

MAIA - MedicAl Imaging and Applications  
**Advanced Image Analysis**

Lectures on Advanced Color Image Processing

# B1 - Human Vision System The Retina and the Brain

March/2018

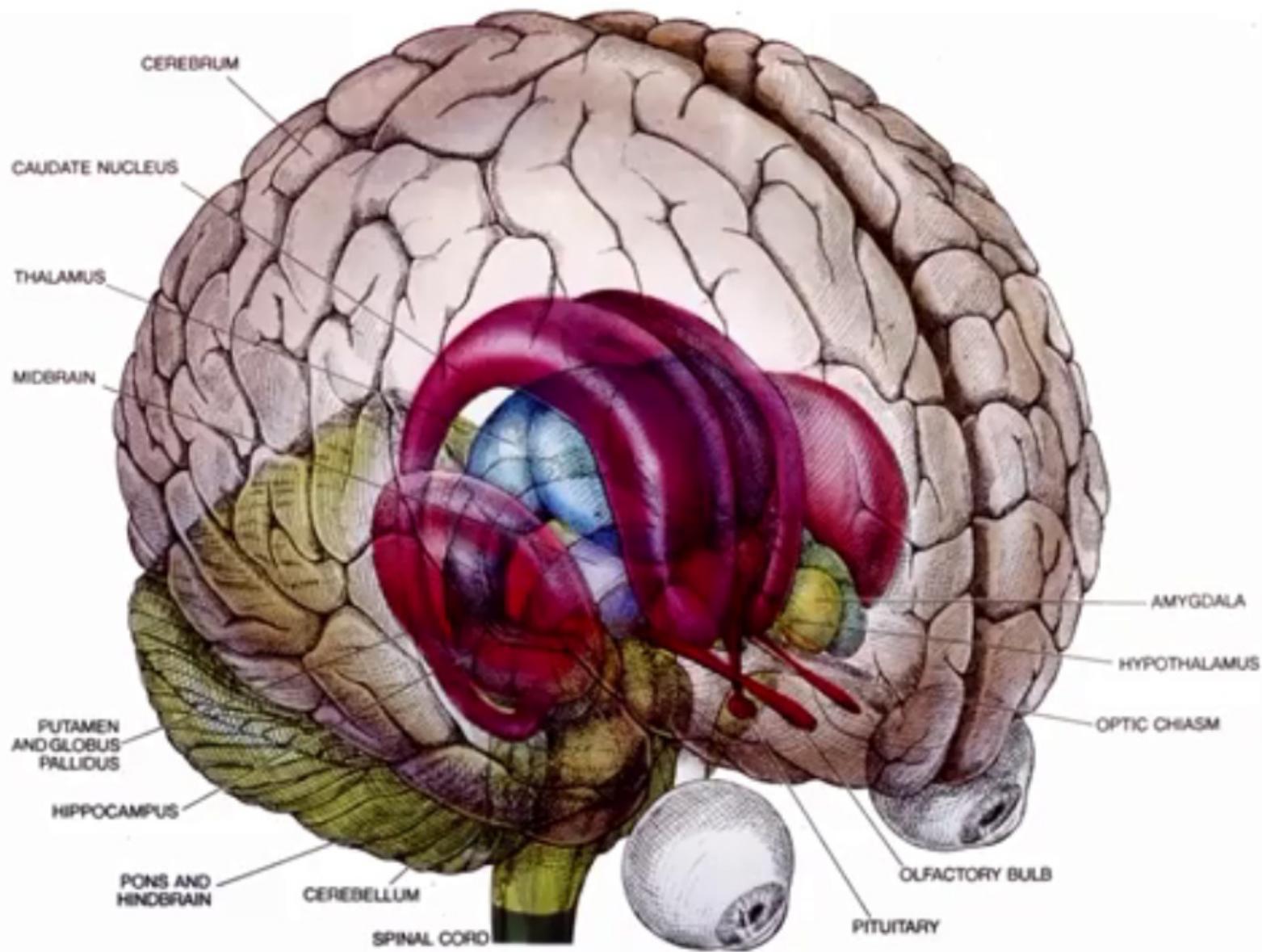
Adrian Galdran - Post-Doctoral Researcher  
Biomedical Imaging Lab – INESC TEC Porto (Portugal)  
<http://bioimglab.inesctec.pt/>



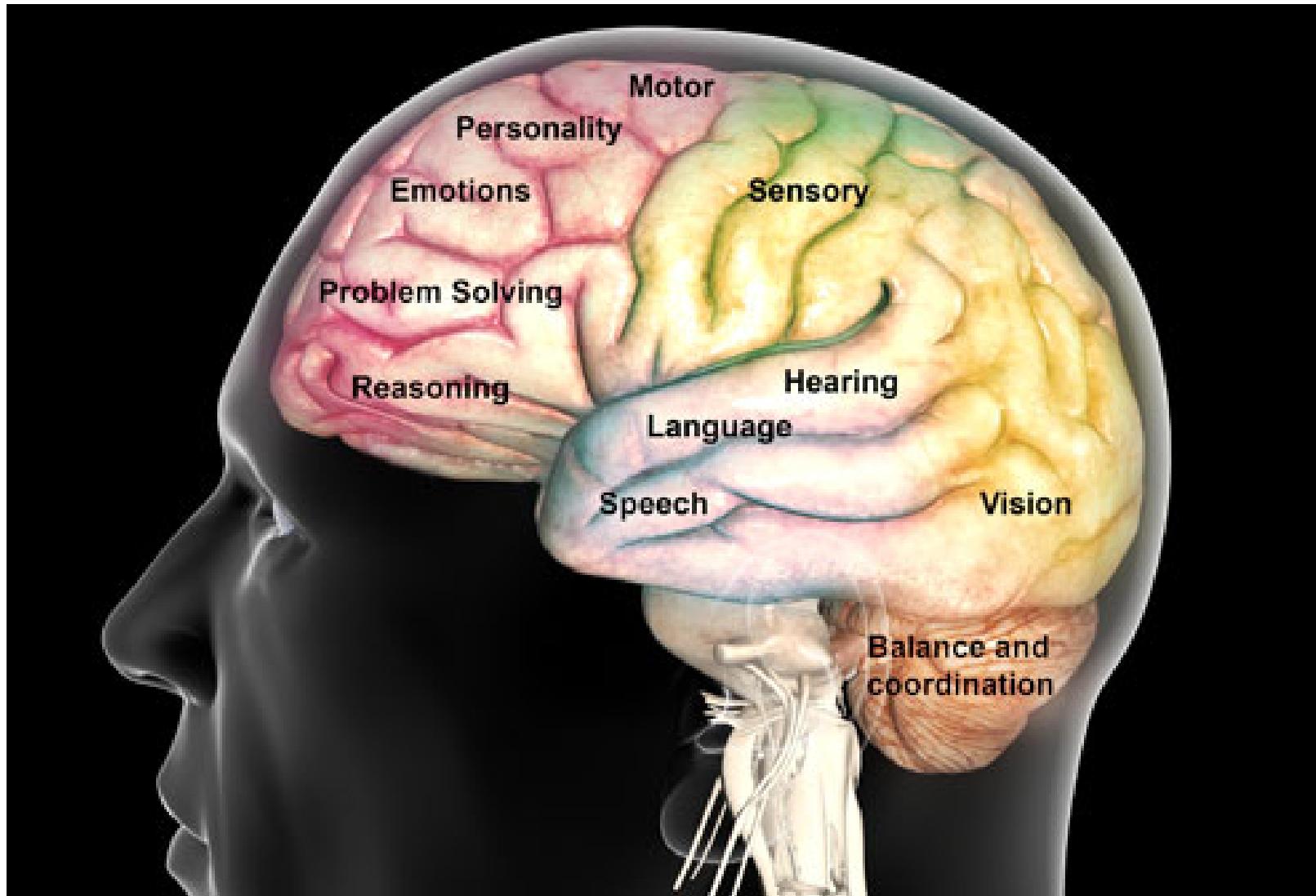
# 1 - Basics of Human Perception

- **B1 - Human Vision System: The Retina and the Brain**
  1. **Basics of Human Perception.**
  2. Perception and Color. Measuring Color.
  3. Color Spaces. Perceptually Uniform Color Spaces.
  4. Application: Color Image Segmentation. Superpixels.
  5. Introduction to Color Constancy and Retinex.
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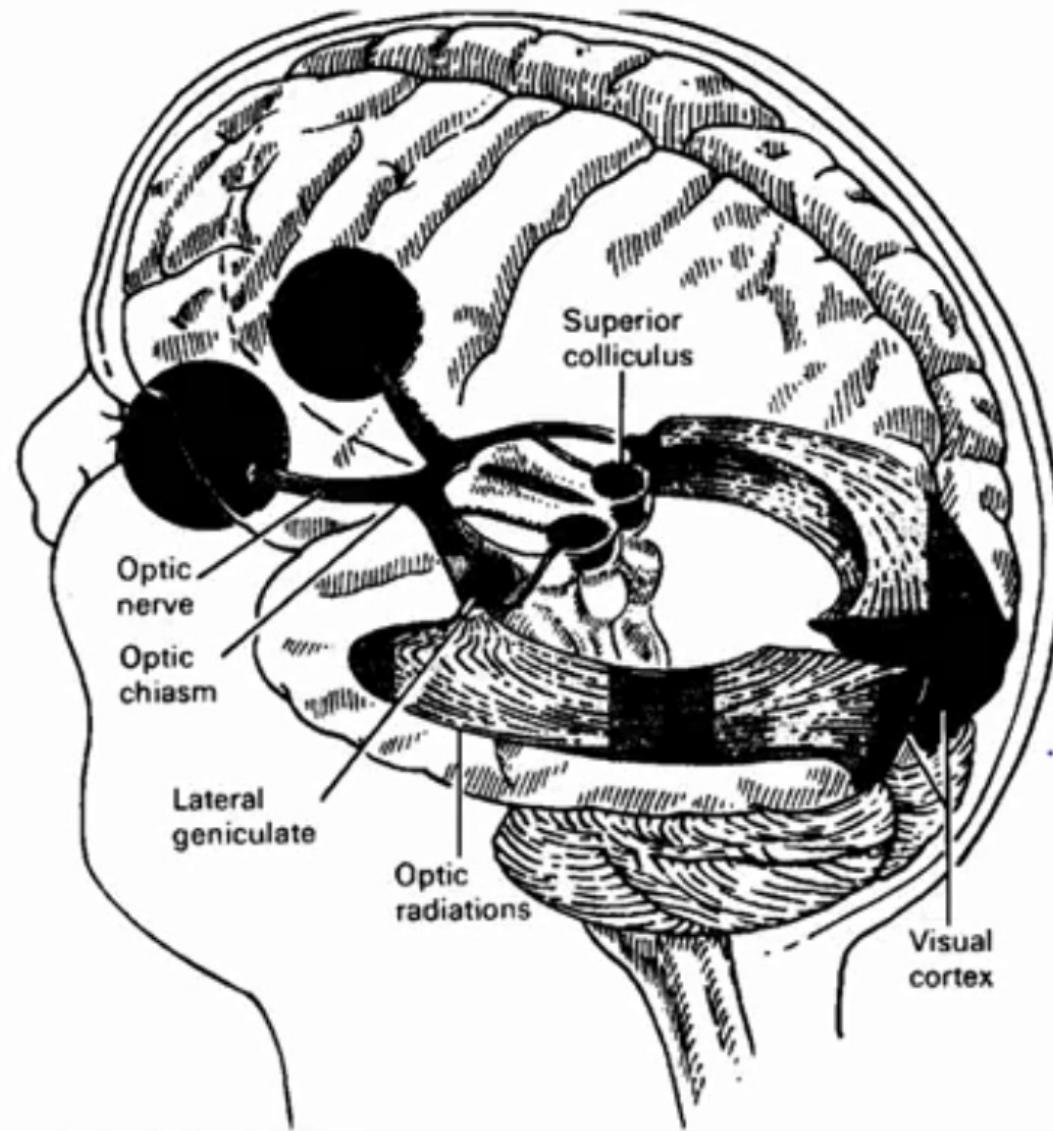
# 1 - Basics of Human Perception



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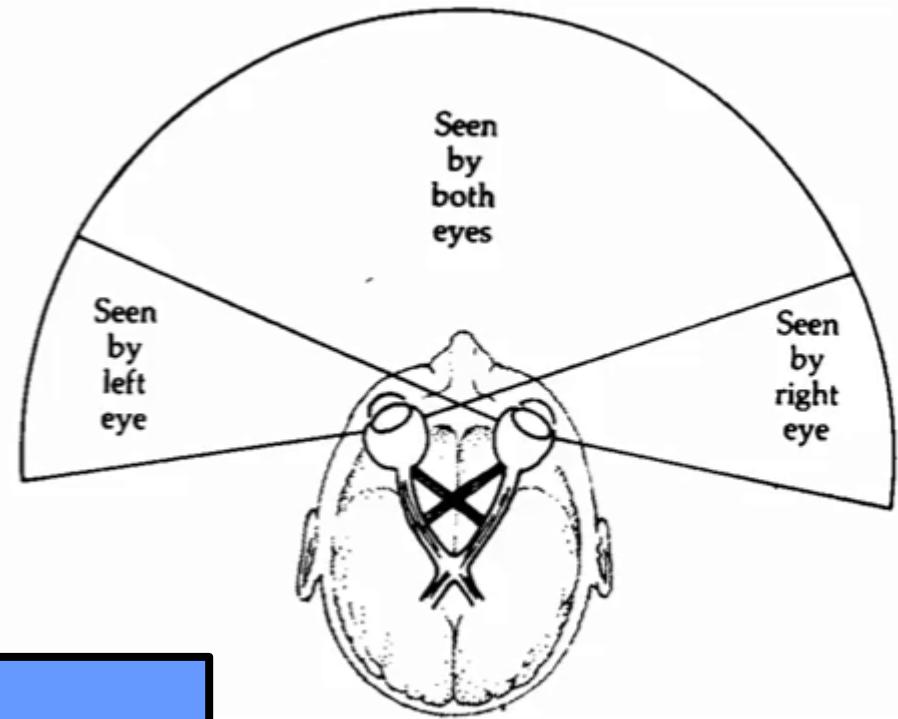
# 1 - Basics of Human Perception

Vision Field (degrees):

Each eye:  $160^\circ$  (**monocular**)

Both eyes:  $160^\circ + 160^\circ = 320^\circ$ ?

