# Package 'HighFreq'

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# R topics documented:

agg_ohlc	3
agg_stats_r	4
back_test	5
calc_eigen	7
calc_endpoints	8
calc_hurst	9
calc_hurst_ohlc	10
calc_inv	12
calc_kurtosis	13
calc_lm	14
calc mean	16
calc_ranks	17
calc_reg	18
calc_scaled	20
calc_skew	21
calc_startpoints	23
calc_var	24
calc_var_ag	25
calc_var_ohlc	26
calc_var_ohlc_ag	28
calc_var_ohlc_r	30
calc_var_onic_r	31
	32
calc_weights	
diff_it	34
diff_vec	35
hf_data	36
lag_it	37
lag_vec	38
mult_vec_mat	39
random_ohlc	40
remove_jumps	42
roll_apply	42
roll_backtest	44
roll_conv	46
roll_count	47
roll_fun	47
roll_hurst	49
roll_kurtosis	50
roll_mean	52
roll_ohlc	54
roll reg	55
roll_scale	56
roll_sharpe	57
roll skew	58
roll_stats	60
roll_sum	61
roll_sumep	62
roll var	63
<del>-</del>	
roll_var_ohlc	65
roll var vec	67

agg\_ohlc 3

ll_vec	68
ll_vecw	69
11_vwap	<b>7</b> 0
11_wsum	71
ll_zscores	73
n_covar	75
n_max	76
n_mean	77
n_min	78
n_returns	80
	81
	81
	82
	83
	85
<del>-</del>	86
	87
66	88
	89
146_488	90
	91
abon_and,	91
	92
	93
	94
	95
	96
hich_jumps	97

agg\_ohlc

Aggregate a time series of data into a single bar of OHLC data.

# **Description**

Aggregate a time series of data into a single bar of OHLC data.

# Usage

```
agg_ohlc(tseries)
```

# **Arguments**

tseries

A time series or a matrix with multiple columns of data.

# **Details**

The function agg\_ohlc() aggregates a time series of data into a single bar of *OHLC* data. It can accept either a single column of data or four columns of *OHLC* data. It can also accept an additional column containing the trading volume.

The function agg\_ohlc() calculates the *open* value as equal to the *open* value of the first row of tseries. The *high* value as the maximum of the *high* column of tseries. The *low* value as the

4 agg\_stats\_r

minimum of the *low* column of tseries. The *close* value as the *close* of the last row of tseries. The *volume* value as the sum of the *volume* column of tseries.

For a single column of data, the open, high, low, and close values are all the same.

# Value

A *matrix* containing a single row, with the *open*, *high*, *low*, and *close* values, and also the total *volume* (if provided as either the second or fifth column of tseries).

# **Examples**

```
## Not run:
# Define matrix of OHLC data
oh_lc <- coredata(rutils::etf_env$VTI[, 1:5])
# Aggregate to single row matrix
ohlc_agg <- HighFreq::agg_ohlc(oh_lc)
# Compare with calculation in R
all.equal(drop(ohlc_agg),
    c(oh_lc[1, 1], max(oh_lc[, 2]), min(oh_lc[, 3]), oh_lc[NROW(oh_lc), 4], sum(oh_lc[, 5])),
    check.attributes=FALSE)
## End(Not run)</pre>
```

agg\_stats\_r

Calculate the aggregation (weighted average) of a statistical estimator over a OHLC time series using R code.

# **Description**

Calculate the aggregation (weighted average) of a statistical estimator over a *OHLC* time series using R code.

## Usage

```
agg_stats_r(oh_lc, calc_bars = "run_variance", weight_ed = TRUE, ...)
```

# Arguments

	additional parameters to the function calc_bars.
oh_lc	An OHLC time series of prices and trading volumes, in xts format.
calc_bars	A <i>character</i> string representing a function for calculating statistics for individual <i>OHLC</i> bars.
weight_ed	<i>Boolean</i> argument: should estimate be weighted by the trading volume? (default is TRUE)

back\_test 5

#### **Details**

The function agg\_stats\_r() calculates a single number representing the volume weighted average of statistics of individual *OHLC* bars. It first calls the function calc\_bars to calculate a vector of statistics for the *OHLC* bars. For example, the statistic may simply be the difference between the *High* minus *Low* prices. In this case the function calc\_bars would calculate a vector of *High* minus *Low* prices. The function agg\_stats\_r() then calculates a trade volume weighted average of the vector of statistics.

The function agg\_stats\_r() is implemented in R code.

#### Value

A single *numeric* value equal to the volume weighted average of an estimator over the time series.

## **Examples**

```
# Calculate weighted average variance for SPY (single number)
vari_ance <- agg_stats_r(oh_lc=HighFreq::SPY, calc_bars="run_variance")
# Calculate time series of daily skew estimates for SPY
skew_daily <- apply.daily(x=HighFreq::SPY, FUN=agg_stats_r, calc_bars="run_skew")</pre>
```

back\_test

Simulate (backtest) a rolling portfolio optimization strategy, using RcppArmadillo.

# **Description**

Simulate (backtest) a rolling portfolio optimization strategy, using RcppArmadillo.

# Usage

```
back_test(
  excess,
  returns,
  startp,
  endp,
  method = "rank_sharpe",
  eigen_thresh = 0.001,
  eigen_max = 0L,
  con_fi = 0.1,
  alpha = 0,
  scale = TRUE,
  vol_target = 0.01,
  coeff = 1,
  bid_offer = 0
)
```

back\_test

# **Arguments**

returns	A <i>time series</i> or a <i>matrix</i> of returns data (the returns in excess of the risk-free rate).
excess	A <i>time series</i> or a <i>matrix</i> of excess returns data (the returns in excess of the risk-free rate).
startp	An integer vector of start points.
endp	An integer vector of end points.
coeff	A numeric multiplier of the weights. (The default is 1)
bid_offer	A numeric bid-offer spread (the default is 0)
method	A $string$ specifying the objective function for calculating the weights (see Details) (the default is method = "rank_sharpe")
eigen_thresh	A <i>numeric</i> threshold level for discarding small singular values in order to regularize the inverse of the returns matrix (the default is 0.001).
eigen_max	An <i>integer</i> equal to the number of singular values used for calculating the regularized inverse of the returns matrix (the default is $\emptyset$ - equivalent to eigen_max equal to the number of columns of returns).
con_fi	The confidence level for calculating the quantiles (the default is $con_fi = 0.75$ ).
alpha	The shrinkage intensity between $\emptyset$ and 1. (the default is $\emptyset$ ).
scale	A $Boolean$ specifying whether the weights should be scaled (the default is scale = TRUE).
vol_target	A numeric volatility target for scaling the weights (the default is 0.001)

# **Details**

The function back\_test() performs a backtest simulation of a rolling portfolio optimization strategy over a *vector* of endp.

It performs a loop over the end points endp, and subsets the *matrix* of excess returns excess along its rows, between the corresponding end point and the start point. It passes the subset matrix of excess returns into the function calc\_weights(), which calculates the optimal portfolio weights. The arguments eigen\_max, alpha, method, and scale are also passed to the function calc\_weights().

The function back\_test() multiplies the weights by the coefficient coeff (with default equal to 1), which allows reverting a strategy if  $co_eff = -1$ .

The function back\_test() then multiplies the weights times the future portfolio returns, to calculate the out-of-sample strategy returns.

The function back\_test() calculates the transaction costs by multiplying the bid-offer spread bid\_offer times the absolute difference between the current weights minus the weights from the previous period. Then it subtracts the transaction costs from the out-of-sample strategy returns.

The function back\_test() returns a *time series* (column *vector*) of strategy returns, of the same length as the number of rows of returns.

## Value

A column *vector* of strategy returns, with the same length as the number of rows of returns.

calc\_eigen 7

#### **Examples**

```
## Not run:
# Calculate the ETF daily excess returns
re_turns <- na.omit(rutils::etf_env$re_turns[, 1:16])</pre>
\# risk_free is the daily risk-free rate
risk_free <- 0.03/260
ex_cess <- re_turns - risk_free</pre>
# Define monthly end points without initial warmpup period
end_p <- rutils::calc_endpoints(re_turns, inter_val="months")</pre>
end_p \leftarrow end_p[end_p > 0]
len_gth <- NROW(end_p)</pre>
# Define 12-month look-back interval and start points over sliding window
look_back <- 12
start_p <- c(rep_len(1, look_back-1), end_p[1:(len_gth-look_back+1)])</pre>
# Define shrinkage and regularization intensities
al_pha <- 0.5
eigen_max <- 3
# Simulate a monthly rolling portfolio optimization strategy
pnl_s <- HighFreq::back_test(ex_cess, re_turns,</pre>
                             start_p-1, end_p-1,
                             eigen_max = eigen_max,
                              alpha = al_pha)
pnl_s <- xts::xts(pnl_s, index(re_turns))</pre>
colnames(pnl_s) <- "strat_rets"</pre>
# Plot dygraph of strategy
dygraphs::dygraph(cumsum(pnl_s),
  main="Cumulative Returns of Max Sharpe Portfolio Strategy")
## End(Not run)
```

calc\_eigen

Calculate the eigen decomposition of the covariance matrix of returns data using RcppArmadillo.

# **Description**

Calculate the eigen decomposition of the covariance *matrix* of returns data using RcppArmadillo.

# Usage

```
calc_eigen(tseries)
```

#### **Arguments**

tseries

A time series or matrix of returns data.

# **Details**

The function calc\_eigen() first calculates the covariance *matrix* of tseries, and then calculates the eigen decomposition of the covariance *matrix*.

8 calc\_endpoints

#### Value

A list with two elements: a *vector* of eigenvalues (named "values"), and a *matrix* of eigenvectors (named "vectors").

# **Examples**

```
## Not run:
# Create matrix of random data
da_ta <- matrix(rnorm(5e6), nc=5)</pre>
# Calculate eigen decomposition
ei_gen <- HighFreq::calc_eigen(scale(da_ta, scale=FALSE))</pre>
# Calculate PCA
pc_a <- prcomp(da_ta)</pre>
# Compare PCA with eigen decomposition
all.equal(pc_a$sdev^2, drop(ei_gen$values))
all.equal(abs(unname(pc_a$rotation)), abs(ei_gen$vectors))
# Compare the speed of Rcpp with R code
summary(microbenchmark(
  Rcpp=HighFreq::calc_eigen(da_ta),
  Rcode=prcomp(da_ta),
  times=10))[, c(1, 4, 5)] # end microbenchmark summary
## End(Not run)
```

calc\_endpoints

Calculate a vector of end points that divides a vector into equal intervals.

# **Description**

Calculate a vector of end points that divides a vector into equal intervals.

## Usage

```
calc_endpoints(length, step = 1L, stub = 0L)
```

# Arguments

length An *integer* equal to the length of the vector to be divided into equal intervals.

Step The number of elements in each interval between neighboring end points.

Stub An *integer* value equal to the first end point for calculating the end points.

# **Details**

The end points are a vector of integers which divide a vector of length equal to length into equally spaced intervals. If a whole number of intervals doesn't fit over the vector, then calc\_endpoints() adds a stub interval at the end.

The first end point is equal to the argument step, unless the argument stub is provided, and then it becomes the first end point.

For example, consider the end points for a vector of length 20 divided into intervals of length step=5: 0,5,10,15,20. In order for all the differences between neighboring end points to be

calc\_hurst 9

equal to 5, the first end point is set equal to 0. But 0 doesn't correspond to any vector element, so calc\_endpoints() doesn't include it and it only retains the non-zero end points equal to: 5,10,15,20.

Since indexing in C++ code starts at 0, then calc\_endpoints() shifts the end points by -1 and returns the vector equal to 4,9,14,19.

If stub = 1 then the first end point is equal to 1 and the end points are equal to: 1,6,11,16,20. The extra stub interval at the end is equal to 4 = 20 - 16. And calc\_endpoints() returns 0,5,10,15,19. The first value is equal to 0 which is the index of the first element in C++ code.

If stub = 2 then the first end point is equal to 2, with an extra stub interval at the end, and the end points are equal to: 2,7,12,17,20. And calc\_endpoints() returns 1,6,11,16,19.

The function calc\_endpoints() is similar to the function rutils::calc\_endpoints() from package rutils.

But the end points are shifted by -1 compared to R code because indexing starts at 0 in C++ code, while it starts at 1 in R code. So if calc\_endpoints() is used in R code then 1 should be added to it.

This works in R code because the vector element corresponding to index  $\emptyset$  is empty. For example, the R code:  $(4:1)[c(\emptyset,1)]$  produces 4. So in R we can select vector elements using the end points starting at zero.

In C++ the end points must be shifted by -1 compared to R code, because indexing starts at 0: -1,4,9,14,19. But there is no vector element corresponding to index -1. So in C++ we cannot select vector elements using the end points starting at -1. The solution is to drop the first placeholder end point.

## Value

A vector of equally spaced *integers* representing the end points.

#### **Examples**

```
# Calculate end points without a stub interval
HighFreq::calc_endpoints(length=20, step=5)
# Calculate end points with a final stub interval
HighFreq::calc_endpoints(length=23, step=5)
# Calculate end points with initial and final stub intervals
HighFreq::calc_endpoints(length=20, step=5, stub=2)
# Calculate end points with initial and final stub intervals
HighFreq::calc_endpoints(length=20, step=5, stub=24)
```

calc\_hurst

Calculate the Hurst exponent from the volatility ratio of aggregated returns.

## **Description**

Calculate the Hurst exponent from the volatility ratio of aggregated returns.

## Usage

```
calc_hurst(tseries, step = 1L)
```

10 calc\_hurst\_ohlc

# **Arguments**

tseries A *time series* or a *matrix* of prices.

step The number of periods in each interval between neighboring end points.

## **Details**

The function calc\_hurst() calculates the Hurst exponent from the ratios of the volatilities of aggregated returns.

The aggregated volatility  $\sigma_t$  scales (increases) with the length of the aggregation interval  $\Delta t$  raised to the power of the *Hurst exponent H*:

$$\sigma_t = \sigma \Delta t^H$$

Where  $\sigma$  is the daily return volatility.

The *Hurst exponent H* is equal to the logarithm of the ratio of the volatilities divided by the logarithm of the time interval  $\Delta t$ :

$$H = \frac{\log \sigma_t - \log \sigma}{\log \Delta t}$$

The function calc\_hurst() calls the function calc\_var\_ag() to calculate the aggregated volatility  $\sigma_t$ .

## Value

The Hurst exponent calculated from the variance of aggregated returns.

# **Examples**

```
## Not run:
# Calculate the log prices
price_s <- na.omit(rutils::etf_env$price_s[, c("XLP", "VTI")])
price_s <- log(price_s)
# Calculate the Hurst exponent from 21 day aggregations
calc_hurst(price_s, step=21)
## End(Not run)</pre>
```

calc\_hurst\_ohlc

Calculate the Hurst exponent from the volatility ratio of aggregated OHLC prices.

# Description

Calculate the Hurst exponent from the volatility ratio of aggregated OHLC prices.

calc\_hurst\_ohlc 11

#### Usage

```
calc_hurst_ohlc(
  ohlc,
  step = 1L,
  method = "yang_zhang",
  lag_close = 0L,
  scale = TRUE,
  in_dex = 0L
)
```

## **Arguments**

ohlc A time series or a matrix of OHLC prices.

step The number of periods in each interval between neighboring end points.

method A *character* string representing the price range estimator for calculating the variance. The estimators include:

• "close" close-to-close estimator,

• "rogers\_satchell" Rogers-Satchell estimator,

• "garman\_klass" Garman-Klass estimator,

• "garman\_klass\_yz" Garman-Klass with account for close-to-open price jumps,

• "yang\_zhang" Yang-Zhang estimator,

(The default is the method = "yang\_zhang".)

lag\_close A vector with the lagged close prices of the OHLC time series. This is an op-

tional argument. (The default is  $lag_close = 0$ ).

scale Boolean argument: Should the returns be divided by the time index, the number

of seconds in each period? (The default is scale = TRUE).

in\_dex A vector with the time index of the time series. This is an optional argument

(the default is  $in_dex = 0$ ).

## **Details**

The function calc\_hurst\_ohlc() calculates the Hurst exponent from the ratios of the volatilities of aggregated *OHLC* prices.

The aggregated volatility  $\sigma_t$  scales (increases) with the length of the aggregation interval  $\Delta t$  raised to the power of the *Hurst exponent H*:

$$\sigma_t = \sigma \Delta t^H$$

Where  $\sigma$  is the daily return volatility.

The *Hurst exponent H* is equal to the logarithm of the ratio of the volatilities divided by the logarithm of the time interval  $\Delta t$ :

$$H = \frac{\log \sigma_t - \log \sigma}{\log \Delta t}$$

The function calc\_hurst\_ohlc() calls the function calc\_var\_ohlc\_ag() to calculate the aggregated volatility  $\sigma_t$ .

## Value

The Hurst exponent calculated from the variance ratio of aggregated OHLC prices.

12 calc\_inv

#### **Examples**

```
## Not run:
# Calculate the log ohlc prices
oh_lc <- log(rutils::etf_env$VTI)
# Calculate the Hurst exponent from 21 day aggregations
calc_hurst_ohlc(oh_lc, step=21)
## End(Not run)</pre>
```

calc\_inv

Calculate the regularized inverse of a rectangular matrix of data using Singular Value Decomposition (SVD).

# **Description**

Calculate the regularized inverse of a rectangular *matrix* of data using Singular Value Decomposition (SVD).

# Usage

```
calc_inv(tseries, eigen_thresh = 0.001, eigen_max = 0L)
```

## **Arguments**

tseries A *time series* or *matrix* of returns data.

eigen\_thresh A numeric threshold level for discarding small singular values in order to regu-

larize the inverse of the matrix tseries (the default is 0.001).

eigen\_max An *integer* equal to the number of singular values used for calculating the regu-

larized inverse of the matrix tseries (the default is 0 - equivalent to eigen\_max

equal to the number of columns of tseries).

#### **Details**

The function calc\_inv() calculates the regularized inverse of tseries using Singular Value Decomposition (SVD).

If eigen\_max is given, then it calculates the regularized inverse from the *SVD* using the first eigen\_max largest singular values. For example, if eigen\_max = 3 then it only uses the 3 largest singular values. If eigen\_max is set equal to the number of columns of tseries then it uses all the singular values without any regularization.

If eigen\_max is not given then it calculates the regularized inverse using the function arma::pinv(). Then it discards small singular values that are less than the threshold level eigen\_thresh.

## Value

A matrix equal to the regularized inverse of the matrix tseries.

calc\_kurtosis 13

#### **Examples**

```
## Not run:
# Calculate ETF returns
re_turns <- na.omit(rutils::etf_env$re_turns)
# Calculate regularized inverse using RcppArmadillo
in_verse <- HighFreq::calc_inv(re_turns, eigen_max=3)
# Calculate regularized inverse from SVD in R
s_vd <- svd(re_turns)
eigen_max <- 1:3
inverse_r <- s_vd$v[, eigen_max] %*% (t(s_vd$u[, eigen_max]) / s_vd$d[eigen_max])
# Compare RcppArmadillo with R
all.equal(in_verse, inverse_r)
## End(Not run)</pre>
```

calc\_kurtosis

Calculate the kurtosis of the columns of a time series or a matrix using RcppArmadillo.

## **Description**

Calculate the kurtosis of the columns of a *time series* or a *matrix* using RcppArmadillo.

#### Usage

```
calc_kurtosis(tseries, method = "moment", con_fi = 0.75)
```

#### **Arguments**

tseries A *time series* or a *matrix* of data.

method A *string* specifying the type of the kurtosis model (the default is method =

"moment" - see Details).

con\_fi The confidence level for calculating the quantiles (the default is  $con_fi = 0.75$ ).

# **Details**

The function calc\_kurtosis() calculates the kurtosis of the columns of the *matrix* tseries using RcppArmadillo C++ code.

If method = "moment" (the default) then calc\_kurtosis() calculates the fourth moment of the data. But it doesn't de-mean the columns of tseries because that requires copying the matrix tseries, so it's time-consuming.

If method = "quantile" then it calculates the skewness  $\kappa$  from the differences between the quantiles of the data as follows:

$$\kappa = \frac{q_{\alpha} - q_{1-\alpha}}{q_{0.75} - q_{0.25}}$$

Where  $\alpha$  is the confidence level for calculating the quantiles.

If method = "nonparametric" then it calculates the kurtosis as the difference between the mean of the data minus its median, divided by the standard deviation.

If the number of rows of tseries is less than 3 then it returns zeros.

The code examples below compare the function calc\_kurtosis() with the kurtosis calculated using R code.

14 calc\_lm

#### Value

A single-row matrix with the kurtosis of the columns of tseries.

```
## Not run:
# Define a single-column time series of returns
re_turns <- na.omit(rutils::etf_env$re_turns$VTI)</pre>
# Calculate the moment kurtosis
HighFreq::calc_kurtosis(re_turns)
# Calculate the moment kurtosis in R
calc_kurtr <- function(x) {</pre>
  x \leftarrow (x-mean(x))
  sum(x^4)/var(x)^2/NROW(x)
} # end calc_kurtr
all.equal(HighFreq::calc_kurtosis(re_turns),
  calc_kurtr(re_turns), check.attributes=FALSE)
# Compare the speed of RcppArmadillo with R code
library(microbenchmark)
summary(microbenchmark(
  Rcpp=HighFreq::calc_kurtosis(re_turns),
  Rcode=calc_kurtr(re_turns),
  times=10))[, c(1, 4, 5)] # end microbenchmark summary
# Calculate the quantile kurtosis
\label{lighteq:con_fi} HighFreq::calc\_kurtosis(re\_turns, method="quantile", con\_fi=0.9)
# Calculate the quantile kurtosis in R
calc_kurtq <- function(x, a=0.9) {</pre>
   quantile_s <- quantile(x, c(1-a, 0.25, 0.75, a), type=5)
   (quantile_s[4] - quantile_s[1])/(quantile_s[3] - quantile_s[2])
} # end calc_kurtq
all.equal(drop(HighFreq::calc_kurtosis(re_turns, method="quantile", con_fi=0.9)),
  calc_kurtq(re_turns, a=0.9), check.attributes=FALSE)
# Compare the speed of RcppArmadillo with R code
summary(microbenchmark(
  Rcpp=HighFreq::calc_kurtosis(re_turns, method="quantile"),
  Rcode=calc_kurtq(re_turns),
  times=10))[, c(1, 4, 5)] # end microbenchmark summary
# Calculate the nonparametric kurtosis
HighFreq::calc_kurtosis(re_turns, method="nonparametric")
# Compare HighFreq::calc_kurtosis() with R nonparametric kurtosis
all.equal(drop(HighFreq::calc_kurtosis(re_turns, method="nonparametric")),
  (mean(re_turns)-median(re_turns))/sd(re_turns),
  check.attributes=FALSE)
\# Compare the speed of RcppArmadillo with R code
summary(microbenchmark(
  Rcpp=HighFreq::calc_kurtosis(re_turns, method="nonparametric"),
  Rcode=(mean(re_turns)-median(re_turns))/sd(re_turns),
  times=10))[, c(1, 4, 5)] # end microbenchmark summary
## End(Not run)
```

calc\_lm 15

# **Description**

Perform multivariate linear regression using least squares and return a named list of regression coefficients, their t-values, and p-values.

