

# **CpE 520: HW#8**

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Through this homework assignment we will download CIFAR-10 dataset and try to train an AlexNet-like neural network to classify the images in the dataset.

```
1 % to load last saved variables to worksapce of Matlab
2 load('HW8_code_workspace.mat')
```

## 0. CIFAR-10 Dataset

CIFAR-10 dataset is a collection of 60,000 labeled images (50,000 for training and 10,000 for testing) of 10 classes which were collected by Alex Krizhevsky, Vinod Nair, and Geoffrey Hinton. In this section we are going to download, unzip and load it into *Matlab*.

### 0.1 Downloading CIFAR-10 Dataset

The code below will check if there exist the dataset and if not, it will download both the train and test set of CIFAR-10.

```
1  clc; clear; close all;
2
3  if ~exist('cifar-10-batches-mat','dir')
4      cifar10Dataset = 'cifar-10-matlab';
5      disp('Downloading 174MB CIFAR-10 dataset...');
6      websave([cifar10Dataset, '.tar.gz'],...
7          ['https://www.cs.toronto.edu/~kriz/',cifar10Dataset, '.tar.gz']);
8      gunzip([cifar10Dataset, '.tar.gz'])
9      delete([cifar10Dataset, '.tar.gz'])
10     untar([cifar10Dataset, '.tar'])
11     delete([cifar10Dataset, '.tar'])
12 else
13     disp('CIFAR-10 dataset already downloaded.')
14 end
```

```
CIFAR-10 dataset already downloaded.
```

### 0.2 Splitting CIFAR-10 into Folders by Their Labels

After downloading the dataset, we need to put every single image in a folder which has the name equal to the image's label. Doing that will make it easier for us to use built-in Matlab function to load the dataset into Matlab workspace.

```
1  if ~exist('cifar10Train','dir')
2      disp('Saving the Images in folders. This might take some time...');
3      saveCIFAR10AsFolderOfImages('cifar-10-batches-mat', pwd, true);
4  else
5      disp('CIFAR-10 dataset already foldered!')
6  end
```

CIFAR-10 dataset already foldered!

### 0.3 Loading Training Images into *Matlab*

Using built-in *imageDatastore* of *Matlab* will help us to import data in batches, so they could be fit into memory easily.

```
1 categories = {'airplane', 'truck', 'horse', ...
2             'deer', 'dog', 'frog', ...
3             'cat', 'ship', 'bird', 'automobile'};
4
5 rootFolder = 'cifar10Train';
6 imds = imageDatastore(fullfile(rootFolder, categories), ...
7             'LabelSource', 'foldernames');
8 clear rootFolder
9
10 disp(countEachLabel(imds));
```

Label	Count
airplane	5000
automobile	5000
bird	5000
cat	5000
deer	5000
dog	5000
frog	5000
horse	5000
ship	5000
truck	5000

### 0.4 Plot One Random Sample of Each Class

We plot one sample of every class in the training dataset.

```
1 rand_nums = randi(size(imds.Files, 1)/10) + [0:5000:45000];
2
3 figure('Position', [100, 100, 1000, 1000]);
4 for i = 1:10
5     subplot(3,4,i);
6     imshow(imread(imds.Files{rand_nums(i)}), 'border', 'tight');
7     title(char(imds.Labels(rand_nums(i))));
8     hold on;
9 end
10 hold off
```

