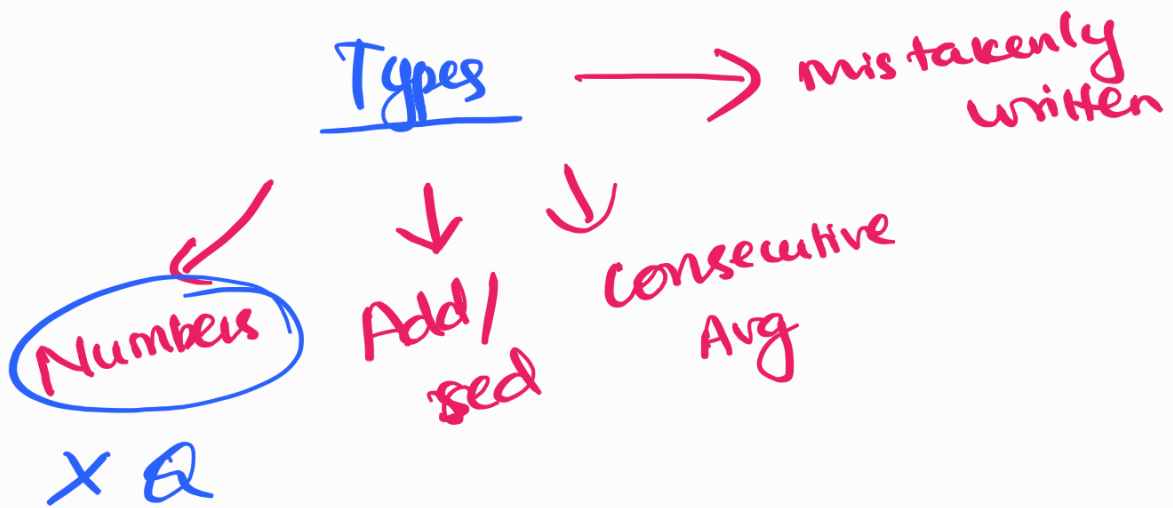


# Average

$$\text{Avg} = \frac{\text{Sum of terms}}{\text{No of terms}}$$



$$\Rightarrow \text{Avg of first } n \text{ natural nos} = \frac{n+1}{2}$$

$$\Rightarrow \text{Avg of first } n \text{ even nos} = (n+1)$$

$$\Rightarrow \text{Avg of first } n \text{ odd nos} = n$$

$$\Rightarrow \left. \begin{array}{l} \text{Avg of sum of squares of first} \\ n \text{ natural nos} \end{array} \right\} = \frac{(n+1)(2n+1)}{6}$$

$$\Rightarrow \text{Avg of cubes of first } n \text{ natural no} = \frac{n(n+1)^2}{4}$$

The average of four consecutive even numbers is 9. Find the largest number.

$$\boxed{6, 8, 10, 12} \Rightarrow 12$$

$$2n, 2n+2, 2n+4, 2n+6$$

$$\frac{(2n) + (2n+2) + (2n+4) + (2n+6)}{4} = 9$$

$$8n + 12 = 36$$

$$8n = 36 - 12 \Rightarrow 8n = 24$$

$$\boxed{n = 3}$$

$$6, 8, 10, 12$$

$$\boxed{\text{Ans} = 12}$$

$$\frac{6}{\quad}, \frac{8}{\quad}, \frac{10}{\quad}, \frac{12}{\quad}$$

↓  
9

$$\frac{1}{\quad}, \frac{2}{\quad}, \frac{3}{\quad}, \frac{4}{\quad}, \frac{5}{\quad} \Rightarrow \frac{15}{5} \Rightarrow 3 \checkmark$$

↓  
Avg

The average age of boys in the class is twice the number of girls in the class. The ratio of boys and girls in the class of 50 is 4 : 1. The total of the ages (in years) of the boys in the class is

$$\text{Avg of boys} = 2 \times \text{No of girls}$$

$$\text{Avg of boys} \Rightarrow 2 \times 10 \Rightarrow 20$$

$$B : G \Rightarrow \text{Sum}$$

$$\text{Boys} \Rightarrow 40$$

$$\text{Girls} \Rightarrow 10$$

$$4 : 1 \Rightarrow 50$$

$$\text{Sum of ratio} \times \text{CM} = \text{Sum of value}$$

$$(4+1) \times \text{CM} = 50$$

$$5 \times \text{CM} \Rightarrow 50 \Rightarrow \boxed{\text{CM} = 10}$$

$$\text{Avg age of boys} = 20$$

$$\text{No of boys} = 40$$

$$\text{Avg} = \frac{\text{Total ages}}{\text{No of boys}}$$

$$\begin{aligned} \text{Total ages} &= \text{Avg} \times \text{No of boys} \\ &= 20 \times 40 \end{aligned}$$

$$\boxed{\text{Total} = 800}$$

The average height of 8 students is 152 cm. Two more students of heights 144 cm and 155 cm join the group. What is the new average height ?

$$\text{Avg} = \frac{\text{Sum of heights}}{\text{No of students}}$$

$$\begin{aligned}\text{Sum} &= \text{Avg} \times \text{No of stu} \\ &= 152 \times 8\end{aligned}$$

$$\boxed{\text{Sum} = 1216}$$

$$\text{Sum of 10 stu height} = 1216 + 144 + 155$$

$$\boxed{\text{Sum} = 1515}$$

$$\text{Avg} = \frac{\text{Sum of h of 10 stu}}{10}$$

$$= \frac{1515}{10} = \boxed{151.5 \text{ cm}}$$

A boy found that the average of 20 numbers is 35 when he writes a number '61' instead of '16'. The correct average of 20 numbers is

$$\text{Avg 20 nos} = \frac{\text{Sum of 20 nos}}{20}$$

$$35 = \frac{\text{Sum}}{20} \Rightarrow \boxed{\text{Sum} = 700}$$

$$\boxed{\text{Sum of 20 nos} = 700} \quad \times$$

$$\text{Correct} \Rightarrow 700 - 61 + 16$$

$$\Rightarrow \boxed{655} \Rightarrow \text{Sum of 20 nos}$$

$$\text{Avg} = \frac{\text{Sum}}{20}$$

$$= \frac{\cancel{655}^{131}}{\cancel{20}_4}$$

$$\Rightarrow \boxed{32.75} \Rightarrow \text{Avg}$$

$$\Rightarrow 4 \overline{) 131} \begin{array}{r} 32.75 \\ 131 \\ \underline{12} \\ 11 \\ 8 \\ \underline{30} \\ 28 \\ \underline{20} \\ 20 \\ \underline{20} \\ 0 \end{array}$$