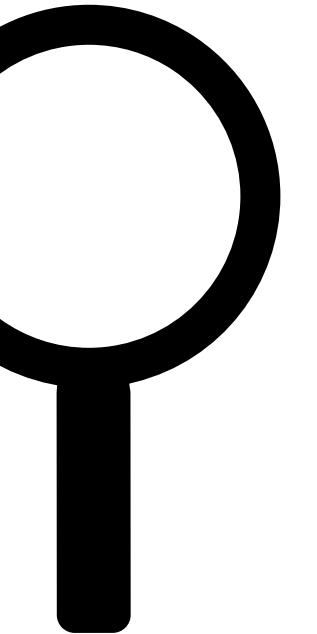
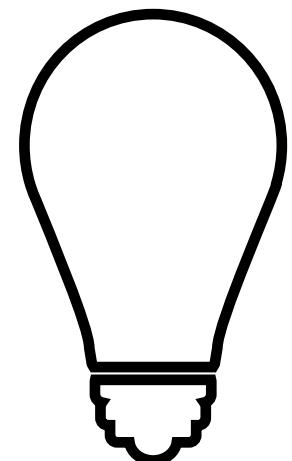


A

Bases: a_1, a_2

Results: ~~{0, 1}~~

{+1, -1}



B

Bases: b_1, b_2

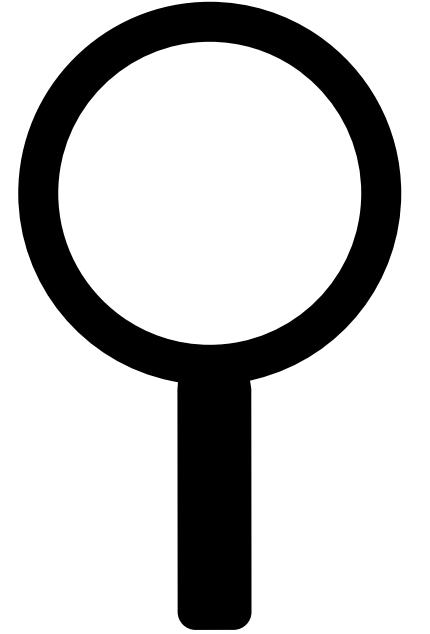
Results: ~~{0, 1}~~

{+1, -1}

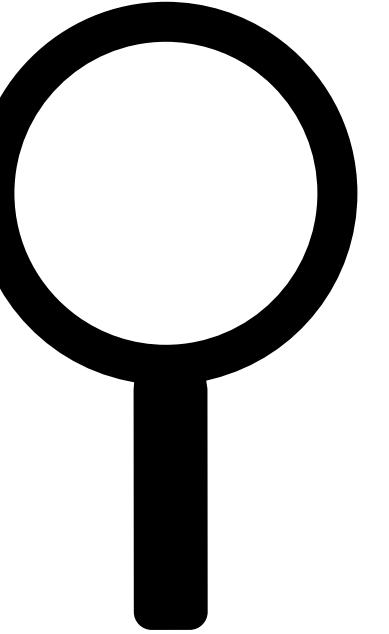
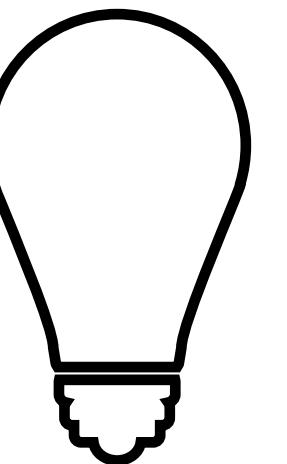
a_i	b_j	$a_i b_j$
+1	+1	+1
+1	-1	-1
-1	+1	-1
-1	-1	+1

Different values
detected at A and B

Bell Test



A



B

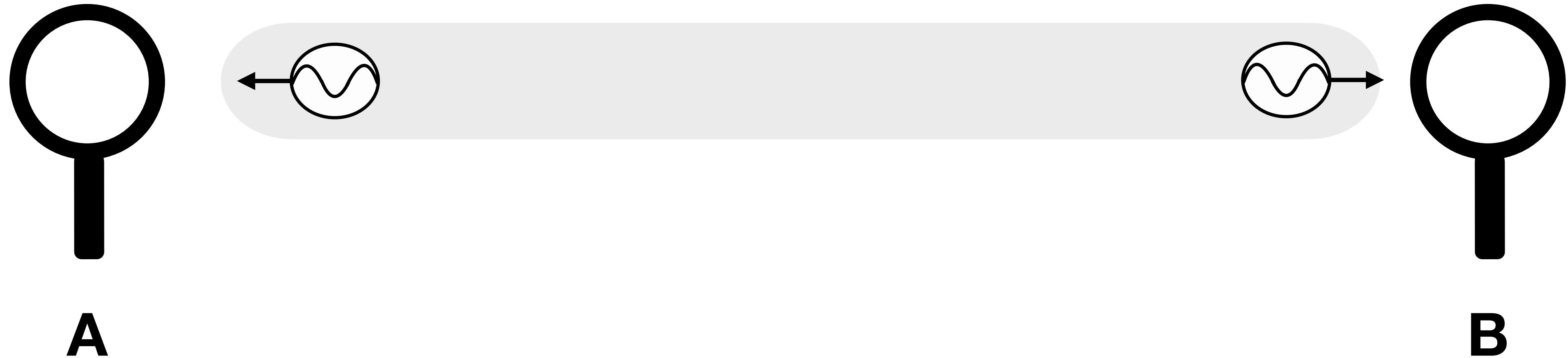
Bases: a_1, a_2

Results: $\{+1, -1\}$

Bases: b_1, b_2

Results: $\{+1, -1\}$

Bell Test



Bases: a_1, a_2

Results: $\{+1, -1\}$

Bases: b_1, b_2

Results: $\{+1, -1\}$

Bell Test



Bases: a_1, a_2

Results: $\{+1, -1\}$

Bases: b_1, b_2

Results: $\{+1, -1\}$

Bell Test



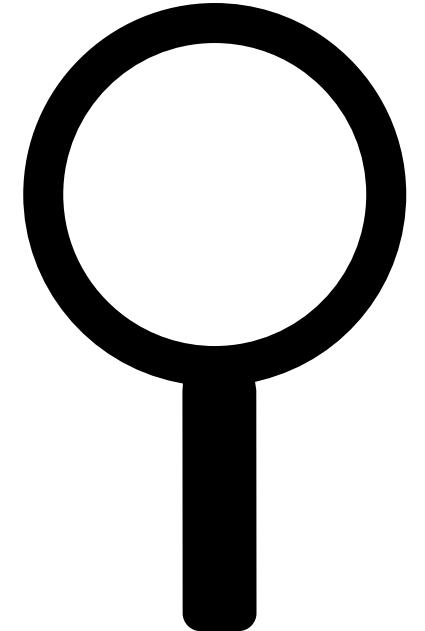
Bases: a_1, a_2

Results: $\{+1, -1\}$

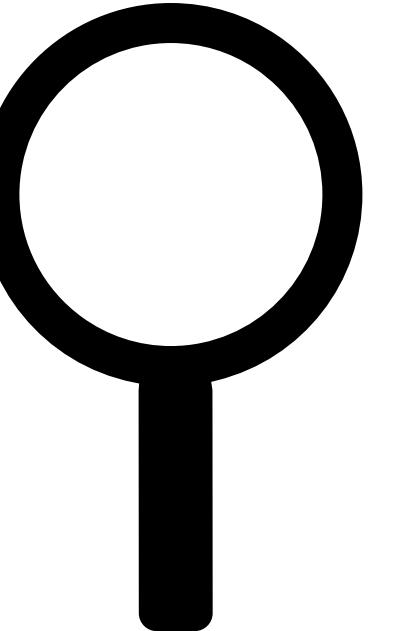
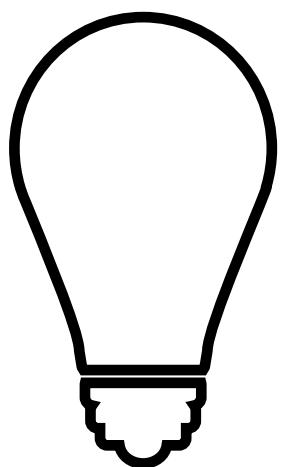
Bases: b_1, b_2