# Usage

```
calc_lm(response, design)
```

# Arguments

response A single-column *time series* or a *vector* of response data.

design A time series or a matrix of design data (predictor or explanatory data).

#### **Details**

The function calc\_lm() performs the same calculations as the function lm() from package *stats*. It uses RcppArmadillo C++ code so it's several times faster than lm(). The code was inspired by this article (but it's not identical to it): http://gallery.rcpp.org/articles/fast-linear-model-with-armadillo/

#### Value

A named list with three elements: a *matrix* of coefficients (named "coefficients"), the *z-score* of the last residual (named "z\_score"), and a *vector* with the R-squared and F-statistic (named "stats"). The numeric *matrix* of coefficients named "coefficients" contains the alpha and beta coefficients, and their *t-values* and *p-values*.

```
## Not run:
# Calculate historical returns
re_turns <- na.omit(rutils::etf_env$re_turns[, c("XLF", "VTI", "IEF")])</pre>
# Response equals XLF returns
res_ponse <- re_turns[, 1]</pre>
# Design matrix equals VTI and IEF returns
de_sign <- re_turns[, -1]</pre>
# Perform multivariate regression using lm()
reg_model <- lm(res_ponse ~ de_sign)</pre>
sum_mary <- summary(reg_model)</pre>
# Perform multivariate regression using calc_lm()
reg_arma <- HighFreq::calc_lm(response=res_ponse, design=de_sign)</pre>
# Compare the outputs of both functions
all.equal(reg_arma$coefficients[, "coeff"], unname(coef(reg_model)))
all.equal(unname(reg_arma$coefficients), unname(sum_mary$coefficients))
all.equal(unname(reg_arma$stats), c(sum_mary$r.squared, unname(sum_mary$fstatistic[1])))
# Compare the speed of RcppArmadillo with R code
summary(microbenchmark(
  Rcpp=HighFreq::calc_lm(response=res_ponse, design=de_sign),
  Rcode=lm(res_ponse ~ de_sign),
  times=10))[, c(1, 4, 5)] # end microbenchmark summary
## End(Not run)
```

16 calc\_mean

calc_mean	Calculate the mean (location) of the columns of a time series or a matrix using RcppArmadillo.

#### **Description**

Calculate the mean (location) of the columns of a time series or a matrix using RcppArmadillo.

## Usage

```
calc_mean(tseries, method = "moment", con_fi = 0.75)
```

# **Arguments**

tseries A time series or a matrix of data.

method A *string* specifying the type of the mean (location) model (the default is method

= "moment" - see Details).

con\_fi The confidence level for calculating the quantiles (the default is  $con_fi = 0.75$ ).

#### **Details**

The function calc\_mean() calculates the mean (location) values of the columns of the *time series* tseries using RcppArmadillo C++ code.

If method = "moment" (the default) then calc\_mean() calculates the location as the mean - the first moment of the data.

If method = "quantile" then it calculates the location  $\mu$  as the sum of the quantiles as follows:

$$\mu = q_{\alpha} + q_{1-\alpha}$$

Where  $\alpha$  is the confidence level for calculating the quantiles.

If method = "nonparametric" then it calculates the location as the median.

The code examples below compare the function calc\_mean() with the mean (location) calculated using R code.

## Value

A single-row matrix with the mean (location) of the columns of tseries.

```
## Not run:
# Calculate historical returns
re_turns <- na.omit(rutils::etf_env$re_turns[, c("XLP", "VTI")])
# Calculate the column means in RcppArmadillo
HighFreq::calc_mean(re_turns)
# Calculate the column means in R
sapply(re_turns, mean)
# Compare the values
all.equal(drop(HighFreq::calc_mean(re_turns)),
    sapply(re_turns, mean), check.attributes=FALSE)
# Compare the speed of RcppArmadillo with R code</pre>
```

calc\_ranks 17

```
library(microbenchmark)
summary(microbenchmark(
  Rcpp=HighFreq::calc_mean(re_turns),
  Rcode=sapply(re_turns, mean),
  times=10))[, c(1, 4, 5)] # end microbenchmark summary
# Calculate the quantile mean (location)
HighFreq::calc_mean(re_turns, method="quantile", con_fi=0.9)
# Calculate the quantile mean (location) in R
colSums(sapply(re_turns, quantile, c(0.9, 0.1), type=5))
# Compare the values
all.equal(drop(HighFreq::calc_mean(re_turns, method="quantile", con_fi=0.9)),
  colSums(sapply(re_turns, quantile, c(0.9, 0.1), type=5)),
  check.attributes=FALSE)
# Compare the speed of RcppArmadillo with R code
summary(microbenchmark(
  Rcpp=HighFreq::calc_mean(re_turns, method="quantile", con_fi=0.9),
  Rcode=colSums(sapply(re_turns, quantile, c(0.9, 0.1), type=5)),
  times=10))[, c(1, 4, 5)] # end microbenchmark summary
# Calculate the column medians in RcppArmadillo
HighFreq::calc_mean(re_turns, method="nonparametric")
# Calculate the column medians in R
sapply(re_turns, median)
# Compare the values
all.equal(drop(HighFreq::calc_mean(re_turns, method="nonparametric")),
  sapply(re_turns, median), check.attributes=FALSE)
# Compare the speed of RcppArmadillo with R code
summary(microbenchmark(
  Rcpp=HighFreq::calc_mean(re_turns, method="nonparametric"),
  Rcode=sapply(re_turns, median),
  times=10))[, c(1, 4, 5)] # end microbenchmark summary
## End(Not run)
```

calc\_ranks

Calculate the ranks of the elements of a single-column time series or a vector using RcppArmadillo.

# **Description**

Calculate the ranks of the elements of a single-column time series or a vector using RcppArmadillo.

# Usage

```
calc_ranks(tseries)
```

# **Arguments**

tseries

A single-column time series or a vector.

18 calc\_reg

#### **Details**

The function calc\_ranks() calculates the ranks of the elements of a single-column *time series* or a *vector*. It uses the RcppArmadillo function arma::sort\_index(). The function arma::sort\_index() calculates the permutation index to sort a given vector into ascending order.

Applying the function arma::sort\_index() twice: arma::sort\_index(arma::sort\_index()), calculates the *reverse* permutation index to sort the vector from ascending order back into its original unsorted order. The permutation index produced by: arma::sort\_index(arma::sort\_index()) is the *reverse* of the permutation index produced by: arma::sort\_index().

The ranks of the elements are equal to the *reverse* permutation index. The function calc\_ranks() calculates the *reverse* permutation index.

#### Value

An *integer vector* with the ranks of the elements of the tseries.

# **Examples**

```
## Not run:
# Create a vector of random data
da_ta <- round(runif(7), 2)</pre>
# Calculate the ranks of the elements in two ways
all.equal(rank(da_ta), drop(HighFreq::calc_ranks(da_ta)))
# Create a time series of random data
da_ta <- xts::xts(runif(7), seq.Date(Sys.Date(), by=1, length.out=7))</pre>
# Calculate the ranks of the elements in two ways
all.equal(rank(coredata(da_ta)), drop(HighFreq::calc_ranks(da_ta)))
# Compare the speed of RcppArmadillo with R code
da_ta <- runif(7)</pre>
library(microbenchmark)
summary(microbenchmark(
  Rcpp=calc_ranks(da_ta),
  Rcode=rank(da_ta),
  times=10))[, c(1, 4, 5)] # end microbenchmark summary
## End(Not run)
```

calc\_reg

Perform multivariate regression using different methods, and return a vector of regression coefficients, their t-values, and the last residual z-score.

# **Description**

Perform multivariate regression using different methods, and return a vector of regression coefficients, their t-values, and the last residual z-score.

calc\_reg 19

#### Usage

```
calc_reg(
  response,
  design,
  method = "least_squares",
  eigen_thresh = 0.001,
  eigen_max = 0L,
  con_fi = 0.1,
  alpha = 0
)
```

#### **Arguments**

A single-column time series or a vector of response data. response design A time series or a matrix of design data (predictor or explanatory data). method A string specifying the type of the regression model the default is method = "least\_squares" - see Details). A numeric threshold level for discarding small singular values in order to regueigen\_thresh larize the inverse of the design matrix (the default is 0.001). eigen\_max An *integer* equal to the number of singular values used for calculating the regularized inverse of the design matrix (the default is 0 - equivalent to eigen\_max equal to the number of columns of design). con\_fi The confidence level for calculating the quantiles (the default is  $con_fi = 0.75$ ).

#### **Details**

alpha

The function calc\_reg() performs multivariate regression using different methods, and returns a vector of regression coefficients, their t-values, and the last residual z-score.

The shrinkage intensity between 0 and 1. (the default is 0).

The length of the return vector depends on the number of columns of design. The number of regression coefficients is equal to the number of columns of design plus 1. The number of t-values is equal to the number of coefficients. And there is only 1 z-score. So if the number of columns of design is equal to n, then the return vector will have 2n+3 elements.

For example, if the design matrix has 2 columns of data, then calc\_reg() returns a vector with 7 elements: 3 regression coefficients (including the intercept coefficient), 3 corresponding t-values, and 1 z-score.

If method = "least\_squares" (the default) then it performs the standard least squares regression, the same as the function calc\_reg(), and the function lm() from package *stats*. It uses RcppArmadillo C++ code so it's several times faster than lm().

If method = "regular" then it performs regularized regression. It calculates the regularized inverse of the design matrix from its singular value decomposition. It applies dimension regularization by selecting only the largest singular values equal in number to eigen\_max.

If method = "quantile" then it performs quantile regression (not implemented yet).

# Value

A vector with the regression coefficients, their t-values, and the last residual z-score.

20 calc\_scaled

#### **Examples**

```
## Not run:
# Calculate historical returns
re_turns <- na.omit(rutils::etf_env$re_turns[, c("XLF", "VTI", "IEF")])</pre>
# Response equals XLF returns
res_ponse <- re_turns[, 1]</pre>
# Design matrix equals VTI and IEF returns
de_sign <- re_turns[, -1]</pre>
# Perform multivariate regression using lm()
reg_model <- lm(res_ponse ~ de_sign)</pre>
sum_mary <- summary(reg_model)</pre>
co_eff <- sum_mary$coefficients</pre>
# Perform multivariate regression using calc_reg()
reg_arma <- drop(HighFreq::calc_reg(response=res_ponse, design=de_sign))</pre>
# Compare the outputs of both functions
all.equal(reg_arma[1:(2*(1+NCOL(de_sign)))],
  c(co_eff[, "Estimate"], co_eff[, "t value"]), check.attributes=FALSE)
# Compare the speed of RcppArmadillo with R code
library(microbenchmark)
summary(microbenchmark(
  Rcpp=HighFreq::calc_reg(response=res_ponse, design=de_sign),
  Rcode=lm(res_ponse ~ de_sign),
  times=10))[, c(1, 4, 5)] # end microbenchmark summary
## End(Not run)
```

calc\_scaled

Scale (standardize) the columns of a matrix of data using RcppArmadillo.

# **Description**

Scale (standardize) the columns of a *matrix* of data using RcppArmadillo.

# Usage

```
calc_scaled(tseries, use_median = FALSE)
```

# **Arguments**

tseries A time series or matrix of data.

use\_median A Boolean argument: if TRUE then the centrality (central tendency) is calculated

as the *median* and the dispersion is calculated as the *median absolute deviation* (MAD). If use\_median = FALSE then the centrality is calculated as the *mean* and the dispersion is calculated as the *standard deviation* (the default is FALSE)

## **Details**

The function calc\_scaled() scales (standardizes) the columns of the tseries argument using RcppArmadillo.

calc\_skew 21

If the argument use\_median is FALSE (the default), then it performs the same calculation as the standard R function scale(), and it calculates the centrality (central tendency) as the *mean* and the dispersion as the *standard deviation*.

If the argument use\_median is TRUE, then it calculates the centrality as the *median* and the dispersion as the *median absolute deviation (MAD)*.

If the number of rows of tseries is less than 3 then it returns tseries unscaled.

The function calc\_scaled() uses RcppArmadillo C++ code and is about 5 times faster than function scale(), for a *matrix* with 1,000 rows and 20 columns.

#### Value

A *matrix* with the same dimensions as the input argument tseries.

# **Examples**

```
## Not run:
# Create a matrix of random data
re_turns <- matrix(rnorm(20000), nc=20)
scale_d <- calc_scaled(tseries=re_turns, use_median=FALSE)
scale_d2 <- scale(re_turns)
all.equal(scale_d, scale_d2, check.attributes=FALSE)
# Compare the speed of Rcpp with R code
library(microbenchmark)
summary(microbenchmark(
   Rcpp=calc_scaled(tseries=re_turns, use_median=FALSE),
   Rcode=scale(re_turns),
   times=100))[, c(1, 4, 5)] # end microbenchmark summary
## End(Not run)</pre>
```

calc\_skew

Calculate the skewness of the columns of a time series or a matrix using RcppArmadillo.

# Description

Calculate the skewness of the columns of a time series or a matrix using RcppArmadillo.

# Usage

```
calc_skew(tseries, method = "moment", con_fi = 0.75)
```

## **Arguments**

tseries	A time series or a matrix of data.
method	A <i>string</i> specifying the type of the skewness model (the default is method = "moment" - see Details).
con_fi	The confidence level for calculating the quantiles (the default is $con_fi = 0.75$ ).

22 calc\_skew

#### **Details**

The function calc\_skew() calculates the skewness of the columns of a *time series* or a *matrix* of data using RcppArmadillo C++ code.

If method = "moment" (the default) then calc\_skew() calculates the skewness as the third moment of the data.

If method = "quantile" then it calculates the skewness  $\varsigma$  from the differences between the quantiles of the data as follows:

$$\varsigma = \frac{q_\alpha + q_{1-\alpha} - 2*q_{0.5}}{q_\alpha - q_{1-\alpha}}$$

Where  $\alpha$  is the confidence level for calculating the quantiles.

If method = "nonparametric" then it calculates the skewness as the difference between the mean of the data minus its median, divided by the standard deviation.

If the number of rows of tseries is less than 3 then it returns zeros.

The code examples below compare the function calc\_skew() with the skewness calculated using R code.

#### Value

A single-row matrix with the skewness of the columns of tseries.

```
## Not run:
# Define a single-column time series of returns
re_turns <- na.omit(rutils::etf_env$re_turns$VTI)</pre>
# Calculate the moment skewness
HighFreq::calc_skew(re_turns)
# Calculate the moment skewness in R
calc_skewr <- function(x) {</pre>
  x \leftarrow (x-mean(x))
  sum(x^3)/var(x)^1.5/NROW(x)
} # end calc_skewr
all.equal(HighFreq::calc_skew(re_turns),
  calc_skewr(re_turns), check.attributes=FALSE)
# Compare the speed of RcppArmadillo with R code
library(microbenchmark)
summary(microbenchmark(
  Rcpp=HighFreq::calc_skew(re_turns),
  Rcode=calc_skewr(re_turns),
  times=10))[, c(1, 4, 5)] # end microbenchmark summary
# Calculate the quantile skewness
HighFreq::calc_skew(re_turns, method="quantile", con_fi=0.9)
\# Calculate the quantile skewness in R
calc_skewq \leftarrow function(x, a = 0.75) {
   quantile_s <- quantile(x, c(1-a, 0.5, a), type=5)
   (quantile_s[3] + quantile_s[1] - 2*quantile_s[2])/(quantile_s[3] - quantile_s[1])
} # end calc_skewq
all.equal(drop(HighFreq::calc_skew(re_turns, method="quantile", con_fi=0.9)),
  calc_skewq(re_turns, a=0.9), check.attributes=FALSE)
# Compare the speed of RcppArmadillo with R code
summary(microbenchmark(
  Rcpp=HighFreq::calc_skew(re_turns, method="quantile"),
  Rcode=calc_skewq(re_turns),
```

calc\_startpoints 23

```
times=10))[, c(1, 4, 5)] # end microbenchmark summary
# Calculate the nonparametric skewness
HighFreq::calc_skew(re_turns, method="nonparametric")
# Compare HighFreq::calc_skew() with R nonparametric skewness
all.equal(drop(HighFreq::calc_skew(re_turns, method="nonparametric")),
    (mean(re_turns)-median(re_turns))/sd(re_turns),
    check.attributes=FALSE)
# Compare the speed of RcppArmadillo with R code
summary(microbenchmark(
    Rcpp=HighFreq::calc_skew(re_turns, method="nonparametric"),
    Rcode=(mean(re_turns)-median(re_turns))/sd(re_turns),
    times=10))[, c(1, 4, 5)] # end microbenchmark summary
## End(Not run)
```

calc\_startpoints

Calculate a vector of start points by lagging (shifting) a vector of end points.

## **Description**

Calculate a vector of start points by lagging (shifting) a vector of end points.

# Usage

```
calc_startpoints(endp, look_back)
```

## **Arguments**

endp An *integer* vector of end points.

look\_back The length of the look-back interval, equal to the lag (shift) applied to the end

points.

# Details

The start points are equal to the values of the vector endp lagged (shifted) by an amount equal to look\_back. In addition, an extra value of 1 is added to them, to avoid data overlaps. The lag operation requires appending a beginning warmup interval containing zeros, so that the vector of start points has the same length as the endp.

For example, consider the end points for a vector of length 25 divided into equal intervals of length 5: 4,9,14,19,24. (In C++ the vector indexing starts at 0 not 1, so it's shifted by -1.) Then the start points for look\_back = 2 are equal to: 0,0,5,10,15. The differences between the end points minus the corresponding start points are equal to 9, except for the warmup interval.

## Value

An integer vector with the same number of elements as the vector endp.

24 calc\_var

#### **Examples**

```
# Calculate end points
end_p <- HighFreq::calc_endpoints(25, 5)
# Calculate start points corresponding to the end points
start_p <- HighFreq::calc_startpoints(end_p, 2)</pre>
```

calc\_var

Calculate the dispersion (variance) of the columns of a time series or a matrix using RcppArmadillo.

# Description

Calculate the dispersion (variance) of the columns of a *time series* or a *matrix* using RcppArmadillo.

## Usage

```
calc_var(tseries, method = "moment", con_fi = 0.75)
```

# **Arguments**

tseries A time series or a matrix of data.

method A *string* specifying the type of the dispersion model (the default is method =

"moment" - see Details).

#### **Details**

The dispersion is a measure of the variability of the data. Examples of dispersion are the variance and the Median Absolute Deviation (*MAD*).

The function calc\_var() calculates the dispersion of the columns of a *time series* or a *matrix* of data using RcppArmadillo C++ code.

If method = "moment" (the default) then calc\_var() calculates the dispersion as the second moment of the data  $\sigma^2$  (the variance).

If method = "moment" then calc\_var() performs the same calculation as the function colVars() from package matrixStats, but it's much faster because it uses RcppArmadillo C++ code.

If method = "quantile" then it calculates the dispersion as the difference between the quantiles as follows:

$$\mu = q_{\alpha} - q_{1-\alpha}$$

Where  $\alpha$  is the confidence level for calculating the quantiles.

If method = "nonparametric" then it calculates the dispersion as the Median Absolute Deviation (MAD):

$$MAD = median(abs(x - median(x)))$$

It also multiplies the MAD by a factor of 1.4826, to make it comparable to the standard deviation.

If method = "nonparametric" then calc\_var() performs the same calculation as the function stats::mad(), but it's much faster because it uses RcppArmadillo C++ code.

If the number of rows of tseries is less than 3 then it returns zeros.

calc\_var\_ag 25

#### Value

A row vector equal to the dispersion of the columns of the matrix tseries.

#### **Examples**

```
## Not run:
# Calculate VTI and XLF returns
re_turns <- na.omit(rutils::etf_env$re_turns[, c("VTI", "XLF")])</pre>
# Compare HighFreq::calc_var() with standard var()
all.equal(drop(HighFreq::calc_var(re_turns)),
  apply(re_turns, 2, var), check.attributes=FALSE)
# Compare HighFreq::calc_var() with matrixStats
all.equal(drop(HighFreq::calc_var(re_turns)),
  matrixStats::colVars(re_turns), check.attributes=FALSE)
# Compare the speed of RcppArmadillo with matrixStats and with R code
library(microbenchmark)
summary(microbenchmark(
  Rcpp=HighFreq::calc_var(re_turns),
  matrixStats=matrixStats::colVars(re_turns),
  Rcode=apply(re_turns, 2, var),
  times=10))[, c(1, 4, 5)] # end microbenchmark summary
# Compare HighFreq::calc_var() with stats::mad()
all.equal(drop(HighFreq::calc\_var(re\_turns, \ method="nonparametric")),\\
  sapply(re_turns, mad), check.attributes=FALSE)
# Compare the speed of RcppArmadillo with stats::mad()
summary(microbenchmark(
  Rcpp=HighFreq::calc_var(re_turns, method="nonparametric"),
  Rcode=sapply(re_turns, mad),
  times=10))[, c(1, 4, 5)] # end microbenchmark summary
## End(Not run)
```

calc\_var\_ag

Calculate the variance of returns aggregated over end points.

# **Description**

Calculate the variance of returns aggregated over end points.

# Usage

```
calc_var_ag(tseries, step = 1L)
```

#### **Arguments**

tseries A time series or a matrix of prices.

step The number of periods in each interval between neighboring end points.

26 calc\_var\_ohlc

#### **Details**

The function calc\_var\_ag() calculates the variance of returns aggregated over end points.

It first calculates the end points spaced apart by the number of periods equal to the argument step. Then it calculates the aggregated returns by differencing the prices tseries calculated at the end points. Finally it calculates the variance of the returns.

If there are extra periods that don't fit over the length of tseries, then calc\_var\_ag() loops over all possible stub intervals, then it calculates all the corresponding variance values, and averages them.