airplane



truck



horse



deer



dog



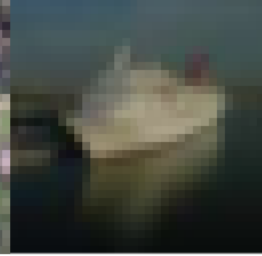
frog



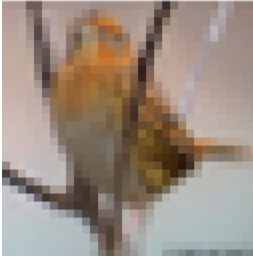
cat



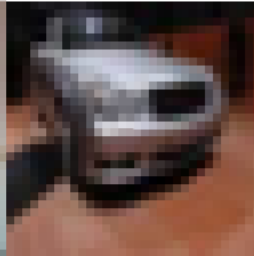
ship



bird



automobile

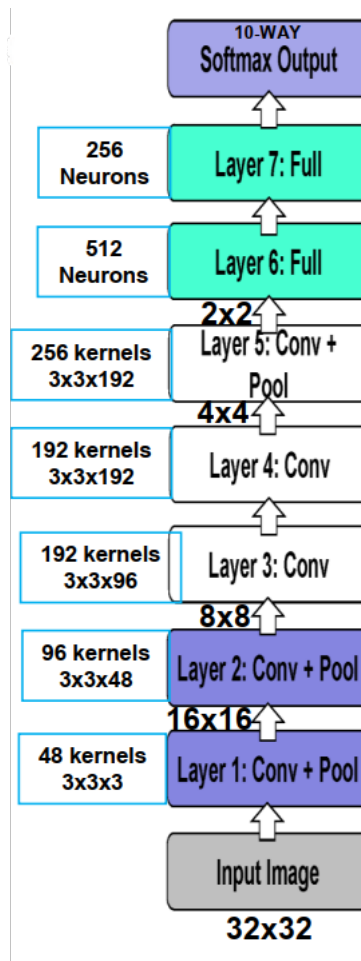


# 1. AlexNet-Like Neural Network to Classify CIFAR-10 Image Dataset

In this section we are going to build the neural network that was proposed in the first question. We also train it on CIFAR-10 dataset and finally evaluate it with the test subset of the dataset.

## 1.1 Defining Network Architecture

We define layers of the neural network according to the picture below with the code snippet that came after the picture.



```
1 image_dim = [32 32 3];
2 kernel_dim = [3 3];
3 maxpool_dim = [2 2];
4 stride_conv_dim = [1 1];
5 stride_maxpool_dim = [2 2];
6
7 layers_1 = [
```

```

8     imageInputLayer(image_dim, 'Name', 'data')
9
10    convolution2dLayer(kernel_dim, 48, 'Name', 'conv1', 'BiasLearnRateFactor',
11        2, 'Stride', stride_conv_dim, 'Padding', 'same')
12    reluLayer('Name', 'relu1')
13    maxPooling2dLayer(maxpool_dim, 'Name', 'pool1', 'Stride', stride_maxpool_dim
14        )
15
16    convolution2dLayer(kernel_dim, 96, 'Name', 'conv2', 'BiasLearnRateFactor',
17        2, 'Stride', stride_conv_dim, 'Padding', 'same')
18    reluLayer('Name', 'relu2')
19    maxPooling2dLayer(maxpool_dim, 'Name', 'pool2', 'Stride', stride_maxpool_dim
20        )
21
22    convolution2dLayer(kernel_dim, 192, 'Name', 'conv3', 'BiasLearnRateFactor',
23        2, 'Stride', stride_conv_dim, 'Padding', 'same')
24    reluLayer('Name', 'relu3')
25
26    convolution2dLayer(kernel_dim, 192, 'Name', 'conv4', 'BiasLearnRateFactor',
27        2, 'Stride', stride_conv_dim, 'Padding', 'same')
28    reluLayer('Name', 'relu4')
29    maxPooling2dLayer(maxpool_dim, 'Name', 'pool4', 'Stride', stride_maxpool_dim
30        )
31
32    convolution2dLayer(kernel_dim, 256, 'Name', 'conv5', 'BiasLearnRateFactor',
33        2, 'Stride', stride_conv_dim, 'Padding', 'same')
34    reluLayer('Name', 'relu5')
35    maxPooling2dLayer(maxpool_dim, 'Name', 'pool5', 'Stride', stride_maxpool_dim
36        )
37
38    fullyConnectedLayer(512, 'Name', 'fc6', 'BiasLearnRateFactor', 2)
39    reluLayer('Name', 'relu6')
40    dropoutLayer(0.5, 'Name', 'drop6')
41
42    fullyConnectedLayer(256, 'Name', 'fc7', 'BiasLearnRateFactor', 2)
43    reluLayer('Name', 'relu7')
44    dropoutLayer(0.5, 'Name', 'drop7')
45
46    fullyConnectedLayer(10, 'Name', 'softmax', 'BiasLearnRateFactor', 2)
47    softmaxLayer('Name', 'prob')
48
49    classificationLayer('Name', 'output')
50    ];
51
52    clear image_dim kernel_dim maxpool_dim stride_conv_dim stride_maxpool_dim
53
54    disp(layers_1);

```



24x1 Layer array with layers:

