Package 'HighFreq'

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`agg_ohlc` *Aggregate a time series of data into a single bar of* OHLC *data.*

Description

Aggregate a time series of data into a single bar of *OHLC* data.

Usage

```
agg_ohlc(tseries)
```

Arguments

`tseries`	A *time series* or a *matrix* with multiple columns of data.

Details

The function `agg_ohlc()` aggregates a time series of data into a single bar of *OHLC* data. It can accept either a single column of data or four columns of *OHLC* data. It can also accept an additional column containing the trading volume.

The function `agg_ohlc()` calculates the *open* value as equal to the *open* value of the first row of `tseries`. The *high* value as the maximum of the *high* column of `tseries`. The *low* value as the minimum of the *low* column of `tseries`. The *close* value as the *close* of the last row of `tseries`. The *volume* value as the sum of the *volume* column of `tseries`.

For a single column of data, the *open*, *high*, *low*, and *close* values are all the same.

Value

A *matrix* containing a single row, with the *open*, *high*, *low*, and *close* values, and also the total *volume* (if provided as either the second or fifth column of `tseries`).

Examples

```
## Not run:
# Define matrix of OHLC data
oh_lc <- coredata(rutils::etf_env$VTI[, 1:5])
# Aggregate to single row matrix
ohlc_agg <- HighFreq::agg_ohlc(oh_lc)
# Compare with calculation in R
all.equal(drop(ohlc_agg),
  c(oh_lc[1, 1], max(oh_lc[, 2]), min(oh_lc[, 3]), oh_lc[NROW(oh_lc), 4], sum(oh_lc[, 5])),
   check.attributes=FALSE)

## End(Not run)
```

`agg_stats_r` *Calculate the aggregation (weighted average) of a statistical estimator over a* OHLC *time series using* R *code.*

Description

Calculate the aggregation (weighted average) of a statistical estimator over a *OHLC* time series using R code.

Usage

```
agg_stats_r(oh_lc, calc_bars = "run_variance", weight_ed = TRUE, ...)
```

Arguments

`...`	additional parameters to the function `calc_bars`.
`oh_lc`	An *OHLC* time series of prices and trading volumes, in *xts* format.
`calc_bars`	A *character* string representing a function for calculating statistics for individual *OHLC* bars.
`weight_ed`	*Boolean* argument: should estimate be weighted by the trading volume? (default is `TRUE`)

Details

The function `agg_stats_r()` calculates a single number representing the volume weighted average of statistics of individual *OHLC* bars. It first calls the function `calc_bars` to calculate a vector of statistics for the *OHLC* bars. For example, the statistic may simply be the difference between the *High* minus *Low* prices. In this case the function `calc_bars` would calculate a vector of *High* minus *Low* prices. The function `agg_stats_r()` then calculates a trade volume weighted average of the vector of statistics.

The function `agg_stats_r()` is implemented in R code.

Value

A single *numeric* value equal to the volume weighted average of an estimator over the time series.

Examples

```
# Calculate weighted average variance for SPY (single number)
vari_ance <- agg_stats_r(oh_lc=HighFreq::SPY, calc_bars="run_variance")
# Calculate time series of daily skew estimates for SPY
skew_daily <- apply.daily(x=HighFreq::SPY, FUN=agg_stats_r, calc_bars="run_skew")
```

`back_test` *Simulate (backtest) a rolling portfolio optimization strategy, using* `RcppArmadillo`.

Description

Simulate (backtest) a rolling portfolio optimization strategy, using `RcppArmadillo`.

Usage

```
back_test(
  excess,
  returns,
  startp,
  endp,
  method = "rank_sharpe",
  eigen_thresh = 0.001,
  eigen_max = 0L,
  con_fi = 0.1,
  alpha = 0,
  scale = TRUE,
  vol_target = 0.01,
  coeff = 1,
  bid_offer = 0
)
```

Arguments

`returns`	A *time series* or a *matrix* of returns data (the returns in excess of the risk-free rate).
`excess`	A *time series* or a *matrix* of excess returns data (the returns in excess of the risk-free rate).
`startp`	An *integer vector* of start points.
`endp`	An *integer vector* of end points.
`coeff`	A *numeric* multiplier of the weights. (The default is `1`)
`bid_offer`	A *numeric* bid-offer spread (the default is `0`)
`method`	A *string* specifying the objective function for calculating the weights (see Details) (the default is `method = "rank_sharpe"`)

eigen_thresh	A *numeric* threshold level for discarding small singular values in order to regularize the inverse of the returns matrix (the default is 0.001).
eigen_max	An *integer* equal to the number of singular values used for calculating the regularized inverse of the returns matrix (the default is 0 - equivalent to eigen_max equal to the number of columns of returns).
con_fi	The confidence level for calculating the quantiles (the default is con_fi = 0.75).
alpha	The shrinkage intensity between 0 and 1. (the default is 0).
scale	A *Boolean* specifying whether the weights should be scaled (the default is scale = TRUE).
vol_target	A *numeric* volatility target for scaling the weights (the default is 0.001)

Details

The function back_test() performs a backtest simulation of a rolling portfolio optimization strategy over a *vector* of endp.

It performs a loop over the end points endp, and subsets the *matrix* of excess returns excess along its rows, between the corresponding end point and the start point. It passes the subset matrix of excess returns into the function calc_weights(), which calculates the optimal portfolio weights. The arguments eigen_max, alpha, method, and scale are also passed to the function calc_weights().

The function back_test() multiplies the weights by the coefficient coeff (with default equal to 1), which allows reverting a strategy if co_eff = -1.

The function back_test() then multiplies the weights times the future portfolio returns, to calculate the out-of-sample strategy returns.

The function back_test() calculates the transaction costs by multiplying the bid-offer spread bid_offer times the absolute difference between the current weights minus the weights from the previous period. Then it subtracts the transaction costs from the out-of-sample strategy returns.

The function back_test() returns a *time series* (column *vector*) of strategy returns, of the same length as the number of rows of returns.

Value

A column *vector* of strategy returns, with the same length as the number of rows of returns.

Examples

```
## Not run:
# Calculate the ETF daily excess returns
re_turns <- na.omit(rutils::etf_env$re_turns[, 1:16])
# risk_free is the daily risk-free rate
risk_free <- 0.03/260
ex_cess <- re_turns - risk_free
# Define monthly end points without initial warmpup period
end_p <- rutils::calc_endpoints(re_turns, inter_val="months")
end_p <- end_p[end_p > 0]
len_gth <- NROW(end_p)
# Define 12-month look-back interval and start points over sliding window
look_back <- 12
start_p <- c(rep_len(1, look_back-1), end_p[1:(len_gth-look_back+1)])
# Define shrinkage and regularization intensities
al_pha <- 0.5
eigen_max <- 3
```

```
# Simulate a monthly rolling portfolio optimization strategy
pnl_s <- HighFreq::back_test(ex_cess, re_turns,
                             start_p-1, end_p-1,
                             eigen_max = eigen_max,
                             alpha = al_pha)
pnl_s <- xts::xts(pnl_s, index(re_turns))
colnames(pnl_s) <- "strat_rets"
# Plot dygraph of strategy
dygraphs::dygraph(cumsum(pnl_s),
  main="Cumulative Returns of Max Sharpe Portfolio Strategy")

## End(Not run)
```

`calc_eigen` *Calculate the eigen decomposition of the covariance* matrix *of returns data using* `RcppArmadillo`.

Description

Calculate the eigen decomposition of the covariance *matrix* of returns data using `RcppArmadillo`.

Usage

```
calc_eigen(tseries)
```

Arguments

`tseries`	A *time series* or *matrix* of returns data.

Details

The function `calc_eigen()` first calculates the covariance *matrix* of `tseries`, and then calculates the eigen decomposition of the covariance *matrix*.

Value

A list with two elements: a *vector* of eigenvalues (named "values"), and a *matrix* of eigenvectors (named "vectors").

Examples

```
## Not run:
# Create matrix of random data
da_ta <- matrix(rnorm(5e6), nc=5)
# Calculate eigen decomposition
ei_gen <- HighFreq::calc_eigen(scale(da_ta, scale=FALSE))
# Calculate PCA
pc_a <- prcomp(da_ta)
# Compare PCA with eigen decomposition
all.equal(pc_a$sdev^2, drop(ei_gen$values))
all.equal(abs(unname(pc_a$rotation)), abs(ei_gen$vectors))
# Compare the speed of Rcpp with R code
summary(microbenchmark(
```

```
  Rcpp=HighFreq::calc_eigen(da_ta),
  Rcode=prcomp(da_ta),
  times=10))[, c(1, 4, 5)]  # end microbenchmark summary

## End(Not run)
```

`calc_endpoints` *Calculate a vector of end points that divides a vector into equal intervals.*

Description

Calculate a vector of end points that divides a vector into equal intervals.

Usage

```
calc_endpoints(length, step = 1L, stub = 0L)
```

Arguments

`length`	An *integer* equal to the length of the vector to be divided into equal intervals.
`step`	The number of elements in each interval between neighboring end points.
`stub`	An *integer* value equal to the first end point for calculating the end points.

Details

The end points are a vector of integers which divide a vector of length equal to `length` into equally spaced intervals. If a whole number of intervals doesn't fit over the vector, then `calc_endpoints()` adds a stub interval at the end.

The first end point is equal to the argument `step`, unless the argument `stub` is provided, and then it becomes the first end point.

For example, consider the end points for a vector of length `20` divided into intervals of length `step=5`: `0,5,10,15,20`. In order for all the differences between neighboring end points to be equal to `5`, the first end point is set equal to `0`. But `0` doesn't correspond to any vector element, so `calc_endpoints()` doesn't include it and it only retains the non-zero end points equal to: `5,10,15,20`.

Since indexing in `C++` code starts at `0`, then `calc_endpoints()` shifts the end points by `-1` and returns the vector equal to `4,9,14,19`.

If `stub = 1` then the first end point is equal to `1` and the end points are equal to: `1,6,11,16,20`. The extra stub interval at the end is equal to `4 = 20 -16`. And `calc_endpoints()` returns `0,5,10,15,19`. The first value is equal to `0` which is the index of the first element in `C++` code.

If `stub = 2` then the first end point is equal to `2`, with an extra stub interval at the end, and the end points are equal to: `2,7,12,17,20`. And `calc_endpoints()` returns `1,6,11,16,19`.

The function `calc_endpoints()` is similar to the function `rutils::calc_endpoints()` from package rutils.

But the end points are shifted by `-1` compared to `R` code because indexing starts at `0` in `C++` code, while it starts at `1` in `R` code. So if `calc_endpoints()` is used in `R` code then `1` should be added to it.

This works in R code because the vector element corresponding to index 0 is empty. For example, the R code: (4:1)[c(0,1)] produces 4. So in R we can select vector elements using the end points starting at zero.

In C++ the end points must be shifted by -1 compared to R code, because indexing starts at 0: -1,4,9,14,19. But there is no vector element corresponding to index -1. So in C++ we cannot select vector elements using the end points starting at -1. The solution is to drop the first placeholder end point.

Value

A vector of equally spaced *integers* representing the end points.

Examples

```
# Calculate end points without a stub interval
HighFreq::calc_endpoints(length=20, step=5)
# Calculate end points with a final stub interval
HighFreq::calc_endpoints(length=23, step=5)
# Calculate end points with initial and final stub intervals
HighFreq::calc_endpoints(length=20, step=5, stub=2)
# Calculate end points with initial and final stub intervals
HighFreq::calc_endpoints(length=20, step=5, stub=24)
```

---

calc_hurst *Calculate the Hurst exponent from the volatility ratio of aggregated returns.*

Description

Calculate the Hurst exponent from the volatility ratio of aggregated returns.

Usage

```
calc_hurst(tseries, step = 1L)
```

Arguments

tseries	A *time series* or a *matrix* of prices.
step	The number of periods in each interval between neighboring end points.

Details

The function calc_hurst() calculates the Hurst exponent from the ratios of the volatilities of aggregated returns.

The aggregated volatility σ_t scales (increases) with the length of the aggregation interval Δt raised to the power of the *Hurst exponent* H:

$$\sigma_t = \sigma \Delta t^H$$

Where σ is the daily return volatility.

The *Hurst exponent* H is equal to the logarithm of the ratio of the volatilities divided by the logarithm of the time interval Δt:

$$H = \frac{\log \sigma_t - \log \sigma}{\log \Delta t}$$

The function `calc_hurst()` calls the function `calc_var_ag()` to calculate the aggregated volatility σ_t.

Value

The Hurst exponent calculated from the variance of aggregated returns.

Examples

```
## Not run:
# Calculate the log prices
price_s <- na.omit(rutils::etf_env$price_s[, c("XLP", "VTI")])
price_s <- log(price_s)
# Calculate the Hurst exponent from 21 day aggregations
calc_hurst(price_s, step=21)

## End(Not run)
```

`calc_hurst_ohlc` *Calculate the Hurst exponent from the volatility ratio of aggregated* OHLC *prices.*

Description

Calculate the Hurst exponent from the volatility ratio of aggregated *OHLC* prices.

Usage

```
calc_hurst_ohlc(
  ohlc,
  step = 1L,
  method = "yang_zhang",
  lag_close = 0L,
  scale = TRUE,
  in_dex = 0L
)
```

Arguments

`ohlc`	A *time series* or a *matrix* of *OHLC* prices.
`step`	The number of periods in each interval between neighboring end points.
`method`	A *character* string representing the price range estimator for calculating the variance. The estimators include: • "close" close-to-close estimator, • "rogers_satchell" Rogers-Satchell estimator, • "garman_klass" Garman-Klass estimator,

- "garman_klass_yz" Garman-Klass with account for close-to-open price jumps,
- "yang_zhang" Yang-Zhang estimator,

(The default is the `method = "yang_zhang"`.)

`lag_close` A *vector* with the lagged *close* prices of the *OHLC time series*. This is an optional argument. (The default is `lag_close = 0`).

`scale` *Boolean* argument: Should the returns be divided by the time index, the number of seconds in each period? (The default is `scale = TRUE`).

`in_dex` A *vector* with the time index of the *time series*. This is an optional argument (the default is `in_dex = 0`).

Details

The function `calc_hurst_ohlc()` calculates the Hurst exponent from the ratios of the volatilities of aggregated *OHLC* prices.

The aggregated volatility σ_t scales (increases) with the length of the aggregation interval Δt raised to the power of the *Hurst exponent* H:

$$\sigma_t = \sigma \Delta t^H$$

Where σ is the daily return volatility.

The *Hurst exponent* H is equal to the logarithm of the ratio of the volatilities divided by the logarithm of the time interval Δt:

$$H = \frac{\log \sigma_t - \log \sigma}{\log \Delta t}$$

The function `calc_hurst_ohlc()` calls the function `calc_var_ohlc_ag()` to calculate the aggregated volatility σ_t.

Value

The Hurst exponent calculated from the variance ratio of aggregated *OHLC* prices.

Examples

```
## Not run:
# Calculate the log ohlc prices
oh_lc <- log(rutils::etf_env$VTI)
# Calculate the Hurst exponent from 21 day aggregations
calc_hurst_ohlc(oh_lc, step=21)

## End(Not run)
```

---

calc_inv *Calculate the regularized inverse of a rectangular* matrix *of data using Singular Value Decomposition (*SVD*).*

Description

Calculate the regularized inverse of a rectangular *matrix* of data using Singular Value Decomposition (*SVD*).

Usage

```
calc_inv(tseries, eigen_thresh = 0.001, eigen_max = 0L)
```

Arguments

tseries	A *time series* or *matrix* of returns data.
eigen_thresh	A *numeric* threshold level for discarding small singular values in order to regularize the inverse of the matrix tseries (the default is 0.001).
eigen_max	An *integer* equal to the number of singular values used for calculating the regularized inverse of the matrix tseries (the default is 0 - equivalent to eigen_max equal to the number of columns of tseries).

Details

The function calc_inv() calculates the regularized inverse of tseries using Singular Value Decomposition (*SVD*).

If eigen_max is given, then it calculates the regularized inverse from the *SVD* using the first eigen_max largest singular values. For example, if eigen_max = 3 then it only uses the 3 largest singular values. If eigen_max is set equal to the number of columns of tseries then it uses all the singular values without any regularization.

If eigen_max is not given then it calculates the regularized inverse using the function arma::pinv(). Then it discards small singular values that are less than the threshold level eigen_thresh.

Value

A *matrix* equal to the regularized inverse of the matrix tseries.

Examples

```
## Not run:
# Calculate ETF returns
re_turns <- na.omit(rutils::etf_env$re_turns)
# Calculate regularized inverse using RcppArmadillo
in_verse <- HighFreq::calc_inv(re_turns, eigen_max=3)
# Calculate regularized inverse from SVD in R
s_vd <- svd(re_turns)
eigen_max <- 1:3
inverse_r <-  s_vd$v[, eigen_max] %*% (t(s_vd$u[, eigen_max]) / s_vd$d[eigen_max])
# Compare RcppArmadillo with R
all.equal(in_verse, inverse_r)

## End(Not run)
```

---

calc_kurtosis *Calculate the kurtosis of the columns of a* time series *or a* matrix *using* RcppArmadillo.

Description

Calculate the kurtosis of the columns of a *time series* or a *matrix* using RcppArmadillo.

Usage

```
calc_kurtosis(tseries, method = "moment", con_fi = 0.75)
```

Arguments

tseries	A *time series* or a *matrix* of data.
method	A *string* specifying the type of the kurtosis model (the default is method = "moment" - see Details).
con_fi	The confidence level for calculating the quantiles (the default is con_fi = 0.75).

Details

The function calc_kurtosis() calculates the kurtosis of the columns of the *matrix* tseries using RcppArmadillo C++ code.

If method = "moment" (the default) then calc_kurtosis() calculates the fourth moment of the data. But it doesn't de-mean the columns of tseries because that requires copying the matrix tseries, so it's time-consuming.

If method = "quantile" then it calculates the skewness κ from the differences between the quantiles of the data as follows:

$$\kappa = \frac{q_\alpha - q_{1-\alpha}}{q_{0.75} - q_{0.25}}$$

Where α is the confidence level for calculating the quantiles.

If method = "nonparametric" then it calculates the kurtosis as the difference between the mean of the data minus its median, divided by the standard deviation.

If the number of rows of tseries is less than 3 then it returns zeros.

The code examples below compare the function calc_kurtosis() with the kurtosis calculated using R code.

Value

A single-row matrix with the kurtosis of the columns of tseries.

Examples

```
## Not run:
# Define a single-column time series of returns
re_turns <- na.omit(rutils::etf_env$re_turns$VTI)
# Calculate the moment kurtosis
HighFreq::calc_kurtosis(re_turns)
# Calculate the moment kurtosis in R
calc_kurtr <- function(x) {
  x <- (x-mean(x))
  sum(x^4)/var(x)^2/NROW(x)
}  # end calc_kurtr
all.equal(HighFreq::calc_kurtosis(re_turns),
  calc_kurtr(re_turns), check.attributes=FALSE)
# Compare the speed of RcppArmadillo with R code
library(microbenchmark)
summary(microbenchmark(
  Rcpp=HighFreq::calc_kurtosis(re_turns),
  Rcode=calc_kurtr(re_turns),
  times=10))[, c(1, 4, 5)]  # end microbenchmark summary
```

```
# Calculate the quantile kurtosis
HighFreq::calc_kurtosis(re_turns, method="quantile", con_fi=0.9)
# Calculate the quantile kurtosis in R
calc_kurtq <- function(x, a=0.9) {
   quantile_s <- quantile(x, c(1-a, 0.25, 0.75, a), type=5)
   (quantile_s[4] - quantile_s[1])/(quantile_s[3] - quantile_s[2])
}  # end calc_kurtq
all.equal(drop(HighFreq::calc_kurtosis(re_turns, method="quantile", con_fi=0.9)),
  calc_kurtq(re_turns, a=0.9), check.attributes=FALSE)
# Compare the speed of RcppArmadillo with R code
summary(microbenchmark(
  Rcpp=HighFreq::calc_kurtosis(re_turns, method="quantile"),
  Rcode=calc_kurtq(re_turns),
  times=10))[, c(1, 4, 5)]  # end microbenchmark summary
# Calculate the nonparametric kurtosis
HighFreq::calc_kurtosis(re_turns, method="nonparametric")
# Compare HighFreq::calc_kurtosis() with R nonparametric kurtosis
all.equal(drop(HighFreq::calc_kurtosis(re_turns, method="nonparametric")),
  (mean(re_turns)-median(re_turns))/sd(re_turns),
  check.attributes=FALSE)
# Compare the speed of RcppArmadillo with R code
summary(microbenchmark(
  Rcpp=HighFreq::calc_kurtosis(re_turns, method="nonparametric"),
  Rcode=(mean(re_turns)-median(re_turns))/sd(re_turns),
  times=10))[, c(1, 4, 5)]  # end microbenchmark summary

## End(Not run)
```

`calc_lm` *Perform multivariate linear regression using least squares and return a named list of regression coefficients, their t-values, and p-values.*

Description

Perform multivariate linear regression using least squares and return a named list of regression coefficients, their t-values, and p-values.

Usage

```
calc_lm(response, design)
```

Arguments

`response`	A single-column *time series* or a *vector* of response data.
`design`	A *time series* or a *matrix* of design data (predictor or explanatory data).