For example, if the number of rows of tseries is equal to 20, and step=3 then 6 end points fit over the length of tseries, and there are 2 extra periods that must fit into stubs, either at the beginning or at the end (or both).

The aggregated volatility  $\sigma_t$  scales (increases) with the length of the aggregation interval  $\Delta t$  raised to the power of the *Hurst exponent H*:

$$\sigma_t = \sigma \Delta t^H$$

Where  $\sigma$  is the daily return volatility.

The function calc\_var\_ag() can therefore be used to calculate the *Hurst exponent* from the volatility ratio.

#### Value

The variance of aggregated returns.

# **Examples**

```
## Not run:
# Calculate the log prices
price_s <- na.omit(rutils::etf_env$price_s[, c("XLP", "VTI")])
price_s <- log(price_s)
# Calculate the daily variance of percentage returns
calc_var_ag(price_s, step=1)
# Calculate the daily variance using R
sapply(rutils::diff_it(price_s), var)
# Calculate the variance of returns aggregated over 21 days
calc_var_ag(price_s, step=21)
# The variance over 21 days is approximately 21 times the daily variance
21*calc_var_ag(price_s, step=1)
## End(Not run)</pre>
```

calc\_var\_ohlc

Calculate the variance of OHLC prices using different price range estimators.

# Description

Calculate the variance of *OHLC* prices using different price range estimators.

calc\_var\_ohlc 27

#### Usage

```
calc_var_ohlc(
  ohlc,
  method = "yang_zhang",
  lag_close = 0L,
  scale = TRUE,
  in_dex = 0L
)
```

# **Arguments**

ohlc

A time series or a matrix of OHLC prices.

method

A *character* string representing the price range estimator for calculating the variance. The estimators include:

- "close" close-to-close estimator,
- "rogers\_satchell" Rogers-Satchell estimator,
- "garman\_klass" Garman-Klass estimator,
- "garman\_klass\_yz" Garman-Klass with account for close-to-open price jumps,
- "yang\_zhang" Yang-Zhang estimator,

(The default is the method = "yang\_zhang".)

lag\_close

A vector with the lagged close prices of the OHLC time series. This is an op-

tional argument. (The default is  $lag\_close = 0$ ).

scale

*Boolean* argument: Should the returns be divided by the time index, the number of seconds in each period? (The default is scale = TRUE).

in\_dex

A *vector* with the time index of the *time series*. This is an optional argument (the default is  $in_dex = 0$ ).

#### **Details**

The function calc\_var\_ohlc() calculates the variance from all the different intra-day and day-over-day returns (defined as the differences of *OHLC* prices), using several different variance estimation methods.

The input *OHLC time series* ohlc is assumed to be the log prices.

The default method is "yang\_zhang", which theoretically has the lowest standard error among unbiased estimators. The methods "close", "garman\_klass\_yz", and "yang\_zhang" do account for close-to-open price jumps, while the methods "garman\_klass" and "rogers\_satchell" do not account for close-to-open price jumps.

If scale is TRUE (the default), then the returns are divided by the differences of the time index (which scales the variance to the units of variance per second squared). This is useful when calculating the variance from minutely bar data, because dividing returns by the number of seconds decreases the effect of overnight price jumps. If the time index is in days, then the variance is equal to the variance per day squared.

If the number of rows of ohlc is less than 3 then it returns zero.

The optional argument in\_dex is the time index of the *time series* ohlc. If the time index is in seconds, then the differences of the index are equal to the number of seconds in each time period. If the time index is in days, then the differences are equal to the number of days in each time period.

The optional argument lag\_close are the lagged *close* prices of the *OHLC time series*. Passing in the lagged *close* prices speeds up the calculation, so it's useful for rolling calculations.

28 calc\_var\_ohlc\_ag

The function calc\_var\_ohlc() is implemented in RcppArmadillo C++ code, and it's over 10 times faster than calc\_var\_ohlc\_r(), which is implemented in R code.

#### Value

A single *numeric* value equal to the variance of the *OHLC time series*.

## **Examples**

```
## Not run:
# Extract the log OHLC prices of SPY
oh_lc <- log(HighFreq::SPY)</pre>
# Extract the time index of SPY prices
in_dex <- c(1, diff(xts::.index(oh_lc)))</pre>
# Calculate the variance of SPY returns, with scaling of the returns
HighFreq::calc_var_ohlc(oh_lc,
method="yang_zhang", scale=TRUE, in_dex=in_dex)
# Calculate variance without accounting for overnight jumps
HighFreq::calc_var_ohlc(oh_lc,
method="rogers_satchell", scale=TRUE, in_dex=in_dex)
# Calculate the variance without scaling the returns
HighFreq::calc_var_ohlc(oh_lc, scale=FALSE)
# Calculate the variance by passing in the lagged close prices
lag_close <- HighFreq::lag_it(oh_lc[, 4])</pre>
all.equal(HighFreq::calc_var_ohlc(oh_lc),
 HighFreq::calc_var_ohlc(oh_lc, lag_close=lag_close))
# Compare with HighFreq::calc_var_ohlc_r()
all.equal(HighFreq::calc_var_ohlc(oh_lc, in_dex=in_dex),
 HighFreq::calc_var_ohlc_r(oh_lc))
# Compare the speed of Rcpp with R code
library(microbenchmark)
summary(microbenchmark(
  Rcpp=HighFreq::calc_var_ohlc(oh_lc),
  Rcode=HighFreq::calc_var_ohlc_r(oh_lc),
  times=10))[, c(1, 4, 5)] # end microbenchmark summary
## End(Not run)
```

calc\_var\_ohlc\_ag

Calculate the variance of aggregated OHLC prices using different price range estimators.

# **Description**

Calculate the variance of aggregated *OHLC* prices using different price range estimators.

## Usage

```
calc_var_ohlc_ag(
  ohlc,
  step = 1L,
  method = "yang_zhang",
  lag_close = 0L,
  scale = TRUE,
```

calc\_var\_ohlc\_ag 29

```
in_dex = 0L
)
```

# **Arguments**

ohlc A time series or a matrix of OHLC prices.

step The number of periods in each interval between neighboring end points.

method A character string representing the price range estimator for calculating the vari-

ance. The estimators include:

• "close" close-to-close estimator,

• "rogers satchell" Rogers-Satchell estimator,

• "garman\_klass" Garman-Klass estimator,

• "garman\_klass\_yz" Garman-Klass with account for close-to-open price jumps,

• "yang\_zhang" Yang-Zhang estimator,

(The default is the method = "yang\_zhang".)

lag\_close A vector with the lagged close prices of the OHLC time series. This is an op-

tional argument. (The default is  $lag_close = 0$ ).

scale Boolean argument: Should the returns be divided by the time index, the number

of seconds in each period? (The default is scale = TRUE).

in\_dex A vector with the time index of the time series. This is an optional argument

(the default is  $in_dex = 0$ ).

# **Details**

The function calc\_var\_ohlc\_ag() calculates the variance of *OHLC* prices aggregated over end points.

It first calculates the end points spaced apart by the number of periods equal to the argument step. Then it aggregates the *OHLC* prices to the end points. Finally it calculates the variance of the aggregated *OHLC* prices.

If there are extra periods that don't fit over the length of ohlc, then calc\_var\_ohlc\_ag() loops over all possible stub intervals, it calculates all the corresponding variance values, and it averages them.

For example, if the number of rows of ohlc is equal to 20, and step=3 then 6 end points fit over the length of ohlc, and there are 2 extra periods that must fit into stubs, either at the beginning or at the end (or both).

The aggregated volatility  $\sigma_t$  scales (increases) with the length of the aggregation interval  $\Delta t$  raised to the power of the *Hurst exponent H*:

$$\sigma_t = \sigma \Delta t^H$$

Where  $\sigma$  is the daily return volatility.

The function calc\_var\_ohlc\_ag() can therefore be used to calculate the *Hurst exponent* from the volatility ratio.

# Value

The variance of aggregated OHLC prices.

30 calc\_var\_ohlc\_r

#### **Examples**

```
## Not run:
# Calculate the log ohlc prices
oh_lc <- log(rutils::etf_env$VTI)
# Calculate the daily variance of percentage returns
calc_var_ohlc_ag(oh_lc, step=1)
# Calculate the variance of returns aggregated over 21 days
calc_var_ohlc_ag(oh_lc, step=21)
# The variance over 21 days is approximately 21 times the daily variance
21*calc_var_ohlc_ag(oh_lc, step=1)
## End(Not run)</pre>
```

calc\_var\_ohlc\_r

Calculate the variance of an OHLC time series, using different range estimators for variance.

# **Description**

Calculate the variance of an *OHLC* time series, using different range estimators for variance.

# Usage

```
calc_var_ohlc_r(oh_lc, calc_method = "yang_zhang", scal_e = TRUE)
```

# Arguments

oh\_lc

An OHLC time series of prices in xts format.

 ${\tt calc\_method}$ 

A *character* string representing the method for estimating variance. The methods include:

- "close" close to close,
- "garman\_klass" Garman-Klass,
- "garman\_klass\_yz" Garman-Klass with account for close-to-open price jumps,
- "rogers\_satchell" Rogers-Satchell,
- "yang\_zhang" Yang-Zhang,

(default is "yang\_zhang")

scal\_e

*Boolean* argument: should the returns be divided by the number of seconds in each period? (default is TRUE)

# Details

The function calc\_var\_ohlc\_r() calculates the variance from all the different intra-day and day-over-day returns (defined as the differences of *OHLC* prices), using several different variance estimation methods.

The default method is "yang\_zhang", which theoretically has the lowest standard error among unbiased estimators. The methods "close", "garman\_klass\_yz", and "yang\_zhang" do account for close-to-open price jumps, while the methods "garman\_klass" and "rogers\_satchell" do not account for close-to-open price jumps.

calc\_var\_vec 31

If scal\_e is TRUE (the default), then the returns are divided by the differences of the time index (which scales the variance to the units of variance per second squared.) This is useful when calculating the variance from minutely bar data, because dividing returns by the number of seconds decreases the effect of overnight price jumps. If the time index is in days, then the variance is equal to the variance per day squared.

The function calc\_var\_ohlc\_r() is implemented in R code.

#### Value

A single *numeric* value equal to the variance.

# **Examples**

```
# Calculate the variance of SPY returns
HighFreq::calc_var_ohlc_r(HighFreq::SPY, calc_method="yang_zhang")
# Calculate variance without accounting for overnight jumps
HighFreq::calc_var_ohlc_r(HighFreq::SPY, calc_method="rogers_satchell")
# Calculate the variance without scaling the returns
HighFreq::calc_var_ohlc_r(HighFreq::SPY, scal_e=FALSE)
```

calc\_var\_vec

Calculate the variance of a a single-column time series or a vector using RcppArmadillo.

# Description

Calculate the variance of a a single-column time series or a vector using RcppArmadillo.

## Usage

```
calc_var_vec(tseries)
```

## **Arguments**

tseries

A single-column time series or a vector.

# **Details**

The function calc\_var\_vec() calculates the variance of a *vector* using RcppArmadillo C++ code, so it's significantly faster than the R function var().

## Value

A numeric value equal to the variance of the vector.

32 calc\_weights

# **Examples**

```
## Not run:
# Create a vector of random returns
re_turns <- rnorm(1e6)
# Compare calc_var_vec() with standard var()
all.equal(HighFreq::calc_var_vec(re_turns),
    var(re_turns))
# Compare the speed of RcppArmadillo with R code
library(microbenchmark)
summary(microbenchmark(
    Rcpp=HighFreq::calc_var_vec(re_turns),
    Rcode=var(re_turns),
    times=10))[, c(1, 4, 5)] # end microbenchmark summary
## End(Not run)</pre>
```

calc\_weights

Calculate the optimal portfolio weights for different types of objective functions.

# **Description**

Calculate the optimal portfolio weights for different types of objective functions.

# Usage

```
calc_weights(
  returns,
  method = "rank_sharpe",
  eigen_thresh = 0.001,
  eigen_max = 0L,
  con_fi = 0.1,
  alpha = 0,
  scale = TRUE,
  vol_target = 0.01
)
```

## **Arguments**

returns	A <i>time series</i> or a <i>matrix</i> of returns data (the returns in excess of the risk-free rate).
method	A <i>string</i> specifying the objective function for calculating the weights (see Details) (the default is method = "rank_sharpe")
eigen_thresh	A <i>numeric</i> threshold level for discarding small singular values in order to regularize the inverse of the returns matrix (the default is 0.001).
eigen_max	An <i>integer</i> equal to the number of singular values used for calculating the regularized inverse of the returns matrix (the default is 0 - equivalent to eigen_max equal to the number of columns of returns).
con_fi	The confidence level for calculating the quantiles (the default is $con_fi = 0.75$ ).

calc\_weights 33

alpha The shrinkage intensity between 0 and 1. (the default is 0).

scale A *Boolean* specifying whether the weights should be scaled (the default is scale = TRUE).

A *numeric* volatility target for scaling the weights (the default is 0.001)

# **Details**

vol\_target

The function calc\_weights() calculates the optimal portfolio weights for different types of objective functions, using RcppArmadillo C++ code.

If method = "rank\_sharpe" (the default) then it calculates the weights as the ranks (order index) of the trailing Sharpe ratios of the asset returns.

If method = "rank" then it calculates the weights as the ranks (order index) of the last row of the returns.

If method = "max\_sharpe" then calc\_weights() calculates the weights of the maximum Sharpe portfolio, by multiplying the inverse of the covariance *matrix* times the mean column returns.

If method = "min\_var" then it calculates the weights of the minimum variance portfolio under linear constraints.

If method = "min\_varpca" then it calculates the weights of the minimum variance portfolio under quadratic constraints (which is the highest order principal component).

If scale = TRUE (the default) then the weights are scaled so that the resulting portfolio has a volatility equal to vol\_target.

calc\_weights() calculates the regularized inverse of the covariance *matrix* of returns from its eigen decomposition. It applies dimension regularization by selecting only the largest eigenvalues equal in number to eigen\_max.

In addition, calc\_weights() applies shrinkage to the columns of returns, by shrinking their means to their common mean value. The shrinkage intensity alpha determines the amount of shrinkage that is applied, with alpha = 0 representing no shrinkage (with the column means of returns unchanged), and alpha = 1 representing complete shrinkage (with the column means of returns all equal to the single mean of all the columns).

# Value

A column *vector* of the same length as the number of columns of returns.

```
## Not run:
# Calculate covariance matrix of ETF returns
re_turns <- na.omit(rutils::etf_env$re_turns[, 1:16])
ei_gen <- eigen(cov(re_turns))
# Calculate regularized inverse of covariance matrix
eigen_max <- 3
eigen_vec <- ei_gen$vectors[, 1:eigen_max]
eigen_val <- ei_gen$values[1:eigen_max]
in_verse <- eigen_vec %*% (t(eigen_vec) / eigen_val)
# Define shrinkage intensity and apply shrinkage to the mean returns
al_pha <- 0.5
col_means <- colMeans(re_turns)
col_means <- ((1-al_pha)*col_means + al_pha*mean(col_means))
# Calculate weights using R
weight_s <- in_verse %*% col_means</pre>
```

34 diff\_it

```
n_col <- NCOL(re_turns)
weights_r <- weights_r*sd(re_turns %*% rep(1/n_col, n_col))/sd(re_turns %*% weights_r)
# Calculate weights using RcppArmadillo
weight_s <- drop(HighFreq::calc_weights(re_turns, eigen_max, alpha=al_pha))
all.equal(weight_s, weights_r)
## End(Not run)</pre>
```

diff\_it

Calculate the row differences of a a time series or a matrix using ReppArmadillo.

## **Description**

Calculate the row differences of a a time series or a matrix using RcppArmadillo.

## Usage

```
diff_it(tseries, lagg = 1L, pad_zeros = TRUE)
```

#### **Arguments**

tseries A time series or a matrix.

lagg An *integer* equal to the number of rows (time periods) to lag when calculating

the differences (the default is lagg = 1).

pad\_zeros Boolean argument: Should the output matrix be padded (extended) with zeros,

in order to return a matrix with the same number of rows as the input? (the

default is pad\_zeros = TRUE)

## **Details**

The function diff\_it() calculates the differences between the rows of the input *matrix* tseries and its lagged version.

The argument lagg specifies the number of lags applied to the rows of the lagged version of tseries. For positive lagg values, the lagged version of tseries has its rows shifted *forward* (down) by the number equal to lagg rows. For negative lagg values, the lagged version of tseries has its rows shifted *backward* (up) by the number equal to -lagg rows. For example, if lagg=3 then the lagged version will have its rows shifted down by 3 rows, and the differences will be taken between each row minus the row three time periods before it (in the past). The default is lagg = 1.

The argument pad\_zeros specifies whether the output *matrix* should be padded (extended) with the rows of the initial (warmup) period at the front, in order to return a *matrix* with the same number of rows as the input tseries. The default is pad\_zeros = TRUE. The padding operation can be time-consuming, because it requires the copying of data.

The function diff\_it() is implemented in RcppArmadillo C++ code, which makes it much faster than R code.

# Value

A matrix containing the differences between the rows of the input matrix tseries.

diff\_vec 35

#### **Examples**

```
## Not run:
# Create a matrix of random data
da_ta <- matrix(sample(15), nc=3)</pre>
# Calculate differences with lagged rows
HighFreq::diff_it(da_ta, lagg=2)
# Calculate differences with advanced rows
HighFreq::diff_it(da_ta, lagg=-2)
# Compare HighFreq::diff_it() with rutils::diff_it()
all.equal(HighFreq::diff_it(da_ta, lagg=2),
  rutils::diff_it(da_ta, lagg=2),
  check.attributes=FALSE)
# Compare the speed of RcppArmadillo with R code
library(microbenchmark)
summary(microbenchmark(
  Rcpp=HighFreq::diff_it(da_ta, lagg=2),
  Rcode=rutils::diff_it(da_ta, lagg=2),
  times=10))[, c(1, 4, 5)] # end microbenchmark summary
## End(Not run)
```

diff\_vec

Calculate the differences between the neighboring elements of a single-column time series or a vector.

# **Description**

Calculate the differences between the neighboring elements of a single-column *time series* or a *vector*.

# Usage

```
diff_vec(tseries, lagg = 1L, pad_zeros = TRUE)
```

# **Arguments**

tseries A single-column time series or a vector.

lagg An *integer* equal to the number of time periods to lag when calculating the dif-

ferences (the default is lagg = 1).

pad\_zeros Boolean argument: Should the output vector be padded (extended) with ze-

ros, in order to return a vector of the same length as the input? (the default is

pad\_zeros = TRUE)

## **Details**

The function diff\_vec() calculates the differences between the input *time series* or *vector* and its lagged version.

The argument lagg specifies the number of lags. For example, if lagg=3 then the differences will be taken between each element minus the element three time periods before it (in the past). The default is lagg = 1.

36 hf\_data

The argument pad\_zeros specifies whether the output *vector* should be padded (extended) with zeros at the front, in order to return a *vector* of the same length as the input. The default is pad\_zeros = TRUE. The padding operation can be time-consuming, because it requires the copying of data.

The function diff\_vec() is implemented in RcppArmadillo C++ code, which makes it several times faster than R code.

#### Value

A column *vector* containing the differences between the elements of the input vector.

## **Examples**

```
## Not run:
# Create a vector of random returns
re_turns <- rnorm(1e6)
# Compare diff_vec() with rutils::diff_it()
all.equal(drop(HighFreq::diff_vec(re_turns, lagg=3, pad=TRUE)),
    rutils::diff_it(re_turns, lagg=3))
# Compare the speed of RcppArmadillo with R code
library(microbenchmark)
summary(microbenchmark(
    Rcpp=HighFreq::diff_vec(re_turns, lagg=3, pad=TRUE),
    Rcode=rutils::diff_it(re_turns, lagg=3),
    times=10))[, c(1, 4, 5)] # end microbenchmark summary
## End(Not run)</pre>
```

hf\_data

High frequency data sets

# **Description**

hf\_data.RData is a file containing the datasets:

**SPY** an xts time series containing 1-minute OHLC bar data for the SPY etf, from 2008-01-02 to 2014-05-19. SPY contains 625,425 rows of data, each row contains a single minute bar.

TLT an xts time series containing 1-minute OHLC bar data for the TLT etf, up to 2014-05-19.

VXX an xts time series containing 1-minute OHLC bar data for the VXX etf, up to 2014-05-19.

# Usage

```
data(hf_data) # not required - data is lazy load
```

## **Format**

Each xts time series contains OHLC data, with each row containing a single minute bar:

**Open** Open price in the bar

**High** High price in the bar

Low Low price in the bar

**Close** Close price in the bar

Volume trading volume in the bar

lag\_it 37

#### Source

```
https://wrds-web.wharton.upenn.edu/wrds/
```

#### References

Wharton Research Data Service (WRDS)

### **Examples**

```
# data(hf_data) # not required - data is lazy load
head(SPY)
chart_Series(x=SPY["2009"])
```

lag\_it Apply a lag to the rows of a time series or a matrix using RcppArmadillo.

### **Description**

Apply a lag to the rows of a time series or a matrix using RcppArmadillo.

### Usage

```
lag_it(tseries, lagg = 1L, pad_zeros = TRUE)
```

# **Arguments**

tseries A time series or a matrix.

lagg An *integer* equal to the number of periods to lag (the default is lagg = 1).

pad\_zeros Boolean argument: Should the output be padded with zeros? (The default is

pad\_zeros = TRUE.)

# **Details**

The function lag\_it() applies a lag to the input *matrix* by shifting its rows by the number equal to the argument lagg. For positive lagg values, the rows are shifted *forward* (down), and for negative lagg values they are shifted *backward* (up).

The output *matrix* is padded with either zeros (the default), or with rows of data from tseries, so that it has the same dimensions as tseries. If the lagg is positive, then the first row is copied and added upfront. If the lagg is negative, then the last row is copied and added to the end.

As a rule, if tseries contains returns data, then the output *matrix* should be padded with zeros, to avoid data snooping. If tseries contains prices, then the output *matrix* should be padded with the prices.

# Value

A *matrix* with the same dimensions as the input argument tseries.

