



**Credit Hours System**

**ELCN101**

**Electronics-1**



**Cairo University**

**Faculty of Engineering**

## **Project 2: BJT Transistor and Amplifier**

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**Program: CCEE**

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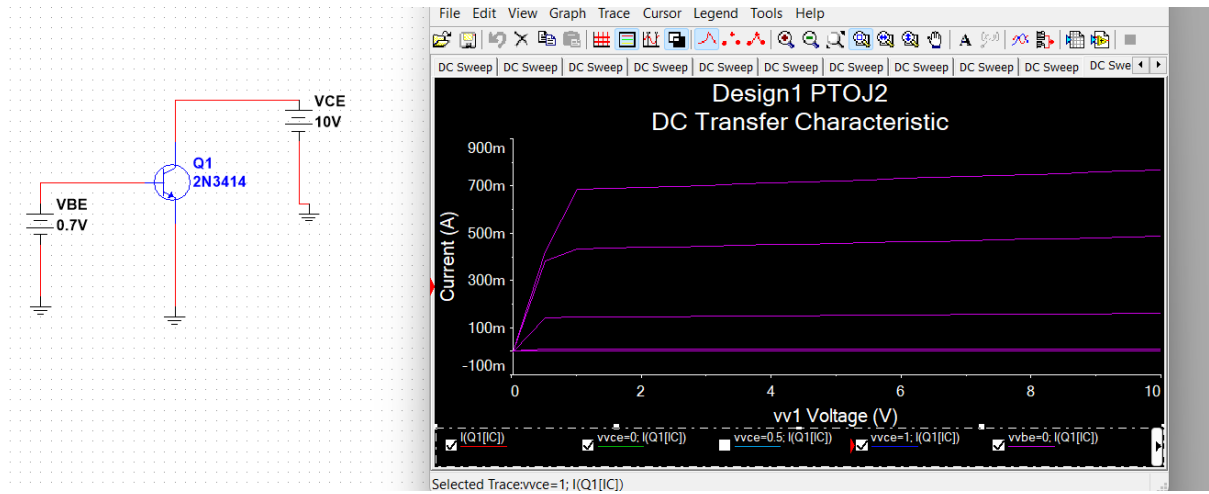
**Dr. Mohamed Refky**

# Part 1: I/V Characteristics:

## NPN

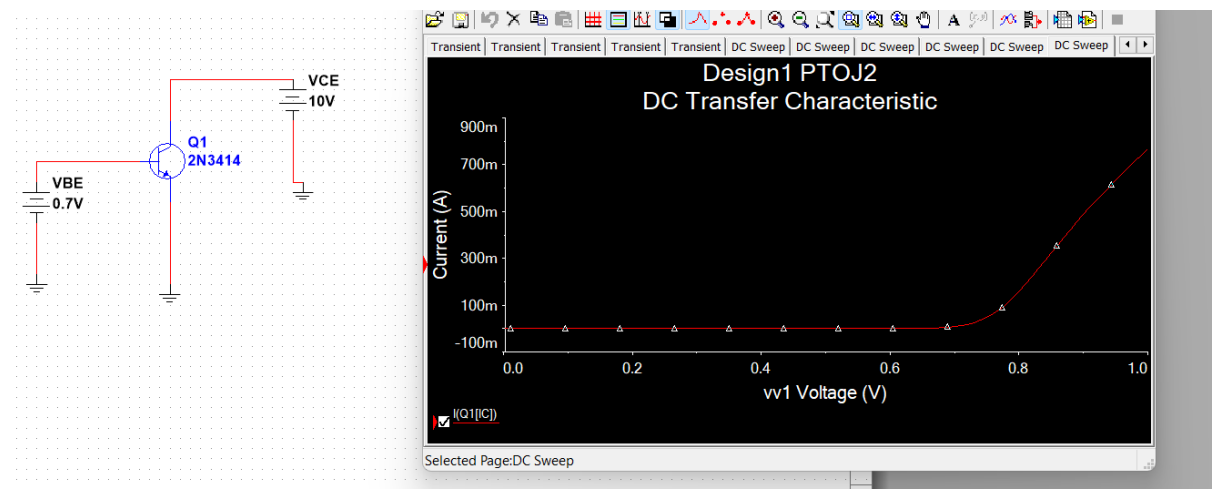
1)

a)  $I_C$  VS  $V_{CE}$  (for different  $V_{BE}$ 's)



**Notice that**  $I_C$  is not constant as  $V_{CE}$  changes; it is affected with the change in the collector-emitter voltage due to Early effect.