Details

The function `calc_lm()` performs the same calculations as the function `lm()` from package *stats*. It uses `RcppArmadillo` `C++` code so it's several times faster than `lm()`. The code was inspired by this article (but it's not identical to it): http://gallery.rcpp.org/articles/fast-linear-model-with-armadillo/

Value

A named list with three elements: a *matrix* of coefficients (named *"coefficients"*), the *z-score* of the last residual (named *"z_score"*), and a *vector* with the R-squared and F-statistic (named *"stats"*). The numeric *matrix* of coefficients named *"coefficients"* contains the alpha and beta coefficients, and their *t-values* and *p-values*.

Examples

```
## Not run:
# Calculate historical returns
re_turns <- na.omit(rutils::etf_env$re_turns[, c("XLF", "VTI", "IEF")])
# Response equals XLF returns
res_ponse <- re_turns[, 1]
# Design matrix equals VTI and IEF returns
de_sign <- re_turns[, -1]
# Perform multivariate regression using lm()
reg_model <- lm(res_ponse ~ de_sign)
sum_mary <- summary(reg_model)
# Perform multivariate regression using calc_lm()
reg_arma <- HighFreq::calc_lm(response=res_ponse, design=de_sign)
# Compare the outputs of both functions
all.equal(reg_arma$coefficients[, "coeff"], unname(coef(reg_model)))
all.equal(unname(reg_arma$coefficients), unname(sum_mary$coefficients))
all.equal(unname(reg_arma$stats), c(sum_mary$r.squared, unname(sum_mary$fstatistic[1])))
# Compare the speed of RcppArmadillo with R code
summary(microbenchmark(
  Rcpp=HighFreq::calc_lm(response=res_ponse, design=de_sign),
  Rcode=lm(res_ponse ~ de_sign),
  times=10))[, c(1, 4, 5)]  # end microbenchmark summary

## End(Not run)
```

`calc_mean` *Calculate the mean (location) of the columns of a* time series *or a* matrix *using* `RcppArmadillo`.

Description

Calculate the mean (location) of the columns of a *time series* or a *matrix* using `RcppArmadillo`.

Usage

```
calc_mean(tseries, method = "moment", con_fi = 0.75)
```

Arguments

`tseries`	A *time series* or a *matrix* of data.
`method`	A *string* specifying the type of the mean (location) model (the default is `method = "moment"` - see Details).
`con_fi`	The confidence level for calculating the quantiles (the default is `con_fi = 0.75`).

Details

The function `calc_mean()` calculates the mean (location) values of the columns of the *time series* `tseries` using `RcppArmadillo` `C++` code.

If `method = "moment"` (the default) then `calc_mean()` calculates the location as the mean - the first moment of the data.

If `method = "quantile"` then it calculates the location μ as the sum of the quantiles as follows:

$$\mu = q_{\alpha} + q_{1-\alpha}$$

Where α is the confidence level for calculating the quantiles.

If `method = "nonparametric"` then it calculates the location as the median.

The code examples below compare the function `calc_mean()` with the mean (location) calculated using `R` code.

Value

A single-row matrix with the mean (location) of the columns of `tseries`.

Examples

```
## Not run:
# Calculate historical returns
re_turns <- na.omit(rutils::etf_env$re_turns[, c("XLP", "VTI")])
# Calculate the column means in RcppArmadillo
HighFreq::calc_mean(re_turns)
# Calculate the column means in R
sapply(re_turns, mean)
# Compare the values
all.equal(drop(HighFreq::calc_mean(re_turns)),
  sapply(re_turns, mean), check.attributes=FALSE)
# Compare the speed of RcppArmadillo with R code
library(microbenchmark)
summary(microbenchmark(
  Rcpp=HighFreq::calc_mean(re_turns),
  Rcode=sapply(re_turns, mean),
  times=10))[, c(1, 4, 5)]  # end microbenchmark summary
# Calculate the quantile mean (location)
HighFreq::calc_mean(re_turns, method="quantile", con_fi=0.9)
# Calculate the quantile mean (location) in R
colSums(sapply(re_turns, quantile, c(0.9, 0.1), type=5))
# Compare the values
all.equal(drop(HighFreq::calc_mean(re_turns, method="quantile", con_fi=0.9)),
  colSums(sapply(re_turns, quantile, c(0.9, 0.1), type=5)),
  check.attributes=FALSE)
# Compare the speed of RcppArmadillo with R code
summary(microbenchmark(
  Rcpp=HighFreq::calc_mean(re_turns, method="quantile", con_fi=0.9),
  Rcode=colSums(sapply(re_turns, quantile, c(0.9, 0.1), type=5)),
  times=10))[, c(1, 4, 5)]  # end microbenchmark summary
# Calculate the column medians in RcppArmadillo
HighFreq::calc_mean(re_turns, method="nonparametric")
# Calculate the column medians in R
sapply(re_turns, median)
# Compare the values
```

```
all.equal(drop(HighFreq::calc_mean(re_turns, method="nonparametric")),
  sapply(re_turns, median), check.attributes=FALSE)
# Compare the speed of RcppArmadillo with R code
summary(microbenchmark(
  Rcpp=HighFreq::calc_mean(re_turns, method="nonparametric"),
  Rcode=sapply(re_turns, median),
  times=10))[, c(1, 4, 5)]  # end microbenchmark summary

## End(Not run)
```

`calc_ranks` *Calculate the ranks of the elements of a single-column* time series *or a* vector *using* `RcppArmadillo`.

Description

Calculate the ranks of the elements of a single-column *time series* or a *vector* using `RcppArmadillo`.

Usage

```
calc_ranks(tseries)
```

Arguments

`tseries`	A single-column *time series* or a *vector*.

Details

The function `calc_ranks()` calculates the ranks of the elements of a single-column *time series* or a *vector*. It uses the `RcppArmadillo` function `arma::sort_index()`. The function `arma::sort_index()` calculates the permutation index to sort a given vector into ascending order.

Applying the function `arma::sort_index()` twice: `arma::sort_index(arma::sort_index())`, calculates the *reverse* permutation index to sort the vector from ascending order back into its original unsorted order. The permutation index produced by: `arma::sort_index(arma::sort_index())` is the *reverse* of the permutation index produced by: `arma::sort_index()`.

The ranks of the elements are equal to the *reverse* permutation index. The function `calc_ranks()` calculates the *reverse* permutation index.

Value

An *integer vector* with the ranks of the elements of the `tseries`.

Examples

```
## Not run:
# Create a vector of random data
da_ta <- round(runif(7), 2)
# Calculate the ranks of the elements in two ways
all.equal(rank(da_ta), drop(HighFreq::calc_ranks(da_ta)))
# Create a time series of random data
da_ta <- xts::xts(runif(7), seq.Date(Sys.Date(), by=1, length.out=7))
# Calculate the ranks of the elements in two ways
```

```
all.equal(rank(coredata(da_ta)), drop(HighFreq::calc_ranks(da_ta)))
# Compare the speed of RcppArmadillo with R code
da_ta <- runif(7)
library(microbenchmark)
summary(microbenchmark(
  Rcpp=calc_ranks(da_ta),
  Rcode=rank(da_ta),
  times=10))[, c(1, 4, 5)]  # end microbenchmark summary

## End(Not run)
```

`calc_reg` *Perform multivariate regression using different methods, and return a vector of regression coefficients, their t-values, and the last residual z-score.*

Description

Perform multivariate regression using different methods, and return a vector of regression coefficients, their t-values, and the last residual z-score.

Usage

```
calc_reg(
  response,
  design,
  method = "least_squares",
  eigen_thresh = 0.001,
  eigen_max = 0L,
  con_fi = 0.1,
  alpha = 0
)
```

Arguments

`response`	A single-column *time series* or a *vector* of response data.
`design`	A *time series* or a *matrix* of design data (predictor or explanatory data).
`method`	A *string* specifying the type of the regression model the default is `method = "least_squares"` - see Details).
`eigen_thresh`	A *numeric* threshold level for discarding small singular values in order to regularize the inverse of the `design` matrix (the default is `0.001`).
`eigen_max`	An *integer* equal to the number of singular values used for calculating the regularized inverse of the `design` matrix (the default is `0` - equivalent to `eigen_max` equal to the number of columns of `design`).
`con_fi`	The confidence level for calculating the quantiles (the default is `con_fi = 0.75`).
`alpha`	The shrinkage intensity between `0` and `1`. (the default is `0`).

Details

The function `calc_reg()` performs multivariate regression using different methods, and returns a vector of regression coefficients, their t-values, and the last residual z-score.

The length of the return vector depends on the number of columns of `design`. The number of regression coefficients is equal to the number of columns of `design` plus `1`. The number of t-values is equal to the number of coefficients. And there is only `1` z-score. So if the number of columns of `design` is equal to `n`, then the return vector will have `2n+3` elements.

For example, if the design matrix has `2` columns of data, then `calc_reg()` returns a vector with `7` elements: `3` regression coefficients (including the intercept coefficient), `3` corresponding t-values, and `1` z-score.

If `method = "least_squares"` (the default) then it performs the standard least squares regression, the same as the function `calc_reg()`, and the function `lm()` from package *stats*. It uses `RcppArmadillo` `C++` code so it's several times faster than `lm()`.

If `method = "regular"` then it performs regularized regression. It calculates the regularized inverse of the `design` matrix from its singular value decomposition. It applies dimension regularization by selecting only the largest singular values equal in number to `eigen_max`.

If `method = "quantile"` then it performs quantile regression (not implemented yet).

Value

A vector with the regression coefficients, their t-values, and the last residual z-score.

Examples

```
## Not run:
# Calculate historical returns
re_turns <- na.omit(rutils::etf_env$re_turns[, c("XLF", "VTI", "IEF")])
# Response equals XLF returns
res_ponse <- re_turns[, 1]
# Design matrix equals VTI and IEF returns
de_sign <- re_turns[, -1]
# Perform multivariate regression using lm()
reg_model <- lm(res_ponse ~ de_sign)
sum_mary <- summary(reg_model)
co_eff <- sum_mary$coefficients
# Perform multivariate regression using calc_reg()
reg_arma <- drop(HighFreq::calc_reg(response=res_ponse, design=de_sign))
# Compare the outputs of both functions
all.equal(reg_arma[1:(2*(1+NCOL(de_sign)))],
  c(co_eff[, "Estimate"], co_eff[, "t value"]), check.attributes=FALSE)
# Compare the speed of RcppArmadillo with R code
library(microbenchmark)
summary(microbenchmark(
  Rcpp=HighFreq::calc_reg(response=res_ponse, design=de_sign),
  Rcode=lm(res_ponse ~ de_sign),
  times=10))[, c(1, 4, 5)]  # end microbenchmark summary

## End(Not run)
```

calc_scaled *Scale (standardize) the columns of a* matrix *of data using* RcppArmadillo.

Description

Scale (standardize) the columns of a *matrix* of data using RcppArmadillo.

Usage

```
calc_scaled(tseries, use_median = FALSE)
```

Arguments

tseries	A *time series* or *matrix* of data.
use_median	A *Boolean* argument: if TRUE then the centrality (central tendency) is calculated as the *median* and the dispersion is calculated as the *median absolute deviation* (*MAD*). If use_median = FALSE then the centrality is calculated as the *mean* and the dispersion is calculated as the *standard deviation* (the default is FALSE)

Details

The function calc_scaled() scales (standardizes) the columns of the tseries argument using RcppArmadillo.

If the argument use_median is FALSE (the default), then it performs the same calculation as the standard R function scale(), and it calculates the centrality (central tendency) as the *mean* and the dispersion as the *standard deviation*.

If the argument use_median is TRUE, then it calculates the centrality as the *median* and the dispersion as the *median absolute deviation* (*MAD*).

If the number of rows of tseries is less than 3 then it returns tseries unscaled.

The function calc_scaled() uses RcppArmadillo C++ code and is about *5* times faster than function scale(), for a *matrix* with *1,000* rows and *20* columns.

Value

A *matrix* with the same dimensions as the input argument tseries.

Examples

```
## Not run:
# Create a matrix of random data
re_turns <- matrix(rnorm(20000), nc=20)
scale_d <- calc_scaled(tseries=re_turns, use_median=FALSE)
scale_d2 <- scale(re_turns)
all.equal(scale_d, scale_d2, check.attributes=FALSE)
# Compare the speed of Rcpp with R code
library(microbenchmark)
summary(microbenchmark(
  Rcpp=calc_scaled(tseries=re_turns, use_median=FALSE),
  Rcode=scale(re_turns),
  times=100))[, c(1, 4, 5)]  # end microbenchmark summary
```

```
## End(Not run)
```

`calc_skew` *Calculate the skewness of the columns of a* time series *or a* matrix *using* `RcppArmadillo`.

Description

Calculate the skewness of the columns of a *time series* or a *matrix* using `RcppArmadillo`.

Usage

```
calc_skew(tseries, method = "moment", con_fi = 0.75)
```

Arguments

`tseries`	A *time series* or a *matrix* of data.
`method`	A *string* specifying the type of the skewness model (the default is `method = "moment"` - see Details).
`con_fi`	The confidence level for calculating the quantiles (the default is `con_fi = 0.75`).

Details

The function `calc_skew()` calculates the skewness of the columns of a *time series* or a *matrix* of data using `RcppArmadillo` `C++` code.

If `method = "moment"` (the default) then `calc_skew()` calculates the skewness as the third moment of the data.

If `method = "quantile"` then it calculates the skewness ς from the differences between the quantiles of the data as follows:

$$\varsigma = \frac{q_\alpha + q_{1-\alpha} - 2 * q_{0.5}}{q_\alpha - q_{1-\alpha}}$$

Where α is the confidence level for calculating the quantiles.

If `method = "nonparametric"` then it calculates the skewness as the difference between the mean of the data minus its median, divided by the standard deviation.

If the number of rows of `tseries` is less than `3` then it returns zeros.

The code examples below compare the function `calc_skew()` with the skewness calculated using `R` code.

Value

A single-row matrix with the skewness of the columns of `tseries`.

Examples

```
## Not run:
# Define a single-column time series of returns
re_turns <- na.omit(rutils::etf_env$re_turns$VTI)
# Calculate the moment skewness
HighFreq::calc_skew(re_turns)
# Calculate the moment skewness in R
calc_skewr <- function(x) {
  x <- (x-mean(x))
  sum(x^3)/var(x)^1.5/NROW(x)
}  # end calc_skewr
all.equal(HighFreq::calc_skew(re_turns),
  calc_skewr(re_turns), check.attributes=FALSE)
# Compare the speed of RcppArmadillo with R code
library(microbenchmark)
summary(microbenchmark(
  Rcpp=HighFreq::calc_skew(re_turns),
  Rcode=calc_skewr(re_turns),
  times=10))[, c(1, 4, 5)]  # end microbenchmark summary
# Calculate the quantile skewness
HighFreq::calc_skew(re_turns, method="quantile", con_fi=0.9)
# Calculate the quantile skewness in R
calc_skewq <- function(x, a = 0.75) {
   quantile_s <- quantile(x, c(1-a, 0.5, a), type=5)
   (quantile_s[3] + quantile_s[1] - 2*quantile_s[2])/(quantile_s[3] - quantile_s[1])
}  # end calc_skewq
all.equal(drop(HighFreq::calc_skew(re_turns, method="quantile", con_fi=0.9)),
  calc_skewq(re_turns, a=0.9), check.attributes=FALSE)
# Compare the speed of RcppArmadillo with R code
summary(microbenchmark(
  Rcpp=HighFreq::calc_skew(re_turns, method="quantile"),
  Rcode=calc_skewq(re_turns),
  times=10))[, c(1, 4, 5)]  # end microbenchmark summary
# Calculate the nonparametric skewness
HighFreq::calc_skew(re_turns, method="nonparametric")
# Compare HighFreq::calc_skew() with R nonparametric skewness
all.equal(drop(HighFreq::calc_skew(re_turns, method="nonparametric")),
  (mean(re_turns)-median(re_turns))/sd(re_turns),
  check.attributes=FALSE)
# Compare the speed of RcppArmadillo with R code
summary(microbenchmark(
  Rcpp=HighFreq::calc_skew(re_turns, method="nonparametric"),
  Rcode=(mean(re_turns)-median(re_turns))/sd(re_turns),
  times=10))[, c(1, 4, 5)]  # end microbenchmark summary

## End(Not run)
```

`calc_startpoints` *Calculate a vector of start points by lagging (shifting) a vector of end points.*

Description

Calculate a vector of start points by lagging (shifting) a vector of end points.

Usage

```
calc_startpoints(endp, look_back)
```

Arguments

endp	An *integer* vector of end points.
look_back	The length of the look-back interval, equal to the lag (shift) applied to the end points.

Details

The start points are equal to the values of the vector endp lagged (shifted) by an amount equal to look_back. In addition, an extra value of 1 is added to them, to avoid data overlaps. The lag operation requires appending a beginning warmup interval containing zeros, so that the vector of start points has the same length as the endp.

For example, consider the end points for a vector of length 25 divided into equal intervals of length 5: 4,9,14,19,24. (In C++ the vector indexing starts at 0 not 1, so it's shifted by -1.) Then the start points for look_back = 2 are equal to: 0,0,5,10,15. The differences between the end points minus the corresponding start points are equal to 9, except for the warmup interval.

Value

An *integer* vector with the same number of elements as the vector endp.

Examples

```
# Calculate end points
end_p <- HighFreq::calc_endpoints(25, 5)
# Calculate start points corresponding to the end points
start_p <- HighFreq::calc_startpoints(end_p, 2)
```

---

calc_var — *Calculate the dispersion (variance) of the columns of a* time series *or a* matrix *using* RcppArmadillo.

Description

Calculate the dispersion (variance) of the columns of a *time series* or a *matrix* using RcppArmadillo.

Usage

```
calc_var(tseries, method = "moment", con_fi = 0.75)
```

Arguments

tseries	A *time series* or a *matrix* of data.
method	A *string* specifying the type of the dispersion model (the default is method = "moment" - see Details).

Details

The dispersion is a measure of the variability of the data. Examples of dispersion are the variance and the Median Absolute Deviation (*MAD*).

The function `calc_var()` calculates the dispersion of the columns of a *time series* or a *matrix* of data using `RcppArmadillo` `C++` code.

If `method = "moment"` (the default) then `calc_var()` calculates the dispersion as the second moment of the data σ^2 (the variance).

If `method = "moment"` then `calc_var()` performs the same calculation as the function `colVars()` from package matrixStats, but it's much faster because it uses `RcppArmadillo` `C++` code.

If `method = "quantile"` then it calculates the dispersion as the difference between the quantiles as follows:

$$\mu = q_{\alpha} - q_{1-\alpha}$$

Where α is the confidence level for calculating the quantiles.

If `method = "nonparametric"` then it calculates the dispersion as the Median Absolute Deviation (*MAD*):

$$MAD = median(abs(x - median(x)))$$

It also multiplies the *MAD* by a factor of `1.4826`, to make it comparable to the standard deviation.

If `method = "nonparametric"` then `calc_var()` performs the same calculation as the function `stats::mad()`, but it's much faster because it uses `RcppArmadillo` `C++` code.

If the number of rows of `tseries` is less than `3` then it returns zeros.

Value

A row vector equal to the dispersion of the columns of the matrix `tseries`.

Examples

```
## Not run:
# Calculate VTI and XLF returns
re_turns <- na.omit(rutils::etf_env$re_turns[, c("VTI", "XLF")])
# Compare HighFreq::calc_var() with standard var()
all.equal(drop(HighFreq::calc_var(re_turns)),
  apply(re_turns, 2, var), check.attributes=FALSE)
# Compare HighFreq::calc_var() with matrixStats
all.equal(drop(HighFreq::calc_var(re_turns)),
  matrixStats::colVars(re_turns), check.attributes=FALSE)
# Compare the speed of RcppArmadillo with matrixStats and with R code
library(microbenchmark)
summary(microbenchmark(
  Rcpp=HighFreq::calc_var(re_turns),
  matrixStats=matrixStats::colVars(re_turns),
  Rcode=apply(re_turns, 2, var),
  times=10))[, c(1, 4, 5)]  # end microbenchmark summary
# Compare HighFreq::calc_var() with stats::mad()
all.equal(drop(HighFreq::calc_var(re_turns, method="nonparametric")),
  sapply(re_turns, mad), check.attributes=FALSE)
# Compare the speed of RcppArmadillo with stats::mad()
summary(microbenchmark(
  Rcpp=HighFreq::calc_var(re_turns, method="nonparametric"),
  Rcode=sapply(re_turns, mad),
  times=10))[, c(1, 4, 5)]  # end microbenchmark summary
```

```
## End(Not run)
```

`calc_var_ag` *Calculate the variance of returns aggregated over end points.*

Description

Calculate the variance of returns aggregated over end points.

Usage

```
calc_var_ag(tseries, step = 1L)
```

Arguments

`tseries`	A *time series* or a *matrix* of prices.
`step`	The number of periods in each interval between neighboring end points.

Details

The function `calc_var_ag()` calculates the variance of returns aggregated over end points.