No, because there is overlap:  
 $120^\circ$  (**binocular**)

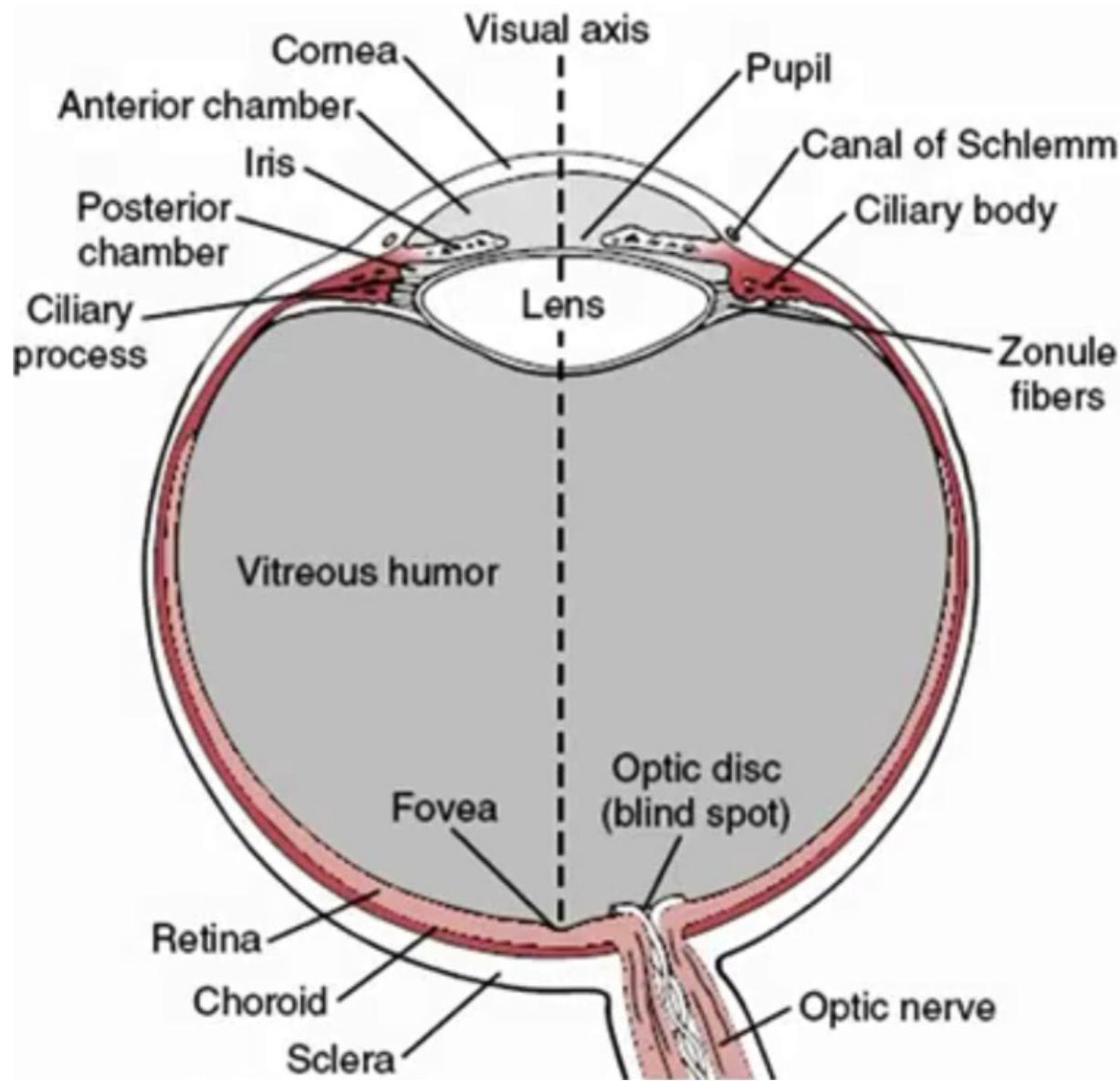


QUIZ!

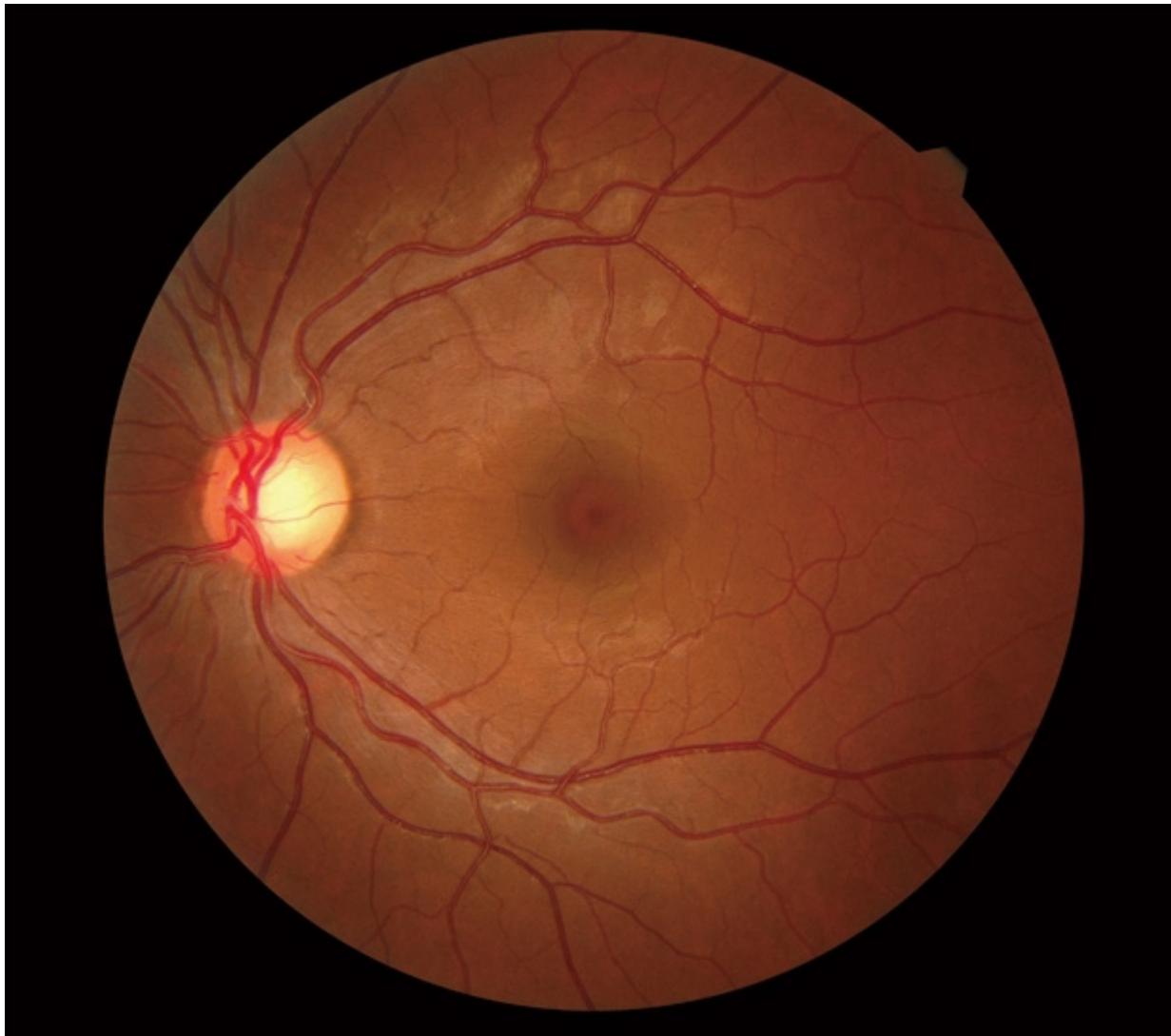
What is our total visual field?

Link: <https://goo.gl/forms/zX8xLDuz6lXOVatg2>

# 1 - Basics of Human Perception



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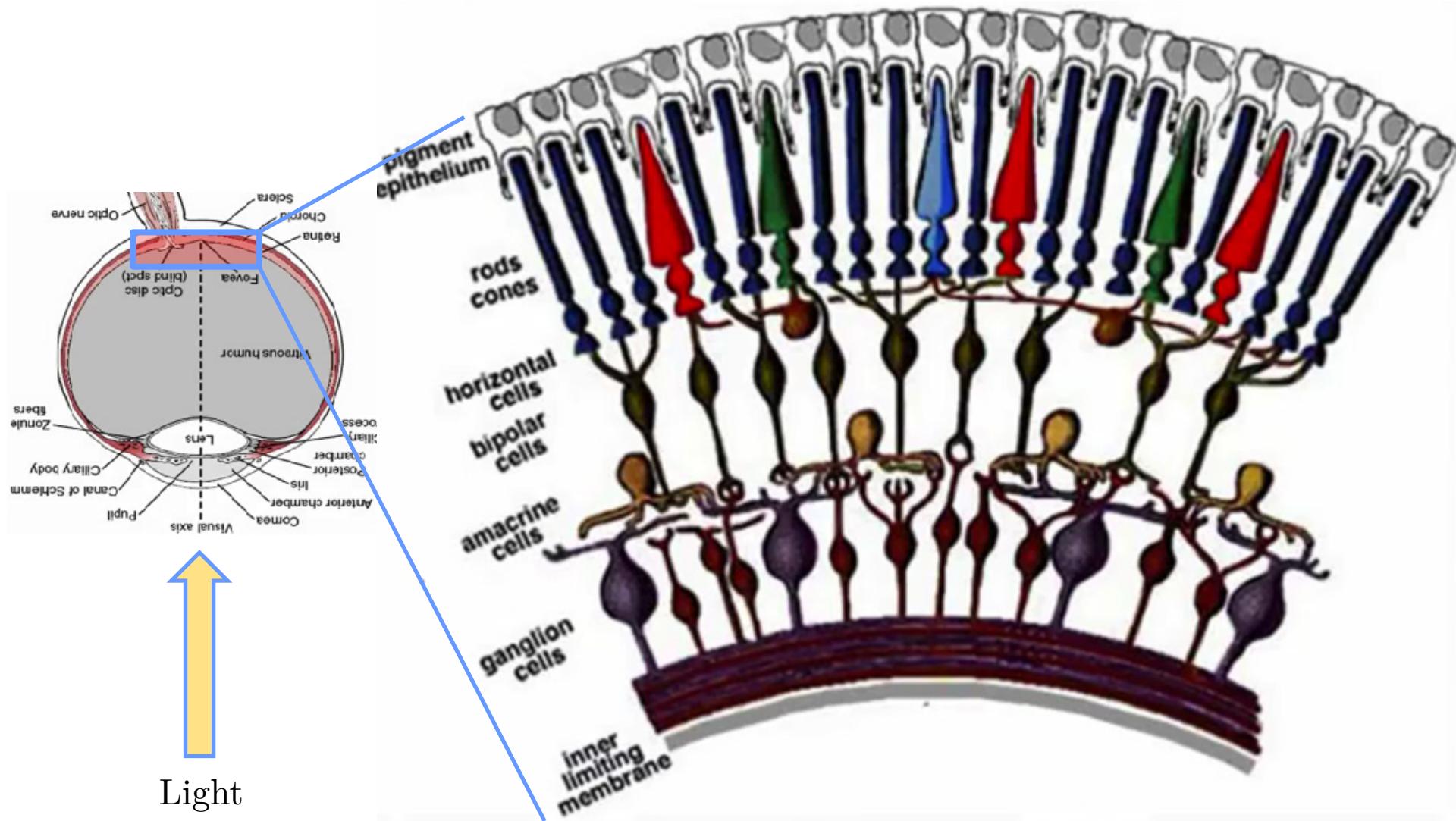


+

.