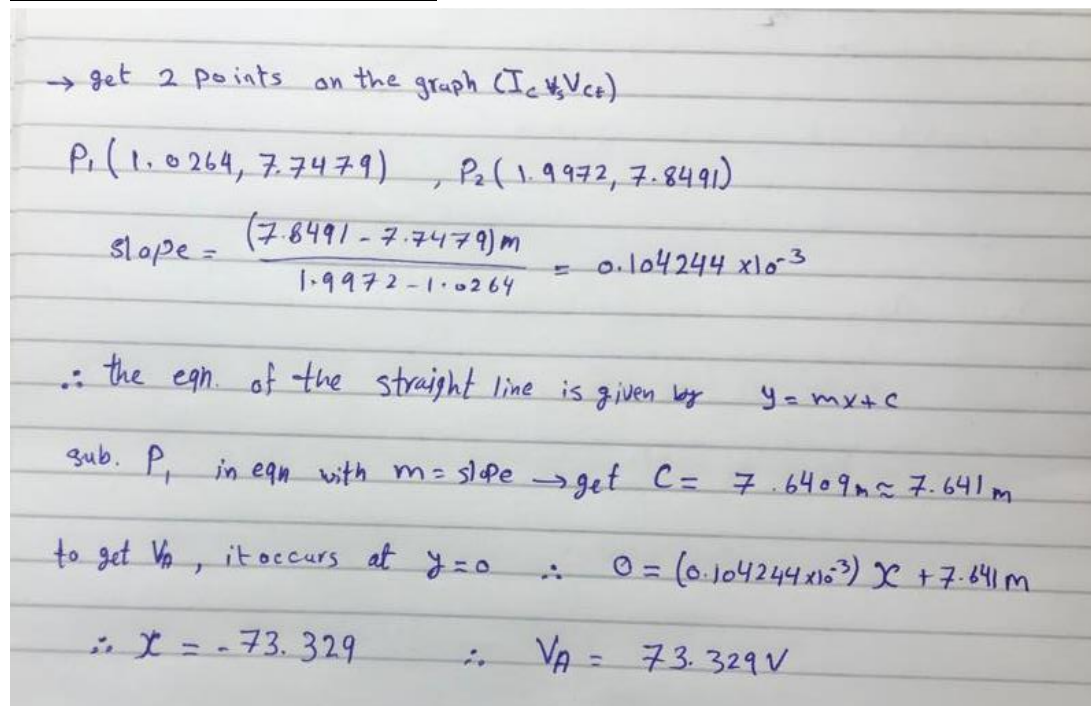
b)  $I_C$  VS  $V_{BE}$



**Notice That** In the active region, the collector current  $I_C$  is exponentially related to the base-emitter voltage  $V_{BE}$ .

c) To get the value of Early voltage ( $V_A$ ) for this transistor

### Using Hand Calculations



Handwritten calculations on lined paper:

→ get 2 points on the graph ( $I_C$  vs  $V_{CE}$ )

$P_1(1.0264, 7.7479)$  ,  $P_2(1.9972, 7.8491)$

$$\text{slope} = \frac{(7.8491 - 7.7479)m}{1.9972 - 1.0264} = 0.104244 \times 10^{-3}$$

∴ the eqn. of the straight line is given by  $y = mx + c$

sub.  $P_1$  in eqn with  $m = \text{slope} \rightarrow \text{get } C = 7.6409m \approx 7.641m$

to get  $V_A$ , it occurs at  $y = 0$  ∴  $0 = (0.104244 \times 10^{-3})x + 7.641m$

∴  $x = -73.329$  ∴  $V_A = 73.329V$

**$V_A = 73.329 V$**

2)