It first calculates the end points spaced apart by the number of periods equal to the argument `step`. Then it calculates the aggregated returns by differencing the prices `tseries` calculated at the end points. Finally it calculates the variance of the returns.

If there are extra periods that don't fit over the length of `tseries`, then `calc_var_ag()` loops over all possible stub intervals, then it calculates all the corresponding variance values, and averages them.

For example, if the number of rows of `tseries` is equal to `20`, and `step=3` then `6` end points fit over the length of `tseries`, and there are `2` extra periods that must fit into stubs, either at the beginning or at the end (or both).

The aggregated volatility σ_t scales (increases) with the length of the aggregation interval Δt raised to the power of the *Hurst exponent* H:

$$\sigma_t = \sigma \Delta t^H$$

Where σ is the daily return volatility.

The function `calc_var_ag()` can therefore be used to calculate the *Hurst exponent* from the volatility ratio.

Value

The variance of aggregated returns.

Examples

```
## Not run:
# Calculate the log prices
price_s <- na.omit(rutils::etf_env$price_s[, c("XLP", "VTI")])
price_s <- log(price_s)
# Calculate the daily variance of percentage returns
calc_var_ag(price_s, step=1)
# Calculate the daily variance using R
sapply(rutils::diff_it(price_s), var)
# Calculate the variance of returns aggregated over 21 days
calc_var_ag(price_s, step=21)
# The variance over 21 days is approximately 21 times the daily variance
21*calc_var_ag(price_s, step=1)

## End(Not run)
```

`calc_var_ohlc` *Calculate the variance of* OHLC *prices using different price range estimators.*

Description

Calculate the variance of *OHLC* prices using different price range estimators.

Usage

```
calc_var_ohlc(
  ohlc,
  method = "yang_zhang",
  lag_close = 0L,
  scale = TRUE,
  in_dex = 0L
)
```

Arguments

`ohlc`	A *time series* or a *matrix* of *OHLC* prices.
`method`	A *character* string representing the price range estimator for calculating the variance. The estimators include: • "close" close-to-close estimator, • "rogers_satchell" Rogers-Satchell estimator, • "garman_klass" Garman-Klass estimator, • "garman_klass_yz" Garman-Klass with account for close-to-open price jumps, • "yang_zhang" Yang-Zhang estimator, (The default is the `method = "yang_zhang"`.)
`lag_close`	A *vector* with the lagged *close* prices of the *OHLC time series*. This is an optional argument. (The default is `lag_close = 0`).
`scale`	*Boolean* argument: Should the returns be divided by the time index, the number of seconds in each period? (The default is `scale = TRUE`).
`in_dex`	A *vector* with the time index of the *time series*. This is an optional argument (the default is `in_dex = 0`).

Details

The function `calc_var_ohlc()` calculates the variance from all the different intra-day and day-over-day returns (defined as the differences of *OHLC* prices), using several different variance estimation methods.

The input *OHLC time series* `ohlc` is assumed to be the log prices.

The default `method` is *"yang_zhang"*, which theoretically has the lowest standard error among unbiased estimators. The methods *"close"*, *"garman_klass_yz"*, and *"yang_zhang"* do account for *close-to-open* price jumps, while the methods *"garman_klass"* and *"rogers_satchell"* do not account for *close-to-open* price jumps.

If `scale` is `TRUE` (the default), then the returns are divided by the differences of the time index (which scales the variance to the units of variance per second squared). This is useful when calculating the variance from minutely bar data, because dividing returns by the number of seconds decreases the effect of overnight price jumps. If the time index is in days, then the variance is equal to the variance per day squared.

If the number of rows of `ohlc` is less than `3` then it returns zero.

The optional argument `in_dex` is the time index of the *time series* `ohlc`. If the time index is in seconds, then the differences of the index are equal to the number of seconds in each time period. If the time index is in days, then the differences are equal to the number of days in each time period.

The optional argument `lag_close` are the lagged *close* prices of the *OHLC time series*. Passing in the lagged *close* prices speeds up the calculation, so it's useful for rolling calculations.

The function `calc_var_ohlc()` is implemented in `RcppArmadillo` `C++` code, and it's over `10` times faster than `calc_var_ohlc_r()`, which is implemented in `R` code.

Value

A single *numeric* value equal to the variance of the *OHLC time series*.

Examples

```
## Not run:
# Extract the log OHLC prices of SPY
oh_lc <- log(HighFreq::SPY)
# Extract the time index of SPY prices
in_dex <- c(1, diff(xts::.index(oh_lc)))
# Calculate the variance of SPY returns, with scaling of the returns
HighFreq::calc_var_ohlc(oh_lc,
 method="yang_zhang", scale=TRUE, in_dex=in_dex)
# Calculate variance without accounting for overnight jumps
HighFreq::calc_var_ohlc(oh_lc,
 method="rogers_satchell", scale=TRUE, in_dex=in_dex)
# Calculate the variance without scaling the returns
HighFreq::calc_var_ohlc(oh_lc, scale=FALSE)
# Calculate the variance by passing in the lagged close prices
lag_close <- HighFreq::lag_it(oh_lc[, 4])
all.equal(HighFreq::calc_var_ohlc(oh_lc),
  HighFreq::calc_var_ohlc(oh_lc, lag_close=lag_close))
# Compare with HighFreq::calc_var_ohlc_r()
all.equal(HighFreq::calc_var_ohlc(oh_lc, in_dex=in_dex),
  HighFreq::calc_var_ohlc_r(oh_lc))
# Compare the speed of Rcpp with R code
library(microbenchmark)
summary(microbenchmark(
```

```
  Rcpp=HighFreq::calc_var_ohlc(oh_lc),
  Rcode=HighFreq::calc_var_ohlc_r(oh_lc),
  times=10))[, c(1, 4, 5)]  # end microbenchmark summary

## End(Not run)
```

`calc_var_ohlc_ag` *Calculate the variance of aggregated* OHLC *prices using different price range estimators.*

Description

Calculate the variance of aggregated *OHLC* prices using different price range estimators.

Usage

```
calc_var_ohlc_ag(
  ohlc,
  step = 1L,
  method = "yang_zhang",
  lag_close = 0L,
  scale = TRUE,
  in_dex = 0L
)
```

Arguments

`ohlc`	A *time series* or a *matrix* of *OHLC* prices.
`step`	The number of periods in each interval between neighboring end points.
`method`	A *character* string representing the price range estimator for calculating the variance. The estimators include: • "close" close-to-close estimator, • "rogers_satchell" Rogers-Satchell estimator, • "garman_klass" Garman-Klass estimator, • "garman_klass_yz" Garman-Klass with account for close-to-open price jumps, • "yang_zhang" Yang-Zhang estimator, (The default is the `method = "yang_zhang"`.)
`lag_close`	A *vector* with the lagged *close* prices of the *OHLC time series*. This is an optional argument. (The default is `lag_close = 0`).
`scale`	*Boolean* argument: Should the returns be divided by the time index, the number of seconds in each period? (The default is `scale = TRUE`).
`in_dex`	A *vector* with the time index of the *time series*. This is an optional argument (the default is `in_dex = 0`).

Details

The function `calc_var_ohlc_ag()` calculates the variance of *OHLC* prices aggregated over end points.

It first calculates the end points spaced apart by the number of periods equal to the argument `step`. Then it aggregates the *OHLC* prices to the end points. Finally it calculates the variance of the aggregated *OHLC* prices.

If there are extra periods that don't fit over the length of `ohlc`, then `calc_var_ohlc_ag()` loops over all possible stub intervals, it calculates all the corresponding variance values, and it averages them.

For example, if the number of rows of `ohlc` is equal to `20`, and `step=3` then `6` end points fit over the length of `ohlc`, and there are `2` extra periods that must fit into stubs, either at the beginning or at the end (or both).

The aggregated volatility σ_t scales (increases) with the length of the aggregation interval Δt raised to the power of the *Hurst exponent* H:

$$\sigma_t = \sigma \Delta t^H$$

Where σ is the daily return volatility.

The function `calc_var_ohlc_ag()` can therefore be used to calculate the *Hurst exponent* from the volatility ratio.

Value

The variance of aggregated *OHLC* prices.

Examples

```
## Not run:
# Calculate the log ohlc prices
oh_lc <- log(rutils::etf_env$VTI)
# Calculate the daily variance of percentage returns
calc_var_ohlc_ag(oh_lc, step=1)
# Calculate the variance of returns aggregated over 21 days
calc_var_ohlc_ag(oh_lc, step=21)
# The variance over 21 days is approximately 21 times the daily variance
21*calc_var_ohlc_ag(oh_lc, step=1)

## End(Not run)
```

`calc_var_ohlc_r` *Calculate the variance of an* OHLC *time series, using different range estimators for variance.*

Description

Calculate the variance of an *OHLC* time series, using different range estimators for variance.

Usage

```
calc_var_ohlc_r(oh_lc, calc_method = "yang_zhang", scal_e = TRUE)
```

Arguments

oh_lc	An *OHLC* time series of prices in *xts* format.
calc_method	A *character* string representing the method for estimating variance. The methods include: • "close" close to close, • "garman_klass" Garman-Klass, • "garman_klass_yz" Garman-Klass with account for close-to-open price jumps, • "rogers_satchell" Rogers-Satchell, • "yang_zhang" Yang-Zhang, (default is "yang_zhang")
scal_e	*Boolean* argument: should the returns be divided by the number of seconds in each period? (default is TRUE)

Details

The function calc_var_ohlc_r() calculates the variance from all the different intra-day and day-over-day returns (defined as the differences of *OHLC* prices), using several different variance estimation methods.

The default method is "yang_zhang", which theoretically has the lowest standard error among unbiased estimators. The methods "close", "garman_klass_yz", and "yang_zhang" do account for close-to-open price jumps, while the methods "garman_klass" and "rogers_satchell" do not account for close-to-open price jumps.

If scal_e is TRUE (the default), then the returns are divided by the differences of the time index (which scales the variance to the units of variance per second squared.) This is useful when calculating the variance from minutely bar data, because dividing returns by the number of seconds decreases the effect of overnight price jumps. If the time index is in days, then the variance is equal to the variance per day squared.

The function calc_var_ohlc_r() is implemented in R code.

Value

A single *numeric* value equal to the variance.

Examples

```
# Calculate the variance of SPY returns
HighFreq::calc_var_ohlc_r(HighFreq::SPY, calc_method="yang_zhang")
# Calculate variance without accounting for overnight jumps
HighFreq::calc_var_ohlc_r(HighFreq::SPY, calc_method="rogers_satchell")
# Calculate the variance without scaling the returns
HighFreq::calc_var_ohlc_r(HighFreq::SPY, scal_e=FALSE)
```

calc_var_vec *Calculate the variance of a a single-column* time series *or a* vector *using* RcppArmadillo.

Description

Calculate the variance of a a single-column *time series* or a *vector* using RcppArmadillo.

Usage

```
calc_var_vec(tseries)
```

Arguments

tseries	A single-column *time series* or a *vector*.

Details

The function calc_var_vec() calculates the variance of a *vector* using RcppArmadillo C++ code, so it's significantly faster than the R function var().

Value

A *numeric* value equal to the variance of the *vector*.

Examples

```
## Not run:
# Create a vector of random returns
re_turns <- rnorm(1e6)
# Compare calc_var_vec() with standard var()
all.equal(HighFreq::calc_var_vec(re_turns),
  var(re_turns))
# Compare the speed of RcppArmadillo with R code
library(microbenchmark)
summary(microbenchmark(
  Rcpp=HighFreq::calc_var_vec(re_turns),
  Rcode=var(re_turns),
  times=10))[, c(1, 4, 5)]  # end microbenchmark summary

## End(Not run)
```

`calc_weights` *Calculate the optimal portfolio weights for different types of objective functions.*

Description

Calculate the optimal portfolio weights for different types of objective functions.

Usage

```
calc_weights(
  returns,
  method = "rank_sharpe",
  eigen_thresh = 0.001,
  eigen_max = 0L,
  con_fi = 0.1,
  alpha = 0,
  scale = TRUE,
  vol_target = 0.01
)
```

Arguments

`returns`	A *time series* or a *matrix* of returns data (the returns in excess of the risk-free rate).
`method`	A *string* specifying the objective function for calculating the weights (see Details) (the default is `method = "rank_sharpe"`)
`eigen_thresh`	A *numeric* threshold level for discarding small singular values in order to regularize the inverse of the `returns` matrix (the default is `0.001`).
`eigen_max`	An *integer* equal to the number of singular values used for calculating the regularized inverse of the `returns` matrix (the default is `0` - equivalent to `eigen_max` equal to the number of columns of `returns`).
`con_fi`	The confidence level for calculating the quantiles (the default is `con_fi = 0.75`).
`alpha`	The shrinkage intensity between `0` and `1`. (the default is `0`).
`scale`	A *Boolean* specifying whether the weights should be scaled (the default is `scale = TRUE`).
`vol_target`	A *numeric* volatility target for scaling the weights (the default is `0.001`)

Details

The function `calc_weights()` calculates the optimal portfolio weights for different types of objective functions, using `RcppArmadillo` `C++` code.

If `method = "rank_sharpe"` (the default) then it calculates the weights as the ranks (order index) of the trailing Sharpe ratios of the asset `returns`.

If `method = "rank"` then it calculates the weights as the ranks (order index) of the last row of the `returns`.

If `method = "max_sharpe"` then `calc_weights()` calculates the weights of the maximum Sharpe portfolio, by multiplying the inverse of the covariance *matrix* times the mean column returns.

If method = "min_var" then it calculates the weights of the minimum variance portfolio under linear constraints.

If method = "min_varpca" then it calculates the weights of the minimum variance portfolio under quadratic constraints (which is the highest order principal component).

If scale = TRUE (the default) then the weights are scaled so that the resulting portfolio has a volatility equal to vol_target.

calc_weights() calculates the regularized inverse of the covariance *matrix* of returns from its eigen decomposition. It applies dimension regularization by selecting only the largest eigenvalues equal in number to eigen_max.

In addition, calc_weights() applies shrinkage to the columns of returns, by shrinking their means to their common mean value. The shrinkage intensity alpha determines the amount of shrinkage that is applied, with alpha = 0 representing no shrinkage (with the column means of returns unchanged), and alpha = 1 representing complete shrinkage (with the column means of returns all equal to the single mean of all the columns).

Value

A column *vector* of the same length as the number of columns of returns.

Examples

```
## Not run:
# Calculate covariance matrix of ETF returns
re_turns <- na.omit(rutils::etf_env$re_turns[, 1:16])
ei_gen <- eigen(cov(re_turns))
# Calculate regularized inverse of covariance matrix
eigen_max <- 3
eigen_vec <- ei_gen$vectors[, 1:eigen_max]
eigen_val <- ei_gen$values[1:eigen_max]
in_verse <- eigen_vec %*% (t(eigen_vec) / eigen_val)
# Define shrinkage intensity and apply shrinkage to the mean returns
al_pha <- 0.5
col_means <- colMeans(re_turns)
col_means <- ((1-al_pha)*col_means + al_pha*mean(col_means))
# Calculate weights using R
weight_s <- in_verse %*% col_means
n_col <- NCOL(re_turns)
weights_r <- weights_r*sd(re_turns %*% rep(1/n_col, n_col))/sd(re_turns %*% weights_r)
# Calculate weights using RcppArmadillo
weight_s <- drop(HighFreq::calc_weights(re_turns, eigen_max, alpha=al_pha))
all.equal(weight_s, weights_r)

## End(Not run)
```

---

diff_it *Calculate the row differences of a a* time series *or a* matrix *using* RcppArmadillo.

Description

Calculate the row differences of a a *time series* or a *matrix* using *RcppArmadillo*.

Usage

```
diff_it(tseries, lagg = 1L, pad_zeros = TRUE)
```

Arguments

tseries	A *time series* or a *matrix*.
lagg	An *integer* equal to the number of rows (time periods) to lag when calculating the differences (the default is lagg = 1).
pad_zeros	*Boolean* argument: Should the output *matrix* be padded (extended) with zeros, in order to return a *matrix* with the same number of rows as the input? (the default is pad_zeros = TRUE)

Details

The function diff_it() calculates the differences between the rows of the input *matrix* tseries and its lagged version.

The argument lagg specifies the number of lags applied to the rows of the lagged version of tseries. For positive lagg values, the lagged version of tseries has its rows shifted *forward* (down) by the number equal to lagg rows. For negative lagg values, the lagged version of tseries has its rows shifted *backward* (up) by the number equal to -lagg rows. For example, if lagg=3 then the lagged version will have its rows shifted down by 3 rows, and the differences will be taken between each row minus the row three time periods before it (in the past). The default is lagg = 1.

The argument pad_zeros specifies whether the output *matrix* should be padded (extended) with the rows of the initial (warmup) period at the front, in order to return a *matrix* with the same number of rows as the input tseries. The default is pad_zeros = TRUE. The padding operation can be time-consuming, because it requires the copying of data.

The function diff_it() is implemented in RcppArmadillo C++ code, which makes it much faster than R code.

Value

A *matrix* containing the differences between the rows of the input *matrix* tseries.

Examples

```
## Not run:
# Create a matrix of random data
da_ta <- matrix(sample(15), nc=3)
# Calculate differences with lagged rows
HighFreq::diff_it(da_ta, lagg=2)
# Calculate differences with advanced rows
HighFreq::diff_it(da_ta, lagg=-2)
# Compare HighFreq::diff_it() with rutils::diff_it()
all.equal(HighFreq::diff_it(da_ta, lagg=2),
  rutils::diff_it(da_ta, lagg=2),
  check.attributes=FALSE)
# Compare the speed of RcppArmadillo with R code
library(microbenchmark)
summary(microbenchmark(
  Rcpp=HighFreq::diff_it(da_ta, lagg=2),
  Rcode=rutils::diff_it(da_ta, lagg=2),
  times=10))[, c(1, 4, 5)]  # end microbenchmark summary
```

```
## End(Not run)
```

`diff_vec` *Calculate the differences between the neighboring elements of a single-column* time series *or a* vector.

Description

Calculate the differences between the neighboring elements of a single-column *time series* or a *vector*.

Usage

```
diff_vec(tseries, lagg = 1L, pad_zeros = TRUE)
```

Arguments

`tseries`	A single-column *time series* or a *vector*.
`lagg`	An *integer* equal to the number of time periods to lag when calculating the differences (the default is `lagg = 1`).
`pad_zeros`	*Boolean* argument: Should the output *vector* be padded (extended) with zeros, in order to return a *vector* of the same length as the input? (the default is `pad_zeros = TRUE`)

Details

The function `diff_vec()` calculates the differences between the input *time series* or *vector* and its lagged version.

The argument `lagg` specifies the number of lags. For example, if `lagg=3` then the differences will be taken between each element minus the element three time periods before it (in the past). The default is `lagg = 1`.

The argument `pad_zeros` specifies whether the output *vector* should be padded (extended) with zeros at the front, in order to return a *vector* of the same length as the input. The default is `pad_zeros = TRUE`. The padding operation can be time-consuming, because it requires the copying of data.

The function `diff_vec()` is implemented in `RcppArmadillo C++` code, which makes it several times faster than `R` code.

Value

A column *vector* containing the differences between the elements of the input vector.

Examples

```
## Not run:
# Create a vector of random returns
re_turns <- rnorm(1e6)
# Compare diff_vec() with rutils::diff_it()
all.equal(drop(HighFreq::diff_vec(re_turns, lagg=3, pad=TRUE)),
  rutils::diff_it(re_turns, lagg=3))
# Compare the speed of RcppArmadillo with R code
```

```
library(microbenchmark)
summary(microbenchmark(
  Rcpp=HighFreq::diff_vec(re_turns, lagg=3, pad=TRUE),
  Rcode=rutils::diff_it(re_turns, lagg=3),
  times=10))[, c(1, 4, 5)]  # end microbenchmark summary

## End(Not run)
```

`hf_data` *High frequency data sets*

Description

hf_data.RData is a file containing the datasets:

SPY an `xts` time series containing 1-minute `OHLC` bar data for the `SPY` etf, from 2008-01-02 to 2014-05-19. SPY contains 625,425 rows of data, each row contains a single minute bar.

TLT an `xts` time series containing 1-minute `OHLC` bar data for the `TLT` etf, up to 2014-05-19.

VXX an `xts` time series containing 1-minute `OHLC` bar data for the `VXX` etf, up to 2014-05-19.

Usage

```
data(hf_data)  # not required - data is lazy load
```

Format

Each `xts` time series contains `OHLC` data, with each row containing a single minute bar:

Open Open price in the bar

High High price in the bar

Low Low price in the bar

Close Close price in the bar

Volume trading volume in the bar

Source

https://wrds-web.wharton.upenn.edu/wrds/

References

Wharton Research Data Service (WRDS)

Examples

```
# data(hf_data)  # not required - data is lazy load
head(SPY)
chart_Series(x=SPY["2009"])
```

lag_it *Apply a lag to the rows of a* time series *or a* matrix *using* RcppArmadillo.

Description

Apply a lag to the rows of a *time series* or a *matrix* using RcppArmadillo.

Usage

```
lag_it(tseries, lagg = 1L, pad_zeros = TRUE)
```

Arguments

tseries	A *time series* or a *matrix*.
lagg	An *integer* equal to the number of periods to lag (the default is lagg = 1).
pad_zeros	*Boolean* argument: Should the output be padded with zeros? (The default is pad_zeros = TRUE.)