38 lag\_vec

### **Examples**

```
## Not run:
# Create a matrix of random returns
re_turns <- matrix(rnorm(5e6), nc=5)
# Compare lag_it() with rutils::lag_it()
all.equal(HighFreq::lag_it(re_turns),
    rutils::lag_it(re_turns))
# Compare the speed of RcppArmadillo with R code
library(microbenchmark)
summary(microbenchmark(
    Rcpp=HighFreq::lag_it(re_turns),
    Rcode=rutils::lag_it(re_turns),
    times=10))[, c(1, 4, 5)] # end microbenchmark summary
## End(Not run)</pre>
```

lag\_vec

Apply a lag to a single-column time series or a vector using RcppArmadillo.

### **Description**

Apply a lag to a single-column time series or a vector using RcppArmadillo.

# Usage

```
lag_vec(tseries, lagg = 1L, pad_zeros = TRUE)
```

# **Arguments**

tseries A single-column *time series* or a *vector*.

lagg An *integer* equal to the number of periods to lag (the default is lagg = 1).

pad\_zeros Boolean argument: Should the output be padded with zeros? (The default is

pad\_zeros = TRUE.)

# Details

The function lag\_vec() applies a lag to the input *time series* tseries by shifting its elements by the number equal to the argument lagg. For positive lagg values, the elements are shifted forward in time (down), and for negative lagg values they are shifted backward (up).

The output *vector* is padded with either zeros (the default), or with data from tseries, so that it has the same number of element as tseries. If the lagg is positive, then the first element is copied and added upfront. If the lagg is negative, then the last element is copied and added to the end.

As a rule, if tseries contains returns data, then the output *matrix* should be padded with zeros, to avoid data snooping. If tseries contains prices, then the output *matrix* should be padded with the prices.

### Value

A column *vector* with the same number of elements as the input time series.

mult\_vec\_mat 39

### **Examples**

```
## Not run:
# Create a vector of random returns
re_turns <- rnorm(1e6)
# Compare lag_vec() with rutils::lag_it()
all.equal(drop(HighFreq::lag_vec(re_turns)),
    rutils::lag_it(re_turns))
# Compare the speed of RcppArmadillo with R code
library(microbenchmark)
summary(microbenchmark(
    Rcpp=HighFreq::lag_vec(re_turns),
    Rcode=rutils::lag_it(re_turns),
    times=10))[, c(1, 4, 5)] # end microbenchmark summary
## End(Not run)</pre>
```

mult\_vec\_mat

Multiply in place (without copying) the columns or rows of a matrix times a vector, element-wise.

### **Description**

Multiply in place (without copying) the columns or rows of a matrix times a vector, element-wise.

# Usage

```
mult_vec_mat(vector, matrix, by_col = TRUE)
```

# Arguments

vector A vector.
matrix A matrix.

by\_col A Boolean argument: if TRUE then multiply the columns, otherwise multiply the

rows (the default is by\_col = TRUE.)

### **Details**

The function mult\_vec\_mat() multiplies the columns or rows of a *matrix* times a *vector*, element-wise

If the number of *vector* elements is equal to the number of matrix columns, then it multiplies the columns by the *vector*, and returns the number of columns. If the number of *vector* elements is equal to the number of rows, then it multiplies the rows, and returns the number of rows.

If the *matrix* is square and if by\_col is TRUE then it multiplies the columns, otherwise it multiplies the rows.

It accepts *pointers* to the *matrix* and *vector*, and replaces the old *matrix* values with the new values. It performs the calculation in place, without copying the *matrix* in memory (which greatly increases the computation speed). It performs an implicit loop over the *matrix* rows and columns using the *Armadillo* operators each\_row() and each\_col(), instead of performing explicit for() loops (both methods are equally fast).

40 random\_ohlc

The function mult\_vec\_mat() uses RcppArmadillo C++ code, so when multiplying large *matrix* columns it's several times faster than vectorized R code, and it's even much faster compared to R when multiplying the *matrix* rows.

#### Value

A single *integer* value, equal to either the number of *matrix* columns or the number of rows.

### **Examples**

```
## Not run:
# Multiply matrix columns using R
mat_rix <- matrix(round(runif(25e4), 2), nc=5e2)</pre>
vec_tor <- round(runif(5e2), 2)</pre>
prod_uct <- vec_tor*mat_rix</pre>
# Multiply the matrix in place
HighFreq::mult_vec_mat(vec_tor, mat_rix)
all.equal(prod_uct, mat_rix)
\# Compare the speed of Rcpp with R code
library(microbenchmark)
summary(microbenchmark(
    Rcpp=HighFreq::mult_vec_mat(vec_tor, mat_rix),
    Rcode=vec_tor*mat_rix,
    times=10))[, c(1, 4, 5)] # end microbenchmark summary
# Multiply matrix rows using R
mat_rix <- matrix(round(runif(25e4), 2), nc=5e2)</pre>
vec_tor <- round(runif(5e2), 2)</pre>
prod_uct <- t(vec_tor*t(mat_rix))</pre>
# Multiply the matrix in place
HighFreq::mult_vec_mat(vec_tor, mat_rix, by_col=FALSE)
all.equal(prod_uct, mat_rix)
# Compare the speed of Rcpp with R code
library(microbenchmark)
summary(microbenchmark(
    Rcpp=HighFreq::mult_vec_mat(vec_tor, mat_rix, by_col=FALSE),
    Rcode=t(vec_tor*t(mat_rix)),
    times=10))[, c(1, 4, 5)] # end microbenchmark summary
## End(Not run)
```

random\_ohlc

Calculate a random OHLC time series of prices and trading volumes, in xts format.

# **Description**

Calculate a random *OHLC* time series either by simulating random prices following geometric Brownian motion, or by randomly sampling from an input time series.

random\_ohlc 41

### Usage

```
random_ohlc(
  oh_lc = NULL,
  re_duce = TRUE,
  vol_at = 6.5e-05,
  dri_ft = 0,
  in_dex = seq(from = as.POSIXct(paste(Sys.Date() - 3, "09:30:00")), to =
    as.POSIXct(paste(Sys.Date() - 1, "16:00:00")), by = "1 sec"),
  ...
)
```

# **Arguments**

oh_lc	An <i>OHLC</i> time series of prices and trading volumes, in <i>xts</i> format (default is <i>NULL</i> ).
vol_at	The volatility per period of the in_dex time index (default is 6.5e-05 per second, or about 0.01=1.0% per day).
dri_ft	The drift per period of the in_dex time index (default is 0.0).
in_dex	The time index for the <i>OHLC</i> time series.
re_duce	<i>Boolean</i> argument: should oh_1c time series be transformed to reduced form? (default is TRUE)

### **Details**

If the input oh\_lc time series is *NULL* (the default), then the function random\_ohlc() simulates a minutely *OHLC* time series of random prices following geometric Brownian motion, over the two previous calendar days.

If the input oh\_lc time series is not *NULL*, then the rows of oh\_lc are randomly sampled, to produce a random time series.

If re\_duce is TRUE (the default), then the oh\_lc time series is first transformed to reduced form, then randomly sampled, and finally converted to standard form.

Note: randomly sampling from an intraday time series over multiple days will cause the overnight price jumps to be re-arranged into intraday price jumps. This will cause moment estimates to become inflated compared to the original time series.

# Value

An xts time series with the same dimensions and the same time index as the input oh\_lc time series.

```
# Create minutely synthetic OHLC time series of random prices
oh_lc <- HighFreq::random_ohlc()
# Create random time series from SPY by randomly sampling it
oh_lc <- HighFreq::random_ohlc(oh_lc=HighFreq::SPY["2012-02-13/2012-02-15"])</pre>
```

42 roll\_apply

remove_jumps	Remove overnight close-to-open price jumps from an OHLC time series, by adding adjustment terms to its prices.

### **Description**

Remove overnight close-to-open price jumps from an *OHLC* time series, by adding adjustment terms to its prices.

# Usage

```
remove_jumps(oh_lc)
```

### **Arguments**

oh\_lc

An OHLC time series of prices and trading volumes, in xts format.

#### **Details**

The function remove\_jumps() removes the overnight close-to-open price jumps from an *OHLC* time series, by adjusting its prices so that the first *Open* price of the day is equal to the last *Close* price of the previous day.

The function remove\_jumps() adds adjustment terms to all the *OHLC* prices, so that intra-day returns and volatilities are not affected.

The function remove\_jumps() identifies overnight periods as those that are greater than 60 seconds. This assumes that intra-day periods between neighboring rows of data are 60 seconds or less.

The time index of the oh\_lc time series is assumed to be in *POSIXct* format, so that its internal value is equal to the number of seconds that have elapsed since the *epoch*.

### Value

An *OHLC* time series with the same dimensions and the same time index as the input oh\_1c time series.

# **Examples**

```
# Remove overnight close-to-open price jumps from SPY data
oh_lc <- remove_jumps(HighFreq::SPY)</pre>
```

roll\_apply Apply an aggregation function over a rolling look-back interval and the end points of an OHLC time series, using R code.

# **Description**

Apply an aggregation function over a rolling look-back interval and the end points of an *OHLC* time series, using R code.

roll\_apply 43

### Usage

```
roll_apply(
   x_ts,
   agg_fun,
   look_back = 2,
   end_points = seq_along(x_ts),
   by_columns = FALSE,
   out_xts = TRUE,
   ...
)
```

### **Arguments**

	additional parameters to the function agg_fun.
x_ts	An OHLC time series of prices and trading volumes, in xts format.
agg_fun	The name of the aggregation function to be applied over a rolling look-back interval.
look_back	The number of end points in the look-back interval used for applying the aggregation function (including the current row).
by_columns	<i>Boolean</i> argument: should the function agg_fun() be applied column-wise (individually), or should it be applied to all the columns combined? (default is FALSE)
out_xts	Boolean argument: should the output be coerced into an $xts$ series? (default is TRUE)
end_points	An integer vector of end points.

# **Details**

The function roll\_apply() applies an aggregation function over a rolling look-back interval attached at the end points of an *OHLC* time series.

The function roll\_apply() is implemented in R code.

HighFreq::roll\_apply() performs similar operations to the functions rollapply() and period.apply() from package xts, and also the function apply.rolling() from package PerformanceAnalytics. (The function rollapply() isn't exported from the package xts.)

But HighFreq::roll\_apply() is faster because it performs less type-checking and skips other overhead. Unlike the other functions, roll\_apply() doesn't produce any leading *NA* values.

The function roll\_apply() can be called in two different ways, depending on the argument end\_points. If the argument end\_points isn't explicitly passed to roll\_apply(), then the default value is used, and roll\_apply() performs aggregations over overlapping intervals at each point in time.

If the argument end\_points is explicitly passed to roll\_apply(), then roll\_apply() performs aggregations over intervals attached at the end\_points. If look\_back=2 then the aggregations are performed over non-overlapping intervals, otherwise they are performed over overlapping intervals.

If the argument out\_xts is TRUE (the default) then the output is coerced into an *xts* series, with the number of rows equal to the length of argument end\_points. Otherwise a list is returned, with the length equal to the length of argument end\_points.

If out\_xts is TRUE and the aggregation function agg\_fun() returns a single value, then roll\_apply() returns an xts time series with a single column. If out\_xts is TRUE and if agg\_fun() returns a vector of values, then roll\_apply() returns an xts time series with multiple columns, equal to the length of the vector returned by the aggregation function agg\_fun().

44 roll\_backtest

#### Value

Either an *xts* time series with the number of rows equal to the length of argument end\_points, or a list the length of argument end\_points.

# **Examples**

```
# extract a single day of SPY data
oh_lc <- HighFreq::SPY["2012-02-13"]
inter_val <- 11 # number of data points between end points</pre>
look_back <- 4 # number of end points in look-back interval</pre>
# Calculate the rolling sums of oh_lc columns over a rolling look-back interval
agg_regations <- roll_apply(oh_lc, agg_fun=sum, look_back=look_back, by_columns=TRUE)
# Apply a vector-valued aggregation function over a rolling look-back interval
agg_function <- function(oh_lc) c(max(oh_lc[, 2]), min(oh_lc[, 3]))</pre>
agg_regations <- roll_apply(oh_lc, agg_fun=agg_function, look_back=look_back)</pre>
# Define end points at 11-minute intervals (HighFreq::SPY is minutely bars)
end_points <- rutils::end_points(oh_lc, inter_val=inter_val)</pre>
# Calculate the sums of oh_lc columns over end_points using non-overlapping intervals
agg_regations <- roll_apply(oh_lc, agg_fun=sum, end_points=end_points, by_columns=TRUE)
# Apply a vector-valued aggregation function over the end_points of oh_lc
# using overlapping intervals
agg_regations <- roll_apply(oh_lc, agg_fun=agg_function,</pre>
                             look_back=5, end_points=end_points)
```

roll\_backtest

Perform a backtest simulation of a trading strategy (model) over a vector of end points along a time series of prices.

### Description

Perform a backtest simulation of a trading strategy (model) over a vector of end points along a time series of prices.

# Usage

```
roll_backtest(
    x_ts,
    train_func,
    trade_func,
    look_back = look_forward,
    look_forward,
    end_points = rutils::calc_endpoints(x_ts, look_forward),
    ...
)
```

### **Arguments**

... additional parameters to the functions train\_func() and trade\_func().

x\_ts A time series of prices, asset returns, trading volumes, and other data, in xts

format.

train\_func The name of the function for training (calibrating) a forecasting model, to be

applied over a rolling look-back interval.

roll\_backtest 45

trade_func	The name of the trading model function, to be applied over a rolling look-forward interval.
look_back	The size of the look-back interval, equal to the number of rows of data used for training the forecasting model.
look_forward	The size of the look-forward interval, equal to the number of rows of data used for trading the strategy.
end_points	A vector of end points along the rows of the x_ts time series, given as either integers or dates.

#### **Details**

The function roll\_backtest() performs a rolling backtest simulation of a trading strategy over a vector of end points. At each end point, it trains (calibrates) a forecasting model using past data taken from the x\_ts time series over the look-back interval, and applies the forecasts to the trade\_func() trading model, using out-of-sample future data from the look-forward interval.

The function trade\_func() should simulate the trading model, and it should return a named list with at least two elements: a named vector of performance statistics, and an xts time series of out-of-sample returns. The list returned by trade\_func() can also have additional elements, like the in-sample calibrated model statistics, etc.

The function roll\_backtest() returns a named list containing the lists returned by function trade\_func(). The list names are equal to the *end\_points* dates. The number of list elements is equal to the number of *end\_points* minus two (because the first and last end points can't be included in the backtest).

# Value

An xts time series with the number of rows equal to the number of end points minus two.

```
## Not run:
# Combine two time series of prices
price_s <- cbind(rutils::etf_env$XLU, rutils::etf_env$XLP)</pre>
look_back <- 252
look_forward <- 22</pre>
# Define end points
end_points <- rutils::calc_endpoints(price_s, look_forward)</pre>
# Perform back-test
back_test <- roll_backtest(end_points=end_points,</pre>
    look_forward=look_forward,
    look_back=look_back,
    train_func = train_model,
    trade_func = trade_model,
    model_params = model_params,
    trading_params = trading_params,
    x_ts=price_s)
## End(Not run)
```

46 roll\_conv

roll_conv	Calculate the rolling convolutions (weighted sums) of a time series with a column vector of weights.

### **Description**

Calculate the rolling convolutions (weighted sums) of a time series with a column vector of weights.

### Usage

```
roll_conv(tseries, weights)
```

# **Arguments**

tseries A *time series* or a *matrix* of data. weights A *column vector* of weights.

### **Details**

The function roll\_conv() calculates the convolutions of the *matrix* columns with a *column vector* of weights. It performs a loop over the *matrix* rows and multiplies the past (higher) values by the weights. It calculates the rolling weighted sums of the past values.

The function roll\_conv() uses the RcppArmadillo function arma::conv2(). It performs a similar calculation to the standard R function filter(x=tseries, filter=weight\_s,method="convolution",sides=1), but it's over 6 times faster, and it doesn't produce any leading NA values.

# Value

A *matrix* with the same dimensions as the input argument tseries.

```
## Not run:
# First example
# Calculate a time series of prices
re_turns <- na.omit(rutils::etf_env$re_turns[, c("IEF", "VTI")])</pre>
# Create simple weights equal to a 1 value plus zeros
weight_s <- matrix(c(1, rep(0, 10)), nc=1)
# Calculate rolling weighted sums
weight_ed <- HighFreq::roll_conv(re_turns, weight_s)</pre>
# Compare with original
all.equal(coredata(re_turns), weight_ed, check.attributes=FALSE)
# Second example
# Calculate exponentially decaying weights
weight_s <- \exp(-0.2*(1:11))
weight_s <- matrix(weight_s/sum(weight_s), nc=1)</pre>
# Calculate rolling weighted sums
weight_ed <- HighFreq::roll_conv(re_turns, weight_s)</pre>
# Calculate rolling weighted sums using filter()
filter_ed <- filter(x=re_turns, filter=weight_s, method="convolution", sides=1)</pre>
# Compare both methods
all.equal(filter_ed[-(1:11), ], weight_ed[-(1:11), ], check.attributes=FALSE)
```

roll\_count 47

## End(Not run)

roll\_count Count the number of consecutive TRUE elements in a Boolean vector, and reset the count to zero after every FALSE element.

# Description

Count the number of consecutive TRUE elements in a Boolean vector, and reset the count to zero after every FALSE element.

# Usage

```
roll_count(tseries)
```

# **Arguments**

tseries

A Boolean vector of data.

#### **Details**

The function roll\_count() calculates the number of consecutive TRUE elements in a Boolean vector, and it resets the count to zero after every FALSE element.

For example, the Boolean vector FALSE, TRUE, TRUE, FALSE, FALSE, TRUE, T

# Value

An *integer vector* of the same length as the argument tseries.

# **Examples**

```
## Not run:
# Calculate the number of consecutive TRUE elements
drop(HighFreq::roll_count(c(FALSE, TRUE, TRUE, FALSE, FALSE, TRUE, TRUE, TRUE, TRUE, TRUE, TRUE, TRUE, FALSE)))
## End(Not run)
```

roll\_fun *Calculate a* matrix *of estimator values over a rolling look-back inter- val attached at the end points of a* time series *or a* matrix.

# Description

Calculate a *matrix* of estimator values over a rolling look-back interval attached at the end points of a *time series* or a *matrix*.

48 roll\_fun

### Usage

```
roll_fun(
   tseries,
   fun = "calc_var",
   startp = 0L,
   endp = 0L,
   step = 1L,
   look_back = 1L,
   stub = 0L,
   method = "moment",
   con_fi = 0.75
)
```

### **Arguments**

tseries	A time series or a matrix of data.
fun	A <i>string</i> specifying the estimator function (the default is fun = "calc_var".)
startp	An <i>integer</i> vector of start points (the default is $startp = 0$ ).
endp	An <i>integer</i> vector of end points (the default is endp = $\emptyset$ ).
step	The number of time periods between the end points (the default is $step = 1$ ).
look_back	The number of end points in the look-back interval (the default is look_back = 1).
stub	An <i>integer</i> value equal to the first end point for calculating the end points (the default is stub = $0$ ).
method	A <i>string</i> specifying the type of the model for the estimator (the default is method = "moment".)
con_fi	The confidence level for calculating the quantiles (the default is $con_fi = 0.75$ ).

# **Details**

The function roll\_fun() calculates a *matrix* of estimator values, over rolling look-back intervals attached at the end points of the *time series* tseries.

The function roll\_fun() performs a loop over the end points, and at each end point it subsets the time series tseries over a look-back interval equal to look\_back number of end points.

It passes the subset time series to the function specified by the argument fun, which calculates the statistic. See the functions calc\_\*() for a description of the different estimators.

If the arguments endp and startp are not given then it first calculates a vector of end points separated by step time periods. It calculates the end points along the rows of design using the function calc\_endpoints(), with the number of time periods between the end points equal to step time periods.

For example, the rolling variance at 25 day end points, with a 75 day look-back, can be calculated using the parameters step = 25 and  $look_back = 3$ .

The function roll\_fun() is implemented in RcppArmadillo C++ code, so it's many times faster than the equivalent R code.

### Value

A *matrix* with the same number of columns as the input time series tseries, and the number of rows equal to the number of end points.

roll\_hurst 49

#### **Examples**

```
## Not run:
# Define time series of returns using package rutils
re_turns <- na.omit(rutils::etf_env$re_turns$VTI)</pre>
# Calculate the rolling variance at 25 day end points, with a 75 day look-back
var_rollfun <- HighFreq::roll_fun(re_turns, fun="calc_var", step=25, look_back=3)</pre>
# Calculate the rolling variance using roll_var()
var_roll <- HighFreq::roll_var(re_turns, step=25, look_back=3)</pre>
# Compare the two methods
all.equal(var_rollfun, var_roll, check.attributes=FALSE)
# Define end points and start points
end_p <- HighFreq::calc_endpoints(NROW(re_turns), step=25)</pre>
start_p <- HighFreq::calc_startpoints(end_p, look_back=3)</pre>
# Calculate the rolling variance using RcppArmadillo
var_rollfun <- HighFreq::roll_fun(re_turns, fun="calc_var", startp=start_p, endp=end_p)</pre>
# Calculate the rolling variance using R code
var_roll <- sapply(1:NROW(end_p), function(it) {</pre>
 var(re_turns[start_p[it]:end_p[it]+1, ])
}) # end sapply
# Compare the two methods
all.equal(drop(var_rollfun), var_roll, check.attributes=FALSE)
# Compare the speed of RcppArmadillo with R code
library(microbenchmark)
summary(microbenchmark(
  Rcpp=HighFreq::roll_fun(re_turns, fun="calc_var", startp=start_p, endp=end_p),
  Rcode=sapply(1:NROW(end_p), function(it) {
    var(re_turns[start_p[it]:end_p[it]+1, ])
  }),
  times=10))[, c(1, 4, 5)] # end microbenchmark summary
## End(Not run)
```

roll\_hurst

Calculate a time series of Hurst exponents over a rolling look-back interval.

### **Description**

Calculate a time series of *Hurst* exponents over a rolling look-back interval.

#### Usage

```
roll_hurst(oh_lc, look_back = 11)
```

# **Arguments**

oh\_lc An *OHLC* time series of prices in *xts* format.

look\_back The size of the look-back interval, equal to the number of rows of data used for

aggregating the OHLC prices.

50 roll\_kurtosis

#### **Details**

The function roll\_hurst() calculates a time series of *Hurst* exponents from *OHLC* prices, over a rolling look-back interval.

The *Hurst* exponent is defined as the logarithm of the ratio of the price range, divided by the standard deviation of returns, and divided by the logarithm of the interval length.