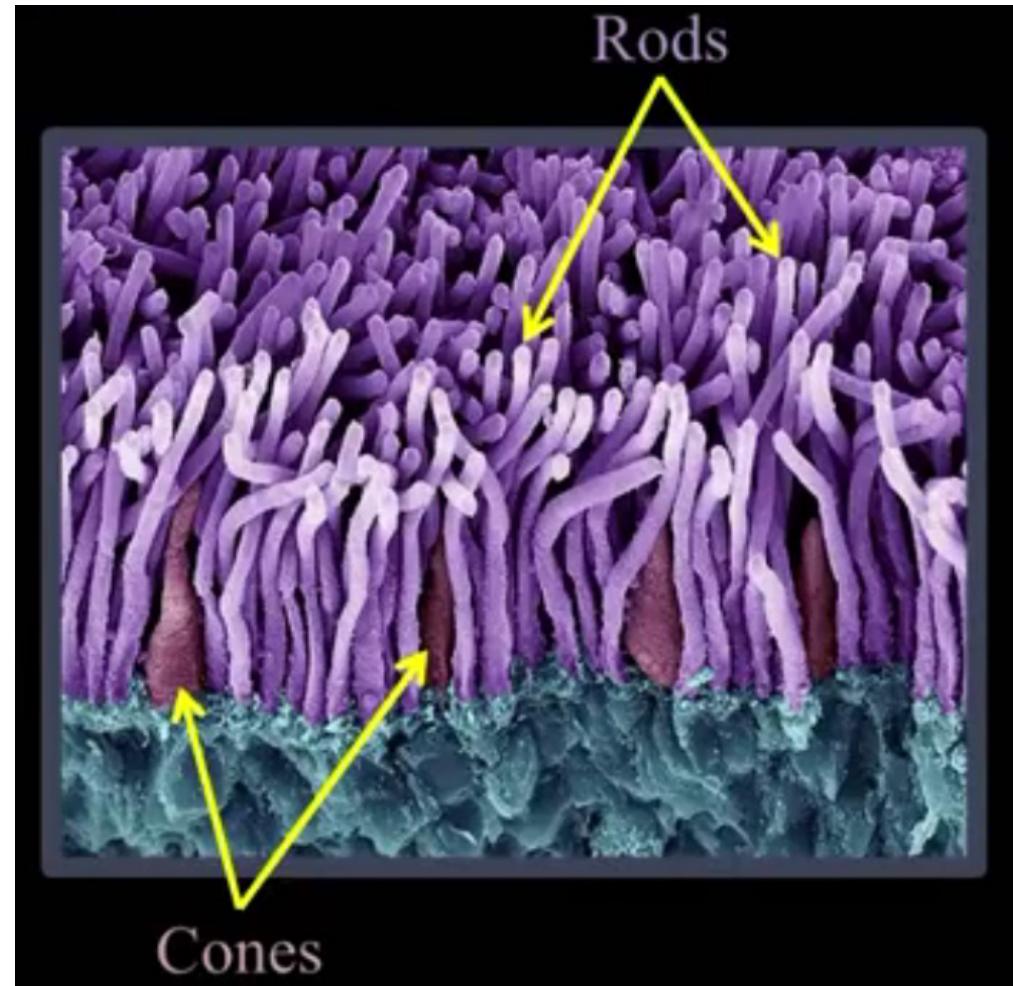
# 1 - Basics of Human Perception



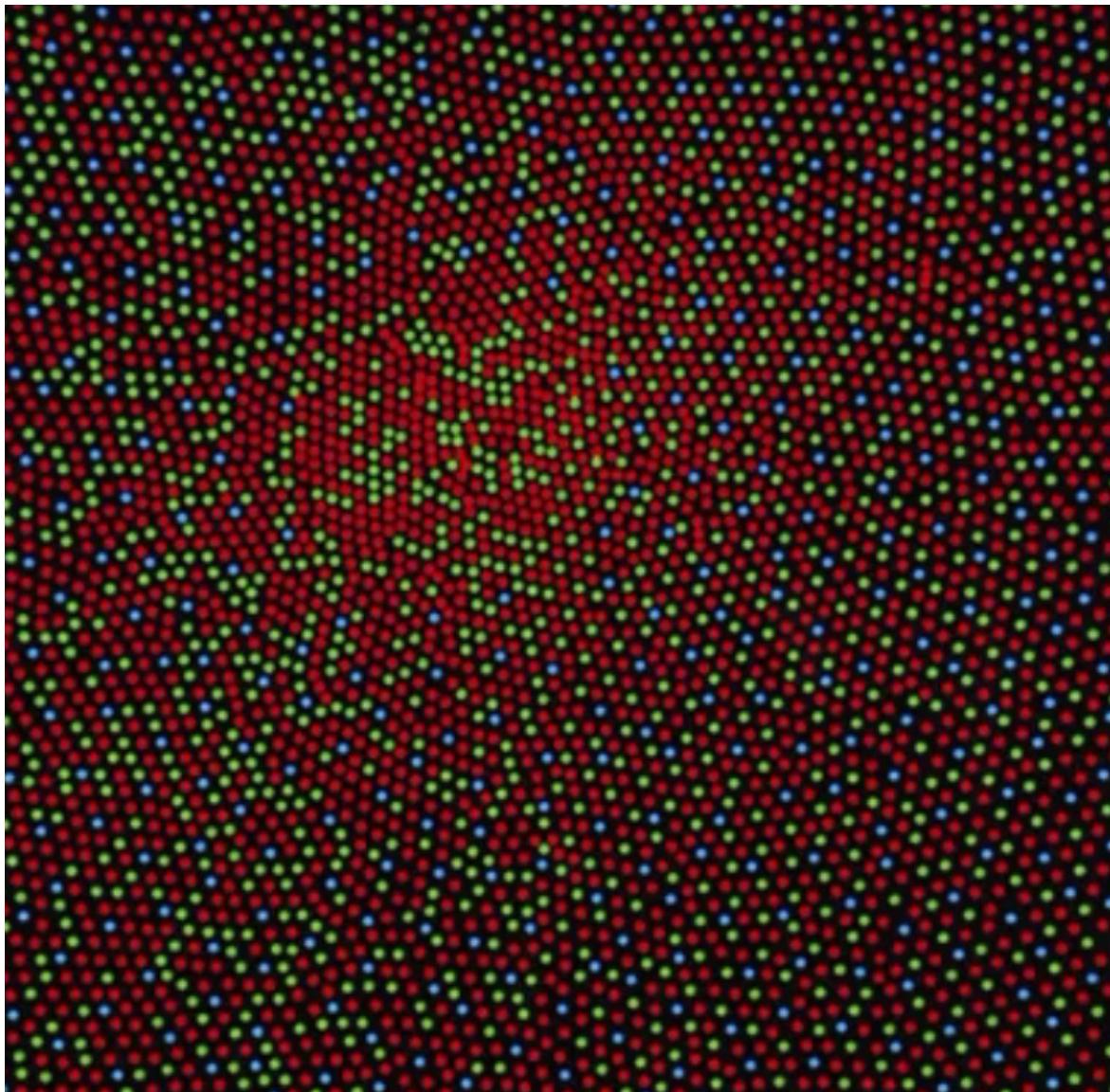
# 1 - Basics of Human Perception

## Rods & Cones:

- 120 million rods
- 6-7 million cones.
- Rods are 1000x more light sensitive than cones.
- Rods discriminate brightness levels when there is low illumination.
- Cones discriminate colors.

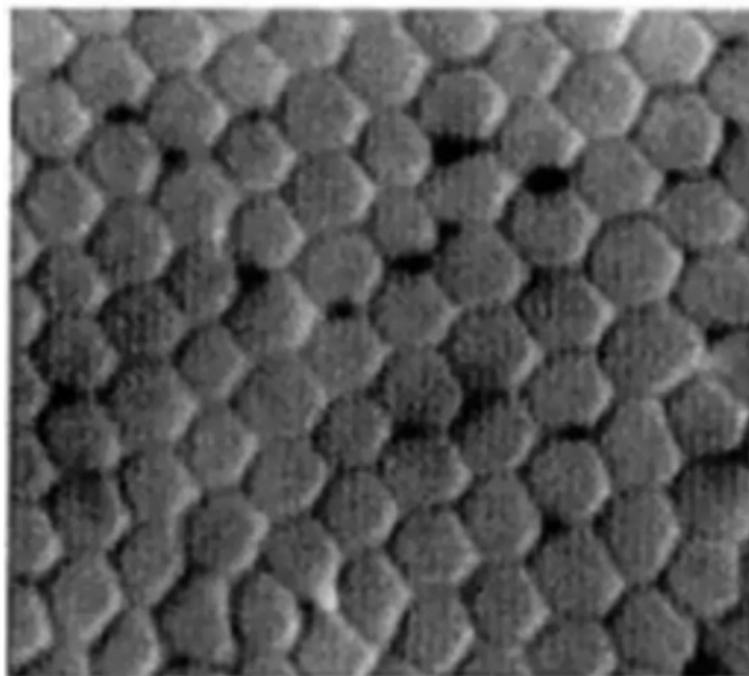


# 1 - Basics of Human Perception

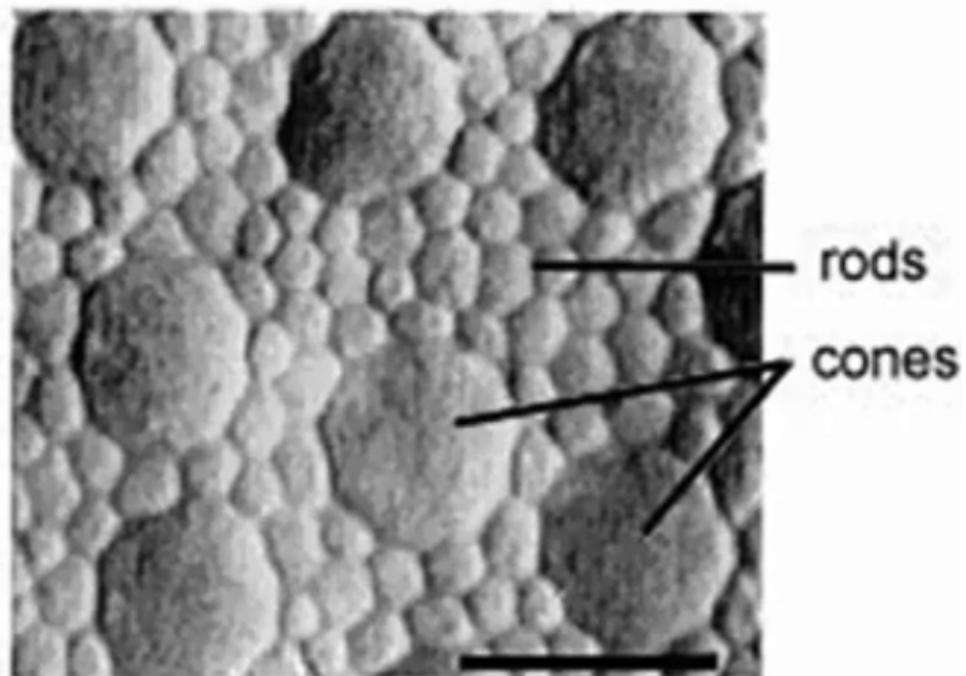


# 1 - Basics of Human Perception

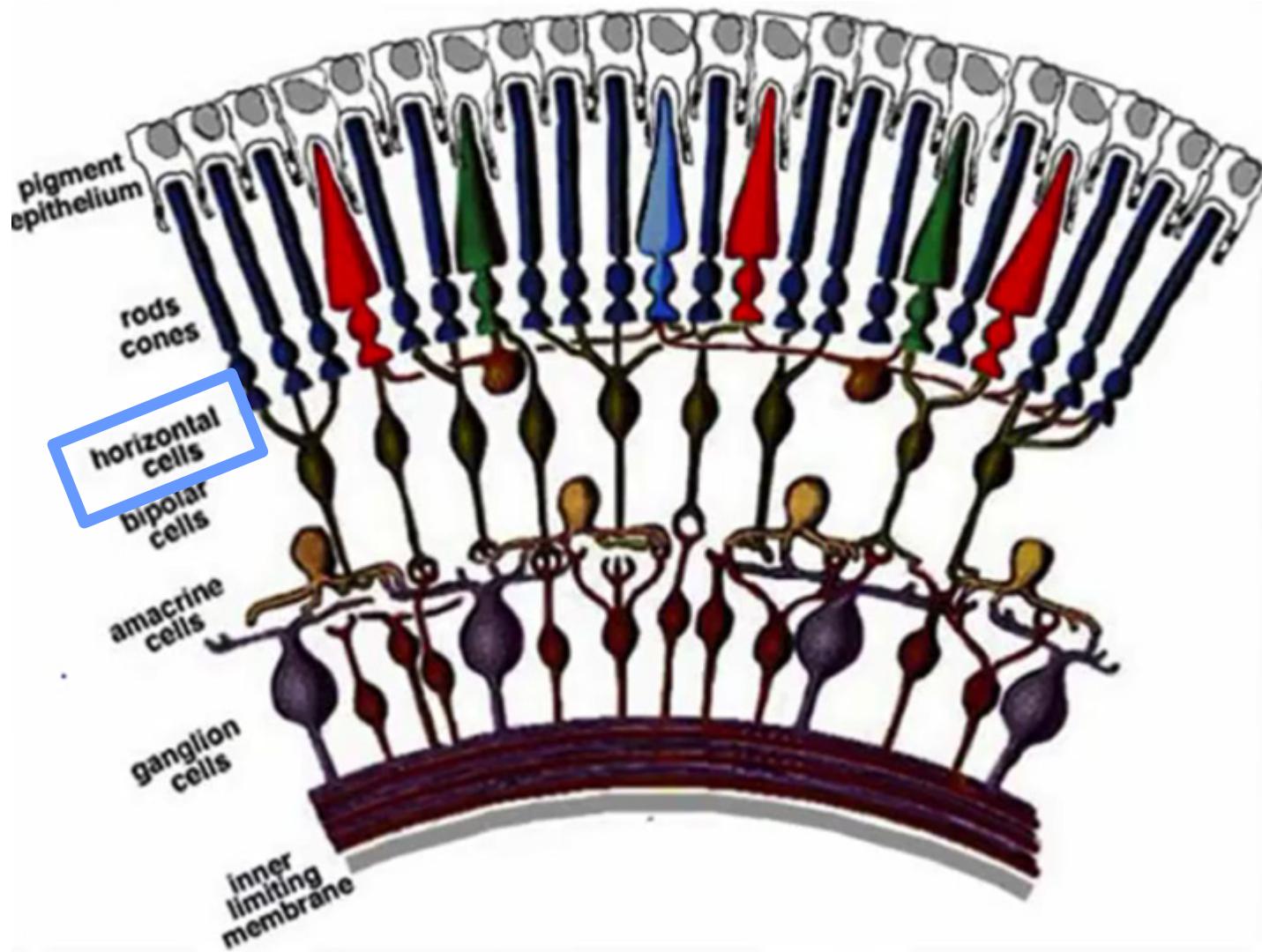
Fovea



Periphery



# 1 - Basics of Human Perception



# 1 - Basics of Human Perception

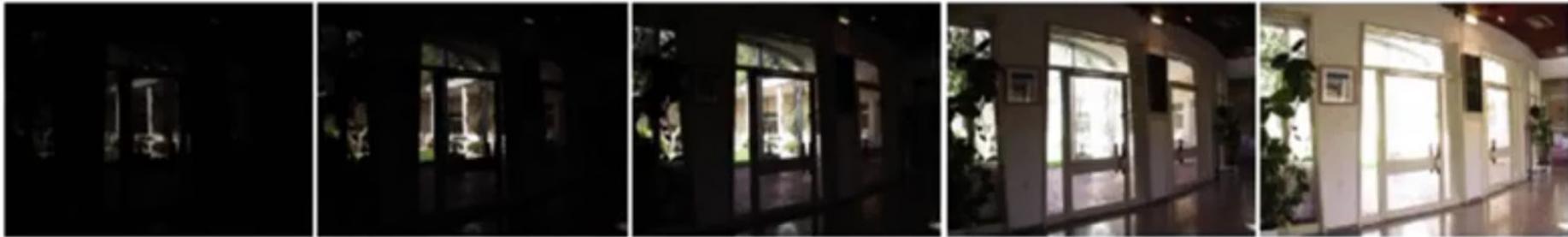
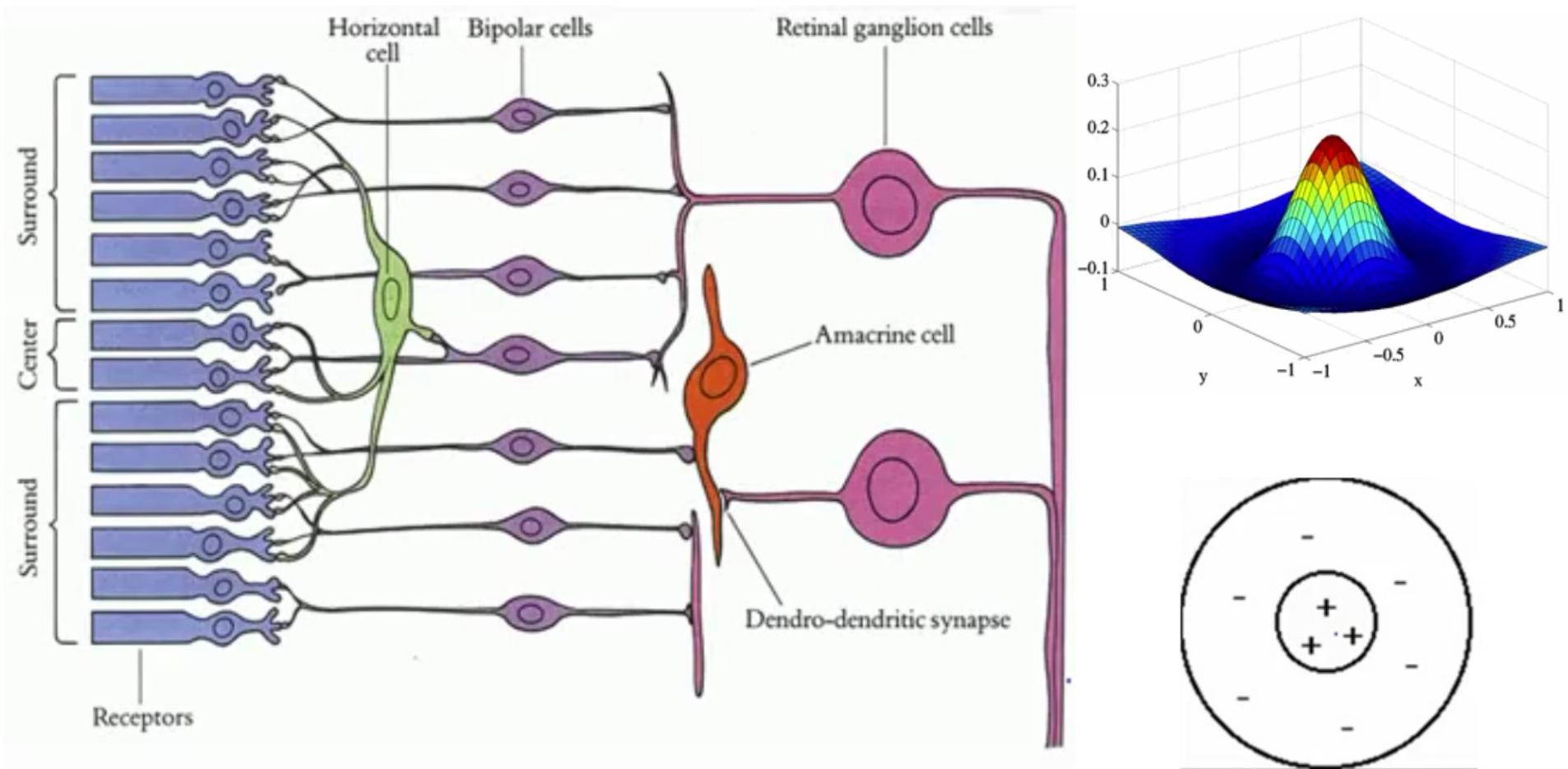