Details

The function lag_it() applies a lag to the input *matrix* by shifting its rows by the number equal to the argument lagg. For positive lagg values, the rows are shifted *forward* (down), and for negative lagg values they are shifted *backward* (up).

The output *matrix* is padded with either zeros (the default), or with rows of data from tseries, so that it has the same dimensions as tseries. If the lagg is positive, then the first row is copied and added upfront. If the lagg is negative, then the last row is copied and added to the end.

As a rule, if tseries contains returns data, then the output *matrix* should be padded with zeros, to avoid data snooping. If tseries contains prices, then the output *matrix* should be padded with the prices.

Value

A *matrix* with the same dimensions as the input argument tseries.

Examples

```
## Not run:
# Create a matrix of random returns
re_turns <- matrix(rnorm(5e6), nc=5)
# Compare lag_it() with rutils::lag_it()
all.equal(HighFreq::lag_it(re_turns),
  rutils::lag_it(re_turns))
# Compare the speed of RcppArmadillo with R code
library(microbenchmark)
summary(microbenchmark(
  Rcpp=HighFreq::lag_it(re_turns),
  Rcode=rutils::lag_it(re_turns),
  times=10))[, c(1, 4, 5)]  # end microbenchmark summary

## End(Not run)
```

lag_vec *Apply a lag to a single-column* time series *or a* vector *using* RcppArmadillo.

Description

Apply a lag to a single-column *time series* or a *vector* using RcppArmadillo.

Usage

```
lag_vec(tseries, lagg = 1L, pad_zeros = TRUE)
```

Arguments

tseries	A single-column *time series* or a *vector*.
lagg	An *integer* equal to the number of periods to lag (the default is lagg = 1).
pad_zeros	*Boolean* argument: Should the output be padded with zeros? (The default is pad_zeros = TRUE.)

Details

The function lag_vec() applies a lag to the input *time series* tseries by shifting its elements by the number equal to the argument lagg. For positive lagg values, the elements are shifted forward in time (down), and for negative lagg values they are shifted backward (up).

The output *vector* is padded with either zeros (the default), or with data from tseries, so that it has the same number of element as tseries. If the lagg is positive, then the first element is copied and added upfront. If the lagg is negative, then the last element is copied and added to the end.

As a rule, if tseries contains returns data, then the output *matrix* should be padded with zeros, to avoid data snooping. If tseries contains prices, then the output *matrix* should be padded with the prices.

Value

A column *vector* with the same number of elements as the input time series.

Examples

```
## Not run:
# Create a vector of random returns
re_turns <- rnorm(1e6)
# Compare lag_vec() with rutils::lag_it()
all.equal(drop(HighFreq::lag_vec(re_turns)),
  rutils::lag_it(re_turns))
# Compare the speed of RcppArmadillo with R code
library(microbenchmark)
summary(microbenchmark(
  Rcpp=HighFreq::lag_vec(re_turns),
  Rcode=rutils::lag_it(re_turns),
  times=10))[, c(1, 4, 5)]  # end microbenchmark summary

## End(Not run)
```

mult_vec_mat *Multiply in place (without copying) the columns or rows of a* matrix *times a* vector*, element-wise.*

Description

Multiply in place (without copying) the columns or rows of a *matrix* times a *vector*, element-wise.

Usage

```
mult_vec_mat(vector, matrix, by_col = TRUE)
```

Arguments

vector	A *vector*.
matrix	A *matrix*.
by_col	A *Boolean* argument: if TRUE then multiply the columns, otherwise multiply the rows (the default is by_col = TRUE.)

Details

The function mult_vec_mat() multiplies the columns or rows of a *matrix* times a *vector*, element-wise.

If the number of *vector* elements is equal to the number of matrix columns, then it multiplies the columns by the *vector*, and returns the number of columns. If the number of *vector* elements is equal to the number of rows, then it multiplies the rows, and returns the number of rows.

If the *matrix* is square and if by_col is TRUE then it multiplies the columns, otherwise it multiplies the rows.

It accepts *pointers* to the *matrix* and *vector*, and replaces the old *matrix* values with the new values. It performs the calculation in place, without copying the *matrix* in memory (which greatly increases the computation speed). It performs an implicit loop over the *matrix* rows and columns using the *Armadillo* operators each_row() and each_col(), instead of performing explicit for() loops (both methods are equally fast).

The function mult_vec_mat() uses RcppArmadillo C++ code, so when multiplying large *matrix* columns it's several times faster than vectorized R code, and it's even much faster compared to R when multiplying the *matrix* rows.

Value

A single *integer* value, equal to either the number of *matrix* columns or the number of rows.

Examples

```
## Not run:
# Multiply matrix columns using R
mat_rix <- matrix(round(runif(25e4), 2), nc=5e2)
vec_tor <- round(runif(5e2), 2)
prod_uct <- vec_tor*mat_rix
# Multiply the matrix in place
HighFreq::mult_vec_mat(vec_tor, mat_rix)
```

```
all.equal(prod_uct, mat_rix)
# Compare the speed of Rcpp with R code
library(microbenchmark)
summary(microbenchmark(
    Rcpp=HighFreq::mult_vec_mat(vec_tor, mat_rix),
    Rcode=vec_tor*mat_rix,
    times=10))[, c(1, 4, 5)]  # end microbenchmark summary

# Multiply matrix rows using R
mat_rix <- matrix(round(runif(25e4), 2), nc=5e2)
vec_tor <- round(runif(5e2), 2)
prod_uct <- t(vec_tor*t(mat_rix))
# Multiply the matrix in place
HighFreq::mult_vec_mat(vec_tor, mat_rix, by_col=FALSE)
all.equal(prod_uct, mat_rix)
# Compare the speed of Rcpp with R code
library(microbenchmark)
summary(microbenchmark(
    Rcpp=HighFreq::mult_vec_mat(vec_tor, mat_rix, by_col=FALSE),
    Rcode=t(vec_tor*t(mat_rix)),
    times=10))[, c(1, 4, 5)]  # end microbenchmark summary

## End(Not run)
```

`remove_jumps` *Remove overnight close-to-open price jumps from an* OHLC *time series, by adding adjustment terms to its prices.*

Description

Remove overnight close-to-open price jumps from an *OHLC* time series, by adding adjustment terms to its prices.

Usage

```
remove_jumps(oh_lc)
```

Arguments

`oh_lc`	An *OHLC* time series of prices and trading volumes, in *xts* format.

Details

The function `remove_jumps()` removes the overnight close-to-open price jumps from an *OHLC* time series, by adjusting its prices so that the first *Open* price of the day is equal to the last *Close* price of the previous day.

The function `remove_jumps()` adds adjustment terms to all the *OHLC* prices, so that intra-day returns and volatilities are not affected.

The function `remove_jumps()` identifies overnight periods as those that are greater than 60 seconds. This assumes that intra-day periods between neighboring rows of data are 60 seconds or less.

The time index of the `oh_lc` time series is assumed to be in *POSIXct* format, so that its internal value is equal to the number of seconds that have elapsed since the *epoch*.

Value

An *OHLC* time series with the same dimensions and the same time index as the input oh_lc time series.

Examples

```
# Remove overnight close-to-open price jumps from SPY data
oh_lc <- remove_jumps(HighFreq::SPY)
```

---

roll_apply *Apply an aggregation function over a rolling look-back interval and the end points of an* OHLC *time series, using* R *code.*

Description

Apply an aggregation function over a rolling look-back interval and the end points of an *OHLC* time series, using R code.

Usage

```
roll_apply(
  x_ts,
  agg_fun,
  look_back = 2,
  end_points = seq_along(x_ts),
  by_columns = FALSE,
  out_xts = TRUE,
  ...
)
```

Arguments

...	additional parameters to the function agg_fun.
x_ts	An *OHLC* time series of prices and trading volumes, in *xts* format.
agg_fun	The name of the aggregation function to be applied over a rolling look-back interval.
look_back	The number of end points in the look-back interval used for applying the aggregation function (including the current row).
by_columns	*Boolean* argument: should the function agg_fun() be applied column-wise (individually), or should it be applied to all the columns combined? (default is FALSE)
out_xts	*Boolean* argument: should the output be coerced into an *xts* series? (default is TRUE)
end_points	An integer vector of end points.

Details

The function roll_apply() applies an aggregation function over a rolling look-back interval attached at the end points of an *OHLC* time series.

The function roll_apply() is implemented in R code.

HighFreq::roll_apply() performs similar operations to the functions rollapply() and period.apply() from package xts, and also the function apply.rolling() from package PerformanceAnalytics. (The function rollapply() isn't exported from the package xts.)

But HighFreq::roll_apply() is faster because it performs less type-checking and skips other overhead. Unlike the other functions, roll_apply() doesn't produce any leading *NA* values.

The function roll_apply() can be called in two different ways, depending on the argument end_points. If the argument end_points isn't explicitly passed to roll_apply(), then the default value is used, and roll_apply() performs aggregations over overlapping intervals at each point in time.

If the argument end_points is explicitly passed to roll_apply(), then roll_apply() performs aggregations over intervals attached at the end_points. If look_back=2 then the aggregations are performed over non-overlapping intervals, otherwise they are performed over overlapping intervals.

If the argument out_xts is TRUE (the default) then the output is coerced into an *xts* series, with the number of rows equal to the length of argument end_points. Otherwise a list is returned, with the length equal to the length of argument end_points.

If out_xts is TRUE and the aggregation function agg_fun() returns a single value, then roll_apply() returns an *xts* time series with a single column. If out_xts is TRUE and if agg_fun() returns a vector of values, then roll_apply() returns an *xts* time series with multiple columns, equal to the length of the vector returned by the aggregation function agg_fun().

Value

Either an *xts* time series with the number of rows equal to the length of argument end_points, or a list the length of argument end_points.

Examples

```
# extract a single day of SPY data
oh_lc <- HighFreq::SPY["2012-02-13"]
inter_val <- 11  # number of data points between end points
look_back <- 4  # number of end points in look-back interval
# Calculate the rolling sums of oh_lc columns over a rolling look-back interval
agg_regations <- roll_apply(oh_lc, agg_fun=sum, look_back=look_back, by_columns=TRUE)
# Apply a vector-valued aggregation function over a rolling look-back interval
agg_function <- function(oh_lc)  c(max(oh_lc[, 2]), min(oh_lc[, 3]))
agg_regations <- roll_apply(oh_lc, agg_fun=agg_function, look_back=look_back)
# Define end points at 11-minute intervals (HighFreq::SPY is minutely bars)
end_points <- rutils::end_points(oh_lc, inter_val=inter_val)
# Calculate the sums of oh_lc columns over end_points using non-overlapping intervals
agg_regations <- roll_apply(oh_lc, agg_fun=sum, end_points=end_points, by_columns=TRUE)
# Apply a vector-valued aggregation function over the end_points of oh_lc
# using overlapping intervals
agg_regations <- roll_apply(oh_lc, agg_fun=agg_function,
                            look_back=5, end_points=end_points)
```

`roll_backtest` *Perform a backtest simulation of a trading strategy (model) over a vector of end points along a time series of prices.*

Description

Perform a backtest simulation of a trading strategy (model) over a vector of end points along a time series of prices.

Usage

```
roll_backtest(
  x_ts,
  train_func,
  trade_func,
  look_back = look_forward,
  look_forward,
  end_points = rutils::calc_endpoints(x_ts, look_forward),
  ...
)
```

Arguments

`...`	additional parameters to the functions `train_func()` and `trade_func()`.
`x_ts`	A time series of prices, asset returns, trading volumes, and other data, in *xts* format.
`train_func`	The name of the function for training (calibrating) a forecasting model, to be applied over a rolling look-back interval.
`trade_func`	The name of the trading model function, to be applied over a rolling look-forward interval.
`look_back`	The size of the look-back interval, equal to the number of rows of data used for training the forecasting model.
`look_forward`	The size of the look-forward interval, equal to the number of rows of data used for trading the strategy.
`end_points`	A vector of end points along the rows of the `x_ts` time series, given as either integers or dates.

Details

The function `roll_backtest()` performs a rolling backtest simulation of a trading strategy over a vector of end points. At each end point, it trains (calibrates) a forecasting model using past data taken from the `x_ts` time series over the look-back interval, and applies the forecasts to the `trade_func()` trading model, using out-of-sample future data from the look-forward interval.

The function `trade_func()` should simulate the trading model, and it should return a named list with at least two elements: a named vector of performance statistics, and an *xts* time series of out-of-sample returns. The list returned by `trade_func()` can also have additional elements, like the in-sample calibrated model statistics, etc.

The function `roll_backtest()` returns a named list containing the lists returned by function `trade_func()`. The list names are equal to the *end_points* dates. The number of list elements is equal to the number of *end_points* minus two (because the first and last end points can't be included in the backtest).

Value

An *xts* time series with the number of rows equal to the number of end points minus two.

Examples

```
## Not run:
# Combine two time series of prices
price_s <- cbind(rutils::etf_env$XLU, rutils::etf_env$XLP)
look_back <- 252
look_forward <- 22
# Define end points
end_points <- rutils::calc_endpoints(price_s, look_forward)
# Perform back-test
back_test <- roll_backtest(end_points=end_points,
    look_forward=look_forward,
    look_back=look_back,
    train_func = train_model,
    trade_func = trade_model,
    model_params = model_params,
    trading_params = trading_params,
    x_ts=price_s)

## End(Not run)
```

---

roll_conv — *Calculate the rolling convolutions (weighted sums) of a* time series *with a* column vector *of weights.*

Description

Calculate the rolling convolutions (weighted sums) of a *time series* with a *column vector* of weights.

Usage

```
roll_conv(tseries, weights)
```

Arguments

tseries	A *time series* or a *matrix* of data.
weights	A *column vector* of weights.

Details

The function `roll_conv()` calculates the convolutions of the *matrix* columns with a *column vector* of weights. It performs a loop over the *matrix* rows and multiplies the past (higher) values by the weights. It calculates the rolling weighted sums of the past values.

The function `roll_conv()` uses the `RcppArmadillo` function `arma::conv2()`. It performs a similar calculation to the standard `R` function `filter(x=tseries,filter=weight_s,method="convolution",sides=1)`, but it's over `6` times faster, and it doesn't produce any leading `NA` values.

Value

A *matrix* with the same dimensions as the input argument `tseries`.

Examples

```
## Not run:
# First example
# Calculate a time series of prices
re_turns <- na.omit(rutils::etf_env$re_turns[, c("IEF", "VTI")])
# Create simple weights equal to a 1 value plus zeros
weight_s <- matrix(c(1, rep(0, 10)), nc=1)
# Calculate rolling weighted sums
weight_ed <- HighFreq::roll_conv(re_turns, weight_s)
# Compare with original
all.equal(coredata(re_turns), weight_ed, check.attributes=FALSE)
# Second example
# Calculate exponentially decaying weights
weight_s <- exp(-0.2*(1:11))
weight_s <- matrix(weight_s/sum(weight_s), nc=1)
# Calculate rolling weighted sums
weight_ed <- HighFreq::roll_conv(re_turns, weight_s)
# Calculate rolling weighted sums using filter()
filter_ed <- filter(x=re_turns, filter=weight_s, method="convolution", sides=1)
# Compare both methods
all.equal(filter_ed[-(1:11), ], weight_ed[-(1:11), ], check.attributes=FALSE)

## End(Not run)
```

`roll_count` *Count the number of consecutive* `TRUE` *elements in a Boolean vector, and reset the count to zero after every* `FALSE` *element.*

Description

Count the number of consecutive `TRUE` elements in a Boolean vector, and reset the count to zero after every `FALSE` element.

Usage

```
roll_count(tseries)
```

Arguments

`tseries`	A *Boolean vector* of data.

Details

The function `roll_count()` calculates the number of consecutive `TRUE` elements in a Boolean vector, and it resets the count to zero after every `FALSE` element.

For example, the Boolean vector `FALSE`, `TRUE`, `TRUE`, `FALSE`, `FALSE`, `TRUE`, `TRUE`, `TRUE`, `TRUE`, `TRUE`, `FALSE`, is translated into `0`, `1`, `2`, `0`, `0`, `1`, `2`, `3`, `4`, `5`, `0`.

Value

An *integer vector* of the same length as the argument `tseries`.

Examples

```
## Not run:
# Calculate the number of consecutive TRUE elements
drop(HighFreq::roll_count(c(FALSE, TRUE, TRUE, FALSE, FALSE, TRUE, TRUE, TRUE, TRUE, TRUE, FALSE)))

## End(Not run)
```

`roll_fun` *Calculate a* matrix *of estimator values over a rolling look-back interval attached at the end points of a* time series *or a* matrix.

Description

Calculate a *matrix* of estimator values over a rolling look-back interval attached at the end points of a *time series* or a *matrix*.

Usage

```
roll_fun(
  tseries,
  fun = "calc_var",
  startp = 0L,
  endp = 0L,
  step = 1L,
  look_back = 1L,
  stub = 0L,
  method = "moment",
  con_fi = 0.75
)
```

Arguments

`tseries`	A *time series* or a *matrix* of data.
`fun`	A *string* specifying the estimator function (the default is `fun = "calc_var"`.)
`startp`	An *integer* vector of start points (the default is `startp = 0`).
`endp`	An *integer* vector of end points (the default is `endp = 0`).
`step`	The number of time periods between the end points (the default is `step = 1`).
`look_back`	The number of end points in the look-back interval (the default is `look_back = 1`).
`stub`	An *integer* value equal to the first end point for calculating the end points (the default is `stub = 0`).
`method`	A *string* specifying the type of the model for the estimator (the default is `method = "moment"`.)
`con_fi`	The confidence level for calculating the quantiles (the default is `con_fi = 0.75`).

Details

The function roll_fun() calculates a *matrix* of estimator values, over rolling look-back intervals attached at the end points of the *time series* tseries.

The function roll_fun() performs a loop over the end points, and at each end point it subsets the time series tseries over a look-back interval equal to look_back number of end points.

It passes the subset time series to the function specified by the argument fun, which calculates the statistic. See the functions calc_*() for a description of the different estimators.

If the arguments endp and startp are not given then it first calculates a vector of end points separated by step time periods. It calculates the end points along the rows of design using the function calc_endpoints(), with the number of time periods between the end points equal to step time periods.

For example, the rolling variance at 25 day end points, with a 75 day look-back, can be calculated using the parameters step = 25 and look_back = 3.

The function roll_fun() is implemented in RcppArmadillo C++ code, so it's many times faster than the equivalent R code.

Value

A *matrix* with the same number of columns as the input time series tseries, and the number of rows equal to the number of end points.

Examples

```
## Not run:
# Define time series of returns using package rutils
re_turns <- na.omit(rutils::etf_env$re_turns$VTI)
# Calculate the rolling variance at 25 day end points, with a 75 day look-back
var_rollfun <- HighFreq::roll_fun(re_turns, fun="calc_var", step=25, look_back=3)
# Calculate the rolling variance using roll_var()
var_roll <- HighFreq::roll_var(re_turns, step=25, look_back=3)
# Compare the two methods
all.equal(var_rollfun, var_roll, check.attributes=FALSE)
# Define end points and start points
end_p <- HighFreq::calc_endpoints(NROW(re_turns), step=25)
start_p <- HighFreq::calc_startpoints(end_p, look_back=3)
# Calculate the rolling variance using RcppArmadillo
var_rollfun <- HighFreq::roll_fun(re_turns, fun="calc_var", startp=start_p, endp=end_p)
# Calculate the rolling variance using R code
var_roll <- sapply(1:NROW(end_p), function(it) {
  var(re_turns[start_p[it]:end_p[it]+1, ])
})  # end sapply
# Compare the two methods
all.equal(drop(var_rollfun), var_roll, check.attributes=FALSE)
# Compare the speed of RcppArmadillo with R code
library(microbenchmark)
summary(microbenchmark(
  Rcpp=HighFreq::roll_fun(re_turns, fun="calc_var", startp=start_p, endp=end_p),
  Rcode=sapply(1:NROW(end_p), function(it) {
    var(re_turns[start_p[it]:end_p[it]+1, ])
  }),
  times=10))[, c(1, 4, 5)]  # end microbenchmark summary

## End(Not run)
```

roll_hurst *Calculate a time series of* Hurst *exponents over a rolling look-back interval.*

Description

Calculate a time series of *Hurst* exponents over a rolling look-back interval.

Usage

```
roll_hurst(oh_lc, look_back = 11)
```

Arguments

oh_lc	An *OHLC* time series of prices in *xts* format.
look_back	The size of the look-back interval, equal to the number of rows of data used for aggregating the *OHLC* prices.

Details

The function roll_hurst() calculates a time series of *Hurst* exponents from *OHLC* prices, over a rolling look-back interval.

The *Hurst* exponent is defined as the logarithm of the ratio of the price range, divided by the standard deviation of returns, and divided by the logarithm of the interval length.

The function roll_hurst() doesn't use the same definition as the rescaled range definition of the *Hurst* exponent. First, because the price range is calculated using *High* and *Low* prices, which produces bigger range values, and higher *Hurst* exponent estimates. Second, because the *Hurst* exponent is estimated using a single aggregation interval, instead of multiple intervals in the rescaled range definition.