The function roll\_hurst() doesn't use the same definition as the rescaled range definition of the *Hurst* exponent. First, because the price range is calculated using *High* and *Low* prices, which produces bigger range values, and higher *Hurst* exponent estimates. Second, because the *Hurst* exponent is estimated using a single aggregation interval, instead of multiple intervals in the rescaled range definition.

The rationale for using a different definition of the *Hurst* exponent is that it's designed to be a technical indicator for use as input into trading models, rather than an estimator for statistical analysis.

### Value

An xts time series with a single column and the same number of rows as the argument oh\_lc.

# Examples

```
# Calculate rolling Hurst for SPY in March 2009
hurst_rolling <- roll_hurst(oh_lc=HighFreq::SPY["2009-03"], look_back=11)
chart_Series(hurst_rolling["2009-03-10/2009-03-12"], name="SPY hurst_rolling")</pre>
```

roll\_kurtosis

Calculate a matrix of kurtosis estimates over a rolling look-back interval attached at the end points of a time series or a matrix.

# **Description**

Calculate a *matrix* of kurtosis estimates over a rolling look-back interval attached at the end points of a *time series* or a *matrix*.

# Usage

```
roll_kurtosis(
   tseries,
   startp = 0L,
   endp = 0L,
   step = 1L,
   look_back = 1L,
   stub = 0L,
   method = "moment",
   con_fi = 0.75
)
```

roll\_kurtosis 51

# **Arguments**

tserie	!S	A time series or a matrix of data.
startp	)	An <i>integer</i> vector of start points (the default is $startp = 0$ ).
endp		An <i>integer</i> vector of end points (the default is endp = $\emptyset$ ).
step		The number of time periods between the end points (the default is $step = 1$ ).
look_b	ack	The number of end points in the look-back interval (the default is look_back = 1).
stub		An <i>integer</i> value equal to the first end point for calculating the end points (the default is $stub = 0$ ).
method	I	A <i>string</i> specifying the type of the kurtosis model (the default is method = "moment" - see Details).
con_fi		The confidence level for calculating the quantiles (the default is $con_fi = 0.75$ ).

#### **Details**

The function roll\_kurtosis() calculates a *matrix* of kurtosis estimates over rolling look-back intervals attached at the end points of the *time series* tseries.

The function roll\_kurtosis() performs a loop over the end points, and at each end point it subsets the time series over a look-back interval equal to look\_back number of end points.

It passes the subset time series to the function calc\_kurtosis(), which calculates the kurtosis. See the function calc\_kurtosis() for a description of the kurtosis methods.

If the arguments endp and startp are not given then it first calculates a vector of end points separated by step time periods. It calculates the end points along the rows of design using the function calc\_endpoints(), with the number of time periods between the end points equal to step time periods.

For example, the rolling kurtosis at 25 day end points, with a 75 day look-back, can be calculated using the parameters step = 25 and  $look_back = 3$ .

The function roll\_kurtosis() is implemented in RcppArmadillo C++ code, so it's many times faster than the equivalent R code.

# Value

A *matrix* of kurtosis estimates with the same number of columns as the input time series tseries, and the number of rows equal to the number of end points.

```
## Not run:
# Define time series of returns using package rutils
re_turns <- na.omit(rutils::etf_env$re_turns$VTI)
# Define end points and start points
end_p <- 1 + HighFreq::calc_endpoints(NROW(re_turns), step=25)
start_p <- HighFreq::calc_startpoints(end_p, look_back=3)
# Calculate the rolling kurtosis at 25 day end points, with a 75 day look-back
kurto_sis <- HighFreq::roll_kurtosis(re_turns, step=25, look_back=3)
# Calculate the rolling kurtosis using R code
kurt_r <- sapply(1:NROW(end_p), function(it) {
    HighFreq::calc_kurtosis(re_turns[start_p[it]:end_p[it], ])
}) # end sapply
# Compare the kurtosis estimates</pre>
```

52 roll\_mean

```
all.equal(drop(kurto_sis), kurt_r, check.attributes=FALSE)
# Compare the speed of RcppArmadillo with R code
library(microbenchmark)
summary(microbenchmark(
    Rcpp=HighFreq::roll_kurtosis(re_turns, step=25, look_back=3),
    Rcode=sapply(1:NROW(end_p), function(it) {
        HighFreq::calc_kurtosis(re_turns[start_p[it]:end_p[it], ])
    }),
    times=10))[, c(1, 4, 5)] # end microbenchmark summary
## End(Not run)
```

roll\_mean

Calculate a matrix of mean (location) estimates over a rolling look-back interval attached at the end points of a time series or a matrix.

# **Description**

Calculate a *matrix* of mean (location) estimates over a rolling look-back interval attached at the end points of a *time series* or a *matrix*.

# Usage

```
roll_mean(
   tseries,
   startp = 0L,
   endp = 0L,
   step = 1L,
   look_back = 1L,
   stub = 0L,
   method = "moment",
   con_fi = 0.75
)
```

# **Arguments**

tseries	A time series or a matrix of data.
startp	An <i>integer</i> vector of start points (the default is $startp = 0$ ).
endp	An <i>integer</i> vector of end points (the default is endp = $\emptyset$ ).
step	The number of time periods between the end points (the default is $step = 1$ ).
look_back	The number of end points in the look-back interval (the default is look_back = 1).
stub	An <i>integer</i> value equal to the first end point for calculating the end points (the default is $stub = 0$ ).
method	A <i>character</i> string representing the type of mean measure of (the default is method = "moment").

roll\_mean 53

#### **Details**

The function roll\_mean() calculates a *matrix* of mean (location) estimates over rolling look-back intervals attached at the end points of the *time series* tseries.

The function roll\_mean() performs a loop over the end points, and at each end point it subsets the time series tseries over a look-back interval equal to look\_back number of end points.

It passes the subset time series to the function calc\_mean(), which calculates the mean (location). See the function calc\_mean() for a description of the mean methods.

If the arguments endp and startp are not given then it first calculates a vector of end points separated by step time periods. It calculates the end points along the rows of tseries using the function calc\_endpoints(), with the number of time periods between the end points equal to step time periods.

For example, the rolling mean at 25 day end points, with a 75 day look-back, can be calculated using the parameters step = 25 and  $look_back = 3$ .

The function roll\_mean() with the parameter step = 1 performs the same calculation as the function roll\_mean() from package RcppRoll, but it's several times faster because it uses RcppArmadillo C++ code.

The function roll\_mean() is implemented in RcppArmadillo C++ code, so it's many times faster than the equivalent R code.

If only a simple rolling mean is required (not the median) then other functions like roll\_sum() or roll\_vec() may be even faster.

#### Value

A *matrix* of mean (location) estimates with the same number of columns as the input time series tseries, and the number of rows equal to the number of end points.

```
# Define time series of returns using package rutils
re_turns <- na.omit(rutils::etf_env$re_turns$VTI)</pre>
# Calculate the rolling means at 25 day end points, with a 75 day look-back
means <- HighFreq::roll_mean(re_turns, step=25, look_back=3)</pre>
# Compare the mean estimates over 11-period look-back intervals
all.equal(HighFreq::roll_mean(re_turns, look_back=11)[-(1:10), ],
  drop(RcppRoll::roll_mean(re_turns, n=11)), check.attributes=FALSE)
# Define end points and start points
end_p <- HighFreq::calc_endpoints(NROW(re_turns), step=25)</pre>
start_p <- HighFreq::calc_startpoints(end_p, look_back=3)</pre>
# Calculate the rolling means using RcppArmadillo
means <- HighFreq::roll_mean(re_turns, startp=start_p, endp=end_p)</pre>
# Calculate the rolling medians using RcppArmadillo
medianscpp <- HighFreq::roll_mean(re_turns, startp=start_p, endp=end_p, method="nonparametric")</pre>
# Calculate the rolling medians using R
medians = sapply(1:NROW(end_p), function(i) {
 median(re_turns[start_p[i]:end_p[i] + 1])
}) # end sapply
all.equal(medians, drop(medianscpp))
# Compare the speed of RcppArmadillo with R code
library(microbenchmark)
summary(microbenchmark(
 Rcpp=HighFreq::roll_mean(re_turns, startp=start_p, endp=end_p, method="nonparametric"),
```

54 roll\_ohlc

```
Rcode=sapply(1:NROW(end_p), function(i) {median(re_turns[start_p[i]:end_p[i] + 1])}),
times=10))[, c(1, 4, 5)]
## End(Not run)
```

roll\_ohlc

Aggregate a time series to an OHLC time series with lower periodicity.

### **Description**

Given a time series of prices at a higher periodicity (say seconds), it calculates the *OHLC* prices at a lower periodicity (say minutes).

# Usage

```
roll_ohlc(tseries, endp)
```

#### **Arguments**

tseries A *time series* or a *matrix* with multiple columns of data.

endp An *integer vector* of end points.

### **Details**

The function roll\_ohlc() performs a loop over the end points *endp*, along the rows of the data tseries. At each end point, it selects the past rows of the data tseries, starting at the first bar after the previous end point, and then calls the function agg\_ohlc() on the selected data tseries to calculate the aggregations.

The function roll\_ohlc() can accept either a single column of data or four columns of *OHLC* data. It can also accept an additional column containing the trading volume.

The function roll\_ohlc() performs a similar aggregation as the function to.period() from package xts.

# Value

A matrix with OHLC data, with the number of rows equal to the number of endp minus one.

```
## Not run:
# Define matrix of OHLC data
oh_lc <- rutils::etf_env$VTI[, 1:5]
# Define end points at 25 day intervals
end_p <- HighFreq::calc_endpoints(NROW(oh_lc), step=25)
# Aggregate over end_p:
ohlc_agg <- HighFreq::roll_ohlc(tseries=oh_lc, endp=end_p)
# Compare with xts::to.period()
ohlc_agg_xts <- .Call("toPeriod", oh_lc, as.integer(end_p+1), TRUE, NCOL(oh_lc), FALSE, FALSE, colnames(oh_lc)
all.equal(ohlc_agg, coredata(ohlc_agg_xts), check.attributes=FALSE)
## End(Not run)</pre>
```

roll\_reg 55

roll_reg	Calculate a matrix of regression coefficients, their t-values, and z-
	scores, at the end points of the design matrix.

# Description

Calculate a *matrix* of regression coefficients, their t-values, and z-scores, at the end points of the design matrix.

# Usage

```
roll_reg(
  response,
  design,
  startp = 0L,
  endp = 0L,
  step = 1L,
  look_back = 1L,
  stub = 0L,
  method = "least_squares",
  eigen_thresh = 0.001,
  eigen_max = 0L,
  con_fi = 0.1,
  alpha = 0
)
```

# Arguments

response	A single-column time series or a vector of response data.
design	A time series or a matrix of design data (predictor or explanatory data).
startp	An <i>integer</i> vector of start points (the default is $startp = 0$ ).
endp	An <i>integer</i> vector of end points (the default is endp = $\emptyset$ ).
step	The number of time periods between the end points (the default is $step = 1$ ).
look_back	The number of end points in the look-back interval (the default is look_back = 1).
stub	An <i>integer</i> value equal to the first end point for calculating the end points (the default is $stub = 0$ ).
method	A <i>string</i> specifying the type of the regression model the default is method = "least_squares" - see Details).
eigen_thresh	A <i>numeric</i> threshold level for discarding small singular values in order to regularize the inverse of the design matrix (the default is 0.001).
eigen_max	An <i>integer</i> equal to the number of singular values used for calculating the regularized inverse of the design matrix (the default is $\emptyset$ - equivalent to eigen_max equal to the number of columns of design).
con_fi	The confidence level for calculating the quantiles (the default is $con_fi = 0.75$ ).
alpha	The shrinkage intensity between $\emptyset$ and 1. (the default is $\emptyset$ ).

56 roll\_scale

#### **Details**

The function roll\_reg() calculates a *matrix* of regression coefficients, their t-values, and z-scores at the end points of the design matrix.

The function roll\_reg() performs a loop over the end points, and at each end point it subsets the time series design over a look-back interval equal to look\_back number of end points.

It passes the subset time series to the function calc\_reg(), which calculates the regression data.

If the arguments endp and startp are not given then it first calculates a vector of end points separated by step time periods. It calculates the end points along the rows of design using the function calc\_endpoints(), with the number of time periods between the end points equal to step time periods.

For example, the rolling regression at 25 day end points, with a 75 day look-back, can be calculated using the parameters step = 25 and look\_back = 3.

#### Value

A *matrix* with the same number of rows as design, and a number of columns equal to 2n+3, where n is the number of columns of design.

### **Examples**

```
## Not run:
# Calculate historical returns
re_turns <- na.omit(rutils::etf_env$re_turns[, c("XLP", "VTI")])</pre>
# Define monthly end points and start points
end_p <- xts::endpoints(re_turns, on="months")[-1]</pre>
look_back <- 12
start_p <- c(rep(1, look_back), end_p[1:(NROW(end_p)-look_back)])</pre>
# Calculate rolling betas using RcppArmadillo
reg_stats <- HighFreq::roll_reg(response=re_turns[, 1], design=re_turns[, 2], endp=(end_p-1), startp=(start_r</pre>
beta_s <- reg_stats[, 2]</pre>
# Calculate rolling betas in R
betas_r <- sapply(1:NROW(end_p), FUN=function(ep) {</pre>
  da_ta <- re_turns[start_p[ep]:end_p[ep], ]</pre>
  drop(cov(da_ta[, 1], da_ta[, 2])/var(da_ta[, 2]))
}) # end sapply
# Compare the outputs of both functions
all.equal(beta_s, betas_r, check.attributes=FALSE)
## End(Not run)
```

roll\_scale

Perform a rolling scaling (standardization) of the columns of a matrix of data using RcppArmadillo.

# Description

Perform a rolling scaling (standardization) of the columns of a matrix of data using RcppArmadillo.

### Usage

```
roll_scale(matrix, look_back, use_median = FALSE)
```

roll\_sharpe 57

### **Arguments**

use\_median A Boolean argument: if TRUE then the centrality (central tendency) is calculated

as the *median* and the dispersion is calculated as the *median absolute deviation* (*MAD*). If use\_median is FALSE then the centrality is calculated as the *mean* and the dispersion is calculated as the *standard deviation* (the default is use\_median

= FALSE)

matrix A matrix of data.

look\_back The length of the look-back interval, equal to the number of rows of data used

in the scaling.

#### Details

The function roll\_scale() performs a rolling scaling (standardization) of the columns of the matrix argument using RcppArmadillo. The function roll\_scale() performs a loop over the rows of matrix, subsets a number of previous (past) rows equal to look\_back, and scales the subset matrix. It assigns the last row of the scaled subset *matrix* to the return matrix.

If the argument use\_median is FALSE (the default), then it performs the same calculation as the function roll::roll\_scale(). If the argument use\_median is TRUE, then it calculates the centrality as the *median* and the dispersion as the *median absolute deviation (MAD)*.

#### Value

A *matrix* with the same dimensions as the input argument matrix.

# **Examples**

```
## Not run:
mat_rix <- matrix(rnorm(20000), nc=2)
look_back <- 11
rolled_scaled <- roll::roll_scale(data=mat_rix, width = look_back, min_obs=1)
rolled_scaled2 <- roll_scale(matrix=mat_rix, look_back = look_back, use_median=FALSE)
all.equal(rolled_scaled[-1, ], rolled_scaled2[-1, ])
## End(Not run)</pre>
```

roll\_sharpe

Calculate a time series of Sharpe ratios over a rolling look-back interval for an OHLC time series.

# **Description**

Calculate a time series of Sharpe ratios over a rolling look-back interval for an OHLC time series.

# Usage

```
roll_sharpe(oh_lc, look_back = 11)
```

58 roll\_skew

# **Arguments**

oh\_lc An *OHLC* time series of prices in *xts* format.

look\_back The size of the look-back interval, equal to the number of rows of data used for

aggregating the OHLC prices.

# **Details**

The function roll\_sharpe() calculates the rolling Sharpe ratio defined as the ratio of percentage returns over the look-back interval, divided by the average volatility of percentage returns.

#### Value

An xts time series with a single column and the same number of rows as the argument oh\_lc.

### **Examples**

```
# Calculate rolling Sharpe ratio over SPY
sharpe_rolling <- roll_sharpe(oh_lc=HighFreq::SPY, look_back=11)</pre>
```

roll\_skew

Calculate a matrix of skewness estimates over a rolling look-back interval attached at the end points of a time series or a matrix.

### **Description**

Calculate a *matrix* of skewness estimates over a rolling look-back interval attached at the end points of a *time series* or a *matrix*.

# Usage

```
roll_skew(
   tseries,
   startp = 0L,
   endp = 0L,
   step = 1L,
   look_back = 1L,
   stub = 0L,
   method = "moment",
   con_fi = 0.75
)
```

# **Arguments**

tseries A time series or a matrix of data.

startp An integer vector of start points (the default is startp = 0).

endp An integer vector of end points (the default is endp = 0).

step The number of time periods between the end points (the default is step = 1).

look\_back The number of end points in the look-back interval (the default is look\_back = 1).

roll\_skew 59

stub	An <i>integer</i> value equal to the first end point for calculating the end points (the default is $stub = 0$ ).
method	A <i>string</i> specifying the type of the skewness model (the default is method = "moment" - see Details).
con_fi	The confidence level for calculating the quantiles (the default is $con_fi = 0.75$ ).

#### **Details**

The function roll\_skew() calculates a *matrix* of skewness estimates over rolling look-back intervals attached at the end points of the *time series* tseries.

The function roll\_skew() performs a loop over the end points, and at each end point it subsets the time series tseries over a look-back interval equal to look\_back number of end points.

It passes the subset time series to the function calc\_skew(), which calculates the skewness. See the function calc\_skew() for a description of the skewness methods.

If the arguments endp and startp are not given then it first calculates a vector of end points separated by step time periods. It calculates the end points along the rows of tseries using the function calc\_endpoints(), with the number of time periods between the end points equal to step time periods.

For example, the rolling skewness at 25 day end points, with a 75 day look-back, can be calculated using the parameters step = 25 and look\_back = 3.

The function roll\_skew() is implemented in RcppArmadillo C++ code, so it's many times faster than the equivalent R code.

### Value

A *matrix* of skewness estimates with the same number of columns as the input time series tseries, and the number of rows equal to the number of end points.

```
## Not run:
# Define time series of returns using package rutils
re_turns <- na.omit(rutils::etf_env$re_turns$VTI)</pre>
# Define end points and start points
end_p <- 1 + HighFreq::calc_endpoints(NROW(re_turns), step=25)</pre>
start_p <- HighFreq::calc_startpoints(end_p, look_back=3)</pre>
# Calculate the rolling skewness at 25 day end points, with a 75 day look-back
skew_ness <- HighFreq::roll_skew(re_turns, step=25, look_back=3)</pre>
# Calculate the rolling skewness using R code
skew_r <- sapply(1:NROW(end_p), function(it) {</pre>
 HighFreq::calc_skew(re_turns[start_p[it]:end_p[it], ])
}) # end sapply
# Compare the skewness estimates
all.equal(drop(skew_ness), skew_r, check.attributes=FALSE)
\# Compare the speed of RcppArmadillo with R code
library(microbenchmark)
summary(microbenchmark(
  Rcpp=HighFreq::roll_skew(re_turns, step=25, look_back=3),
  Rcode=sapply(1:NROW(end_p), function(it) {
    HighFreq::calc_skew(re_turns[start_p[it]:end_p[it], ])
  }),
  times=10))[, c(1, 4, 5)] # end microbenchmark summary
```

roll\_stats

roll\_stats Calculate a vector of statistics over an OHLC time series, and calculate a rolling mean over the statistics.

### **Description**

Calculate a vector of statistics over an *OHLC* time series, and calculate a rolling mean over the statistics.

# Usage

```
roll_stats(
  oh_lc,
  calc_stats = "run_variance",
  look_back = 11,
  weight_ed = TRUE,
  ...
)
```

### **Arguments**

additional parameters to the function calc\_stats.
 An OHLC time series of prices and trading volumes, in xts format.
 The name of the function for estimating statistics of a single row of OHLC data, such as volatility, skew, and higher moments.
 The size of the look-back interval, equal to the number of rows of data used for calculating the rolling mean.
 Boolean argument: should statistic be weighted by trade volume? (default TRUE)

# **Details**

The function roll\_stats() calculates a vector of statistics over an *OHLC* time series, such as volatility, skew, and higher moments. The statistics could also be any other aggregation of a single row of *OHLC* data, for example the *High* price minus the *Low* price squared. The length of the vector of statistics is equal to the number of rows of the argument oh\_lc. Then it calculates a trade volume weighted rolling mean over the vector of statistics over and calculate statistics.

### Value

An xts time series with a single column and the same number of rows as the argument oh\_lc.

```
# Calculate time series of rolling variance and skew estimates
var_rolling <- roll_stats(oh_lc=HighFreq::SPY, look_back=21)
skew_rolling <- roll_stats(oh_lc=HighFreq::SPY, calc_stats="run_skew", look_back=21)
skew_rolling <- skew_rolling/(var_rolling)^(1.5)
skew_rolling[1, ] <- 0
skew_rolling <- rutils::na_locf(skew_rolling)</pre>
```

roll\_sum 61

roll\_sum

Calculate the rolling sums over a time series or a matrix using Rcpp.

### **Description**

Calculate the rolling sums over a *time series* or a *matrix* using *Rcpp*.

# Usage

```
roll_sum(tseries, look_back = 1L)
```

### **Arguments**

tseries A time series or a matrix.

look\_back The length of the look-back interval, equal to the number of data points included

in calculating the rolling sum (the default is look\_back = 1).

### **Details**

The function roll\_sum() calculates the rolling sums over the columns of the data tseries.

The function roll\_sum() returns a *matrix* with the same dimensions as the input argument tseries.

The function roll\_sum() uses the fast RcppArmadillo function arma::cumsum(), without explicit loops. The function roll\_sum() is several times faster than rutils::roll\_sum() which uses vectorized R code.

# Value

A matrix with the same dimensions as the input argument tseries.

```
## Not run:
# Calculate historical returns
re_turns <- na.omit(rutils::etf_env$re_turns[, c("VTI", "IEF")])
# Define parameters
look_back <- 22
# Calculate rolling sums and compare with rutils::roll_sum()
c_sum <- HighFreq::roll_sum(re_turns, look_back)
r_sum <- rutils::roll_sum(re_turns, look_back)
all.equal(c_sum, coredata(r_sum), check.attributes=FALSE)
# Calculate rolling sums using R code
r_sum <- apply(zoo::coredata(re_turns), 2, cumsum)
lag_sum <- rbind(matrix(numeric(2*look_back), nc=2), r_sum[1:(NROW(r_sum) - look_back),])
r_sum <- (r_sum - lag_sum)
all.equal(c_sum, r_sum, check.attributes=FALSE)
## End(Not run)</pre>
```

62 roll\_sumep

roll\_sumep

Calculate the rolling sums at the end points of a time series or a matrix.