### Bias Point

**AT  $V_{BE} = 0.7V$**

**$V_{CE} = 10V$**

**$I_C = 8.68 \times 10^{-3} A$**

**Analytical  $g_m = (8.68 \times 10^{-3}) / (26 \times 10^{-3}) = 333.85m$**

**$g_m$  (from graph)  $= 2.5284$**

**Percentage error  $= 86\%$**

**-Very large error**

## $R_o$

$$R_o = |-73.3| / (8.68 \times 10^{-3}) = 8.4447k$$

$$R_o \text{ From Graph} = 9.593k$$

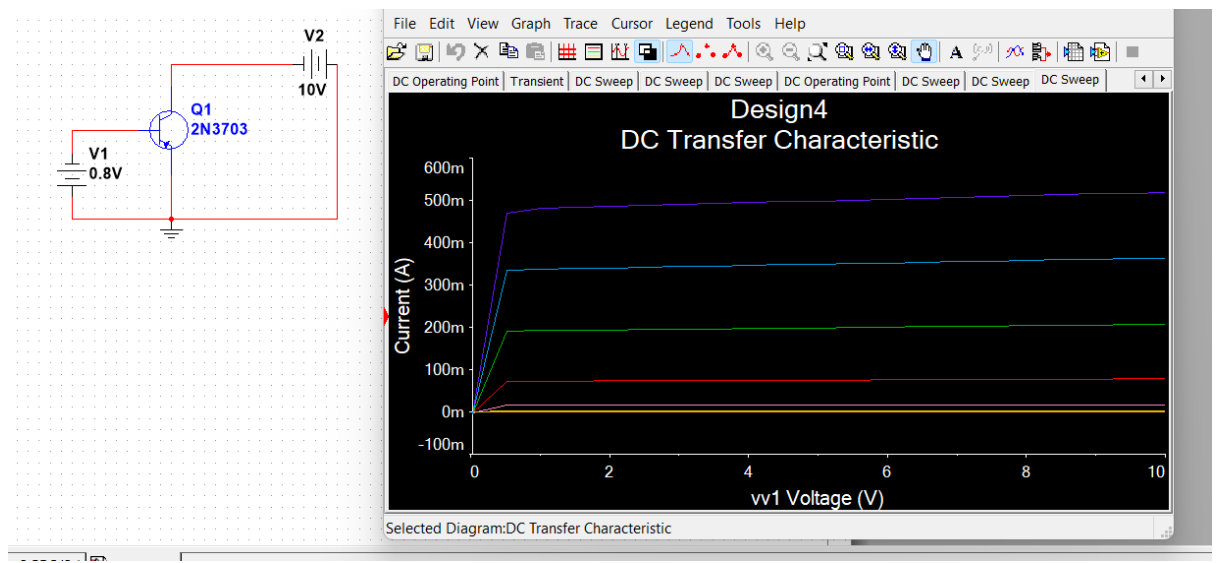
$$\text{Percentage Error} = 11.95\%$$

**Notice that calculation of  $R_o$  from the graph by assuming a linear relation is valid only if the change in  $V_{CE}$  is minimal.**

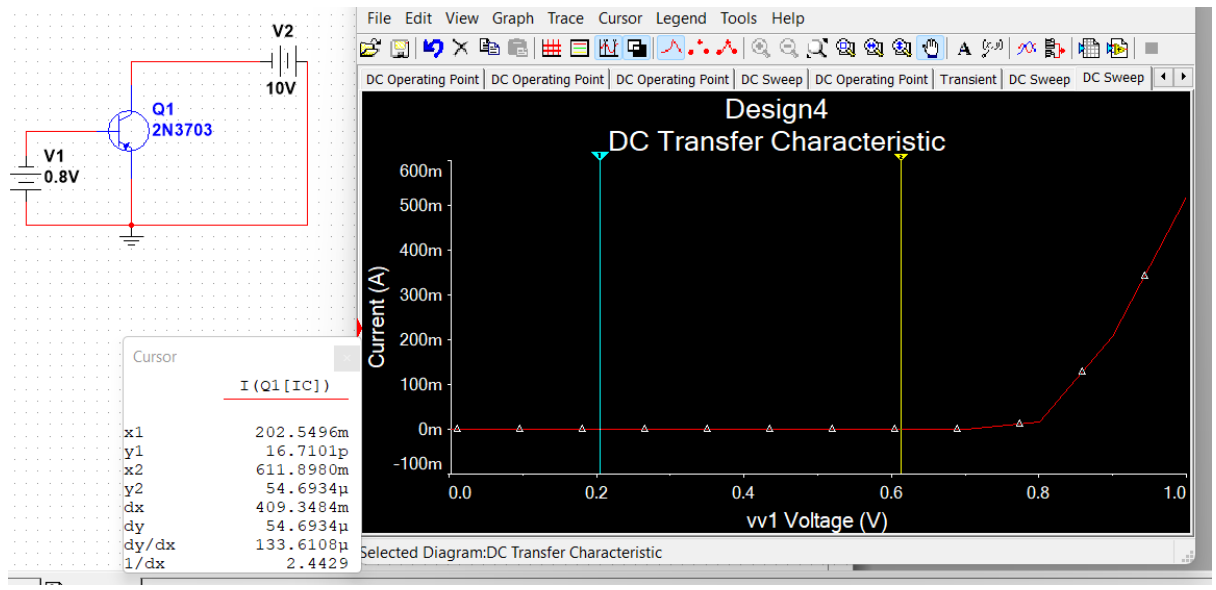
## PNP

1)