The rationale for using a different definition of the *Hurst* exponent is that it's designed to be a technical indicator for use as input into trading models, rather than an estimator for statistical analysis.

Value

An *xts* time series with a single column and the same number of rows as the argument oh_lc.

Examples

```
# Calculate rolling Hurst for SPY in March 2009
hurst_rolling <- roll_hurst(oh_lc=HighFreq::SPY["2009-03"], look_back=11)
chart_Series(hurst_rolling["2009-03-10/2009-03-12"], name="SPY hurst_rolling")
```

roll_kurtosis *Calculate a* matrix *of kurtosis estimates over a rolling look-back interval attached at the end points of a* time series *or a* matrix.

Description

Calculate a *matrix* of kurtosis estimates over a rolling look-back interval attached at the end points of a *time series* or a *matrix*.

Usage

```
roll_kurtosis(
  tseries,
  startp = 0L,
  endp = 0L,
  step = 1L,
  look_back = 1L,
  stub = 0L,
  method = "moment",
  con_fi = 0.75
)
```

Arguments

tseries	A *time series* or a *matrix* of data.
startp	An *integer* vector of start points (the default is startp = 0).
endp	An *integer* vector of end points (the default is endp = 0).
step	The number of time periods between the end points (the default is step = 1).
look_back	The number of end points in the look-back interval (the default is look_back = 1).
stub	An *integer* value equal to the first end point for calculating the end points (the default is stub = 0).
method	A *string* specifying the type of the kurtosis model (the default is method = "moment" - see Details).
con_fi	The confidence level for calculating the quantiles (the default is con_fi = 0.75).

Details

The function roll_kurtosis() calculates a *matrix* of kurtosis estimates over rolling look-back intervals attached at the end points of the *time series* tseries.

The function roll_kurtosis() performs a loop over the end points, and at each end point it subsets the time series tseries over a look-back interval equal to look_back number of end points.

It passes the subset time series to the function calc_kurtosis(), which calculates the kurtosis. See the function calc_kurtosis() for a description of the kurtosis methods.

If the arguments endp and startp are not given then it first calculates a vector of end points separated by step time periods. It calculates the end points along the rows of design using the function calc_endpoints(), with the number of time periods between the end points equal to step time periods.

For example, the rolling kurtosis at 25 day end points, with a 75 day look-back, can be calculated using the parameters step = 25 and look_back = 3.

The function roll_kurtosis() is implemented in RcppArmadillo C++ code, so it's many times faster than the equivalent R code.

Value

A *matrix* of kurtosis estimates with the same number of columns as the input time series tseries, and the number of rows equal to the number of end points.

Examples

```
## Not run:
# Define time series of returns using package rutils
re_turns <- na.omit(rutils::etf_env$re_turns$VTI)
# Define end points and start points
end_p <- 1 + HighFreq::calc_endpoints(NROW(re_turns), step=25)
start_p <- HighFreq::calc_startpoints(end_p, look_back=3)
# Calculate the rolling kurtosis at 25 day end points, with a 75 day look-back
kurto_sis <- HighFreq::roll_kurtosis(re_turns, step=25, look_back=3)
# Calculate the rolling kurtosis using R code
kurt_r <- sapply(1:NROW(end_p), function(it) {
  HighFreq::calc_kurtosis(re_turns[start_p[it]:end_p[it], ])
})  # end sapply
# Compare the kurtosis estimates
all.equal(drop(kurto_sis), kurt_r, check.attributes=FALSE)
# Compare the speed of RcppArmadillo with R code
library(microbenchmark)
summary(microbenchmark(
  Rcpp=HighFreq::roll_kurtosis(re_turns, step=25, look_back=3),
  Rcode=sapply(1:NROW(end_p), function(it) {
    HighFreq::calc_kurtosis(re_turns[start_p[it]:end_p[it], ])
  }),
  times=10))[, c(1, 4, 5)]  # end microbenchmark summary

## End(Not run)
```

---

roll_mean — *Calculate a* matrix *of mean (location) estimates over a rolling look-back interval attached at the end points of a* time series *or a* matrix.

Description

Calculate a *matrix* of mean (location) estimates over a rolling look-back interval attached at the end points of a *time series* or a *matrix*.

Usage

```
roll_mean(
  tseries,
  startp = 0L,
  endp = 0L,
  step = 1L,
```

```
  look_back = 1L,
  stub = 0L,
  method = "moment",
  con_fi = 0.75
)
```

Arguments

tseries	A *time series* or a *matrix* of data.
startp	An *integer* vector of start points (the default is startp = 0).
endp	An *integer* vector of end points (the default is endp = 0).
step	The number of time periods between the end points (the default is step = 1).
look_back	The number of end points in the look-back interval (the default is look_back = 1).
stub	An *integer* value equal to the first end point for calculating the end points (the default is stub = 0).
method	A *character* string representing the type of mean measure of (the default is method = "moment").

Details

The function roll_mean() calculates a *matrix* of mean (location) estimates over rolling look-back intervals attached at the end points of the *time series* tseries.

The function roll_mean() performs a loop over the end points, and at each end point it subsets the time series tseries over a look-back interval equal to look_back number of end points.

It passes the subset time series to the function calc_mean(), which calculates the mean (location). See the function calc_mean() for a description of the mean methods.

If the arguments endp and startp are not given then it first calculates a vector of end points separated by step time periods. It calculates the end points along the rows of tseries using the function calc_endpoints(), with the number of time periods between the end points equal to step time periods.

For example, the rolling mean at 25 day end points, with a 75 day look-back, can be calculated using the parameters step = 25 and look_back = 3.

The function roll_mean() with the parameter step = 1 performs the same calculation as the function roll_mean() from package RcppRoll, but it's several times faster because it uses RcppArmadillo C++ code.

The function roll_mean() is implemented in RcppArmadillo C++ code, so it's many times faster than the equivalent R code.

If only a simple rolling mean is required (not the median) then other functions like roll_sum() or roll_vec() may be even faster.

Value

A *matrix* of mean (location) estimates with the same number of columns as the input time series tseries, and the number of rows equal to the number of end points.

Examples

```
## Not run:
# Define time series of returns using package rutils
re_turns <- na.omit(rutils::etf_env$re_turns$VTI)
# Calculate the rolling means at 25 day end points, with a 75 day look-back
means <- HighFreq::roll_mean(re_turns, step=25, look_back=3)
# Compare the mean estimates over 11-period look-back intervals
all.equal(HighFreq::roll_mean(re_turns, look_back=11)[-(1:10), ],
  drop(RcppRoll::roll_mean(re_turns, n=11)), check.attributes=FALSE)
# Define end points and start points
end_p <- HighFreq::calc_endpoints(NROW(re_turns), step=25)
start_p <- HighFreq::calc_startpoints(end_p, look_back=3)
# Calculate the rolling means using RcppArmadillo
means <- HighFreq::roll_mean(re_turns, startp=start_p, endp=end_p)
# Calculate the rolling medians using RcppArmadillo
medianscpp <- HighFreq::roll_mean(re_turns, startp=start_p, endp=end_p, method="nonparametric")
# Calculate the rolling medians using R
medians = sapply(1:NROW(end_p), function(i) {
  median(re_turns[start_p[i]:end_p[i] + 1])
})  # end sapply
all.equal(medians, drop(medianscpp))
# Compare the speed of RcppArmadillo with R code
library(microbenchmark)
summary(microbenchmark(
  Rcpp=HighFreq::roll_mean(re_turns, startp=start_p, endp=end_p, method="nonparametric"),
  Rcode=sapply(1:NROW(end_p), function(i) {median(re_turns[start_p[i]:end_p[i] + 1])}),
  times=10))[, c(1, 4, 5)]

## End(Not run)
```

`roll_ohlc` *Aggregate a time series to an* OHLC *time series with lower periodicity.*

Description

Given a time series of prices at a higher periodicity (say seconds), it calculates the *OHLC* prices at a lower periodicity (say minutes).

Usage

```
roll_ohlc(tseries, endp)
```

Arguments

`tseries`	A *time series* or a *matrix* with multiple columns of data.
endp	An *integer vector* of end points.

Details

The function `roll_ohlc()` performs a loop over the end points *endp*, along the rows of the data `tseries`. At each end point, it selects the past rows of the data `tseries`, starting at the first bar after the previous end point, and then calls the function `agg_ohlc()` on the selected data `tseries` to calculate the aggregations.

The function `roll_ohlc()` can accept either a single column of data or four columns of *OHLC* data. It can also accept an additional column containing the trading volume.

The function `roll_ohlc()` performs a similar aggregation as the function `to.period()` from package xts.

Value

A *matrix* with *OHLC* data, with the number of rows equal to the number of *endp* minus one.

Examples

```
## Not run:
# Define matrix of OHLC data
oh_lc <- rutils::etf_env$VTI[, 1:5]
# Define end points at 25 day intervals
end_p <- HighFreq::calc_endpoints(NROW(oh_lc), step=25)
# Aggregate over end_p:
ohlc_agg <- HighFreq::roll_ohlc(tseries=oh_lc, endp=end_p)
# Compare with xts::to.period()
ohlc_agg_xts <- .Call("toPeriod", oh_lc, as.integer(end_p+1), TRUE, NCOL(oh_lc), FALSE, FALSE, colnames(oh_lc)
all.equal(ohlc_agg, coredata(ohlc_agg_xts), check.attributes=FALSE)

## End(Not run)
```

---

roll_reg *Calculate a* matrix *of regression coefficients, their t-values, and z-scores, at the end points of the design matrix.*

Description

Calculate a *matrix* of regression coefficients, their t-values, and z-scores, at the end points of the design matrix.

Usage

```
roll_reg(
  response,
  design,
  startp = 0L,
  endp = 0L,
  step = 1L,
  look_back = 1L,
  stub = 0L,
  method = "least_squares",
  eigen_thresh = 0.001,
  eigen_max = 0L,
  con_fi = 0.1,
  alpha = 0
)
```

Arguments

response	A single-column *time series* or a *vector* of response data.
design	A *time series* or a *matrix* of design data (predictor or explanatory data).
startp	An *integer* vector of start points (the default is startp = 0).
endp	An *integer* vector of end points (the default is endp = 0).
step	The number of time periods between the end points (the default is step = 1).
look_back	The number of end points in the look-back interval (the default is look_back = 1).
stub	An *integer* value equal to the first end point for calculating the end points (the default is stub = 0).
method	A *string* specifying the type of the regression model the default is method = "least_squares" - see Details).
eigen_thresh	A *numeric* threshold level for discarding small singular values in order to regularize the inverse of the design matrix (the default is 0.001).
eigen_max	An *integer* equal to the number of singular values used for calculating the regularized inverse of the design matrix (the default is 0 - equivalent to eigen_max equal to the number of columns of design).
con_fi	The confidence level for calculating the quantiles (the default is con_fi = 0.75).
alpha	The shrinkage intensity between 0 and 1. (the default is 0).

Details

The function roll_reg() calculates a *matrix* of regression coefficients, their t-values, and z-scores at the end points of the design matrix.

The function roll_reg() performs a loop over the end points, and at each end point it subsets the time series design over a look-back interval equal to look_back number of end points.

It passes the subset time series to the function calc_reg(), which calculates the regression data.

If the arguments endp and startp are not given then it first calculates a vector of end points separated by step time periods. It calculates the end points along the rows of design using the function calc_endpoints(), with the number of time periods between the end points equal to step time periods.

For example, the rolling regression at 25 day end points, with a 75 day look-back, can be calculated using the parameters step = 25 and look_back = 3.

Value

A *matrix* with the same number of rows as design, and a number of columns equal to 2n+3, where n is the number of columns of design.

Examples

```
## Not run:
# Calculate historical returns
re_turns <- na.omit(rutils::etf_env$re_turns[, c("XLP", "VTI")])
# Define monthly end points and start points
end_p <- xts::endpoints(re_turns, on="months")[-1]
look_back <- 12
start_p <- c(rep(1, look_back), end_p[1:(NROW(end_p)-look_back)])
# Calculate rolling betas using RcppArmadillo
```

```
reg_stats <- HighFreq::roll_reg(response=re_turns[, 1], design=re_turns[, 2], endp=(end_p-1), startp=(start_p
beta_s <- reg_stats[, 2]
# Calculate rolling betas in R
betas_r <- sapply(1:NROW(end_p), FUN=function(ep) {
  da_ta <- re_turns[start_p[ep]:end_p[ep], ]
  drop(cov(da_ta[, 1], da_ta[, 2])/var(da_ta[, 2]))
})  # end sapply
# Compare the outputs of both functions
all.equal(beta_s, betas_r, check.attributes=FALSE)

## End(Not run)
```

`roll_scale` *Perform a rolling scaling (standardization) of the columns of a* matrix *of data using* `RcppArmadillo`.

Description

Perform a rolling scaling (standardization) of the columns of a *matrix* of data using `RcppArmadillo`.

Usage

```
roll_scale(matrix, look_back, use_median = FALSE)
```

Arguments

`use_median`	A *Boolean* argument: if `TRUE` then the centrality (central tendency) is calculated as the *median* and the dispersion is calculated as the *median absolute deviation* (*MAD*). If `use_median` is `FALSE` then the centrality is calculated as the *mean* and the dispersion is calculated as the *standard deviation* (the default is `use_median = FALSE`)
`matrix`	A *matrix* of data.
`look_back`	The length of the look-back interval, equal to the number of rows of data used in the scaling.

Details

The function `roll_scale()` performs a rolling scaling (standardization) of the columns of the `matrix` argument using `RcppArmadillo`. The function `roll_scale()` performs a loop over the rows of `matrix`, subsets a number of previous (past) rows equal to `look_back`, and scales the subset matrix. It assigns the last row of the scaled subset *matrix* to the return matrix.

If the argument `use_median` is `FALSE` (the default), then it performs the same calculation as the function `roll::roll_scale()`. If the argument `use_median` is `TRUE`, then it calculates the centrality as the *median* and the dispersion as the *median absolute deviation* (*MAD*).

Value

A *matrix* with the same dimensions as the input argument `matrix`.

Examples

```
## Not run:
mat_rix <- matrix(rnorm(20000), nc=2)
look_back <- 11
rolled_scaled <- roll::roll_scale(data=mat_rix, width = look_back, min_obs=1)
rolled_scaled2 <- roll_scale(matrix=mat_rix, look_back = look_back, use_median=FALSE)
all.equal(rolled_scaled[-1, ], rolled_scaled2[-1, ])

## End(Not run)
```

`roll_sharpe` *Calculate a time series of Sharpe ratios over a rolling look-back interval for an* OHLC *time series.*

Description

Calculate a time series of Sharpe ratios over a rolling look-back interval for an *OHLC* time series.

Usage

```
roll_sharpe(oh_lc, look_back = 11)
```

Arguments

`oh_lc`	An *OHLC* time series of prices in *xts* format.
`look_back`	The size of the look-back interval, equal to the number of rows of data used for aggregating the *OHLC* prices.

Details

The function `roll_sharpe()` calculates the rolling Sharpe ratio defined as the ratio of percentage returns over the look-back interval, divided by the average volatility of percentage returns.

Value

An *xts* time series with a single column and the same number of rows as the argument `oh_lc`.

Examples

```
# Calculate rolling Sharpe ratio over SPY
sharpe_rolling <- roll_sharpe(oh_lc=HighFreq::SPY, look_back=11)
```

roll_skew *Calculate a* matrix *of skewness estimates over a rolling look-back interval attached at the end points of a* time series *or a* matrix.

Description

Calculate a *matrix* of skewness estimates over a rolling look-back interval attached at the end points of a *time series* or a *matrix*.

Usage

```
roll_skew(
  tseries,
  startp = 0L,
  endp = 0L,
  step = 1L,
  look_back = 1L,
  stub = 0L,
  method = "moment",
  con_fi = 0.75
)
```

Arguments

tseries	A *time series* or a *matrix* of data.
startp	An *integer* vector of start points (the default is startp = 0).
endp	An *integer* vector of end points (the default is endp = 0).
step	The number of time periods between the end points (the default is step = 1).
look_back	The number of end points in the look-back interval (the default is look_back = 1).
stub	An *integer* value equal to the first end point for calculating the end points (the default is stub = 0).
method	A *string* specifying the type of the skewness model (the default is method = "moment" - see Details).
con_fi	The confidence level for calculating the quantiles (the default is con_fi = 0.75).

Details

The function roll_skew() calculates a *matrix* of skewness estimates over rolling look-back intervals attached at the end points of the *time series* tseries.

The function roll_skew() performs a loop over the end points, and at each end point it subsets the time series tseries over a look-back interval equal to look_back number of end points.

It passes the subset time series to the function calc_skew(), which calculates the skewness. See the function calc_skew() for a description of the skewness methods.

If the arguments endp and startp are not given then it first calculates a vector of end points separated by step time periods. It calculates the end points along the rows of tseries using the function calc_endpoints(), with the number of time periods between the end points equal to step time periods.

For example, the rolling skewness at 25 day end points, with a 75 day look-back, can be calculated using the parameters step = 25 and look_back = 3.

The function roll_skew() is implemented in RcppArmadillo C++ code, so it's many times faster than the equivalent R code.

Value

A *matrix* of skewness estimates with the same number of columns as the input time series tseries, and the number of rows equal to the number of end points.

Examples

```
## Not run:
# Define time series of returns using package rutils
re_turns <- na.omit(rutils::etf_env$re_turns$VTI)
# Define end points and start points
end_p <- 1 + HighFreq::calc_endpoints(NROW(re_turns), step=25)
start_p <- HighFreq::calc_startpoints(end_p, look_back=3)
# Calculate the rolling skewness at 25 day end points, with a 75 day look-back
skew_ness <- HighFreq::roll_skew(re_turns, step=25, look_back=3)
# Calculate the rolling skewness using R code
skew_r <- sapply(1:NROW(end_p), function(it) {
  HighFreq::calc_skew(re_turns[start_p[it]:end_p[it], ])
})  # end sapply
# Compare the skewness estimates
all.equal(drop(skew_ness), skew_r, check.attributes=FALSE)
# Compare the speed of RcppArmadillo with R code
library(microbenchmark)
summary(microbenchmark(
  Rcpp=HighFreq::roll_skew(re_turns, step=25, look_back=3),
  Rcode=sapply(1:NROW(end_p), function(it) {
    HighFreq::calc_skew(re_turns[start_p[it]:end_p[it], ])
  }),
  times=10))[, c(1, 4, 5)]  # end microbenchmark summary

## End(Not run)
```

---

roll_stats *Calculate a vector of statistics over an* OHLC *time series, and calculate a rolling mean over the statistics.*

Description

Calculate a vector of statistics over an *OHLC* time series, and calculate a rolling mean over the statistics.

Usage

```
roll_stats(
  oh_lc,
  calc_stats = "run_variance",
  look_back = 11,
  weight_ed = TRUE,
  ...
)
```

Arguments

...	additional parameters to the function calc_stats.
oh_lc	An *OHLC* time series of prices and trading volumes, in *xts* format.
calc_stats	The name of the function for estimating statistics of a single row of *OHLC* data, such as volatility, skew, and higher moments.
look_back	The size of the look-back interval, equal to the number of rows of data used for calculating the rolling mean.
weight_ed	*Boolean* argument: should statistic be weighted by trade volume? (default TRUE)

Details

The function roll_stats() calculates a vector of statistics over an *OHLC* time series, such as volatility, skew, and higher moments. The statistics could also be any other aggregation of a single row of *OHLC* data, for example the *High* price minus the *Low* price squared. The length of the vector of statistics is equal to the number of rows of the argument oh_lc. Then it calculates a trade volume weighted rolling mean over the vector of statistics over and calculate statistics.

Value

An *xts* time series with a single column and the same number of rows as the argument oh_lc.

Examples

```
# Calculate time series of rolling variance and skew estimates
var_rolling <- roll_stats(oh_lc=HighFreq::SPY, look_back=21)
skew_rolling <- roll_stats(oh_lc=HighFreq::SPY, calc_stats="run_skew", look_back=21)
skew_rolling <- skew_rolling/(var_rolling)^(1.5)
skew_rolling[1, ] <- 0
skew_rolling <- rutils::na_locf(skew_rolling)
```

---

roll_sum *Calculate the rolling sums over a* time series *or a* matrix *using* Rcpp.

Description

Calculate the rolling sums over a *time series* or a *matrix* using *Rcpp*.

Usage

```
roll_sum(tseries, look_back = 1L)
```

Arguments

tseries	A *time series* or a *matrix*.
look_back	The length of the look-back interval, equal to the number of data points included in calculating the rolling sum (the default is look_back = 1).

Details

The function `roll_sum()` calculates the rolling sums over the columns of the data `tseries`.

The function `roll_sum()` returns a *matrix* with the same dimensions as the input argument `tseries`.

The function `roll_sum()` uses the fast `RcppArmadillo` function `arma::cumsum()`, without explicit loops. The function `roll_sum()` is several times faster than `rutils::roll_sum()` which uses vectorized `R` code.

Value

A *matrix* with the same dimensions as the input argument `tseries`.