### **Description**

Calculate the rolling sums at the end points of a time series or a matrix.

# Usage

```
roll_sumep(
  tseries,
  startp = 0L,
  endp = 0L,
  step = 1L,
  look_back = 1L,
  stub = 0L
)
```

### **Arguments**

tseries	A time series or a matrix.
startp	An <i>integer</i> vector of start points (the default is $startp = 0$ ).
endp	An <i>integer</i> vector of end points (the default is endp = $\emptyset$ ).
step	The number of time periods between the end points (the default is step = 1).
look_back	The number of end points in the look-back interval (the default is look_back = 1).
stub	An <i>integer</i> value equal to the first end point for calculating the end points.

### **Details**

The function roll\_sumep() calculates the rolling sums at the end points of the *time series* tseries. The function roll\_sumep() is implemented in RcppArmadillo C++ code, which makes it several times faster than R code.

# Value

A *matrix* with the same number of columns as the input time series tseries, and the number of rows equal to the number of end points.

```
## Not run:
# Calculate historical returns
re_turns <- na.omit(rutils::etf_env$re_turns[, c("VTI", "IEF")])
# Define end points at 25 day intervals
end_p <- HighFreq::calc_endpoints(NROW(re_turns), step=25)
# Define start points as 75 day lag of end points
start_p <- HighFreq::calc_startpoints(end_p, look_back=3)
# Calculate rolling sums using Rcpp
c_sum <- HighFreq::roll_sumep(re_turns, startp=start_p, endp=end_p)</pre>
```

roll\_var 63

```
# Calculate rolling sums using R code
r_sum <- sapply(1:NROW(end_p), function(ep) {
colSums(re_turns[(start_p[ep]+1):(end_p[ep]+1), ])
}) # end sapply
r_sum <- t(r_sum)
all.equal(c_sum, r_sum, check.attributes=FALSE)
## End(Not run)</pre>
```

roll\_var

Calculate a matrix of dispersion (variance) estimates over a rolling look-back interval attached at the end points of a time series or a matrix.

# Description

Calculate a *matrix* of dispersion (variance) estimates over a rolling look-back interval attached at the end points of a *time series* or a *matrix*.

# Usage

```
roll_var(
  tseries,
  startp = 0L,
  endp = 0L,
  step = 1L,
  look_back = 1L,
  stub = 0L,
  method = "moment",
  con_fi = 0.75
)
```

# Arguments

tseries	A time series or a matrix of data.
startp	An <i>integer</i> vector of start points (the default is $startp = 0$ ).
endp	An <i>integer</i> vector of end points (the default is endp = $\emptyset$ ).
step	The number of time periods between the end points (the default is step = 1).
look_back	The number of end points in the look-back interval (the default is look_back = 1).
stub	An <i>integer</i> value equal to the first end point for calculating the end points (the default is $stub = 0$ ).
method	A <i>character</i> string representing the type of the measure of dispersion (the default is method = "moment").

64 roll\_var

#### **Details**

The function roll\_var() calculates a *matrix* of dispersion (variance) estimates over rolling look-back intervals attached at the end points of the *time series* tseries.

The function roll\_var() performs a loop over the end points, and at each end point it subsets the time series tseries over a look-back interval equal to look\_back number of end points.

It passes the subset time series to the function calc\_var(), which calculates the dispersion. See the function calc\_var() for a description of the dispersion methods.

If the arguments endp and startp are not given then it first calculates a vector of end points separated by step time periods. It calculates the end points along the rows of tseries using the function calc\_endpoints(), with the number of time periods between the end points equal to step time periods.

For example, the rolling variance at 25 day end points, with a 75 day look-back, can be calculated using the parameters step = 25 and look\_back = 3.

The function roll\_var() with the parameter step = 1 performs the same calculation as the function roll\_var() from package RcppRoll, but it's several times faster because it uses RcppArmadillo C++ code.

The function roll\_var() is implemented in RcppArmadillo C++ code, so it's many times faster than the equivalent R code.

### Value

A *matrix* dispersion (variance) estimates with the same number of columns as the input time series tseries, and the number of rows equal to the number of end points.

```
## Not run:
# Define time series of returns using package rutils
re_turns <- na.omit(rutils::etf_env$re_turns$VTI)</pre>
# Calculate the rolling variance at 25 day end points, with a 75 day look-back
vari_ance <- HighFreq::roll_var(re_turns, step=25, look_back=3)</pre>
# Compare the variance estimates over 11-period look-back intervals
all.equal(HighFreq::roll_var(re_turns, look_back=11)[-(1:10), ],
  drop(RcppRoll::roll_var(re_turns, n=11)), check.attributes=FALSE)
# Compare the speed of HighFreq::roll_var() with RcppRoll::roll_var()
library(microbenchmark)
summary(microbenchmark(
  Rcpp=HighFreq::roll_var(re_turns, look_back=11),
  RcppRoll=RcppRoll::roll_var(re_turns, n=11),
  times=10))[, c(1, 4, 5)] # end microbenchmark summary
# Compare the speed of HighFreq::roll_var() with TTR::runMAD()
summary(microbenchmark(
    Rcpp=HighFreq::roll_var(re_turns, look_back=11, method="quantile"),
    TTR=TTR::runMAD(re_turns, n = 11),
    times=10))[, c(1, 4, 5)] # end microbenchmark summary
## End(Not run)
```

roll\_var\_ohlc 65

roll_var_ohlc	Calculate a vector of variance estimates over a rolling look-back interval attached at the end points of a time series or a matrix with OHLC price data.
	price data.

# Description

Calculate a *vector* of variance estimates over a rolling look-back interval attached at the end points of a *time series* or a *matrix* with *OHLC* price data.

# Usage

```
roll_var_ohlc(
  ohlc,
  startp = 0L,
  endp = 0L,
  step = 1L,
  look_back = 1L,
  stub = 0L,
  method = "yang_zhang",
  scale = TRUE,
  in_dex = 0L
)
```

# **Arguments** ohlc

ohlc	A time series or a matrix with OHLC price data.
startp	An <i>integer</i> vector of start points (the default is $startp = 0$ ).
endp	An <i>integer</i> vector of end points (the default is endp = $\emptyset$ ).
step	The number of time periods between the end points (the default is $step = 1$ ).
look_back	The number of end points in the look-back interval (the default is look_back = 1).
stub	An <i>integer</i> value equal to the first end point for calculating the end points (the default is stub = $0$ ).
method	A <i>character</i> string representing the price range estimator for calculating the variance. The estimators include:
	• "close" close-to-close estimator,
	<ul> <li>"rogers_satchell" Rogers-Satchell estimator,</li> </ul>
	<ul> <li>"garman_klass" Garman-Klass estimator,</li> </ul>
	• "garman_klass_yz" Garman-Klass with account for close-to-open price jumps,
	<ul> <li>"yang_zhang" Yang-Zhang estimator,</li> </ul>
	(The default is the "yang_zhang" estimator.)
scale	<i>Boolean</i> argument: Should the returns be divided by the time index, the number of seconds in each period? (The default is scale = TRUE.)
in_dex	A <i>vector</i> with the time index of the <i>time series</i> . This is an optional argument (the default is in_dex=0).

66 roll\_var\_ohlc

#### **Details**

The function roll\_var\_ohlc() calculates a *vector* of variance estimates over a rolling look-back interval attached at the end points of the *time series* ohlc.

The input *OHLC time series* ohlc is assumed to contain the log prices.

The function roll\_var\_ohlc() performs a loop over the end points, subsets the previous (past) rows of ohlc, and passes them into the function calc\_var\_ohlc().

At each end point, the variance is calculated over a look-back interval equal to look\_back number of end points. In the initial warmup period, the variance is calculated over an expanding look-back interval.

If the arguments endp and startp are not given then it first calculates a vector of end points separated by step time periods. It calculates the end points along the rows of ohlc using the function calc\_endpoints(), with the number of time periods between the end points equal to step time periods.

For example, the rolling variance at daily end points with an 11 day look-back, can be calculated using the parameters step = 1 and look\_back = 1 (Assuming the ohlc data has daily frequency.)

Similarly, the rolling variance at 25 day end points with a 75 day look-back, can be calculated using the parameters step = 25 and look\_back = 3 (because 3\*25 = 75).

The function roll\_var\_ohlc() calculates the variance from all the different intra-day and day-over-day returns (defined as the differences between *OHLC* prices), using several different variance estimation methods.

The default method is "yang\_zhang", which theoretically has the lowest standard error among unbiased estimators. The methods "close", "garman\_klass\_yz", and "yang\_zhang" do account for close-to-open price jumps, while the methods "garman\_klass" and "rogers\_satchell" do not account for close-to-open price jumps.

If scale is TRUE (the default), then the returns are divided by the differences of the time index (which scales the variance to the units of variance per second squared.) This is useful when calculating the variance from minutely bar data, because dividing returns by the number of seconds decreases the effect of overnight price jumps. If the time index is in days, then the variance is equal to the variance per day squared.

The optional argument in\_dex is the time index of the *time series* ohlc. If the time index is in seconds, then the differences of the index are equal to the number of seconds in each time period. If the time index is in days, then the differences are equal to the number of days in each time period.

The function roll\_var\_ohlc() is implemented in RcppArmadillo C++ code, so it's many times faster than the equivalent R code.

# Value

A column *vector* of variance estimates, with the number of rows equal to the number of end points.

roll\_var\_vec 67

```
in_dex=in_dex, scale=TRUE)
# Daily OHLC prices
oh_lc <- rutils::etf_env$VTI
in_dex <- c(1, diff(xts::.index(oh_lc)))</pre>
\# Rolling variance at 5 day end points, with a 20 day look-back (20=4*5)
var_rolling <- HighFreq::roll_var_ohlc(oh_lc,</pre>
                                step=5, look_back=4,
                                method="yang_zhang",
                                in_dex=in_dex, scale=TRUE)
# Same calculation in R
n_rows <- NROW(oh_lc)</pre>
lag_close = HighFreq::lag_it(oh_lc[, 4])
end_p <- drop(HighFreq::calc_endpoints(n_rows, 3)) + 1</pre>
start_p <- drop(HighFreq::calc_startpoints(end_p, 2))</pre>
n_pts <- NROW(end_p)</pre>
var_rollingr <- sapply(2:n_pts, function(it) {</pre>
  ran_ge <- start_p[it]:end_p[it]</pre>
  sub_ohlc = oh_lc[ran_ge, ]
  sub_close = lag_close[ran_ge]
  sub_index = in_dex[ran_ge]
 HighFreq::calc_var_ohlc(sub_ohlc, lag_close=sub_close, scale=TRUE, in_dex=sub_index)
}) # end sapply
var_rollingr <- c(0, var_rollingr)</pre>
all.equal(drop(var_rolling), var_rollingr)
## End(Not run)
```

roll\_var\_vec

Calculate a vector of variance estimates over a rolling look-back interval for a single-column time series or a column vector, using RcppArmadillo.

# Description

Calculate a *vector* of variance estimates over a rolling look-back interval for a single-column *time* series or a *column vector*, using RcppArmadillo.

# Usage

```
roll_var_vec(tseries, look_back = 1L)
```

# **Arguments**

tseries A single-column time series or a column vector.

look\_back The length of the look-back interval, equal to the number of *vector* elements

used for calculating a single variance estimate (the default is look\_back = 1).

### **Details**

The function roll\_var\_vec() calculates a *vector* of variance estimates over a rolling look-back interval for a single-column *time series* or a *column vector*, using RcppArmadillo C++ code.

The function roll\_var\_vec() uses an expanding look-back interval in the initial warmup period, to calculate the same number of elements as the input argument tseries.

68 roll\_vec

The function roll\_var\_vec() performs the same calculation as the function roll\_var() from package RcppRoll, but it's several times faster because it uses RcppArmadillo C++ code.

#### Value

A column vector with the same number of elements as the input argument tseries.

# **Examples**

```
## Not run:
# Create a vector of random returns
re_turns <- rnorm(1e6)
# Compare the variance estimates over 11-period look-back intervals
all.equal(drop(HighFreq::roll_var_vec(re_turns, look_back=11))[-(1:10)],
    RcppRoll::roll_var(re_turns, n=11))
# Compare the speed of RcppArmadillo with RcppRoll
library(microbenchmark)
summary(microbenchmark(
    Rcpp=HighFreq::roll_var_vec(re_turns, look_back=11),
    RcppRoll=RcppRoll::roll_var(re_turns, n=11),
    times=10))[, c(1, 4, 5)] # end microbenchmark summary
## End(Not run)</pre>
```

roll\_vec

Calculate the rolling sums over a single-column time series or a column vector using Rcpp.

# **Description**

Calculate the rolling sums over a single-column time series or a column vector using Rcpp.

# Usage

```
roll_vec(tseries, look_back)
```

### **Arguments**

tseries A single-column *time series* or a *column vector* (a single-column matrix).

look\_back The length of the look-back interval, equal to the number of elements of data

used for calculating the sum.

# **Details**

The function roll\_vec() calculates a *column vector* of rolling sums, over a *column vector* of data, using fast *Rcpp* C++ code. The function roll\_vec() is several times faster than rutils::roll\_sum() which uses vectorized R code.

# Value

A *column vector* of the same length as the argument tseries.

roll\_vecw 69

### **Examples**

```
## Not run:
# Define a single-column matrix of returns
re_turns <- zoo::coredata(na.omit(rutils::etf_env$re_turns$VTI))</pre>
# Calculate rolling sums over 11-period look-back intervals
sum_rolling <- HighFreq::roll_vec(re_turns, look_back=11)</pre>
# Compare HighFreq::roll_vec() with rutils::roll_sum()
all.equal(HighFreq::roll_vec(re_turns, look_back=11),
         rutils::roll_sum(re_turns, look_back=11),
         check.attributes=FALSE)
# Compare the speed of Rcpp with R code
library(microbenchmark)
summary(microbenchmark(
  Rcpp=HighFreq::roll_vec(re_turns, look_back=11),
  Rcode=rutils::roll_sum(re_turns, look_back=11),
  times=10))[, c(1, 4, 5)] # end microbenchmark summary
## End(Not run)
```

roll\_vecw

Calculate the rolling weighted sums over a single-column time series or a column vector using RcppArmadillo.

# **Description**

Calculate the rolling weighted sums over a single-column *time series* or a *column vector* using RcppArmadillo.

# Usage

```
roll_vecw(tseries, weights)
```

### **Arguments**

tseries A single-column *time series* or a *column vector* (a single-column matrix).

weights A column vector of weights.

# **Details**

The function roll\_vecw() calculates the rolling weighted sums of a *column vector* over its past values (a convolution with the *column vector* of weights), using RcppArmadillo. It performs a similar calculation as the standard R function stats::filter(x=series, filter=weight\_s, method="convolution", sides=but it's over 6 times faster, and it doesn't produce any NA values.

### Value

A *column vector* of the same length as the argument tseries.

70 roll\_vwap

### **Examples**

```
## Not run:
# First example
# Define a single-column matrix of returns
re_turns <- zoo::coredata(na.omit(rutils::etf_env$re_turns$VTI))</pre>
# Create simple weights
weight_s <- matrix(c(1, rep(0, 10)))
# Calculate rolling weighted sums
weight_ed <- HighFreq::roll_vecw(tseries=re_turns, weights=weight_s)</pre>
# Compare with original
all.equal(zoo::coredata(re_turns), weight_ed, check.attributes=FALSE)
# Second example
# Create exponentially decaying weights
weight_s <- matrix(exp(-0.2*1:11))
weight_s <- weight_s/sum(weight_s)</pre>
# Calculate rolling weighted sums
weight_ed <- HighFreq::roll_vecw(tseries=re_turns, weights=weight_s)</pre>
# Calculate rolling weighted sums using filter()
filter_ed <- stats::filter(x=re_turns, filter=weight_s, method="convolution", sides=1)
# Compare both methods
all.equal(filter_ed[-(1:11)], weight_ed[-(1:11)], check.attributes=FALSE)
# Compare the speed of Rcpp with R code
library(microbenchmark)
summary(microbenchmark(
  Rcpp=HighFreq::roll_vecw(tseries=re_turns, weights=weight_s),
  Rcode=stats::filter(x=re_turns, filter=weight_s, method="convolution", sides=1),
  times=10))[, c(1, 4, 5)] # end microbenchmark summary
## End(Not run)
```

roll\_vwap

Calculate the volume-weighted average price of an OHLC time series over a rolling look-back interval.

# Description

Performs the same operation as function VWAP() from package VWAP, but using vectorized functions, so it's a little faster.

# Usage

```
roll_vwap(oh_lc, x_ts = oh_lc[, 4], look_back)
```

# **Arguments**

oh\_lc An *OHLC* time series of prices in *xts* format.

x\_ts A single-column *xts* time series.

look\_back The size of the look-back interval, equal to the number of rows of data used for

calculating the average price.

roll\_wsum 71

#### **Details**

The function roll\_vwap() calculates the volume-weighted average closing price, defined as the sum of the prices multiplied by trading volumes in the look-back interval, divided by the sum of trading volumes in the interval. If the argument x\_ts is passed in explicitly, then its volumeweighted average value over time is calculated.

### Value

An xts time series with a single column and the same number of rows as the argument oh\_lc.

# **Examples**

```
# Calculate and plot rolling volume-weighted average closing prices (VWAP)
prices_rolling <- roll_vwap(oh_lc=HighFreq::SPY["2013-11"], look_back=11)</pre>
chart_Series(HighFreq::SPY["2013-11-12"], name="SPY prices")
add_TA(prices_rolling["2013-11-12"], on=1, col="red", lwd=2)
legend("top", legend=c("SPY prices", "VWAP prices"),
bg="white", lty=c(1, 1), lwd=c(2, 2),
col=c("black", "red"), bty="n")
# Calculate running returns
returns_running <- run_returns(x_ts=HighFreq::SPY)</pre>
# Calculate the rolling volume-weighted average returns
roll_vwap(oh_lc=HighFreq::SPY, x_ts=returns_running, look_back=11)
```

roll\_wsum Calculate the rolling weighted sums over a time series or a matrix using Rcpp.

### **Description**

Calculate the rolling weighted sums over a *time series* or a *matrix* using *Rcpp*.

# Usage

```
roll_wsum(tseries, endp = NULL, look_back = 1L, stub = NULL, weights = NULL)
```

# **Arguments**

tseries	A time series or a matrix.
endp	An <i>integer</i> vector of end points (the default is endp = NULL).
look_back	The length of the look-back interval, equal to the number of data points included in calculating the rolling sum (the default is look_back = 1).
stub	An <i>integer</i> value equal to the first end point for calculating the end points (the default is stub = NULL).
weights	A <i>column vector</i> of weights (the default is weights = NULL).

72 roll\_wsum

#### **Details**

The function roll\_wsum() calculates the rolling weighted sums over the columns of the data tseries.

The function roll\_wsum() calculates the rolling weighted sums as convolutions of the columns of tseries with the *column vector* of weights using the RcppArmadillo function arma::conv2(). It performs a similar calculation to the standard R function stats::filter(x=re\_turns, filter=weight\_s, method="conbut it can be many times faster, and it doesn't produce any leading NA values.

The function roll\_wsum() returns a *matrix* with the same dimensions as the input argument tseries.

The arguments weights, endp, and stub are optional.

If the argument weights is not supplied, then simple sums are calculated, not weighted sums.

If either the stub or endp arguments are supplied, then the rolling sums are calculated at the end points.

If only the argument stub is supplied, then the end points are calculated from the stub and look\_back arguments. The first end point is equal to stub and the end points are spaced look\_back periods apart.

If the arguments weights, endp, and stub are not supplied, then the sums are calculated over a number of data points equal to look\_back.

The function roll\_wsum() is also several times faster than rutils::roll\_sum() which uses vectorized R code.

Technical note: The function roll\_wsum() has arguments with default values equal to NULL, which are implemented in Rcpp code.

#### Value

A *matrix* with the same dimensions as the input argument tseries.

```
## Not run:
# First example
# Calculate historical returns
re_turns <- na.omit(rutils::etf_env$re_turns[, c("VTI", "IEF")])</pre>
# Define parameters
look_back <- 22
# Calculate rolling sums and compare with rutils::roll_sum()
c_sum <- HighFreq::roll_sum(re_turns, look_back)</pre>
r_sum <- rutils::roll_sum(re_turns, look_back)</pre>
all.equal(c_sum, coredata(r_sum), check.attributes=FALSE)
# Calculate rolling sums using R code
r_sum <- apply(zoo::coredata(re_turns), 2, cumsum)</pre>
lag_sum <- rbind(matrix(numeric(2*look_back), nc=2), r_sum[1:(NROW(r_sum) - look_back), ])</pre>
r_sum <- (r_sum - lag_sum)</pre>
all.equal(c_sum, r_sum, check.attributes=FALSE)
# Calculate rolling sums at end points
stu_b <- 21
c_sum <- HighFreq::roll_wsum(re_turns, look_back, stub=stu_b)</pre>
end_p <- (stu_b + look_back*(0:(NROW(re_turns) %/% look_back)))</pre>
end_p <- end_p[end_p < NROW(re_turns)]</pre>
r_sum <- apply(zoo::coredata(re_turns), 2, cumsum)</pre>
r_sum <- r_sum[end_p+1, ]
```

roll\_zscores 73

```
lag_sum <- rbind(numeric(2), r_sum[1:(NROW(r_sum) - 1), ])</pre>
r_sum <- (r_sum - lag_sum)</pre>
all.equal(c_sum, r_sum, check.attributes=FALSE)
# Calculate rolling sums at end points - pass in end_p
c_sum <- HighFreq::roll_wsum(re_turns, endp=end_p)</pre>
all.equal(c_sum, r_sum, check.attributes=FALSE)
# Create exponentially decaying weights
weight_s <- exp(-0.2*(1:11))
weight_s <- matrix(weight_s/sum(weight_s), nc=1)</pre>
# Calculate rolling weighted sum
c_sum <- HighFreq::roll_wsum(re_turns, weights=weight_s)</pre>
# Calculate rolling weighted sum using filter()
filter_ed <- filter(x=re_turns, filter=weight_s, method="convolution", sides=1)</pre>
all.equal(c_sum[-(1:11), ], filter_ed[-(1:11), ], check.attributes=FALSE)
# Calculate rolling weighted sums at end points
c_sum <- HighFreq::roll_wsum(re_turns, endp=end_p, weights=weight_s)</pre>
all.equal(c_sum, filter_ed[end_p+1, ], check.attributes=FALSE)
# Create simple weights equal to a 1 value plus zeros
weight_s <- matrix(c(1, rep(0, 10)), nc=1)
# Calculate rolling weighted sum
weight_ed <- HighFreq::roll_wsum(re_turns, weights=weight_s)</pre>
# Compare with original
all.equal(coredata(re_turns), weight_ed, check.attributes=FALSE)
## End(Not run)
```

roll\_zscores

Calculate a vector of z-scores of the residuals of rolling regressions at the end points of the design matrix.

