# Package 'HighFreq'

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```
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agg\_ohlc

Aggregate a time series of data into a single bar of OHLC data.

# Description

Aggregate a time series of data into a single bar of OHLC data.

# Usage

agg\_ohlc(tseries)

# **Arguments**

tseries

A time series or a matrix with multiple columns of data.

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#### **Details**

The function agg\_ohlc() aggregates a time series of data into a single bar of *OHLC* data. It can accept either a single column of data or four columns of *OHLC* data. It can also accept an additional column containing the trading volume.

The function agg\_ohlc() calculates the *open* value as equal to the *open* value of the first row of tseries. The *high* value as the maximum of the *high* column of tseries. The *low* value as the minimum of the *low* column of tseries. The *close* value as the *close* of the last row of tseries. The *volume* value as the sum of the *volume* column of tseries.

For a single column of data, the open, high, low, and close values are all the same.

#### Value

A *matrix* containing a single row, with the *open*, *high*, *low*, and *close* values, and also the total *volume* (if provided as either the second or fifth column of tseries).

# **Examples**

```
## Not run:
# Define matrix of OHLC data
ohlc <- coredata(rutils::etfenv$VTI[, 1:5])
# Aggregate to single row matrix
ohlcagg <- HighFreq::agg_ohlc(ohlc)
# Compare with calculation in R
all.equal(drop(ohlcagg),
    c(ohlc[1, 1], max(ohlc[, 2]), min(ohlc[, 3]), ohlc[NROW(ohlc), 4], sum(ohlc[, 5])),
    check.attributes=FALSE)
## End(Not run)</pre>
```

agg\_stats\_r

Calculate the aggregation (weighted average) of a statistical estimator over a OHLC time series using R code.

# Description

Calculate the aggregation (weighted average) of a statistical estimator over a *OHLC* time series using R code.

# Usage

```
agg_stats_r(ohlc, calc_bars = "ohlc_variance", weighted = TRUE, ...)
```

# Arguments

... additional parameters to the function calc\_bars.

ohlc An *OHLC* time series of prices and trading volumes, in *xts* format.

calc\_bars A character string representing a function for calculating statistics for individual

OHLC bars.

weighted Boolean argument: should estimate be weighted by the trading volume? (default

is TRUE)

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#### **Details**

The function agg\_stats\_r() calculates a single number representing the volume weighted average of statistics of individual *OHLC* bars. It first calls the function calc\_bars to calculate a vector of statistics for the *OHLC* bars. For example, the statistic may simply be the difference between the *High* minus *Low* prices. In this case the function calc\_bars would calculate a vector of *High* minus *Low* prices. The function agg\_stats\_r() then calculates a trade volume weighted average of the vector of statistics.

The function agg\_stats\_r() is implemented in R code.

#### Value

A single *numeric* value equal to the volume weighted average of an estimator over the time series.

## **Examples**

```
# Calculate weighted average variance for SPY (single number)
variance <- agg_stats_r(ohlc=HighFreq::SPY, calc_bars="ohlc_variance")
# Calculate time series of daily skew estimates for SPY
skew_daily <- apply.daily(x=HighFreq::SPY, FUN=agg_stats_r, calc_bars="ohlc_skew")</pre>
```

back\_test

Simulate (backtest) a rolling portfolio optimization strategy, using RcppArmadillo.

# Description

Simulate (backtest) a rolling portfolio optimization strategy, using RcppArmadillo.

# Usage

```
back_test(
 excess,
 returns,
  startp,
  endp,
  lambda,
 method = "ranksharpe",
 eigen\_thresh = 1e-05,
  eigen_max = 0L,
 conf_lev = 0.1,
 alpha = 0,
  scale = TRUE,
  vol_target = 0.01,
  coeff = 1,
 bid_offer = 0
)
```

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## **Arguments**

| returns      | A <i>time series</i> or a <i>matrix</i> of returns data (the returns in excess of the risk-free rate).  |
|--------------|---|
| excess       | A <i>time series</i> or a <i>matrix</i> of excess returns data (the returns in excess of the risk-free rate).   |
| startp       | An integer vector of start points.  |
| endp         | An integer vector of end points.  |
| lambda       | A <i>numeric</i> decay factor to multiply the past portfolio weights. (The default is $lambda = 0$ - no memory.)  |
| coeff        | A numeric multiplier of the weights. (The default is 1)   |
| bid_offer    | A <i>numeric</i> bid-offer spread (the default is 0)  |
| method       | A <i>string</i> specifying the method for calculating the weights (see Details) (the default is method = "ranksharpe")  |
| eigen_thresh | A <i>numeric</i> threshold level for discarding small singular values in order to regularize the inverse of the returns matrix (the default is 1e–5).   |
| eigen_max    | An <i>integer</i> equal to the number of singular values used for calculating the shrinkage inverse of the returns matrix (the default is $\emptyset$ - equivalent to eigen_max equal to the number of columns of returns). |
| conf_lev     | The confidence level for calculating the quantiles (the default is $conf_{lev} = 0.75$ ).   |
| alpha        | The shrinkage intensity between $\emptyset$ and 1. (the default is $\emptyset$ ).   |
| scale        | A <i>Boolean</i> specifying whether the weights should be scaled (the default is scale = TRUE).   |
| vol_target   | A <i>numeric</i> volatility target for scaling the weights (the default is 1e-5)  |

#### **Details**

The function back\_test() performs a backtest simulation of a rolling portfolio optimization strategy over a *vector* of the end points endp.

It performs a loop over the end points endp, and subsets the *matrix* of the excess asset returns excess along its rows, between the corresponding *start point* and the *end point*. It passes the subset matrix of excess returns into the function calc\_weights(), which calculates the optimal portfolio weights at each *end point*. The arguments eigen\_max, alpha, method, and scale are also passed to the function calc\_weights().

It then recursively averages the weights  $w_i$  at the *end point* = i with the weights  $w_{i-1}$  from the previous *end point* = (i-1), using the decay factor lambda =  $\lambda$ :

$$w_i = (1 - \lambda)w_i + \lambda w_{i-1}$$

The purpose of averaging the weights is to reduce their variance to improve their out-of-sample performance. It is equivalent to extending the portfolio holding period beyond the time interval between neighboring *end points*.

The function back\_test() then calculates the out-of-sample strategy returns by multiplying the average weights times the future asset returns.

The function back\_test() multiplies the out-of-sample strategy returns by the coefficient coeff (with default equal to 1), which allows simulating either a trending strategy (if coeff = 1), or a reverting strategy (if coeff = -1).

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The function back\_test() calculates the transaction costs by multiplying the bid-offer spread bid\_offer times the absolute difference between the current weights minus the weights from the previous period. Then it subtracts the transaction costs from the out-of-sample strategy returns.

The function back\_test() returns a *time series* (column *vector*) of strategy returns, of the same length as the number of rows of returns.

#### Value

A column *vector* of strategy returns, with the same length as the number of rows of returns.

## **Examples**

```
## Not run:
# Calculate the ETF daily excess returns
returns <- na.omit(rutils::etfenv$returns[, 1:16])</pre>
# riskf is the daily risk-free rate
riskf <- 0.03/260
excess <- returns - riskf
# Define monthly end points without initial warmpup period
endp <- rutils::calc_endpoints(returns, interval="months")</pre>
endp <- endp[endp > 0]
nrows <- NROW(endp)</pre>
# Define 12-month look-back interval and start points over sliding window
look_back <- 12
startp <- c(rep_len(1, look_back-1), endp[1:(nrows-look_back+1)])</pre>
# Define shrinkage and regularization intensities
alpha <- 0.5
eigen_max <- 3
# Simulate a monthly rolling portfolio optimization strategy
pnls <- HighFreq::back_test(excess, returns,</pre>
                             startp-1, endp-1,
                             eigen_max = eigen_max,
                             alpha = alpha)
pnls <- xts::xts(pnls, index(returns))</pre>
colnames(pnls) <- "strat_rets"</pre>
# Plot dygraph of strategy
dygraphs::dygraph(cumsum(pnls),
  main="Cumulative Returns of Max Sharpe Portfolio Strategy")
## End(Not run)
```

calc\_cvar

Calculate the Value at Risk (VaR) or the Conditional Value at Risk (CVaR) of an xts time series of returns, using R code.

# **Description**

Calculate the Value at Risk (VaR) or the Conditional Value at Risk (CVaR) of an xts time series of returns, using R code.

## Usage

```
calc_cvar(tseries, method = "var", confi = pnorm(-2))
```

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## **Arguments**

tseries An xts time series of returns with multiple columns.

method A *string* specifying the type of risk measure (the default is method = "var" - see

Details).

confi The confidence level for calculating the quantile (the default is confi = pnorm(-2)

= 0.02275).

#### **Details**

The function calc\_cvar() calculates the Value at Risk (VaR) or the Conditional Value at Risk (CVaR) of an xts time series of returns, using R

The Value at Risk (VaR) and the Conditional Value at Risk (CVaR) are measures of the tail risk of returns.

If method = "var" then  $calc_cvar()$  calculates the Value at Risk (VaR) as the quantile of the returns as follows:

$$\alpha = \int_{-\infty}^{\text{VaR}(\alpha)} f(r) \, \mathrm{d}r$$

Where  $\alpha$  is the confidence level for calculating the quantile, and f(r) is the probability density (distribution) of returns.

If method = "cvar" then calc\_cvar() calculates the Value at Risk (VaR) as the Expected Tail Loss (ETL) of the returns as follows:

$$CVaR = \frac{1}{\alpha} \int_0^{\alpha} VaR(p) dp$$

Where  $\alpha$  is the confidence level for calculating the quantile.

#### Value

A vector with the risk measures of the columns of the input time series tseries.

```
## Not run:
# Calculate VTI and XLF returns
returns <- na.omit(rutils::etfenv$returns[, c("VTI", "XLF")])
# Calculate VaR
all.equal(HighFreq::calc_cvar(returns),
    sapply(returns, quantile, probs=pnorm(-2)), check.attributes=FALSE)
# Calculate CVaR
all.equal(HighFreq::calc_cvar(returns, method="cvar", confi=0.02),
    sapply(returns, function(x) mean(x[x < quantile(x, 0.02)])),
    check.attributes=FALSE)
## End(Not run)</pre>
```

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| calc_eigen | Calculate the eigen decomposition of the covariance matrix of returns data using RcppArmadillo. |
|------------|---|
|            |   |

# Description

Calculate the eigen decomposition of the covariance matrix of returns data using RcppArmadillo.

# Usage

```
calc_eigen(tseries)
```

# **Arguments**

tseries

A time series or matrix of returns data.

#### **Details**

The function calc\_eigen() first calculates the covariance *matrix* of tseries, and then calculates the eigen decomposition of the covariance *matrix*.

# Value

A list with two elements: a *vector* of eigenvalues (named "values"), and a *matrix* of eigenvectors (named "vectors").

```
## Not run:
# Create matrix of random data
datav <- matrix(rnorm(5e6), nc=5)</pre>
# Calculate eigen decomposition
eigend <- HighFreq::calc_eigen(scale(datav, scale=FALSE))</pre>
# Calculate PCA
pcad <- prcomp(datav)</pre>
# Compare PCA with eigen decomposition
all.equal(pcad$sdev^2, drop(eigend$values))
all.equal(abs(unname(pcad$rotation)), abs(eigend$vectors))
# Compare the speed of Rcpp with R code
summary(microbenchmark(
  Rcpp=HighFreq::calc_eigen(datav),
  Rcode=prcomp(datav),
  times=10))[, c(1, 4, 5)] # end microbenchmark summary
## End(Not run)
```

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| calc_endpoints | Calculate a vector of end points that divides a vector into equal intervals. |
|----------------|--|
|----------------|--|

#### **Description**

Calculate a vector of end points that divides a vector into equal intervals.

#### Usage

```
calc_endpoints(length, step = 1L, stub = 0L)
```

# Arguments

| length | An <i>integer</i> equal to the length of the vector to be divided into equal intervals. |
|--------|---|
| step   | The number of elements in each interval between neighboring end points.                 |
| stub   | An <i>integer</i> value equal to the first end point for calculating the end points.    |

#### **Details**

The end points are a vector of integers which divide a vector of length equal to length into equally spaced intervals. If a whole number of intervals doesn't fit over the vector, then calc\_endpoints() adds a stub interval at the end.

The first end point is equal to the argument step, unless the argument stub is provided, and then it becomes the first end point.

For example, consider the end points for a vector of length 20 divided into intervals of length step=5: 0,5,10,15,20. In order for all the differences between neighboring end points to be equal to 5, the first end point is set equal to 0. But 0 doesn't correspond to any vector element, so calc\_endpoints() doesn't include it and it only retains the non-zero end points equal to: 5,10,15,20.

Since indexing in C++ code starts at 0, then calc\_endpoints() shifts the end points by -1 and returns the vector equal to 4,9,14,19.

If stub = 1 then the first end point is equal to 1 and the end points are equal to: 1,6,11,16,20. The extra stub interval at the end is equal to 4 = 20 - 16. And calc\_endpoints() returns 0,5,10,15,19. The first value is equal to 0 which is the index of the first element in C++ code.

If stub = 2 then the first end point is equal to 2, with an extra stub interval at the end, and the end points are equal to: 2,7,12,17,20. And calc\_endpoints() returns 1,6,11,16,19.

The function calc\_endpoints() is similar to the function rutils::calc\_endpoints() from package rutils.

But the end points are shifted by -1 compared to R code because indexing starts at 0 in C++ code, while it starts at 1 in R code. So if calc\_endpoints() is used in R code then 1 should be added to it.

This works in R code because the vector element corresponding to index 0 is empty. For example, the R code: (4:1)[c(0,1)] produces 4. So in R we can select vector elements using the end points starting at zero.

In C++ the end points must be shifted by -1 compared to R code, because indexing starts at 0: -1,4,9,14,19. But there is no vector element corresponding to index -1. So in C++ we cannot select vector elements using the end points starting at -1. The solution is to drop the first placeholder end point.

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#### Value

A vector of equally spaced *integers* representing the end points.

#### **Examples**

```
# Calculate end points without a stub interval
HighFreq::calc_endpoints(length=20, step=5)
# Calculate end points with a final stub interval
HighFreq::calc_endpoints(length=23, step=5)
# Calculate end points with initial and final stub intervals
HighFreq::calc_endpoints(length=20, step=5, stub=2)
# Calculate end points with initial and final stub intervals
HighFreq::calc_endpoints(length=20, step=5, stub=24)
```

calc\_hurst

Calculate the Hurst exponent from the volatility ratio of aggregated returns.

#### **Description**

Calculate the Hurst exponent from the volatility ratio of aggregated returns.

#### Usage

```
calc_hurst(tseries, step = 1L)
```

# Arguments

tseries A time series or a matrix of prices.

step The number of periods in each interval between neighboring end points.

#### **Details**

The function calc\_hurst() calculates the Hurst exponent from the ratios of the volatilities of aggregated returns.

The aggregated volatility  $\sigma_t$  scales (increases) with the length of the aggregation interval  $\Delta t$  raised to the power of the *Hurst exponent H*:

$$\sigma_t = \sigma \Delta t^H$$

Where  $\sigma$  is the daily return volatility.

The *Hurst exponent H* is equal to the logarithm of the ratio of the volatilities divided by the logarithm of the time interval  $\Delta t$ :

$$H = \frac{\log \sigma_t - \log \sigma}{\log \Delta t}$$

The function calc\_hurst() calls the function calc\_var\_ag() to calculate the aggregated volatility  $\sigma_t$ .

## Value

The Hurst exponent calculated from the variance of aggregated returns.

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#### **Examples**

```
## Not run:
# Calculate the log prices
prices <- na.omit(rutils::etfenv$prices[, c("XLP", "VTI")])
prices <- log(prices)
# Calculate the Hurst exponent from 21 day aggregations
calc_hurst(prices, step=21)
## End(Not run)</pre>
```

calc\_hurst\_ohlc

Calculate the Hurst exponent from the volatility ratio of aggregated OHLC prices.

#### **Description**

Calculate the Hurst exponent from the volatility ratio of aggregated OHLC prices.

## Usage

```
calc_hurst_ohlc(
  ohlc,
  step = 1L,
  method = "yang_zhang",
  close_lag = 0L,
  scale = TRUE,
  index = 0L
)
```

#### **Arguments**

ohlc

A time series or a matrix of OHLC prices.

step

The number of periods in each interval between neighboring end points.

method

A *character* string representing the price range estimator for calculating the variance. The estimators include:

- "close" close-to-close estimator,
- "rogers\_satchell" Rogers-Satchell estimator,
- "garman\_klass" Garman-Klass estimator,
- "garman\_klass\_yz" Garman-Klass with account for close-to-open price jumps,
- "yang\_zhang" Yang-Zhang estimator,

(The default is the method = "yang\_zhang".)

close\_lag

A *vector* with the lagged *close* prices of the *OHLC time series*. This is an optional argument. (The default is  $close_lag = 0$ ).

scale

*Boolean* argument: Should the returns be divided by the time index, the number of seconds in each period? (The default is scale = TRUE).

A *vector* with the time index of the *time series*. This is an optional argument (the default is index = 0).

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#### **Details**

The function calc\_hurst\_ohlc() calculates the Hurst exponent from the ratios of the volatilities of aggregated *OHLC* prices.

The aggregated volatility  $\sigma_t$  scales (increases) with the length of the aggregation interval  $\Delta t$  raised to the power of the *Hurst exponent H*:

$$\sigma_t = \sigma \Delta t^H$$

Where  $\sigma$  is the daily return volatility.

The *Hurst exponent H* is equal to the logarithm of the ratio of the volatilities divided by the logarithm of the time interval  $\Delta t$ :

$$H = \frac{\log \sigma_t - \log \sigma}{\log \Delta t}$$

The function calc\_hurst\_ohlc() calls the function calc\_var\_ohlc\_ag() to calculate the aggregated volatility  $\sigma_t$ .

#### Value

The Hurst exponent calculated from the variance ratio of aggregated OHLC prices.

# **Examples**

```
## Not run:
# Calculate the log ohlc prices
ohlc <- log(rutils::etfenv$VTI)
# Calculate the Hurst exponent from 21 day aggregations
calc_hurst_ohlc(ohlc, step=21)
## End(Not run)</pre>
```

calc\_inv

Calculate the shrinkage inverse of a matrix of data using Singular Value Decomposition (SVD).

# Description

Calculate the shrinkage inverse of a matrix of data using Singular Value Decomposition (SVD).

# Usage

```
calc_inv(tseries, eigen_thresh = 0.01, eigen_max = 0L)
```

## **Arguments**

tseries A time series or matrix of data.

eigen\_thresh A numeric threshold level for discarding small singular values in order to regu-

larize the inverse of the matrix tseries (the default is 0.01).

eigen\_max An integer equal to the number of singular values used for calculating the shrink-

age inverse of the matrix tseries (the default is eigen\_max = 0 - equivalent to

eigen\_max equal to the number of columns of tseries).

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#### **Details**

The function calc\_inv() calculates the shrinkage inverse of the matrix tseries using Singular Value Decomposition (SVD).

The function calc\_inv() first performs Singular Value Decomposition (*SVD*) of the matrix tseries. The *SVD* of a matrix *A* is defined as the factorization:

$$A = U \Sigma V^T$$

Where U and V are the left and right *singular matrices*, and  $\Sigma$  is a diagonal matrix of *singular values*  $\Sigma = {\sigma_i}$ .

The inverse  $A^{-1}$  of the matrix A can be calculated from the SVD matrices as:

$$A^{-1} = V \Sigma^{-1} U^T$$

The *regularized inverse* of the matrix A is given by:

$$A^{-1} = V_n \Sigma_n^{-1} U_n^T$$

Where  $U_n$ ,  $V_n$  and  $\Sigma_n$  are the SVD matrices with the rows and columns corresponding to zero singular values removed.

The function calc\_inv() applies regularization by discarding the smallest singular values  $\sigma_i$  that are less than the threshold level eigen\_thresh times the sum of all the singular values:

$$\sigma_i < eigen\_thresh \cdot (\sum \sigma_i)$$

It then discards additional singular values so that only the largest eigen\_max singular values remain. It calculates the shrinkage inverse from the *SVD* matrices using only the largest singular values up to eigen\_max. For example, if eigen\_max = 3 then it only uses the 3 largest singular values. This has the effect of dimension shrinkage.

If the matrix tseries has a large number of small singular values, then the number of remaining singular values may be less than eigen\_max.

#### Value

A *matrix* equal to the shrinkage inverse of the matrix tseries.

```
## Not run:
# Calculate ETF returns
returns <- na.omit(rutils::etfenv$returns)
# Calculate covariance matrix
covmat <- cov(returns)
# Calculate shrinkage inverse using RcppArmadillo
inverse <- HighFreq::calc_inv(covmat, eigen_max=3)
# Calculate shrinkage inverse from SVD in R
svdec <- svd(covmat)
eigen_max <- 1:3
inverser <- svdec$v[, eigen_max] %*% (t(svdec$u[, eigen_max]) / svdec$d[eigen_max])
# Compare RcppArmadillo with R
all.equal(inverse, inverser)
## End(Not run)</pre>
```

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|  | Calculate the kurtosis of the columns of a time series or a matrix using RcppArmadillo. |
|--|---|
|--|---|

#### **Description**

Calculate the kurtosis of the columns of a time series or a matrix using RcppArmadillo.

# Usage

```
calc_kurtosis(tseries, method = "moment", conf_lev = 0.75)
```

#### **Arguments**

tseries A time series or a matrix of data.

method A string specifying the type of the kurtosis model (the default is method = "moment" - see Details).

conf\_lev The confidence level for calculating the quantiles (the default is conf\_lev =

0.75).

#### **Details**

The function calc\_kurtosis() calculates the kurtosis of the columns of the *matrix* tseries using RcppArmadillo C++ code.

If method = "moment" (the default) then calc\_kurtosis() calculates the fourth moment of the data. But it doesn't de-mean the columns of tseries because that requires copying the matrix tseries, so it's time-consuming.

If method = "quantile" then it calculates the skewness  $\kappa$  from the differences between the quantiles of the data as follows:

$$\kappa = \frac{q_{\alpha} - q_{1-\alpha}}{q_{0.75} - q_{0.25}}$$

Where  $\alpha$  is the confidence level for calculating the quantiles.

If method = "nonparametric" then it calculates the kurtosis as the difference between the mean of the data minus its median, divided by the standard deviation.

If the number of rows of tseries is less than 3 then it returns zeros.

The code examples below compare the function calc\_kurtosis() with the kurtosis calculated using R code.