**a)  $I_C$  VS  $V_{EC}$  (for different  $V_{EB}$ 's)**

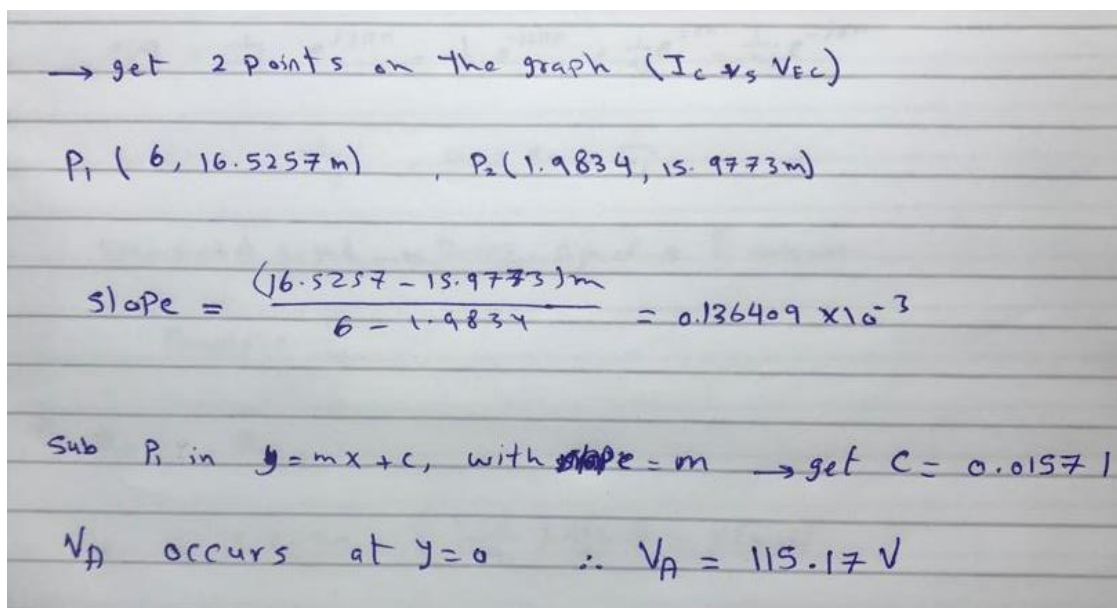


**b)  $I_C$  VS  $V_{EB}$**



c) To get the value of Early voltage ( $V_A$ ) for this transistor

### Using Hand Calculations



**$V_A = 115.17V$**

It is noted that the Early voltage effect is higher for the PNP transistor as compared to the NPN transistor.

2)

### Bias Point

AT  $V_{EB} = 0.8V$

$V_{EC} = 10V$

$I_C = 17.07365m$

3	I(Q1[IC])	17.07365 m
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Analytical  $g_m = (17.07 \cdot 10^{-3}) / (26 \cdot 10^{-3}) = 656.67m$