Results: $\{+1, -1\}$

Bell Test



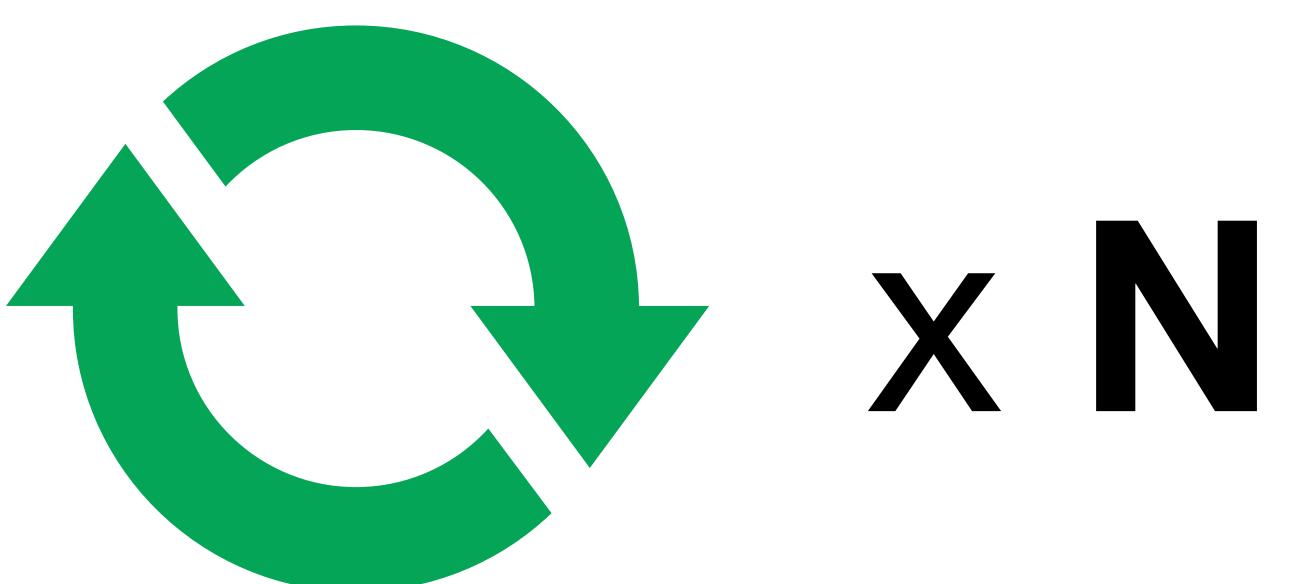
A



B

Bases: a_1, a_2

Results: $\{+1, -1\}$



Bases: b_1, b_2

Results: $\{+1, -1\}$



CHSH Inequality

$$S = |E_{a_1, b_1} + E_{a_2, b_1} + E_{a_2, b_2} - E_{a_1, b_2}|$$

$$E_{a_i, b_j} = \frac{1}{n} \sum_{k=0}^n a_i b_j$$



CHSH Inequality

$$S = |E_{a_1, b_1} + E_{a_2, b_1} + E_{a_2, b_2} - E_{a_1, b_2}|$$

$$E_{a_i, b_j} = \frac{1}{n} \sum_{k=0}^n a_i b_j$$

E_{a_i, b_j}

Interpretation

1 $a_i = b_j$ is always true

-1 $a_i = -b_j$ is always true

0 a_i and b_j are independant of each other



CHSH Inequality

$$S = |E_{a_1, b_1} + E_{a_2, b_1} + E_{a_2, b_2} - E_{a_1, b_2}|$$

$$E_{a_i, b_j} = \frac{1}{n} \sum_{k=0}^n a_i b_j$$

$$S' = a_1 b_1 + a_1 b_2 + a_2 b_2 - a_1 b_2$$



CHSH Inequality

$$S = |E_{a_1, b_1} + E_{a_2, b_1} + E_{a_2, b_2} - E_{a_1, b_2}|$$

$$E_{a_i, b_j} = \frac{1}{n} \sum_{k=0}^n a_i b_j$$

$$\begin{aligned} S' &= a_1 b_1 + a_1 b_2 + a_2 b_2 - a_1 b_2 \\ &= a_1(b_1 - b_2) + a_2(b_1 + b_2) \end{aligned}$$



CHSH Inequality

$$S = |E_{a_1, b_1} + E_{a_2, b_1} + E_{a_2, b_2} - E_{a_1, b_2}|$$

$$E_{a_i, b_j} = \frac{1}{n} \sum_{k=0}^n a_i b_j$$

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b_1	b_2	$b_1 - b_2$	$b_1 + b_2$
+1	+1	0	2
+1	-1	2	0
-1	+1	-2	0
-1	-1	0	-2



CHSH Inequality

$$S = |E_{a_1, b_1} + E_{a_2, b_1} + E_{a_2, b_2} - E_{a_1, b_2}|$$

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+1	+1	0	2
+1	-1	2	0
-1	+1	-2	0
-1	-1	0	-2



CHSH Inequality

$$S = |E_{a_1, b_1} + E_{a_2, b_1} + E_{a_2, b_2} - E_{a_1, b_2}|$$

$$E_{a_i, b_j} = \frac{1}{n} \sum_{k=0}^n a_i b_j$$

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+1	+1	0	2
+1	-1	2	0
-1	+1	-2	0
-1	-1	0	-2

$$|S'| \leq 2$$



CHSH Inequality

$$S = |E_{a_1, b_1} + E_{a_2, b_1} + E_{a_2, b_2} - E_{a_1, b_2}|$$

$$E_{a_i, b_j} = \frac{1}{n} \sum_{k=0}^n a_i b_j$$

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+1	+1	0	2
+1	-1	2	0
-1	+1	-2	0
-1	-1	0	-2

$$|S'| \leq 2$$

The results could be explained by hidden variables



CHSH Inequality

$$S = |E_{a_1, b_1} + E_{a_2, b_1} + E_{a_2, b_2} - E_{a_1, b_2}|$$

$$E_{a_i, b_j} = \frac{1}{n} \sum_{k=0}^n a_i b_j$$

$$\begin{aligned} S' &= a_1 b_1 + a_1 b_2 + a_2 b_2 - a_1 b_2 \\ &= a_1(b_1 - b_2) + a_2(b_1 + b_2) \end{aligned}$$

b_1	b_2	$b_1 - b_2$	$b_1 + b_2$
+1	+1	0	2
+1	-1	2	0
-1	+1	-2	0
-1	-1	0	-2

$$|S'| \leq 2$$

Classical

The results could be explained by hidden variables



CHSH Inequality

$$S = |E_{a_1,b_1} + E_{a_2,b_1} + E_{a_2,b_2} - E_{a_1,b_2}| \{ \leq 2 \text{ Classical}$$



CHSH Inequality

$$S = |E_{a_1,b_1} + E_{a_2,b_1} + E_{a_2,b_2} - E_{a_1,b_2}| \{ \begin{array}{l} \leq 2 \text{ Classical} \\ \in]2, 2\sqrt{2}] \text{ With Bell Pairs!} \end{array}$$



CHSH Inequality

$$S = |E_{a_1,b_1} + E_{a_2,b_1} + E_{a_2,b_2} - E_{a_1,b_2}| \{ \begin{array}{l} \leq 2 \text{ Classical} \\ \in [2, 2\sqrt{2}] \text{ Quantum Maximum} \end{array}$$

Computing the CHSH Inequality

$$S = |E_{a_1,b_1} + E_{a_2,b_1} + E_{a_2,b_2} - E_{a_1,b_2}| \{ \begin{array}{l} \leq 2 \text{ Classical} \\ \in [2, 2\sqrt{2}] \text{ Quantum Maximum} \end{array}$$

A		B		$a_i \cdot b_j$
Basis	Result	Basis	Result	
a_1	+1	b_1	+1	+1
a_1	+1	b_1	-1	-1
a_1	-1	b_1	-1	+1

$$E_{a_1,b_1} = \frac{1 - 1 + 1}{3} = \frac{1}{3}$$

$$E_{a_i,b_j} = \frac{1}{n} \sum_{k=0}^n a_i b_j$$



Computing the CHSH Inequality

$$S = |E_{a_1,b_1} + E_{a_2,b_1} + E_{a_2,b_2} - E_{a_1,b_2}| \{ \begin{array}{l} \leq 2 \text{ Classical} \\ \in [2, 2\sqrt{2}] \text{ Quantum Maximum} \end{array}$$

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a_1	-1	b_1	-1	+1
a_2	+1	b_1	+1	+1
a_2	-1	b_1	+1	-1

$$E_{a_1,b_1} = \frac{1 - 1 + 1}{3} = \frac{1}{3}$$

$$E_{a_2,b_1} = \frac{1 - 1}{3} = 0$$



Computing the CHSH Inequality

$$S = |E_{a_1,b_1} + E_{a_2,b_1} + E_{a_2,b_2} - E_{a_1,b_2}| \{ \begin{array}{l} \leq 2 \text{ Classical} \\ \in [2, 2\sqrt{2}] \text{ Quantum Maximum} \end{array}$$

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$$E_{a_1,b_1} = \frac{1 - 1 + 1}{3} = \frac{1}{3}$$

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$$E_{a_2,b_2} = \frac{1}{1} = 1$$



Computing the CHSH Inequality

$$S = |E_{a_1,b_1} + E_{a_2,b_1} + E_{a_2,b_2} - E_{a_1,b_2}| \{ \begin{array}{l} \leq 2 \text{ Classical} \\ \in [2, 2\sqrt{2}] \text{ Quantum Maximum} \end{array}$$

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a_1	-1	b_1	-1	+1
a_2	+1	b_1	+1	+1
a_2	-1	b_1	+1	-1
a_2	+1	b_2	+1	+1

$$E_{a_1,b_1} = \frac{1 - 1 + 1}{3} = \frac{1}{3}$$

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$$E_{a_2,b_2} = \frac{1}{1} = 1$$

$$E_{a_1,b_2} = 0$$



Computing the CHSH Inequality

$$S = |E_{a_1,b_1} + E_{a_2,b_1} + E_{a_2,b_2} - E_{a_1,b_2}| \{ \begin{array}{l} \leq 2 \text{ Classical} \\ \in [2, 2\sqrt{2}] \text{ Quantum Maximum} \end{array}$$

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Basis	Result	Basis	Result	
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a_1	+1	b_1	-1	-1
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a_2	-1	b_1	+1	-1
a_2	+1	b_2	+1	+1

$$E_{a_1,b_1} = \frac{1 - 1 + 1}{3} = \frac{1}{3}$$

$$E_{a_2,b_1} = \frac{1 - 1}{3} = 0$$

$$E_{a_2,b_2} = \frac{1}{1} = 1$$

$$E_{a_1,b_2} = 0$$

$$S = 0.33 + 0 + 1 - 0 = 1.33 \leq 2$$



Computing the CHSH Inequality

$$S = |E_{a_1,b_1} + E_{a_2,b_1} + E_{a_2,b_2} - E_{a_1,b_2}| \{ \begin{array}{l} \leq 2 \text{ Classical} \\ \in [2, 2\sqrt{2}] \text{ Quantum Maximum} \end{array}$$

A		B		$a_i \cdot b_j$
Basis	Result	Basis	Result	
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a_2	-1	b_1	+1	-1
a_2	+1	b_2	+1	+1

$$E_{a_1,b_1} = \frac{1 - 1 + 1}{3} = \frac{1}{3}$$

$$E_{a_2,b_1} = \frac{1 - 1}{3} = 0$$

$$E_{a_2,b_2} = \frac{1}{1} = 1$$

$$E_{a_1,b_2} = 0$$

$$S = 0.33 + 0 + 1 - 0 = 1.33 \leq 2$$

Not enough measurements
to draw a conclusion!