## Value

A single-row matrix with the kurtosis of the columns of tseries.

```
## Not run:
# Define a single-column time series of returns
returns <- na.omit(rutils::etfenv$returns$VTI)
# Calculate the moment kurtosis
HighFreq::calc_kurtosis(returns)
# Calculate the moment kurtosis in R</pre>
```

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```
calc_kurtr <- function(x) {</pre>
  x \leftarrow (x-mean(x))
  sum(x^4)/var(x)^2/NROW(x)
} # end calc_kurtr
all.equal(HighFreq::calc_kurtosis(returns),
  calc_kurtr(returns), check.attributes=FALSE)
# Compare the speed of RcppArmadillo with R code
library(microbenchmark)
summary(microbenchmark(
  Rcpp=HighFreq::calc_kurtosis(returns),
  Rcode=calc_kurtr(returns),
  times=10))[, c(1, 4, 5)] # end microbenchmark summary
# Calculate the quantile kurtosis
HighFreq::calc_kurtosis(returns, method="quantile", conf_lev=0.9)
# Calculate the quantile kurtosis in R
calc_kurtq <- function(x, a=0.9) {</pre>
   quantiles <- quantile(x, c(1-a, 0.25, 0.75, a), type=5)
   (quantiles[4] - quantiles[1])/(quantiles[3] - quantiles[2])
} # end calc_kurtq
all.equal(drop(HighFreq::calc_kurtosis(returns, method="quantile", conf_lev=0.9)),
  calc_kurtq(returns, a=0.9), check.attributes=FALSE)
# Compare the speed of RcppArmadillo with R code
summary(microbenchmark(
  Rcpp=HighFreq::calc_kurtosis(returns, method="quantile"),
  Rcode=calc_kurtq(returns),
  times=10))[, c(1, 4, 5)] # end microbenchmark summary
# Calculate the nonparametric kurtosis
HighFreq::calc_kurtosis(returns, method="nonparametric")
# Compare HighFreq::calc_kurtosis() with R nonparametric kurtosis
all.equal(drop(HighFreq::calc_kurtosis(returns, method="nonparametric")),
  (mean(returns)-median(returns))/sd(returns),
  check.attributes=FALSE)
# Compare the speed of RcppArmadillo with R code
summary(microbenchmark(
  Rcpp=HighFreq::calc_kurtosis(returns, method="nonparametric"),
  Rcode=(mean(returns)-median(returns))/sd(returns),
  times=10))[, c(1, 4, 5)] # end microbenchmark summary
## End(Not run)
```

calc\_lm

Perform multivariate linear regression using least squares and return a named list of regression coefficients, their t-values, and p-values.

# Description

Perform multivariate linear regression using least squares and return a named list of regression coefficients, their t-values, and p-values.

# Usage

```
calc_lm(response, predictor)
```

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### **Arguments**

response A single-column time series or a vector of response data.

predictor A time series or a matrix of predictor data.

#### **Details**

The function calc\_lm() performs the same calculations as the function lm() from package *stats*. It uses RcppArmadillo C++ code so it's several times faster than lm(). The code was inspired by this article (but it's not identical to it): http://gallery.rcpp.org/articles/fast-linear-model-with-armadillo/

#### Value

A named list with three elements: a *matrix* of coefficients (named "coefficients"), the z-score of the last residual (named "zscore"), and a vector with the R-squared and F-statistic (named "stats"). The numeric matrix of coefficients named "coefficients" contains the alpha and beta coefficients, and their t-values and p-values.

# **Examples**

```
## Not run:
# Calculate historical returns
returns <- na.omit(rutils::etfenv$returns[, c("XLF", "VTI", "IEF")])</pre>
# Response equals XLF returns
response <- returns[, 1]</pre>
# Predictor matrix equals VTI and IEF returns
predictor <- returns[, -1]</pre>
# Perform multivariate regression using lm()
reg_model <- lm(response ~ predictor)</pre>
sum_mary <- summary(reg_model)</pre>
# Perform multivariate regression using calc_lm()
reg_arma <- HighFreq::calc_lm(response=response, predictor=predictor)</pre>
# Compare the outputs of both functions
all.equal(reg_arma$coefficients[, "coeff"], unname(coef(reg_model)))
all.equal(unname(reg_arma$coefficients), unname(sum_mary$coefficients))
all.equal(unname(reg_arma$stats), c(sum_mary$r.squared, unname(sum_mary$fstatistic[1])))
# Compare the speed of RcppArmadillo with R code
summary(microbenchmark(
  Rcpp=HighFreq::calc_lm(response=response, predictor=predictor),
  Rcode=lm(response ~ predictor),
  times=10))[, c(1, 4, 5)] # end microbenchmark summary
## End(Not run)
```

calc\_mean

Calculate the mean (location) of the columns of a time series or a matrix using RcppArmadillo.

## **Description**

Calculate the mean (location) of the columns of a time series or a matrix using RcppArmadillo.

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#### Usage

```
calc_mean(tseries, method = "moment", conf_lev = 0.75)
```

#### **Arguments**

tseries A time series or a matrix of data.

method A string specifying the type of the mean (location) model (the default is method

= "moment" - see Details).

conf\_lev The confidence level for calculating the quantiles (the default is conf\_lev =

0.75).

#### **Details**

The function calc\_mean() calculates the mean (location) values of the columns of the *time series* tseries using RcppArmadillo C++ code.

If method = "moment" (the default) then calc\_mean() calculates the location as the mean - the first moment of the data.

If method = "quantile" then it calculates the location  $\mu$  as the sum of the quantiles as follows:

$$\mu = q_{\alpha} + q_{1-\alpha}$$

Where  $\alpha$  is the confidence level for calculating the quantiles.

If method = "nonparametric" then it calculates the location as the median.

The code examples below compare the function calc\_mean() with the mean (location) calculated using R code.

# Value

A single-row matrix with the mean (location) of the columns of tseries.

```
## Not run:
# Calculate historical returns
returns <- na.omit(rutils::etfenv$returns[, c("XLP", "VTI")])</pre>
# Calculate the column means in RcppArmadillo
HighFreq::calc_mean(returns)
# Calculate the column means in R
sapply(returns, mean)
# Compare the values
all.equal(drop(HighFreq::calc_mean(returns)),
  sapply(returns, mean), check.attributes=FALSE)
# Compare the speed of RcppArmadillo with R code
library(microbenchmark)
summary(microbenchmark(
  Rcpp=HighFreq::calc_mean(returns),
  Rcode=sapply(returns, mean),
  times=10))[, c(1, 4, 5)] # end microbenchmark summary
# Calculate the quantile mean (location)
HighFreq::calc_mean(returns, method="quantile", conf_lev=0.9)
# Calculate the quantile mean (location) in R
colSums(sapply(returns, quantile, c(0.9, 0.1), type=5))
# Compare the values
```

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```
all.equal(drop(HighFreq::calc_mean(returns, method="quantile", conf_lev=0.9)),
  colSums(sapply(returns, quantile, c(0.9, 0.1), type=5)),
  check.attributes=FALSE)
# Compare the speed of RcppArmadillo with R code
summary(microbenchmark(
  Rcpp=HighFreq::calc_mean(returns, method="quantile", conf_lev=0.9),
  Rcode=colSums(sapply(returns, quantile, c(0.9, 0.1), type=5)),
  times=10))[, c(1, 4, 5)] # end microbenchmark summary
# Calculate the column medians in RcppArmadillo
HighFreq::calc_mean(returns, method="nonparametric")
# Calculate the column medians in R
sapply(returns, median)
# Compare the values
all.equal(drop(HighFreq::calc_mean(returns, method="nonparametric")),
  sapply(returns, median), check.attributes=FALSE)
# Compare the speed of RcppArmadillo with R code
summary(microbenchmark(
  Rcpp=HighFreq::calc_mean(returns, method="nonparametric"),
  Rcode=sapply(returns, median),
  times=10))[, c(1, 4, 5)] # end microbenchmark summary
## End(Not run)
```

calc\_ranks

Calculate the ranks of the elements of a single-column time series or a vector using RcppArmadillo.

## **Description**

Calculate the ranks of the elements of a single-column time series or a vector using RcppArmadillo.

# Usage

```
calc_ranks(tseries)
```

## **Arguments**

tseries

A single-column time series or a vector.

## **Details**

The function calc\_ranks() calculates the ranks of the elements of a single-column *time series* or a *vector*. It uses the RcppArmadillo function arma::sort\_index(). The function arma::sort\_index() calculates the permutation index to sort a given vector into ascending order.

Applying the function arma::sort\_index() twice: arma::sort\_index(arma::sort\_index()), calculates the *reverse* permutation index to sort the vector from ascending order back into its original unsorted order. The permutation index produced by: arma::sort\_index(arma::sort\_index()) is the *reverse* of the permutation index produced by: arma::sort\_index().

The ranks of the elements are equal to the *reverse* permutation index. The function calc\_ranks() calculates the *reverse* permutation index.

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#### Value

An *integer vector* with the ranks of the elements of the tseries.

# **Examples**

```
## Not run:
# Create a vector of random data
datav <- round(runif(7), 2)</pre>
# Calculate the ranks of the elements in two ways
all.equal(rank(datav), drop(HighFreq::calc_ranks(datav)))
# Create a time series of random data
datav <- xts::xts(runif(7), seq.Date(Sys.Date(), by=1, length.out=7))</pre>
# Calculate the ranks of the elements in two ways
all.equal(rank(coredata(datav)), drop(HighFreq::calc_ranks(datav)))
# Compare the speed of RcppArmadillo with R code
datav <- runif(7)</pre>
library(microbenchmark)
summary(microbenchmark(
  Rcpp=calc_ranks(datav),
  Rcode=rank(datav),
  times=10))[, c(1, 4, 5)] # end microbenchmark summary
## End(Not run)
```

calc\_reg

Perform multivariate regression using different methods, and return a vector of regression coefficients, their t-values, and the last residual z-score.

## **Description**

Perform multivariate regression using different methods, and return a vector of regression coefficients, their t-values, and the last residual z-score.

# Usage

```
calc_reg(
  response,
  predictor,
  intercept = FALSE,
  method = "least_squares",
  eigen_thresh = 1e-05,
  eigen_max = 0L,
  conf_lev = 0.1,
  alpha = 0
)
```

## **Arguments**

response A single-column *time series* or a *vector* of response data.

predictor A time series or a matrix of predictor data.

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| intercept    | A <i>Boolean</i> specifying whether an intercept term should be added to the predictor (the default is intercept = FALSE).  |
|--------------|---|
| method       | A <i>string</i> specifying the type of the regression model the default is method = "least_squares" - see Details).   |
| eigen_thresh | A <i>numeric</i> threshold level for discarding small singular values in order to regularize the inverse of the predictor matrix (the default is 1e-5).   |
| eigen_max    | An <i>integer</i> equal to the number of singular values used for calculating the shrinkage inverse of the predictor matrix (the default is 0 - equivalent to eigen_max equal to the number of columns of predictor). |
| conf_lev     | The confidence level for calculating the quantiles (the default is $conf_lev = 0.75$ ).   |
| alpha        | The shrinkage intensity between 0 and 1. (the default is 0).  |

#### **Details**

The function calc\_reg() performs multivariate regression using different methods, and returns a vector of regression coefficients, their t-values, and the last residual z-score.

If method = "least\_squares" (the default) then it performs the standard least squares regression, the same as the function calc\_lm(), and the function lm() from the R package *stats*. But it uses RcppArmadillo C++ code so it's several times faster than lm().

If method = "regular" then it performs shrinkage regression. It calculates the shrinkage inverse of the predictor matrix from its singular value decomposition. It applies dimension regularization by selecting only the largest singular values equal in number to eigen\_max.

If method = "quantile" then it performs quantile regression (not implemented yet).

If intercept = TRUE then an extra intercept column (unit column) is added to the predictor matrix (the default is intercept = FALSE).

The length of the return vector depends on the number of columns of the predictor matrix (including the intercept column, if it's added). The length of the return vector is equal to the number of regression coefficients, plus their t-values, plus the z-score. The number of regression coefficients is equal to the number of columns of the predictor matrix (including the intercept column, if it's added). The number of t-values is equal to the number of coefficients.

For example, if the number of columns of the predictor matrix is equal to n, and if intercept = TRUE, then calc\_reg() returns a vector with 2n+3 elements: n+1 regression coefficients (including the intercept coefficient), n+1 corresponding t-values, and 1 z-score.

#### Value

A single-row matrix with A vector with the regression coefficients, their t-values, and the last residual z-score.

```
## Not run:
# Calculate historical returns
returns <- na.omit(rutils::etfenv$returns[, c("XLF", "VTI", "IEF")])
# Response equals XLF returns
response <- returns[, 1]
# Predictor matrix equals VTI and IEF returns
predictor <- returns[, -1]
# Perform multivariate regression using lm()</pre>
```

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```
reg_model <- lm(response ~ predictor)
sum_mary <- summary(reg_model)
coeff <- sum_mary$coefficients
# Perform multivariate regression using calc_reg()
reg_arma <- drop(HighFreq::calc_reg(response=response, predictor=predictor))
# Compare the outputs of both functions
all.equal(reg_arma[1:(2*(1+NCOL(predictor)))],
    c(coeff[, "Estimate"], coeff[, "t value"]), check.attributes=FALSE)
# Compare the speed of RcppArmadillo with R code
library(microbenchmark)
summary(microbenchmark(
    Rcpp=HighFreq::calc_reg(response=response, predictor=predictor),
    Rcode=lm(response ~ predictor),
    times=10))[, c(1, 4, 5)] # end microbenchmark summary</pre>
## End(Not run)
```

calc\_scaled

Scale (standardize) the columns of a matrix of data using RcppArmadillo.

# **Description**

Scale (standardize) the columns of a *matrix* of data using RcppArmadillo.

#### Usage

```
calc_scaled(tseries, use_median = FALSE)
```

# **Arguments**

tseries A time series or matrix of data.

use\_median A Boolean argument: if TRUE then the centrality (central tendency) is calculated

as the *median* and the dispersion is calculated as the *median absolute deviation* (*MAD*). If use\_median = FALSE then the centrality is calculated as the *mean* and the dispersion is calculated as the *standard deviation* (the default is FALSE)

# **Details**

The function calc\_scaled() scales (standardizes) the columns of the tseries argument using RcppArmadillo.

If the argument use\_median is FALSE (the default), then it performs the same calculation as the standard R function scale(), and it calculates the centrality (central tendency) as the *mean* and the dispersion as the *standard deviation*.

If the argument use\_median is TRUE, then it calculates the centrality as the *median* and the dispersion as the *median absolute deviation (MAD)*.

If the number of rows of tseries is less than 3 then it returns tseries unscaled.

The function calc\_scaled() uses RcppArmadillo C++ code and is about 5 times faster than function scale(), for a *matrix* with 1,000 rows and 20 columns.

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#### Value

A *matrix* with the same dimensions as the input argument tseries.

# **Examples**

```
## Not run:
# Create a matrix of random data
returns <- matrix(rnorm(20000), nc=20)
scaled <- calc_scaled(tseries=returns, use_median=FALSE)
scaled2 <- scale(returns)
all.equal(scaled, scaled2, check.attributes=FALSE)
# Compare the speed of Rcpp with R code
library(microbenchmark)
summary(microbenchmark(
   Rcpp=calc_scaled(tseries=returns, use_median=FALSE),
   Rcode=scale(returns),
   times=100))[, c(1, 4, 5)] # end microbenchmark summary
## End(Not run)</pre>
```

calc\_skew

Calculate the skewness of the columns of a time series or a matrix using RcppArmadillo.

# Description

Calculate the skewness of the columns of a time series or a matrix using RcppArmadillo.

# Usage

```
calc_skew(tseries, method = "moment", conf_lev = 0.75)
```

# **Arguments**

tseries A *time series* or a *matrix* of data.

method A *string* specifying the type of the skewness model (the default is method =

"moment" - see Details).

conf\_lev The confidence level for calculating the quantiles (the default is conf\_lev =

0.75).

## **Details**

The function calc\_skew() calculates the skewness of the columns of a *time series* or a *matrix* of data using RcppArmadillo C++ code.

If method = "moment" (the default) then calc\_skew() calculates the skewness as the third moment of the data.

If method = "quantile" then it calculates the skewness  $\varsigma$  from the differences between the quantiles of the data as follows:

$$\varsigma = \frac{q_\alpha + q_{1-\alpha} - 2*q_{0.5}}{q_\alpha - q_{1-\alpha}}$$

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Where  $\alpha$  is the confidence level for calculating the quantiles.

If method = "nonparametric" then it calculates the skewness as the difference between the mean of the data minus its median, divided by the standard deviation.

If the number of rows of tseries is less than 3 then it returns zeros.

The code examples below compare the function calc\_skew() with the skewness calculated using R code.

#### Value

A single-row matrix with the skewness of the columns of tseries.

```
## Not run:
# Define a single-column time series of returns
returns <- na.omit(rutils::etfenv$returns$VTI)</pre>
# Calculate the moment skewness
HighFreq::calc_skew(returns)
\# Calculate the moment skewness in R
calc_skewr <- function(x) {</pre>
 x <- (x-mean(x))
  sum(x^3)/var(x)^1.5/NROW(x)
} # end calc_skewr
all.equal(HighFreq::calc_skew(returns),
  calc_skewr(returns), check.attributes=FALSE)
# Compare the speed of RcppArmadillo with R code
library(microbenchmark)
summary(microbenchmark(
  Rcpp=HighFreq::calc_skew(returns),
  Rcode=calc_skewr(returns),
  times=10))[, c(1, 4, 5)] # end microbenchmark summary
# Calculate the quantile skewness
HighFreq::calc_skew(returns, method="quantile", conf_lev=0.9)
# Calculate the quantile skewness in R
calc_skewq \leftarrow function(x, a = 0.75) {
   quantiles <- quantile(x, c(1-a, 0.5, a), type=5)
   (quantiles[3] + quantiles[1] - 2*quantiles[2])/(quantiles[3] - quantiles[1])
} # end calc_skewq
all.equal(drop(HighFreq::calc_skew(returns, method="quantile", conf_lev=0.9)),
  calc_skewq(returns, a=0.9), check.attributes=FALSE)
# Compare the speed of RcppArmadillo with R code
summary(microbenchmark(
  Rcpp=HighFreq::calc_skew(returns, method="quantile"),
  Rcode=calc_skewq(returns),
  times=10))[, c(1, 4, 5)] # end microbenchmark summary
# Calculate the nonparametric skewness
HighFreq::calc_skew(returns, method="nonparametric")
# Compare HighFreq::calc_skew() with R nonparametric skewness
all.equal(drop(HighFreq::calc_skew(returns, method="nonparametric")),
  (mean(returns)-median(returns))/sd(returns),
  check.attributes=FALSE)
# Compare the speed of RcppArmadillo with R code
summary(microbenchmark(
  Rcpp=HighFreq::calc_skew(returns, method="nonparametric"),
  Rcode=(mean(returns)-median(returns))/sd(returns),
  times=10))[, c(1, 4, 5)] # end microbenchmark summary
```

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```
## End(Not run)
```

calc\_startpoints Calculate a vector of start points by lagging (shifting) a vector of end points.

# Description

Calculate a vector of start points by lagging (shifting) a vector of end points.

#### Usage

```
calc_startpoints(endp, look_back)
```

## **Arguments**

endp An *integer* vector of end points.

look\_back The length of the look-back interval, equal to the lag (shift) applied to the end

points.

#### **Details**

The start points are equal to the values of the vector endp lagged (shifted) by an amount equal to look\_back. In addition, an extra value of 1 is added to them, to avoid data overlaps. The lag operation requires appending a beginning warmup interval containing zeros, so that the vector of start points has the same length as the endp.

For example, consider the end points for a vector of length 25 divided into equal intervals of length 5: 4,9,14,19,24. (In C++ the vector indexing starts at 0 not 1, so it's shifted by -1.) Then the start points for look\_back = 2 are equal to: 0,0,5,10,15. The differences between the end points minus the corresponding start points are equal to 9, except for the warmup interval.

#### Value

An integer vector with the same number of elements as the vector endp.

```
# Calculate end points
endp <- HighFreq::calc_endpoints(25, 5)
# Calculate start points corresponding to the end points
startp <- HighFreq::calc_startpoints(endp, 2)</pre>
```

26 calc\_var

| calc_var | Calculate the dispersion (variance) of the columns of a time series or a matrix using RcppArmadillo. |
|----------|--|
|          | 0 11   |

# **Description**

Calculate the dispersion (variance) of the columns of a *time series* or a *matrix* using RcppArmadillo.

## Usage

```
calc_var(tseries, method = "moment", conf_lev = 0.75)
```

#### **Arguments**

tseries A time series or a matrix of data.

method A string specifying the type of the dispersion model (the default is method = "moment" - see Details).

conf\_lev The confidence level for calculating the quantiles (the default is conf\_lev =

0.75).

#### **Details**

The dispersion is a measure of the variability of the data. Examples of dispersion are the variance and the Median Absolute Deviation (*MAD*).

The function calc\_var() calculates the dispersion of the columns of a *time series* or a *matrix* of data using RcppArmadillo C++ code.

If method = "moment" (the default) then calc\_var() calculates the dispersion as the second moment of the data  $\sigma^2$  (the variance).

If method = "moment" then calc\_var() performs the same calculation as the function colVars() from package matrixStats, but it's much faster because it uses RcppArmadillo C++ code.

If method = "quantile" then it calculates the dispersion as the difference between the quantiles as follows:

$$\mu = q_{\alpha} - q_{1-\alpha}$$

Where  $\alpha$  is the confidence level for calculating the quantiles.

If method = "nonparametric" then it calculates the dispersion as the Median Absolute Deviation (MAD):

$$MAD = median(abs(x - median(x)))$$

It also multiplies the  $M\!AD$  by a factor of 1.4826, to make it comparable to the standard deviation.

If method = "nonparametric" then calc\_var() performs the same calculation as the function stats::mad(), but it's much faster because it uses RcppArmadillo C++ code.

If the number of rows of tseries is less than 3 then it returns zeros.

# Value

A row vector equal to the dispersion of the columns of the matrix tseries.

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#### **Examples**

```
## Not run:
# Calculate VTI and XLF returns
returns <- na.omit(rutils::etfenv$returns[, c("VTI", "XLF")])</pre>
# Compare HighFreq::calc_var() with standard var()
all.equal(drop(HighFreq::calc_var(returns)),
  apply(returns, 2, var), check.attributes=FALSE)
# Compare HighFreq::calc_var() with matrixStats
all.equal(drop(HighFreq::calc_var(returns)),
  matrixStats::colVars(returns), check.attributes=FALSE)
\mbox{\#} Compare the speed of RcppArmadillo with matrixStats and with R code
library(microbenchmark)
summary(microbenchmark(
  Rcpp=HighFreq::calc_var(returns),
  matrixStats=matrixStats::colVars(returns),
  Rcode=apply(returns, 2, var),
  times=10))[, c(1, 4, 5)] # end microbenchmark summary
# Compare HighFreq::calc_var() with stats::mad()
all.equal(drop(HighFreq::calc_var(returns, method="nonparametric")),
  sapply(returns, mad), check.attributes=FALSE)
# Compare the speed of RcppArmadillo with stats::mad()
summary(microbenchmark(
  Rcpp=HighFreq::calc_var(returns, method="nonparametric"),
  Rcode=sapply(returns, mad),
  times=10))[, c(1, 4, 5)] # end microbenchmark summary
## End(Not run)
```

calc\_varvec

Calculate the variance of a single-column time series  $or\ a$  vector  $using\ RcppArmadillo.$ 

# Description

Calculate the variance of a single-column time series or a vector using RcppArmadillo.

# Usage

```
calc_varvec(tseries)
```

# Arguments

tseries

A single-column time series or a vector.

#### **Details**

The function calc\_varvec() calculates the variance of a *vector* using RcppArmadillo C++ code, so it's significantly faster than the R function var().

## Value

A numeric value equal to the variance of the vector.

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#### **Examples**

```
## Not run:
# Create a vector of random returns
returns <- rnorm(1e6)
# Compare calc_varvec() with standard var()
all.equal(HighFreq::calc_varvec(returns),
    var(returns))
# Compare the speed of RcppArmadillo with R code
library(microbenchmark)
summary(microbenchmark(
    Rcpp=HighFreq::calc_varvec(returns),
    Rcode=var(returns),
    times=10))[, c(1, 4, 5)] # end microbenchmark summary
## End(Not run)</pre>
```

calc\_var\_ag

Calculate the variance of returns aggregated over end points.

#### **Description**

Calculate the variance of returns aggregated over end points.

#### **Usage**

```
calc_var_ag(tseries, step = 1L)
```

# **Arguments**

tseries A time series or a matrix of prices.

step The number of periods in each interval between neighboring end points.

## **Details**

The function calc\_var\_ag() calculates the variance of returns aggregated over end points.

It first calculates the end points spaced apart by the number of periods equal to the argument step. Then it calculates the aggregated returns by differencing the prices tseries calculated at the end points. Finally it calculates the variance of the returns.

If there are extra periods that don't fit over the length of tseries, then calc\_var\_ag() loops over all possible stub intervals, then it calculates all the corresponding variance values, and averages them

For example, if the number of rows of tseries is equal to 20, and step=3 then 6 end points fit over the length of tseries, and there are 2 extra periods that must fit into stubs, either at the beginning or at the end (or both).

The aggregated volatility  $\sigma_t$  scales (increases) with the length of the aggregation interval  $\Delta t$  raised to the power of the *Hurst exponent H*:

$$\sigma_t = \sigma \Delta t^H$$

Where  $\sigma$  is the daily return volatility.

The function calc\_var\_ag() can therefore be used to calculate the *Hurst exponent* from the volatility ratio.

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#### Value

The variance of aggregated returns.

# **Examples**

```
## Not run:
# Calculate the log prices
prices <- na.omit(rutils::etfenv$prices[, c("XLP", "VTI")])
prices <- log(prices)
# Calculate the daily variance of percentage returns
calc_var_ag(prices, step=1)
# Calculate the daily variance using R
sapply(rutils::diffit(prices), var)
# Calculate the variance of returns aggregated over 21 days
calc_var_ag(prices, step=21)
# The variance over 21 days is approximately 21 times the daily variance
21*calc_var_ag(prices, step=1)
## End(Not run)</pre>
```

calc\_var\_ohlc

Calculate the variance of returns from OHLC prices using different price range estimators.

# **Description**

Calculate the variance of returns from *OHLC* prices using different price range estimators.

# Usage

```
calc_var_ohlc(
  ohlc,
  method = "yang_zhang",
  close_lag = 0L,
  scale = TRUE,
  index = 0L
)
```

# **Arguments**

ohlc

A time series or a matrix of OHLC prices.

method

A *character* string representing the price range estimator for calculating the variance. The estimators include:

- "close" close-to-close estimator,
- "rogers\_satchell" Rogers-Satchell estimator,
- "garman\_klass" Garman-Klass estimator,
- "garman\_klass\_yz" Garman-Klass with account for close-to-open price jumps,
- "yang\_zhang" Yang-Zhang estimator,

(The default is the method = "yang\_zhang".)