$g_m$  (from graph) = 388.7

Percentage error = 41%

-large error

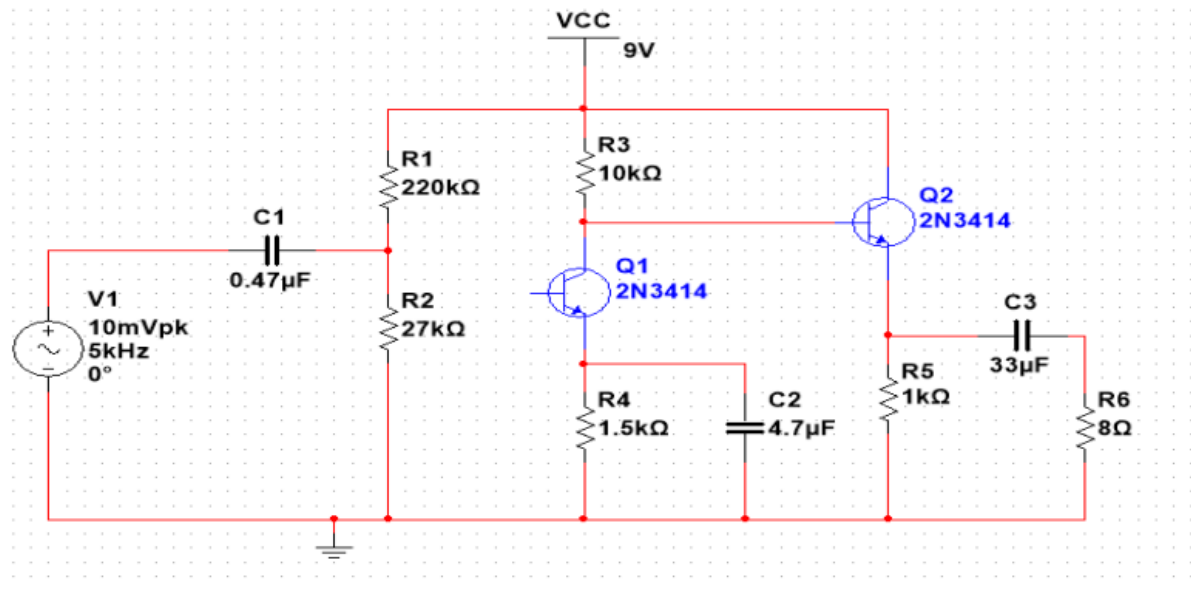
### - $R_o$

$R_o = |-127.14| / (17.07 \cdot 10^{-3}) = 7.448k$

$R_o$  From Graph = 6.993k

Percentage Error = 6.1%

## Part 2: Amplifier Simulation:



### AT DC OPERATING POINTS

#### At Q1

$$\beta_1 = (I_c / I_b) = 213.43 / 2.33 = 91.6$$

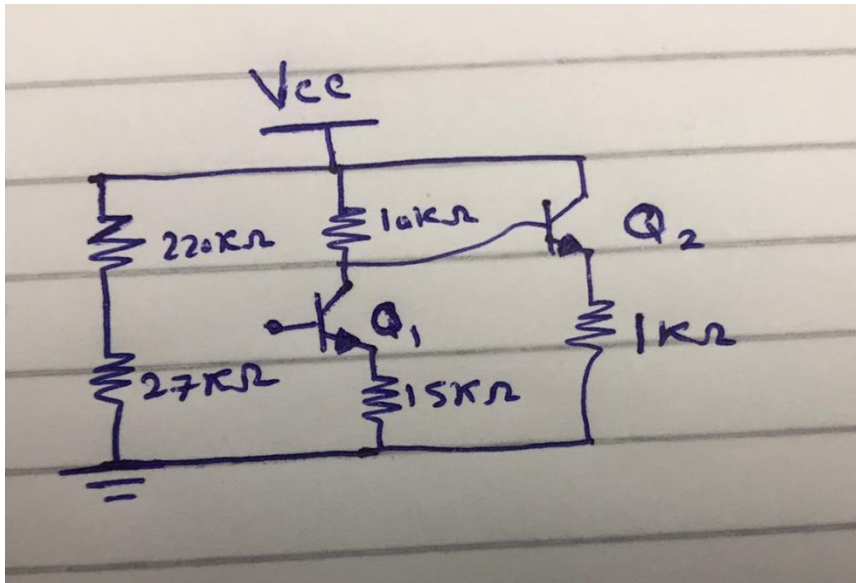
$$V_{BE1} = 0.6V$$

#### At Q2

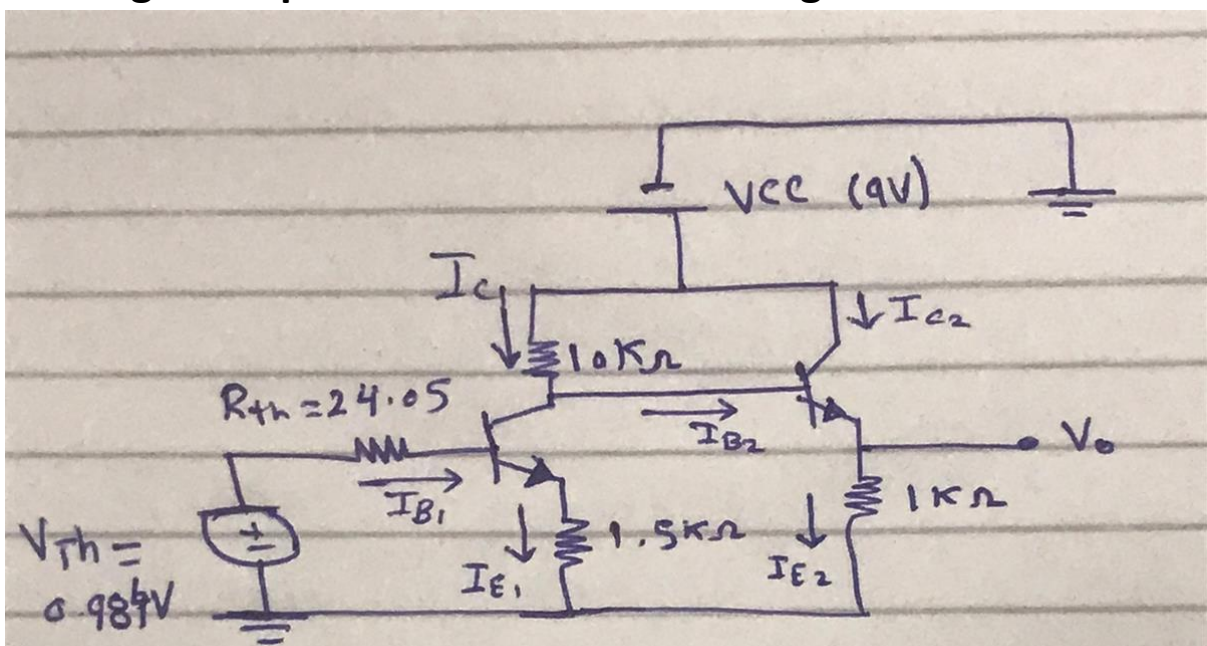
$$\beta_2 = (I_c / I_b) = (5.65 / 0.047) = 120.21$$

$$V_{BE1} = 0.69V$$

### DC Analysis (Capacitors are O.C.)



Getting the equivalent circuit for the original circuit



$$V_{Th} = \left( \frac{27}{220+27} \right) 9 = 0.984V$$

$$R_{Th} = 220k // 27k = 24.05k\Omega$$



$$V_{th} = 0.984V$$

$$R_{th} = 24.05 \text{ k}\Omega$$

### **KVL at loop 1:**

$$-V_{th} + I_{B1} * R_{th} + 0.6 + I_{E1} * 1.5 = 0, I_{E1} = (\beta + 1) I_{B1}$$