BREAK

Back at

00:00

Plan

- Presentation
- Cryptography
- The qubit
- The photon: messenger of quantum information
- Entanglement and CHSH inequality
- Protocol E91
- Hands-on session

Plan

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Plan

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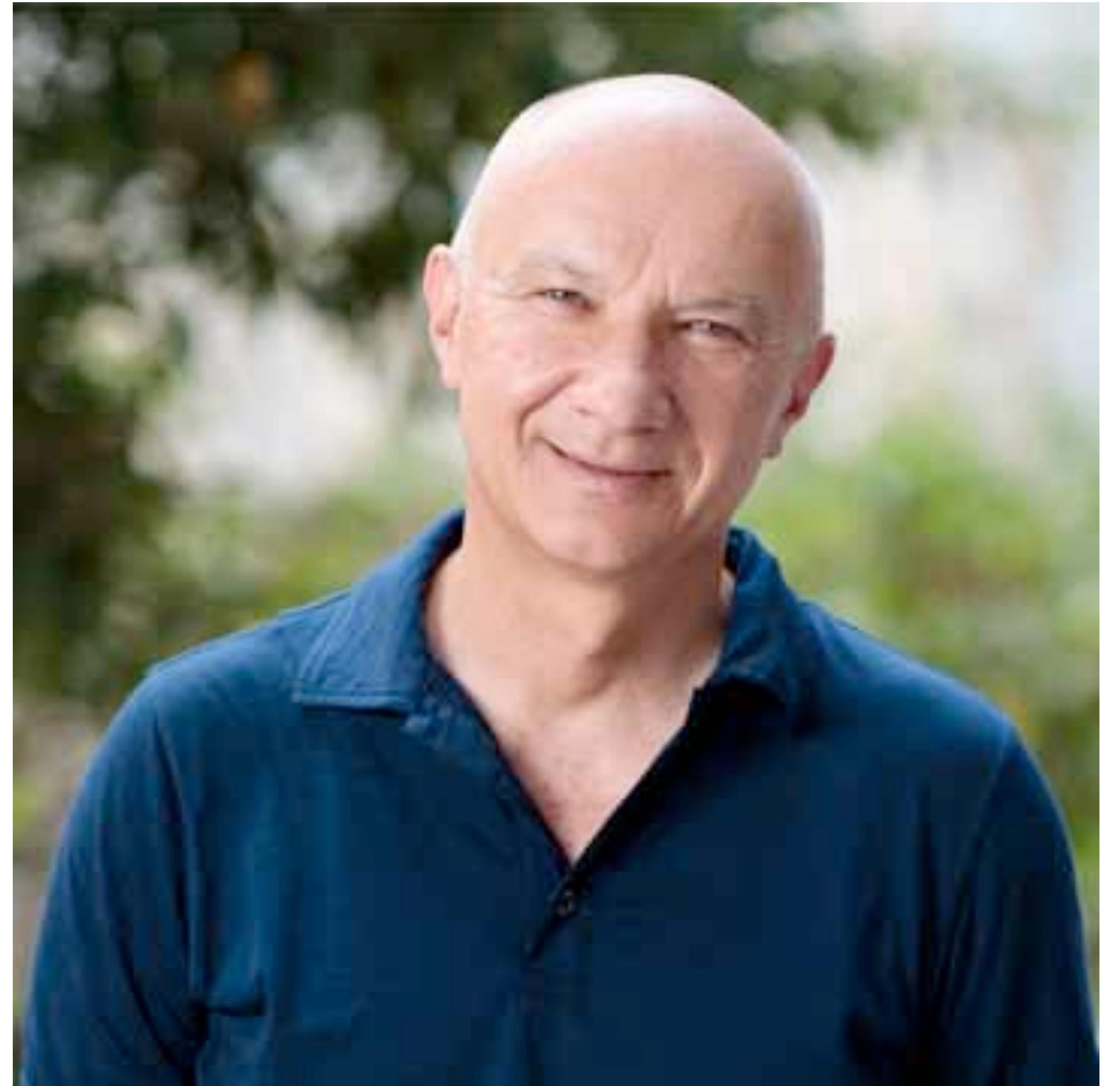
Protocol E91

Created by **Artur Ekert** in **1991**

Quantum Symmetric Key Distribution
Protocol

Perfect theoretical security

ensured by:



<https://www.cqt.sg/groups/artur-ekert/>



Protocol E91

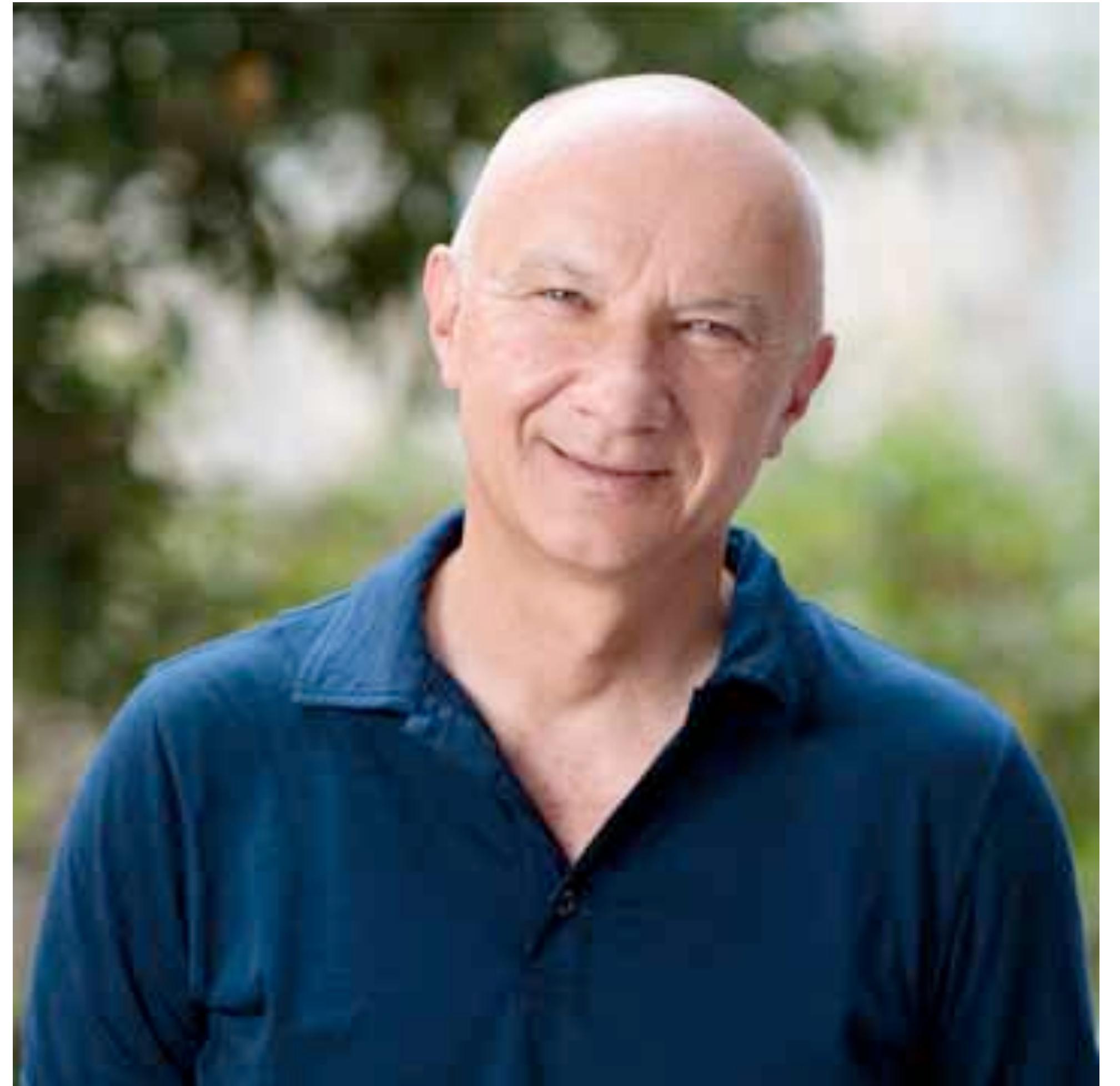
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Perfect theoretical security
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**Quantum
Measurement**

Distribution of
the symmetric
key



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Created by **Artur Ekert** in **1991**

