# **Problem B. Sherlock and the Bit Strings**

## Confused? Read the <u>quick-start guide</u>.

Small input 11 points	Solve B-small You may try multiple times, with penalties for wrong submissions.
Large input 26 points	You must solve the small input first. You have 8 minutes to solve 1 input file. (Judged after contest.)

#### Problem

Sherlock and Watson are playing a game involving bit strings, i.e., strings consisting only of the digits  $^{0}$  and  $^{1}$ . Watson has challenged Sherlock to generate a bit string S of **N**characters  $S_{1}$ ,  $S_{2}$ , ...,  $S_{N}$ . The string must obey each of **K** different constraints; each of these constraints is specified via three integers  $A_{i}$ ,  $B_{i}$ , and  $C_{i}$ . The number of  $^{1}$ s in the substring  $S_{A_{i}}$ ,  $S_{A_{i}+1}$ , ...,  $S_{B_{i}}$  must be equal to  $C_{i}$ .

Watson chooses the constraints in a way that guarantees that there is at least one string of the right length that obeys all of the constraints. However, since there could be multiple such strings, Watson wants Sherlock to choose the string from this set that is **P**<sup>th</sup> in lexicographic order, with **P** counted starting from 1.

## Input

The first line of the input gives the number of test cases,  $\mathbf{T}$ .  $\mathbf{T}$  test cases follow. Each test case begins with one line containing three integers  $\mathbf{N}$ ,  $\mathbf{K}$ , and  $\mathbf{P}$ , as described above. Then, there are  $\mathbf{K}$  more lines; the i-th of these contains three integers  $\mathbf{A}_i$ ,  $\mathbf{B}_i$  and  $\mathbf{C}_i$ , representing the parameters of the i-th constraint, as described above.

### Output

For each test case, output one line containing Case #x: Y, where x is the test case number (starting from 1) and Y is the Pth lexicographically smallest bit string among all possible strings following the K specified constraints.

## Limits

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\begin{split} &1 \leq \textbf{T} \leq 100. \\ &1 \leq \textbf{N} \leq 100. \\ &1 \leq \textbf{K} \leq 100. \\ &1 \leq \textbf{P} \leq \min(10^{18}, \text{ the number of bit strings that obey all of the constraints}). \\ &1 \leq \textbf{A}_i \leq \textbf{B}_i \leq \textbf{N} \text{ for all } 1 \leq i \leq \textbf{K}. \\ &0 \leq \textbf{C}_i \leq \textbf{N}, \text{ for all } 1 \leq i \leq \textbf{K}. \\ &(\textbf{A}_i, \textbf{B}_i) \neq (\textbf{A}_j, \textbf{B}_j), \text{ for all } 1 \leq i < j \leq \textbf{K}. \end{split}
```

Small dataset

 $\mathbf{A}_{i} = \mathbf{B}_{i}$  for all  $1 \le i \le \mathbf{K}$ .

Large dataset

 $\mathbf{B_i} - \mathbf{A_i} \le 15$  for all  $1 \le i \le \mathbf{K}$ .

Sample

Input			Output			
	1 2		Case Case			
4	3 2 3	1 1				
	4					

Note that the last sample case would not appear in Small dataset.

In Sample Case #1, the bit strings that obey the only constraint in lexicographically increasing order are [010, 011, 110, 111].

In Sample Case #2, the bit strings that obey the given constraints in lexicographically increasing order are [0101, 1010].