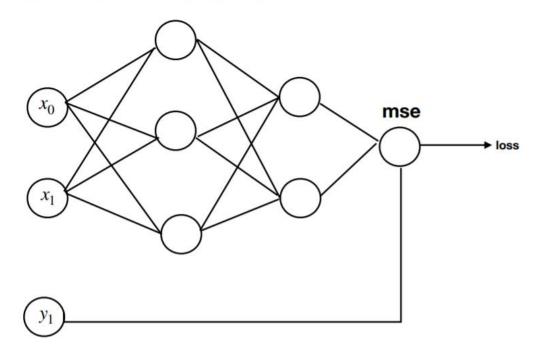
아래 그림에서 모든 \mathbf{w} 에 대한 $\frac{\partial loss}{\partial w}$ 을 구하시오



$$\frac{\partial loss}{\partial pred} = (pred - true) \quad s.t.mse = \frac{(pred - true)^2}{2}$$

$$pred = a_1^2 w_{11}^3 + a_2^2 w_{12}^3$$

$$\frac{\partial loss}{\partial w_{11}^3} = \frac{\partial loss}{\partial pred} \cdot \frac{\partial pred}{\partial w_{11}^3} = (pred - true) \cdot a_1^2$$

$$\frac{\partial loss}{\partial w_{12}^3} = \frac{\partial loss}{\partial pred} \cdot \frac{\partial pred}{\partial w_{12}^3} = (pred - true) \cdot a_2^2$$

$$\frac{\partial loss}{\partial a_1^2} = \frac{\partial loss}{\partial pred} \cdot \frac{\partial pred}{\partial a_1^2} = (pred - true) \cdot w_{11}^3$$

$$\frac{\partial loss}{\partial a_2^2} = \frac{\partial loss}{\partial pred} \cdot \frac{\partial pred}{\partial a_2^2} = (pred - true) \cdot w_{12}^3$$

$$\frac{\partial loss}{\partial z_1^2} = \frac{\partial loss}{\partial pred} \cdot \frac{\partial pred}{\partial a_1^2} \cdot \frac{\partial a_1^2}{\partial z_1^2} = (pred - true) \cdot w_{11}^3 \cdot a_1^2 (1 - a_1^2)$$

$$\frac{\partial loss}{\partial z_2^2} = \frac{\partial loss}{\partial pred} \cdot \frac{\partial pred}{\partial a_2^2} \cdot \frac{\partial a_2^2}{\partial z_2^2} = (pred - true) \cdot w_{12}^3 \cdot a_2^2 (1 - a_2^2)$$

$$\frac{\partial loss}{\partial w_{11}^2} = \frac{\partial loss}{\partial z_1^2} \cdot \frac{\partial z_1^2}{\partial w_{11}^2} = (pred - true) \cdot w_{11}^3 \cdot a_1^2 (1 - a_1^2) \cdot a_1^2$$

$$\frac{\partial loss}{\partial w_{12}^2} = \frac{\partial loss}{\partial z_1^2} \cdot \frac{\partial z_1^2}{\partial w_{12}^2} = (pred - true) \cdot w_{11}^3 \cdot a_1^2 (1 - a_1^2) \cdot a_2^1$$

$$\frac{\partial loss}{\partial w_{13}^2} = \frac{\partial loss}{\partial z_1^2} \cdot \frac{\partial z_1^2}{\partial w_{13}^2} = (pred-true) \cdot w_{11}^3 \cdot a_1^2 (1-a_1^2) \cdot a_3^2$$

$$\frac{\partial loss}{\partial w_{21}^2} = \frac{\partial loss}{\partial z_2^2} \cdot \frac{\partial z_2^2}{\partial w_{21}^2} = (pred - true) \cdot w_{12}^3 \cdot a_2^2 (1 - a_2^2) \cdot a_1^2$$

$$\frac{\partial loss}{\partial w_{22}^2} = \frac{\partial loss}{\partial z_2^2} \cdot \frac{\partial z_2^2}{\partial w_{22}^2} = (pred - true) \cdot w_{12}^3 \cdot a_2^2 (1 - a_2^2) \cdot a_2^2$$

$$\frac{\partial loss}{\partial w_{23}^2} = \frac{\partial loss}{\partial z_2^2} \cdot \frac{\partial z_2^2}{\partial w_{23}^2} = (pred-true) \cdot w_{12}^3 \cdot a_2^2 (1-a_2^2) \cdot a_3^1$$

$$\frac{\partial loss}{\partial a_1^1} = \frac{\partial loss}{\partial z_1^2} \cdot \frac{\partial z_1^2}{\partial a_1^1} + \frac{\partial loss}{\partial z_2^2} \cdot \frac{\partial z_2^2}{\partial a_1^1} = \frac{\partial loss}{\partial z_1^2} \cdot w_{11}^2 + \frac{\partial loss}{\partial z_2^2} \cdot w_{21}^2$$

$$\frac{\partial loss}{\partial a_{1}^{2}} = \frac{\partial loss}{\partial z_{1}^{2}} \cdot \frac{\partial z_{1}^{2}}{\partial a_{2}^{1}} + \frac{\partial loss}{\partial z_{2}^{2}} \cdot \frac{\partial z_{2}^{2}}{\partial a_{1}^{2}} = \frac{\partial loss}{\partial z_{1}^{2}} \cdot w_{12}^{2} + \frac{\partial loss}{\partial z_{2}^{2}} \cdot w_{22}^{2}$$

