Introduction to Neural Netwroks (CPE 520) HW#13: Dec. 14, 2021

Q.1: Find the expression for the Inverse for the following linear matrix equations (systems):

(a):
$$\mathbf{y}_{n \times 1} = \mathbf{A}_{n \times m} \mathbf{x}_{m \times 1}$$
 where $n < m$ and rank=n

(b):
$$\mathbf{y}_{n \times 1} = \mathbf{A}_{n \times m} \mathbf{x}_{m \times 1}$$
 where $n > m$ and rank=m

Q.2: (a) What is the difference between Ridge and LASSO regressions?

(b) Write the expressions for them.

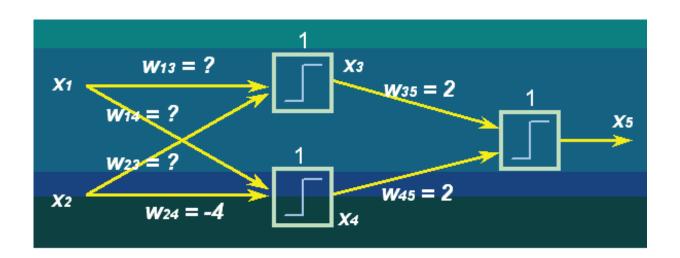
Q.3: Convolve the following kernels:

$$\begin{bmatrix} 1 \\ 2 \\ 2 \\ 1 \end{bmatrix} * 1 1 1$$

Q.4: A number of DNN architectures use 1x1 convolution, what does it mean and what is its purpose?

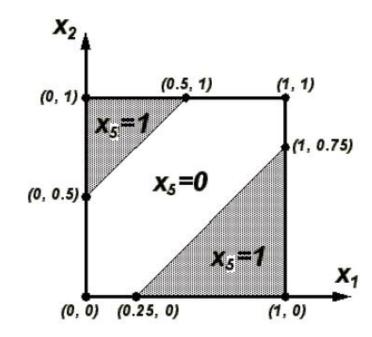
- Q.5: What is the difference between learning update term and Momentum term in DNN.
- Q.6: Why we need to do regularization on weights in DNN?
- Q.7: Give examples of different pooling methods used in DNN.
- Q.8: What is Global Pooling.
- Q.9: What is the difference between logistic regression and Softmax?
- Q.10: Write the **hinge loss** expression and in which classifier it is usually used.
- Q.11: The common regularization in machine learning are based on L2 or L1 norm on the weights, write the expressions for these two norms.
- Q.12: In DNN we use auto-encoders, what are the usefulness & applications of developing autoencoders?
- Q13: Describe the Kohonen Feature Maps.
- Q.14: Describe how learning vector quantization works.
- Q.15: Give two examples of unsupervised deep neural network architectures.

Q.16: An 2-2-1 MLP has the following configuration:



Suppose that the above MLP has the following decision boundary for XOR problem:

Find the missing weights of the MLP.



Q.17: Consider sigmoid function $f(NET_i)$:

Find its gradient.

$$f(NET_j) = \frac{1}{1 + e^{-\lambda NET_j}}$$

Q.18: What is kernel function? What is the kernel trick?

Q.19: Given 2-dimensional vectors $\mathbf{x}_i = [x_1, x_2]^T$ for i=1,2,...,N, let the kernel be a polynomial $k(\mathbf{x}_i, \mathbf{x}_j) = (\mathbf{x}_i^T \mathbf{x}_j)^2$

show that
$$k(\mathbf{x}_i, \mathbf{x}_j) = \phi(\mathbf{x}_i)^T \phi(\mathbf{x}_j)$$
 where $\phi(\mathbf{x}_i) = (x_1^2, \sqrt{2}x_1x_2, x_2^2)^T$