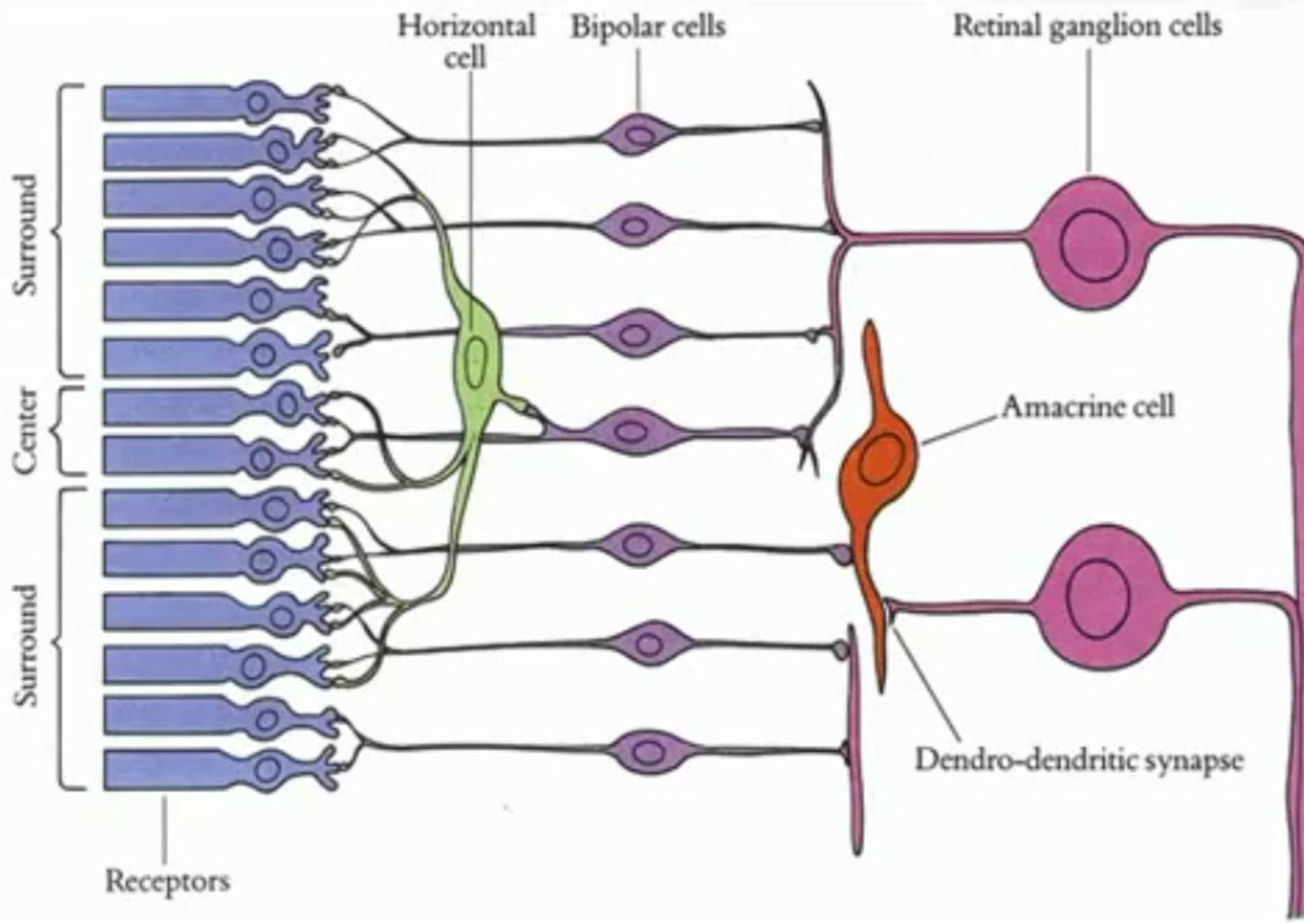
Figure 1: A series of five photographs. The exposure is increasing from left (1/1000 of a second) to right (1/4 of a second).



# 1 - Basics of Human Perception



# 1 - Basics of Human Perception



## 2 - Perception and Color. Measuring Color

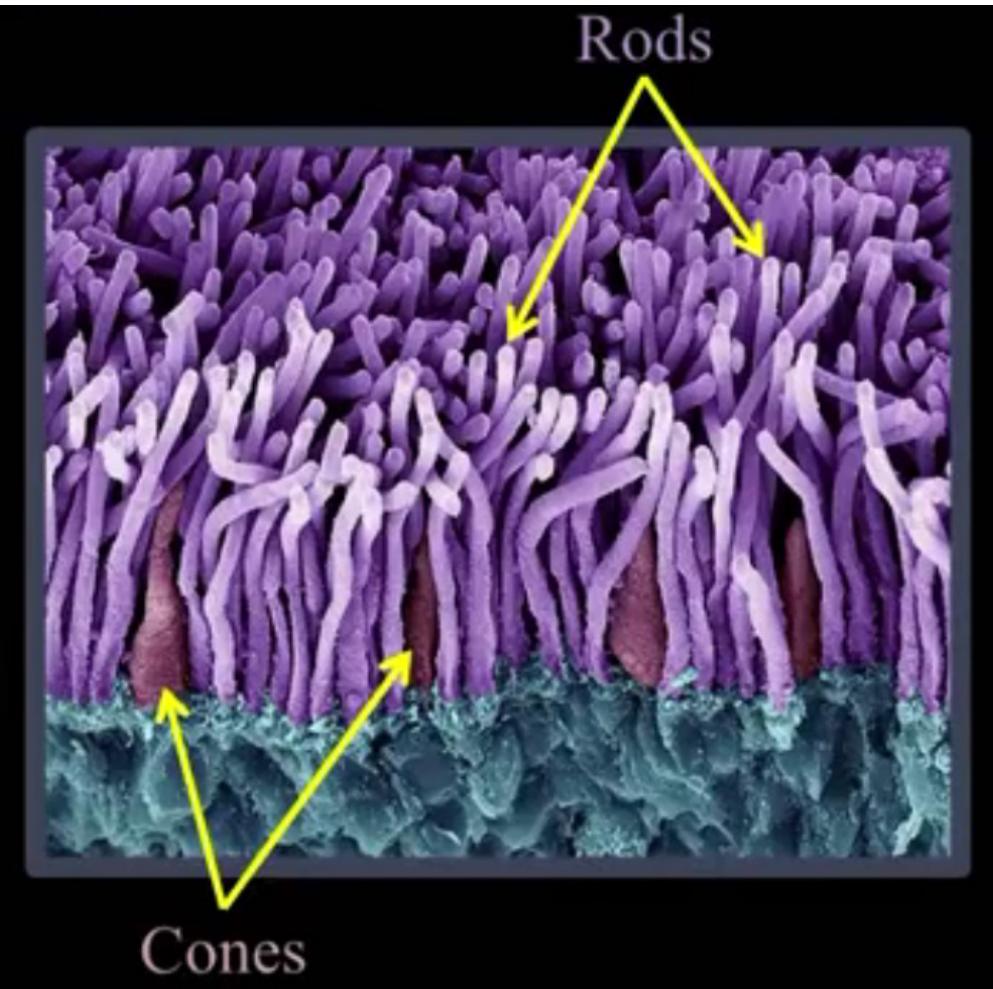
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### QUIZ!

Which photoreceptor is responsible for color discrimination?

Link: <https://goo.gl/forms/IPkIQSYPsFCu5JIU2>

## 2 - Perception and Color. Measuring Color



### Cones:

- 6-7 Million cones in the retina
- High-resolution (details) vision
- Packed into the fovea
- Color Discrimination
- Three types of cones:
  1. **Red Cones (64%)**
  2. **Green Cones (32%)**
  3. **Blue Cones (2%)**

### QUIZ!

Which photoreceptor is responsible for color discrimination?

Link: <https://goo.gl/forms/IPkIQSYPsFCu5JIU2>

## 2 - Perception and Color. Measuring Color

### How to measure color?

**Radiometric Approach:**

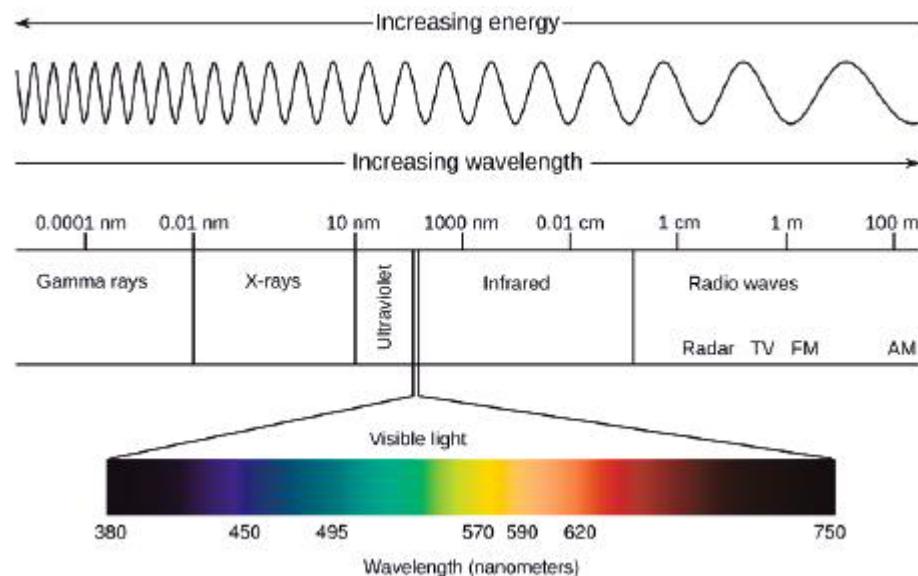
(independent of HVS)

**Irradiance**  $I(\lambda)$

**Reflectance**  $R(\lambda)$

**Radiance**  $E(\lambda)$

$$E(\lambda) = I(\lambda) \times R(\lambda)$$



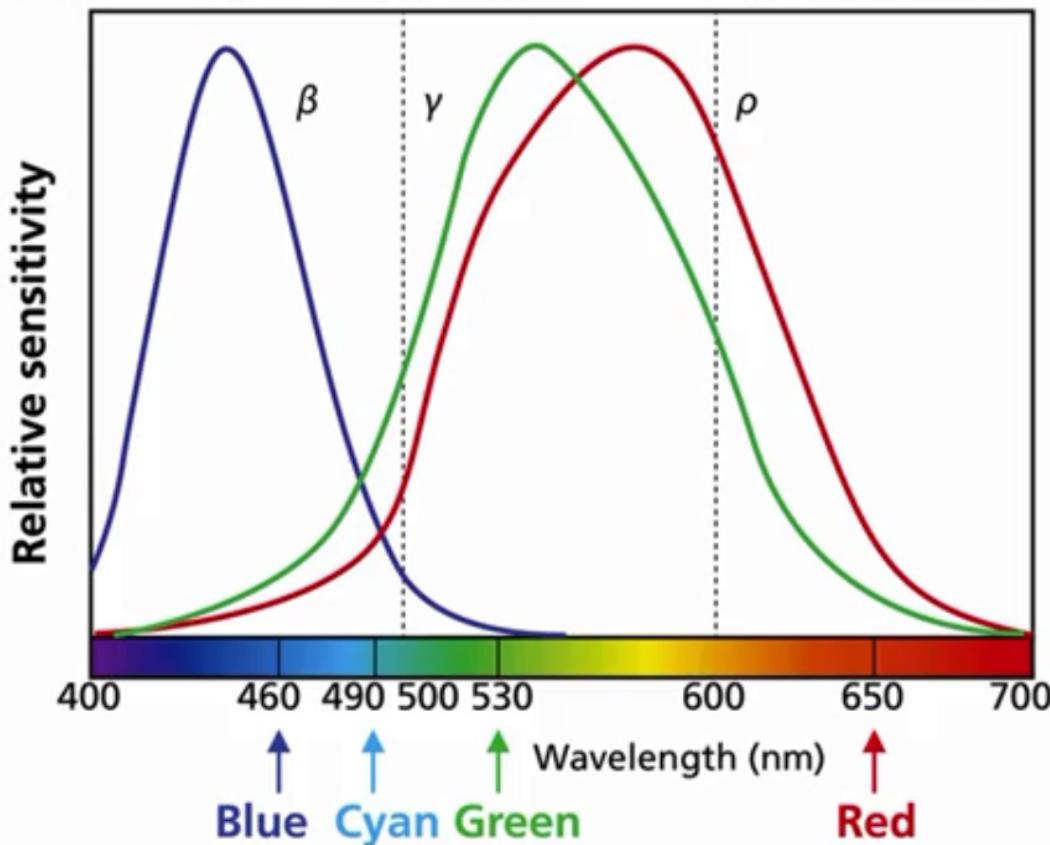
**Colorimetric Approach:**

(takes into account the HVS)

### Colorimetric Point of View

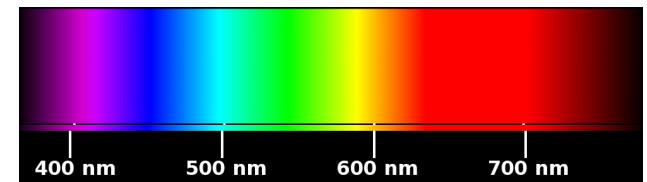
#### Human spectral sensitivity to color

Three cone types ( $\rho$ ,  $\gamma$ ,  $\beta$ ) correspond roughly to R, G, B.



Konig, XIX century

Use these three sensors  
to describe other colors?