$$I_{B1} = 2.35 \text{ }\mu\text{A}$$

$$I_{C1} = 214.9 \text{ }\mu\text{A}$$

$$I_{E1} = 217.25 \text{ }\mu\text{A}$$

### **KVL at loop 2:**

$$-V_{CC} + 10(I_{C1} + I_{B2}) + 0.69 + I_{E2} * 1 = 0, I_E = (\beta_2 + 1) I_{B2}$$

$$I_{B2} = 47.23 \text{ }\mu\text{A},$$

$$I_{C2} = 5.64 \text{ mA},$$

$$I_{E2} = 5.695 \text{ mA}$$

### **Model Parameters**

$$g_{m1} = I_{c1} / V_T = 8.26 \text{ micro Siemens}$$

$$g_{m2} = I_{c1} / V_T = 0.216 \text{ Siemens}$$

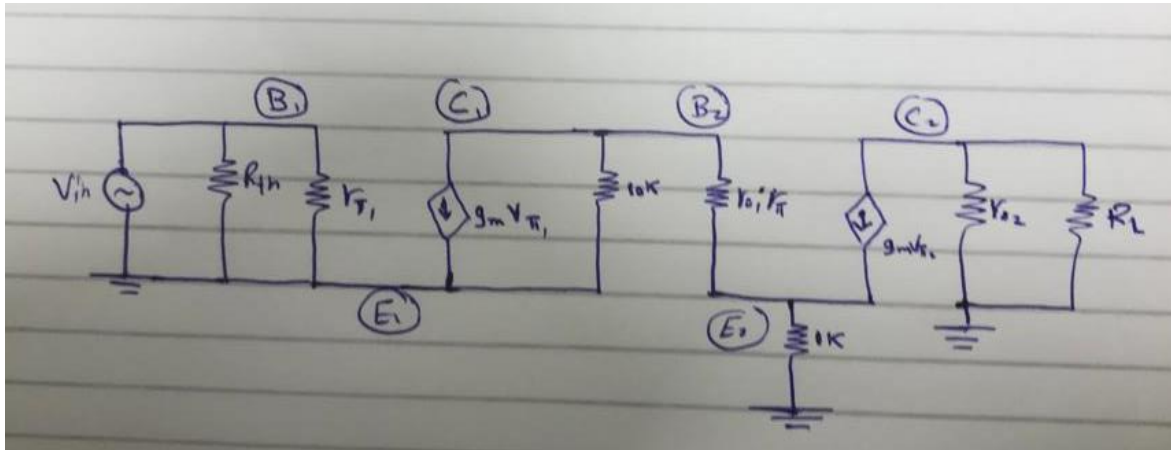
$$r_{\pi 1} = \beta_1 / g_{m1} = 11.071 \text{ k}\Omega$$

$$r_{\pi 2} = \beta_2 / g_{m2} = 551.27 \Omega$$

$$r_{o1} = V_{A1} / I_{c1} = 342.48 \text{ k}\Omega$$

$$r_{o2} = V_{A2} / I_{c2} = 13.0496 \text{ k}\Omega$$

**The circuit reduces to the model shown:**

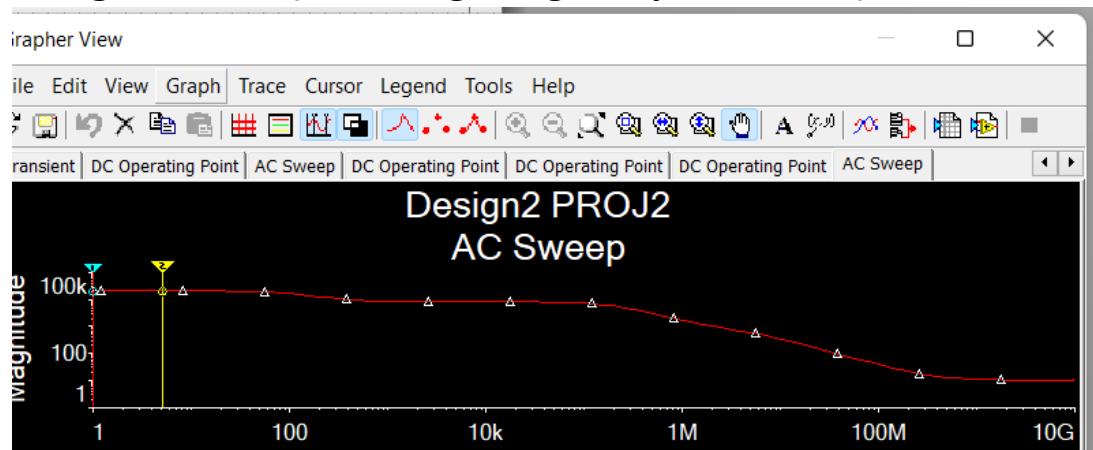


## AC Analysis (Capacitors are Open-circuited)

### To get $R_{in}$

$$R_{in} = V_{in} / I_{in} = R_{th} // r_{\pi 1} = 7.54 \text{ k}\Omega$$

### Using Multisim (assuming the given parameters)



$$\% \text{error} = ((7.54 - 8.26) / 7.54) * 100 = 9.55\%$$

### To get $R_{out}$

$V_{in} = 0$  and Remove  $R_L$

## Hand Analysis

KCL at (E)

