

Clase 3

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$$\begin{aligned} |J_1 m_1\rangle \quad \rightarrow \quad [J_{1i}, J_{1j}] = i\hbar \epsilon_{ijk} J_{1k} \quad &\rightarrow \quad J_1^2 |J_1 m_1\rangle = \hbar^2 J_1(J_1 + 1) |J_1 m_1\rangle \\ &\rightarrow \quad J_{1z} |J_1 m_1\rangle = \hbar m_1 |J_1 m_1\rangle \end{aligned}$$

$$|J_1 m_1\rangle \otimes |J_2 m_2\rangle = |J_1 J_2 m_1 m_2\rangle = |m_1 m_2\rangle$$

$$[\vec{J}_1, \vec{J}_2] = 0$$

$$[J_1^2, J_2^2] = 0$$

$$[J_{1z}, J_2^2] = 0$$

$$J^2 |jm\rangle = \hbar^2 j(j+1) |jm\rangle$$

$$J_z |jm\rangle = \hbar m |jm\rangle$$

$\{J^2, J_z, J_1^2, J_2^2\}$ conmutan entre sí.

$$|jm\rangle = \sum_{m_1=-1/2}^{1/2} \sum_{m_2=-1/2}^{1/2} |m_1 m_2\rangle \langle m_2 m_1 | J_m \rangle$$

$$|m_1 m_2\rangle = \sum_{j=J_{min}}^{J_{max}} \sum_{m_j=-j}^j |jm\rangle \langle jm | m_1 m_2 \rangle$$

$$\delta_{jj'} \delta_{mm'} = \sum_{m_1} \sum_{m_2} \langle j' m' | m_1 m_2 \rangle \langle m_1 m_2 | jm \rangle$$