

## Task 1.1)

Let's split it up

Starting with ( $'a \rightarrow 'b \rightarrow 'b$ ), it is easy to see what they corresponds to:

$x :: xs \rightarrow f x$  (foldBack f xs e)  
↑                            brace           brace  
 $'a$                              $'b$                     $'b$

Next is  $x$  itself which is  $'a$  list.

Then we return  $e$  if  $xs = []$ ,  $e$  is  $'b$

Lastly the output of the method is  $'b$

$\text{fold}(\text{fun } a x \rightarrow x - 2 \cdot a) \circ [1; 2; 3] = 3$

$$\begin{aligned}x &= 1 \\xs &= [2; 3] \\f 0 1 &= 1 - 2 \cdot 0 = 1 \\&\text{fold}(\text{fun } a x \rightarrow 1 - 2 \cdot 0) \circ [2; 3]\end{aligned}$$

$$\begin{aligned}x &= 2 \\xs &= [3] \\f 1 2 &= 2 - 2 \cdot 1 = 0 \\&\text{fold}(\text{fun } a x \rightarrow 2 - 2 \cdot 1) \circ [3]\end{aligned}$$

$$\begin{aligned}x &= 3 \\xs &= [] \\f 0 3 &= 3 - 2 \cdot 0 = 3 \\&\text{fold}(\text{fun } a x \rightarrow 3 - 2 \cdot 0) \circ 3 \circ []\end{aligned}$$

$$[] = 3$$

$\text{foldBack}(\text{fun } x \mapsto x - 2a) [1; 2; 3] \quad 0 \rightsquigarrow 9$

$$f = \text{fun } x \mapsto x - 2a$$

$$e = 0$$

$$x = 1$$

$$xs = [2; 3]$$

$$f 1 (\text{foldBack } f [2; 3] \ 0) = f 1 -4 = 1 - 2 \cdot (-4) = \underline{\underline{9}}$$

$$\hookrightarrow e = 0$$

$$x = 2$$

$$xs = [3]$$

$$f 2 (\text{foldBack } f [3] \ 0) = f 2 3 = 2 - 2 \cdot 3 = -4$$

$$\hookrightarrow e = 0$$

$$x = 3$$

$$xs = []$$

$$f 3 (\text{foldBack } f [] \ 0) = f 3 0 = 3 - 2 \cdot 0 = 3$$

$$\hookrightarrow e = 0$$

Thus it evaluates  
to 9