1	'data '	Image Input	32x32x3 images with 'zerocenter' normalization
2	'conv1 '	Convolution	48 3x3 convolutions with stride [1 1] and padding 'same'
3	'relu1 '	ReLU	ReLU
4	'pool1 '	Max Pooling	2x2 max pooling with stride [2 2] and padding [0 0 0 0]
5	'conv2 '	Convolution	96 3x3 convolutions with stride [1 1] and padding 'same'
6	'relu2 '	ReLU	ReLU
7	'pool2 '	Max Pooling	2x2 max pooling with stride [2 2] and padding [0 0 0 0]
8	'conv3 '	Convolution	192 3x3 convolutions with stride [1 1] and padding 'same'
9	'relu3 '	ReLU	ReLU
10	'conv4 '	Convolution	192 3x3 convolutions with stride [1 1] and padding 'same'
11	'relu4 '	ReLU	ReLU
12	'pool4 '	Max Pooling	2x2 max pooling with stride [2 2] and padding [0 0 0 0]
13	'conv5 '	Convolution	256 3x3 convolutions with stride [1 1] and padding 'same'
14	'relu5 '	ReLU	ReLU
15	'pool5 '	Max Pooling	2x2 max pooling with stride [2 2] and padding [0 0 0 0]
16	'fc6 '	Fully Connected	512 fully connected layer
17	'relu6 '	ReLU	ReLU
18	'drop6 '	Dropout	50% dropout
19	'fc7 '	Fully Connected	256 fully connected layer
20	'relu7 '	ReLU	ReLU
21	'drop7 '	Dropout	50% dropout
22	'softmax '	Fully Connected	10 fully connected layer
23	'prob '	Softmax	softmax
24	'output '	Classification Output	crossentropyex

In the figure below, we can see the whole network at a glance:

```
1 %analyzeNetwork(layers_1);
2 plot(layerGraph(layers_1));
```



## 1.3 Training the Network

### 1.3.1 Split Training Data into *train* and *validation* Subsets

15 percent of the 50,000 training images are assigned to the validation set and the rest are kept for the neural network training.

```

1 [imdsTrain, imdsValidation] = splitEachLabel(imds,0.85,'randomized');
2 disp(countEachLabel(imdsTrain));

```

Label	Count
airplane	4250
automobile	4250
bird	4250
cat	4250
deer	4250
dog	4250
frog	4250
horse	4250
ship	4250
truck	4250

```

1 disp(countEachLabel(imdsValidation));

```

Label	Count
airplane	750
automobile	750
bird	750
cat	750
deer	750
dog	750
frog	750
horse	750
ship	750
truck	750

### 1.3.2 Preprocessing the Training Data

To strengthen the training process and make the network invariant to distortions in images, we did some preprocessing on the training subset of the images, as listed below:

- Random reflection of images in the left-right direction with probability of 0.5
- Random horizontal translation picked from a continuous distribution of range [-3 3]
- Random vertical translation picked from a continuous distribution of range [-3 3]

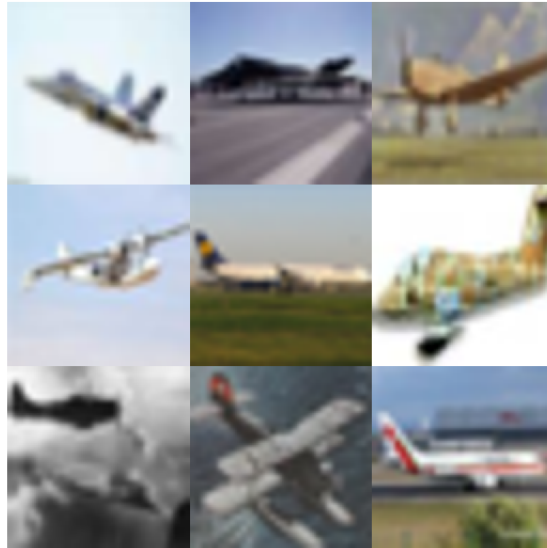
```

1 pixelRange = [-3 3];
2 imageAugmenter = imageDataAugmenter( ...
3     'RandXReflection',true, ...
4     'RandXTranslation',pixelRange, ...
5     'RandYTranslation',pixelRange);
6 augimdsTrain = augmentedImageDatastore([32 32], imdsTrain, ...
7     'DataAugmentation',imageAugmenter);

```

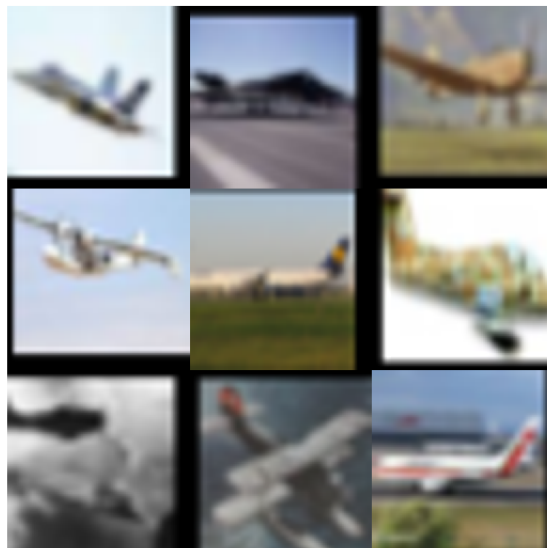
The first nine images before preprocessing:

```
1  montage(subset(imdsTrain, 1:9));
```