Examples

```
## Not run:
# Calculate historical returns
re_turns <- na.omit(rutils::etf_env$re_turns[, c("VTI", "IEF")])
# Define parameters
look_back <- 22
# Calculate rolling sums and compare with rutils::roll_sum()
c_sum <- HighFreq::roll_sum(re_turns, look_back)
r_sum <- rutils::roll_sum(re_turns, look_back)
all.equal(c_sum, coredata(r_sum), check.attributes=FALSE)
# Calculate rolling sums using R code
r_sum <- apply(zoo::coredata(re_turns), 2, cumsum)
lag_sum <- rbind(matrix(numeric(2*look_back), nc=2), r_sum[1:(NROW(r_sum) - look_back), ])
r_sum <- (r_sum - lag_sum)
all.equal(c_sum, r_sum, check.attributes=FALSE)

## End(Not run)
```

---

roll_sumep *Calculate the rolling sums at the end points of a* time series *or a* matrix.

Description

Calculate the rolling sums at the end points of a *time series* or a *matrix*.

Usage

```
roll_sumep(
  tseries,
  startp = 0L,
  endp = 0L,
  step = 1L,
  look_back = 1L,
  stub = 0L
)
```

Arguments

tseries	A *time series* or a *matrix*.
startp	An *integer* vector of start points (the default is startp = 0).
endp	An *integer* vector of end points (the default is endp = 0).
step	The number of time periods between the end points (the default is step = 1).
look_back	The number of end points in the look-back interval (the default is look_back = 1).
stub	An *integer* value equal to the first end point for calculating the end points.

Details

The function roll_sumep() calculates the rolling sums at the end points of the *time series* tseries.

The function roll_sumep() is implemented in RcppArmadillo C++ code, which makes it several times faster than R code.

Value

A *matrix* with the same number of columns as the input time series tseries, and the number of rows equal to the number of end points.

Examples

```
## Not run:
# Calculate historical returns
re_turns <- na.omit(rutils::etf_env$re_turns[, c("VTI", "IEF")])
# Define end points at 25 day intervals
end_p <- HighFreq::calc_endpoints(NROW(re_turns), step=25)
# Define start points as 75 day lag of end points
start_p <- HighFreq::calc_startpoints(end_p, look_back=3)
# Calculate rolling sums using Rcpp
c_sum <- HighFreq::roll_sumep(re_turns, startp=start_p, endp=end_p)
# Calculate rolling sums using R code
r_sum <- sapply(1:NROW(end_p), function(ep) {
colSums(re_turns[(start_p[ep]+1):(end_p[ep]+1), ])
  })  # end sapply
r_sum <- t(r_sum)
all.equal(c_sum, r_sum, check.attributes=FALSE)

## End(Not run)
```

---

roll_var — *Calculate a* matrix *of dispersion (variance) estimates over a rolling look-back interval attached at the end points of a* time series *or a* matrix.

Description

Calculate a *matrix* of dispersion (variance) estimates over a rolling look-back interval attached at the end points of a *time series* or a *matrix*.

Usage

```
roll_var(
  tseries,
  startp = 0L,
  endp = 0L,
  step = 1L,
  look_back = 1L,
  stub = 0L,
  method = "moment",
  con_fi = 0.75
)
```

Arguments

tseries	A *time series* or a *matrix* of data.
startp	An *integer* vector of start points (the default is startp = 0).
endp	An *integer* vector of end points (the default is endp = 0).
step	The number of time periods between the end points (the default is step = 1).
look_back	The number of end points in the look-back interval (the default is look_back = 1).
stub	An *integer* value equal to the first end point for calculating the end points (the default is stub = 0).
method	A *character* string representing the type of the measure of dispersion (the default is method = "moment").

Details

The function roll_var() calculates a *matrix* of dispersion (variance) estimates over rolling look-back intervals attached at the end points of the *time series* tseries.

The function roll_var() performs a loop over the end points, and at each end point it subsets the time series tseries over a look-back interval equal to look_back number of end points.

It passes the subset time series to the function calc_var(), which calculates the dispersion. See the function calc_var() for a description of the dispersion methods.

If the arguments endp and startp are not given then it first calculates a vector of end points separated by step time periods. It calculates the end points along the rows of tseries using the function calc_endpoints(), with the number of time periods between the end points equal to step time periods.

For example, the rolling variance at 25 day end points, with a 75 day look-back, can be calculated using the parameters step = 25 and look_back = 3.

The function roll_var() with the parameter step = 1 performs the same calculation as the function roll_var() from package RcppRoll, but it's several times faster because it uses RcppArmadillo C++ code.

The function roll_var() is implemented in RcppArmadillo C++ code, so it's many times faster than the equivalent R code.

Value

A *matrix* dispersion (variance) estimates with the same number of columns as the input time series tseries, and the number of rows equal to the number of end points.

Examples

```
## Not run:
# Define time series of returns using package rutils
re_turns <- na.omit(rutils::etf_env$re_turns$VTI)
# Calculate the rolling variance at 25 day end points, with a 75 day look-back
vari_ance <- HighFreq::roll_var(re_turns, step=25, look_back=3)
# Compare the variance estimates over 11-period look-back intervals
all.equal(HighFreq::roll_var(re_turns, look_back=11)[-(1:10), ],
  drop(RcppRoll::roll_var(re_turns, n=11)), check.attributes=FALSE)
# Compare the speed of HighFreq::roll_var() with RcppRoll::roll_var()
library(microbenchmark)
summary(microbenchmark(
  Rcpp=HighFreq::roll_var(re_turns, look_back=11),
  RcppRoll=RcppRoll::roll_var(re_turns, n=11),
  times=10))[, c(1, 4, 5)]  # end microbenchmark summary
# Compare the speed of HighFreq::roll_var() with TTR::runMAD()
summary(microbenchmark(
    Rcpp=HighFreq::roll_var(re_turns, look_back=11, method="quantile"),
    TTR=TTR::runMAD(re_turns, n = 11),
    times=10))[, c(1, 4, 5)]  # end microbenchmark summary

## End(Not run)
```

`roll_var_ohlc` *Calculate a* vector *of variance estimates over a rolling look-back interval attached at the end points of a* time series *or a* matrix *with* OHLC *price data.*

Description

Calculate a *vector* of variance estimates over a rolling look-back interval attached at the end points of a *time series* or a *matrix* with *OHLC* price data.

Usage

```
roll_var_ohlc(
  ohlc,
  startp = 0L,
  endp = 0L,
  step = 1L,
  look_back = 1L,
  stub = 0L,
  method = "yang_zhang",
  scale = TRUE,
  in_dex = 0L
)
```

Arguments

`ohlc`	A *time series* or a *matrix* with *OHLC* price data.
`startp`	An *integer* vector of start points (the default is `startp = 0`).
`endp`	An *integer* vector of end points (the default is `endp = 0`).

step	The number of time periods between the end points (the default is step = 1).
look_back	The number of end points in the look-back interval (the default is look_back = 1).
stub	An *integer* value equal to the first end point for calculating the end points (the default is stub = 0).
method	A *character* string representing the price range estimator for calculating the variance. The estimators include: • "close" close-to-close estimator, • "rogers_satchell" Rogers-Satchell estimator, • "garman_klass" Garman-Klass estimator, • "garman_klass_yz" Garman-Klass with account for close-to-open price jumps, • "yang_zhang" Yang-Zhang estimator, (The default is the *"yang_zhang"* estimator.)
scale	*Boolean* argument: Should the returns be divided by the time index, the number of seconds in each period? (The default is scale = TRUE.)
in_dex	A *vector* with the time index of the *time series*. This is an optional argument (the default is in_dex=0).

Details

The function roll_var_ohlc() calculates a *vector* of variance estimates over a rolling look-back interval attached at the end points of the *time series* ohlc.

The input *OHLC time series* ohlc is assumed to contain the log prices.

The function roll_var_ohlc() performs a loop over the end points, subsets the previous (past) rows of ohlc, and passes them into the function calc_var_ohlc().

At each end point, the variance is calculated over a look-back interval equal to look_back number of end points. In the initial warmup period, the variance is calculated over an expanding look-back interval.

If the arguments endp and startp are not given then it first calculates a vector of end points separated by step time periods. It calculates the end points along the rows of ohlc using the function calc_endpoints(), with the number of time periods between the end points equal to step time periods.

For example, the rolling variance at daily end points with an 11 day look-back, can be calculated using the parameters step = 1 and look_back = 1 (Assuming the ohlc data has daily frequency.)

Similarly, the rolling variance at 25 day end points with a 75 day look-back, can be calculated using the parameters step = 25 and look_back = 3 (because 3*25 = 75).

The function roll_var_ohlc() calculates the variance from all the different intra-day and day-over-day returns (defined as the differences between *OHLC* prices), using several different variance estimation methods.

The default method is *"yang_zhang"*, which theoretically has the lowest standard error among unbiased estimators. The methods *"close"*, *"garman_klass_yz"*, and *"yang_zhang"* do account for *close-to-open* price jumps, while the methods *"garman_klass"* and *"rogers_satchell"* do not account for *close-to-open* price jumps.

If scale is TRUE (the default), then the returns are divided by the differences of the time index (which scales the variance to the units of variance per second squared.) This is useful when calculating the variance from minutely bar data, because dividing returns by the number of seconds

decreases the effect of overnight price jumps. If the time index is in days, then the variance is equal to the variance per day squared.

The optional argument `in_dex` is the time index of the *time series* `ohlc`. If the time index is in seconds, then the differences of the index are equal to the number of seconds in each time period. If the time index is in days, then the differences are equal to the number of days in each time period.

The function `roll_var_ohlc()` is implemented in `RcppArmadillo` `C++` code, so it's many times faster than the equivalent `R` code.

Value

A column *vector* of variance estimates, with the number of rows equal to the number of end points.

Examples

```
## Not run:
# Extract the log OHLC prices of SPY
oh_lc <- log(HighFreq::SPY)
# Extract the time index of SPY prices
in_dex <- c(1, diff(xts::.index(oh_lc)))
# Rolling variance at minutely end points, with a 21 minute look-back
var_rolling <- HighFreq::roll_var_ohlc(oh_lc,
                               step=1, look_back=21,
                               method="yang_zhang",
                               in_dex=in_dex, scale=TRUE)
# Daily OHLC prices
oh_lc <- rutils::etf_env$VTI
in_dex <- c(1, diff(xts::.index(oh_lc)))
# Rolling variance at 5 day end points, with a 20 day look-back (20=4*5)
var_rolling <- HighFreq::roll_var_ohlc(oh_lc,
                               step=5, look_back=4,
                               method="yang_zhang",
                               in_dex=in_dex, scale=TRUE)
# Same calculation in R
n_rows <- NROW(oh_lc)
lag_close = HighFreq::lag_it(oh_lc[, 4])
end_p <- drop(HighFreq::calc_endpoints(n_rows, 3)) + 1
start_p <- drop(HighFreq::calc_startpoints(end_p, 2))
n_pts <- NROW(end_p)
var_rollingr <- sapply(2:n_pts, function(it) {
  ran_ge <- start_p[it]:end_p[it]
  sub_ohlc = oh_lc[ran_ge, ]
  sub_close = lag_close[ran_ge]
  sub_index = in_dex[ran_ge]
  HighFreq::calc_var_ohlc(sub_ohlc, lag_close=sub_close, scale=TRUE, in_dex=sub_index)
})  # end sapply
var_rollingr <- c(0, var_rollingr)
all.equal(drop(var_rolling), var_rollingr)

## End(Not run)
```

`roll_var_vec` *Calculate a* vector *of variance estimates over a rolling look-back interval for a single-column* time series *or a* column vector*, using* `RcppArmadillo`.

Description

Calculate a *vector* of variance estimates over a rolling look-back interval for a single-column *time series* or a *column vector*, using `RcppArmadillo`.

Usage

```
roll_var_vec(tseries, look_back = 1L)
```

Arguments

`tseries`	A single-column *time series* or a *column vector*.
`look_back`	The length of the look-back interval, equal to the number of *vector* elements used for calculating a single variance estimate (the default is `look_back = 1`).

Details

The function `roll_var_vec()` calculates a *vector* of variance estimates over a rolling look-back interval for a single-column *time series* or a *column vector*, using `RcppArmadillo` `C++` code.

The function `roll_var_vec()` uses an expanding look-back interval in the initial warmup period, to calculate the same number of elements as the input argument `tseries`.

The function `roll_var_vec()` performs the same calculation as the function `roll_var()` from package RcppRoll, but it's several times faster because it uses `RcppArmadillo` `C++` code.

Value

A *column vector* with the same number of elements as the input argument `tseries`.

Examples

```
## Not run:
# Create a vector of random returns
re_turns <- rnorm(1e6)
# Compare the variance estimates over 11-period look-back intervals
all.equal(drop(HighFreq::roll_var_vec(re_turns, look_back=11))[-(1:10)],
  RcppRoll::roll_var(re_turns, n=11))
# Compare the speed of RcppArmadillo with RcppRoll
library(microbenchmark)
summary(microbenchmark(
  Rcpp=HighFreq::roll_var_vec(re_turns, look_back=11),
  RcppRoll=RcppRoll::roll_var(re_turns, n=11),
  times=10))[, c(1, 4, 5)]  # end microbenchmark summary

## End(Not run)
```

roll_vec *Calculate the rolling sums over a single-column* time series *or a* column vector *using* Rcpp.

Description

Calculate the rolling sums over a single-column *time series* or a *column vector* using *Rcpp*.

Usage

```
roll_vec(tseries, look_back)
```

Arguments

tseries	A single-column *time series* or a *column vector* (a single-column matrix).
look_back	The length of the look-back interval, equal to the number of elements of data used for calculating the sum.

Details

The function `roll_vec()` calculates a *column vector* of rolling sums, over a *column vector* of data, using fast *Rcpp* `C++` code. The function `roll_vec()` is several times faster than `rutils::roll_sum()` which uses vectorized `R` code.

Value

A *column vector* of the same length as the argument `tseries`.

Examples

```
## Not run:
# Define a single-column matrix of returns
re_turns <- zoo::coredata(na.omit(rutils::etf_env$re_turns$VTI))
# Calculate rolling sums over 11-period look-back intervals
sum_rolling <- HighFreq::roll_vec(re_turns, look_back=11)
# Compare HighFreq::roll_vec() with rutils::roll_sum()
all.equal(HighFreq::roll_vec(re_turns, look_back=11),
         rutils::roll_sum(re_turns, look_back=11),
         check.attributes=FALSE)
# Compare the speed of Rcpp with R code
library(microbenchmark)
summary(microbenchmark(
  Rcpp=HighFreq::roll_vec(re_turns, look_back=11),
  Rcode=rutils::roll_sum(re_turns, look_back=11),
  times=10))[, c(1, 4, 5)]  # end microbenchmark summary

## End(Not run)
```

roll_vecw *Calculate the rolling weighted sums over a single-column* time series *or a* column vector *using* RcppArmadillo.

Description

Calculate the rolling weighted sums over a single-column *time series* or a *column vector* using RcppArmadillo.

Usage

```
roll_vecw(tseries, weights)
```

Arguments

tseries	A single-column *time series* or a *column vector* (a single-column matrix).
weights	A *column vector* of weights.

Details

The function roll_vecw() calculates the rolling weighted sums of a *column vector* over its past values (a convolution with the *column vector* of weights), using RcppArmadillo. It performs a similar calculation as the standard R function stats::filter(x=series,filter=weight_s,method="convolution",sides=
but it's over 6 times faster, and it doesn't produce any NA values.

Value

A *column vector* of the same length as the argument tseries.

Examples

```
## Not run:
# First example
# Define a single-column matrix of returns
re_turns <- zoo::coredata(na.omit(rutils::etf_env$re_turns$VTI))
# Create simple weights
weight_s <- matrix(c(1, rep(0, 10)))
# Calculate rolling weighted sums
weight_ed <- HighFreq::roll_vecw(tseries=re_turns, weights=weight_s)
# Compare with original
all.equal(zoo::coredata(re_turns), weight_ed, check.attributes=FALSE)
# Second example
# Create exponentially decaying weights
weight_s <- matrix(exp(-0.2*1:11))
weight_s <- weight_s/sum(weight_s)
# Calculate rolling weighted sums
weight_ed <- HighFreq::roll_vecw(tseries=re_turns, weights=weight_s)
# Calculate rolling weighted sums using filter()
filter_ed <- stats::filter(x=re_turns, filter=weight_s, method="convolution", sides=1)
# Compare both methods
all.equal(filter_ed[-(1:11)], weight_ed[-(1:11)], check.attributes=FALSE)
# Compare the speed of Rcpp with R code
library(microbenchmark)
```

```
summary(microbenchmark(
  Rcpp=HighFreq::roll_vecw(tseries=re_turns, weights=weight_s),
  Rcode=stats::filter(x=re_turns, filter=weight_s, method="convolution", sides=1),
  times=10))[, c(1, 4, 5)]  # end microbenchmark summary

## End(Not run)
```

`roll_vwap` *Calculate the volume-weighted average price of an* OHLC *time series over a rolling look-back interval.*

Description

Performs the same operation as function `VWAP()` from package VWAP, but using vectorized functions, so it's a little faster.

Usage

```
roll_vwap(oh_lc, x_ts = oh_lc[, 4], look_back)
```

Arguments

`oh_lc`	An *OHLC* time series of prices in *xts* format.
`x_ts`	A single-column *xts* time series.
`look_back`	The size of the look-back interval, equal to the number of rows of data used for calculating the average price.

Details

The function `roll_vwap()` calculates the volume-weighted average closing price, defined as the sum of the prices multiplied by trading volumes in the look-back interval, divided by the sum of trading volumes in the interval. If the argument `x_ts` is passed in explicitly, then its volume-weighted average value over time is calculated.

Value

An *xts* time series with a single column and the same number of rows as the argument `oh_lc`.

Examples

```
# Calculate and plot rolling volume-weighted average closing prices (VWAP)
prices_rolling <- roll_vwap(oh_lc=HighFreq::SPY["2013-11"], look_back=11)
chart_Series(HighFreq::SPY["2013-11-12"], name="SPY prices")
add_TA(prices_rolling["2013-11-12"], on=1, col="red", lwd=2)
legend("top", legend=c("SPY prices", "VWAP prices"),
bg="white", lty=c(1, 1), lwd=c(2, 2),
col=c("black", "red"), bty="n")
# Calculate running returns
returns_running <- run_returns(x_ts=HighFreq::SPY)
# Calculate the rolling volume-weighted average returns
roll_vwap(oh_lc=HighFreq::SPY, x_ts=returns_running, look_back=11)
```

roll_wsum *Calculate the rolling weighted sums over a* time series *or a* matrix *using* Rcpp.

Description

Calculate the rolling weighted sums over a *time series* or a *matrix* using *Rcpp*.

Usage

```
roll_wsum(tseries, endp = NULL, look_back = 1L, stub = NULL, weights = NULL)
```

Arguments

tseries	A *time series* or a *matrix*.
endp	An *integer* vector of end points (the default is endp = NULL).
look_back	The length of the look-back interval, equal to the number of data points included in calculating the rolling sum (the default is look_back = 1).
stub	An *integer* value equal to the first end point for calculating the end points (the default is stub = NULL).
weights	A *column vector* of weights (the default is weights = NULL).

Details

The function roll_wsum() calculates the rolling weighted sums over the columns of the data tseries.

The function roll_wsum() calculates the rolling weighted sums as convolutions of the columns of tseries with the *column vector* of weights using the RcppArmadillo function arma::conv2(). It performs a similar calculation to the standard R function stats::filter(x=re_turns,filter=weight_s,method="con but it can be many times faster, and it doesn't produce any leading NA values.

The function roll_wsum() returns a *matrix* with the same dimensions as the input argument tseries.

The arguments weights, endp, and stub are optional.

If the argument weights is not supplied, then simple sums are calculated, not weighted sums.

If either the stub or endp arguments are supplied, then the rolling sums are calculated at the end points.

If only the argument stub is supplied, then the end points are calculated from the stub and look_back arguments. The first end point is equal to stub and the end points are spaced look_back periods apart.

If the arguments weights, endp, and stub are not supplied, then the sums are calculated over a number of data points equal to look_back.

The function roll_wsum() is also several times faster than rutils::roll_sum() which uses vectorized R code.

Technical note: The function roll_wsum() has arguments with default values equal to NULL, which are implemented in Rcpp code.

Value

A *matrix* with the same dimensions as the input argument tseries.