### **Description**

Calculate a *vector* of z-scores of the residuals of rolling regressions at the end points of the design matrix.

## Usage

```
roll_zscores(
  response,
  design,
  startp = 0L,
  endp = 0L,
  step = 1L,
  look_back = 1L,
  stub = 0L
)
```

74 roll\_zscores

### **Arguments**

response	A single-column time series or a vector of response data.
design	A time series or a matrix of design data (predictor or explanatory data).
startp	An <i>integer</i> vector of start points (the default is $startp = 0$ ).
endp	An <i>integer</i> vector of end points (the default is endp = $\emptyset$ ).
step	The number of time periods between the end points (the default is step = 1).
look_back	The number of end points in the look-back interval (the default is look_back = 1).
stub	An <i>integer</i> value equal to the first end point for calculating the end points (the default is $stub = 0$ ).

### **Details**

The function roll\_zscores() calculates a *vector* of z-scores of the residuals of rolling regressions at the end points of the *time series* design.

The function roll\_zscores() performs a loop over the end points, and at each end point it subsets the time series design over a look-back interval equal to look\_back number of end points.

It passes the subset time series to the function calc\_lm(), which calculates the regression data.

If the arguments endp and startp are not given then it first calculates a vector of end points separated by step time periods. It calculates the end points along the rows of design using the function calc\_endpoints(), with the number of time periods between the end points equal to step time periods.

For example, the rolling variance at 25 day end points, with a 75 day look-back, can be calculated using the parameters step = 25 and look\_back = 3.

## Value

A column *vector* of the same length as the number of rows of design.

```
## Not run:
# Calculate historical returns
re_turns <- na.omit(rutils::etf_env$re_turns[, c("XLF", "VTI", "IEF")])</pre>
# Response equals XLF returns
res_ponse <- re_turns[, 1]</pre>
# Design matrix equals VTI and IEF returns
de_sign <- re_turns[, -1]</pre>
# Calculate Z-scores from rolling time series regression using RcppArmadillo
look_back <- 11
z_scores <- HighFreq::roll_zscores(response=res_ponse, design=de_sign, look_back)</pre>
\# Calculate z-scores in R from rolling multivariate regression using lm()
z_scoresr <- sapply(1:NROW(de_sign), function(ro_w) {</pre>
  if (ro_w == 1) return(0)
  start_point <- max(1, ro_w-look_back+1)</pre>
  sub_response <- res_ponse[start_point:ro_w]</pre>
  sub_design <- de_sign[start_point:ro_w, ]</pre>
  reg_model <- lm(sub_response ~ sub_design)</pre>
  resid_uals <- reg_model$residuals</pre>
  resid_uals[NROW(resid_uals)]/sd(resid_uals)
}) # end sapply
```

run\_covar 75

```
# Compare the outputs of both functions
all.equal(z_scores[-(1:look_back)], z_scoresr[-(1:look_back)],
    check.attributes=FALSE)
## End(Not run)
```

run\_covar

Calculate the rolling covariance of two streaming time series of re-

### **Description**

Calculate the rolling covariance of two streaming time series of returns.

### Usage

```
run_covar(tseries, lambda)
```

### Arguments

tseries A *time series* or a *matrix* with two columns of returns data.

lambda A *numeric* decay factor.

### **Details**

The function run\_covar() calculates the rolling covariance of two streaming *time series* of returns by recursively weighing the products of their present returns with past covariance estimates, using the decay factor  $\lambda$ :

$$\sigma_t^{12} = (1 - \lambda)r_t^1 r_t^2 + \lambda \sigma_{t-1}^{12}$$

Where  $\sigma_t^{12}$  is the covariance estimate at time t, and  $r_t^1$  and  $r_t^2$  are the streaming returns data.

The value of the decay factor  $\lambda$  should be in the range between 0 and 1. If  $\lambda$  is close to 1 then the decay is weak and past values have a greater weight, and the rolling covariance values have a stronger dependence on past values. This is equivalent to a long look-back interval. If  $\lambda$  is much less than 1 then the decay is strong and past values have a smaller weight, and the rolling covariance values have a weaker dependence on past values. This is equivalent to a short look-back interval.

The above formula slightly overestimates the covariance because it doesn't subtract the mean returns.

The above recursive formula is convenient for processing live streaming data because it doesn't require maintaining a buffer of past data. The formula is equivalent to a convolution with exponentially decaying weights, but it's faster.

The function run\_covar() returns three columns of data: the covariance and the variances of the two columns of the argument tseries. This allows calculating the rolling correlation.

The function run\_covar() performs the same calculation as the standard R function stats::filter(x=series,filter=weight\_s,method="convolution",sides=1), but it's several times faster.

## Value

A *matrix* with three columns of data: the covariance and the variances of the two columns of the argument tseries.

76 run\_max

### **Examples**

```
## Not run:
# Calculate historical returns
re_turns <- zoo::coredata(na.omit(rutils::etf_env$re_turns[, c("IEF", "VTI")]))
# Calculate the rolling covariance
lamb_da <- 0.9
covars <- HighFreq::run_covar(re_turns, lambda=lamb_da)
# Calculate rolling covariance using R code
filter_ed <- (1-lamb_da)*filter(re_turns[, 1]*re_turns[, 2], filter=lamb_da, init=as.numeric(re_turns[1, 1]*re_all.equal(covars[, 1], unclass(filter_ed), check.attributes=FALSE)
# Calculate the rolling correlation
correl <- covars[, 1]/sqrt(covars[, 2]*covars[, 3])
## End(Not run)</pre>
```

run\_max

Calculate the rolling maximum of streaming time series data.

### **Description**

Calculate the rolling maximum of streaming time series data.

## Usage

```
run_max(tseries, lambda)
```

### **Arguments**

tseries A time series or a matrix.

lambda A numeric decay factor.

### **Details**

The function run\_max() calculates the rolling maximum of streaming *time series* data by recursively weighing present and past values using the decay factor  $\lambda$ .

It first calculates the rolling mean of streaming data:

$$\mu_t = (1 - \lambda)p_t + \lambda\mu_{t-1}$$

Where  $\mu_t$  is the mean value at time t, and  $p_t$  is the streaming data.

It then calculates the rolling maximums of streaming data,  $p_t^{max}$ :

$$p_t^{max} = max(p_t, p_{t-1}^{max}) + (1 - \lambda)(\mu_{t-1} - p_{t-1}^{max})$$

The second term pulls the maximum value down to the mean value, allowing it to gradually "forget" the maximum value from the more distant past.

The value of the decay factor  $\lambda$  should be in the range between 0 and 1. If  $\lambda$  is close to 1 then the decay is weak and past values have a greater weight, and the rolling maximum values have a stronger dependence on past values. This is equivalent to a long look-back interval. If  $\lambda$  is much less than 1 then the decay is strong and past values have a smaller weight, and the rolling maximum values have a weaker dependence on past values. This is equivalent to a short look-back interval.

run\_mean 77

The above recursive formula is convenient for processing live streaming data because it doesn't require maintaining a buffer of past data.

The function run\_max() returns a *matrix* with the same dimensions as the input argument tseries.

### Value

A matrix with the same dimensions as the input argument tseries.

### **Examples**

```
## Not run:
# Calculate historical prices
price_s <- zoo::coredata(quantmod::Cl(rutils::etf_env$VTI))
# Calculate the rolling maximums
lamb_da <- 0.9
maxs <- HighFreq::run_max(price_s, lambda=lamb_da)
# Plot dygraph of VTI prices and rolling maximums
da_ta <- cbind(quantmod::Cl(rutils::etf_env$VTI), maxs)
colnames(da_ta) <- c("prices", "max")
col_names <- colnames(da_ta)
dygraphs::dygraph(da_ta, main="VTI Prices and Rolling Maximums") %>%
    dySeries(name=col_names[1], label=col_names[1], strokeWidth=2, col="blue") %>%
    dySeries(name=col_names[2], label=col_names[2], strokeWidth=2, col="red")
## End(Not run)
```

run\_mean

Calculate the rolling mean of streaming time series data.

### **Description**

Calculate the rolling mean of streaming *time series* data.

# Usage

```
run_mean(tseries, lambda)
```

# **Arguments**

tseries A time series or a matrix.

lambda A numeric decay factor.

# **Details**

The function run\_mean() calculates the rolling mean of streaming *time series* data by recursively weighing present and past values using the decay factor  $\lambda$ :

$$\mu_t = (1 - \lambda)p_t + \lambda\mu_{t-1}$$

Where  $\mu_t$  is the mean value at time t, and  $p_t$  is the streaming data.

The value of the decay factor  $\lambda$  should be in the range between 0 and 1. If  $\lambda$  is close to 1 then the decay is weak and past values have a greater weight, and the rolling mean values have a stronger

78 run\_min

dependence on past values. This is equivalent to a long look-back interval. If  $\lambda$  is much less than 1 then the decay is strong and past values have a smaller weight, and the rolling mean values have a weaker dependence on past values. This is equivalent to a short look-back interval.

The above recursive formula is convenient for processing live streaming data because it doesn't require maintaining a buffer of past data. The formula is equivalent to a convolution with exponentially decaying weights, but it's faster.

The function run\_mean() performs the same calculation as the standard R function stats::filter(x=series,filter=weight\_s,method="convolution",sides=1), but it's several times faster.

The function run\_mean() returns a *matrix* with the same dimensions as the input argument tseries.

### Value

A *matrix* with the same dimensions as the input argument tseries.

# **Examples**

```
## Not run:
# Calculate historical prices
price_s <- zoo::coredata(quantmod::Cl(rutils::etf_env$VTI))</pre>
# Calculate the rolling means
lamb da <-0.9
means <- HighFreq::run_mean(price_s, lambda=lamb_da)</pre>
# Calculate rolling means using R code
filter\_ed <- (1-lamb\_da) * filter(price\_s, filter=lamb\_da, init=as.numeric(price\_s[1, 1]) / (1-lamb\_da), method=lamb\_da) * filter\_ed <- (1-lamb\_da) * filter(price\_s, filter=lamb\_da, init=as.numeric(price\_s[1, 1]) / (1-lamb\_da), method=lamb\_da) * filter\_ed <- (1-lamb\_da) * filter\_ed <- (1-
all.equal(means, unclass(filter_ed), check.attributes=FALSE)
# Compare the speed of RcppArmadillo with R code
library(microbenchmark)
summary(microbenchmark(
       Rcpp=HighFreq::run_mean(price_s, lambda=lamb_da),
     Rcode=filter(price\_s,\ filter=lamb\_da,\ init=as.numeric(price\_s[1,\ 1])/(1-lamb\_da),\ method="recursive"),
        times=10))[, c(1, 4, 5)] # end microbenchmark summary
## End(Not run)
```

run\_min

Calculate the rolling minimum of streaming time series data.

# **Description**

Calculate the rolling minimum of streaming time series data.

# Usage

```
run_min(tseries, lambda)
```

### **Arguments**

tseries A time series or a matrix.

lambda A numeric decay factor.

run\_min 79

#### **Details**

The function run\_min() calculates the rolling minimum of streaming *time series* data by recursively weighing present and past values using the decay factor  $\lambda$ .

It first calculates the rolling mean of streaming data:

$$\mu_t = (1 - \lambda)p_t + \lambda\mu_{t-1}$$

Where  $\mu_t$  is the mean value at time t, and  $p_t$  is the streaming data.

It then calculates the rolling minimums of streaming data,  $p_t^{min}$ :

$$p_t^{min} = min(p_t, p_{t-1}^{min}) + (1 - \lambda)(\mu_{t-1} - p_{t-1}^{min})$$

The second term pulls the minimum value up to the mean value, allowing it to gradually "forget" the minimum value from the more distant past.

The value of the decay factor  $\lambda$  should be in the range between 0 and 1. If  $\lambda$  is close to 1 then the decay is weak and past values have a greater weight, and the rolling minimum values have a stronger dependence on past values. This is equivalent to a long look-back interval. If  $\lambda$  is much less than 1 then the decay is strong and past values have a smaller weight, and the rolling minimum values have a weaker dependence on past values. This is equivalent to a short look-back interval.

The above recursive formula is convenient for processing live streaming data because it doesn't require maintaining a buffer of past data.

The function run\_min() returns a *matrix* with the same dimensions as the input argument tseries.

## Value

A *matrix* with the same dimensions as the input argument tseries.

```
## Not run:
# Calculate historical prices
price_s <- zoo::coredata(quantmod::Cl(rutils::etf_env$VTI))
# Calculate the rolling minimums
lamb_da <- 0.9
mins <- HighFreq::run_min(price_s, lambda=lamb_da)
# Plot dygraph of VTI prices and rolling minimums
da_ta <- cbind(quantmod::Cl(rutils::etf_env$VTI), mins)
colnames(da_ta) <- c("prices", "min")
col_names <- colnames(da_ta)
dygraphs::dygraph(da_ta, main="VTI Prices and Rolling Minimums") %>%
    dySeries(name=col_names[1], label=col_names[1], strokeWidth=2, col="blue") %>%
    dySeries(name=col_names[2], label=col_names[2], strokeWidth=2, col="red")
## End(Not run)
```

80 run\_returns

run_returns	Calculate single period percentage returns from either TAQ or OHLC prices.

### **Description**

Calculate single period percentage returns from either TAQ or OHLC prices.

### Usage

```
run_returns(x_ts, lagg = 1, col_umn = 4, scal_e = TRUE)
```

# **Arguments**

x_ts	An xts time series of either TAQ or OHLC data.
lagg	An integer equal to the number of time periods of lag. (default is 1)
col_umn	The column number to extract from the <i>OHLC</i> data. (default is 4, or the <i>Close</i> prices column)
scal_e	<i>Boolean</i> argument: should the returns be divided by the number of seconds in each period? (default is TRUE)

### **Details**

The function run\_returns() calculates the percentage returns for either *TAQ* or *OHLC* data, defined as the difference of log prices. Multi-period returns can be calculated by setting the lag parameter to values greater than 1 (the default).

If scal\_e is TRUE (the default), then the returns are divided by the differences of the time index (which scales the returns to units of returns per second.)

The time index of the x\_ts time series is assumed to be in *POSIXct* format, so that its internal value is equal to the number of seconds that have elapsed since the *epoch*.

If scal\_e is TRUE (the default), then the returns are expressed in the scale of the time index of the x\_ts time series. For example, if the time index is in seconds, then the returns are given in units of returns per second. If the time index is in days, then the returns are equal to the returns per day.

The function run\_returns() identifies the x\_ts time series as *TAQ* data when it has six columns, otherwise assumes it's *OHLC* data. By default, for *OHLC* data, it differences the *Close* prices, but can also difference other prices depending on the value of col\_umn.

## Value

A single-column xts time series of returns.

```
# Calculate secondly returns from TAQ data
re_turns <- HighFreq::run_returns(x_ts=HighFreq::SPY_TAQ)
# Calculate close to close returns
re_turns <- HighFreq::run_returns(x_ts=HighFreq::SPY)
# Calculate open to open returns
re_turns <- HighFreq::run_returns(x_ts=HighFreq::SPY, col_umn=1)</pre>
```

run\_sharpe 81

run_sharpe	Calculate time series of point Sharpe-like statistics for each row of a OHLC time series.
------------	---

# **Description**

Calculate time series of point Sharpe-like statistics for each row of a *OHLC* time series.

# Usage

```
run_sharpe(oh_lc, calc_method = "close")
```

# **Arguments**

oh\_lc An *OHLC* time series of prices in *xts* format.

calc\_method A character string representing method for estimating the Sharpe-like exponent.

### **Details**

The function run\_sharpe() calculates Sharpe-like statistics for each row of a *OHLC* time series. The Sharpe-like statistic is defined as the ratio of the difference between *Close* minus *Open* prices divided by the difference between *High* minus *Low* prices. This statistic may also be interpreted as something like a *Hurst exponent* for a single row of data. The motivation for the Sharpe-like statistic is the notion that if prices are trending in the same direction inside a given time bar of data, then this statistic is close to either 1 or -1.

### Value

An xts time series with the same number of rows as the argument oh\_lc.

# **Examples**

```
# Calculate time series of running Sharpe ratios for SPY
sharpe_running <- run_sharpe(HighFreq::SPY)</pre>
```

run_skew	Calculate time series of point skew estimates from a OHLC time series,
	assuming zero drift.

### **Description**

Calculate time series of point skew estimates from a OHLC time series, assuming zero drift.

# Usage

```
run_skew(oh_lc, calc_method = "rogers_satchell")
```

# **Arguments**

oh\_lc An *OHLC* time series of prices in *xts* format.

calc\_method A *character* string representing method for estimating skew.

82 run\_var

#### **Details**

The function run\_skew() calculates a time series of skew estimates from *OHLC* prices, one for each row of *OHLC* data. The skew estimates are expressed in the time scale of the index of the *OHLC* time series. For example, if the time index is in seconds, then the skew is given in units of skew per second. If the time index is in days, then the skew is equal to the skew per day.

Currently only the "close" skew estimation method is correct (assuming zero drift), while the "rogers\_satchell" method produces a skew-like indicator, proportional to the skew. The default method is "rogers\_satchell".

### Value

A time series of point skew estimates.

# **Examples**

```
# Calculate time series of skew estimates for SPY
sk_ew <- HighFreq::run_skew(HighFreq::SPY)</pre>
```

run\_var

Calculate the rolling variance of streaming time series of returns.

## **Description**

Calculate the rolling variance of streaming time series of returns.

# Usage

```
run_var(tseries, lambda)
```

# **Arguments**

tseries A time series or a matrix of returns.

lambda A numeric decay factor.

# **Details**

The function run\_var() calculates the rolling variance of a streaming *time series* of returns by recursively weighing the squared present returns with past variance estimates, using the decay factor  $\lambda$ :

$$\sigma_t^2 = (1 - \lambda)r_t^2 + \lambda \sigma_{t-1}^2$$

Where  $\sigma_t^2$  is the variance estimate at time t, and  $r_t$  are the streaming returns data.

The value of the decay factor  $\lambda$  should be in the range between 0 and 1. If  $\lambda$  is close to 1 then the decay is weak and past values have a greater weight, and the rolling variance values have a stronger dependence on past values. This is equivalent to a long look-back interval. If  $\lambda$  is much less than 1 then the decay is strong and past values have a smaller weight, and the rolling variance values have a weaker dependence on past values. This is equivalent to a short look-back interval.

The above formula slightly overestimates the variance because it doesn't subtract the mean returns.

The above recursive formula is convenient for processing live streaming data because it doesn't require maintaining a buffer of past data. The formula is equivalent to a convolution with exponentially decaying weights, but it's faster.

run\_variance 83

The function run\_var() performs the same calculation as the standard R function stats::filter(x=series,filter=weight\_s,method="convolution",sides=1), but it's several times faster.

The function run\_var() returns a *matrix* with the same dimensions as the input argument tseries.

### Value

A matrix with the same dimensions as the input argument tseries.

### **Examples**

```
## Not run:
# Calculate historical returns
re_turns <- zoo::coredata(na.omit(rutils::etf_env$re_turns$VTI))</pre>
# Calculate the rolling variance
lamb_da <- 0.9
vars <- HighFreq::run_var(re_turns, lambda=lamb_da)</pre>
# Calculate rolling variance using R code
filter_ed <- (1-lamb_da)*filter(re_turns^2, filter=lamb_da, init=as.numeric(re_turns[1, 1])^2/(1-lamb_da), more filter_ed <- (1-lamb_da)*filter(re_turns^2, filter=lamb_da, init=as.numeric(re_turns[1, 1])^2/(1-lamb_da)
all.equal(vars, unclass(filter_ed), check.attributes=FALSE)
# Compare the speed of RcppArmadillo with R code
library(microbenchmark)
summary(microbenchmark(
  Rcpp=HighFreq::run_var(re_turns, lambda=lamb_da),
 Rcode=filter(re_turns^2, filter=lamb_da, init=as.numeric(re_turns[1, 1])^2/(1-lamb_da), method="recursive"
  times=10))[, c(1, 4, 5)] # end microbenchmark summary
## End(Not run)
```

run\_variance

Calculate a time series of point estimates of variance for an OHLC time series, using different range estimators for variance.

# **Description**

Calculates the point variance estimates from individual rows of *OHLC* prices (rows of data), using the squared differences of *OHLC* prices at each point in time, without averaging them over time.

# Usage

```
run_variance(oh_lc, calc_method = "yang_zhang", scal_e = TRUE)
```

### **Arguments**

oh\_lc

An OHLC time series of prices in xts format.

calc\_method

A *character* string representing the method for estimating variance. The methods include:

- "close" close to close,
- "garman\_klass" Garman-Klass,
- "garman\_klass\_yz" Garman-Klass with account for close-to-open price jumps,
- "rogers\_satchell" Rogers-Satchell,

84 run\_variance

```
    "yang_zhang" Yang-Zhang,
(default is "yang_zhang")
```

scal\_e

*Boolean* argument: should the returns be divided by the number of seconds in each period? (default is TRUE)

### **Details**

The function run\_variance() calculates a time series of point variance estimates of percentage returns, from *OHLC* prices, without averaging them over time. For example, the method "close" simply calculates the squares of the differences of the log *Close* prices.

The other methods calculate the squares of other possible differences of the log *OHLC* prices. This way the point variance estimates only depend on the price differences within individual rows of data (and possibly from the neighboring rows.) All the methods are implemented assuming zero drift, since the calculations are performed only for a single row of data, at a single point in time.

The user can choose from several different variance estimation methods. The methods "close", "garman\_klass\_yz", and "yang\_zhang" do account for close-to-open price jumps, while the methods "garman\_klass" and "rogers\_satchell" do not account for close-to-open price jumps. The default method is "yang\_zhang", which theoretically has the lowest standard error among unbiased estimators.