Quantum Symmetric Key Distribution
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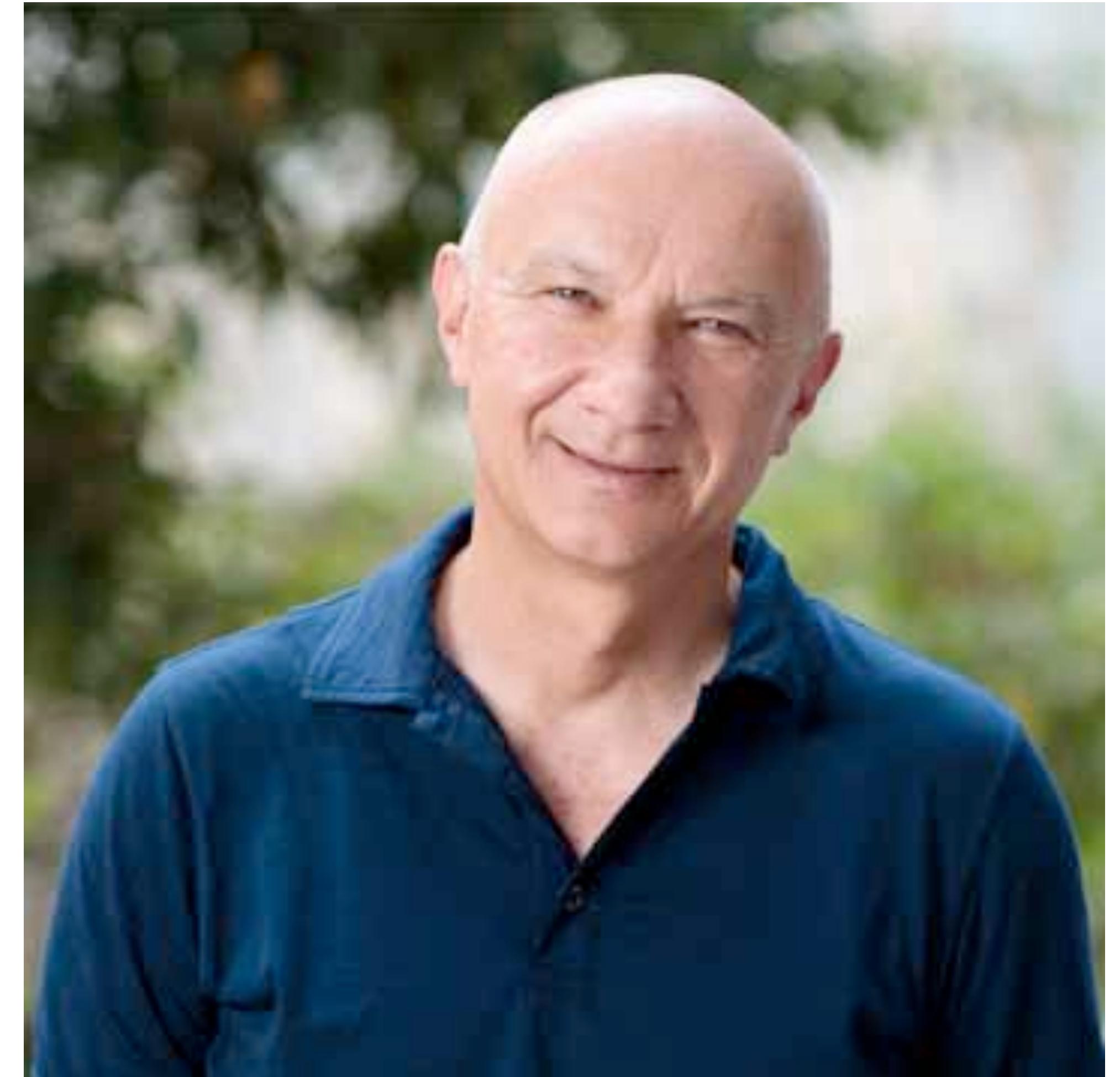
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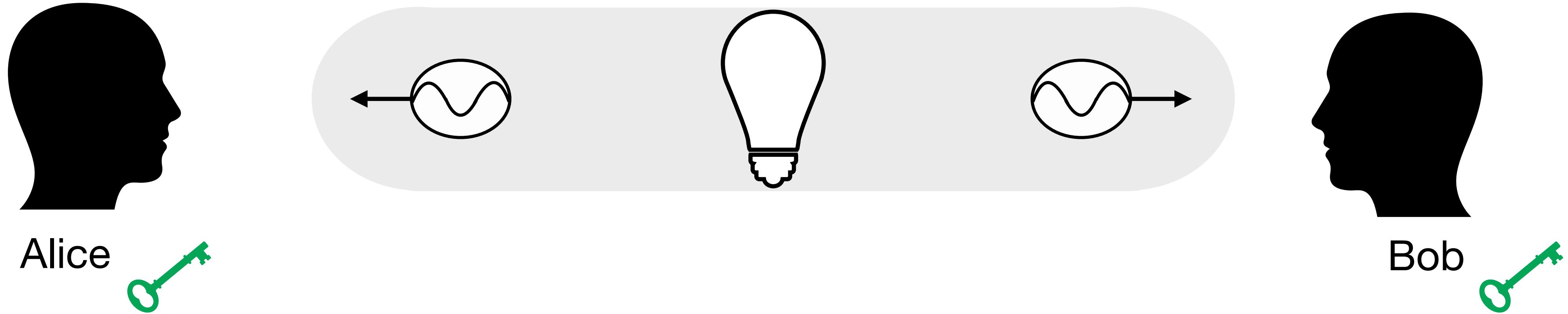
**Entanglement and
CHSH Inequality**

Spy detection



<https://www.cqt.sg/groups/artur-ekert/>

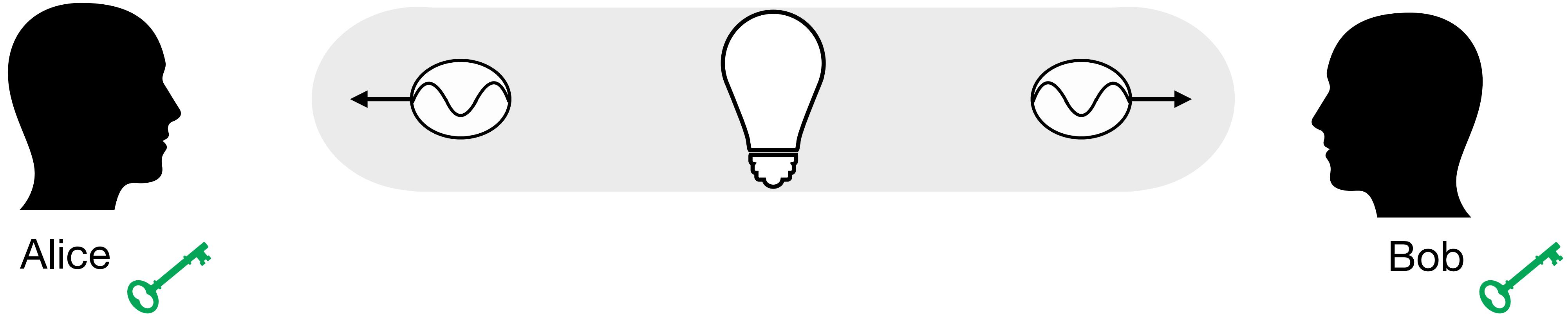
Protocol steps



Goal

Establish a secret symmetric key between Alice and Bob

Protocol steps

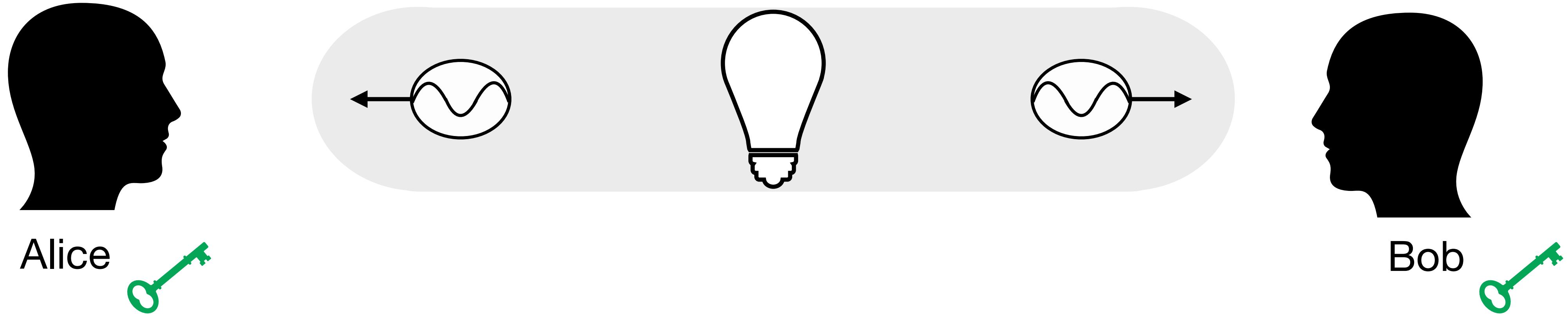


Goal

Establish a secret symmetric key between Alice and Bob

1. Reception of the entangled photons

Protocol steps

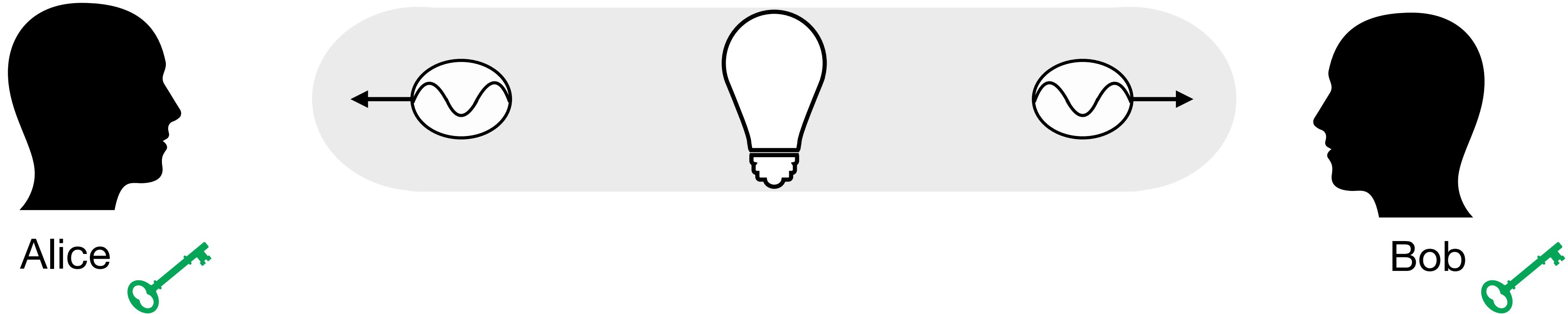


Goal

Establish a secret symmetric key between Alice and Bob

1. Reception of the entangled photons
2. Announcement of the bases

Protocol steps



Goal

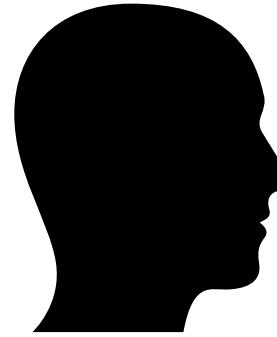
Establish a secret symmetric key between Alice and Bob

1. Reception of the entangled photons
2. Announcement of the bases
3. Spy/Error Detection

Step 1: Reception of the entangled photons

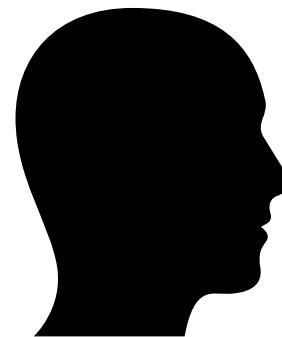


Alice and Bob each receive one photon of an entangled pair



Alice

(0° , 45° , 90°)



Bob

(45° , 90° , 135°)

Step 1: Reception of the entangled photons

Alice and Bob each receive one photon of an entangled pair



Alice

(0° , 45° , 90°)



Bob

(45° , 90° , 135°)