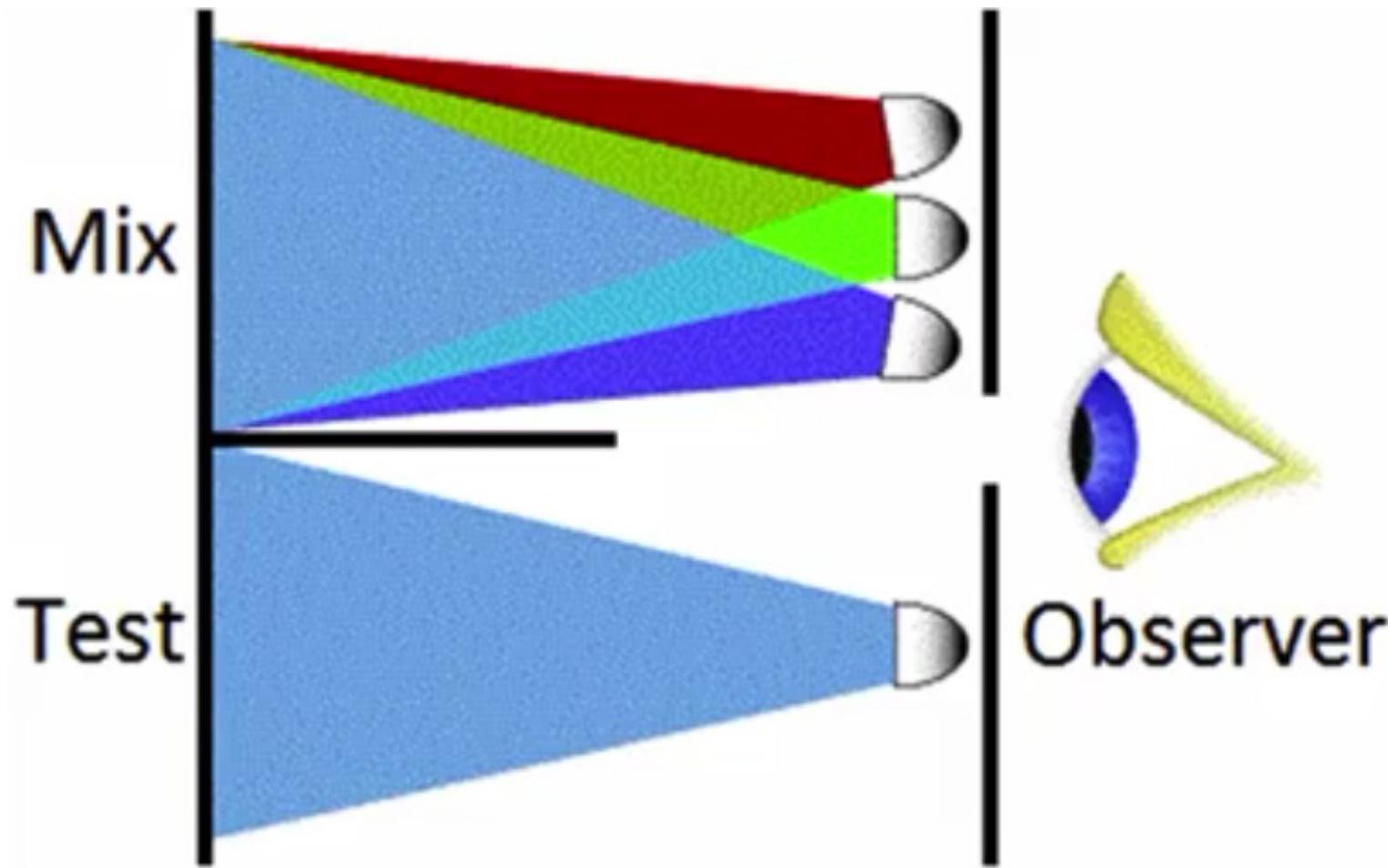


$$L = \int_{380}^{740} l(\lambda) \times E(\lambda) d\lambda$$

$$M = \int_{380}^{740} m(\lambda) \times E(\lambda) d\lambda$$

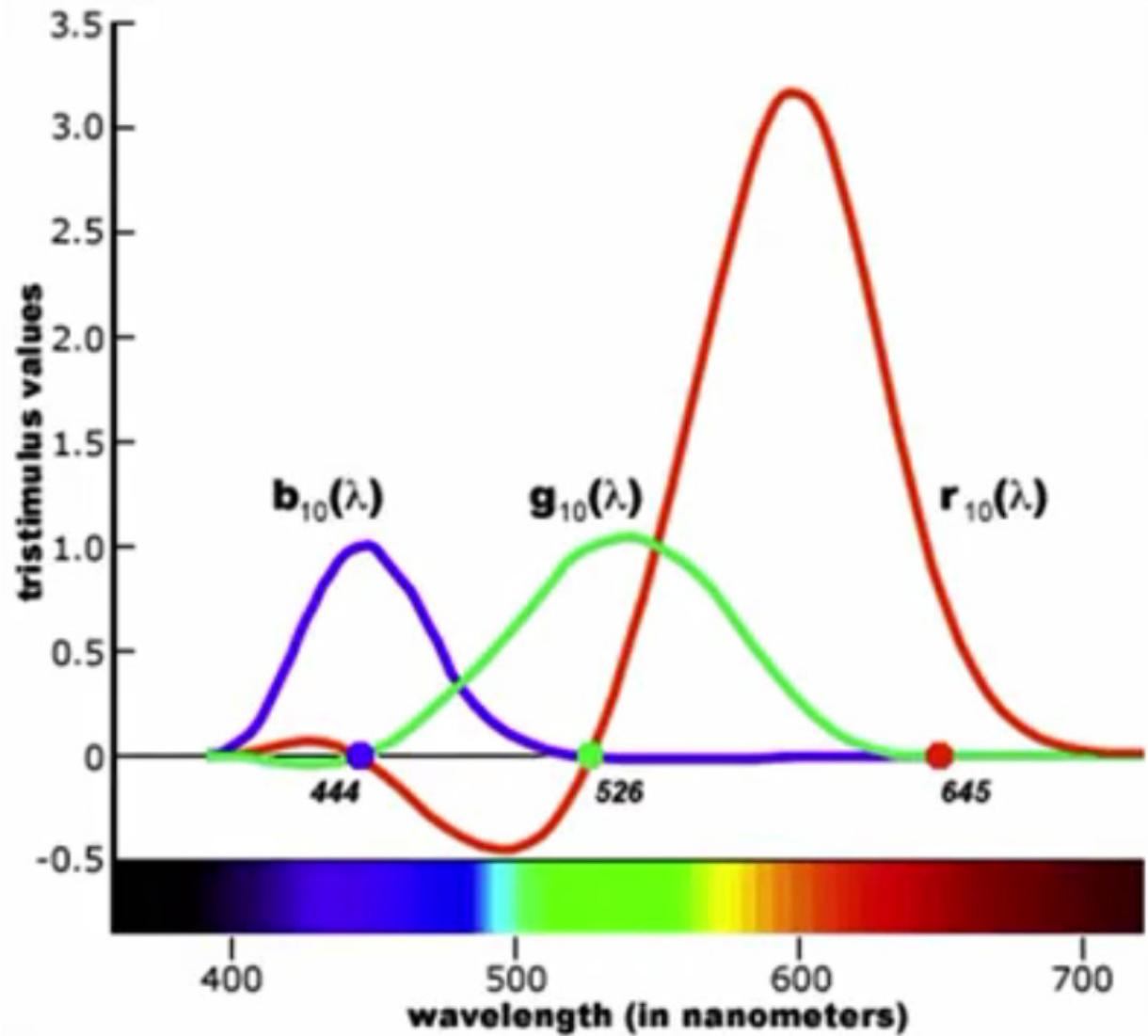
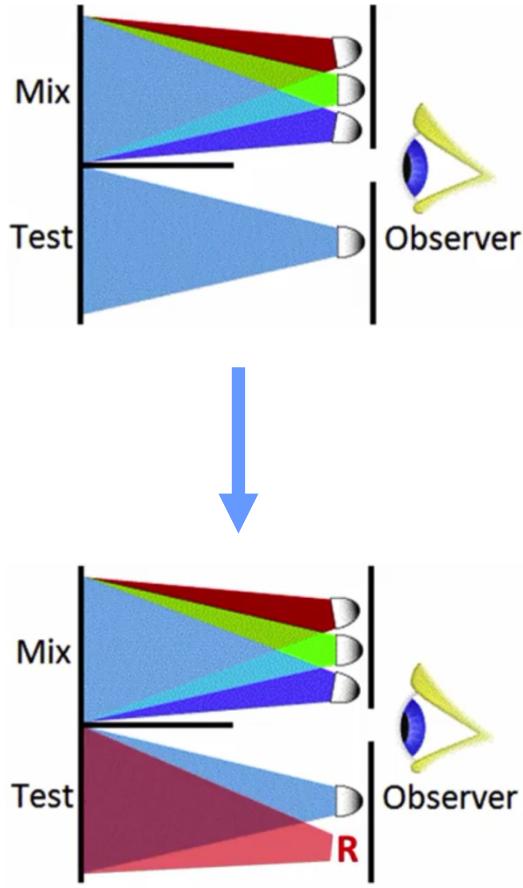
$$S = \int_{380}^{740} s(\lambda) \times E(\lambda) d\lambda$$

## 2 - Perception and Color. Measuring Color



Wright & Guild, 1920

## 2 - Perception and Color. Measuring Color



Wright & Guild, 1920

# 3 - Color Spaces. Perceptually Uniform Color Spaces

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# 3 - Color Spaces. Perceptually Uniform Color Spaces

## CIE RGB Color Space:

- CIE = Comission International de l'Eclairage
- CIE amalgamated Wright & Guilt results mapped wavelengths with perceived color.
- **Result:** CIE RGB color space.

$$R = \int_{380}^{740} r(\lambda) \times E(\lambda) \, d\lambda \quad G = \int_{380}^{740} g(\lambda) \times E(\lambda) \, d\lambda \quad B = \int_{380}^{740} b(\lambda) \times E(\lambda) \, d\lambda$$

## CIE XYZ Color Space:

- **Easy Computation:** Linear Transform of RGB
- **Decouples Color:** Y= Luminance, X,Z = Perceived Color
- Represents a **wide range** of colors

$$X = \int_{380}^{740} x(\lambda) \times E(\lambda) \, d\lambda \quad Y = \int_{380}^{740} y(\lambda) \times E(\lambda) \, d\lambda \quad Z = \int_{380}^{740} z(\lambda) \times E(\lambda) \, d\lambda$$

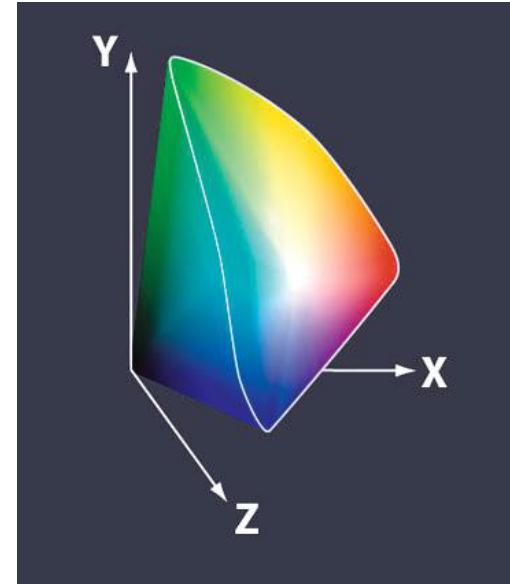
# 3 - Color Spaces. Perceptually Uniform Color Spaces

## Chromaticity Coordinates

$$x = \frac{X}{X+Y+Z}$$

$$y = \frac{Y}{X+Y+Z}$$

$$z = \frac{Z}{X+Y+Z}$$



### QUIZ!

Given two colors with CIEXYZ coordinates:

$$C_1 = (X_1, Y_1, Z_1) \quad C_2 = (2 \cdot X_1, 2 \cdot Y_1, 2 \cdot Z_1)$$

How are their chromaticity coordinates related?

<https://goo.gl/forms/dhVSV3IobbbiSyJM2>

### 3 - Color Spaces. Perceptually Uniform Color Spaces

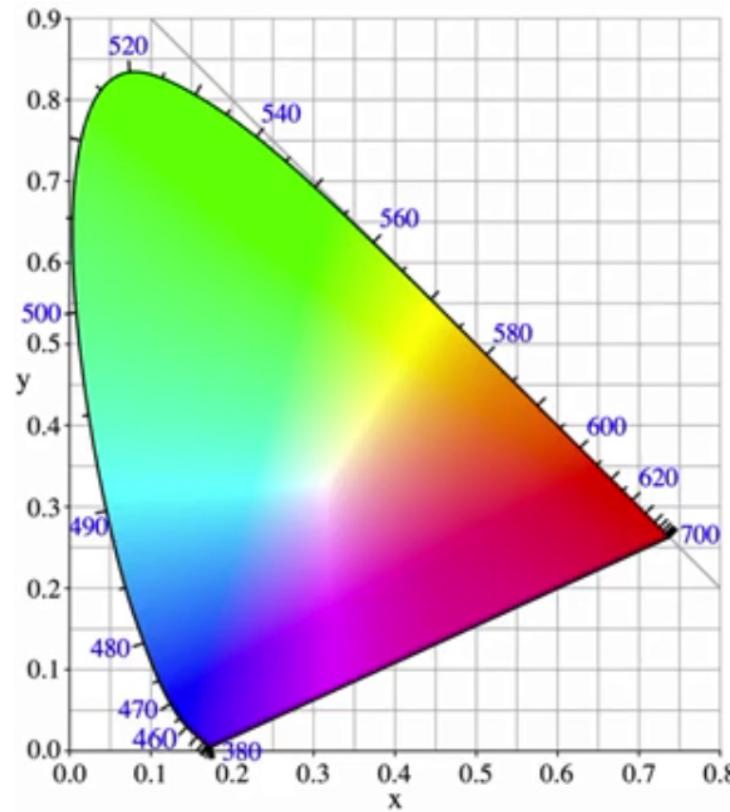
$$x = \frac{X}{X+Y+Z}$$

$$y = \frac{Y}{X+Y+Z}$$

$$z = \frac{Z}{X+Y+Z}$$

#### Chromaticity Diagram

$$x + y + z = 1 \quad \rightarrow \quad z = 1 - (x + y)$$



# 3 - Color Spaces. Perceptually Uniform Color Spaces

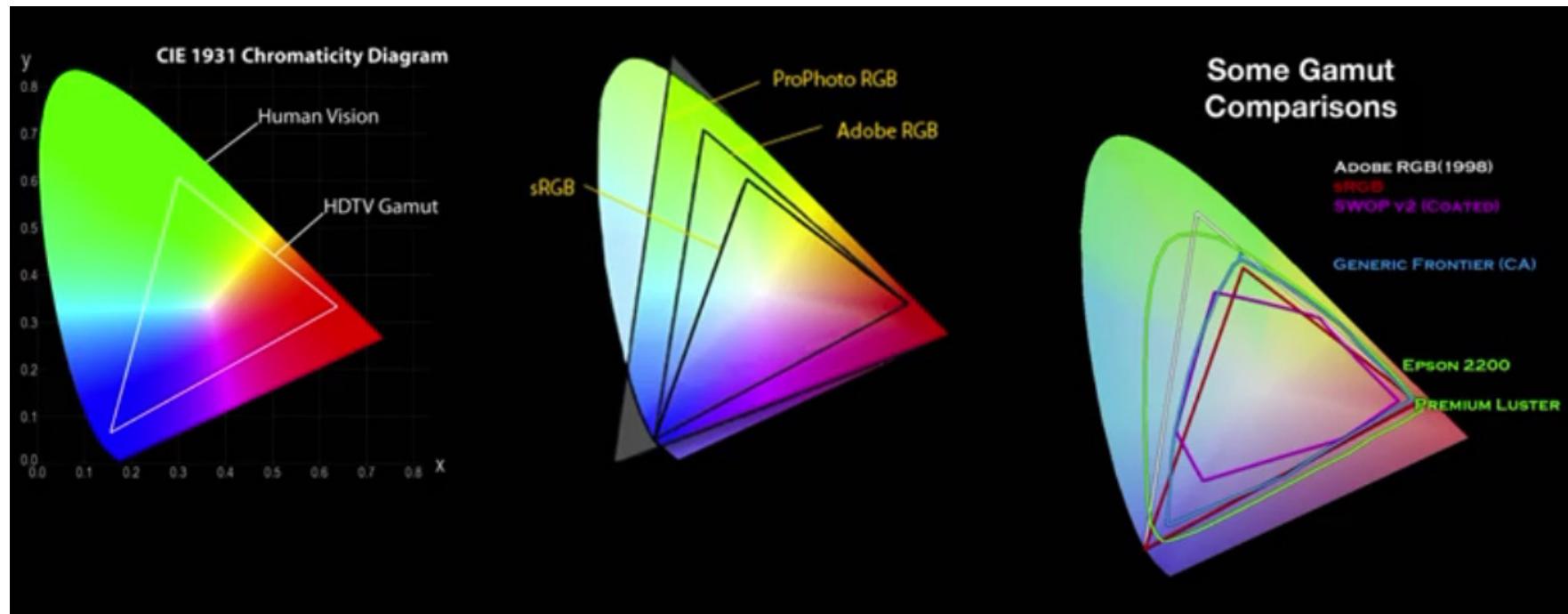
$$x = \frac{X}{X+Y+Z}$$

$$y = \frac{Y}{X+Y+Z}$$

$$z = \frac{Z}{X+Y+Z}$$

## Chromaticity Diagram

$$x + y + z = 1 \quad \rightarrow \quad z = 1 - (x + y)$$



# 1 - Basics of Human Perception

## Limitations of CIExyz – Perceptually Uniform Color Spaces

- Distance between two points in XYZ space or in the xy diagram is **not proportional** to the perceived difference between the colors corresponding to the points.
- A mixture of two lights in equal proportions will have chromaticity coordinates that **do not lie exactly at the middle** of the segment joining the chromaticities of the original two lights