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close\_lag A *vector* with the lagged *close* prices of the *OHLC time series*. This is an optional argument. (The default is close\_lag = 0).

Boolean argument: Should the returns be divided by the time index, the number

of seconds in each period? (The default is scale = TRUE).

index A vector with the time index of the time series. This is an optional argument

(the default is index = 0).

#### **Details**

scale

The function calc\_var\_ohlc() calculates the variance from all the different intra-day and day-over-day returns (defined as the differences of *OHLC* prices), using several different variance estimation methods.

The function calc\_var\_ohlc() does not calculate the logarithm of the prices. So if the argument ohlc contains dollar prices then calc\_var\_ohlc() calculates the dollar variance. If the argument ohlc contains the log prices then calc\_var\_ohlc() calculates the percentage variance.

The default method is "yang\_zhang", which theoretically has the lowest standard error among unbiased estimators. The methods "close", "garman\_klass\_yz", and "yang\_zhang" do account for close-to-open price jumps, while the methods "garman\_klass" and "rogers\_satchell" do not account for close-to-open price jumps.

If scale is TRUE (the default), then the returns are divided by the differences of the time index (which scales the variance to the units of variance per second squared). This is useful when calculating the variance from minutely bar data, because dividing returns by the number of seconds decreases the effect of overnight price jumps. If the time index is in days, then the variance is equal to the variance per day squared.

If the number of rows of ohlc is less than 3 then it returns zero.

The optional argument index is the time index of the *time series* ohlc. If the time index is in seconds, then the differences of the index are equal to the number of seconds in each time period. If the time index is in days, then the differences are equal to the number of days in each time period.

The optional argument close\_lag are the lagged *close* prices of the *OHLC time series*. Passing in the lagged *close* prices speeds up the calculation, so it's useful for rolling calculations.

The function calc\_var\_ohlc() is implemented in RcppArmadillo C++ code, and it's over 10 times faster than calc\_var\_ohlc\_r(), which is implemented in R code.

## Value

A single numeric value equal to the variance of the OHLC time series.

```
## Not run:
# Extract the log OHLC prices of SPY
ohlc <- log(HighFreq::SPY)
# Extract the time index of SPY prices
indeks <- c(1, diff(xts::.index(ohlc)))
# Calculate the variance of SPY returns, with scaling of the returns
HighFreq::calc_var_ohlc(ohlc,
method="yang_zhang", scale=TRUE, index=indeks)
# Calculate variance without accounting for overnight jumps
HighFreq::calc_var_ohlc(ohlc,
method="rogers_satchell", scale=TRUE, index=indeks)
# Calculate the variance without scaling the returns</pre>
```

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```
HighFreq::calc_var_ohlc(ohlc, scale=FALSE)
# Calculate the variance by passing in the lagged close prices
close_lag <- HighFreq::lagit(ohlc[, 4])
all.equal(HighFreq::calc_var_ohlc(ohlc),
    HighFreq::calc_var_ohlc(ohlc, close_lag=close_lag))
# Compare with HighFreq::calc_var_ohlc_r()
all.equal(HighFreq::calc_var_ohlc(ohlc, index=indeks),
    HighFreq::calc_var_ohlc_r(ohlc))
# Compare the speed of Rcpp with R code
library(microbenchmark)
summary(microbenchmark(
    Rcpp=HighFreq::calc_var_ohlc(ohlc),
    Rcode=HighFreq::calc_var_ohlc_r(ohlc),
    times=10))[, c(1, 4, 5)] # end microbenchmark summary</pre>
## End(Not run)
```

calc\_var\_ohlc\_ag

Calculate the variance of aggregated OHLC prices using different price range estimators.

## **Description**

Calculate the variance of aggregated *OHLC* prices using different price range estimators.

#### Usage

```
calc_var_ohlc_ag(
  ohlc,
  step = 1L,
  method = "yang_zhang",
  close_lag = 0L,
  scale = TRUE,
  index = 0L
)
```

## **Arguments**

ohlc

A time series or a matrix of OHLC prices.

step

The number of periods in each interval between neighboring end points.

method

A *character* string representing the price range estimator for calculating the variance. The estimators include:

- "close" close-to-close estimator,
- "rogers\_satchell" Rogers-Satchell estimator,
- "garman\_klass" Garman-Klass estimator,
- "garman\_klass\_yz" Garman-Klass with account for close-to-open price jumps,
- "yang\_zhang" Yang-Zhang estimator,

(The default is the method = "yang\_zhang".)

close\_lag

A *vector* with the lagged *close* prices of the *OHLC time series*. This is an optional argument. (The default is  $close_lag = 0$ ).

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scale Boolean argument: Should the returns be divided by the time index, the number

of seconds in each period? (The default is scale = TRUE).

index A vector with the time index of the time series. This is an optional argument

(the default is index = 0).

#### **Details**

The function calc\_var\_ohlc\_ag() calculates the variance of *OHLC* prices aggregated over end points.

It first calculates the end points spaced apart by the number of periods equal to the argument step. Then it aggregates the *OHLC* prices to the end points. Finally it calculates the variance of the aggregated *OHLC* prices.

If there are extra periods that don't fit over the length of ohlc, then calc\_var\_ohlc\_ag() loops over all possible stub intervals, it calculates all the corresponding variance values, and it averages them.

For example, if the number of rows of ohlc is equal to 20, and step=3 then 6 end points fit over the length of ohlc, and there are 2 extra periods that must fit into stubs, either at the beginning or at the end (or both).

The aggregated volatility  $\sigma_t$  scales (increases) with the length of the aggregation interval  $\Delta t$  raised to the power of the *Hurst exponent H*:

$$\sigma_t = \sigma \Delta t^H$$

Where  $\sigma$  is the daily return volatility.

The function calc\_var\_ohlc\_ag() can therefore be used to calculate the *Hurst exponent* from the volatility ratio.

#### Value

The variance of aggregated OHLC prices.

```
## Not run:
# Calculate the log ohlc prices
ohlc <- log(rutils::etfenv$VTI)
# Calculate the daily variance of percentage returns
calc_var_ohlc_ag(ohlc, step=1)
# Calculate the variance of returns aggregated over 21 days
calc_var_ohlc_ag(ohlc, step=21)
# The variance over 21 days is approximately 21 times the daily variance
21*calc_var_ohlc_ag(ohlc, step=1)
## End(Not run)</pre>
```

calc\_var\_ohlc\_r 33

|  | Calculate the variance of an OHLC time series, using different range estimators for variance. |
|--|---|
|--|---|

# **Description**

Calculate the variance of an OHLC time series, using different range estimators for variance.

#### Usage

```
calc_var_ohlc_r(ohlc, method = "yang_zhang", scalit = TRUE)
```

## **Arguments**

ohlc

An *OHLC* time series of prices in xts format.

method

A *character* string representing the method for estimating variance. The methods include:

- "close" close to close,
- "garman\_klass" Garman-Klass,
- "garman\_klass\_yz" Garman-Klass with account for close-to-open price jumps,
- "rogers\_satchell" Rogers-Satchell,
- "yang\_zhang" Yang-Zhang,

(default is "yang\_zhang")

scalit

*Boolean* argument: should the returns be divided by the number of seconds in each period? (default is TRUE)

# Details

The function calc\_var\_ohlc\_r() calculates the variance from all the different intra-day and day-over-day returns (defined as the differences of *OHLC* prices), using several different variance estimation methods.

The default method is "yang\_zhang", which theoretically has the lowest standard error among unbiased estimators. The methods "close", "garman\_klass\_yz", and "yang\_zhang" do account for close-to-open price jumps, while the methods "garman\_klass" and "rogers\_satchell" do not account for close-to-open price jumps.

If scalit is TRUE (the default), then the returns are divided by the differences of the time index (which scales the variance to the units of variance per second squared.) This is useful when calculating the variance from minutely bar data, because dividing returns by the number of seconds decreases the effect of overnight price jumps. If the time index is in days, then the variance is equal to the variance per day squared.

The function  $calc\_var\_ohlc\_r()$  is implemented in R code.

# Value

A single *numeric* value equal to the variance.

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#### **Examples**

```
# Calculate the variance of SPY returns
HighFreq::calc_var_ohlc_r(HighFreq::SPY, method="yang_zhang")
# Calculate variance without accounting for overnight jumps
HighFreq::calc_var_ohlc_r(HighFreq::SPY, method="rogers_satchell")
# Calculate the variance without scaling the returns
HighFreq::calc_var_ohlc_r(HighFreq::SPY, scalit=FALSE)
```

calc\_weights

Calculate the optimal portfolio weights for different types of objective functions.

# **Description**

Calculate the optimal portfolio weights for different types of objective functions.

## Usage

```
calc_weights(
  returns,
  method = "ranksharpe",
  eigen_thresh = 1e-05,
  eigen_max = 0L,
  conf_lev = 0.1,
  alpha = 0,
  scale = TRUE,
  vol_target = 0.01
)
```

# **Arguments**

A time series or a matrix of returns data (the returns in excess of the risk-free returns

A string specifying the method for calculating the weights (see Details) (the method

default is method = "ranksharpe")

eigen\_thresh A numeric threshold level for discarding small singular values in order to regu-

larize the inverse of the returns matrix (the default is 1e-5).

An integer equal to the number of singular values used for calculating the shrinkeigen\_max

age inverse of the returns matrix (the default is 0 - equivalent to eigen\_max

equal to the number of columns of returns).

conf\_lev The confidence level for calculating the quantiles (the default is conf\_lev =

alpha The shrinkage intensity between 0 and 1. (the default is 0).

scale A Boolean specifying whether the weights should be scaled (the default is scale

A *numeric* volatility target for scaling the weights (the default is 0.001) vol\_target

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#### **Details**

The function calc\_weights() calculates the optimal portfolio weights for different types of methods, using RcppArmadillo C++ code.

If method = "ranksharpe" (the default) then it calculates the weights as the ranks (order index) of the trailing Sharpe ratios of the asset returns.

If method = "rank" then it calculates the weights as the ranks (order index) of the last row of the returns.

If method = "max\_sharpe" then calc\_weights() calculates the weights of the maximum Sharpe portfolio, by multiplying the inverse of the covariance *matrix* times the mean column returns.

If method = "min\_var" then it calculates the weights of the minimum variance portfolio under linear constraints.

If method = "min\_varpca" then it calculates the weights of the minimum variance portfolio under quadratic constraints (which is the highest order principal component).

If scale = TRUE (the default) then the weights are scaled so that the resulting portfolio has a volatility equal to vol\_target.

calc\_weights() calculates the shrinkage inverse of the covariance *matrix* of returns from its eigen decomposition. It applies dimension regularization by selecting only the largest eigenvalues equal in number to eigen\_max.

In addition, calc\_weights() applies shrinkage to the columns of returns, by shrinking their means to their common mean value. The shrinkage intensity alpha determines the amount of shrinkage that is applied, with alpha = 0 representing no shrinkage (with the column means of returns unchanged), and alpha = 1 representing complete shrinkage (with the column means of returns all equal to the single mean of all the columns).

## Value

A column *vector* of the same length as the number of columns of returns.

```
## Not run:
# Calculate covariance matrix of ETF returns
returns <- na.omit(rutils::etfenv$returns[, 1:16])</pre>
eigend <- eigen(cov(returns))</pre>
# Calculate shrinkage inverse of covariance matrix
eigen_max <- 3
eigenvec <- eigend$vectors[, 1:eigen_max]</pre>
eigenval <- eigend$values[1:eigen_max]</pre>
inverse <- eigenvec %*% (t(eigenvec) / eigenval)</pre>
# Define shrinkage intensity and apply shrinkage to the mean returns
alpha <- 0.5
colmeans <- colMeans(returns)</pre>
colmeans <- ((1-alpha)*colmeans + alpha*mean(colmeans))</pre>
# Calculate weights using R
weights <- inverse %*% colmeans</pre>
n_col <- NCOL(returns)</pre>
weightsr <- weightsr*sd(returns %*% rep(1/n_col, n_col))/sd(returns %*% weightsr)</pre>
# Calculate weights using RcppArmadillo
weights <- drop(HighFreq::calc_weights(returns, eigen_max, alpha=alpha))</pre>
all.equal(weights, weightsr)
## End(Not run)
```

36 diffit

| diffit | Calculate the row differences of a time series or a matrix using Rcp-pArmadillo. |
|--------|--|
|        |  |

# Description

Calculate the row differences of a time series or a matrix using RcppArmadillo.

## Usage

```
diffit(tseries, lagg = 1L, pad_zeros = TRUE)
```

# Arguments

tseries A time series or a matrix.

lagg An *integer* equal to the number of rows (time periods) to lag when calculating

the differences (the default is lagg = 1).

pad\_zeros Boolean argument: Should the output matrix be padded (extended) with zeros,

in order to return a matrix with the same number of rows as the input? (the

default is pad\_zeros = TRUE)

## **Details**

The function diffit() calculates the differences between the rows of the input *matrix* tseries and its lagged version.

The argument lagg specifies the number of lags applied to the rows of the lagged version of tseries. For positive lagg values, the lagged version of tseries has its rows shifted *forward* (down) by the number equal to lagg rows. For negative lagg values, the lagged version of tseries has its rows shifted *backward* (up) by the number equal to -lagg rows. For example, if lagg=3 then the lagged version will have its rows shifted down by 3 rows, and the differences will be taken between each row minus the row three time periods before it (in the past). The default is lagg = 1.

The argument pad\_zeros specifies whether the output *matrix* should be padded (extended) with the rows of the initial (warmup) period at the front, in order to return a *matrix* with the same number of rows as the input tseries. The default is pad\_zeros = TRUE. The padding operation can be time-consuming, because it requires the copying of data.

The function diffit() is implemented in RcppArmadillo C++ code, which makes it much faster than R code.

#### Value

A matrix containing the differences between the rows of the input matrix tseries.

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#### **Examples**

```
## Not run:
# Create a matrix of random data
datav <- matrix(sample(15), nc=3)</pre>
# Calculate differences with lagged rows
HighFreq::diffit(datav, lagg=2)
# Calculate differences with advanced rows
HighFreq::diffit(datav, lagg=-2)
# Compare HighFreq::diffit() with rutils::diffit()
all.equal(HighFreq::diffit(datav, lagg=2),
  rutils::diffit(datav, lagg=2),
  check.attributes=FALSE)
# Compare the speed of RcppArmadillo with R code
library(microbenchmark)
summary(microbenchmark(
  Rcpp=HighFreq::diffit(datav, lagg=2),
  Rcode=rutils::diffit(datav, lagg=2),
  times=10))[, c(1, 4, 5)] # end microbenchmark summary
## End(Not run)
```

diff\_vec

Calculate the differences between the neighboring elements of a single-column time series or a vector.

# Description

Calculate the differences between the neighboring elements of a single-column *time series* or a *vector*.

# Usage

```
diff_vec(tseries, lagg = 1L, pad_zeros = TRUE)
```

# **Arguments**

tseries A single-column *time series* or a *vector*.

lagg An *integer* equal to the number of time periods to lag when calculating the dif-

ferences (the default is lagg = 1).

pad\_zeros Boolean argument: Should the output vector be padded (extended) with ze-

ros, in order to return a vector of the same length as the input? (the default is

pad\_zeros = TRUE)

### **Details**

The function diff\_vec() calculates the differences between the input *time series* or *vector* and its lagged version.

The argument lagg specifies the number of lags. For example, if lagg=3 then the differences will be taken between each element minus the element three time periods before it (in the past). The default is lagg = 1.

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The argument pad\_zeros specifies whether the output *vector* should be padded (extended) with zeros at the front, in order to return a *vector* of the same length as the input. The default is pad\_zeros = TRUE. The padding operation can be time-consuming, because it requires the copying of data.

The function diff\_vec() is implemented in RcppArmadillo C++ code, which makes it several times faster than R code.

#### Value

A column *vector* containing the differences between the elements of the input vector.

## **Examples**

```
## Not run:
# Create a vector of random returns
returns <- rnorm(1e6)
# Compare diff_vec() with rutils::diffit()
all.equal(drop(HighFreq::diff_vec(returns, lagg=3, pad=TRUE)),
    rutils::diffit(returns, lagg=3))
# Compare the speed of RcppArmadillo with R code
library(microbenchmark)
summary(microbenchmark(
    Rcpp=HighFreq::diff_vec(returns, lagg=3, pad=TRUE),
    Rcode=rutils::diffit(returns, lagg=3),
    times=10))[, c(1, 4, 5)] # end microbenchmark summary
## End(Not run)</pre>
```

hf\_data

High frequency data sets

# **Description**

hf\_data.RData is a file containing the datasets:

**SPY** an xts time series containing 1-minute OHLC bar data for the SPY etf, from 2008-01-02 to 2014-05-19. SPY contains 625,425 rows of data, each row contains a single minute bar.

TLT an xts time series containing 1-minute OHLC bar data for the TLT etf, up to 2014-05-19.

VXX an xts time series containing 1-minute OHLC bar data for the VXX etf, up to 2014-05-19.

# Usage

```
data(hf_data) # not required - data is lazy load
```

### **Format**

Each xts time series contains OHLC data, with each row containing a single minute bar:

**Open** Open price in the bar

**High** High price in the bar

**Low** Low price in the bar

Close Close price in the bar

Volume trading volume in the bar

lagit 39

#### Source

```
https://wrds-web.wharton.upenn.edu/wrds/
```

#### References

Wharton Research Data Service (WRDS)

### **Examples**

```
# data(hf_data) # not required - data is lazy load
head(SPY)
chart_Series(x=SPY["2009"])
```

lagit

Apply a lag to the rows of a time series or a matrix using RcppArmadillo.

### **Description**

Apply a lag to the rows of a time series or a matrix using RcppArmadillo.

### Usage

```
lagit(tseries, lagg = 1L, pad_zeros = TRUE)
```

# **Arguments**

tseries A time series or a matrix.

lagg An *integer* equal to the number of periods to lag (the default is lagg = 1).

pad\_zeros Boolean argument: Should the output be padded with zeros? (The default is

pad\_zeros = TRUE.)

# **Details**

The function lagit() applies a lag to the input *matrix* by shifting its rows by the number equal to the argument lagg. For positive lagg values, the rows are shifted *forward* (down), and for negative lagg values they are shifted *backward* (up).

The output *matrix* is padded with either zeros (the default), or with rows of data from tseries, so that it has the same dimensions as tseries. If the lagg is positive, then the first row is copied and added upfront. If the lagg is negative, then the last row is copied and added to the end.

As a rule, if tseries contains returns data, then the output *matrix* should be padded with zeros, to avoid data snooping. If tseries contains prices, then the output *matrix* should be padded with the prices.

# Value

A *matrix* with the same dimensions as the input argument tseries.

40 lag\_vec

#### **Examples**

```
## Not run:
# Create a matrix of random returns
returns <- matrix(rnorm(5e6), nc=5)
# Compare lagit() with rutils::lagit()
all.equal(HighFreq::lagit(returns), rutils::lagit(returns))
# Compare the speed of RcppArmadillo with R code
library(microbenchmark)
summary(microbenchmark(
   Rcpp=HighFreq::lagit(returns),
   Rcode=rutils::lagit(returns),
   times=10))[, c(1, 4, 5)] # end microbenchmark summary
## End(Not run)</pre>
```

lag\_vec

Apply a lag to a single-column time series or a vector using RcppArmadillo.

# **Description**

Apply a lag to a single-column time series or a vector using RcppArmadillo.

#### **Usage**

```
lag_vec(tseries, lagg = 1L, pad_zeros = TRUE)
```

# Arguments

tseries A single-column *time series* or a *vector*.

lagg An *integer* equal to the number of periods to lag. (The default is lagg = 1.)

pad\_zeros Boolean argument: Should the output be padded with zeros? (The default is

pad\_zeros = TRUE.)

## **Details**

The function lag\_vec() applies a lag to the input *time series* tseries by shifting its elements by the number equal to the argument lagg. For positive lagg values, the elements are shifted forward in time (down), and for negative lagg values they are shifted backward (up).

The output *vector* is padded with either zeros (the default), or with data from tseries, so that it has the same number of element as tseries. If the lagg is positive, then the first element is copied and added upfront. If the lagg is negative, then the last element is copied and added to the end.

As a rule, if tseries contains returns data, then the output *matrix* should be padded with zeros, to avoid data snooping. If tseries contains prices, then the output *matrix* should be padded with the prices.

# Value

A column *vector* with the same number of elements as the input time series.

lik\_garch 41

#### **Examples**

```
## Not run:
# Create a vector of random returns
returns <- rnorm(1e6)
# Compare lag_vec() with rutils::lagit()
all.equal(drop(HighFreq::lag_vec(returns)),
    rutils::lagit(returns))
# Compare the speed of RcppArmadillo with R code
library(microbenchmark)
summary(microbenchmark(
    Rcpp=HighFreq::lag_vec(returns),
    Rcode=rutils::lagit(returns),
    times=10))[, c(1, 4, 5)] # end microbenchmark summary
## End(Not run)</pre>
```

lik\_garch

Calculate the log-likelihood of a time series of returns assuming a GARCH(1,1) process.

### **Description**

Calculate the log-likelihood of a time series of returns assuming a GARCH(1,1) process.

#### **Usage**

lik\_garch(omega, alpha, beta, returns, minval = 1e-06)

## **Arguments**

omega Parameter proportional to the long-term average level of variance.

The weight associated with recent realized variance updates.

The weight associated with the past variance estimates.

The weight associated with the past variance estimates.

A single-column matrix of returns.

The floor value applied to the variance, to avoid zero values. (The default is minval = 0.000001.)

# **Details**

The function lik\_garch() calculates the log-likelihood of a time series of returns assuming a GARCH(1,1) process.

It first estimates the rolling variance of the returns argument using function sim\_garch():

$$\sigma_i^2 = \omega + \alpha r_i^2 + \beta \sigma_{i-1}^2$$

Where  $r_i$  is the time series of returns, and  $\sigma_i^2$  is the estimated rolling variance. And  $\omega$ ,  $\alpha$ , and  $\beta$  are the *GARCH* parameters. It applies the floor value minval to the variance, to avoid zero values. So the minimum value of the variance is equal to minval.

The function lik\_garch() calculates the log-likelihood assuming a normal distribution of returns conditional on the variance  $\sigma_{i-1}^2$  in the previous period, as follows:

$$likelihood = -\sum_{i=1}^n (\frac{r_i^2}{\sigma_{i-1}^2} + \log(\sigma_{i-1}^2))$$

42 mult\_vec\_mat

#### Value

The log-likelihood value.

#### **Examples**

```
## Not run:
# Define the GARCH model parameters
alpha <- 0.79
betav <- 0.2
om_ega <- 1e-4*(1-alpha-betav)
# Calculate historical VTI returns
returns <- na.omit(rutils::etfenv$returns$VTI)
# Calculate the log-likelihood of VTI returns assuming GARCH(1,1)
HighFreq::lik_garch(omega=om_ega, alpha=alpha, beta=betav, returns=returns)
## End(Not run)</pre>
```

mult\_vec\_mat

Multiply in place (without copying) the columns or rows of a matrix times a vector, element-wise.

# Description

Multiply in place (without copying) the columns or rows of a matrix times a vector, element-wise.

### Usage

```
mult_vec_mat(vector, matrix, by_col = TRUE)
```

# **Arguments**

vector A vector.
matrix A matrix.

by\_col A Boolean argument: if TRUE then multiply the columns, otherwise multiply the

rows (the default is by\_col = TRUE.)

# **Details**

The function mult\_vec\_mat() multiplies the columns or rows of a *matrix* times a *vector*, elementwise.

If the number of *vector* elements is equal to the number of matrix columns, then it multiplies the columns by the *vector*, and returns the number of columns. If the number of *vector* elements is equal to the number of rows, then it multiplies the rows, and returns the number of rows.

If the *matrix* is square and if by\_col is TRUE then it multiplies the columns, otherwise it multiplies the rows.

It accepts *pointers* to the *matrix* and *vector*, and replaces the old *matrix* values with the new values. It performs the calculation in place, without copying the *matrix* in memory (which greatly increases the computation speed). It performs an implicit loop over the *matrix* rows and columns using the *Armadillo* operators each\_row() and each\_col(), instead of performing explicit for() loops (both methods are equally fast).

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The function mult\_vec\_mat() uses RcppArmadillo C++ code, so when multiplying large *matrix* columns it's several times faster than vectorized R code, and it's even much faster compared to R when multiplying the *matrix* rows.

#### Value

A single *integer* value, equal to either the number of *matrix* columns or the number of rows.

### **Examples**

```
## Not run:
\# Multiply matrix columns using R
matrixv <- matrix(round(runif(25e4), 2), nc=5e2)</pre>
vectorv <- round(runif(5e2), 2)</pre>
prod_uct <- vectorv*matrixv</pre>
# Multiply the matrix in place
HighFreq::mult_vec_mat(vectorv, matrixv)
all.equal(prod_uct, matrixv)
# Compare the speed of Rcpp with R code
library(microbenchmark)
summary(microbenchmark(
    Rcpp=HighFreq::mult_vec_mat(vectorv, matrixv),
    Rcode=vectorv*matrixv,
    times=10))[, c(1, 4, 5)] # end microbenchmark summary
# Multiply matrix rows using R
matrixv <- matrix(round(runif(25e4), 2), nc=5e2)</pre>
vectorv <- round(runif(5e2), 2)</pre>
prod_uct <- t(vectorv*t(matrixv))</pre>
# Multiply the matrix in place
HighFreq::mult_vec_mat(vectorv, matrixv, by_col=FALSE)
all.equal(prod_uct, matrixv)
\# Compare the speed of Rcpp with R code
library(microbenchmark)
summary(microbenchmark(
    Rcpp=HighFreq::mult_vec_mat(vectorv, matrixv, by_col=FALSE),
    Rcode=t(vectorv*t(matrixv)),
    times=10))[, c(1, 4, 5)] # end microbenchmark summary
## End(Not run)
```

ohlc\_returns

Calculate single period percentage returns from either TAQ or OHLC prices.

# Description

Calculate single period percentage returns from either TAQ or OHLC prices.