**Choose
a basis
randomly**

0°

90°



Step 1: Reception of the entangled photons

Alice and Bob each receive one photon of an entangled pair



Alice

(0° , 45° , 90°)



Bob

(45° , 90° , 135°)

Choose
a basis
randomly

0°

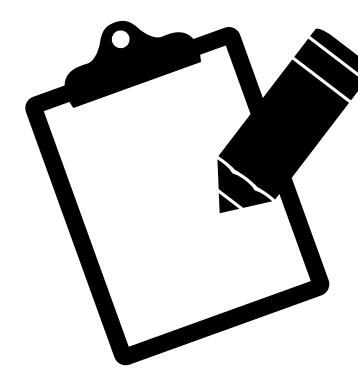
90°



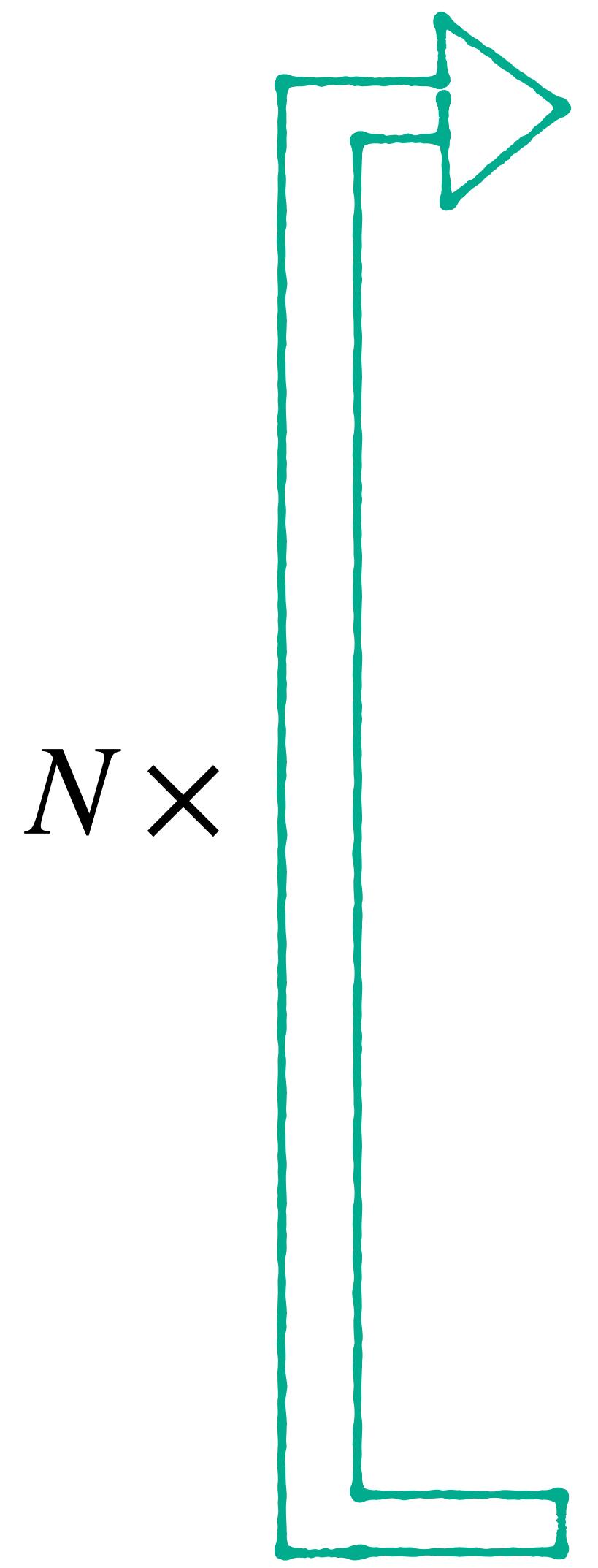
Photon
Measurement

0 ou 1

0 ou 1



Step 1: Reception of the entangled photons

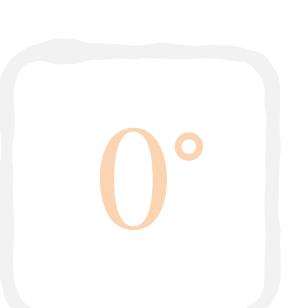


Alice and Bob each receive one photon of an entangled pair



Alice

(0° , 45° , 90°)



0°

0 ou 1



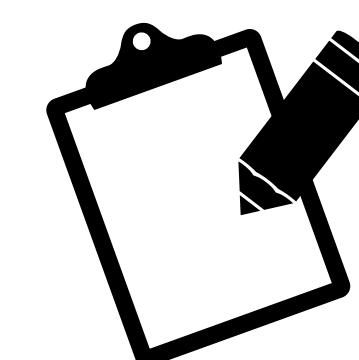
Bob

(45° , 90° , 135°)

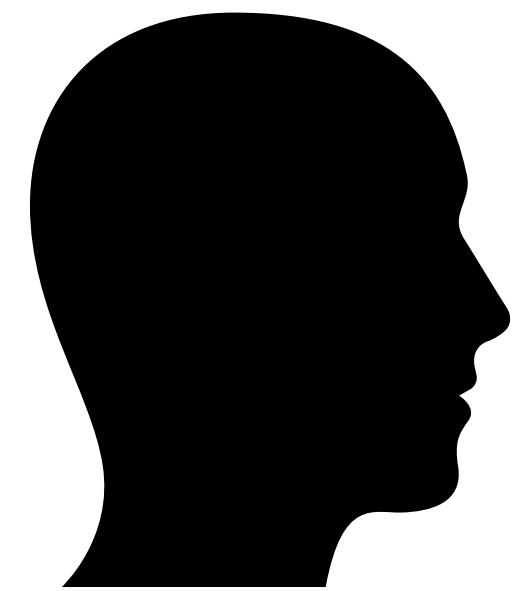


90°

0 ou 1

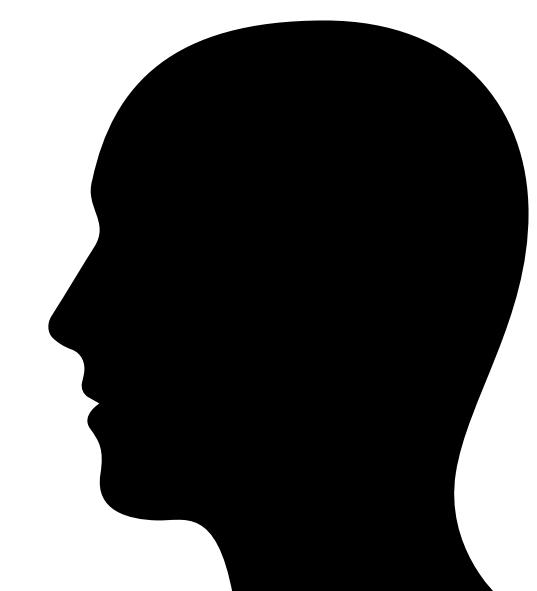


Step 2: Announcement of the bases



Alice

$(0^\circ, 45^\circ, 90^\circ)$



Bob

$(45^\circ, 90^\circ, 135^\circ)$

Step 2: Announcement of the bases



Alice

$(0^\circ, 45^\circ, 90^\circ)$



Bob

$(45^\circ, 90^\circ, 135^\circ)$



9 combinations

$(0^\circ, 45^\circ)(0^\circ, 90^\circ)(0^\circ, 135^\circ)(45^\circ, 45^\circ)(45^\circ, 90^\circ)(45^\circ, 135^\circ)(90^\circ, 45^\circ)(90^\circ, 90^\circ)(90^\circ, 135^\circ)$



Step 2: Announcement of the bases

**Creation of the
symmetric key**

Alice	Bob
45°	45°
90°	90°



Step 2: Announcement of the bases

Creation of the symmetric key

Alice	Bob
45°	45°
90°	90°

Spy Detection

Alice	Bob
0°	45°
0°	90°
0°	135°
45°	90°
45°	135°
90°	45°
90°	135°

Step 2: Announcement of the bases

Creation of the symmetric key

Alice	Bob
45°	45°
90°	90°

Spy Detection

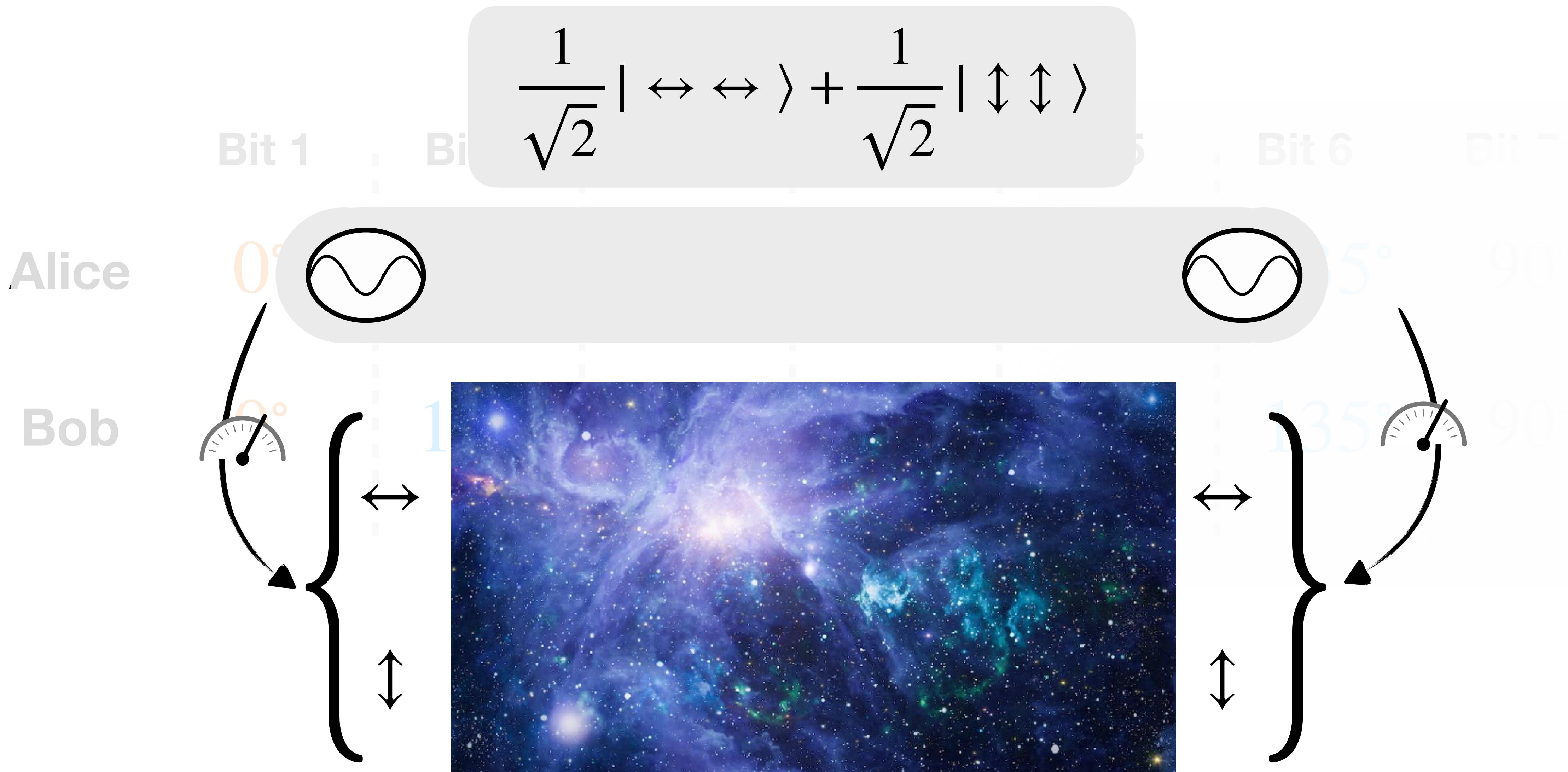
Alice	Bob
0°	45°
0°	90°
0°	135°
45°	90°
45°	135°
90°	45°
90°	135°