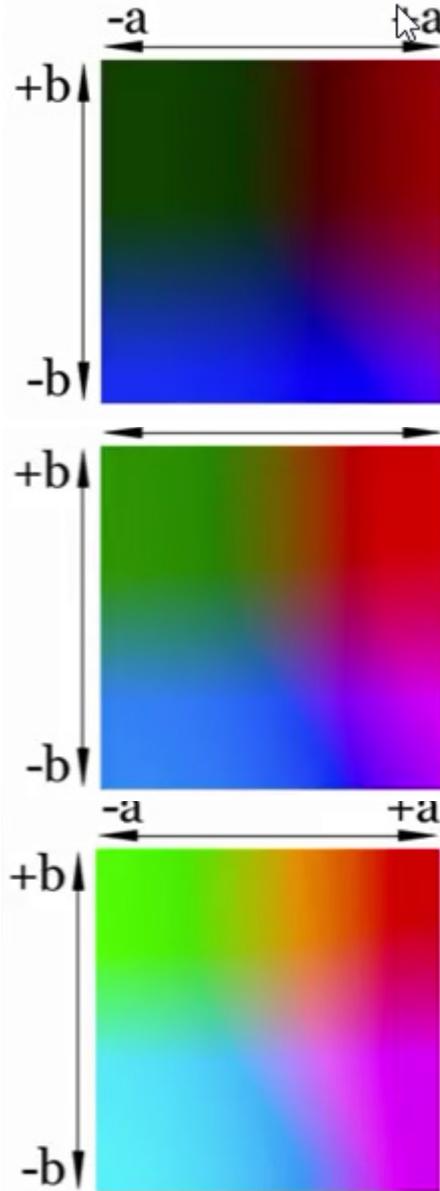
**But we want Perceptual Uniformity!**

In 1976, CIE introduced the **Lab color space**. Euclidean distance between two points in CIELAB space becomes proportional to the perceptual difference between the colors corresponding to those points.

You go from CIExyz to Lab through a complex non-linear transformation.

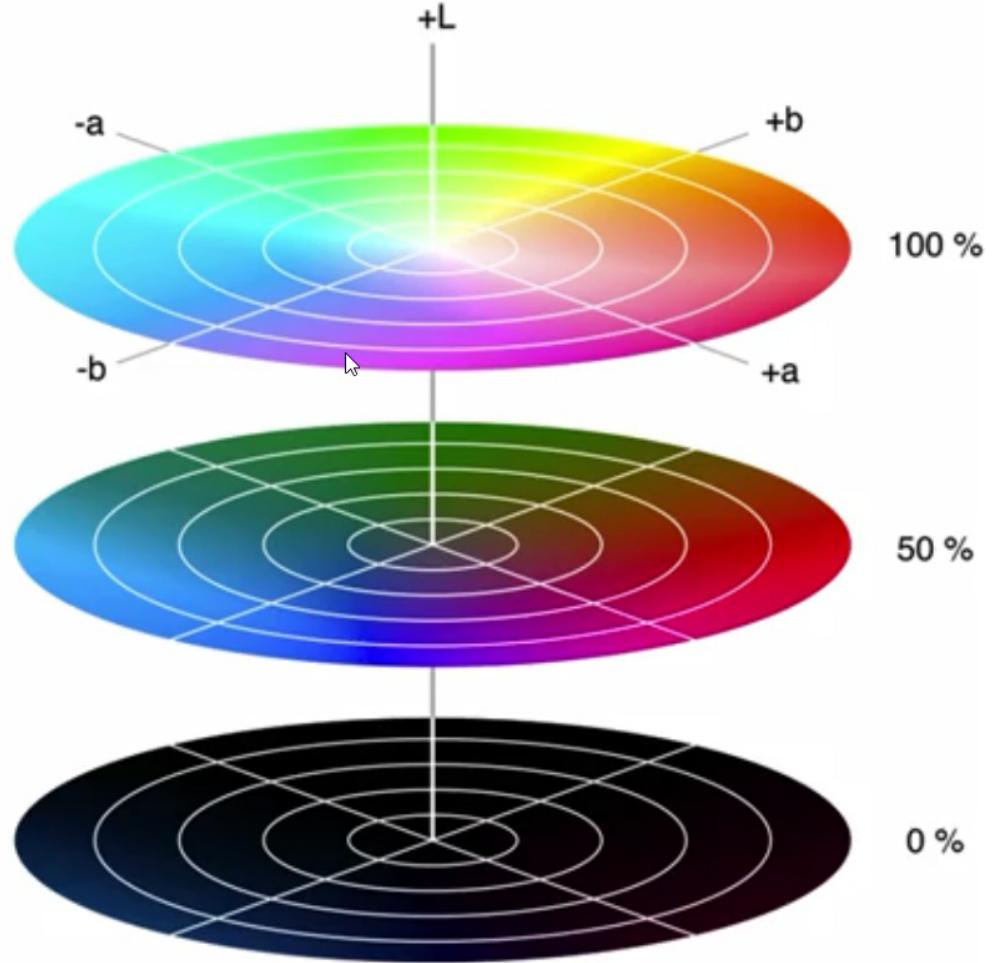
In CIELAB the chromaticity coordinates ( $a$ ,  $b$ ) can be positive or negative:  $a > 0$  indicates redness,  $a < 0$  greenness,  $b > 0$  yellowness and  $b < 0$  blueness.

### 3 - Color Spaces. Perceptually Uniform Color Spaces



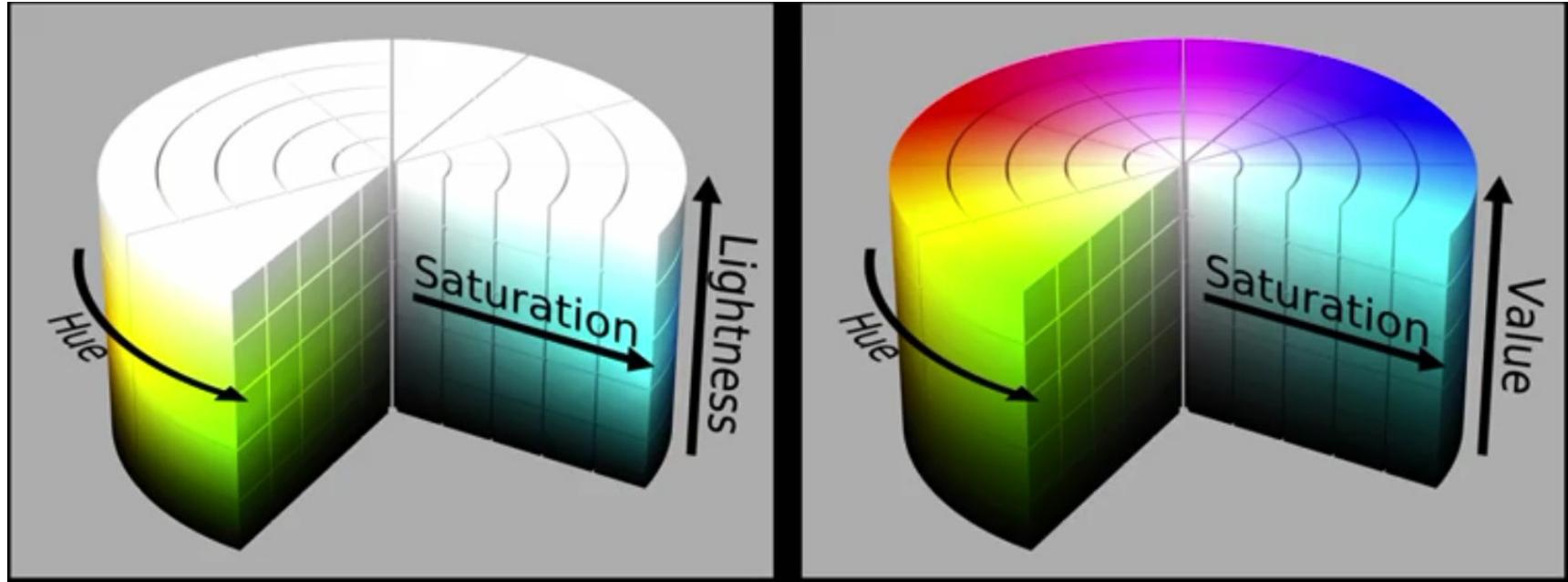
L increases

CIELAB COLOR SPACE



# 3 - Color Spaces. Perceptually Uniform Color Spaces

## OTHER COLOR SPACES: HS\*



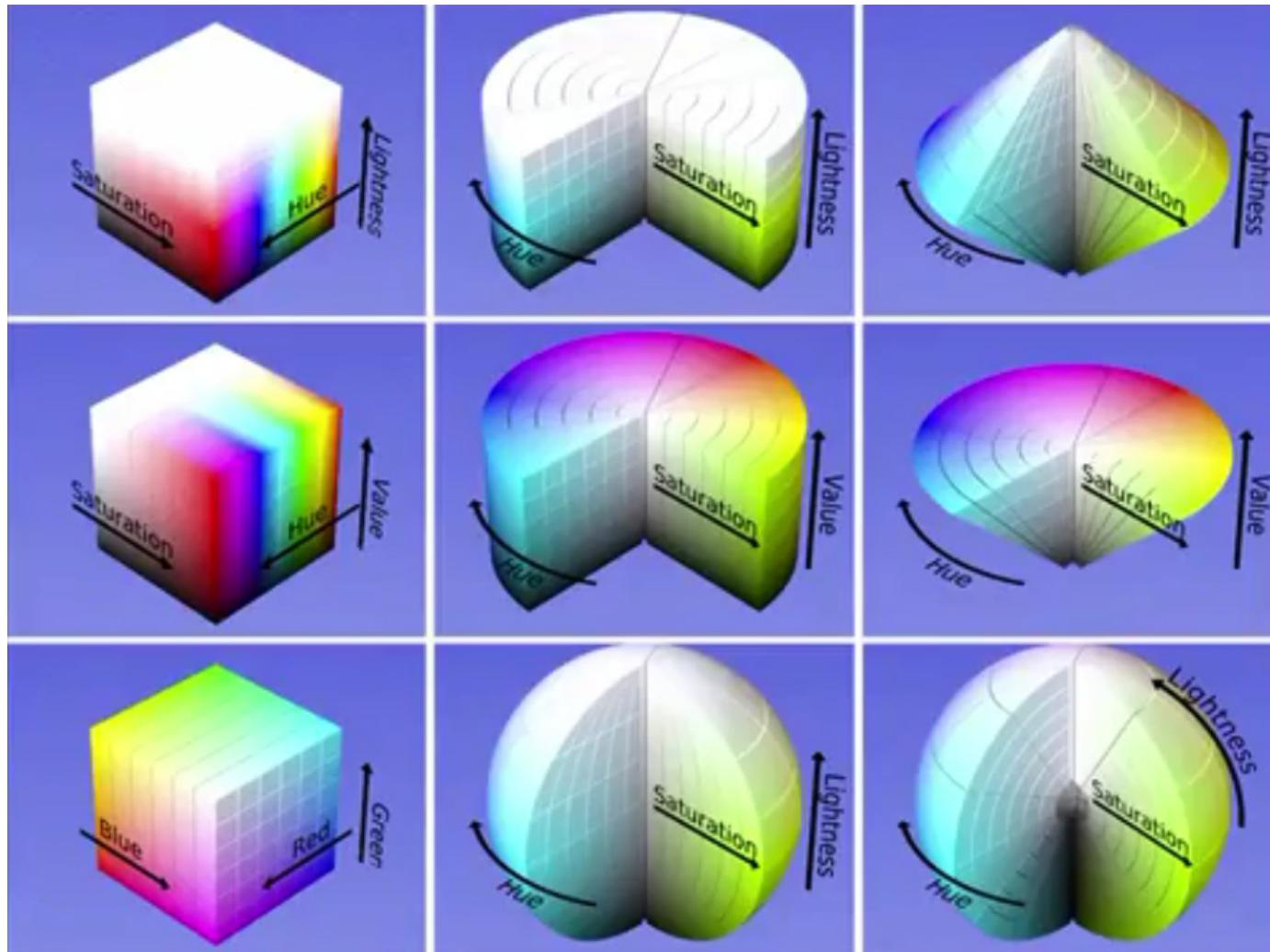
### QUIZ!

How would you expect a color with HSV coordinates  $(h,s,v)$  to change if we multiply  $h$  by 2?

Link: <https://goo.gl/forms/6Ny9LfxONAf8CCPq2>

# 3 - Color Spaces. Perceptually Uniform Color Spaces

## EXTENSIONS



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### From pixels to superpixels



### From pixels to superpixels



### From pixels to superpixels



### From pixels to superpixels

Clear your mind for a moment, and consider how we represent images.

Why pixels? Why square unitary regions within a rectangular grid?

It is a **limitation** of our HW/SW, but it does not come from the HVS.