```
ohlc_returns(xtes, lagg = 1, colnum = 4, scalit = TRUE)
```

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#### **Arguments**

| xtes   | An xts time series of either TAQ or OHLC data.  |
|--------|---|
| lagg   | An integer equal to the number of time periods of lag. (default is 1)   |
| colnum | The column number to extract from the <i>OHLC</i> data. (default is 4, or the <i>Close</i> prices column)         |
| scalit | <i>Boolean</i> argument: should the returns be divided by the number of seconds in each period? (default is TRUE) |

#### **Details**

The function ohlc\_returns() calculates the percentage returns for either *TAQ* or *OHLC* data, defined as the difference of log prices. Multi-period returns can be calculated by setting the lag parameter to values greater than 1 (the default).

If scalit is TRUE (the default), then the returns are divided by the differences of the time index (which scales the returns to units of returns per second.)

The time index of the xtes time series is assumed to be in *POSIXct* format, so that its internal value is equal to the number of seconds that have elapsed since the *epoch*.

If scalit is TRUE (the default), then the returns are expressed in the scale of the time index of the xtes time series. For example, if the time index is in seconds, then the returns are given in units of returns per second. If the time index is in days, then the returns are equal to the returns per day.

The function ohlc\_returns() identifies the xtes time series as *TAQ* data when it has six columns, otherwise assumes it's *OHLC* data. By default, for *OHLC* data, it differences the *Close* prices, but can also difference other prices depending on the value of colnum.

### Value

A single-column xts time series of returns.

# **Examples**

```
# Calculate secondly returns from TAQ data
returns <- HighFreq::ohlc_returns(xtes=HighFreq::SPY_TAQ)
# Calculate close to close returns
returns <- HighFreq::ohlc_returns(xtes=HighFreq::SPY)
# Calculate open to open returns
returns <- HighFreq::ohlc_returns(xtes=HighFreq::SPY, colnum=1)</pre>
```

ohlc\_sharpe Calculate time series of point Sharpe-like statistics for each row of a OHLC time series.

# Description

Calculate time series of point Sharpe-like statistics for each row of a *OHLC* time series.

```
ohlc_sharpe(ohlc, method = "close")
```

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### **Arguments**

ohlc An *OHLC* time series of prices in *xts* format.

method A *character* string representing method for estimating the Sharpe-like exponent.

#### **Details**

The function ohlc\_sharpe() calculates Sharpe-like statistics for each row of a *OHLC* time series. The Sharpe-like statistic is defined as the ratio of the difference between *Close* minus *Open* prices divided by the difference between *High* minus *Low* prices. This statistic may also be interpreted as something like a *Hurst exponent* for a single row of data. The motivation for the Sharpe-like statistic is the notion that if prices are trending in the same direction inside a given time bar of data, then this statistic is close to either 1 or -1.

### Value

An xts time series with the same number of rows as the argument ohlc.

### **Examples**

```
# Calculate time series of running Sharpe ratios for SPY
sharpe_running <- ohlc_sharpe(HighFreq::SPY)</pre>
```

ohlc\_skew Calculate time series of point skew estimates from a OHLC time series, assuming zero drift.

#### **Description**

Calculate time series of point skew estimates from a OHLC time series, assuming zero drift.

# Usage

```
ohlc_skew(ohlc, method = "rogers_satchell")
```

# Arguments

ohlc An *OHLC* time series of prices in *xts* format.

method A *character* string representing method for estimating skew.

#### Details

The function ohlc\_skew() calculates a time series of skew estimates from *OHLC* prices, one for each row of *OHLC* data. The skew estimates are expressed in the time scale of the index of the *OHLC* time series. For example, if the time index is in seconds, then the skew is given in units of skew per second. If the time index is in days, then the skew is equal to the skew per day.

Currently only the "close" skew estimation method is correct (assuming zero drift), while the "rogers\_satchell" method produces a skew-like indicator, proportional to the skew. The default method is "rogers\_satchell".

### Value

A time series of point skew estimates.

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## **Examples**

```
# Calculate time series of skew estimates for SPY
skew <- HighFreq::ohlc_skew(HighFreq::SPY)</pre>
```

ohlc\_variance

Calculate a time series of point estimates of variance for an OHLC time series, using different range estimators for variance.

### **Description**

Calculates the point variance estimates from individual rows of *OHLC* prices (rows of data), using the squared differences of *OHLC* prices at each point in time, without averaging them over time.

### Usage

```
ohlc_variance(ohlc, method = "yang_zhang", scalit = TRUE)
```

# **Arguments**

ohlc

An *OHLC* time series of prices in *xts* format.

method

A *character* string representing the method for estimating variance. The methods include:

- "close" close to close,
- "garman\_klass" Garman-Klass,
- "garman\_klass\_yz" Garman-Klass with account for close-to-open price jumps,
- "rogers\_satchell" Rogers-Satchell,
- "yang\_zhang" Yang-Zhang,

(default is "yang\_zhang")

scalit

*Boolean* argument: should the returns be divided by the number of seconds in each period? (default is TRUE)

# Details

The function ohlc\_variance() calculates a time series of point variance estimates of percentage returns, from *OHLC* prices, without averaging them over time. For example, the method "close" simply calculates the squares of the differences of the log *Close* prices.

The other methods calculate the squares of other possible differences of the log *OHLC* prices. This way the point variance estimates only depend on the price differences within individual rows of data (and possibly from the neighboring rows.) All the methods are implemented assuming zero drift, since the calculations are performed only for a single row of data, at a single point in time.

The user can choose from several different variance estimation methods. The methods "close", "garman\_klass\_yz", and "yang\_zhang" do account for close-to-open price jumps, while the methods "garman\_klass" and "rogers\_satchell" do not account for close-to-open price jumps. The default method is "yang\_zhang", which theoretically has the lowest standard error among unbiased estimators.

The point variance estimates can be passed into function roll\_vwap() to perform averaging, to calculate rolling variance estimates. This is appropriate only for the methods "garman\_klass" and

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"rogers\_satchell", since they don't require subtracting the rolling mean from the point variance estimates.

The point variance estimates can also be considered to be technical indicators, and can be used as inputs into trading models.

If scalit is TRUE (the default), then the variance is divided by the squared differences of the time index (which scales the variance to units of variance per second squared.) This is useful for example, when calculating intra-day variance from minutely bar data, because dividing returns by the number of seconds decreases the effect of overnight price jumps.

If scalit is TRUE (the default), then the variance is expressed in the scale of the time index of the *OHLC* time series. For example, if the time index is in seconds, then the variance is given in units of variance per second squared. If the time index is in days, then the variance is equal to the variance per day squared.

The time index of the ohlc time series is assumed to be in *POSIXct* format, so that its internal value is equal to the number of seconds that have elapsed since the *epoch*.

The function ohlc\_variance() performs similar calculations to the function volatility() from package TTR, but it assumes zero drift, and doesn't calculate a running sum using runSum(). It's also a little faster because it performs less data validation.

### Value

An xts time series with a single column and the same number of rows as the argument ohlc.

### **Examples**

```
# Create minutely OHLC time series of random prices
ohlc <- HighFreq::random_ohlc()
# Calculate variance estimates for ohlc
var_running <- HighFreq::ohlc_variance(ohlc)
# Calculate variance estimates for SPY
var_running <- HighFreq::ohlc_variance(HighFreq::SPY, method="yang_zhang")
# Calculate SPY variance without overnight jumps
var_running <- HighFreq::ohlc_variance(HighFreq::SPY, method="rogers_satchell")</pre>
```

random\_ohlc

Calculate a random OHLC time series of prices and trading volumes, in xts format.

#### **Description**

Calculate a random *OHLC* time series either by simulating random prices following geometric Brownian motion, or by randomly sampling from an input time series.

```
random_ohlc(
  ohlc = NULL,
  reducit = TRUE,
  volat = 6.5e-05,
  drift = 0,
  indeks = seq(from = as.POSIXct(paste(Sys.Date() - 3, "09:30:00")), to =
```

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```
as.POSIXct(paste(Sys.Date() - 1, "16:00:00")), by = "1 sec"),
...
)
```

### **Arguments**

| ohlc    | An $OHLC$ time series of prices and trading volumes, in $xts$ format (default is $NULL$ ).                           |
|---------|--|
| volat   | The volatility per period of the indeks time index (default is $6.5e-05$ per second, or about $0.01=1.0\%$ per day). |
| drift   | The drift per period of the indeks time index (default is 0.0).  |
| indeks  | The time index for the <i>OHLC</i> time series.  |
| reducit | Boolean argument: should ohlc time series be transformed to reduced form? (default is TRUE)                          |

### **Details**

If the input ohlc time series is *NULL* (the default), then the function random\_ohlc() simulates a minutely *OHLC* time series of random prices following geometric Brownian motion, over the two previous calendar days.

If the input ohlc time series is not *NULL*, then the rows of ohlc are randomly sampled, to produce a random time series.

If reducit is TRUE (the default), then the ohlc time series is first transformed to reduced form, then randomly sampled, and finally converted to standard form.

Note: randomly sampling from an intraday time series over multiple days will cause the overnight price jumps to be re-arranged into intraday price jumps. This will cause moment estimates to become inflated compared to the original time series.

## Value

An xts time series with the same dimensions and the same time index as the input ohlc time series.

# **Examples**

```
# Create minutely synthetic OHLC time series of random prices
ohlc <- HighFreq::random_ohlc()
# Create random time series from SPY by randomly sampling it
ohlc <- HighFreq::random_ohlc(ohlc=HighFreq::SPY["2012-02-13/2012-02-15"])</pre>
```

| random_tag   | Calculate a random TAQ time series of prices and trading volumes, in  |
|--------------|---|
| r arraom_taq | calculate a random 11 Q time series of prices and trading volumes, in |
|              | xts format.   |

# Description

Calculate a *TAQ* time series of random prices following geometric Brownian motion, combined with random trading volumes.

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#### Usage

```
random_taq(
  volat = 6.5e-05,
  drift = 0,
  indeks = seq(from = as.POSIXct(paste(Sys.Date() - 3, "09:30:00")), to =
    as.POSIXct(paste(Sys.Date() - 1, "16:00:00")), by = "1 sec"),
  bid_offer = 0.001,
  ...
)
```

### **Arguments**

bid\_offer

The bid-offer spread expressed as a fraction of the prices (default is 0.001=10bps).

The volatility per period of the indeks time index (default is 6.5e-05 per second, or about 0.01=1.0% per day).

The drift per period of the indeks time index (default is 0.0).

The time index for the TAQ time series.

### **Details**

The function random\_taq() calculates an *xts* time series with four columns containing random prices following geometric Brownian motion: the bid, ask, and trade prices, combined with random trade volume data. If indeks isn't supplied as an argument, then by default it's equal to the secondly index over the two previous calendar days.

#### Value

An *xts* time series, with time index equal to the input indeks time index, and with four columns containing the bid, ask, and trade prices, and the trade volume.

## **Examples**

```
# Create secondly TAQ time series of random prices
taq <- HighFreq::random_taq()
# Create random TAQ time series from SPY index
taq <- HighFreq::random_taq(indeks=index(HighFreq::SPY["2012-02-13/2012-02-15"]))</pre>
```

remove\_jumps Remove overnight close-to-open price jumps from an OHLC time series, by adding adjustment terms to its prices.

### **Description**

Remove overnight close-to-open price jumps from an *OHLC* time series, by adding adjustment terms to its prices.

```
remove_jumps(ohlc)
```

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## **Arguments**

ohlc

An OHLC time series of prices and trading volumes, in xts format.

### **Details**

The function remove\_jumps() removes the overnight close-to-open price jumps from an *OHLC* time series, by adjusting its prices so that the first *Open* price of the day is equal to the last *Close* price of the previous day.

The function remove\_jumps() adds adjustment terms to all the *OHLC* prices, so that intra-day returns and volatilities are not affected.

The function remove\_jumps() identifies overnight periods as those that are greater than 60 seconds. This assumes that intra-day periods between neighboring rows of data are 60 seconds or less.

The time index of the ohlc time series is assumed to be in *POSIXct* format, so that its internal value is equal to the number of seconds that have elapsed since the *epoch*.

#### Value

An *OHLC* time series with the same dimensions and the same time index as the input ohlc time series.

# **Examples**

```
# Remove overnight close-to-open price jumps from SPY data
ohlc <- remove_jumps(HighFreq::SPY)</pre>
```

roll\_apply

Apply an aggregation function over a rolling look-back interval and the end points of an OHLC time series, using R code.

# Description

Apply an aggregation function over a rolling look-back interval and the end points of an *OHLC* time series, using R code.

```
roll_apply(
   xtes,
   agg_fun,
   look_back = 2,
   endpoints = seq_along(xtes),
   by_columns = FALSE,
   out_xts = TRUE,
   ...
)
```

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#### **Arguments**

| • • •      | additional parameters to the function agg_fun.  |
|------------|---|
| xtes       | An OHLC time series of prices and trading volumes, in xts format.   |
| agg_fun    | The name of the aggregation function to be applied over a rolling look-back interval.   |
| look_back  | The number of end points in the look-back interval used for applying the aggregation function (including the current row).  |
| by_columns | Boolean argument: should the function $agg\_fun()$ be applied column-wise (individually), or should it be applied to all the columns combined? (default is FALSE) |
| out_xts    | Boolean argument: should the output be coerced into an $xts$ series? (default is TRUE)  |
| endpoints  | An integer vector of end points.  |

#### **Details**

The function roll\_apply() applies an aggregation function over a rolling look-back interval attached at the end points of an *OHLC* time series.

The function roll\_apply() is implemented in R code.

HighFreq::roll\_apply() performs similar operations to the functions rollapply() and period.apply() from package xts, and also the function apply.rolling() from package PerformanceAnalytics. (The function rollapply() isn't exported from the package xts.)

But HighFreq::roll\_apply() is faster because it performs less type-checking and skips other overhead. Unlike the other functions, roll\_apply() doesn't produce any leading *NA* values.

The function roll\_apply() can be called in two different ways, depending on the argument endpoints. If the argument endpoints isn't explicitly passed to roll\_apply(), then the default value is used, and roll\_apply() performs aggregations over overlapping intervals at each point in time.

If the argument endpoints is explicitly passed to roll\_apply(), then roll\_apply() performs aggregations over intervals attached at the endpoints. If look\_back=2 then the aggregations are performed over non-overlapping intervals, otherwise they are performed over overlapping intervals.

If the argument out\_xts is TRUE (the default) then the output is coerced into an *xts* series, with the number of rows equal to the length of argument endpoints. Otherwise a list is returned, with the length equal to the length of argument endpoints.

If out\_xts is TRUE and the aggregation function agg\_fun() returns a single value, then roll\_apply() returns an xts time series with a single column. If out\_xts is TRUE and if agg\_fun() returns a vector of values, then roll\_apply() returns an xts time series with multiple columns, equal to the length of the vector returned by the aggregation function agg\_fun().

## Value

Either an *xts* time series with the number of rows equal to the length of argument endpoints, or a list the length of argument endpoints.

### **Examples**

```
# extract a single day of SPY data
ohlc <- HighFreq::SPY["2012-02-13"]
interval <- 11  # number of data points between end points
look_back <- 4  # number of end points in look-back interval</pre>
```

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roll\_backtest

Perform a backtest simulation of a trading strategy (model) over a vector of end points along a time series of prices.

# **Description**

Perform a backtest simulation of a trading strategy (model) over a vector of end points along a time series of prices.

# Usage

```
roll_backtest(
   xtes,
   train_func,
   trade_func,
   look_back = look_forward,
   look_forward,
   endpoints = rutils::calc_endpoints(xtes, look_forward),
   ...
)
```

## **Arguments**

|              | additional parameters to the functions train_func() and trade_func().   |
|--------------|---|
| xtes         | A time series of prices, asset returns, trading volumes, and other data, in <i>xts</i> format.                            |
| train_func   | The name of the function for training (calibrating) a forecasting model, to be applied over a rolling look-back interval. |
| trade_func   | The name of the trading model function, to be applied over a rolling look-forward interval.                               |
| look_back    | The size of the look-back interval, equal to the number of rows of data used for training the forecasting model.          |
| look_forward | The size of the look-forward interval, equal to the number of rows of data used for trading the strategy.                 |
| endpoints    | A vector of end points along the rows of the xtes time series, given as either integers or dates.                         |

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#### **Details**

The function roll\_backtest() performs a rolling backtest simulation of a trading strategy over a vector of end points. At each end point, it trains (calibrates) a forecasting model using past data taken from the xtes time series over the look-back interval, and applies the forecasts to the trade\_func() trading model, using out-of-sample future data from the look-forward interval.

The function trade\_func() should simulate the trading model, and it should return a named list with at least two elements: a named vector of performance statistics, and an xts time series of out-of-sample returns. The list returned by trade\_func() can also have additional elements, like the in-sample calibrated model statistics, etc.

The function roll\_backtest() returns a named list containing the listv returned by function trade\_func(). The list names are equal to the *endpoints* dates. The number of list elements is equal to the number of *endpoints* minus two (because the first and last end points can't be included in the backtest).

#### Value

An xts time series with the number of rows equal to the number of end points minus two.

### **Examples**

```
## Not run:
# Combine two time series of prices
prices <- cbind(rutils::etfenv$XLU, rutils::etfenv$XLP)</pre>
look_back <- 252
look_forward <- 22</pre>
# Define end points
endpoints <- rutils::calc_endpoints(prices, look_forward)</pre>
# Perform back-test
back_test <- roll_backtest(endpoints=endpoints,</pre>
    look_forward=look_forward,
    look_back=look_back,
    train_func = train_model,
    trade_func = trade_model,
    model_params = model_params,
    trading_params = trading_params,
    xtes=prices)
## End(Not run)
```

roll\_conv

Calculate the rolling convolutions (weighted sums) of a time series with a single-column matrix of weights.

### **Description**

Calculate the rolling convolutions (weighted sums) of a *time series* with a single-column *matrix* of weights.

```
roll_conv(tseries, weights)
```

54 roll\_count

#### **Arguments**

tseries A *time series* or a *matrix* of data.

weights A single-column *matrix* of weights.

#### **Details**

The function roll\_conv() calculates the convolutions of the *matrix* columns with a single-column *matrix* of weights. It performs a loop over the *matrix* rows and multiplies the past (higher) values by the weights. It calculates the rolling weighted sums of the past values.

The function roll\_conv() uses the RcppArmadillo function arma::conv2(). It performs a similar calculation to the standard R function

filter(x=tseries, filter=weights, method="convolution", sides=1), but it's over 6 times faster, and it doesn't produce any leading NA values.

### Value

A *matrix* with the same dimensions as the input argument tseries.

### **Examples**

```
## Not run:
# First example
# Calculate a time series of returns
returns <- na.omit(rutils::etfenv$returns[, c("IEF", "VTI")])</pre>
# Create simple weights equal to a 1 value plus zeros
weights \leftarrow matrix(c(1, rep(0, 10)), nc=1)
# Calculate rolling weighted sums
weighted <- HighFreq::roll_conv(returns, weights)</pre>
# Compare with original
all.equal(coredata(returns), weighted, check.attributes=FALSE)
# Second example
# Calculate exponentially decaying weights
weights <- \exp(-0.2*(1:11))
weights <- matrix(weights/sum(weights), nc=1)</pre>
# Calculate rolling weighted sums
weighted <- HighFreq::roll_conv(returns, weights)</pre>
# Calculate rolling weighted sums using filter()
filtered <- filter(x=returns, filter=weights, method="convolution", sides=1)</pre>
# Compare both methods
all.equal(filtered[-(1:11), ], weighted[-(1:11), ], check.attributes=FALSE)
## End(Not run)
```

roll\_count

Count the number of consecutive TRUE elements in a Boolean vector, and reset the count to zero after every FALSE element.

## **Description**

Count the number of consecutive TRUE elements in a Boolean vector, and reset the count to zero after every FALSE element.

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# Usage

```
roll_count(tseries)
```

### **Arguments**

tseries

A Boolean vector of data.

#### Details

The function roll\_count() calculates the number of consecutive TRUE elements in a Boolean vector, and it resets the count to zero after every FALSE element.

For example, the Boolean vector FALSE, TRUE, TRUE, FALSE, FALSE, TRUE, T

### Value

An *integer vector* of the same length as the argument tseries.

# **Examples**

```
## Not run:
# Calculate the number of consecutive TRUE elements
drop(HighFreq::roll_count(c(FALSE, TRUE, TRUE, FALSE, FALSE, TRUE, TR
```

roll\_fun

Calculate a matrix of estimator values over a rolling look-back interval attached at the end points of a time series or a matrix.

# Description

Calculate a *matrix* of estimator values over a rolling look-back interval attached at the end points of a *time series* or a *matrix*.

```
roll_fun(
   tseries,
   fun = "calc_var",
   startp = 0L,
   endp = 0L,
   step = 1L,
   look_back = 1L,
   stub = 0L,
   method = "moment",
   conf_lev = 0.75
)
```

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#### **Arguments**

| tseries   | A time series or a matrix of data.  |
|-----------|---|
| fun       | A <i>string</i> specifying the estimator function (the default is fun = "calc_var".)                              |
| startp    | An <i>integer</i> vector of start points (the default is $startp = 0$ ).  |
| endp      | An <i>integer</i> vector of end points (the default is endp = $\emptyset$ ).                                      |
| step      | The number of time periods between the end points (the default is step = 1).                                      |
| look_back | The number of end points in the look-back interval (the default is look_back = 1).                                |
| stub      | An <i>integer</i> value equal to the first end point for calculating the end points (the default is stub = $0$ ). |
| method    | A <i>string</i> specifying the type of the model for the estimator (the default is $method = "moment"$ .)         |
| conf_lev  | The confidence level for calculating the quantiles (the default is $conf_{lev} = 0.75$ ).                         |

#### **Details**

The function roll\_fun() calculates a *matrix* of estimator values, over rolling look-back intervals attached at the end points of the *time series* tseries.

The function roll\_fun() performs a loop over the end points, and at each end point it subsets the time series tseries over a look-back interval equal to look\_back number of end points.

It passes the subset time series to the function specified by the argument fun, which calculates the statistic. See the functions  $calc_*()$  for a description of the different estimators.

If the arguments endp and startp are not given then it first calculates a vector of end points separated by step time periods. It calculates the end points along the rows of tseries using the function calc\_endpoints(), with the number of time periods between the end points equal to step time periods.

For example, the rolling variance at 25 day end points, with a 75 day look-back, can be calculated using the parameters step = 25 and look\_back = 3.

The function roll\_fun() is implemented in RcppArmadillo C++ code, so it's many times faster than the equivalent R code.

# Value

A *matrix* with the same number of columns as the input time series tseries, and the number of rows equal to the number of end points.