$$-\frac{V_{out}}{r_{\pi 2} + (10k \parallel r_{o1})} + g_{m2} V_{\pi 2} + I_{out} = \frac{V_{out}}{1k \parallel r_{o2}}$$

$$V_B = \frac{V_{out} (10k \parallel r_{o1})}{r_{\pi 2} (10k \parallel r_{o1})}$$

$$V_{BF} = V_B - V_E = V_{out} \left[ \frac{10k \parallel r_{o1}}{r_{\pi 2} + 10k \parallel r_{o1}} - 1 \right]$$

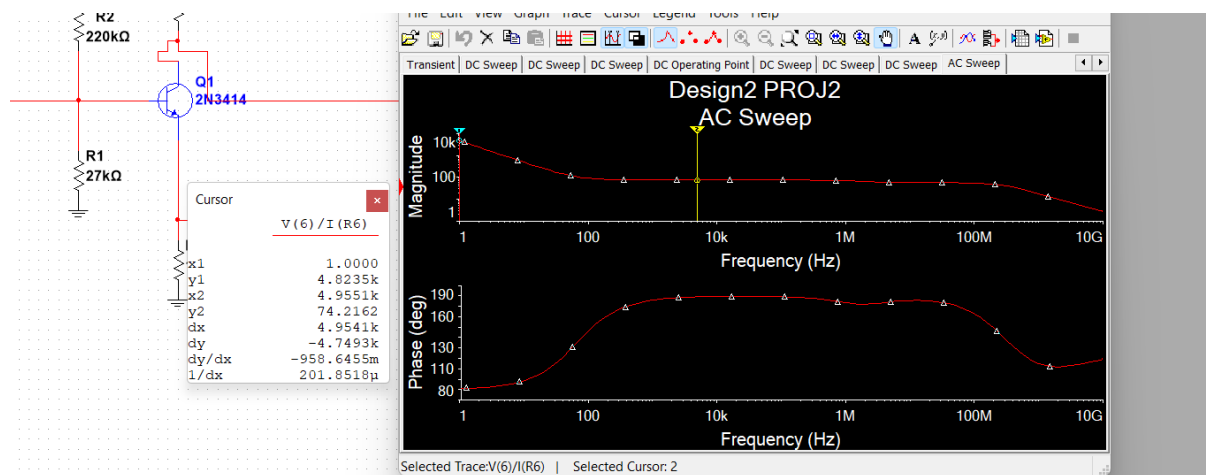
By sub. and rearrangement

$$I_{out} = V_{out} \left[ \frac{1}{1k \parallel r_{o2}} + \frac{1}{r_{\pi 2} + 10k \parallel r_{o1}} - g_{m2} \left( \frac{10k \parallel r_{o1}}{r_{\pi 2} + 10k \parallel r_{o1}} \right) \right]$$

$$R_{out} = \frac{V_{out}}{I_{out}}$$

substituting with the obtained values,  $R_{out} \approx 77.9843 \Omega$

## On Multisim



$$\%error = ((77.9843 - 74.2162) / 77.9843) * 100 = 4.832\%$$

## Notice that:

- Rin is large (in kilos), contrary to Rout (7.54kohm vs 77ohm), which is what we seek in an amplifier circuit.

- An amplifier is ideal if it has infinite input resistance ( $R_{in}$ ) and zero output impedance ( $R_{out}$ )
- Percentage errors in  $R_{in}$ ,  $R_{out}$ , and  $A_v$  are all small ( $< 10\%$ ) which make the results acceptable.

### To Get $A_v$ (Voltage Gain)

#### Using Hand Calculations

KCL @ (E)

$$g_{m2} V_{\pi 2} + \frac{V_{\pi 2}}{r_{\pi 2}} = \frac{V_{out}}{r_{o2} \parallel \frac{1}{126}}$$

$$V_{\pi 2} \left( g_{m2} + \frac{1}{r_{\pi 2}} \right) = \frac{V_{out}}{r_{o2} \parallel \frac{1}{126}}$$

$$\therefore V_{\pi 2} = 0.554 V_{out}$$
  

KCL @ ( $B_2$ )

$$\frac{V_{B2}}{10} + \frac{V_{B2}}{r_{\pi 2}} + g_{m1} V_{\pi 1} + \frac{V_{B2}}{r_{o1}} = 0$$