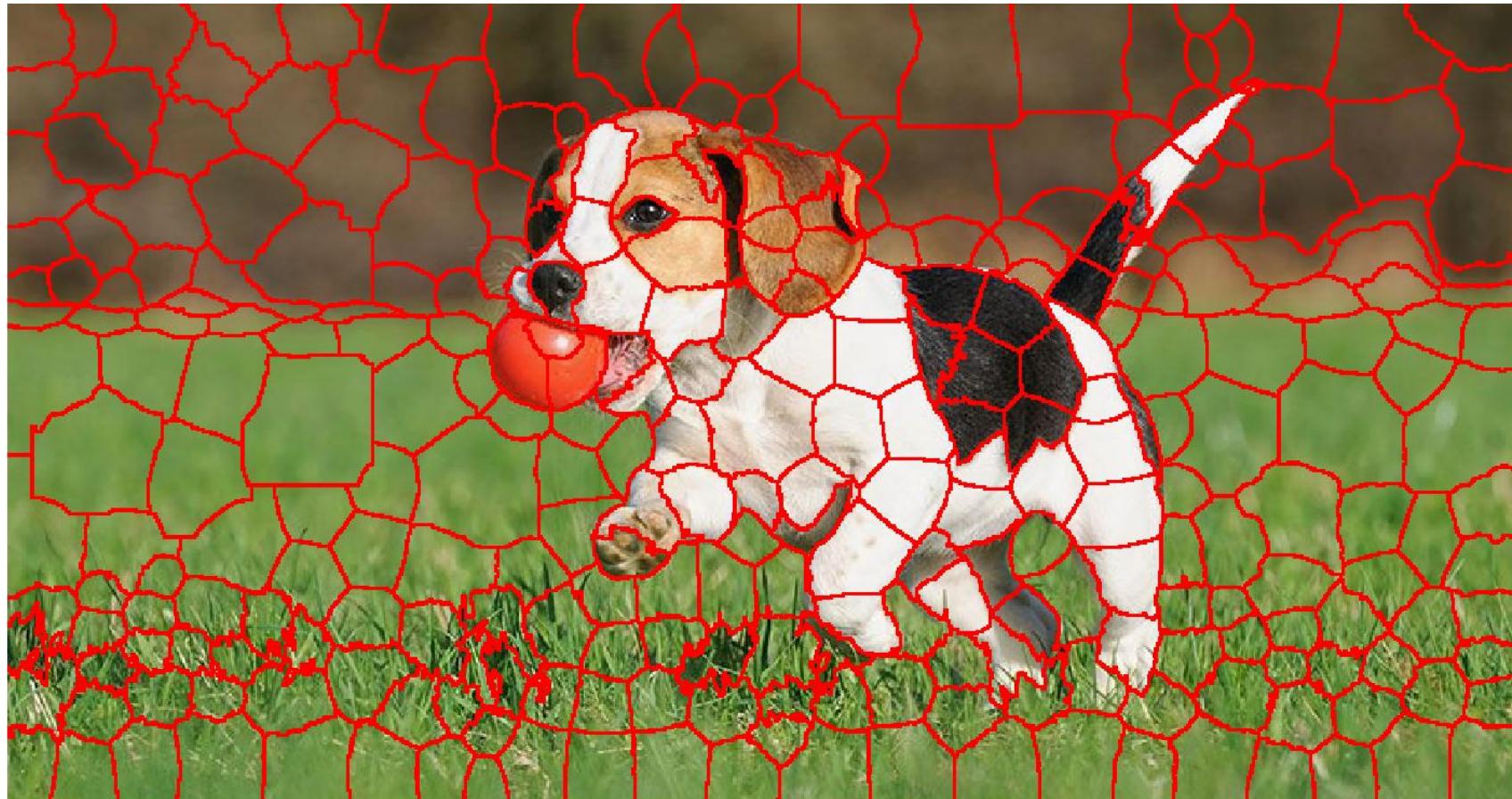
Pixels do not carry any kind of semantic information with them.

**Superpixels** are methods for locally grouping pixels such that the resulting super-atomic representations contain perceptually meaningful information.

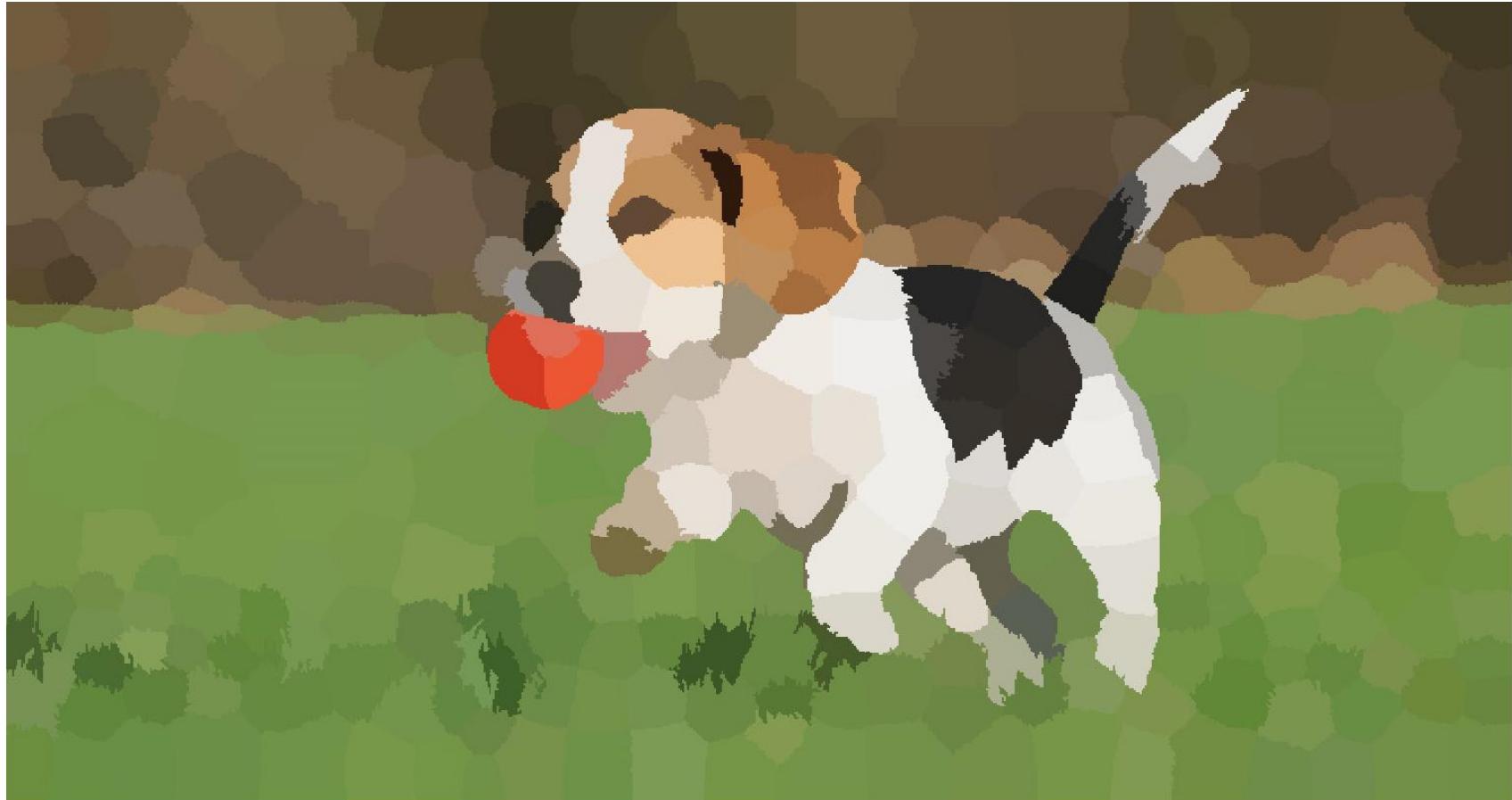
**Superpixels** capture image redundancy, provide a convenient primitive from which to compute image features, and reduce the complexity of subsequent image processing tasks.

There are many approaches to generating superpixels. You have already studied some of them! mean shift, quick shift, watershed.

### From pixels to superpixels



### From pixels to superpixels



## SLIC superpixels

SLIC stands for Simple Linear Iterative Clustering, quite a descriptive name!

**Simple** to use: only one parameter  
(number of wanted superpixels)

**Perceptually meaningful**: it clusters pixels in the xy-Lab color space

**Memory-efficient**: The complexity of SLIC is linear in the number of pixels in the image,  $O(n)$

**Let's see the algorithm:**

$$d_c = \sqrt{(l_j - l_i)^2 + (a_j - a_i)^2 + (b_j - b_i)^2}$$

$$d_s = \sqrt{(x_j - x_i)^2 + (y_j - y_i)^2},$$

$$D' = \sqrt{\left(\frac{d_c}{N_c}\right)^2 + \left(\frac{d_s}{N_s}\right)^2}.$$

```

Algorithm 1. SLIC superpixel segmentation
/* Initialization */
Initialize cluster centers  $C_k = [l_k, a_k, b_k, x_k, y_k]^T$  by sampling
pixels at regular grid steps  $S$ .
Move cluster centers to the lowest gradient position in a  $3 \times 3$ 
neighborhood.
Set label  $l(i) = -1$  for each pixel  $i$ .
Set distance  $d(i) = \infty$  for each pixel  $i$ .

repeat
/* Assignment */
for each cluster center  $C_k$  do
    for each pixel  $i$  in a  $2S \times 2S$  region around  $C_k$  do
        Compute the distance  $D$  between  $C_k$  and  $i$ .
        if  $D < d(i)$  then
            set  $d(i) = D$ 
            set  $l(i) = k$ 
        end if
    end for
end for
/* Update */
Compute new cluster centers.
Compute residual error  $E$ .
until  $E \leq$  threshold

```

# 5 - Introduction to Color Constancy and Retinex

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# 5 - Introduction to Color Constancy and Retinex

## Color Constancy

When we light a surface of reflectance  $R(\lambda)$  with an illuminant of spectrum  $I(\lambda)$ , we receive a radiance  $E(\lambda)$ . However, we can usually tell apart colors regardless of the color of the illuminant. This ability is **Color Constancy**.

[Link](#)

### Land's Experiments



### Reminder

**Irradiance**  $I(\lambda)$

**Reflectance**  $R(\lambda)$

**Radiance**  $E(\lambda)$

$$E(\lambda) = I(\lambda) \times R(\lambda)$$

# 6 - Introduction to Computational Image Processing

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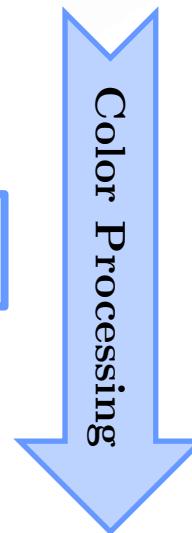
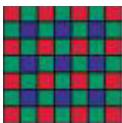
# 6 - Introduction to Computational Image Processing



3D World Scene



Demosaicking



Aperture

Exposure

Focus

White Balance

Display on Device



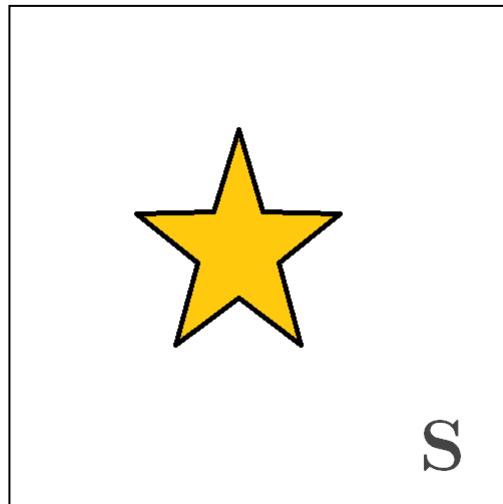
2D Representation

# Application: A first example - Image Composition

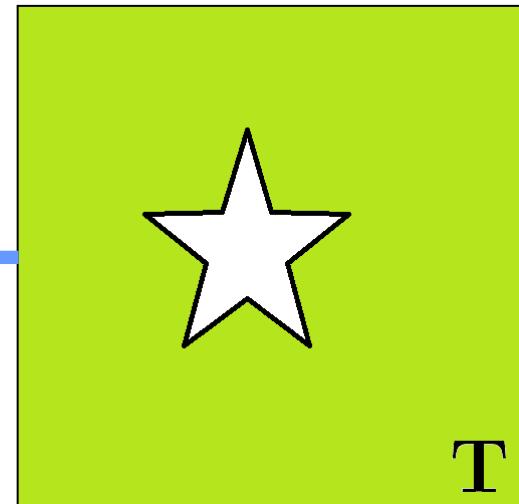
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### Image Composition

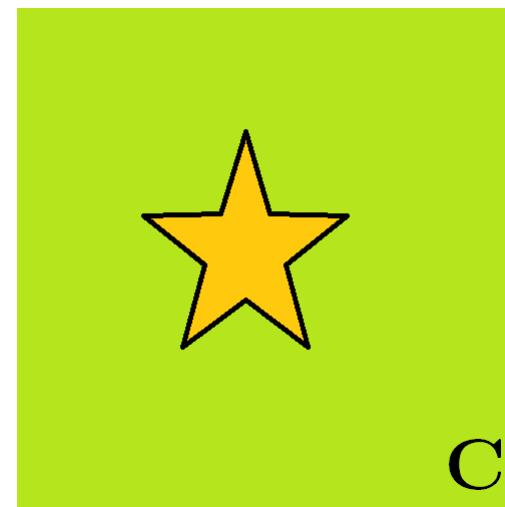
Source Image S



Target Image T



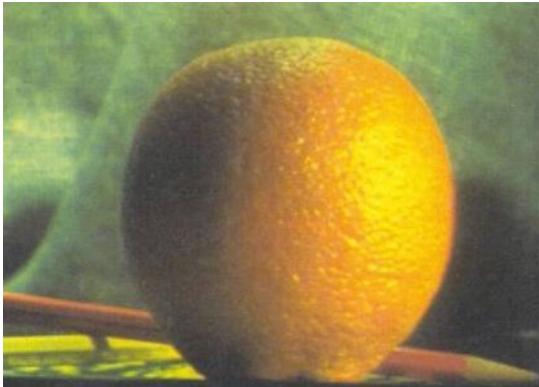
Blending



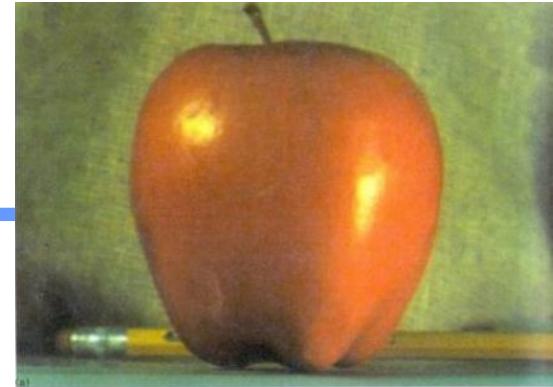
## Application: A first example - Image Composition

### Image Composition

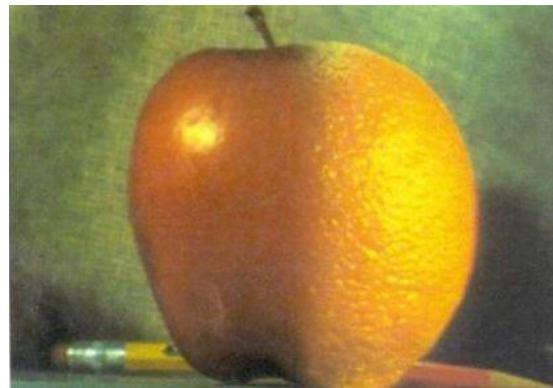
Source Image S



Target Image T



Blending



The Orangapple!

### Image Composition

- **Naive Approach:** Given a binary mask  $\mathbf{M}$ , compute  $\mathbf{C} = \mathbf{M} \cdot \mathbf{S} + (1-\mathbf{M}) \cdot \mathbf{T}$

This gives bad results, since the seam between  $\mathbf{S}$  and  $\mathbf{T}$  will be visible

How to “**hide**” that seam?