### **Examples**

```
## Not run:
# Define time series of returns using package rutils
returns <- na.omit(rutils::etfenv$returns$VTI)
# Calculate the rolling variance at 25 day end points, with a 75 day look-back
var_rollfun <- HighFreq::roll_fun(returns, fun="calc_var", step=25, look_back=3)
# Calculate the rolling variance using roll_var()
var_roll <- HighFreq::roll_var(returns, step=25, look_back=3)
# Compare the two methods
all.equal(var_rollfun, var_roll, check.attributes=FALSE)
# Define end points and start points</pre>
```

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```
endp <- HighFreq::calc_endpoints(NROW(returns), step=25)</pre>
startp <- HighFreq::calc_startpoints(endp, look_back=3)</pre>
# Calculate the rolling variance using RcppArmadillo
var_rollfun <- HighFreq::roll_fun(returns, fun="calc_var", startp=startp, endp=endp)</pre>
# Calculate the rolling variance using R code
var_roll <- sapply(1:NROW(endp), function(it) {</pre>
  var(returns[startp[it]:endp[it]+1, ])
}) # end sapply
# Compare the two methods
all.equal(drop(var_rollfun), var_roll, check.attributes=FALSE)
# Compare the speed of RcppArmadillo with R code
library(microbenchmark)
summary(microbenchmark(
  Rcpp=HighFreq::roll_fun(returns, fun="calc_var", startp=startp, endp=endp),
  Rcode=sapply(1:NROW(endp), function(it) {
    var(returns[startp[it]:endp[it]+1, ])
  }),
  times=10))[, c(1, 4, 5)] # end microbenchmark summary
## End(Not run)
```

roll\_hurst

Calculate a time series of Hurst exponents over a rolling look-back interval.

### **Description**

Calculate a time series of *Hurst* exponents over a rolling look-back interval.

### Usage

```
roll_hurst(ohlc, look_back = 11)
```

# **Arguments**

ohlc An *OHLC* time series of prices in *xts* format.

look\_back The size of the look-back interval, equal to the number of rows of data used for

aggregating the OHLC prices.

## **Details**

The function roll\_hurst() calculates a time series of *Hurst* exponents from *OHLC* prices, over a rolling look-back interval.

The *Hurst* exponent is defined as the logarithm of the ratio of the price range, divided by the standard deviation of returns, and divided by the logarithm of the interval length.

The function roll\_hurst() doesn't use the same definition as the rescaled range definition of the *Hurst* exponent. First, because the price range is calculated using *High* and *Low* prices, which produces bigger range values, and higher *Hurst* exponent estimates. Second, because the *Hurst* exponent is estimated using a single aggregation interval, instead of multiple intervals in the rescaled range definition.

The rationale for using a different definition of the *Hurst* exponent is that it's designed to be a technical indicator for use as input into trading models, rather than an estimator for statistical analysis.

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### Value

An xts time series with a single column and the same number of rows as the argument ohlc.

# **Examples**

```
# Calculate rolling Hurst for SPY in March 2009
hurst_rolling <- roll_hurst(ohlc=HighFreq::SPY["2009-03"], look_back=11)
chart_Series(hurst_rolling["2009-03-10/2009-03-12"], name="SPY hurst_rolling")</pre>
```

roll\_kurtosis

Calculate a matrix of kurtosis estimates over a rolling look-back interval attached at the end points of a time series or a matrix.

# Description

Calculate a *matrix* of kurtosis estimates over a rolling look-back interval attached at the end points of a *time series* or a *matrix*.

# Usage

```
roll_kurtosis(
  tseries,
  startp = 0L,
  endp = 0L,
  step = 1L,
  look_back = 1L,
  stub = 0L,
  method = "moment",
  conf_lev = 0.75
)
```

# **Arguments**

| tseries   | A time series or a matrix of data.  |
|-----------|---|
| startp    | An <i>integer</i> vector of start points (the default is $startp = 0$ ).  |
| endp      | An <i>integer</i> vector of end points (the default is endp = $\emptyset$ ).                                      |
| step      | The number of time periods between the end points (the default is $step = 1$ ).                                   |
| look_back | The number of end points in the look-back interval (the default is look_back = 1).                                |
| stub      | An <i>integer</i> value equal to the first end point for calculating the end points (the default is stub = $0$ ). |
| method    | A <i>string</i> specifying the type of the kurtosis model (the default is method = "moment" - see Details).       |
| conf_lev  | The confidence level for calculating the quantiles (the default is $conf_{ev} = 0.75$ ).                          |

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#### **Details**

The function roll\_kurtosis() calculates a *matrix* of kurtosis estimates over rolling look-back intervals attached at the end points of the *time series* tseries.

The function roll\_kurtosis() performs a loop over the end points, and at each end point it subsets the time series over a look-back interval equal to look\_back number of end points.

It passes the subset time series to the function calc\_kurtosis(), which calculates the kurtosis. See the function calc\_kurtosis() for a description of the kurtosis methods.

If the arguments endp and startp are not given then it first calculates a vector of end points separated by step time periods. It calculates the end points along the rows of tseries using the function calc\_endpoints(), with the number of time periods between the end points equal to step time periods.

For example, the rolling kurtosis at 25 day end points, with a 75 day look-back, can be calculated using the parameters step = 25 and look\_back = 3.

The function roll\_kurtosis() is implemented in RcppArmadillo C++ code, so it's many times faster than the equivalent R code.

#### Value

A *matrix* of kurtosis estimates with the same number of columns as the input time series tseries, and the number of rows equal to the number of end points.

## **Examples**

```
## Not run:
# Define time series of returns using package rutils
returns <- na.omit(rutils::etfenv$returns$VTI)</pre>
# Define end points and start points
endp <- 1 + HighFreq::calc_endpoints(NROW(returns), step=25)</pre>
startp <- HighFreq::calc_startpoints(endp, look_back=3)</pre>
# Calculate the rolling kurtosis at 25 day end points, with a 75 day look-back
kurto_sis <- HighFreq::roll_kurtosis(returns, step=25, look_back=3)</pre>
# Calculate the rolling kurtosis using R code
kurt_r <- sapply(1:NROW(endp), function(it) {</pre>
 HighFreq::calc_kurtosis(returns[startp[it]:endp[it], ])
}) # end sapply
# Compare the kurtosis estimates
all.equal(drop(kurto_sis), kurt_r, check.attributes=FALSE)
# Compare the speed of RcppArmadillo with R code
library(microbenchmark)
summary(microbenchmark(
  Rcpp=HighFreq::roll_kurtosis(returns, step=25, look_back=3),
  Rcode=sapply(1:NROW(endp), function(it) {
    HighFreq::calc_kurtosis(returns[startp[it]:endp[it], ])
  }),
  times=10))[, c(1, 4, 5)] # end microbenchmark summary
## End(Not run)
```

60 roll\_mean

| roll_mean | Calculate a matrix of mean (location) estimates over a rolling look-<br>back interval attached at the end points of a time series or a matrix. |
|-----------|--|
|           | buck interval attached at the cha points of a time series or a matrix.   |

# **Description**

Calculate a *matrix* of mean (location) estimates over a rolling look-back interval attached at the end points of a *time series* or a *matrix*.

# Usage

```
roll_mean(
   tseries,
   startp = 0L,
   endp = 0L,
   step = 1L,
   look_back = 1L,
   stub = 0L,
   method = "moment",
   conf_lev = 0.75
)
```

# Arguments

| tseries   | A time series or a matrix of data.  |
|-----------|---|
| startp    | An <i>integer</i> vector of start points (the default is $startp = 0$ ).  |
| endp      | An <i>integer</i> vector of end points (the default is endp = $\emptyset$ ).                                      |
| step      | The number of time periods between the end points (the default is step = 1).                                      |
| look_back | The number of end points in the look-back interval (the default is look_back = 1).                                |
| stub      | An <i>integer</i> value equal to the first end point for calculating the end points (the default is $stub = 0$ ). |
| method    | A <i>character</i> string representing the type of mean measure of (the default is method = "moment").            |

# **Details**

The function roll\_mean() calculates a *matrix* of mean (location) estimates over rolling look-back intervals attached at the end points of the *time series* tseries.

The function roll\_mean() performs a loop over the end points, and at each end point it subsets the time series tseries over a look-back interval equal to look\_back number of end points.

It passes the subset time series to the function calc\_mean(), which calculates the mean (location). See the function calc\_mean() for a description of the mean methods.

If the arguments endp and startp are not given then it first calculates a vector of end points separated by step time periods. It calculates the end points along the rows of tseries using the function calc\_endpoints(), with the number of time periods between the end points equal to step time periods.

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For example, the rolling mean at 25 day end points, with a 75 day look-back, can be calculated using the parameters step = 25 and look\_back = 3.

The function roll\_mean() with the parameter step = 1 performs the same calculation as the function roll\_mean() from package RcppRoll, but it's several times faster because it uses RcppArmadillo C++ code.

The function roll\_mean() is implemented in RcppArmadillo C++ code, so it's many times faster than the equivalent R code.

If only a simple rolling mean is required (not the median) then other functions like roll\_sum() or roll\_vec() may be even faster.

#### Value

A *matrix* of mean (location) estimates with the same number of columns as the input time series tseries, and the number of rows equal to the number of end points.

## **Examples**

```
## Not run:
# Define time series of returns using package rutils
returns <- na.omit(rutils::etfenv$returns$VTI)</pre>
# Calculate the rolling means at 25 day end points, with a 75 day look-back
means <- HighFreq::roll_mean(returns, step=25, look_back=3)</pre>
# Compare the mean estimates over 11-period look-back intervals
all.equal(HighFreq::roll_mean(returns, look_back=11)[-(1:10), ],
  drop(RcppRoll::roll_mean(returns, n=11)), check.attributes=FALSE)
# Define end points and start points
endp <- HighFreq::calc_endpoints(NROW(returns), step=25)</pre>
startp <- HighFreq::calc_startpoints(endp, look_back=3)</pre>
# Calculate the rolling means using RcppArmadillo
means <- HighFreq::roll_mean(returns, startp=startp, endp=endp)</pre>
# Calculate the rolling medians using RcppArmadillo
medianscpp <- HighFreq::roll_mean(returns, startp=startp, endp=endp, method="nonparametric")</pre>
# Calculate the rolling medians using R
medians = sapply(1:NROW(endp), function(i) {
  median(returns[startp[i]:endp[i] + 1])
}) # end sapply
all.equal(medians, drop(medianscpp))
# Compare the speed of RcppArmadillo with R code
library(microbenchmark)
summary(microbenchmark(
  Rcpp=HighFreq::roll_mean(returns, startp=startp, endp=endp, method="nonparametric"),
  Rcode=sapply(1:NROW(endp), function(i) {median(returns[startp[i]:endp[i] + 1])}),
  times=10))[, c(1, 4, 5)]
## End(Not run)
```

roll\_ohlc

Aggregate a time series to an OHLC time series with lower periodicity.

## **Description**

Given a time series of prices at a higher periodicity (say seconds), it calculates the *OHLC* prices at a lower periodicity (say minutes).

62 roll\_reg

#### **Usage**

```
roll_ohlc(tseries, endp)
```

## Arguments

tseries A time series or a matrix with multiple columns of data.

endp An integer vector of end points.

#### **Details**

The function roll\_ohlc() performs a loop over the end points *endp*, along the rows of the data tseries. At each end point, it selects the past rows of the data tseries, starting at the first bar after the previous end point, and then calls the function agg\_ohlc() on the selected data tseries to calculate the aggregations.

The function roll\_ohlc() can accept either a single column of data or four columns of *OHLC* data. It can also accept an additional column containing the trading volume.

The function roll\_ohlc() performs a similar aggregation as the function to.period() from package xts.

### Value

A matrix with OHLC data, with the number of rows equal to the number of endp minus one.

# Examples

```
## Not run:
# Define matrix of OHLC data
ohlc <- rutils::etfenv$VTI[, 1:5]
# Define end points at 25 day intervals
endp <- HighFreq::calc_endpoints(NROW(ohlc), step=25)
# Aggregate over endp:
ohlcagg <- HighFreq::roll_ohlc(tseries=ohlc, endp=endp)
# Compare with xts::to.period()
ohlcagg_xts <- .Call("toPeriod", ohlc, as.integer(endp+1), TRUE, NCOL(ohlc), FALSE, FALSE, colnames(ohlc), PAC
all.equal(ohlcagg, coredata(ohlcagg_xts), check.attributes=FALSE)
## End(Not run)</pre>
```

roll\_reg

Calculate a matrix of regression coefficients, their t-values, and z-scores, at the end points of the predictor matrix.

# **Description**

Calculate a *matrix* of regression coefficients, their t-values, and z-scores, at the end points of the predictor matrix.

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# Usage

```
roll_reg(
  response,
  predictor,
  intercept = FALSE,
  startp = 0L,
  endp = 0L,
  step = 1L,
  look_back = 1L,
  stub = 0L,
  method = "least_squares",
  eigen_thresh = 1e-05,
  eigen_max = 0L,
  conf_lev = 0.1,
  alpha = 0
)
```

# Arguments

| response     | A single-column time series or a vector of response data.   |
|--------------|---|
| predictor    | A time series or a matrix of predictor data.  |
| startp       | An <i>integer</i> vector of start points (the default is $startp = 0$ ).  |
| endp         | An <i>integer</i> vector of end points (the default is endp = $\emptyset$ ).  |
| step         | The number of time periods between the end points (the default is step = 1).  |
| look_back    | The number of end points in the look-back interval (the default is look_back = 1).  |
| stub         | An <i>integer</i> value equal to the first end point for calculating the end points (the default is $stub = 0$ ).   |
| intercept    | A <i>Boolean</i> specifying whether an intercept term should be added to the predictor (the default is intercept = FALSE).  |
| method       | A <i>string</i> specifying the type of the regression model the default is method = "least_squares" - see Details).   |
| eigen_thresh | A <i>numeric</i> threshold level for discarding small singular values in order to regularize the inverse of the predictor matrix (the default is 1e-5).   |
| eigen_max    | An <i>integer</i> equal to the number of singular values used for calculating the shrinkage inverse of the predictor matrix (the default is $\emptyset$ - equivalent to eigen_max equal to the number of columns of predictor). |
| conf_lev     | The confidence level for calculating the quantiles (the default is $conf_lev = 0.75$ ).   |
| alpha        | The shrinkage intensity between 0 and 1. (the default is 0).  |
|              |   |

# **Details**

The function roll\_reg() calculates a *matrix* of regression coefficients, their t-values, and z-scores at the end points of the predictor matrix.

The function roll\_reg() performs a loop over the end points, and at each end point it subsets the time series predictor over a look-back interval equal to look\_back number of end points.

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If the arguments endp and startp are not given then it first calculates a vector of end points separated by step time periods. It calculates the end points along the rows of predictor using the function calc\_endpoints(), with the number of time periods between the end points equal to step time periods.

For example, the rolling regression at 25 day end points, with a 75 day look-back, can be calculated using the parameters step = 25 and look\_back = 3.

It passes the subset time series to the function calc\_reg(), which calculates the regression coefficients, their t-values, and the z-score.

If intercept = TRUE then an extra intercept column (unit column) is added to the predictor matrix (the default is intercept = FALSE).

The number of columns of the return matrix depends on the number of columns of the predictor matrix (including the intercept column, if it's added). The number of columns of the return matrix is equal to the number of regression coefficients, plus their t-values, plus the z-score column. The number of regression coefficients is equal to the number of columns of the predictor matrix (including the intercept column, if it's added). The number of t-values is equal to the number of coefficients. For example, if the number of columns of the predictor matrix is equal to n, and if intercept = TRUE, then roll\_reg() returns a matrix with 2n+3 columns: n+1 regression coefficients (including the intercept coefficient), n+1 corresponding t-values, and 1 z-score column.

#### Value

A *matrix* with the regression coefficients, their t-values, and z-scores, and with the same number of rows as predictor a number of columns equal to 2n+3, where n is the number of columns of predictor.

# **Examples**

## End(Not run)

```
## Not run:
# Calculate historical returns
returns <- na.omit(rutils::etfenv$returns[, c("XLP", "VTI")])</pre>
# Define monthly end points and start points
endp <- xts::endpoints(returns, on="months")[-1]</pre>
look_back <- 12
startp <- c(rep(1, look_back), endp[1:(NROW(endp)-look_back)])</pre>
# Calculate rolling betas using RcppArmadillo
reg_stats <- HighFreq::roll_reg(response=returns[, 1], predictor=returns[, 2], endp=(endp-1), startp=(startp-
betas <- reg_stats[, 2]</pre>
# Calculate rolling betas in R
betas_r <- sapply(1:NROW(endp), FUN=function(ep) {</pre>
  datav <- returns[startp[ep]:endp[ep], ]</pre>
  drop(cov(datav[, 1], datav[, 2])/var(datav[, 2]))
}) # end sapply
# Compare the outputs of both functions
all.equal(betas, betas_r, check.attributes=FALSE)
```

roll\_scale 65

| roll_scale | Perform a rolling scaling (standardization) of the columns of a matrix of data using RcppArmadillo. |
|------------|---|
|            |   |

## **Description**

Perform a rolling scaling (standardization) of the columns of a matrix of data using RcppArmadillo.

### Usage

```
roll_scale(matrix, look_back, use_median = FALSE)
```

### Arguments

use\_median A Boolean argument: if TRUE then the centrality (central tendency) is calculated

as the *median* and the dispersion is calculated as the *median absolute deviation* (*MAD*). If use\_median is FALSE then the centrality is calculated as the *mean* and the dispersion is calculated as the *standard deviation* (the default is use\_median

= FALSE)

matrix A matrix of data.

look\_back The length of the look-back interval, equal to the number of rows of data used

in the scaling.

# Details

The function roll\_scale() performs a rolling scaling (standardization) of the columns of the matrix argument using RcppArmadillo. The function roll\_scale() performs a loop over the rows of matrix, subsets a number of previous (past) rows equal to look\_back, and scales the subset matrix. It assigns the last row of the scaled subset *matrix* to the return matrix.

If the argument use\_median is FALSE (the default), then it performs the same calculation as the function roll::roll\_scale(). If the argument use\_median is TRUE, then it calculates the centrality as the *median* and the dispersion as the *median absolute deviation (MAD)*.

# Value

A *matrix* with the same dimensions as the input argument matrix.

# **Examples**

```
## Not run:
matrixv <- matrix(rnorm(20000), nc=2)
look_back <- 11
rolled_scaled <- roll::roll_scale(data=matrixv, width = look_back, min_obs=1)
rolled_scaled2 <- roll_scale(matrix=matrixv, look_back = look_back, use_median=FALSE)
all.equal(rolled_scaled[-1, ], rolled_scaled2[-1, ])
## End(Not run)</pre>
```

66 roll\_skew

| roll_sharpe | Calculate a time series of Sharpe ratios over a rolling look-back interval for an OHLC time series. |
|-------------|---|
|             |   |

# **Description**

Calculate a time series of Sharpe ratios over a rolling look-back interval for an OHLC time series.

# Usage

```
roll_sharpe(ohlc, look_back = 11)
```

### **Arguments**

ohlc An *OHLC* time series of prices in *xts* format.

look\_back The size of the look-back interval, equal to the number of rows of data used for

aggregating the OHLC prices.

### **Details**

The function roll\_sharpe() calculates the rolling Sharpe ratio defined as the ratio of percentage returns over the look-back interval, divided by the average volatility of percentage returns.

### Value

An xts time series with a single column and the same number of rows as the argument ohlc.

# **Examples**

```
# Calculate rolling Sharpe ratio over SPY
sharpe_rolling <- roll_sharpe(ohlc=HighFreq::SPY, look_back=11)</pre>
```

roll\_skew

Calculate a matrix of skewness estimates over a rolling look-back interval attached at the end points of a time series or a matrix.

# **Description**

Calculate a *matrix* of skewness estimates over a rolling look-back interval attached at the end points of a *time series* or a *matrix*.

```
roll_skew(
  tseries,
  startp = 0L,
  endp = 0L,
  step = 1L,
  look_back = 1L,
  stub = 0L,
```

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```
method = "moment",
  conf_lev = 0.75
)
```

#### **Arguments**

tseries A *time series* or a *matrix* of data.

startp An *integer* vector of start points (the default is startp =  $\emptyset$ ). endp An *integer* vector of end points (the default is endp =  $\emptyset$ ).

step The number of time periods between the end points (the default is step = 1).

look\_back The number of end points in the look-back interval (the default is look\_back =

1).

stub An *integer* value equal to the first end point for calculating the end points (the

default is stub = 0).

method A *string* specifying the type of the skewness model (the default is method =

"moment" - see Details).

conf\_lev The confidence level for calculating the quantiles (the default is conf\_lev =

0.75).

#### **Details**

The function roll\_skew() calculates a *matrix* of skewness estimates over rolling look-back intervals attached at the end points of the *time series* tseries.

The function roll\_skew() performs a loop over the end points, and at each end point it subsets the time series tseries over a look-back interval equal to look\_back number of end points.

It passes the subset time series to the function calc\_skew(), which calculates the skewness. See the function calc\_skew() for a description of the skewness methods.

If the arguments endp and startp are not given then it first calculates a vector of end points separated by step time periods. It calculates the end points along the rows of tseries using the function calc\_endpoints(), with the number of time periods between the end points equal to step time periods.

For example, the rolling skewness at 25 day end points, with a 75 day look-back, can be calculated using the parameters step = 25 and look\_back = 3.

The function roll\_skew() is implemented in RcppArmadillo C++ code, so it's many times faster than the equivalent R code.

## Value

A *matrix* of skewness estimates with the same number of columns as the input time series tseries, and the number of rows equal to the number of end points.