$$\frac{\partial loss}{\partial a_3^1} = \frac{\partial loss}{\partial z_1^2} \cdot \frac{\partial z_1^2}{\partial a_3^1} + \frac{\partial loss}{\partial z_2^2} \cdot \frac{\partial z_2^2}{\partial a_3^1} = \frac{\partial loss}{\partial z_1^2} \cdot w_{13}^2 + \frac{\partial loss}{\partial z_2^2} \cdot w_{23}^2$$

$$\frac{\partial loss}{\partial z_1^1} = \frac{\partial loss}{\partial a_1^1} \cdot \frac{\partial a_1^1}{\partial z_1^1} = \left(\frac{\partial loss}{\partial z_1^2} \cdot w_{11}^2 + \frac{\partial loss}{\partial z_2^2} \cdot w_{21}^2\right) \cdot a_1^1 (1 - a_1^1)$$

$$\frac{\partial loss}{\partial z_{2}^{1}} = \frac{\partial loss}{\partial a_{2}^{1}} \cdot \frac{\partial a_{2}^{1}}{\partial z_{2}^{1}} = \left(\frac{\partial loss}{\partial z_{1}^{2}} \cdot w_{12}^{2} + \frac{\partial loss}{\partial z_{2}^{2}} \cdot w_{22}^{2}\right) \cdot a_{2}^{1}(1 - a_{2}^{1})$$

$$\frac{\partial loss}{\partial z_{3}^{1}} = \frac{\partial loss}{\partial a_{3}^{1}} \cdot \frac{\partial a_{3}^{1}}{\partial z_{3}^{1}} = \left(\frac{\partial loss}{\partial z_{1}^{2}} \cdot w_{13}^{2} + \frac{\partial loss}{\partial z_{2}^{2}} \cdot w_{23}^{2}\right) \cdot a_{3}^{1}(1 - a_{3}^{1})$$

$$\frac{\partial loss}{\partial w_{11}^1} = \frac{\partial loss}{\partial z_1^1} \cdot \frac{\partial z_1^1}{\partial w_{11}^1} = \frac{\partial loss}{\partial z_1^1} \cdot x_0$$

$$\frac{\partial loss}{\partial w_{12}^1} = \frac{\partial loss}{\partial z_1^1} \cdot \frac{\partial z_1^1}{\partial w_{12}^1} = \frac{\partial loss}{\partial z_1^1} \cdot x_1$$

$$\begin{split} &\frac{\partial loss}{\partial w_{21}^1} = \frac{\partial loss}{\partial z_2^1} \cdot \frac{\partial z_2^1}{\partial w_{21}^1} = \frac{\partial loss}{\partial z_2^1} \cdot x_0 \\ &\frac{\partial loss}{\partial w_{22}^1} = \frac{\partial loss}{\partial z_2^1} \cdot \frac{\partial z_2^1}{\partial w_{22}^1} = \frac{\partial loss}{\partial z_2^1} \cdot x_1 \\ &\frac{\partial loss}{\partial w_{31}^1} = \frac{\partial loss}{\partial z_3^1} \cdot \frac{\partial z_3^1}{\partial w_{31}^1} = \frac{\partial loss}{\partial z_3^1} \cdot x_0 \\ &\frac{\partial loss}{\partial w_{32}^1} = \frac{\partial loss}{\partial z_3^1} \cdot \frac{\partial z_3^1}{\partial w_{32}^1} = \frac{\partial loss}{\partial z_3^1} \cdot x_1 \end{split}$$

S = sigmoid

$$\frac{W_1}{W_1 \, shape : (2,100)} \qquad \boxed{S} \quad \frac{W_2}{W_2 \, shape : (100,50)} \qquad \boxed{S} \quad \frac{W_3}{W_3 \, shape : (50,1)} \qquad \boxed{MSE}$$

$$\frac{\partial loss}{\partial W_1} = ? \qquad \frac{\partial loss}{\partial W_1} \, shape = ?$$

$$\frac{\partial loss}{\partial W_2} = ? \qquad \frac{\partial loss}{\partial W_2} \, shape = ?$$

$$\frac{\partial loss}{\partial W_3} = ? \qquad \frac{\partial loss}{\partial W_3} \, shape = ?$$

$$\begin{split} \frac{\partial loss}{\partial W_{1}} &= \frac{\partial loss}{\partial pred} \cdot \frac{\partial pred}{\partial W_{1}} = X^{T} \cdot \delta & \frac{\partial loss}{\partial W_{1}} shape = (2,1) \\ \frac{\partial loss}{\partial W_{2}} &= \frac{\partial loss}{\partial Z_{2}} \cdot \frac{\partial Z_{2}}{\partial W_{2}} = A_{1}^{T} \cdot \delta & \frac{\partial loss}{\partial W_{2}} shape = (100,1) \\ \frac{\partial loss}{\partial W_{3}} &= \frac{\partial loss}{\partial Z_{3}} \cdot \frac{\partial Z_{3}}{\partial W_{3}} = A_{2}^{T} \cdot \delta & \frac{\partial loss}{\partial W_{3}} shape = (50,1) \end{split}$$