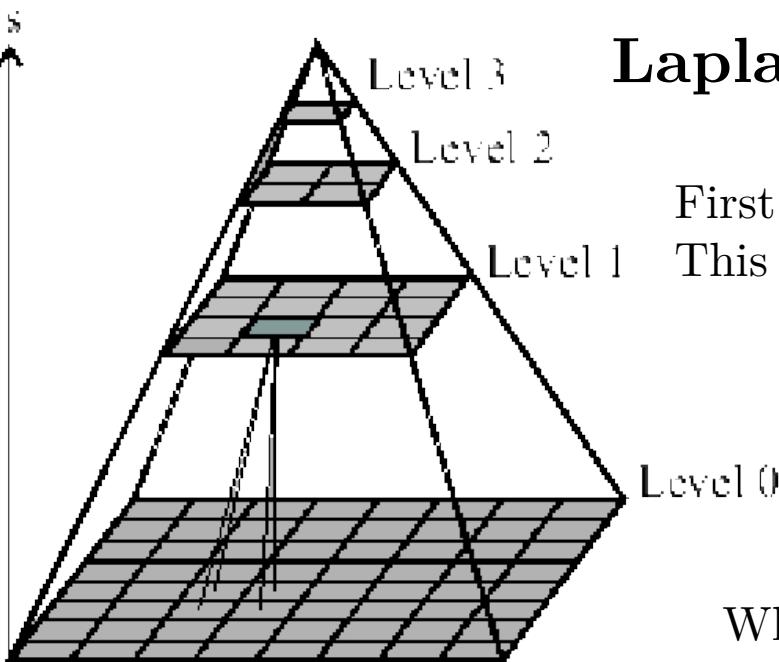
- **2nd Naive Approach:** Given a binary mask  $\mathbf{M}$ , blur its edges and then blend:

$$\mathbf{C} = \mathbf{G}_\sigma * M \cdot \mathbf{S} + (1 - \mathbf{G}_\sigma * M) \cdot \mathbf{T}$$

- **Better Approach:** Multi-resolution blending with **Laplacian Pyramids**

Merge different frequencies separately

# Application: A first example - Image Composition



## Laplacian Pyramids

First, imagine you want to build a **Gaussian pyramid**. This is a hierarchy of images. Given a kernel  $K_\sigma$ ,

$$G_0 = \text{Image at original resolution}$$
$$G_i = (K_\sigma * G_{i-1}) \searrow 2$$

Which is basically a series of blurrier, smaller images

Now you want to find relevant edges at different scales.

Look at the DoG (Difference of Gaussians = Laplacian) at each scale.

Which means you need to build the **Laplacian Pyramid**:

$$L_i = G_i - K_\sigma * G_i$$

### Laplacian Pyramids

**Reconstruction :** From the Laplacian decomposition, you can come back to the original image by upsampling and adding back edges iteratively to the smallest image:

$$I = \sum_{i=1}^N L_i \nearrow^2, \quad L_N = G_N \quad (1)$$

### Laplacian Image Blending

We compute a Gaussian Pyramid for the target and the source,  $L_i^T, L_i^S, i = 1, \dots, N$

We compute a Gaussian Pyramid for the mask,  $G_i^M$

We compute a Laplacian Pyramid for the composite image,

$$L_i^T = G_i^M \cdot L_i^S + (1 - G_i^M) \cdot L_i^T, \quad i = 1, \dots, N$$

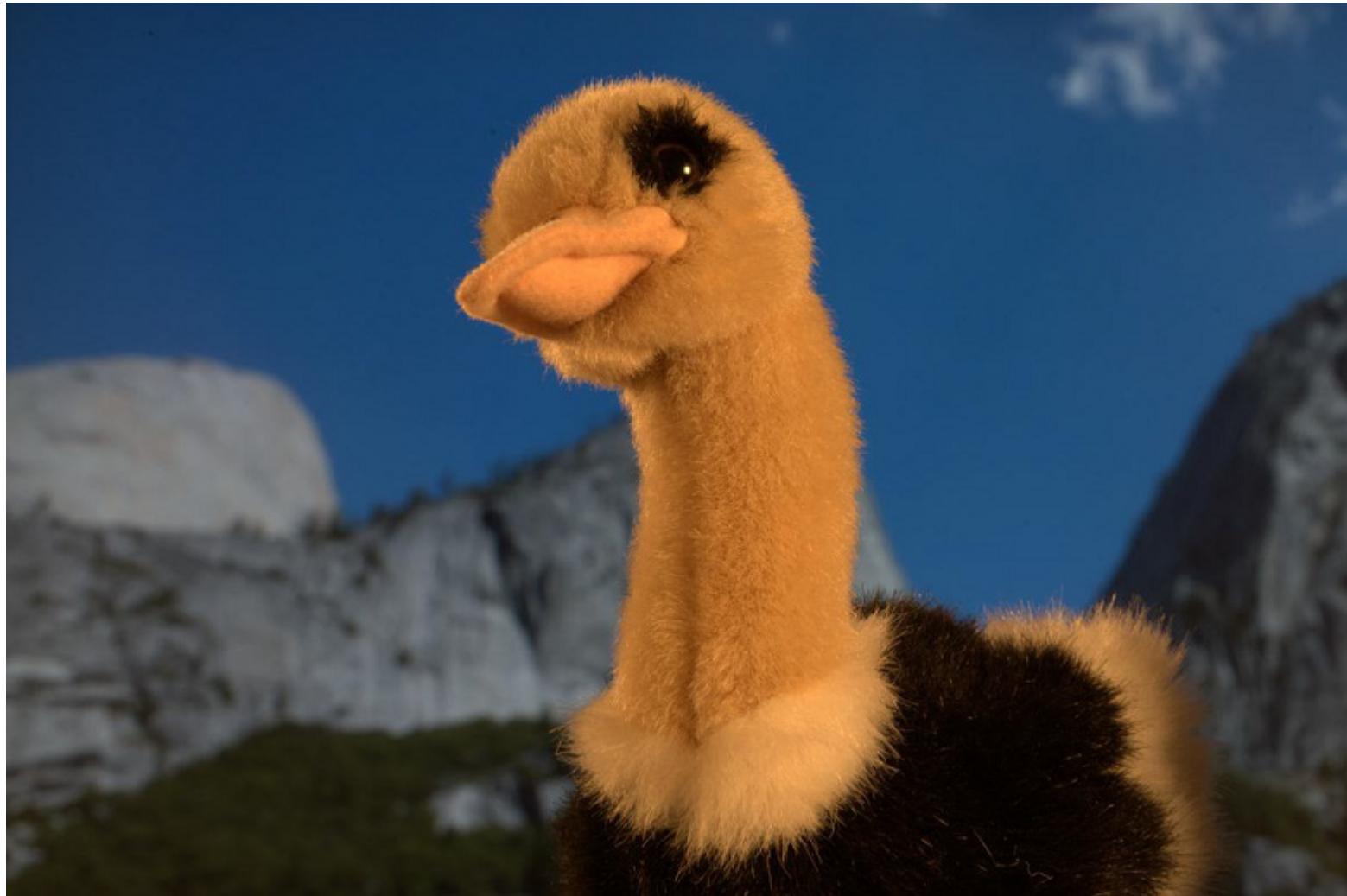
Apply the reconstruction formula (1) to the composite Laplacian Pyramid

## Image Matting



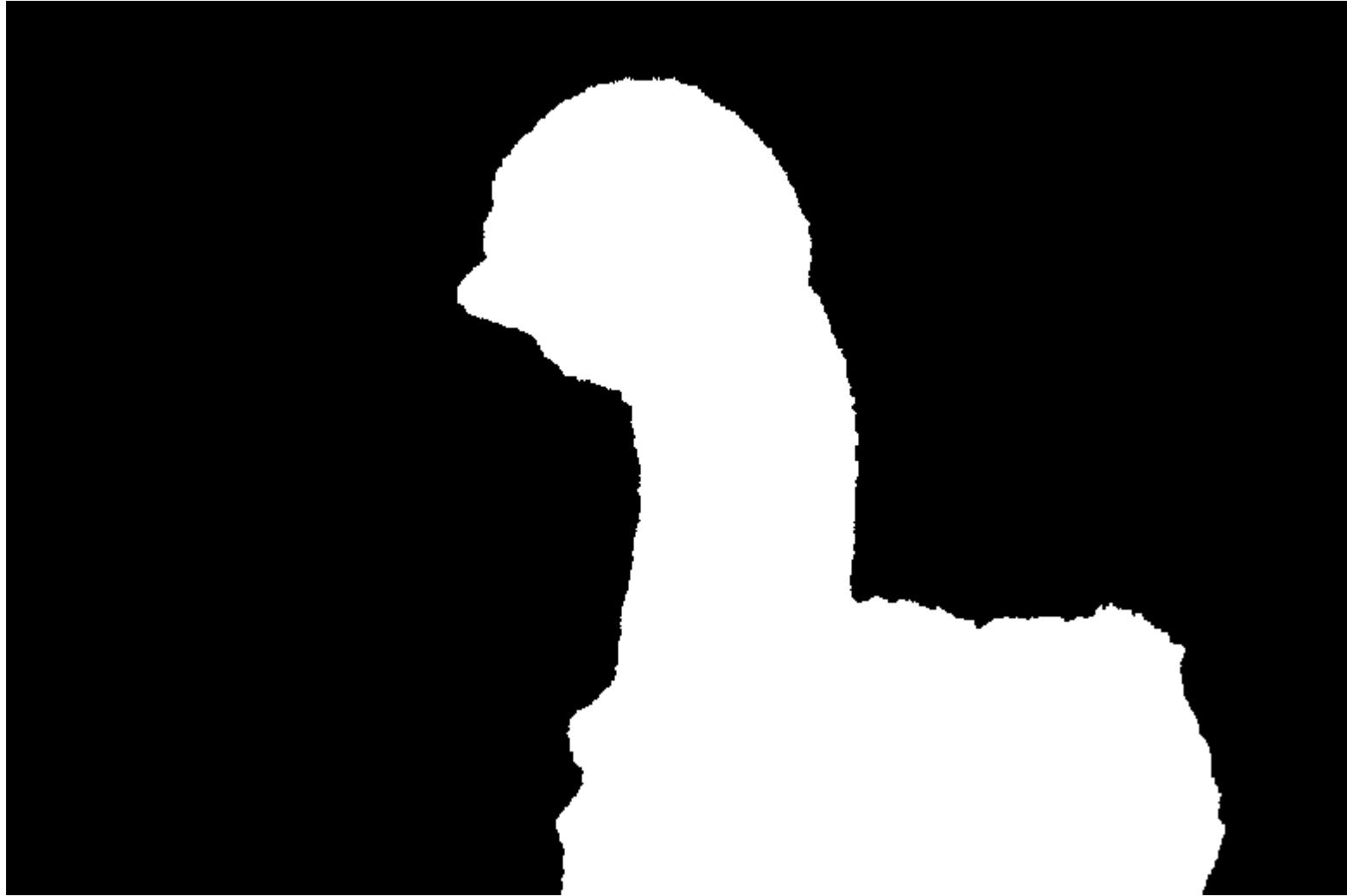
## Application: A first example - Image Composition

### Image Matting



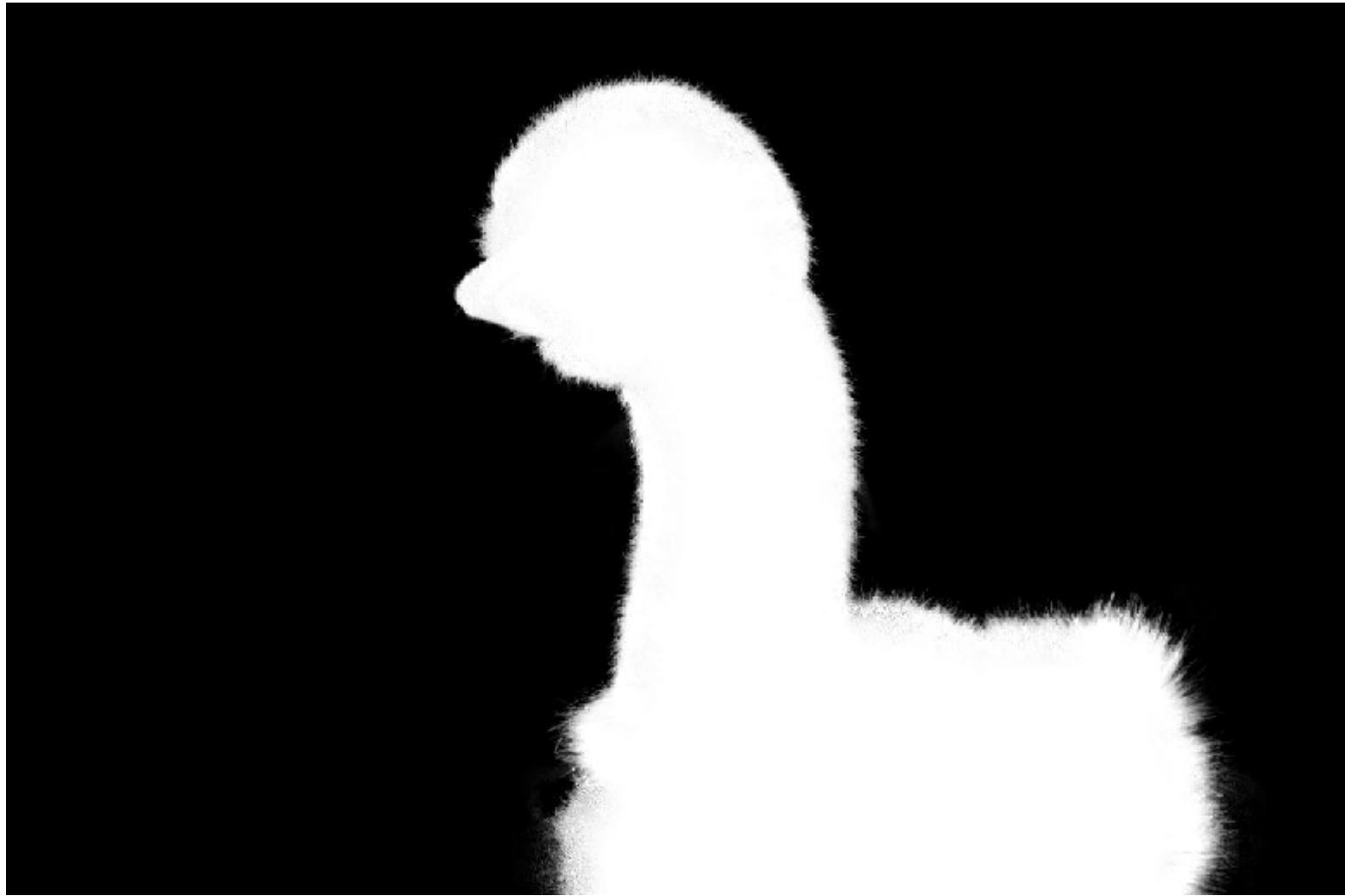
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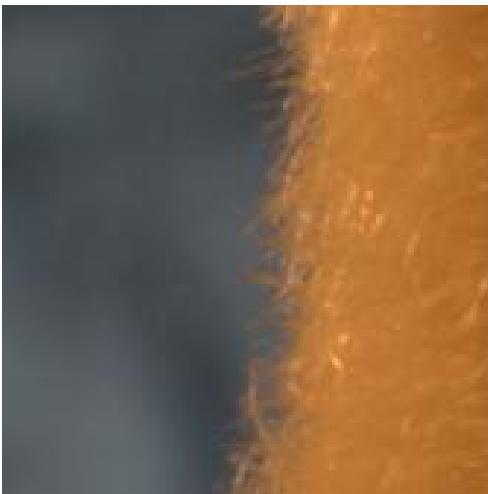
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