#### **Examples**

```
## Not run:
# Define time series of returns using package rutils
returns <- na.omit(rutils::etfenv$returns$VTI)
# Define end points and start points
endp <- 1 + HighFreq::calc_endpoints(NROW(returns), step=25)
startp <- HighFreq::calc_startpoints(endp, look_back=3)
# Calculate the rolling skewness at 25 day end points, with a 75 day look-back</pre>
```

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```
skew_ness <- HighFreq::roll_skew(returns, step=25, look_back=3)
# Calculate the rolling skewness using R code
skew_r <- sapply(1:NROW(endp), function(it) {
    HighFreq::calc_skew(returns[startp[it]:endp[it], ])
}) # end sapply
# Compare the skewness estimates
all.equal(drop(skew_ness), skew_r, check.attributes=FALSE)
# Compare the speed of RcppArmadillo with R code
library(microbenchmark)
summary(microbenchmark(
    Rcpp=HighFreq::roll_skew(returns, step=25, look_back=3),
    Rcode=sapply(1:NROW(endp), function(it) {
        HighFreq::calc_skew(returns[startp[it]:endp[it], ])
    }),
    times=10))[, c(1, 4, 5)] # end microbenchmark summary
## End(Not run)</pre>
```

roll\_stats

Calculate a vector of statistics over an OHLC time series, and calculate a rolling mean over the statistics.

# **Description**

Calculate a vector of statistics over an *OHLC* time series, and calculate a rolling mean over the statistics.

# Usage

```
roll_stats(
  ohlc,
  calc_stats = "ohlc_variance",
  look_back = 11,
  weighted = TRUE,
  ...
)
```

# Arguments

additional parameters to the function calc\_stats.
 An OHLC time series of prices and trading volumes, in xts format.
 The name of the function for estimating statistics of a single row of OHLC data, such as volatility, skew, and higher moments.
 The size of the look-back interval, equal to the number of rows of data used for calculating the rolling mean.
 Weighted
 Boolean argument: should statistic be weighted by trade volume? (default TRUE)

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#### **Details**

The function roll\_stats() calculates a vector of statistics over an *OHLC* time series, such as volatility, skew, and higher moments. The statistics could also be any other aggregation of a single row of *OHLC* data, for example the *High* price minus the *Low* price squared. The length of the vector of statistics is equal to the number of rows of the argument ohlc. Then it calculates a trade volume weighted rolling mean over the vector of statistics over and calculate statistics.

### Value

An xts time series with a single column and the same number of rows as the argument ohlc.

# **Examples**

```
# Calculate time series of rolling variance and skew estimates
var_rolling <- roll_stats(ohlc=HighFreq::SPY, look_back=21)
skew_rolling <- roll_stats(ohlc=HighFreq::SPY, calc_stats="ohlc_skew", look_back=21)
skew_rolling <- skew_rolling/(var_rolling)^(1.5)
skew_rolling[1, ] <- 0
skew_rolling <- rutils::na_locf(skew_rolling)</pre>
```

roll\_sum

Calculate the rolling sums over a time series or a matrix using Rcpp.

### Description

Calculate the rolling sums over a *time series* or a *matrix* using *Rcpp*.

#### **Usage**

```
roll_sum(tseries, look_back = 1L)
```

## **Arguments**

tseries A time series or a matrix.

look\_back The length of the look-back interval, equal to the number of data points included

in calculating the rolling sum (the default is look\_back = 1).

#### **Details**

The function roll\_sum() calculates the rolling sums over the columns of the data tseries.

The function roll\_sum() returns a *matrix* with the same dimensions as the input argument tseries.

The function roll\_sum() uses the fast RcppArmadillo function arma::cumsum(), without explicit loops. The function roll\_sum() is several times faster than rutils::roll\_sum() which uses vectorized R code.

# Value

A matrix with the same dimensions as the input argument tseries.

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#### **Examples**

```
## Not run:
# Calculate historical returns
returns <- na.omit(rutils::etfenv$returns[, c("VTI", "IEF")])
# Define parameters
look_back <- 22
# Calculate rolling sums and compare with rutils::roll_sum()
c_sum <- HighFreq::roll_sum(returns, look_back)
r_sum <- rutils::roll_sum(returns, look_back)
all.equal(c_sum, coredata(r_sum), check.attributes=FALSE)
# Calculate rolling sums using R code
r_sum <- apply(zoo::coredata(returns), 2, cumsum)
lag_sum <- rbind(matrix(numeric(2*look_back), nc=2), r_sum[1:(NROW(r_sum) - look_back),])
r_sum <- (r_sum - lag_sum)
all.equal(c_sum, r_sum, check.attributes=FALSE)
## End(Not run)</pre>
```

roll\_sumep

Calculate the rolling sums at the end points of a time series or a matrix.

# **Description**

Calculate the rolling sums at the end points of a time series or a matrix.

# Usage

```
roll_sumep(
  tseries,
  startp = 0L,
  endp = 0L,
  step = 1L,
  look_back = 1L,
  stub = 0L
)
```

#### **Arguments**

tseries A time series or a matrix.

Startp An integer vector of start points (the default is startp = 0).

endp An integer vector of end points (the default is endp = 0).

Step The number of time periods between the end points (the default is step = 1).

look\_back The number of end points in the look-back interval (the default is look\_back = 1).

Stub An integer value equal to the first end point for calculating the end points.

# **Details**

The function roll\_sumep() calculates the rolling sums at the end points of the *time series* tseries. The function roll\_sumep() is implemented in RcppArmadillo C++ code, which makes it several times faster than R code.

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#### Value

A *matrix* with the same number of columns as the input time series tseries, and the number of rows equal to the number of end points.

# **Examples**

```
## Not run:
# Calculate historical returns
returns <- na.omit(rutils::etfenv$returns[, c("VTI", "IEF")])</pre>
# Define end points at 25 day intervals
endp <- HighFreq::calc_endpoints(NROW(returns), step=25)</pre>
\# Define start points as 75 day lag of end points
startp <- HighFreq::calc_startpoints(endp, look_back=3)</pre>
# Calculate rolling sums using Rcpp
c_sum <- HighFreq::roll_sumep(returns, startp=startp, endp=endp)</pre>
# Calculate rolling sums using R code
r_sum <- sapply(1:NROW(endp), function(ep) {</pre>
colSums(returns[(startp[ep]+1):(endp[ep]+1), ])
  }) # end sapply
r_sum \leftarrow t(r_sum)
all.equal(c_sum, r_sum, check.attributes=FALSE)
## End(Not run)
```

roll\_var

Calculate a matrix of dispersion (variance) estimates over a rolling look-back interval attached at the end points of a time series or a matrix.

# **Description**

Calculate a *matrix* of dispersion (variance) estimates over a rolling look-back interval attached at the end points of a *time series* or a *matrix*.

# Usage

```
roll_var(
   tseries,
   startp = 0L,
   endp = 0L,
   step = 1L,
   look_back = 1L,
   stub = 0L,
   method = "moment",
   conf_lev = 0.75
)
```

### **Arguments**

tseries A time series or a matrix of data. startp An integer vector of start points (the default is startp = 0). 72 roll\_var

An *integer* vector of end points (the default is endp = 0).

The number of time periods between the end points (the default is step = 1).

The number of end points in the look-back interval (the default is look\_back = 1).

Stub

An *integer* value equal to the first end point for calculating the end points (the default is stub = 0).

A character string representing the type of the measure of dispersion (the default

A *character* string representing the type of the measure of dispersion (the default

is method = "moment").

#### **Details**

The function roll\_var() calculates a *matrix* of dispersion (variance) estimates over rolling look-back intervals attached at the end points of the *time series* tseries.

The function roll\_var() performs a loop over the end points, and at each end point it subsets the time series tseries over a look-back interval equal to look\_back number of end points.

It passes the subset time series to the function calc\_var(), which calculates the dispersion. See the function calc\_var() for a description of the dispersion methods.

If the arguments endp and startp are not given then it first calculates a vector of end points separated by step time periods. It calculates the end points along the rows of tseries using the function calc\_endpoints(), with the number of time periods between the end points equal to step time periods.

For example, the rolling variance at 25 day end points, with a 75 day look-back, can be calculated using the parameters step = 25 and  $look_back = 3$ .

The function roll\_var() with the parameter step = 1 performs the same calculation as the function roll\_var() from package RcppRoll, but it's several times faster because it uses RcppArmadillo C++ code.

The function roll\_var() is implemented in RcppArmadillo C++ code, so it's many times faster than the equivalent R code.

## Value

A *matrix* dispersion (variance) estimates with the same number of columns as the input time series tseries, and the number of rows equal to the number of end points.

# **Examples**

```
## Not run:
# Define time series of returns using package rutils
returns <- na.omit(rutils::etfenv$returns$VTI)
# Calculate the rolling variance at 25 day end points, with a 75 day look-back
variance <- HighFreq::roll_var(returns, step=25, look_back=3)
# Compare the variance estimates over 11-period look-back intervals
all.equal(HighFreq::roll_var(returns, look_back=11)[-(1:10), ],
    drop(RcppRoll::roll_var(returns, n=11)), check.attributes=FALSE)
# Compare the speed of HighFreq::roll_var() with RcppRoll::roll_var()
library(microbenchmark)
summary(microbenchmark(
    Rcpp=HighFreq::roll_var(returns, look_back=11),
    RcppRoll=RcppRoll::roll_var(returns, n=11),
    times=10))[, c(1, 4, 5)] # end microbenchmark summary
# Compare the speed of HighFreq::roll_var() with TTR::runMAD()</pre>
```

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```
summary(microbenchmark(
   Rcpp=HighFreq::roll_var(returns, look_back=11, method="quantile"),
   TTR=TTR::runMAD(returns, n = 11),
   times=10))[, c(1, 4, 5)] # end microbenchmark summary

## End(Not run)
```

roll\_varvec

Calculate a vector of variance estimates over a rolling look-back interval for a single-column time series or a single-column matrix, using RcppArmadillo.

## **Description**

Calculate a *vector* of variance estimates over a rolling look-back interval for a single-column *time series* or a single-column *matrix*, using RcppArmadillo.

## Usage

```
roll_varvec(tseries, look_back = 1L)
```

# Arguments

tseries A single-column *time series* or a single-column *matrix*.

look\_back The length of the look-back interval, equal to the number of *vector* elements

used for calculating a single variance estimate (the default is look\_back = 1).

# Details

The function roll\_varvec() calculates a *vector* of variance estimates over a rolling look-back interval for a single-column *time series* or a single-column *matrix*, using RcppArmadillo C++ code.

The function roll\_varvec() uses an expanding look-back interval in the initial warmup period, to calculate the same number of elements as the input argument tseries.

The function roll\_varvec() performs the same calculation as the function roll\_var() from package RcppRoll, but it's several times faster because it uses RcppArmadillo C++ code.

## Value

A single-column *matrix* with the same number of elements as the input argument tseries.

```
## Not run:
# Create a vector of random returns
returns <- rnorm(1e6)
# Compare the variance estimates over 11-period look-back intervals
all.equal(drop(HighFreq::roll_varvec(returns, look_back=11))[-(1:10)],
    RcppRoll::roll_var(returns, n=11))
# Compare the speed of RcppArmadillo with RcppRoll
library(microbenchmark)
summary(microbenchmark(
    Rcpp=HighFreq::roll_varvec(returns, look_back=11),</pre>
```

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```
RcppRoll=RcppRoll::roll_var(returns, n=11),
  times=10))[, c(1, 4, 5)] # end microbenchmark summary
## End(Not run)
```

roll\_var\_ohlc

Calculate a vector of variance estimates over a rolling look-back interval attached at the end points of a time series or a matrix with OHLC price data.

# Description

Calculate a *vector* of variance estimates over a rolling look-back interval attached at the end points of a *time series* or a *matrix* with *OHLC* price data.

# Usage

```
roll_var_ohlc(
  ohlc,
  startp = 0L,
  endp = 0L,
  step = 1L,
  look_back = 1L,
  stub = 0L,
  method = "yang_zhang",
  scale = TRUE,
  index = 0L
)
```

# Arguments

A time series or a matrix with OHLC price data. ohlc An *integer* vector of start points (the default is startp = 0). startp endp An *integer* vector of end points (the default is endp = 0). The number of time periods between the end points (the default is step = 1). step The number of end points in the look-back interval (the default is look\_back = look\_back 1). An integer value equal to the first end point for calculating the end points (the stub default is stub = 0). A character string representing the price range estimator for calculating the varimethod ance. The estimators include: • "close" close-to-close estimator, • "rogers\_satchell" Rogers-Satchell estimator,

- "garman\_klass" Garman-Klass estimator,
- "garman\_klass\_yz" Garman-Klass with account for close-to-open price jumps,
- "yang\_zhang" Yang-Zhang estimator,

(The default is the "yang\_zhang" estimator.)

scale Boolean argument: Should the returns be divided by the time index, the number

of seconds in each period? (The default is scale = TRUE.)

index A vector with the time index of the time series. This is an optional argument

(the default is index=0).

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#### **Details**

The function roll\_var\_ohlc() calculates a *vector* of variance estimates over a rolling look-back interval attached at the end points of the *time series* ohlc.

The input *OHLC time series* ohlc is assumed to contain the log prices.

The function roll\_var\_ohlc() performs a loop over the end points, subsets the previous (past) rows of ohlc, and passes them into the function calc\_var\_ohlc().

At each end point, the variance is calculated over a look-back interval equal to look\_back number of end points. In the initial warmup period, the variance is calculated over an expanding look-back interval.

If the arguments endp and startp are not given then it first calculates a vector of end points separated by step time periods. It calculates the end points along the rows of ohlc using the function calc\_endpoints(), with the number of time periods between the end points equal to step time periods.

For example, the rolling variance at daily end points with an 11 day look-back, can be calculated using the parameters step = 1 and look\_back = 1 (Assuming the ohlc data has daily frequency.)

Similarly, the rolling variance at 25 day end points with a 75 day look-back, can be calculated using the parameters step = 25 and look\_back = 3 (because 3\*25 = 75).

The function roll\_var\_ohlc() calculates the variance from all the different intra-day and day-over-day returns (defined as the differences between *OHLC* prices), using several different variance estimation methods.

The default method is "yang\_zhang", which theoretically has the lowest standard error among unbiased estimators. The methods "close", "garman\_klass\_yz", and "yang\_zhang" do account for close-to-open price jumps, while the methods "garman\_klass" and "rogers\_satchell" do not account for close-to-open price jumps.

If scale is TRUE (the default), then the returns are divided by the differences of the time index (which scales the variance to the units of variance per second squared.) This is useful when calculating the variance from minutely bar data, because dividing returns by the number of seconds decreases the effect of overnight price jumps. If the time index is in days, then the variance is equal to the variance per day squared.

The optional argument index is the time index of the *time series* ohlc. If the time index is in seconds, then the differences of the index are equal to the number of seconds in each time period. If the time index is in days, then the differences are equal to the number of days in each time period.

The function roll\_var\_ohlc() is implemented in RcppArmadillo C++ code, so it's many times faster than the equivalent R code.

## Value

A column *vector* of variance estimates, with the number of rows equal to the number of end points.

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```
index=indeks, scale=TRUE)
# Daily OHLC prices
ohlc <- rutils::etfenv$VTI</pre>
indeks <- c(1, diff(xts::.index(ohlc)))</pre>
\# Rolling variance at 5 day end points, with a 20 day look-back (20=4*5)
var_rolling <- HighFreq::roll_var_ohlc(ohlc,</pre>
                                step=5, look_back=4,
                                method="yang_zhang",
                                index=indeks, scale=TRUE)
# Same calculation in R
nrows <- NROW(ohlc)</pre>
close_lag = HighFreq::lagit(ohlc[, 4])
endp <- drop(HighFreq::calc_endpoints(nrows, 3)) + 1</pre>
startp <- drop(HighFreq::calc_startpoints(endp, 2))</pre>
n_pts <- NROW(endp)</pre>
var_rollingr <- sapply(2:n_pts, function(it) {</pre>
  rangev <- startp[it]:endp[it]</pre>
  sub_ohlc = ohlc[rangev, ]
  sub_close = close_lag[rangev]
  sub_index = indeks[rangev]
  HighFreq::calc_var_ohlc(sub_ohlc, close_lag=sub_close, scale=TRUE, index=sub_index)
}) # end sapply
var_rollingr <- c(0, var_rollingr)</pre>
all.equal(drop(var_rolling), var_rollingr)
## End(Not run)
```

roll\_vec

Calculate the rolling sums over a single-column time series or a single-column matrix using Rcpp.

# Description

Calculate the rolling sums over a single-column time series or a single-column matrix using Rcpp.

# Usage

```
roll_vec(tseries, look_back)
```

#### **Arguments**

tseries A single-column time series or a single-column matrix.

look\_back The length of the look-back interval, equal to the number of elements of data

used for calculating the sum.

#### **Details**

The function roll\_vec() calculates a single-column *matrix* of rolling sums, over a single-column *matrix* of data, using fast *Rcpp* C++ code. The function roll\_vec() is several times faster than rutils::roll\_sum() which uses vectorized R code.

# Value

A single-column *matrix* of the same length as the argument tseries.

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#### **Examples**

```
## Not run:
# Define a single-column matrix of returns
returns <- zoo::coredata(na.omit(rutils::etfenv$returns$VTI))</pre>
# Calculate rolling sums over 11-period look-back intervals
sum_rolling <- HighFreq::roll_vec(returns, look_back=11)</pre>
# Compare HighFreq::roll_vec() with rutils::roll_sum()
all.equal(HighFreq::roll_vec(returns, look_back=11),
         rutils::roll_sum(returns, look_back=11),
         check.attributes=FALSE)
# Compare the speed of Rcpp with R code
library(microbenchmark)
summary(microbenchmark(
  Rcpp=HighFreq::roll_vec(returns, look_back=11),
  Rcode=rutils::roll_sum(returns, look_back=11),
  times=10))[, c(1, 4, 5)] # end microbenchmark summary
## End(Not run)
```

roll\_vecw

Calculate the rolling weighted sums over a single-column time series or a single-column matrix using RcppArmadillo.

## **Description**

Calculate the rolling weighted sums over a single-column *time series* or a single-column *matrix* using RcppArmadillo.

#### Usage

```
roll_vecw(tseries, weights)
```

# **Arguments**

tseries A single-column *time series* or a single-column *matrix*.

weights A single-column matrix of weights.

# **Details**

The function roll\_vecw() calculates the rolling weighted sums of a single-column *matrix* over its past values (a convolution with the single-column *matrix* of weights), using RcppArmadillo. It performs a similar calculation as the standard R function

stats::filter(x=series,filter=weights,method="convolution",sides=1), but it's over 6 times faster, and it doesn't produce any NA values.

### Value

A single-column *matrix* of the same length as the argument tseries.

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#### **Examples**

```
## Not run:
# First example
# Define a single-column matrix of returns
returns <- zoo::coredata(na.omit(rutils::etfenv$returns$VTI))</pre>
# Create simple weights
weights <- matrix(c(1, rep(0, 10)))
# Calculate rolling weighted sums
weighted <- HighFreq::roll_vecw(tseries=returns, weights=weights)</pre>
# Compare with original
all.equal(zoo::coredata(returns), weighted, check.attributes=FALSE)
# Second example
# Create exponentially decaying weights
weights \leftarrow matrix(exp(-0.2*1:11))
weights <- weights/sum(weights)</pre>
# Calculate rolling weighted sums
weighted <- HighFreq::roll_vecw(tseries=returns, weights=weights)</pre>
# Calculate rolling weighted sums using filter()
filtered <- stats::filter(x=returns, filter=weights, method="convolution", sides=1)</pre>
# Compare both methods
all.equal(filtered[-(1:11)], weighted[-(1:11)], check.attributes=FALSE)
# Compare the speed of Rcpp with R code
library(microbenchmark)
summary(microbenchmark(
  Rcpp=HighFreq::roll_vecw(tseries=returns, weights=weights),
  Rcode=stats::filter(x=returns, filter=weights, method="convolution", sides=1),
  times=10))[, c(1, 4, 5)] # end microbenchmark summary
## End(Not run)
```

roll\_vwap

Calculate the volume-weighted average price of an OHLC time series over a rolling look-back interval.

# **Description**

Performs the same operation as function VWAP() from package TTR, but using vectorized functions, so it's a little faster.

# Usage

```
roll_vwap(ohlc, close = ohlc[, 4, drop = FALSE], look_back)
```

# Arguments

ohlc An *OHLC* time series of prices in *xts* format.

close A time series of close prices.

look\_back The size of the look-back interval, equal to the number of rows of data used for

calculating the average price.

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#### **Details**

The function roll\_vwap() calculates the volume-weighted average closing price, defined as the sum of the prices multiplied by trading volumes in the look-back interval, divided by the sum of trading volumes in the interval. If the argument close is passed in explicitly, then its volume-weighted average value over time is calculated.

#### Value

An xts time series with a single column and the same number of rows as the argument ohlc.

# **Examples**

```
# Calculate and plot rolling volume-weighted average closing prices (VWAP)
prices_rolling <- roll_vwap(ohlc=HighFreq::SPY["2013-11"], look_back=11)
chart_Series(HighFreq::SPY["2013-11-12"], name="SPY prices")
add_TA(prices_rolling["2013-11-12"], on=1, col="red", lwd=2)
legend("top", legend=c("SPY prices", "VWAP prices"),
bg="white", lty=c(1, 1), lwd=c(2, 2),
col=c("black", "red"), bty="n")
# Calculate running returns
returns_running <- ohlc_returns(xtes=HighFreq::SPY)
# Calculate the rolling volume-weighted average returns
roll_vwap(ohlc=HighFreq::SPY, close=returns_running, look_back=11)</pre>
```

roll\_wsum Calculate the rolling weighted sums over a time series or a matrix using Rcpp.

### **Description**

Calculate the rolling weighted sums over a *time series* or a *matrix* using *Rcpp*.

# Usage

```
roll_wsum(tseries, endp = NULL, look_back = 1L, stub = NULL, weights = NULL)
```

### Arguments

| tseries   | A time series or a matrix.   |
|-----------|--|
| endp      | An <i>integer</i> vector of end points (the default is endp = NULL).   |
| look_back | The length of the look-back interval, equal to the number of data points included in calculating the rolling sum (the default is look_back = 1). |
| stub      | An $integer$ value equal to the first end point for calculating the end points (the default is stub = NULL).                                     |
| weights   | A single-column <i>matrix</i> of weights (the default is weights = NULL).  |

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#### **Details**

The function roll\_wsum() calculates the rolling weighted sums over the columns of the data tseries.

The function roll\_wsum() calculates the rolling weighted sums as convolutions of the columns of tseries with the *column vector* of weights using the RcppArmadillo function arma::conv2(). It performs a similar calculation to the standard R function

stats::filter(x=returns,filter=weights,method="convolution",sides=1), but it can be many times faster, and it doesn't produce any leading NA values.

The function roll\_wsum() returns a *matrix* with the same dimensions as the input argument tseries.

The arguments weights, endp, and stub are optional.

If the argument weights is not supplied, then simple sums are calculated, not weighted sums.

If either the stub or endp arguments are supplied, then the rolling sums are calculated at the end points.

If only the argument stub is supplied, then the end points are calculated from the stub and look\_back arguments. The first end point is equal to stub and the end points are spaced look\_back periods apart.

If the arguments weights, endp, and stub are not supplied, then the sums are calculated over a number of data points equal to look\_back.

The function roll\_wsum() is also several times faster than rutils::roll\_sum() which uses vectorized R code.

Technical note: The function roll\_wsum() has arguments with default values equal to NULL, which are implemented in Rcpp code.

## Value

A *matrix* with the same dimensions as the input argument tseries.

```
## Not run:
# First example
# Calculate historical returns
returns <- na.omit(rutils::etfenv$returns[, c("VTI", "IEF")])</pre>
# Define parameters
look_back <- 22
# Calculate rolling sums and compare with rutils::roll_sum()
c_sum <- HighFreq::roll_sum(returns, look_back)</pre>
r_sum <- rutils::roll_sum(returns, look_back)</pre>
all.equal(c_sum, coredata(r_sum), check.attributes=FALSE)
# Calculate rolling sums using R code
r_sum <- apply(zoo::coredata(returns), 2, cumsum)</pre>
lag_sum <- rbind(matrix(numeric(2*look_back), nc=2), r_sum[1:(NROW(r_sum) - look_back), ])</pre>
r_sum <- (r_sum - lag_sum)</pre>
all.equal(c_sum, r_sum, check.attributes=FALSE)
# Calculate rolling sums at end points
stu_b <- 21
c_sum <- HighFreq::roll_wsum(returns, look_back, stub=stu_b)</pre>
endp <- (stu_b + look_back*(0:(NROW(returns) %/% look_back)))</pre>
endp <- endp[endp < NROW(returns)]</pre>
r_sum <- apply(zoo::coredata(returns), 2, cumsum)</pre>
```

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```
r_sum <- r_sum[endp+1, ]
lag_sum <- rbind(numeric(2), r_sum[1:(NROW(r_sum) - 1), ])</pre>
r_sum <- (r_sum - lag_sum)</pre>
all.equal(c_sum, r_sum, check.attributes=FALSE)
# Calculate rolling sums at end points - pass in endp
c_sum <- HighFreq::roll_wsum(returns, endp=endp)</pre>
all.equal(c_sum, r_sum, check.attributes=FALSE)
# Create exponentially decaying weights
weights <- \exp(-0.2*(1:11))
weights <- matrix(weights/sum(weights), nc=1)</pre>
# Calculate rolling weighted sum
c_sum <- HighFreq::roll_wsum(returns, weights=weights)</pre>
# Calculate rolling weighted sum using filter()
filtered <- filter(x=returns, filter=weights, method="convolution", sides=1)</pre>
all.equal(c_sum[-(1:11), ], filtered[-(1:11), ], check.attributes=FALSE)
# Calculate rolling weighted sums at end points
c_sum <- HighFreq::roll_wsum(returns, endp=endp, weights=weights)</pre>
all.equal(c_sum, filtered[endp+1, ], check.attributes=FALSE)
# Create simple weights equal to a 1 value plus zeros
weights \leftarrow matrix(c(1, rep(0, 10)), nc=1)
# Calculate rolling weighted sum
weighted <- HighFreq::roll_wsum(returns, weights=weights)</pre>
# Compare with original
all.equal(coredata(returns), weighted, check.attributes=FALSE)
## End(Not run)
```

roll\_zscores

Calculate a vector of z-scores of the residuals of rolling regressions at the end points of the predictor matrix.

#### **Description**

Calculate a *vector* of z-scores of the residuals of rolling regressions at the end points of the predictor matrix.

# Usage

```
roll_zscores(
  response,
  predictor,
  startp = 0L,
  endp = 0L,
  step = 1L,
  look_back = 1L,
  stub = 0L
```

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## **Arguments**

response A single-column *time series* or a *vector* of response data.

A *time series* or a *matrix* of predictor data.

Startp An *integer* vector of start points (the default is startp = 0).

An *integer* vector of end points (the default is endp = 0).

The number of time periods between the end points (the default is step = 1).

The number of end points in the look-back interval (the default is look\_back = 1).

stub An *integer* value equal to the first end point for calculating the end points (the

default is stub = 0).

#### **Details**

The function roll\_zscores() calculates a *vector* of z-scores of the residuals of rolling regressions at the end points of the *time series* predictor.

The function roll\_zscores() performs a loop over the end points, and at each end point it subsets the time series predictor over a look-back interval equal to look\_back number of end points.

It passes the subset time series to the function calc\_lm(), which calculates the regression data.

If the arguments endp and startp are not given then it first calculates a vector of end points separated by step time periods. It calculates the end points along the rows of predictor using the function calc\_endpoints(), with the number of time periods between the end points equal to step time periods.

For example, the rolling variance at 25 day end points, with a 75 day look-back, can be calculated using the parameters step = 25 and look\_back = 3.

### Value

A column *vector* of the same length as the number of rows of predictor.