$$\therefore V_{in} = V_{\pi 1}$$

$$V_{B2} = V_{B2} - V_{C2} = V_{B2} - V_{out}$$

$$V_{B2} = 1.55 V_{out}$$

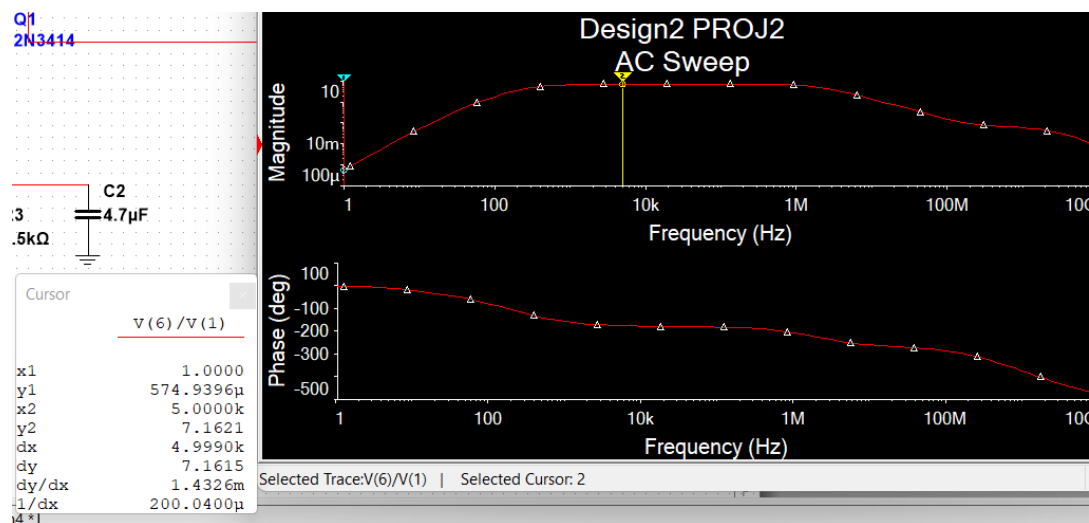
$\therefore$  By sub. and rearranging, we obtain

$$V_{out} \left[ \frac{0.554}{r_{\pi 2}} + \frac{1.55}{r_{o1}} + \frac{0.554}{10} \right] = -g_{m1} V_{in}$$

$$\therefore A_v = \frac{V_{out}}{V_{in}} = -7.0818 V$$

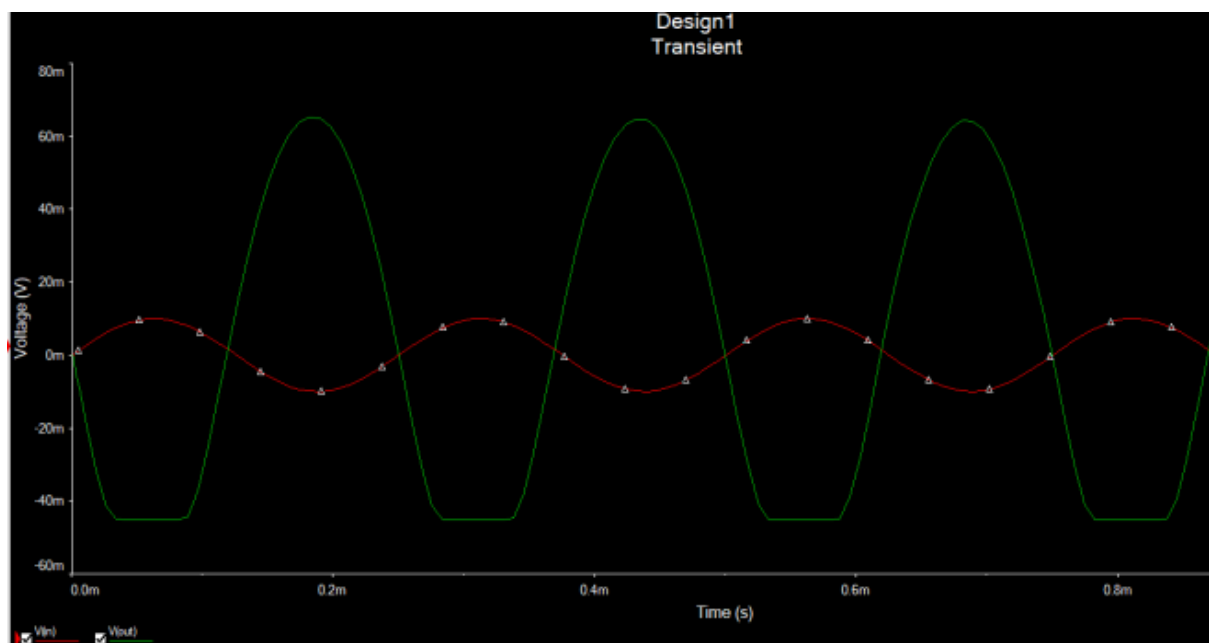
**Notice That:** The voltage gain is negative as the common emitter gain is negative and it is the dominant transistor here.

## On Multisim



$$\%error = ((7.0818 - 7.1621) / 7.0818) * 100 = 1.14\%$$

## Simulation of Vin vs Vout using Transient analysis



**Notice that** Vout is > Vin which is the goal of an amplifier circuit.