Generating the symmetric key



	Bit 1	Bit 2	Bit 3	Bit 4	Bit 5	Bit 6	Bit 7
Alice	0°	135°	0°	45°	90°	135°	90°
Bob	0°	135°	0°	45°	90°	135°	90°

Generating the symmetric key



Generating the symmetric key



	Bit 1	Bit 2	Bit 3	Bit 4	Bit 5	Bit 6	Bit 7
Alice	0°	135°	0°	45°	90°	135°	90°
Bob	0°	135°	0°	45°	90°	135°	90°

Generating the symmetric key



	Bit 1	Bit 2	Bit 3	Bit 4	Bit 5	Bit 6	Bit 7
Alice	0°	135°	0°	45°	90°	135°	90°
Bob	0°	135°	0°	45°	90°	135°	90°
	1	1	0	0	1	0	0

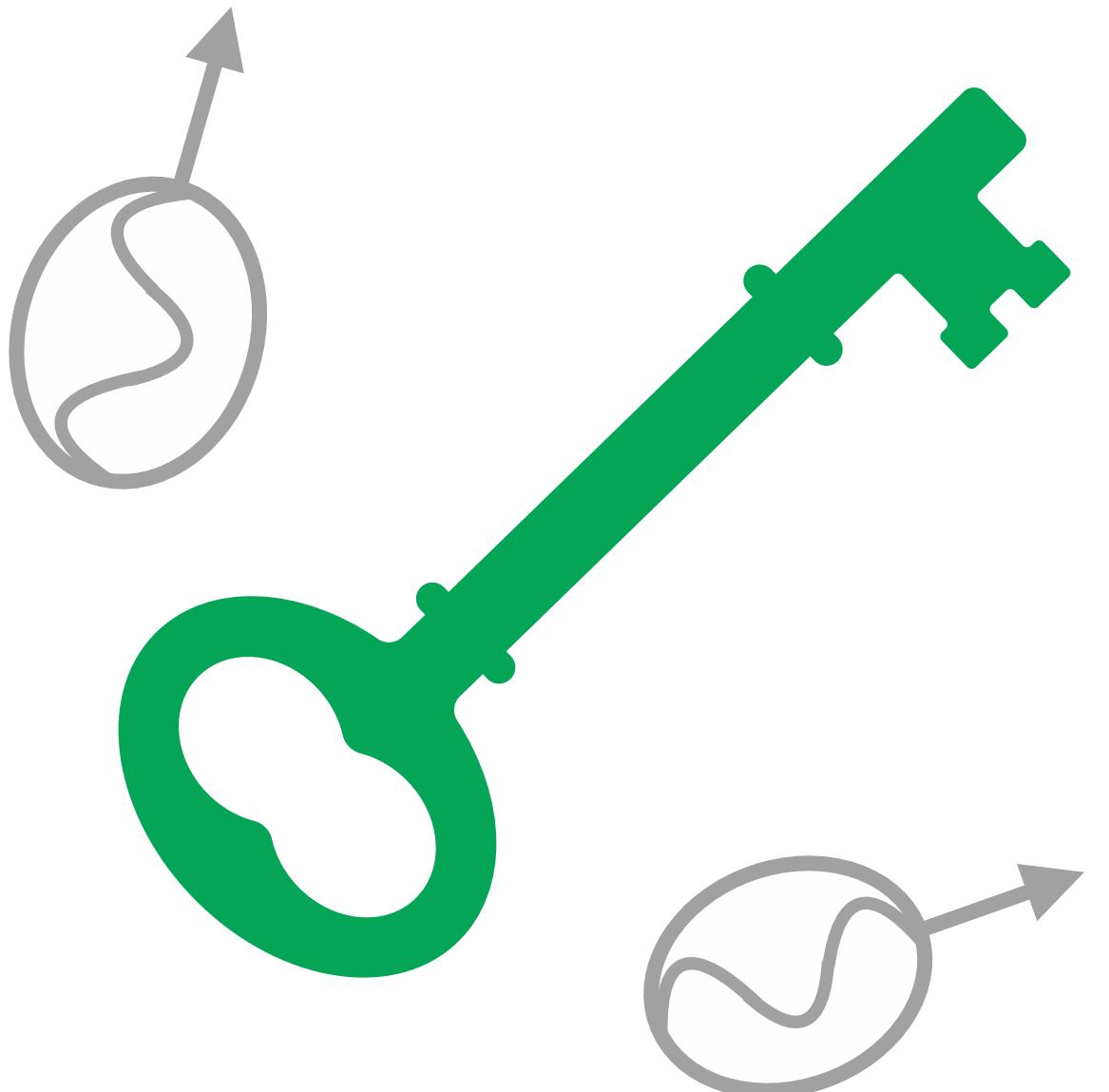


Properties of the quantum symmetric key



Binary

The quantum measurement results are labeled 0 or 1.



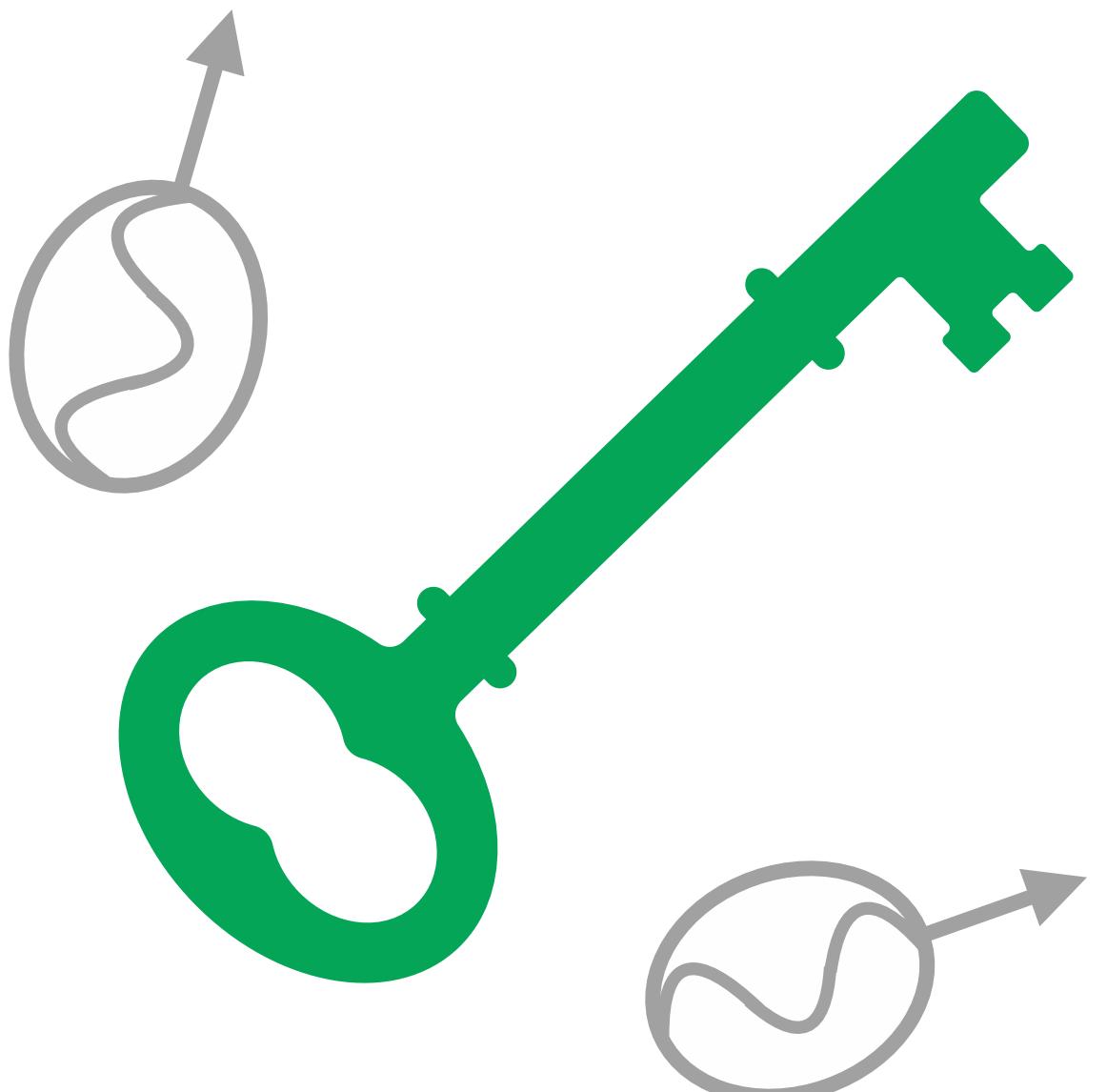
Properties of the quantum symmetric key

Binary

The quantum measurement results are labeled 0 or 1.