```
## Not run:
# Calculate historical returns
returns <- na.omit(rutils::etfenv$returns[, c("XLF", "VTI", "IEF")])</pre>
# Response equals XLF returns
response <- returns[, 1]</pre>
# Predictor matrix equals VTI and IEF returns
predictor <- returns[, -1]</pre>
# Calculate Z-scores from rolling time series regression using RcppArmadillo
look_back <- 11
z_scores <- HighFreq::roll_zscores(response=response, predictor=predictor, look_back)</pre>
\# Calculate z-scores in R from rolling multivariate regression using lm()
z_scoresr <- sapply(1:NROW(predictor), function(ro_w) {</pre>
  if (ro_w == 1) return(0)
  startpoint <- max(1, ro_w-look_back+1)</pre>
  responsi <- response[startpoint:ro_w]</pre>
  predicti <- predictor[startpoint:ro_w, ]</pre>
  reg_model <- lm(responsi ~ predicti)</pre>
  residuals <- reg_model$residuals</pre>
  residuals[NROW(residuals)]/sd(residuals)
}) # end sapply
```

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```
# Compare the outputs of both functions
all.equal(z_scores[-(1:look_back)], z_scoresr[-(1:look_back)],
    check.attributes=FALSE)
## End(Not run)
```

run\_covar

Calculate the running covariance of two streaming time series of returns.

# **Description**

Calculate the running covariance of two streaming time series of returns.

# Usage

run\_covar(tseries, lambda)

# **Arguments**

tseries A *time series* or a *matrix* with two columns of returns data.

lambda A *numeric* decay factor to multiply past estimates.

#### **Details**

The function run\_covar() calculates the running covariance of two streaming *time series* of returns, by recursively weighing the products of their returns minus their means, with past covariance estimates  $\sigma_{t-1}^{cov}$ , using the decay factor  $\lambda$ :

$$\begin{split} \mu_t^1 &= (1-\lambda)r_t^1 + \lambda \mu_{t-1}^1 \\ \mu_t^2 &= (1-\lambda)r_t^2 + \lambda \mu_{t-1}^2 \\ \sigma_t^{cov} &= (1-\lambda)(r_t^1 - \mu_t^1)(r_t^2 - \mu_t^2) + \lambda \sigma_{t-1}^{cov} \end{split}$$

Where  $\sigma_t^{cov}$  is the covariance estimate at time t,  $r_t^1$  and  $r_t^2$  are the two streaming returns data, and  $\mu_t^1$  and  $\mu_t^2$  are the means of the returns.

The above recursive formula is convenient for processing live streaming data because it doesn't require maintaining a buffer of past data. The formula is equivalent to a convolution with exponentially decaying weights, but it's faster.

The value of the decay factor  $\lambda$  should be in the range between 0 and 1. If  $\lambda$  is close to 1 then the decay is weak and past values have a greater weight, and the running covariance values have a stronger dependence on past values. This is equivalent to a long look-back interval. If  $\lambda$  is much less than 1 then the decay is strong and past values have a smaller weight, and the running covariance values have a weaker dependence on past values. This is equivalent to a short look-back interval.

The function run\_covar() returns three columns of data: the covariance and the variances of the two columns of the argument tseries. This allows calculating the running correlation.

### Value

A *matrix* with three columns of data: the covariance and the variances of the two columns of the argument tseries.

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#### **Examples**

```
## Not run:
# Calculate historical returns
returns <- zoo::coredata(na.omit(rutils::etfenv$returns[, c("IEF", "VTI")]))
# Calculate the running covariance
lambda <- 0.9
covars <- HighFreq::run_covar(returns, lambda=lambda)
# Calculate running covariance using R code
filtered <- (1-lambda)*filter(returns[, 1]*returns[, 2],
    filter=lambda, init=as.numeric(returns[1, 1]*returns[1, 2])/(1-lambda),
    method="recursive")
all.equal(covars[, 1], unclass(filtered), check.attributes=FALSE)
# Calculate the running correlation
correl <- covars[, 1]/sqrt(covars[, 2]*covars[, 3])
## End(Not run)</pre>
```

run\_max

Calculate the running maximum of streaming time series data.

#### **Description**

Calculate the running maximum of streaming time series data.

## Usage

```
run_max(tseries, lambda)
```

# **Arguments**

tseries A time series or a matrix.

lambda A *numeric* decay factor to multiply past estimates.

#### **Details**

The function run\_max() calculates the running maximum of streaming *time series* data by recursively weighing present and past values using the decay factor  $\lambda$ .

It first calculates the running mean of streaming data:

$$\mu_t = (1 - \lambda)p_t + \lambda\mu_{t-1}$$

Where  $\mu_t$  is the mean value at time t, and  $p_t$  is the streaming data.

It then calculates the running maximums of streaming data,  $p_t^{max}$ :

$$p_t^{max} = max(p_t, p_{t-1}^{max}) + (1 - \lambda)(\mu_{t-1} - p_{t-1}^{max})$$

The second term pulls the maximum value down to the mean value, allowing it to gradually "forget" the maximum value from the more distant past.

The above recursive formulas are convenient for processing live streaming data because it doesn't require maintaining a buffer of past data.

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The value of the decay factor  $\lambda$  should be in the range between 0 and 1. If  $\lambda$  is close to 1 then the decay is weak and past values have a greater weight, and the running maximum values have a stronger dependence on past values. This is equivalent to a long look-back interval. If  $\lambda$  is much less than 1 then the decay is strong and past values have a smaller weight, and the running maximum values have a weaker dependence on past values. This is equivalent to a short look-back interval.

The function run\_max() returns a *matrix* with the same dimensions as the input argument tseries.

#### Value

A matrix with the same dimensions as the input argument tseries.

# **Examples**

```
## Not run:
# Calculate historical prices
prices <- zoo::coredata(quantmod::Cl(rutils::etfenv$VTI))
# Calculate the running maximums
lambda <- 0.9
maxs <- HighFreq::run_max(prices, lambda=lambda)
# Plot dygraph of VTI prices and running maximums
datav <- cbind(quantmod::Cl(rutils::etfenv$VTI), maxs)
colnames(datav) <- c("prices", "max")
colnamev <- colnames(datav)
dygraphs::dygraph(datav, main="VTI Prices and Running Maximums") %>%
    dySeries(name=colnamev[1], label=colnamev[1], strokeWidth=2, col="blue") %>%
    dySeries(name=colnamev[2], label=colnamev[2], strokeWidth=2, col="red")
## End(Not run)
```

run\_mean

Calculate the running weighted means of streaming time series data.

# **Description**

Calculate the running weighted means of streaming *time series* data.

### Usage

```
run_mean(tseries, lambda, weights = 0L)
```

### **Arguments**

tseries A time series or a matrix.

lambda A *numeric* decay factor to multiply past estimates.

weights A single-column *matrix* of weights.

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#### **Details**

The function run\_mean() calculates the running weighted means of the streaming *time series* data  $p_t$  by recursively weighing present and past values using the decay factor  $\lambda$ :

$$\mu_t^w = (1 - \lambda)w_t + \lambda \mu_{t-1}^w$$

$$\mu_t^p = (1 - \lambda)w_t p_t + \lambda \mu_{t-1}^p$$

Where  $p_t$  is the streaming data,  $w_t$  are the streaming weights,  $\mu_t^w$  are the running mean weights, and  $\mu_t^p$  are the running mean products of the data and the weights.

The running mean weighted value  $\mu_t$  is equal to the ratio of the data and weights products, divided by the mean weights:

$$\mu_t = \frac{\mu_t^p}{\mu_t^w}$$

If the weights argument is omitted, then the function run\_mean() simply calculates the running means of  $p_t$ :

$$\mu_t = (1 - \lambda)p_t + \lambda\mu_{t-1}$$

The above recursive formulas are convenient for processing live streaming data because it doesn't require maintaining a buffer of past data. The formula is equivalent to a convolution with exponentially decaying weights, but it's faster.

The value of the decay factor  $\lambda$  should be in the range between 0 and 1. If  $\lambda$  is close to 1 then the decay is weak and past values have a greater weight, and the running mean values have a stronger dependence on past values. This is equivalent to a long look-back interval. If  $\lambda$  is much less than 1 then the decay is strong and past values have a smaller weight, and the running mean values have a weaker dependence on past values. This is equivalent to a short look-back interval.

The function run\_mean() performs the same calculation as the standard R function stats::filter(x=series,filter=lambda,method="recursive"), but it's several times faster.

The function run\_mean() returns a *matrix* with the same dimensions as the input argument tseries.

#### Value

A *matrix* with the same dimensions as the input argument tseries.

```
## Not run:
# Calculate historical prices
ohlc <- rutils::etfenv$VTI
closep <- quantmod::Cl(ohlc)</pre>
# Calculate the running means
lambda <- 0.95
means <- HighFreq::run_mean(closep, lambda=lambda)</pre>
# Calculate running means using R code
filtered <- (1-lambda)*filter(prices,</pre>
  filter=lambda, init=as.numeric(prices[1, 1])/(1-lambda),
  method="recursive")
all.equal(drop(means), unclass(filtered), check.attributes=FALSE)
# Compare the speed of RcppArmadillo with R code
library(microbenchmark)
summary(microbenchmark(
  Rcpp=HighFreq::run_mean(prices, lambda=lambda),
```

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```
Rcode=filter(prices, filter=lambda, init=as.numeric(prices[1, 1])/(1-lambda), method="recursive"),
    times=10))[, c(1, 4, 5)] # end microbenchmark summary

# Create weights equal to the trading volumes
weights <- quantmod::Vo(ohlc)
# Calculate the running weighted means
meanw <- HighFreq::run_mean(prices, lambda=lambda, weights=weights)
# Plot dygraph of the running weighted means
datav <- xts(cbind(means, meanw), zoo::index(ohlc))
colnames(datav) <- c("means running", "means weighted")
dygraphs::dygraph(datav, main="Running Means") %>%
    dyOptions(colors=c("blue", "red"), strokeWidth=1) %>%
    dyLegend(show="always", width=500)

## End(Not run)
```

run\_min

Calculate the running minimum of streaming time series data.

#### **Description**

Calculate the running minimum of streaming time series data.

#### **Usage**

```
run_min(tseries, lambda)
```

# **Arguments**

tseries A time series or a matrix.

lambda A *numeric* decay factor to multiply past estimates.

#### **Details**

The function run\_min() calculates the running minimum of streaming *time series* data by recursively weighing present and past values using the decay factor  $\lambda$ .

It first calculates the running mean of streaming data:

$$\mu_t = (1 - \lambda)p_t + \lambda\mu_{t-1}$$

Where  $\mu_t$  is the mean value at time t, and  $p_t$  is the streaming data.

It then calculates the running minimums of streaming data,  $p_t^{min}$ :

$$p_t^{min} = min(p_t, p_{t-1}^{min}) + (1 - \lambda)(\mu_{t-1} - p_{t-1}^{min})$$

The second term pulls the minimum value up to the mean value, allowing it to gradually "forget" the minimum value from the more distant past.

The above recursive formula is convenient for processing live streaming data because it doesn't require maintaining a buffer of past data.

The value of the decay factor  $\lambda$  should be in the range between 0 and 1. If  $\lambda$  is close to 1 then the decay is weak and past values have a greater weight, and the running minimum values have a

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stronger dependence on past values. This is equivalent to a long look-back interval. If  $\lambda$  is much less than 1 then the decay is strong and past values have a smaller weight, and the running minimum values have a weaker dependence on past values. This is equivalent to a short look-back interval.

The function run\_min() returns a *matrix* with the same dimensions as the input argument tseries.

#### Value

A *matrix* with the same dimensions as the input argument tseries.

### **Examples**

```
## Not run:
# Calculate historical prices
prices <- zoo::coredata(quantmod::Cl(rutils::etfenv$VTI))
# Calculate the running minimums
lambda <- 0.9
mins <- HighFreq::run_min(prices, lambda=lambda)
# Plot dygraph of VTI prices and running minimums
datav <- cbind(quantmod::Cl(rutils::etfenv$VTI), mins)
colnames(datav) <- c("prices", "min")
colnamev <- colnames(datav)
dygraphs::dygraph(datav, main="VTI Prices and Running Minimums") %>%
    dySeries(name=colnamev[1], label=colnamev[1], strokeWidth=2, col="blue") %>%
    dySeries(name=colnamev[2], label=colnamev[2], strokeWidth=2, col="red")
## End(Not run)
```

run\_reg

Perform running regressions of streaming time series of response and predictor data, and calculate the alphas, betas, and the residuals.

# **Description**

Perform running regressions of streaming *time series* of response and predictor data, and calculate the alphas, betas, and the residuals.

## Usage

```
run_reg(response, predictor, lambda, method = "none")
```

#### **Arguments**

response A single-column *time series* or a single-column *matrix* of response data.

predictor A time series or a matrix of predictor data.

lambda A *numeric* decay factor to multiply past estimates.

method A *string* specifying the method for scaling the residuals (see Details) (the default

is method = "none" - no scaling)

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#### **Details**

The function run\_reg() calculates the vectors of alphas  $\alpha_t$ , betas  $\beta_t$ , and the residuals  $\epsilon_t$  of running regressions, by recursively weighing the current estimates with past estimates, using the decay factor  $\lambda$ :

$$\mu_{t}^{r} = (1 - \lambda)r_{t}^{r} + \lambda\mu_{t-1}^{r}$$

$$\mu_{t}^{p} = (1 - \lambda)r_{t}^{p} + \lambda\mu_{t-1}^{p}$$

$$\sigma_{t}^{2} = (1 - \lambda)(r_{t}^{p2} - \mu_{t}^{p2}) + \lambda\sigma_{t-1}^{2}$$

$$\sigma_{t}^{cov} = (1 - \lambda)(r_{t}^{r} - \mu_{t}^{r})(r_{t}^{p} - \mu_{t}^{p}) + \lambda\sigma_{t-1}^{cov}$$

$$\beta_{t} = (1 - \lambda)\frac{\sigma_{t}^{cov}}{\sigma_{t}^{2}} + \lambda\beta_{t-1}$$

$$\epsilon_{t} = (1 - \lambda)(r_{t}^{r} - \beta_{t}r_{t}^{p}) + \lambda\epsilon_{t-1}$$

Where  $\sigma_t^{cov}$  are the covariances between the response and predictor data at time t;  $\sigma_t^2$  is the vector of predictor variances, and  $r_t^r$  and  $r_t^p$  are the streaming data of the response and predictor data.

The matrices  $\sigma^2$ ,  $\sigma^{cov}$ , and  $\beta$  have the same dimensions as the input argument predictor.

The above recursive formulas are convenient for processing live streaming data because it doesn't require maintaining a buffer of past data. The formula is equivalent to a convolution with exponentially decaying weights, but it's faster to calculate.

The value of the decay factor  $\lambda$  should be in the range between 0 and 1. If  $\lambda$  is close to 1 then the decay is weak and past values have a greater weight, and the running *z-score* values have a stronger dependence on past values. This is equivalent to a long look-back interval. If  $\lambda$  is much less than 1 then the decay is strong and past values have a smaller weight, and the running *z-score* values have a weaker dependence on past values. This is equivalent to a short look-back interval.

The *residuals* may be scaled by their volatilities. The default is method = "none" - no scaling. If the argument method = "scale" then the *residuals*  $\epsilon_t$  are divided by their volatilities  $\sigma^\epsilon$  without subtracting their means:

$$\epsilon_t = \frac{\epsilon_t}{\sigma^{\epsilon}}$$

If the argument method = "standardize" then the means  $\mu_{\epsilon}$  are subtracted from the *residuals*, and then they are divided by their volatilities  $\sigma^{\epsilon}$ :

$$\epsilon_t = \frac{\epsilon_t - \mu_\epsilon}{\sigma^\epsilon}$$

The function run\_reg() returns multiple columns of data. If the matrix predictor has n columns then run\_reg() returns a matrix with n+2 columns. The first column contains the *residuals*, the second the *alphas*, and the last columns contain the *betas*.

# Value

A matrix with the regression alphas, betas, and residuals.

```
## Not run:
# Calculate historical returns
returns <- na.omit(rutils::etfenv$returns[, c("XLF", "VTI", "IEF")])
# Response equals XLF returns
response <- returns[, 1]
# Predictor matrix equals VTI and IEF returns</pre>
```

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run\_var

Calculate the running variance of streaming time series of returns.

#### **Description**

Calculate the running variance of streaming *time series* of returns.

#### Usage

```
run_var(tseries, lambda)
```

#### **Arguments**

tseries A time series or a matrix of returns.

lambda A *numeric* decay factor to multiply past estimates.

# **Details**

The function run\_var() calculates the running variance of a streaming *time series* of returns, by recursively weighing the squared returns  $r_t^2$  minus the squared means  $\mu_t^2$ , with the past variance estimates  $\sigma_{t-1}^2$ , using the decay factor  $\lambda$ :

$$\mu_t = (1 - \lambda)r_t + \lambda \mu_{t-1}$$

$$\sigma_t^2 = (1 - \lambda)(r_t^2 - \mu_t^2) + \lambda \sigma_{t-1}^2$$

Where  $\sigma_t^2$  is the variance estimate at time t, and  $r_t$  are the streaming returns data.

The above recursive formula is convenient for processing live streaming data because it doesn't require maintaining a buffer of past data. The formula is equivalent to a convolution with exponentially decaying weights, but it's faster.

The value of the decay factor  $\lambda$  should be in the range between 0 and 1. If  $\lambda$  is close to 1 then the decay is weak and past values have a greater weight, and the running variance values have a stronger dependence on past values. This is equivalent to a long look-back interval. If  $\lambda$  is much less than 1 then the decay is strong and past values have a smaller weight, and the running variance values have a weaker dependence on past values. This is equivalent to a short look-back interval.

The function run\_var() performs the same calculation as the standard R function stats::filter(x=series,filter=weights,method="recursive"), but it's several times faster. The function run\_var() returns a *matrix* with the same dimensions as the input argument tseries.

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#### Value

A matrix with the same dimensions as the input argument tseries.

#### **Examples**

```
## Not run:
# Calculate historical returns
returns <- zoo::coredata(na.omit(rutils::etfenv$returns$VTI))</pre>
# Calculate the running variance
lambda <- 0.9
vars <- HighFreq::run_var(returns, lambda=lambda)</pre>
# Calculate running variance using R code
filtered <- (1-lambda)*filter(returns^2, filter=lambda,</pre>
  init=as.numeric(returns[1, 1])^2/(1-lambda),
  method="recursive")
all.equal(vars, unclass(filtered), check.attributes=FALSE)
# Compare the speed of RcppArmadillo with R code
library(microbenchmark)
summary(microbenchmark(
  Rcpp=HighFreq::run_var(returns, lambda=lambda),
 Rcode=filter(returns^2, filter=lambda, init=as.numeric(returns[1, 1])^2/(1-lambda), method="recursive"),
  times=10))[, c(1, 4, 5)] # end microbenchmark summary
## End(Not run)
```

run\_var\_ohlc

Calculate the running variance of streaming OHLC price data.

### Description

Calculate the running variance of streaming OHLC price data.

### Usage

```
run_var_ohlc(ohlc, lambda)
```

#### **Arguments**

ohlc A *time series* or a *matrix* with *OHLC* price data.

lambda A *numeric* decay factor to multiply past estimates.

#### **Details**

The function run\_var\_ohlc() calculates a single-column *matrix* of variance estimates of streaming *OHLC* price data.

The function run\_var\_ohlc() calculates the variance from the differences between the *Open*, *High*, *Low*, and *Close* prices, using the *Yang-Zhang* range volatility estimator:

$$\sigma_t^2 = (1 - \lambda)((O_t - C_{t-1})^2 + 0.134(C_t - O_t)^2 + 0.866((H_i - O_i)(H_i - C_i) + (L_i - O_i)(L_i - C_i))) + \lambda \sigma_{t-1}^2$$

It recursively weighs the current variance estimate with the past estimates  $\sigma_{t-1}^2$ , using the decay factor  $\lambda$ .

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The above recursive formula is convenient for processing live streaming data because it doesn't require maintaining a buffer of past data. The formula is equivalent to a convolution with exponentially decaying weights, but it's faster.

The function run\_var\_ohlc() does not calculate the logarithm of the prices. So if the argument ohlc contains dollar prices then run\_var\_ohlc() calculates the dollar variance. If the argument ohlc contains the log prices then run\_var\_ohlc() calculates the percentage variance.

The function run\_var\_ohlc() is implemented in RcppArmadillo C++ code, so it's many times faster than the equivalent R code.

#### Value

A single-column *matrix* of variance estimates, with the same number of rows as the input ohlc price data.

# **Examples**

```
## Not run:
# Extract the log OHLC prices of VTI
ohlc <- log(rutils::etfenv$VTI)</pre>
# Calculate the running variance
var_running <- HighFreq::run_var_ohlc(ohlc, lambda=0.8)</pre>
# Calculate the rolling variance
var_rolling <- HighFreq::roll_var_ohlc(ohlc, look_back=5, method="yang_zhang", scale=FALSE)</pre>
datav <- cbind(var_running, var_rolling)</pre>
colnames(datav) <- c("running", "rolling")</pre>
colnamev <- colnames(datav)</pre>
datav <- xts::xts(datav, index(ohlc))</pre>
# dygraph plot of VTI running versus rolling volatility
dygraphs::dygraph(sqrt(datav[-(1:111), ]), main="Running and Rolling Volatility of VTI") %>%
  dyOptions(colors=c("red", "blue"), strokeWidth=1) %>%
  dyLegend(show="always", width=500)
# Compare the speed of running versus rolling volatility
library(microbenchmark)
summary(microbenchmark(
  running=HighFreq::run_var_ohlc(ohlc, lambda=0.8),
  rolling=HighFreq::roll_var_ohlc(ohlc, look_back=5, method="yang_zhang", scale=FALSE),
  times=10)[, c(1, 4, 5)]
## End(Not run)
```

run\_zscores

Calculate the z-scores of running regressions of streaming time series of returns.

#### **Description**

Calculate the z-scores of running regressions of streaming time series of returns.

# Usage

```
run_zscores(response, predictor, lambda, demean = TRUE)
```

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#### **Arguments**

response A single-column *time series* or a single-column *matrix* of response data.

predictor A time series or a matrix of predictor data.

lambda A *numeric* decay factor to multiply past estimates.

demean A Boolean specifying whether the z-scores should be de-meaned (the default is

demean = TRUE).

#### **Details**

The function run\_zscores() calculates the vectors of *betas*  $\beta_t$  and the residuals  $\epsilon_t$  of running regressions by recursively weighing the current estimates with past estimates, using the decay factor  $\lambda$ .

$$\sigma_t^2 = (1 - \lambda)r_t^{p^2} + \lambda \sigma_{t-1}^2$$

$$\sigma_t^{cov} = (1 - \lambda)r_t^r r_t^p + \lambda \sigma_{t-1}^{cov}$$

$$\beta_t = (1 - \lambda)\frac{\sigma_t^{cov}}{\sigma_t^2} + \lambda \beta_{t-1}$$

$$\epsilon_t = (1 - \lambda)(r_t^r - \beta_t r_t^p) + \lambda \epsilon_{t-1}$$

Where  $\sigma_t^{cov}$  is the vector of covariances between the response and predictor returns, at time t;  $\sigma_t^2$  is the vector of predictor variances, and  $r_t^p$  and  $r_t^p$  are the streaming returns of the response and predictor data.

The above formulas for  $\sigma^2$  and  $\sigma^{cov}$  are approximate because they don't subtract the means before squaring the returns. But they're very good approximations for daily returns.

The matrices  $\sigma^2$ ,  $\sigma^{cov}$ ,  $\beta$  have the same dimensions as the input argument predictor.

If the argument demean = TRUE (the default) then the *z-scores*  $z_t$  are calculated as equal to the residuals  $\epsilon_t$  minus their means  $\mu_{\epsilon}$ , divided by their volatilities  $\sigma^{\epsilon}$ :

$$z_t = \frac{\epsilon_t - \mu_\epsilon}{\sigma^\epsilon}$$

If the argument demean = FALSE then the z-scores are only divided by their volatilities without subtracting their means:

$$z_t = \frac{\epsilon_t}{\sigma^{\epsilon}}$$

The above recursive formulas are convenient for processing live streaming data because it doesn't require maintaining a buffer of past data. The formula is equivalent to a convolution with exponentially decaying weights, but it's faster to calculate.

The value of the decay factor  $\lambda$  should be in the range between 0 and 1. If  $\lambda$  is close to 1 then the decay is weak and past values have a greater weight, and the running *z-score* values have a stronger dependence on past values. This is equivalent to a long look-back interval. If  $\lambda$  is much less than 1 then the decay is strong and past values have a smaller weight, and the running *z-score* values have a weaker dependence on past values. This is equivalent to a short look-back interval.

The function run\_zscores() returns multiple columns of data. If the matrix predictor has n columns then run\_zscores() returns a matrix with 2n+1 columns. The first column contains the *z-scores*, and the remaining columns contain the *betas* and the *variances* of the predictor data.

### Value

A matrix with the z-scores, betas, and the variances of the predictor data.

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#### **Examples**

```
## Not run:
# Calculate historical returns
returns <- na.omit(rutils::etfenv$returns[, c("XLF", "VTI", "IEF")])</pre>
# Response equals XLF returns
response <- returns[, 1]</pre>
# Predictor matrix equals VTI and IEF returns
predictor <- returns[, -1]</pre>
# Calculate the running z-scores
lambda <- 0.9
zscores <- HighFreq::run_zscores(response=response, predictor=predictor, lambda=lambda)
# Plot the running z-scores
datav <- cbind(cumsum(response), zscores[, 1])</pre>
colnames(datav) <- c("XLF", "zscores")</pre>
colnamev <- colnames(datav)</pre>
dygraphs::dygraph(datav, main="Z-Scores of XLF Versus VTI and IEF") %>%
  dyAxis("y", label=colnamev[1], independentTicks=TRUE) %>%
  dyAxis("y2", label=colnamev[2], independentTicks=TRUE) %>%
  dySeries(name=colnamev[1], axis="y", label=colnamev[1], strokeWidth=1, col="blue") %>%
  dySeries(name=colnamev[2], axis="y2", label=colnamev[2], strokeWidth=1, col="red")
## End(Not run)
```

save\_rets

Load, scrub, aggregate, and rbind multiple days of TAQ data for a single symbol. Calculate returns and save them to a single '\*.RData' file.

## **Description**

Load, scrub, aggregate, and rbind multiple days of *TAQ* data for a single symbol. Calculate returns and save them to a single '\*.RData' file.

### Usage

```
save_rets(
  symbol,
  data_dir = "E:/mktdata/sec/",
  output_dir = "E:/output/data/",
  look_back = 51,
  vol_mult = 2,
  period = "minutes",
  tzone = "America/New_York"
)
```

### **Details**

The function save\_rets loads multiple days of TAQ data, then scrubs, aggregates, and rbinds them into a OHLC time series. It then calculates returns using function ohlc\_returns(), and stores them in a variable named 'symbol.rets', and saves them to a file called 'symbol.rets.RData'. The TAQ data files are assumed to be stored in separate directories for each 'symbol'. Each 'symbol' has its own directory (named 'symbol') in the 'data\_dir' directory. Each 'symbol' directory contains multiple daily '\*.RData' files, each file containing one day of TAQ data.

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# Value

A time series of returns and volume in xts format.

# **Examples**

```
## Not run:
save_rets("SPY")
## End(Not run)
```

save\_rets\_ohlc

Load OHLC time series data for a single symbol, calculate its returns, and save them to a single '\*.RData' file, without aggregation.

# Description

Load *OHLC* time series data for a single symbol, calculate its returns, and save them to a single '\*.RData' file, without aggregation.

# Usage

```
save_rets_ohlc(
   symbol,
   data_dir = "E:/output/data/",
   output_dir = "E:/output/data/")
```

#### **Details**

The function save\_rets\_ohlc() loads *OHLC* time series data from a single file. It then calculates returns using function ohlc\_returns(), and stores them in a variable named 'symbol.rets', and saves them to a file called 'symbol.rets.RData'.

# Value

A time series of returns and volume in xts format.