Examples

```
## Not run:
# First example
# Calculate historical returns
re_turns <- na.omit(rutils::etf_env$re_turns[, c("VTI", "IEF")])
# Define parameters
look_back <- 22
# Calculate rolling sums and compare with rutils::roll_sum()
c_sum <- HighFreq::roll_sum(re_turns, look_back)
r_sum <- rutils::roll_sum(re_turns, look_back)
all.equal(c_sum, coredata(r_sum), check.attributes=FALSE)
# Calculate rolling sums using R code
r_sum <- apply(zoo::coredata(re_turns), 2, cumsum)
lag_sum <- rbind(matrix(numeric(2*look_back), nc=2), r_sum[1:(NROW(r_sum) - look_back), ])
r_sum <- (r_sum - lag_sum)
all.equal(c_sum, r_sum, check.attributes=FALSE)

# Calculate rolling sums at end points
stu_b <- 21
c_sum <- HighFreq::roll_wsum(re_turns, look_back, stub=stu_b)
end_p <- (stu_b + look_back*(0:(NROW(re_turns) %/% look_back)))
end_p <- end_p[end_p < NROW(re_turns)]
r_sum <- apply(zoo::coredata(re_turns), 2, cumsum)
r_sum <- r_sum[end_p+1, ]
lag_sum <- rbind(numeric(2), r_sum[1:(NROW(r_sum) - 1), ])
r_sum <- (r_sum - lag_sum)
all.equal(c_sum, r_sum, check.attributes=FALSE)

# Calculate rolling sums at end points - pass in end_p
c_sum <- HighFreq::roll_wsum(re_turns, endp=end_p)
all.equal(c_sum, r_sum, check.attributes=FALSE)

# Create exponentially decaying weights
weight_s <- exp(-0.2*(1:11))
weight_s <- matrix(weight_s/sum(weight_s), nc=1)
# Calculate rolling weighted sum
c_sum <- HighFreq::roll_wsum(re_turns, weights=weight_s)
# Calculate rolling weighted sum using filter()
filter_ed <- filter(x=re_turns, filter=weight_s, method="convolution", sides=1)
all.equal(c_sum[-(1:11), ], filter_ed[-(1:11), ], check.attributes=FALSE)

# Calculate rolling weighted sums at end points
c_sum <- HighFreq::roll_wsum(re_turns, endp=end_p, weights=weight_s)
all.equal(c_sum, filter_ed[end_p+1, ], check.attributes=FALSE)

# Create simple weights equal to a 1 value plus zeros
weight_s <- matrix(c(1, rep(0, 10)), nc=1)
# Calculate rolling weighted sum
weight_ed <- HighFreq::roll_wsum(re_turns, weights=weight_s)
# Compare with original
all.equal(coredata(re_turns), weight_ed, check.attributes=FALSE)

## End(Not run)
```

roll_zscores *Calculate a* vector *of z-scores of the residuals of rolling regressions at the end points of the design matrix.*

Description

Calculate a *vector* of z-scores of the residuals of rolling regressions at the end points of the design matrix.

Usage

```
roll_zscores(
  response,
  design,
  startp = 0L,
  endp = 0L,
  step = 1L,
  look_back = 1L,
  stub = 0L
)
```

Arguments

response	A single-column *time series* or a *vector* of response data.
design	A *time series* or a *matrix* of design data (predictor or explanatory data).
startp	An *integer* vector of start points (the default is startp = 0).
endp	An *integer* vector of end points (the default is endp = 0).
step	The number of time periods between the end points (the default is step = 1).
look_back	The number of end points in the look-back interval (the default is look_back = 1).
stub	An *integer* value equal to the first end point for calculating the end points (the default is stub = 0).

Details

The function roll_zscores() calculates a *vector* of z-scores of the residuals of rolling regressions at the end points of the *time series* design.

The function roll_zscores() performs a loop over the end points, and at each end point it subsets the time series design over a look-back interval equal to look_back number of end points.

It passes the subset time series to the function calc_lm(), which calculates the regression data.

If the arguments endp and startp are not given then it first calculates a vector of end points separated by step time periods. It calculates the end points along the rows of design using the function calc_endpoints(), with the number of time periods between the end points equal to step time periods.

For example, the rolling variance at 25 day end points, with a 75 day look-back, can be calculated using the parameters step = 25 and look_back = 3.

Value

A column *vector* of the same length as the number of rows of design.

Examples

```
## Not run:
# Calculate historical returns
re_turns <- na.omit(rutils::etf_env$re_turns[, c("XLF", "VTI", "IEF")])
# Response equals XLF returns
res_ponse <- re_turns[, 1]
# Design matrix equals VTI and IEF returns
de_sign <- re_turns[, -1]
# Calculate Z-scores from rolling time series regression using RcppArmadillo
look_back <- 11
z_scores <- HighFreq::roll_zscores(response=res_ponse, design=de_sign, look_back)
# Calculate z-scores in R from rolling multivariate regression using lm()
z_scoresr <- sapply(1:NROW(de_sign), function(ro_w) {
  if (ro_w == 1) return(0)
  start_point <- max(1, ro_w-look_back+1)
  sub_response <- res_ponse[start_point:ro_w]
  sub_design <- de_sign[start_point:ro_w, ]
  reg_model <- lm(sub_response ~ sub_design)
  resid_uals <- reg_model$residuals
  resid_uals[NROW(resid_uals)]/sd(resid_uals)
})  # end sapply
# Compare the outputs of both functions
all.equal(z_scores[-(1:look_back)], z_scoresr[-(1:look_back)],
  check.attributes=FALSE)

## End(Not run)
```

---

run_covar — *Calculate the rolling covariance of two streaming* time series *of returns.*

Description

Calculate the rolling covariance of two streaming *time series* of returns.

Usage

```
run_covar(tseries, lambda)
```

Arguments

tseries	A *time series* or a *matrix* with two columns of returns data.
lambda	A *numeric* decay factor.

Details

The function `run_covar()` calculates the rolling covariance of two streaming *time series* of returns by recursively weighing the products of their present returns with past covariance estimates, using the decay factor λ:

$$\sigma_t^{12} = (1 - \lambda) r_t^1 r_t^2 + \lambda \sigma_{t-1}^{12}$$

Where σ_t^{12} is the covariance estimate at time t, and r_t^1 and r_t^2 are the streaming returns data.

The value of the decay factor λ should be in the range between `0` and `1`. If λ is close to `1` then the decay is weak and past values have a greater weight, and the rolling covariance values have a stronger dependence on past values. This is equivalent to a long look-back interval. If λ is much less than `1` then the decay is strong and past values have a smaller weight, and the rolling covariance values have a weaker dependence on past values. This is equivalent to a short look-back interval.

The above formula slightly overestimates the covariance because it doesn't subtract the mean returns.

The above recursive formula is convenient for processing live streaming data because it doesn't require maintaining a buffer of past data. The formula is equivalent to a convolution with exponentially decaying weights, but it's faster.

The function `run_covar()` returns three columns of data: the covariance and the variances of the two columns of the argument `tseries`. This allows calculating the rolling correlation.

The function `run_covar()` performs the same calculation as the standard `R` function `stats::filter(x=series,filter=weight_s,method="convolution",sides=1)`, but it's several times faster.

Value

A *matrix* with three columns of data: the covariance and the variances of the two columns of the argument `tseries`.

Examples

```
## Not run:
# Calculate historical returns
re_turns <- zoo::coredata(na.omit(rutils::etf_env$re_turns[, c("IEF", "VTI")]))
# Calculate the rolling covariance
lamb_da <- 0.9
covars <- HighFreq::run_covar(re_turns, lambda=lamb_da)
# Calculate rolling covariance using R code
filter_ed <- (1-lamb_da)*filter(re_turns[, 1]*re_turns[, 2], filter=lamb_da, init=as.numeric(re_turns[1, 1]*r
all.equal(covars[, 1], unclass(filter_ed), check.attributes=FALSE)
# Calculate the rolling correlation
correl <- covars[, 1]/sqrt(covars[, 2]*covars[, 3])

## End(Not run)
```

`run_max` *Calculate the rolling maximum of streaming* time series *data.*

Description

Calculate the rolling maximum of streaming *time series* data.

Usage

```
run_max(tseries, lambda)
```

Arguments

`tseries`	A *time series* or a *matrix*.
`lambda`	A *numeric* decay factor.

Details

The function `run_max()` calculates the rolling maximum of streaming *time series* data by recursively weighing present and past values using the decay factor λ.

It first calculates the rolling mean of streaming data:

$$\mu_t = (1 - \lambda)p_t + \lambda\mu_{t-1}$$

Where μ_t is the mean value at time t, and p_t is the streaming data.

It then calculates the rolling maximums of streaming data, p_t^{max}:

$$p_t^{max} = max(p_t, p_{t-1}^{max}) + (1 - \lambda)(\mu_{t-1} - p_{t-1}^{max})$$

The second term pulls the maximum value down to the mean value, allowing it to gradually "forget" the maximum value from the more distant past.

The value of the decay factor λ should be in the range between `0` and `1`. If λ is close to `1` then the decay is weak and past values have a greater weight, and the rolling maximum values have a stronger dependence on past values. This is equivalent to a long look-back interval. If λ is much less than `1` then the decay is strong and past values have a smaller weight, and the rolling maximum values have a weaker dependence on past values. This is equivalent to a short look-back interval.

The above recursive formula is convenient for processing live streaming data because it doesn't require maintaining a buffer of past data.

The function `run_max()` returns a *matrix* with the same dimensions as the input argument `tseries`.

Value

A *matrix* with the same dimensions as the input argument `tseries`.

Examples

```
## Not run:
# Calculate historical prices
price_s <- zoo::coredata(quantmod::Cl(rutils::etf_env$VTI))
# Calculate the rolling maximums
lamb_da <- 0.9
maxs <- HighFreq::run_max(price_s, lambda=lamb_da)
# Plot dygraph of VTI prices and rolling maximums
da_ta <- cbind(quantmod::Cl(rutils::etf_env$VTI), maxs)
colnames(da_ta) <- c("prices", "max")
col_names <- colnames(da_ta)
dygraphs::dygraph(da_ta, main="VTI Prices and Rolling Maximums") %>%
  dySeries(name=col_names[1], label=col_names[1], strokeWidth=2, col="blue") %>%
  dySeries(name=col_names[2], label=col_names[2], strokeWidth=2, col="red")

## End(Not run)
```

run_mean *Calculate the rolling mean of streaming* time series *data.*

Description

Calculate the rolling mean of streaming *time series* data.

Usage

```
run_mean(tseries, lambda)
```

Arguments

tseries	A *time series* or a *matrix*.
lambda	A *numeric* decay factor.

Details

The function run_mean() calculates the rolling mean of streaming *time series* data by recursively weighing present and past values using the decay factor λ:

$$\mu_t = (1 - \lambda)p_t + \lambda\mu_{t-1}$$

Where μ_t is the mean value at time t, and p_t is the streaming data.

The value of the decay factor λ should be in the range between 0 and 1. If λ is close to 1 then the decay is weak and past values have a greater weight, and the rolling mean values have a stronger dependence on past values. This is equivalent to a long look-back interval. If λ is much less than 1 then the decay is strong and past values have a smaller weight, and the rolling mean values have a weaker dependence on past values. This is equivalent to a short look-back interval.

The above recursive formula is convenient for processing live streaming data because it doesn't require maintaining a buffer of past data. The formula is equivalent to a convolution with exponentially decaying weights, but it's faster.

The function run_mean() performs the same calculation as the standard R function stats::filter(x=series,filter=weight_s,method="convolution",sides=1), but it's several times faster.

The function run_mean() returns a *matrix* with the same dimensions as the input argument tseries.

Value

A *matrix* with the same dimensions as the input argument tseries.

Examples

```
## Not run:
# Calculate historical prices
price_s <- zoo::coredata(quantmod::Cl(rutils::etf_env$VTI))
# Calculate the rolling means
lamb_da <- 0.9
means <- HighFreq::run_mean(price_s, lambda=lamb_da)
# Calculate rolling means using R code
filter_ed <- (1-lamb_da)*filter(price_s, filter=lamb_da, init=as.numeric(price_s[1, 1])/(1-lamb_da), method="
```

```
all.equal(means, unclass(filter_ed), check.attributes=FALSE)
# Compare the speed of RcppArmadillo with R code
library(microbenchmark)
summary(microbenchmark(
  Rcpp=HighFreq::run_mean(price_s, lambda=lamb_da),
 Rcode=filter(price_s, filter=lamb_da, init=as.numeric(price_s[1, 1])/(1-lamb_da), method="recursive"),
  times=10))[, c(1, 4, 5)]  # end microbenchmark summary

## End(Not run)
```

`run_min` *Calculate the rolling minimum of streaming* time series *data.*

Description

Calculate the rolling minimum of streaming *time series* data.

Usage

```
run_min(tseries, lambda)
```

Arguments

`tseries`	A *time series* or a *matrix*.
`lambda`	A *numeric* decay factor.

Details

The function `run_min()` calculates the rolling minimum of streaming *time series* data by recursively weighing present and past values using the decay factor λ.

It first calculates the rolling mean of streaming data:

$$\mu_t = (1 - \lambda)p_t + \lambda\mu_{t-1}$$

Where μ_t is the mean value at time t, and p_t is the streaming data.

It then calculates the rolling minimums of streaming data, p_t^{min}:

$$p_t^{min} = min(p_t, p_{t-1}^{min}) + (1 - \lambda)(\mu_{t-1} - p_{t-1}^{min})$$

The second term pulls the minimum value up to the mean value, allowing it to gradually "forget" the minimum value from the more distant past.

The value of the decay factor λ should be in the range between `0` and `1`. If λ is close to `1` then the decay is weak and past values have a greater weight, and the rolling minimum values have a stronger dependence on past values. This is equivalent to a long look-back interval. If λ is much less than `1` then the decay is strong and past values have a smaller weight, and the rolling minimum values have a weaker dependence on past values. This is equivalent to a short look-back interval.

The above recursive formula is convenient for processing live streaming data because it doesn't require maintaining a buffer of past data.

The function `run_min()` returns a *matrix* with the same dimensions as the input argument `tseries`.

Value

A *matrix* with the same dimensions as the input argument `tseries`.

Examples

```
## Not run:
# Calculate historical prices
price_s <- zoo::coredata(quantmod::Cl(rutils::etf_env$VTI))
# Calculate the rolling minimums
lamb_da <- 0.9
mins <- HighFreq::run_min(price_s, lambda=lamb_da)
# Plot dygraph of VTI prices and rolling minimums
da_ta <- cbind(quantmod::Cl(rutils::etf_env$VTI), mins)
colnames(da_ta) <- c("prices", "min")
col_names <- colnames(da_ta)
dygraphs::dygraph(da_ta, main="VTI Prices and Rolling Minimums") %>%
  dySeries(name=col_names[1], label=col_names[1], strokeWidth=2, col="blue") %>%
  dySeries(name=col_names[2], label=col_names[2], strokeWidth=2, col="red")

## End(Not run)
```

`run_returns` *Calculate single period percentage returns from either* TAQ *or* OHLC *prices.*

Description

Calculate single period percentage returns from either *TAQ* or *OHLC* prices.

Usage

```
run_returns(x_ts, lagg = 1, col_umn = 4, scal_e = TRUE)
```

Arguments

`x_ts`	An *xts* time series of either *TAQ* or *OHLC* data.
`lagg`	An integer equal to the number of time periods of lag. (default is 1)
`col_umn`	The column number to extract from the *OHLC* data. (default is 4, or the *Close* prices column)
`scal_e`	*Boolean* argument: should the returns be divided by the number of seconds in each period? (default is `TRUE`)

Details

The function `run_returns()` calculates the percentage returns for either *TAQ* or *OHLC* data, defined as the difference of log prices. Multi-period returns can be calculated by setting the `lag` parameter to values greater than 1 (the default).

If `scal_e` is `TRUE` (the default), then the returns are divided by the differences of the time index (which scales the returns to units of returns per second.)

The time index of the x_ts time series is assumed to be in *POSIXct* format, so that its internal value is equal to the number of seconds that have elapsed since the *epoch*.

If scal_e is TRUE (the default), then the returns are expressed in the scale of the time index of the x_ts time series. For example, if the time index is in seconds, then the returns are given in units of returns per second. If the time index is in days, then the returns are equal to the returns per day.

The function run_returns() identifies the x_ts time series as *TAQ* data when it has six columns, otherwise assumes it's *OHLC* data. By default, for *OHLC* data, it differences the *Close* prices, but can also difference other prices depending on the value of col_umn.

Value

A single-column *xts* time series of returns.

Examples

```
# Calculate secondly returns from TAQ data
re_turns <- HighFreq::run_returns(x_ts=HighFreq::SPY_TAQ)
# Calculate close to close returns
re_turns <- HighFreq::run_returns(x_ts=HighFreq::SPY)
# Calculate open to open returns
re_turns <- HighFreq::run_returns(x_ts=HighFreq::SPY, col_umn=1)
```

---

run_sharpe *Calculate time series of point Sharpe-like statistics for each row of a* OHLC *time series.*

Description

Calculate time series of point Sharpe-like statistics for each row of a *OHLC* time series.

Usage

```
run_sharpe(oh_lc, calc_method = "close")
```

Arguments

oh_lc	An *OHLC* time series of prices in *xts* format.
calc_method	A *character* string representing method for estimating the Sharpe-like exponent.

Details

The function run_sharpe() calculates Sharpe-like statistics for each row of a *OHLC* time series. The Sharpe-like statistic is defined as the ratio of the difference between *Close* minus *Open* prices divided by the difference between *High* minus *Low* prices. This statistic may also be interpreted as something like a *Hurst exponent* for a single row of data. The motivation for the Sharpe-like statistic is the notion that if prices are trending in the same direction inside a given time bar of data, then this statistic is close to either 1 or -1.

Value

An *xts* time series with the same number of rows as the argument oh_lc.

Examples

```
# Calculate time series of running Sharpe ratios for SPY
sharpe_running <- run_sharpe(HighFreq::SPY)
```

`run_skew` *Calculate time series of point skew estimates from a* OHLC *time series, assuming zero drift.*

Description

Calculate time series of point skew estimates from a *OHLC* time series, assuming zero drift.

Usage

```
run_skew(oh_lc, calc_method = "rogers_satchell")
```

Arguments

`oh_lc`	An *OHLC* time series of prices in *xts* format.
`calc_method`	A *character* string representing method for estimating skew.

Details

The function `run_skew()` calculates a time series of skew estimates from *OHLC* prices, one for each row of *OHLC* data. The skew estimates are expressed in the time scale of the index of the *OHLC* time series. For example, if the time index is in seconds, then the skew is given in units of skew per second. If the time index is in days, then the skew is equal to the skew per day.

Currently only the `"close"` skew estimation method is correct (assuming zero drift), while the `"rogers_satchell"` method produces a skew-like indicator, proportional to the skew. The default method is `"rogers_satchell"`.

Value

A time series of point skew estimates.

Examples

```
# Calculate time series of skew estimates for SPY
sk_ew <- HighFreq::run_skew(HighFreq::SPY)
```

run_var *Calculate the rolling variance of streaming* time series *of returns.*

Description

Calculate the rolling variance of streaming *time series* of returns.

Usage

```
run_var(tseries, lambda)
```

Arguments

tseries	A *time series* or a *matrix* of returns.
lambda	A *numeric* decay factor.

Details

The function run_var() calculates the rolling variance of a streaming *time series* of returns by recursively weighing the squared present returns with past variance estimates, using the decay factor λ:

$$\sigma_t^2 = (1 - \lambda) r_t^2 + \lambda \sigma_{t-1}^2$$

Where σ_t^2 is the variance estimate at time t, and r_t are the streaming returns data.

The value of the decay factor λ should be in the range between 0 and 1. If λ is close to 1 then the decay is weak and past values have a greater weight, and the rolling variance values have a stronger dependence on past values. This is equivalent to a long look-back interval. If λ is much less than 1 then the decay is strong and past values have a smaller weight, and the rolling variance values have a weaker dependence on past values. This is equivalent to a short look-back interval.

The above formula slightly overestimates the variance because it doesn't subtract the mean returns.

The above recursive formula is convenient for processing live streaming data because it doesn't require maintaining a buffer of past data. The formula is equivalent to a convolution with exponentially decaying weights, but it's faster.

The function run_var() performs the same calculation as the standard R function stats::filter(x=series,filter=weight_s,method="convolution",sides=1), but it's several times faster.

The function run_var() returns a *matrix* with the same dimensions as the input argument tseries.

Value

A *matrix* with the same dimensions as the input argument tseries.

Examples

```
## Not run:
# Calculate historical returns
re_turns <- zoo::coredata(na.omit(rutils::etf_env$re_turns$VTI))
# Calculate the rolling variance
lamb_da <- 0.9
vars <- HighFreq::run_var(re_turns, lambda=lamb_da)
# Calculate rolling variance using R code
```

```
filter_ed <- (1-lamb_da)*filter(re_turns^2, filter=lamb_da, init=as.numeric(re_turns[1, 1])^2/(1-lamb_da), me
all.equal(vars, unclass(filter_ed), check.attributes=FALSE)
# Compare the speed of RcppArmadillo with R code
library(microbenchmark)
summary(microbenchmark(
  Rcpp=HighFreq::run_var(re_turns, lambda=lamb_da),
 Rcode=filter(re_turns^2, filter=lamb_da, init=as.numeric(re_turns[1, 1])^2/(1-lamb_da), method="recursive")
  times=10))[, c(1, 4, 5)]  # end microbenchmark summary

## End(Not run)
```

`run_variance` *Calculate a time series of point estimates of variance for an* OHLC *time series, using different range estimators for variance.*

Description

Calculates the point variance estimates from individual rows of *OHLC* prices (rows of data), using the squared differences of *OHLC* prices at each point in time, without averaging them over time.