The point variance estimates can be passed into function roll\_vwap() to perform averaging, to calculate rolling variance estimates. This is appropriate only for the methods "garman\_klass" and "rogers\_satchell", since they don't require subtracting the rolling mean from the point variance estimates.

The point variance estimates can also be considered to be technical indicators, and can be used as inputs into trading models.

If scal\_e is TRUE (the default), then the variance is divided by the squared differences of the time index (which scales the variance to units of variance per second squared.) This is useful for example, when calculating intra-day variance from minutely bar data, because dividing returns by the number of seconds decreases the effect of overnight price jumps.

If scal\_e is TRUE (the default), then the variance is expressed in the scale of the time index of the *OHLC* time series. For example, if the time index is in seconds, then the variance is given in units of variance per second squared. If the time index is in days, then the variance is equal to the variance per day squared.

The time index of the oh\_lc time series is assumed to be in *POSIXct* format, so that its internal value is equal to the number of seconds that have elapsed since the *epoch*.

The function run\_variance() performs similar calculations to the function volatility() from package TTR, but it assumes zero drift, and doesn't calculate a running sum using runSum(). It's also a little faster because it performs less data validation.

# Value

An *xts* time series with a single column and the same number of rows as the argument oh\_lc.

```
# Create minutely OHLC time series of random prices
oh_lc <- HighFreq::random_ohlc()
# Calculate variance estimates for oh_lc
var_running <- HighFreq::run_variance(oh_lc)
# Calculate variance estimates for SPY</pre>
```

run\_zscores 85

```
var_running <- HighFreq::run_variance(HighFreq::SPY, calc_method="yang_zhang")
# Calculate SPY variance without overnight jumps
var_running <- HighFreq::run_variance(HighFreq::SPY, calc_method="rogers_satchell")</pre>
```

run\_zscores

Calculate the z-scores of rolling regressions of streaming time series of returns.

## **Description**

Calculate the z-scores of rolling regressions of streaming time series of returns.

### Usage

run\_zscores(response, design, lambda)

## **Arguments**

response A single-column *time series* or a *vector* of response data.

design A time series or a matrix of design data (predictor or explanatory data).

lambda A *numeric* decay factor.

### **Details**

The function run\_zscores() calculates the vectors of *betas*  $\beta_t$  and the residuals  $\epsilon_t$  of rolling regressions by recursively weighing the current estimates with past estimates, using the decay factor  $\lambda$ :

$$\beta_t = (1 - \lambda) \frac{\sigma_t^{cov}}{\sigma_t^2} + \lambda \beta_{t-1}$$

$$\epsilon_t = (1 - \lambda)(r_t^r - \beta_t r_t^d) + \lambda \epsilon_{t-1}$$

Where  $\sigma_t^{cov}$  is the vector of covariances between the response and design returns, at time t;  $\sigma_t^2$  is the vector of design variances, and  $r_t^r$  and  $r_t^d$  are the streaming returns of the response and design data.

The matrices  $\sigma^2$ ,  $\sigma^{cov}$ ,  $\beta$  have the same dimensions as the input argument design.

The above formula is approximate because it doesn't subtract the mean returns.

The z-score  $z_t$  is equal to the residual  $\epsilon_t$  divided by its volatility  $\sigma_t^{\epsilon}$ :

$$z_t = \frac{\epsilon_t}{\sigma_t^{\epsilon}}$$

The value of the decay factor  $\lambda$  should be in the range between 0 and 1. If  $\lambda$  is close to 1 then the decay is weak and past values have a greater weight, and the rolling z-score values have a stronger dependence on past values. This is equivalent to a long look-back interval. If  $\lambda$  is much less than 1 then the decay is strong and past values have a smaller weight, and the rolling z-score values have a weaker dependence on past values. This is equivalent to a short look-back interval.

The above recursive formula is convenient for processing live streaming data because it doesn't require maintaining a buffer of past data. The formula is equivalent to a convolution with exponentially decaying weights, but it's faster.

86 save\_rets

The function run\_zscores() returns four columns of data: the z-score and the variances of the two columns of the argument tseries. This allows calculating the rolling correlation.

The function run\_zscores() performs the same calculation as the standard R function stats::filter(x=series,filter=weight\_s,method="convolution",sides=1), but it's several times faster.

### Value

A matrix with the z-scores, betas, and variances of the design data.

### **Examples**

```
## Not run:
# Calculate historical returns
re_turns <- na.omit(rutils::etf_env$re_turns[, c("XLF", "VTI", "IEF")])</pre>
# Response equals XLF returns
res_ponse <- re_turns[, 1]</pre>
# Design matrix equals VTI and IEF returns
de_sign <- re_turns[, -1]</pre>
# Calculate the running z-scores
lamb_da <- 0.9
zscores <- HighFreq::run_zscores(response=res_ponse, design=de_sign, lambda=lamb_da)</pre>
# Plot the running z-scores
da_ta <- cbind(cumsum(res_ponse), zscores[, 1])</pre>
colnames(da_ta) <- c("XLF", "zscores")</pre>
col_names <- colnames(da_ta)</pre>
dygraphs::dygraph(da_ta, main="Z-Scores of XLF Versus VTI and IEF") %>%
  dyAxis("y", label=col_names[1], independentTicks=TRUE) %>%
  dyAxis("y2", label=col_names[2], independentTicks=TRUE) %>%
 dySeries(name=col_names[1], axis="y", label=col_names[1], strokeWidth=1, col="blue") %>%
  dySeries(name=col_names[2], axis="y2", label=col_names[2], strokeWidth=1, col="red")
## End(Not run)
```

save\_rets

Load, scrub, aggregate, and rbind multiple days of TAQ data for a single symbol. Calculate returns and save them to a single '\*.RData' file.

# **Description**

Load, scrub, aggregate, and rbind multiple days of *TAQ* data for a single symbol. Calculate returns and save them to a single '\*.RData' file.

### Usage

```
save_rets(
  sym_bol,
  data_dir = "E:/mktdata/sec/",
  output_dir = "E:/output/data/",
  look_back = 51,
  vol_mult = 2,
```

save\_rets\_ohlc 87

```
period = "minutes",
  tzone = "America/New_York"
)
```

## **Details**

The function save\_rets loads multiple days of TAQ data, then scrubs, aggregates, and rbinds them into a OHLC time series. It then calculates returns using function run\_returns(), and stores them in a variable named 'symbol.rets', and saves them to a file called 'symbol.rets.RData'. The TAQ data files are assumed to be stored in separate directories for each 'symbol'. Each 'symbol' has its own directory (named 'symbol') in the 'data\_dir' directory. Each 'symbol' directory contains multiple daily '\*.RData' files, each file containing one day of TAQ data.

### Value

A time series of returns and volume in xts format.

### **Examples**

```
## Not run:
save_rets("SPY")
## End(Not run)
```

save\_rets\_ohlc

Load OHLC time series data for a single symbol, calculate its returns, and save them to a single '\*.RData' file, without aggregation.

# **Description**

Load *OHLC* time series data for a single symbol, calculate its returns, and save them to a single '\*.RData' file, without aggregation.

# Usage

```
save_rets_ohlc(
   sym_bol,
   data_dir = "E:/output/data/",
   output_dir = "E:/output/data/")
```

## **Details**

The function save\_rets\_ohlc() loads *OHLC* time series data from a single file. It then calculates returns using function run\_returns(), and stores them in a variable named 'symbol.rets', and saves them to a file called 'symbol.rets.RData'.

# Value

A time series of returns and volume in xts format.

88 save\_scrub\_agg

### **Examples**

```
## Not run:
save_rets_ohlc("SPY")
## End(Not run)
```

save\_scrub\_agg

Load, scrub, aggregate, and rbind multiple days of TAQ data for a single symbol, and save the OHLC time series to a single '\*.RData' file.

# Description

Load, scrub, aggregate, and rbind multiple days of *TAQ* data for a single symbol, and save the *OHLC* time series to a single '\*.RData' file.

# Usage

```
save_scrub_agg(
  sym_bol,
  data_dir = "E:/mktdata/sec/",
  output_dir = "E:/output/data/",
  look_back = 51,
  vol_mult = 2,
  period = "minutes",
  tzone = "America/New_York"
)
```

# **Arguments**

sym\_bol A *character* string representing symbol or ticker.

data\_dir A *character* string representing directory containing input '\*.RData' files.

output\_dir A character string representing directory containing output '\*.RData' files.

## **Details**

The function save\_scrub\_agg() loads multiple days of TAQ data, then scrubs, aggregates, and rbinds them into a OHLC time series, and finally saves it to a single '\*.RData' file. The OHLC time series is stored in a variable named 'symbol', and then it's saved to a file named 'symbol.RData' in the 'output\_dir' directory. The TAQ data files are assumed to be stored in separate directories for each 'symbol'. Each 'symbol' has its own directory (named 'symbol') in the 'data\_dir' directory. Each 'symbol' directory contains multiple daily '\*.RData' files, each file containing one day of TAQ data.

# Value

An *OHLC* time series in *xts* format.

save\_taq 89

### **Examples**

```
## Not run:
# set data directories
data_dir <- "C:/Develop/data/hfreq/src/"
output_dir <- "C:/Develop/data/hfreq/scrub/"
sym_bol <- "SPY"
# Aggregate SPY TAQ data to 15-min OHLC bar data, and save the data to a file
save_scrub_agg(sym_bol=sym_bol, data_dir=data_dir, output_dir=output_dir, period="15 min")
## End(Not run)</pre>
```

save\_taq

Load and scrub multiple days of TAQ data for a single symbol, and save it to multiple '\*.RData' files.

# **Description**

Load and scrub multiple days of TAQ data for a single symbol, and save it to multiple '\*.RData' files.

# Usage

```
save_taq(
  sym_bol,
  data_dir = "E:/mktdata/sec/",
  output_dir = "E:/output/data/",
  look_back = 51,
  vol_mult = 2,
  tzone = "America/New_York"
)
```

### **Details**

The function save\_taq() loads multiple days of TAQ data, scrubs it, and saves the scrubbed TAQ data to individual '\*.RData' files. It uses the same file names for output as the input file names. The TAQ data files are assumed to be stored in separate directories for each 'symbol'. Each 'symbol' has its own directory (named 'symbol') in the 'data\_dir' directory. Each 'symbol' directory contains multiple daily '\*.RData' files, each file containing one day of TAQ data.

# Value

a TAQ time series in xts format.

```
## Not run:
save_taq("SPY")
## End(Not run)
```

90 scrub\_agg

scrub\_agg

Scrub a single day of TAQ data, aggregate it, and convert to OHLC format.

### **Description**

Scrub a single day of TAQ data, aggregate it, and convert to OHLC format.

# Usage

```
scrub_agg(
  ta_q,
  look_back = 51,
  vol_mult = 2,
  period = "minutes",
  tzone = "America/New_York"
)
```

# **Arguments**

period

The aggregation period.

### **Details**

The function scrub\_agg() performs:

- index timezone conversion,
- data subset to trading hours,
- removal of duplicate time stamps,
- scrubbing of quotes with suspect bid-offer spreads,
- scrubbing of quotes with suspect price jumps,
- cbinding of mid prices with volume data,
- aggregation to OHLC using function to.period() from package xts,

Valid 'period' character strings include: "minutes", "3 min", "5 min", "10 min", "15 min", "30 min", and "hours". The time index of the output time series is rounded up to the next integer multiple of 'period'.

# Value

A OHLC time series in xts format.

```
# Create random TAQ prices
ta_q <- HighFreq::random_taq()
# Aggregate to ten minutes OHLC data
oh_lc <- HighFreq::scrub_agg(ta_q, period="10 min")
chart_Series(oh_lc, name="random prices")
# scrub and aggregate a single day of SPY TAQ data to OHLC
oh_lc <- HighFreq::scrub_agg(ta_q=HighFreq::SPY_TAQ)
chart_Series(oh_lc, name=sym_bol)</pre>
```

scrub\_taq 91

scrub\_taq

Scrub a single day of TAQ data in xts format, without aggregation.

## **Description**

Scrub a single day of TAQ data in xts format, without aggregation.

### Usage

```
scrub_taq(ta_q, look_back = 51, vol_mult = 2, tzone = "America/New_York")
```

### **Arguments**

ta\_q TAQ A time series in xts format.

tzone The timezone to convert.

### **Details**

The function scrub\_taq() performs the same scrubbing operations as scrub\_agg, except it doesn't aggregate, and returns the *TAQ* data in *xts* format.

### Value

A TAQ time series in xts format.

# **Examples**

```
ta_q <- HighFreq::scrub_taq(ta_q=HighFreq::SPY_TAQ, look_back=11, vol_mult=1)
# Create random TAQ prices and scrub them
ta_q <- HighFreq::random_taq()
ta_q <- HighFreq::scrub_taq(ta_q=ta_q)
ta_q <- HighFreq::scrub_taq(ta_q=ta_q, look_back=11, vol_mult=1)</pre>
```

season\_ality

Perform seasonality aggregations over a single-column xts time series.

# Description

Perform seasonality aggregations over a single-column xts time series.

# Usage

```
season\_ality(x\_ts, in\_dex = format(zoo::index(x\_ts), "%H:%M"))
```

# **Arguments**

x\_ts A single-column xts time series.

in\_dex A vector of *character* strings representing points in time, of the same length as

the argument x\_ts.

92 sim\_arima

#### **Details**

The function season\_ality() calculates the mean of values observed at the same points in time specified by the argument in\_dex. An example of a daily seasonality aggregation is the average price of a stock between 9:30AM and 10:00AM every day, over many days. The argument in\_dex is passed into function tapply(), and must be the same length as the argument x\_ts.

### Value

An xts time series with mean aggregations over the seasonality interval.

### **Examples**

```
# Calculate running variance of each minutely OHLC bar of data
x_ts <- run_variance(HighFreq::SPY)
# Remove overnight variance spikes at "09:31"
in_dex <- format(index(x_ts), "%H:%M")
x_ts <- x_ts[!in_dex=="09:31", ]
# Calculate daily seasonality of variance
var_seasonal <- season_ality(x_ts=x_ts)
chart_Series(x=var_seasonal, name=paste(colnames(var_seasonal),
    "daily seasonality of variance"))</pre>
```

sim\_arima

Recursively filter a vector of innovations through a vector of ARIMA coefficients.

# Description

Recursively filter a vector of innovations through a vector of ARIMA coefficients.

# Usage

```
sim_arima(innov, coeff)
```

# **Arguments**

innov A *vector* of innovations (random numbers).

coeff A vector of ARIMA coefficients.

### **Details**

The function sim\_arima() recursively filters a *vector* of innovations through a *vector* of *ARIMA* coefficients, using RcppArmadillo C++ code. It performs the same calculation as the standard R function filter(x=innov, filter=co\_eff, method="recursive"), but it's over 6 times faster.

# Value

A column *vector* of the same length as the argument innov.

sim\_garch 93

### **Examples**

```
## Not run:
# Calculate vector of prices
price_s <- drop(zoo::coredata(quantmod::Cl(rutils::etf_env$VTI)))
# Create ARIMA coefficients
co_eff <- c(-0.8, 0.2)
# Calculate recursive filter using filter()
filter_ed <- filter(price_s, filter=co_eff, method="recursive")
# Calculate recursive filter using RcppArmadillo
ari_ma <- HighFreq::sim_arima(price_s, rev(co_eff))
# Compare the two methods
all.equal(as.numeric(ari_ma), as.numeric(filter_ed))
## End(Not run)</pre>
```

sim\_garch

Simulate a GARCH process using Rcpp.

# **Description**

Simulate a *GARCH* process using *Rcpp*.

### Usage

```
sim_garch(omega, alpha, beta, innov)
```

# Arguments

omega	Parameter proportional to the long-term average level of variance.
alpha	The weight associated with recent realized variance updates.
beta	The weight associated with the past variance estimates.
innov	A <i>vector</i> of innovations (random numbers).

### **Details**

The function sim\_garch() simulates a *GARCH* process using fast *Rcpp* C++ code.

# Value

A *matrix* with two columns: the simulated returns and variance, and with the same number of rows as the length of the argument innov.

```
## Not run:
# Define the GARCH model parameters
ome_ga <- 0.01
al_pha <- 0.5
be_ta <- 0.2
# Simulate the GARCH process using Rcpp
garch_rcpp <- sim_garch(omega=ome_ga, alpha=al_pha, beta=be_ta, innov=rnorm(10000))</pre>
```

94 sim\_ou

```
## End(Not run)
```

sim\_ou

Simulate an Ornstein-Uhlenbeck process using Rcpp.

# **Description**

Simulate an Ornstein-Uhlenbeck process using Rcpp.

# Usage

```
sim_ou(eq_price, volat, theta, innov)
```

# **Arguments**

eq\_price The equilibrium price.
volat The volatility of returns.

theta The strength of mean reversion.

innov A *vector* of innovations (random numbers).

## **Details**

The function sim\_ou() simulates an *Ornstein-Uhlenbeck* process using fast *Rcpp* C++ code. It returns a column *vector* representing the *time series* of log prices. The function sim\_ou() simulates the percentage returns as equal to the difference between the equilibrium price eq\_price minus the latest price, times the mean reversion parameter theta, plus a random innovation. The log prices are calculated as the sum of returns (not compounded), so they can become negative.

# Value

A column *vector* representing the *time series* of log prices, with the same length as the argument innov.

```
## Not run:
# Define the Ornstein-Uhlenbeck model parameters
eq_price <- 5.0
vol_at <- 0.01
the_ta <- 0.01
# Simulate Ornstein-Uhlenbeck process using Rcpp
price_s <- HighFreq::sim_ou(eq_price=eq_price, volat=vol_at, theta=the_ta, innov=rnorm(1000))
## End(Not run)</pre>
```

sim\_schwartz 95

### **Description**

Simulate a Schwartz process using Rcpp.

# Usage

```
sim_schwartz(eq_price, volat, theta, innov)
```

# **Arguments**

eq\_price The equilibrium price.

volat The volatility of returns.

theta The strength of mean reversion.

innov A *vector* of innovations (random numbers).

### **Details**

The function sim\_schwartz() simulates a *Schwartz* process using fast *Rcpp* C++ code. It returns a column *vector* representing the *time series* of prices. The function sim\_schwartz() simulates the percentage returns as equal to the difference between the equilibrium price eq\_price minus the latest price, times the mean reversion parameter theta, plus a random innovation. The prices are calculated as the exponentially compounded returns, so they are never negative. The log prices can be obtained by taking the logarithm of the prices.

### Value

A column vector representing the time series of prices, with the same length as the argument innov.

```
## Not run:
# Define the Schwartz model parameters
eq_price <- 5.0
vol_at <- 0.01
the_ta <- 0.01
# Simulate Schwartz process using Rcpp
price_s <- HighFreq::sim_schwartz(eq_price=eq_price, volat=vol_at, theta=the_ta, innov=rnorm(1000))
## End(Not run)</pre>
```

96 which\_extreme

which_extreme	Calculate a Boolean vector that identifies extreme tail values in a single-column xts time series or vector, over a rolling look-back interval.
---------------	---

# **Description**

Calculate a *Boolean* vector that identifies extreme tail values in a single-column *xts* time series or vector, over a rolling look-back interval.

# Usage

```
which_extreme(x_ts, look_back = 51, vol_mult = 2)
```

## **Arguments**

x\_ts A single-column xts time series, or a numeric or Boolean vector.

look\_back The number of data points in rolling look-back interval for estimating rolling

quantile.

vol\_mult The quantile multiplier.

### **Details**

The function which\_extreme() calculates a *Boolean* vector, with TRUE for values that belong to the extreme tails of the distribution of values.

The function which\_extreme() applies a version of the Hampel median filter to identify extreme values, but instead of using the median absolute deviation (MAD), it uses the 0.9 quantile values calculated over a rolling look-back interval.

Extreme values are defined as those that exceed the product of the multiplier times the rolling quantile. Extreme values belong to the fat tails of the recent (trailing) distribution of values, so they are present only when the trailing distribution of values has fat tails. If the trailing distribution of values is closer to normal (without fat tails), then there are no extreme values.

The quantile multiplier vol\_mult controls the threshold at which values are identified as extreme. Smaller quantile multiplier values will cause more values to be identified as extreme.

## Value

A Boolean vector with the same number of rows as the input time series or vector.

```
# Create local copy of SPY TAQ data
ta_q <- HighFreq::SPY_TAQ
# scrub quotes with suspect bid-offer spreads
bid_offer <- ta_q[, "Ask.Price"] - ta_q[, "Bid.Price"]
sus_pect <- which_extreme(bid_offer, look_back=51, vol_mult=3)
# Remove suspect values
ta_q <- ta_q[!sus_pect]</pre>
```

which\_jumps 97

which_jumps	Calculate a Boolean vector that identifies isolated jumps (spikes) in a single-column xts time series or vector, over a rolling interval.

## **Description**

Calculate a *Boolean* vector that identifies isolated jumps (spikes) in a single-column *xts* time series or vector, over a rolling interval.

### **Usage**

```
which_jumps(x_ts, look_back = 51, vol_mult = 2)
```

### **Details**

The function which\_jumps() calculates a *Boolean* vector, with TRUE for values that are isolated jumps (spikes).

The function which\_jumps() applies a version of the Hampel median filter to identify jumps, but instead of using the median absolute deviation (MAD), it uses the 0.9 quantile of returns calculated over a rolling interval. This is in contrast to function which\_extreme(), which applies a Hampel filter to the values themselves, instead of the returns. Returns are defined as simple differences between neighboring values.

Jumps (or spikes), are defined as isolated values that are very different from the neighboring values, either before or after. Jumps create pairs of large neighboring returns of opposite sign.

Jumps (spikes) must satisfy two conditions:

- 1. Neighboring returns both exceed a multiple of the rolling quantile,
- 2. The sum of neighboring returns doesn't exceed that multiple.

The quantile multiplier vol\_mult controls the threshold at which values are identified as jumps. Smaller quantile multiplier values will cause more values to be identified as jumps.

# Value

A Boolean vector with the same number of rows as the input time series or vector.

```
# Create local copy of SPY TAQ data
ta_q <- SPY_TAQ
# Calculate mid prices
mid_prices <- 0.5 * (ta_q[, "Bid.Price"] + ta_q[, "Ask.Price"])
# Replace whole rows containing suspect price jumps with NA, and perform locf()
ta_q[which_jumps(mid_prices, look_back=31, vol_mult=1.0), ] <- NA
ta_q <- xts:::na.locf.xts(ta_q)</pre>
```