Identical

Measuring the photons of an entangled pair in the same basis, guarantees the same measurement result for Alice and Bob.



Properties of the quantum symmetric key



Binary

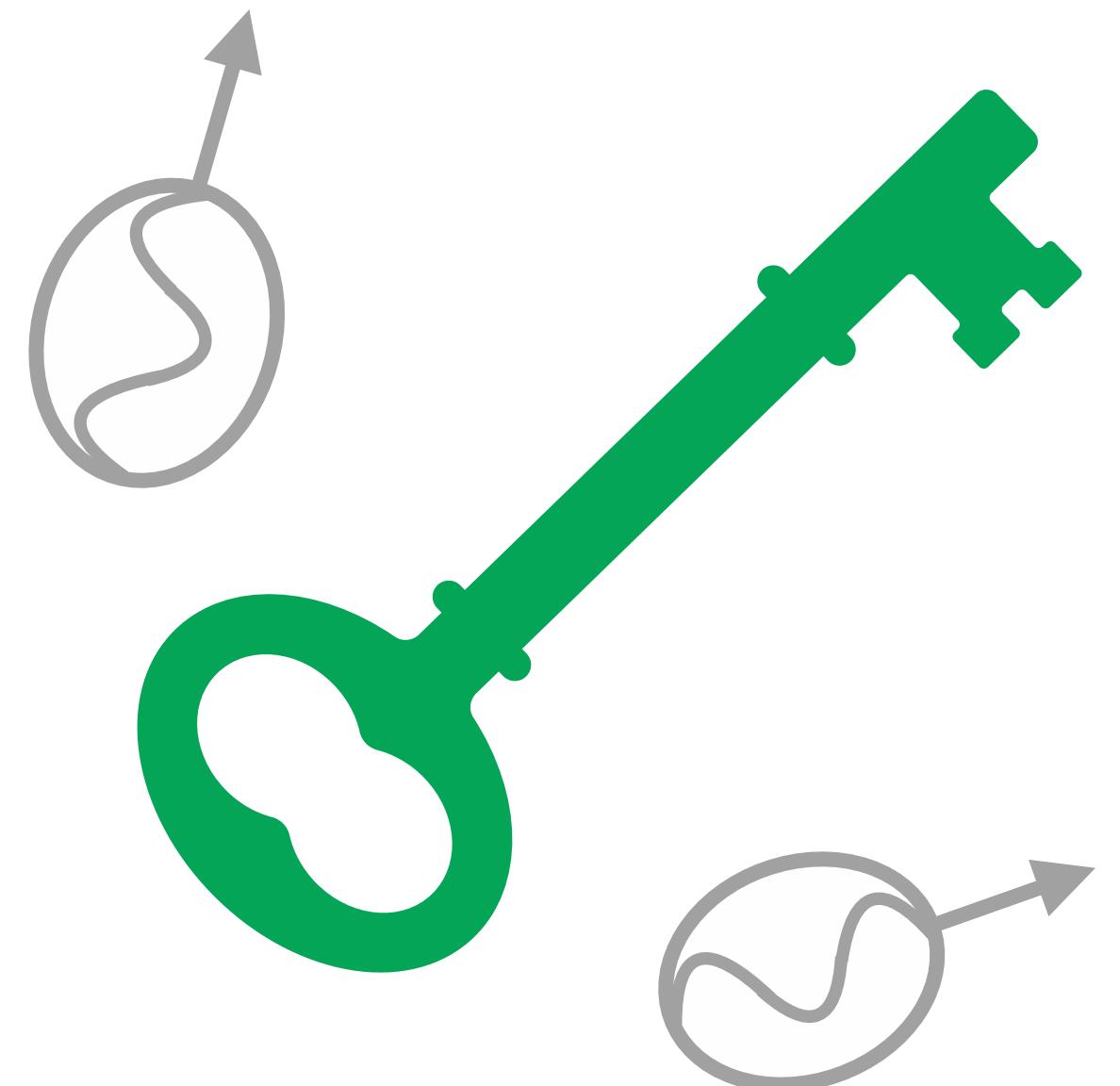
The quantum measurement results are labeled 0 or 1.

Identical

Measuring the photons of an entangled pair in the same basis, guarantees the same measurement result for Alice and Bob.

Truly Random

La mesure quantique d'une paire intriquée garantie l'aléatoire.



Creation of the symmetric key

Alice	Bob
45°	45°
90°	90°

Spy Detection

Alice	Bob
0°	45°
0°	90°
0°	135°
45°	90°
45°	135°
90°	45°
90°	135°

Creation of the symmetric key

Alice	Bob
45°	45°
90°	90°

Spy Detection

Alice	Bob
0°	45°
0°	90°
0°	135°
45°	90°
45°	135°
90°	45°
90°	135°

Step 3: Spy/Error Detection

Creation of the symmetric key

Alice	Bob
45°	45°
90°	90°

Spy Detection

Alice	Bob
0°	45°
0°	90°
0°	135°
45°	90°
45°	135°
90°	45°
90°	135°



Step 3: Spy/Error Detection

Bases combinations used: (0° , 45°) (0° , 135°) (90° , 45°) (90° , 135°)

Alice { 0° , 90° }

Bob { 45° , 135° }



Step 3: Spy/Error Detection

Bases combinations used: $(0^\circ, 45^\circ)$ $(0^\circ, 135^\circ)$ $(90^\circ, 45^\circ)$ $(90^\circ, 135^\circ)$

Alice $\{0^\circ, 90^\circ\}$ $\{a_1, a_2\}$

Bob $\{45^\circ, 135^\circ\}$ $\{b_1, b_2\}$



Step 3: Spy/Error Detection

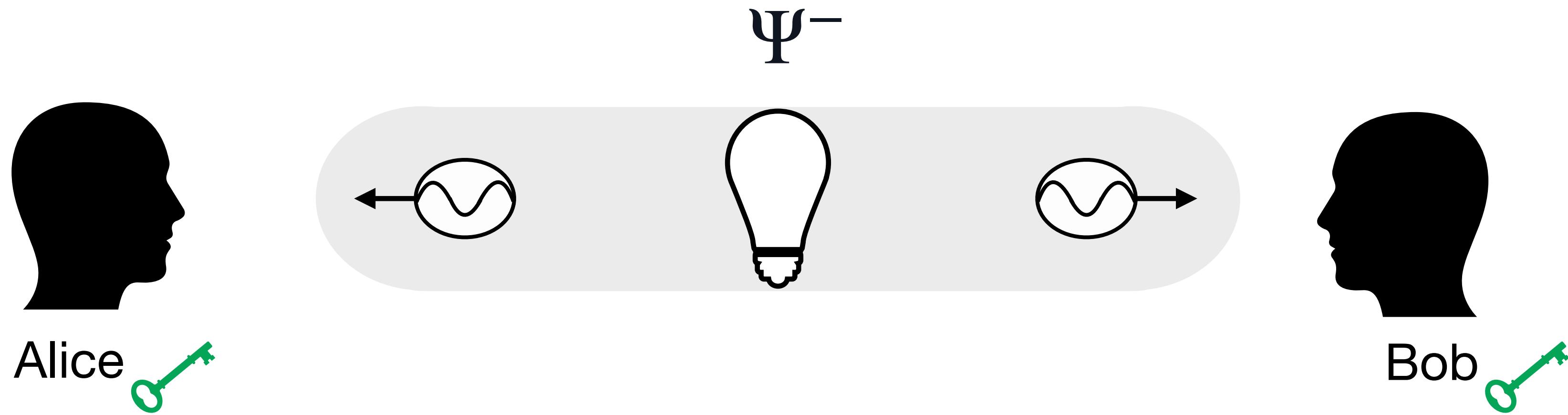
Bases combinations used: $(0^\circ, 45^\circ)$ $(0^\circ, 135^\circ)$ $(90^\circ, 45^\circ)$ $(90^\circ, 135^\circ)$

Alice $\{0^\circ, 90^\circ\}$ $\{a_1, a_2\}$

Bob $\{45^\circ, 135^\circ\}$ $\{b_1, b_2\}$

$$S = |E_{a_1, b_1} + E_{a_2, b_1} + E_{a_2, b_2} - E_{a_1, b_2}| \left\{ \begin{array}{l} \leq 2 \text{ Classical} \\ \in [2, 2\sqrt{2}] \text{ Quantum maximum} \end{array} \right.$$

Case 1: Using Bell Pairs



$$S = |E_{a_1,b_1} + E_{a_2,b_1} + E_{a_2,b_2} - E_{a_1,b_2}| \{ \begin{array}{l} \leq 2 \text{ Classical} \\ \in [2, 2\sqrt{2}] \text{ Quantum maximum} \end{array}$$

Case 2: Eve spies on the conversation



Case 2: Eve spies on the conversation



Choice of Basis

45°

135°

90°

Case 2: Eve spies on the conversation



Choice of Basis

45°

Measurement Result

{0 ,1}

135°

{0 ,1}

90°

{0 ,1}

Case 2: Eve spies on the conversation



Choice of Basis	Measurement Result	Encoding
45°	$\{0, 1\}$	$\{ \nearrow \rangle, \swarrow \rangle \}$
135°	$\{0, 1\}$	$\{ \searrow \rangle, \nwarrow \rangle \}$
90°	$\{0, 1\}$	$\{ \leftrightarrow \rangle, \uparrow \downarrow \rangle \}$

Case 2: Eve spies on the conversation



$$S = |E_{a_1, b_1} + E_{a_2, b_1} + E_{a_2, b_2} - E_{a_1, b_2}| \{ \begin{array}{l} \leq 2 \text{ Classical} \\ \in [2, 2\sqrt{2}] \text{ Quantum Maximum} \end{array}$$