```
## Not run:
save_rets_ohlc("SPY")
## End(Not run)
```

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| save_scrub_agg | Load, scrub, aggregate, and rbind multiple days of TAQ data for a single symbol, and save the OHLC time series to a single '*.RData' |
|----------------|--|
|                | file.  |

# **Description**

Load, scrub, aggregate, and rbind multiple days of TAQ data for a single symbol, and save the OHLC time series to a single '\*.RData' file.

# Usage

```
save_scrub_agg(
  symbol,
  data_dir = "E:/mktdata/sec/",
  output_dir = "E:/output/data/",
  look_back = 51,
  vol_mult = 2,
  period = "minutes",
  tzone = "America/New_York"
)
```

### **Arguments**

symbol A character string representing symbol or ticker.

data\_dir A character string representing directory containing input '\*.RData' files.

output\_dir A character string representing directory containing output '\*.RData' files.

# **Details**

The function save\_scrub\_agg() loads multiple days of TAQ data, then scrubs, aggregates, and rbinds them into a OHLC time series, and finally saves it to a single '\*.RData' file. The OHLC time series is stored in a variable named 'symbol', and then it's saved to a file named 'symbol. RData' in the 'output\_dir' directory. The TAQ data files are assumed to be stored in separate directories for each 'symbol'. Each 'symbol' has its own directory (named 'symbol') in the 'data\_dir' directory. Each 'symbol' directory contains multiple daily '\*.RData' files, each file containing one day of TAQ data.

## Value

An OHLC time series in xts format.

```
## Not run:
# set data directories
data_dir <- "C:/Develop/data/hfreq/src/"
output_dir <- "C:/Develop/data/hfreq/scrub/"
symbol <- "SPY"
# Aggregate SPY TAQ data to 15-min OHLC bar data, and save the data to a file
save_scrub_agg(symbol=symbol, data_dir=data_dir, output_dir=output_dir, period="15 min")
## End(Not run)</pre>
```

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save\_taq

Load and scrub multiple days of TAQ data for a single symbol, and save it to multiple '\*.RData' files.

# **Description**

Load and scrub multiple days of TAQ data for a single symbol, and save it to multiple '\*.RData' files

# Usage

```
save_taq(
  symbol,
  data_dir = "E:/mktdata/sec/",
  output_dir = "E:/output/data/",
  look_back = 51,
  vol_mult = 2,
  tzone = "America/New_York"
)
```

# **Details**

The function save\_taq() loads multiple days of TAQ data, scrubs it, and saves the scrubbed TAQ data to individual '\*.RData' files. It uses the same file names for output as the input file names. The TAQ data files are assumed to be stored in separate directories for each 'symbol'. Each 'symbol' has its own directory (named 'symbol') in the 'data\_dir' directory. Each 'symbol' directory contains multiple daily '\*.RData' files, each file containing one day of TAQ data.

# Value

a TAQ time series in xts format.

# **Examples**

```
## Not run:
save_taq("SPY")
## End(Not run)
```

scrub\_agg

Scrub a single day of TAQ data, aggregate it, and convert to OHLC format.

# Description

Scrub a single day of TAQ data, aggregate it, and convert to OHLC format.

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### Usage

```
scrub_agg(
  taq,
  look_back = 51,
  vol_mult = 2,
  period = "minutes",
  tzone = "America/New_York"
)
```

# **Arguments**

period

The aggregation period.

# **Details**

The function scrub\_agg() performs:

- index timezone conversion,
- data subset to trading hours,
- removal of duplicate time stamps,
- scrubbing of quotes with suspect bid-offer spreads,
- scrubbing of quotes with suspect price jumps,
- cbinding of mid prices with volume data,
- aggregation to OHLC using function to.period() from package xts,

Valid 'period' character strings include: "minutes", "3 min", "5 min", "10 min", "15 min", "30 min", and "hours". The time index of the output time series is rounded up to the next integer multiple of 'period'.

#### Value

A *OHLC* time series in *xts* format.

```
# Create random TAQ prices
taq <- HighFreq::random_taq()
# Aggregate to ten minutes OHLC data
ohlc <- HighFreq::scrub_agg(taq, period="10 min")
chart_Series(ohlc, name="random prices")
# scrub and aggregate a single day of SPY TAQ data to OHLC
ohlc <- HighFreq::scrub_agg(taq=HighFreq::SPY_TAQ)
chart_Series(ohlc, name=symbol)</pre>
```

scrub\_taq 99

scrub\_taq

Scrub a single day of TAQ data in xts format, without aggregation.

### **Description**

Scrub a single day of TAQ data in xts format, without aggregation.

#### Usage

```
scrub_taq(taq, look_back = 51, vol_mult = 2, tzone = "America/New_York")
```

### **Arguments**

taq TAQ A time series in xts format.

tzone The timezone to convert.

#### **Details**

The function scrub\_taq() performs the same scrubbing operations as scrub\_agg, except it doesn't aggregate, and returns the *TAQ* data in *xts* format.

## Value

A TAQ time series in xts format.

# **Examples**

```
taq <- HighFreq::scrub_taq(taq=HighFreq::SPY_TAQ, look_back=11, vol_mult=1)
# Create random TAQ prices and scrub them
taq <- HighFreq::random_taq()
taq <- HighFreq::scrub_taq(taq=taq)
taq <- HighFreq::scrub_taq(taq=taq, look_back=11, vol_mult=1)</pre>
```

season\_ality

Perform seasonality aggregations over a single-column xts time series.

# Description

Perform seasonality aggregations over a single-column xts time series.

# Usage

```
season_ality(xtes, indeks = format(zoo::index(xtes), "%H:%M"))
```

# **Arguments**

xtes A single-column xts time series.

indeks A vector of *character* strings representing points in time, of the same length as

the argument xtes.

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#### **Details**

The function season\_ality() calculates the mean of values observed at the same points in time specified by the argument indeks. An example of a daily seasonality aggregation is the average price of a stock between 9:30AM and 10:00AM every day, over many days. The argument indeks is passed into function tapply(), and must be the same length as the argument xtes.

#### Value

An xts time series with mean aggregations over the seasonality interval.

# **Examples**

```
# Calculate running variance of each minutely OHLC bar of data
xtes <- ohlc_variance(HighFreq::SPY)
# Remove overnight variance spikes at "09:31"
indeks <- format(index(xtes), "%H:%M")
xtes <- xtes[!indeks=="09:31", ]
# Calculate daily seasonality of variance
var_seasonal <- season_ality(xtes=xtes)
chart_Series(x=var_seasonal, name=paste(colnames(var_seasonal),
    "daily seasonality of variance"))</pre>
```

sim\_ar

Simulate autoregressive returns by recursively filtering a matrix of innovations through a matrix of autoregressive coefficients.

# **Description**

Simulate *autoregressive* returns by recursively filtering a *matrix* of innovations through a *matrix* of *autoregressive* coefficients.

# Usage

```
sim_ar(coeff, innov)
```

# **Arguments**

innov A single-column *matrix* of innovations.

coeff A single-column *matrix* of *autoregressive* coefficients.

#### **Details**

The function sim\_ar() recursively filters the *matrix* of innovations innov through the *matrix* of *autoregressive* coefficients coeff, using fast RcppArmadillo C++ code.

The function  $sim_ar()$  simulates an *autoregressive* process AR(n) of order n:

$$r_i = \varphi_1 r_{i-1} + \varphi_2 r_{i-2} + \ldots + \varphi_n r_{i-n} + \xi_i$$

Where  $r_i$  is the simulated output time series,  $\varphi_i$  are the *autoregressive* coefficients, and  $\xi_i$  are the standard normal *innovations*.

The order n of the *autoregressive* process AR(n), is equal to the number of rows of the *autoregressive* coefficients coeff.

The function sim\_ar() performs the same calculation as the standard R function filter(x=innov, filter=coeff, method="recursive"), but it's several times faster.

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#### Value

A single-column matrix of simulated returns, with the same number of rows as the argument innov.

#### **Examples**

```
## Not run:
# Define AR coefficients
coeff <- matrix(c(0.1, 0.3, 0.5))
# Calculate matrix of innovations
innov <- matrix(rnorm(1e4, sd=0.01))</pre>
# Calculate recursive filter using filter()
filtered <- filter(innov, filter=coeff, method="recursive")</pre>
# Calculate recursive filter using RcppArmadillo
returns <- HighFreq::sim_ar(coeff, innov)</pre>
\# Compare the two methods
all.equal(as.numeric(returns), as.numeric(filtered))
# Compare the speed of RcppArmadillo with R code
library(microbenchmark)
summary(microbenchmark(
  Rcpp=HighFreq::sim_ar(coeff, innov),
  Rcode=filter(innov, filter=coeff, method="recursive"),
  times=10))[, c(1, 4, 5)] # end microbenchmark summary
## End(Not run)
```

sim\_df

Simulate a Dickey-Fuller process using Rcpp.

# **Description**

Simulate a *Dickey-Fuller* process using *Rcpp*.

#### **Usage**

```
sim_df(init_price, eq_price, theta, coeff, innov)
```

### **Arguments**

The initial price. init\_price eq\_price The equilibrium price. theta The strength of mean reversion. coeff A single-column matrix of autoregressive coefficients. A single-column *matrix* of innovations (random numbers).

# **Details**

innov

The function sim\_df() simulates the following *Dickey-Fuller* process:

$$r_i = \theta \left( \mu - p_{i-1} \right) + \varphi_1 r_{i-1} + \ldots + \varphi_n r_{i-n} + \xi_i$$
$$p_i = p_{i-1} + r_i$$

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Where  $r_i$  and  $p_i$  are the simulated returns and prices,  $\theta$  and  $\mu$  are the *Ornstein-Uhlenbeck* parameters,  $\varphi_i$  are the *autoregressive* coefficients, and  $\xi_i$  are the normal *innovations*. The recursion starts with:  $r_1 = \xi_1$  and  $p_1 = init\_price$ .

The Dickey-Fuller process is a combination of an Ornstein-Uhlenbeck process and an autoregressive process. The order n of the autoregressive process AR(n), is equal to the number of rows of the autoregressive coefficients coeff.

The function sim\_df() simulates the *Dickey-Fuller* process using fast *Rcpp* C++ code.

The function sim\_df() returns a single-column matrix representing the time series of prices.

#### Value

A single-column matrix of simulated prices, with the same number of rows as the argument innov.

# **Examples**

```
## Not run:
# Define the Ornstein-Uhlenbeck model parameters
init_price <- 1.0
eq_price <- 2.0
thetav <- 0.01
# Define AR coefficients
coeff <- matrix(c(0.1, 0.3, 0.5))
# Calculate matrix of standard normal innovations
innov <- matrix(rnorm(1e3, sd=0.01))
# Simulate Dickey-Fuller process using Rcpp
prices <- HighFreq::sim_df(init_price=init_price, eq_price=eq_price, theta=thetav, coeff=coeff, innov=innov)
plot(prices, t="1", main="Simulated Dickey-Fuller Prices")
## End(Not run)</pre>
```

Simulate or estimate the rolling variance under a GARCH(1,1) pro-

# Description

sim\_garch

Simulate or estimate the rolling variance under a *GARCH*(1,1) process using *Rcpp*.

# Usage

```
sim_garch(omega, alpha, beta, innov, is_random = TRUE)
```

cess using Rcpp.

# Arguments

| omega     | Parameter proportional to the long-term average level of variance.   |
|-----------|--|
| alpha     | The weight associated with recent realized variance updates.   |
| beta      | The weight associated with the past variance estimates.  |
| innov     | A single-column <i>matrix</i> of innovations.  |
| is_random | Boolean argument: Are the innovations random numbers or historical returns? (The default is is_random = TRUE.) |

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#### **Details**

The function  $sim_garch()$  simulates or estimates the rolling variance under a GARCH(1,1) process using Rcpp.

If is\_random = TRUE (the default) then the innovations innov are treated as random numbers  $\xi_i$  and the GARCH(1,1) process is given by:

$$r_i = \sigma_{i-1} \xi_i$$
 
$$\sigma_i^2 = \omega + \alpha r_i^2 + \beta \sigma_{i-1}^2$$

Where  $r_i$  and  $\sigma_i^2$  are the simulated returns and variance, and  $\omega$ ,  $\alpha$ , and  $\beta$  are the *GARCH* parameters, and  $\xi_i$  are standard normal *innovations*.

The long-term equilibrium level of the simulated variance is proportional to the parameter  $\omega$ :

$$\sigma^2 = \frac{\omega}{1 - \alpha - \beta}$$

So the sum of  $\alpha$  plus  $\beta$  should be less than 1, otherwise the volatility becomes explosive.

If is\_random = FALSE then the function  $sim_garch()$  estimates the rolling variance from the historical returns. The innovations innov are equal to the historical returns  $r_i$  and the GARCH(1,1) process is simply:

$$\sigma_i^2 = \omega + \alpha r_i^2 + \beta \sigma_{i-1}^2$$

Where  $\sigma_i^2$  is the rolling variance.

The above should be viewed as a formula for *estimating* the rolling variance from the historical returns, rather than simulating them. It represents exponential smoothing of the squared returns with a decay factor equal to  $\beta$ .

The function sim\_garch() simulates the *GARCH* process using fast *Rcpp* C++ code.

# Value

A *matrix* with two columns and with the same number of rows as the argument innov. The first column are the simulated returns and the second column is the variance.

```
## Not run:
# Define the GARCH model parameters
alpha <- 0.79
betav <- 0.2
om_ega <- 1e-4*(1-alpha-betav)
# Calculate matrix of standard normal innovations
innov <- matrix(rnorm(1e3))</pre>
# Simulate the GARCH process using Rcpp
garch_data <- HighFreq::sim_garch(omega=om_ega, alpha=alpha, beta=betav, innov=innov)</pre>
# Plot the GARCH rolling volatility and cumulative returns
plot(sqrt(garch_data[, 2]), t="1", main="Simulated GARCH Volatility", ylab="volatility")
plot(cumsum(garch_data[, 1]), t="1", main="Simulated GARCH Cumulative Returns", ylab="cumulative returns")
# Calculate historical VTI returns
returns <- na.omit(rutils::etfenv$returns$VTI)</pre>
# Estimate the GARCH volatility of VTI returns
garch_data <- HighFreq::sim_garch(omega=om_ega, alpha=alpha, beta=betav,</pre>
  innov=returns, is_random=FALSE)
# Plot dygraph of the estimated GARCH volatility
dygraphs::dygraph(xts::xts(sqrt(garch_data[, 2]), index(returns)),
  main="Estimated GARCH Volatility of VTI")
```

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## End(Not run)

sim\_ou

Simulate an Ornstein-Uhlenbeck process using Rcpp.

# **Description**

Simulate an Ornstein-Uhlenbeck process using Rcpp.

# Usage

```
sim_ou(init_price, eq_price, theta, innov)
```

# **Arguments**

init\_price The initial price.

eq\_price The equilibrium price.

theta The strength of mean reversion.

innov A single-column *matrix* of innovations (random numbers).

#### **Details**

The function sim\_ou() simulates the following *Ornstein-Uhlenbeck* process:

$$r_i = p_i - p_{i-1} = \theta (\mu - p_{i-1}) + \xi_i$$
  
$$p_i = p_{i-1} + r_i$$

Where  $r_i$  and  $p_i$  are the simulated returns and prices,  $\theta$ ,  $\mu$ , and  $\sigma$  are the *Ornstein-Uhlenbeck* parameters, and  $\xi_i$  are the standard *innovations*. The recursion starts with:  $r_1 = \xi_1$  and  $p_1 = init\_price$ .

The function  $sim_ou()$  simulates the percentage returns as equal to the difference between the equilibrium price  $\mu$  minus the latest price  $p_{i-1}$ , times the mean reversion parameter  $\theta$ , plus a random normal innovation. The log prices are calculated as the sum of returns (not compounded), so they can become negative.

The function sim\_ou() simulates the *Ornstein-Uhlenbeck* process using fast *Rcpp* C++ code.

The function sim\_ou() returns a single-column *matrix* representing the *time series* of simulated prices.

#### Value

A single-column matrix of simulated prices, with the same number of rows as the argument innov.

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#### **Examples**

```
## Not run:
# Define the Ornstein-Uhlenbeck model parameters
init_price <- 0.0
eq_price <- 1.0
sigmav <- 0.01
thetav <- 0.01
innov <- matrix(rnorm(1e3))
# Simulate Ornstein-Uhlenbeck process using Rcpp
prices <- HighFreq::sim_ou(init_price=init_price, eq_price=eq_price, volat=sigmav, theta=thetav, innov=innov
plot(prices, t="1", main="Simulated Ornstein-Uhlenbeck Prices", ylab="prices")
## End(Not run)</pre>
```

sim\_schwartz

Simulate a Schwartz process using Rcpp.

# Description

Simulate a Schwartz process using Rcpp.

#### Usage

```
sim_schwartz(init_price, eq_price, theta, innov)
```

#### **Arguments**

init\_price The initial price.

eq\_price The equilibrium price.

theta The strength of mean reversion.

innov A single-column *matrix* of innovations (random numbers).

# **Details**

The function sim\_schwartz() simulates a *Schwartz* process using fast *Rcpp* C++ code.

The *Schwartz* process is the exponential of the *Ornstein-Uhlenbeck* process, and similar comments apply to it. The prices are calculated as the exponentially compounded returns, so they are never negative. The log prices can be obtained by taking the logarithm of the prices.

The function sim\_schwartz() simulates the percentage returns as equal to the difference between the equilibrium price  $\mu$  minus the latest price  $p_{i-1}$ , times the mean reversion parameter  $\theta$ , plus a random normal innovation.

The function sim\_schwartz() returns a single-column *matrix* representing the *time series* of simulated prices.

# Value

A single-column matrix of simulated prices, with the same number of rows as the argument innov.

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#### **Examples**

```
## Not run:
# Define the Schwartz model parameters
init_price <- 1.0
eq_price <- 2.0
thetav <- 0.01
innov <- matrix(rnorm(1e3, sd=0.01))
# Simulate Schwartz process using Rcpp
prices <- HighFreq::sim_schwartz(init_price=init_price, eq_price=eq_price, theta=thetav, innov=innov)
plot(prices, t="1", main="Simulated Schwartz Prices", ylab="prices")
## End(Not run)</pre>
```

which\_extreme

Calculate a Boolean vector that identifies extreme tail values in a single-column xts time series or vector, over a rolling look-back interval.

# **Description**

Calculate a *Boolean* vector that identifies extreme tail values in a single-column *xts* time series or vector, over a rolling look-back interval.

## Usage

```
which_extreme(xtes, look_back = 51, vol_mult = 2)
```

### **Arguments**

xtes A single-column xts time series, or a numeric or Boolean vector.

look\_back The number of data points in rolling look-back interval for estimating rolling

quantile.

vol\_mult The quantile multiplier.

### **Details**

The function which\_extreme() calculates a *Boolean* vector, with TRUE for values that belong to the extreme tails of the distribution of values.

The function which\_extreme() applies a version of the Hampel median filter to identify extreme values, but instead of using the median absolute deviation (MAD), it uses the 0.9 quantile values calculated over a rolling look-back interval.

Extreme values are defined as those that exceed the product of the multiplier times the rolling quantile. Extreme values belong to the fat tails of the recent (trailing) distribution of values, so they are present only when the trailing distribution of values has fat tails. If the trailing distribution of values is closer to normal (without fat tails), then there are no extreme values.

The quantile multiplier vol\_mult controls the threshold at which values are identified as extreme. Smaller quantile multiplier values will cause more values to be identified as extreme.

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#### Value

A Boolean vector with the same number of rows as the input time series or vector.

### **Examples**

```
# Create local copy of SPY TAQ data
taq <- HighFreq::SPY_TAQ
# scrub quotes with suspect bid-offer spreads
bid_offer <- taq[, "Ask.Price"] - taq[, "Bid.Price"]
sus_pect <- which_extreme(bid_offer, look_back=51, vol_mult=3)
# Remove suspect values
taq <- taq[!sus_pect]</pre>
```

which\_jumps

Calculate a Boolean vector that identifies isolated jumps (spikes) in a single-column xts time series or vector, over a rolling interval.

# **Description**

Calculate a *Boolean* vector that identifies isolated jumps (spikes) in a single-column *xts* time series or vector, over a rolling interval.

# Usage

```
which_jumps(xtes, look_back = 51, vol_mult = 2)
```

## **Details**

The function which\_jumps() calculates a *Boolean* vector, with TRUE for values that are isolated jumps (spikes).

The function which\_jumps() applies a version of the Hampel median filter to identify jumps, but instead of using the median absolute deviation (MAD), it uses the 0.9 quantile of returns calculated over a rolling interval. This is in contrast to function which\_extreme(), which applies a Hampel filter to the values themselves, instead of the returns. Returns are defined as simple differences between neighboring values.

Jumps (or spikes), are defined as isolated values that are very different from the neighboring values, either before or after. Jumps create pairs of large neighboring returns of opposite sign.

Jumps (spikes) must satisfy two conditions:

- 1. Neighboring returns both exceed a multiple of the rolling quantile,
- 2. The sum of neighboring returns doesn't exceed that multiple.

The quantile multiplier vol\_mult controls the threshold at which values are identified as jumps. Smaller quantile multiplier values will cause more values to be identified as jumps.

# Value

A Boolean vector with the same number of rows as the input time series or vector.

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```
# Create local copy of SPY TAQ data
taq <- SPY_TAQ
# Calculate mid prices
mid_prices <- 0.5 * (taq[, "Bid.Price"] + taq[, "Ask.Price"])
# Replace whole rows containing suspect price jumps with NA, and perform locf()
taq[which_jumps(mid_prices, look_back=31, vol_mult=1.0), ] <- NA
taq <- xts:::na.locf.xts(taq)</pre>
```