Usage

```
run_variance(oh_lc, calc_method = "yang_zhang", scal_e = TRUE)
```

Arguments

`oh_lc`	An *OHLC* time series of prices in *xts* format.
`calc_method`	A *character* string representing the method for estimating variance. The methods include: • "close" close to close, • "garman_klass" Garman-Klass, • "garman_klass_yz" Garman-Klass with account for close-to-open price jumps, • "rogers_satchell" Rogers-Satchell, • "yang_zhang" Yang-Zhang, (default is `"yang_zhang"`)
`scal_e`	*Boolean* argument: should the returns be divided by the number of seconds in each period? (default is `TRUE`)

Details

The function `run_variance()` calculates a time series of point variance estimates of percentage returns, from *OHLC* prices, without averaging them over time. For example, the method `"close"` simply calculates the squares of the differences of the log *Close* prices.

The other methods calculate the squares of other possible differences of the log *OHLC* prices. This way the point variance estimates only depend on the price differences within individual rows of data (and possibly from the neighboring rows.) All the methods are implemented assuming zero drift, since the calculations are performed only for a single row of data, at a single point in time.

The user can choose from several different variance estimation methods. The methods "close", "garman_klass_yz", and "yang_zhang" do account for close-to-open price jumps, while the methods "garman_klass" and "rogers_satchell" do not account for close-to-open price jumps. The default method is "yang_zhang", which theoretically has the lowest standard error among unbiased estimators.

The point variance estimates can be passed into function roll_vwap() to perform averaging, to calculate rolling variance estimates. This is appropriate only for the methods "garman_klass" and "rogers_satchell", since they don't require subtracting the rolling mean from the point variance estimates.

The point variance estimates can also be considered to be technical indicators, and can be used as inputs into trading models.

If scal_e is TRUE (the default), then the variance is divided by the squared differences of the time index (which scales the variance to units of variance per second squared.) This is useful for example, when calculating intra-day variance from minutely bar data, because dividing returns by the number of seconds decreases the effect of overnight price jumps.

If scal_e is TRUE (the default), then the variance is expressed in the scale of the time index of the *OHLC* time series. For example, if the time index is in seconds, then the variance is given in units of variance per second squared. If the time index is in days, then the variance is equal to the variance per day squared.

The time index of the oh_lc time series is assumed to be in *POSIXct* format, so that its internal value is equal to the number of seconds that have elapsed since the *epoch*.

The function run_variance() performs similar calculations to the function volatility() from package TTR, but it assumes zero drift, and doesn't calculate a running sum using runSum(). It's also a little faster because it performs less data validation.

Value

An *xts* time series with a single column and the same number of rows as the argument oh_lc.

Examples

```
# Create minutely OHLC time series of random prices
oh_lc <- HighFreq::random_ohlc()
# Calculate variance estimates for oh_lc
var_running <- HighFreq::run_variance(oh_lc)
# Calculate variance estimates for SPY
var_running <- HighFreq::run_variance(HighFreq::SPY, calc_method="yang_zhang")
# Calculate SPY variance without overnight jumps
var_running <- HighFreq::run_variance(HighFreq::SPY, calc_method="rogers_satchell")
```

---

run_zscores *Calculate the z-scores of rolling regressions of streaming* time series *of returns.*

Description

Calculate the z-scores of rolling regressions of streaming *time series* of returns.

Usage

```
run_zscores(response, design, lambda)
```

Arguments

response	A single-column *time series* or a *vector* of response data.
design	A *time series* or a *matrix* of design data (predictor or explanatory data).
lambda	A *numeric* decay factor.

Details

The function run_zscores() calculates the vectors of *betas* β_t and the residuals ϵ_t of rolling regressions by recursively weighing the current estimates with past estimates, using the decay factor λ:

$$\beta_t = (1 - \lambda)\frac{\sigma_t^{cov}}{\sigma_t^2} + \lambda\beta_{t-1}$$

$$\epsilon_t = (1 - \lambda)(r_t^r - \beta_t r_t^d) + \lambda\epsilon_{t-1}$$

Where σ_t^{cov} is the vector of covariances at time t, between the response and design returns; σ_t^2 is the vector of design variances, and r_t^r and r_t^2 are the streaming returns of the response and design data.

The matrices σ^2, σ^{cov}, β have the same dimensions as the input argument design.

The above formula is approximate because it doesn't subtract the mean returns.

The z-score z_t is equal to the residual ϵ_t divided by volatility σ_t^ϵ:

$$z_t = \frac{\epsilon_t}{\sigma_t^\epsilon}$$

The value of the decay factor λ should be in the range between 0 and 1. If λ is close to 1 then the decay is weak and past values have a greater weight, and the rolling z-score values have a stronger dependence on past values. This is equivalent to a long look-back interval. If λ is much less than 1 then the decay is strong and past values have a smaller weight, and the rolling z-score values have a weaker dependence on past values. This is equivalent to a short look-back interval.

The above recursive formula is convenient for processing live streaming data because it doesn't require maintaining a buffer of past data. The formula is equivalent to a convolution with exponentially decaying weights, but it's faster.

The function run_zscores() returns four columns of data: the z-score and the variances of the two columns of the argument tseries. This allows calculating the rolling correlation.

The function run_zscores() performs the same calculation as the standard R function stats::filter(x=series,filter=weight_s,method="convolution",sides=1), but it's several times faster.

Value

A single-column *matrix* with the z-scores.

Examples

```
## Not run:
# Calculate historical returns
re_turns <- na.omit(rutils::etf_env$re_turns[, c("XLF", "VTI", "IEF")])
# Response equals XLF returns
res_ponse <- re_turns[, 1]
# Design matrix equals VTI and IEF returns
de_sign <- re_turns[, -1]
```

```
run_zscores(re_turns[, 1, drop=FALSE], re_turns[, 2, drop=FALSE], lambda=lamb_da)
# Calculate the running z-scores
lamb_da <- 0.9
zscores <- HighFreq::run_zscores(response=res_ponse, design=de_sign, lambda=lamb_da)
# Plot the running z-scores
da_ta <- cbind(cumsum(res_ponse), zscores)
colnames(da_ta) <- c("XLF", "zscores")
col_names <- colnames(da_ta)
dygraphs::dygraph(da_ta, main="Z-Scores of XLF Versus VTI and IEF") %>%
  dyAxis("y", label=col_names[1], independentTicks=TRUE) %>%
  dyAxis("y2", label=col_names[2], independentTicks=TRUE) %>%
 dySeries(name=col_names[1], axis="y", label=col_names[1], strokeWidth=1, col="blue") %>%
  dySeries(name=col_names[2], axis="y2", label=col_names[2], strokeWidth=1, col="red")

## End(Not run)
```

`save_rets` *Load, scrub, aggregate, and rbind multiple days of* TAQ *data for a single symbol. Calculate returns and save them to a single '*`*.RData`*' file.*

Description

Load, scrub, aggregate, and rbind multiple days of *TAQ* data for a single symbol. Calculate returns and save them to a single '`*.RData`' file.

Usage

```
save_rets(
  sym_bol,
  data_dir = "E:/mktdata/sec/",
  output_dir = "E:/output/data/",
  look_back = 51,
  vol_mult = 2,
  period = "minutes",
  tzone = "America/New_York"
)
```

Details

The function `save_rets` loads multiple days of *TAQ* data, then scrubs, aggregates, and rbinds them into a *OHLC* time series. It then calculates returns using function `run_returns()`, and stores them in a variable named '`symbol.rets`', and saves them to a file called '`symbol.rets.RData`'. The *TAQ* data files are assumed to be stored in separate directories for each '`symbol`'. Each '`symbol`' has its own directory (named '`symbol`') in the '`data_dir`' directory. Each '`symbol`' directory contains multiple daily '`*.RData`' files, each file containing one day of *TAQ* data.

Value

A time series of returns and volume in *xts* format.

Examples

```
## Not run:
save_rets("SPY")

## End(Not run)
```

`save_rets_ohlc` *Load* OHLC *time series data for a single symbol, calculate its returns, and save them to a single '*`*.RData`*' file, without aggregation.*

Description

Load *OHLC* time series data for a single symbol, calculate its returns, and save them to a single '`*.RData`' file, without aggregation.

Usage

```
save_rets_ohlc(
  sym_bol,
  data_dir = "E:/output/data/",
  output_dir = "E:/output/data/"
)
```

Details

The function `save_rets_ohlc()` loads *OHLC* time series data from a single file. It then calculates returns using function `run_returns()`, and stores them in a variable named '`symbol.rets`', and saves them to a file called '`symbol.rets.RData`'.

Value

A time series of returns and volume in *xts* format.

Examples

```
## Not run:
save_rets_ohlc("SPY")

## End(Not run)
```

`save_scrub_agg` *Load, scrub, aggregate, and rbind multiple days of* TAQ *data for a single symbol, and save the* OHLC *time series to a single '*`*.RData`*' file.*

Description

Load, scrub, aggregate, and rbind multiple days of *TAQ* data for a single symbol, and save the *OHLC* time series to a single '`*.RData`' file.

Usage

```
save_scrub_agg(
  sym_bol,
  data_dir = "E:/mktdata/sec/",
  output_dir = "E:/output/data/",
  look_back = 51,
  vol_mult = 2,
  period = "minutes",
  tzone = "America/New_York"
)
```

Arguments

sym_bol	A *character* string representing symbol or ticker.
data_dir	A *character* string representing directory containing input '*.RData' files.
output_dir	A *character* string representing directory containing output '*.RData' files.

Details

The function save_scrub_agg() loads multiple days of *TAQ* data, then scrubs, aggregates, and rbinds them into a *OHLC* time series, and finally saves it to a single '*.RData' file. The *OHLC* time series is stored in a variable named 'symbol', and then it's saved to a file named 'symbol.RData' in the 'output_dir' directory. The *TAQ* data files are assumed to be stored in separate directories for each 'symbol'. Each 'symbol' has its own directory (named 'symbol') in the 'data_dir' directory. Each 'symbol' directory contains multiple daily '*.RData' files, each file containing one day of *TAQ* data.

Value

An *OHLC* time series in *xts* format.

Examples

```
## Not run:
# set data directories
data_dir <- "C:/Develop/data/hfreq/src/"
output_dir <- "C:/Develop/data/hfreq/scrub/"
sym_bol <- "SPY"
# Aggregate SPY TAQ data to 15-min OHLC bar data, and save the data to a file
save_scrub_agg(sym_bol=sym_bol, data_dir=data_dir, output_dir=output_dir, period="15 min")

## End(Not run)
```

---

scrub_agg *Scrub a single day of* TAQ *data, aggregate it, and convert to* OHLC *format.*

Description

Scrub a single day of *TAQ* data, aggregate it, and convert to *OHLC* format.

Usage

```
scrub_agg(
  ta_q,
  look_back = 51,
  vol_mult = 2,
  period = "minutes",
  tzone = "America/New_York"
)
```

Arguments

period	The aggregation period.

Details

The function scrub_agg() performs:

- index timezone conversion,
- data subset to trading hours,
- removal of duplicate time stamps,
- scrubbing of quotes with suspect bid-offer spreads,
- scrubbing of quotes with suspect price jumps,
- cbinding of mid prices with volume data,
- aggregation to OHLC using function to.period() from package *xts*,

Valid 'period' character strings include: "minutes", "3 min", "5 min", "10 min", "15 min", "30 min", and "hours". The time index of the output time series is rounded up to the next integer multiple of 'period'.

Value

A *OHLC* time series in *xts* format.

Examples

```
# Create random TAQ prices
ta_q <- HighFreq::random_taq()
# Aggregate to ten minutes OHLC data
oh_lc <- HighFreq::scrub_agg(ta_q, period="10 min")
chart_Series(oh_lc, name="random prices")
# scrub and aggregate a single day of SPY TAQ data to OHLC
oh_lc <- HighFreq::scrub_agg(ta_q=HighFreq::SPY_TAQ)
chart_Series(oh_lc, name=sym_bol)
```

season_ality *Perform seasonality aggregations over a single-column* xts *time series.*

Description

Perform seasonality aggregations over a single-column *xts* time series.

Usage

```
season_ality(x_ts, in_dex = format(zoo::index(x_ts), "%H:%M"))
```

Arguments

x_ts	A single-column *xts* time series.
in_dex	A vector of *character* strings representing points in time, of the same length as the argument x_ts.

Details

The function season_ality() calculates the mean of values observed at the same points in time specified by the argument in_dex. An example of a daily seasonality aggregation is the average price of a stock between 9:30AM and 10:00AM every day, over many days. The argument in_dex is passed into function tapply(), and must be the same length as the argument x_ts.

Value

An *xts* time series with mean aggregations over the seasonality interval.

Examples

```
# Calculate running variance of each minutely OHLC bar of data
x_ts <- run_variance(HighFreq::SPY)
# Remove overnight variance spikes at "09:31"
in_dex <- format(index(x_ts), "%H:%M")
x_ts <- x_ts[!in_dex=="09:31", ]
# Calculate daily seasonality of variance
var_seasonal <- season_ality(x_ts=x_ts)
chart_Series(x=var_seasonal, name=paste(colnames(var_seasonal),
  "daily seasonality of variance"))
```

sim_arima *Recursively filter a* vector *of innovations through a* vector *of* ARIMA *coefficients.*

Description

Recursively filter a *vector* of innovations through a *vector* of *ARIMA* coefficients.

Usage

```
sim_arima(innov, coeff)
```

Arguments

innov	A *vector* of innovations (random numbers).
coeff	A *vector* of *ARIMA* coefficients.

Details

The function sim_arima() recursively filters a *vector* of innovations through a *vector* of *ARIMA* coefficients, using RcppArmadillo C++ code. It performs the same calculation as the standard R function filter(x=innov,filter=co_eff,method="recursive"), but it's over 6 times faster.

Value

A column *vector* of the same length as the argument innov.

Examples

```
## Not run:
# Calculate vector of prices
price_s <- drop(zoo::coredata(quantmod::Cl(rutils::etf_env$VTI)))
# Create ARIMA coefficients
co_eff <- c(-0.8, 0.2)
# Calculate recursive filter using filter()
filter_ed <- filter(price_s, filter=co_eff, method="recursive")
# Calculate recursive filter using RcppArmadillo
ari_ma <- HighFreq::sim_arima(price_s, rev(co_eff))
# Compare the two methods
all.equal(as.numeric(ari_ma), as.numeric(filter_ed))

## End(Not run)
```

---

sim_garch *Simulate a* GARCH *process using* Rcpp.

Description

Simulate a *GARCH* process using *Rcpp*.

Usage

```
sim_garch(omega, alpha, beta, innov)
```

Arguments

omega	Parameter proportional to the long-term average level of variance.
alpha	The weight associated with recent realized variance updates.
beta	The weight associated with the past variance estimates.
innov	A *vector* of innovations (random numbers).

Details

The function sim_garch() simulates a *GARCH* process using fast *Rcpp* C++ code.

Value

A *matrix* with two columns: the simulated returns and variance, and with the same number of rows as the length of the argument `innov`.

Examples

```
## Not run:
# Define the GARCH model parameters
ome_ga <- 0.01
al_pha <- 0.5
be_ta <- 0.2
# Simulate the GARCH process using Rcpp
garch_rcpp <- sim_garch(omega=ome_ga, alpha=al_pha, beta=be_ta, innov=rnorm(10000))

## End(Not run)
```

---

sim_ou *Simulate an* Ornstein-Uhlenbeck *process using* Rcpp.

Description

Simulate an *Ornstein-Uhlenbeck* process using *Rcpp*.

Usage

```
sim_ou(eq_price, volat, theta, innov)
```

Arguments

`eq_price`	The equilibrium price.
`volat`	The volatility of returns.
`theta`	The strength of mean reversion.
`innov`	A *vector* of innovations (random numbers).

Details

The function `sim_ou()` simulates an *Ornstein-Uhlenbeck* process using fast *Rcpp* `C++` code. It returns a column *vector* representing the *time series* of log prices. The function `sim_ou()` simulates the percentage returns as equal to the difference between the equilibrium price `eq_price` minus the latest price, times the mean reversion parameter `theta`, plus a random innovation. The log prices are calculated as the sum of returns (not compounded), so they can become negative.

Value

A column *vector* representing the *time series* of log prices, with the same length as the argument `innov`.

Examples

```
## Not run:
# Define the Ornstein-Uhlenbeck model parameters
eq_price <- 5.0
vol_at <- 0.01
the_ta <- 0.01
# Simulate Ornstein-Uhlenbeck process using Rcpp
price_s <- HighFreq::sim_ou(eq_price=eq_price, volat=vol_at, theta=the_ta, innov=rnorm(1000))

## End(Not run)
```

`sim_schwartz` *Simulate a* Schwartz *process using* Rcpp.

Description

Simulate a *Schwartz* process using *Rcpp*.

Usage

```
sim_schwartz(eq_price, volat, theta, innov)
```

Arguments

`eq_price`	The equilibrium price.
`volat`	The volatility of returns.
`theta`	The strength of mean reversion.
`innov`	A *vector* of innovations (random numbers).

Details

The function `sim_schwartz()` simulates a *Schwartz* process using fast *Rcpp* `C++` code. It returns a column *vector* representing the *time series* of prices. The function `sim_schwartz()` simulates the percentage returns as equal to the difference between the equilibrium price `eq_price` minus the latest price, times the mean reversion parameter `theta`, plus a random innovation. The prices are calculated as the exponentially compounded returns, so they are never negative. The log prices can be obtained by taking the logarithm of the prices.

Value

A column *vector* representing the *time series* of prices, with the same length as the argument `innov`.

Examples

```
## Not run:
# Define the Schwartz model parameters
eq_price <- 5.0
vol_at <- 0.01
the_ta <- 0.01
# Simulate Schwartz process using Rcpp
price_s <- HighFreq::sim_schwartz(eq_price=eq_price, volat=vol_at, theta=the_ta, innov=rnorm(1000))
```

```
## End(Not run)
```

`which_extreme` *Calculate a* Boolean *vector that identifies extreme tail values in a single-column* xts *time series or vector, over a rolling look-back interval.*

Description

Calculate a *Boolean* vector that identifies extreme tail values in a single-column *xts* time series or vector, over a rolling look-back interval.

Usage

```
which_extreme(x_ts, look_back = 51, vol_mult = 2)
```

Arguments

`x_ts`	A single-column *xts* time series, or a *numeric* or *Boolean* vector.
`look_back`	The number of data points in rolling look-back interval for estimating rolling quantile.
`vol_mult`	The quantile multiplier.

Details

The function `which_extreme()` calculates a *Boolean* vector, with `TRUE` for values that belong to the extreme tails of the distribution of values.

The function `which_extreme()` applies a version of the Hampel median filter to identify extreme values, but instead of using the median absolute deviation (MAD), it uses the `0.9` quantile values calculated over a rolling look-back interval.

Extreme values are defined as those that exceed the product of the multiplier times the rolling quantile. Extreme values belong to the fat tails of the recent (trailing) distribution of values, so they are present only when the trailing distribution of values has fat tails. If the trailing distribution of values is closer to normal (without fat tails), then there are no extreme values.

The quantile multiplier `vol_mult` controls the threshold at which values are identified as extreme. Smaller quantile multiplier values will cause more values to be identified as extreme.

Value

A *Boolean* vector with the same number of rows as the input time series or vector.

Examples

```
# Create local copy of SPY TAQ data
ta_q <- HighFreq::SPY_TAQ
# scrub quotes with suspect bid-offer spreads
bid_offer <- ta_q[, "Ask.Price"] - ta_q[, "Bid.Price"]
sus_pect <- which_extreme(bid_offer, look_back=51, vol_mult=3)
# Remove suspect values
ta_q <- ta_q[!sus_pect]
```

`which_jumps` *Calculate a* Boolean *vector that identifies isolated jumps (spikes) in a single-column* xts *time series or vector, over a rolling interval.*

Description

Calculate a *Boolean* vector that identifies isolated jumps (spikes) in a single-column *xts* time series or vector, over a rolling interval.

Usage

```
which_jumps(x_ts, look_back = 51, vol_mult = 2)
```

Details

The function `which_jumps()` calculates a *Boolean* vector, with `TRUE` for values that are isolated jumps (spikes).

The function `which_jumps()` applies a version of the Hampel median filter to identify jumps, but instead of using the median absolute deviation (MAD), it uses the `0.9` quantile of returns calculated over a rolling interval. This is in contrast to function `which_extreme()`, which applies a Hampel filter to the values themselves, instead of the returns. Returns are defined as simple differences between neighboring values.

Jumps (or spikes), are defined as isolated values that are very different from the neighboring values, either before or after. Jumps create pairs of large neighboring returns of opposite sign.

Jumps (spikes) must satisfy two conditions:

1. Neighboring returns both exceed a multiple of the rolling quantile,
2. The sum of neighboring returns doesn't exceed that multiple.

The quantile multiplier `vol_mult` controls the threshold at which values are identified as jumps. Smaller quantile multiplier values will cause more values to be identified as jumps.

Value

A *Boolean* vector with the same number of rows as the input time series or vector.

Examples

```
# Create local copy of SPY TAQ data
ta_q <- SPY_TAQ
# Calculate mid prices
mid_prices <- 0.5 * (ta_q[, "Bid.Price"] + ta_q[, "Ask.Price"])
# Replace whole rows containing suspect price jumps with NA, and perform locf()
ta_q[which_jumps(mid_prices, look_back=31, vol_mult=1.0), ] <- NA
ta_q <- xts:::na.locf.xts(ta_q)
```