Case 2: Eve spies on the conversation



$$S = |E_{a_1,b_1} + E_{a_2,b_1} + E_{a_2,b_2} - E_{a_1,b_2}| \{ \begin{array}{l} \leq 2 \text{ Classical} \\ \in [2, 2\sqrt{2}] \text{ Quantum Maximum} \end{array}$$

Number of Measurements

Creation of the
symmetric key

Alice	Bob
45°	45°
90°	90°

Spy Detection

Alice	Bob
0°	45°
0°	90°
0°	135°
45°	90°
45°	135°
90°	45°
90°	135°



Number of Measurements

Creation of the symmetric key

Alice	Bob
45°	45°
90°	90°

$$\frac{2}{9} \sim 22\% \text{ Generating the symmetric key}$$

Spy Detection

Alice	Bob
0°	45°
0°	90°
0°	135°
45°	90°
45°	135°
90°	45°
90°	135°



Keypoints

Key length

Number of Measurements

Creation of the symmetric key

Alice	Bob
45°	45°
90°	90°

$\frac{2}{9} \sim 22\%$ Generating the symmetric key

$\frac{4}{9} \sim 45\%$ Spy detection

Spy Detection

Alice	Bob
0°	45°
0°	90°
0°	135°
45°	90°
45°	135°
90°	45°
90°	135°



Keypoints

Key length

Security of the key

Number of Measurements

Creation of the symmetric key

Alice	Bob
45°	45°
90°	90°

Spy Detection

Alice	Bob
0°	45°
0°	90°
0°	135°
45°	90°
45°	135°
90°	45°
90°	135°

$\frac{2}{9} \sim 22\%$ Generating the symmetric key

$\frac{4}{9} \sim 45\%$ Spy detection

$\frac{3}{9} \sim 33\%$ Thrown away

Keypoints

Key length

Security of the key

Plan

- Presentation
- Cryptography
- The qubit
- The photon: messenger of quantum information
- Entanglement and CHSH inequality
- Protocol E91
- Hands-on session

Plan

- Presentation
- Cryptography
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Plan

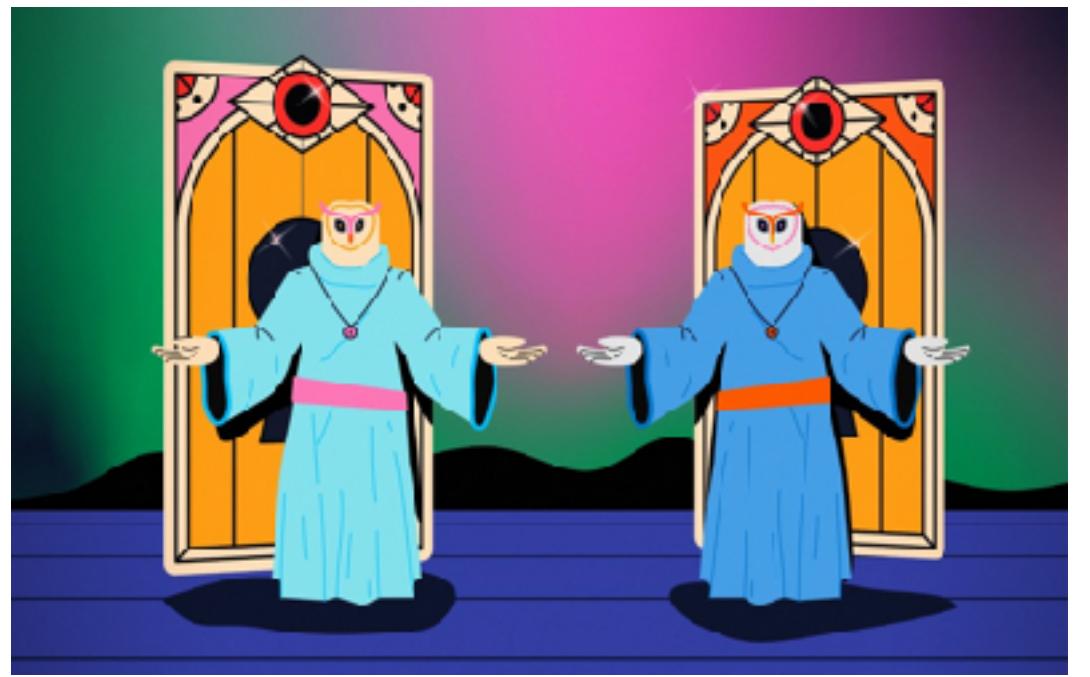
- ✓ Presentation
- ✓ Cryptography
- ✓ The qubit
- ✓ The photon: messenger of quantum information
- ✓ Entanglement and CHSH inequality
- ✓ Protocol E91
- Hands-on session

Hands-On Session

<https://github.com/algolab-quantique/CMAI-E91-Students.git>

Conclusion

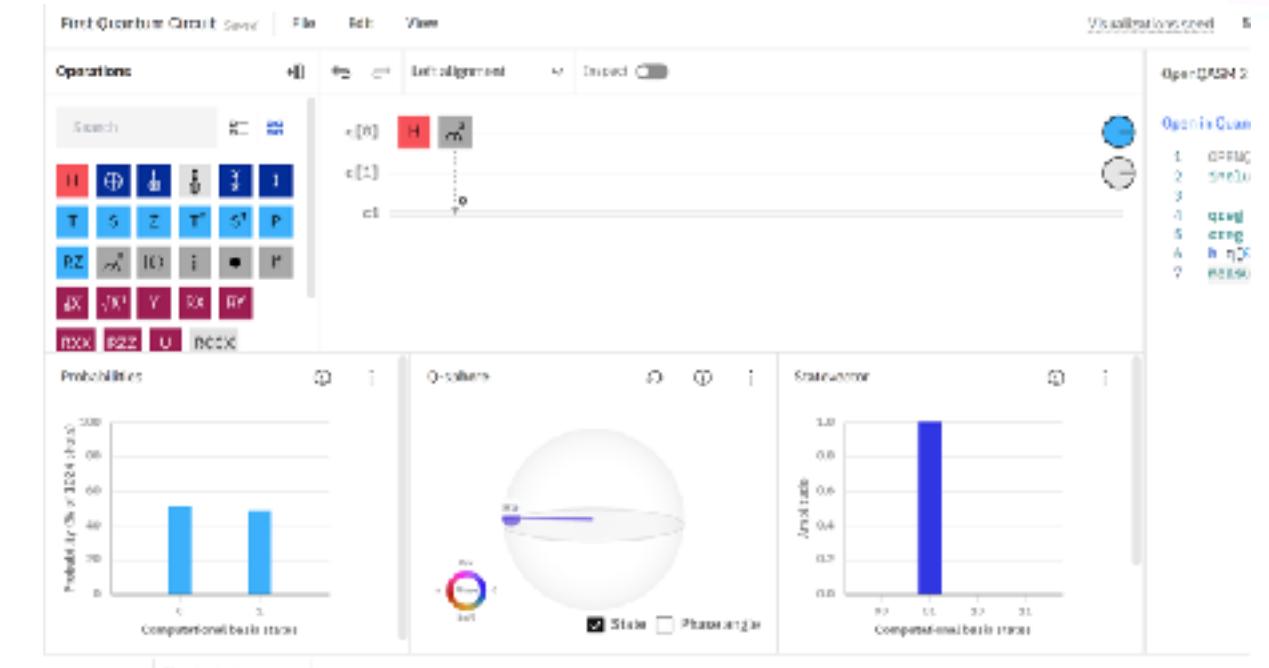
References



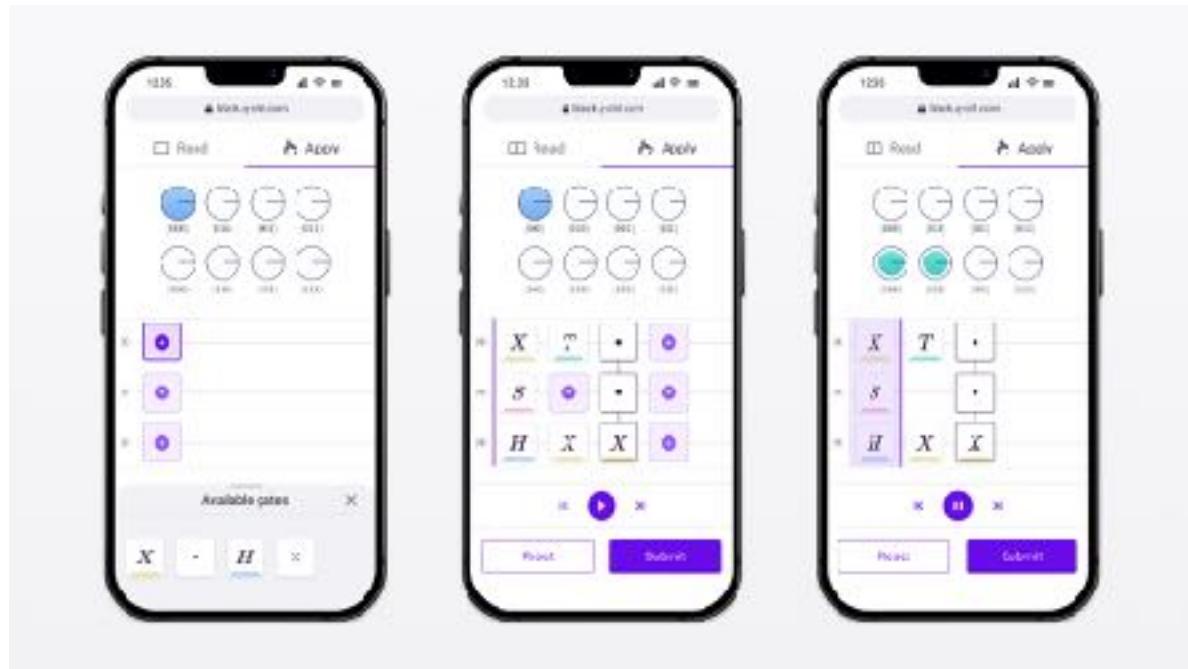
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