The first nine images after preprocessing:

```
1  montage(readByIndex(augimdsTrain, 1:9).input);
```



### 1.3.3 Defining Options for Training

We have used 40 epoches with mini-batch size of 512 and used the *Adam* Optimizer.

```
1  opts = trainingOptions('adam', ...
2      'ExecutionEnvironment','auto', ...
3      'MaxEpochs', 40, ...
4      'MiniBatchSize', 512, ...
5      'Shuffle', 'every-epoch', ...
6      'Plots', 'training-progress', ...
7      'Verbose', true, ...
8      'ValidationData', imdsValidation);
```

### 1.3.4 Learning Curves and Training Process

We trained the network on single GPU system nad print the results in a table every 50 iterations. Besides, the learning curves are plotted after the table. Finally the network reached 84.38% on training and 81.37% on validation subset. The training process took about 90 minutes long.

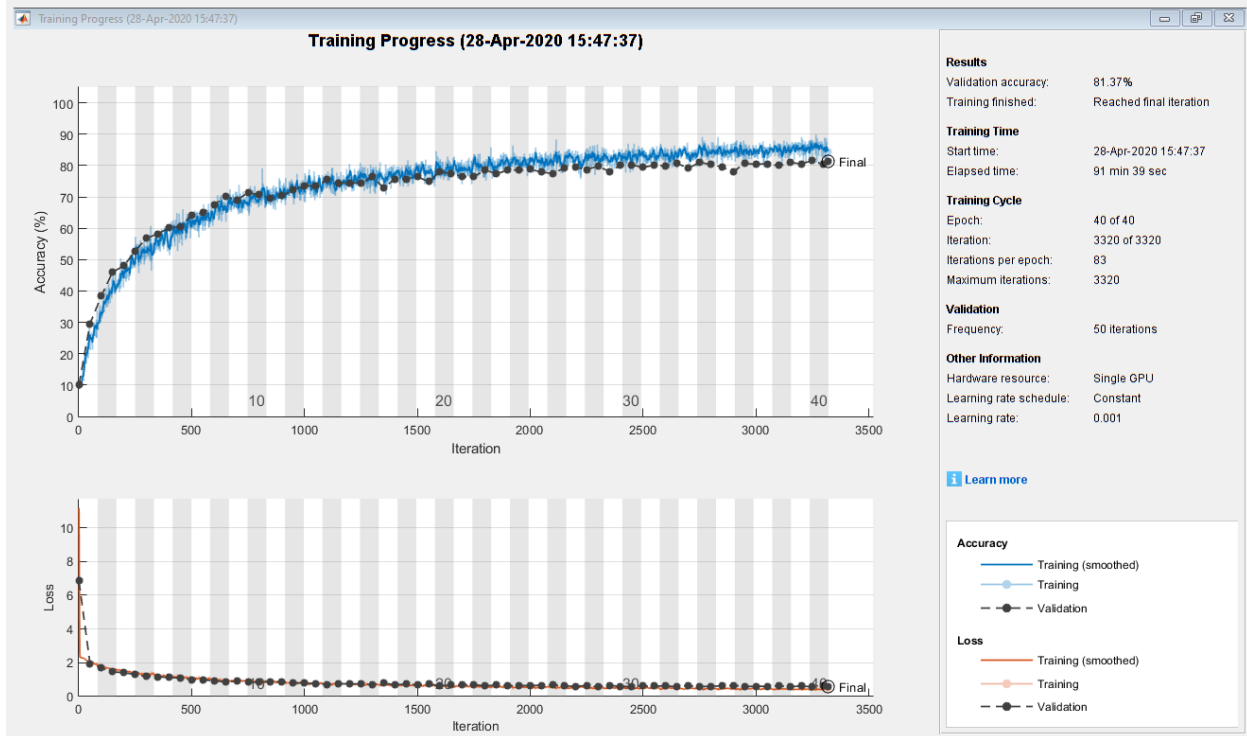
```
1  trained_net_1 = trainNetwork(augimdsTrain, layers_1, opts);
```

Warning: Support for GPU devices with Compute Capability 3.0 will be removed in a future MATLAB release. For more information on GPU support, see GPU Support by Release.  
Training on single GPU.  
Initializing input data normalization.

Epoch Learning	Iteration	Time Elapsed (hh:mm:ss)	Mini-batch Accuracy	Validation Accuracy	Mini-batch Loss	Validation Loss	Base Rate
1	1	00:02:46	10.55%	10.00%	11.1746	6.8502	
0.0010							
1	50	00:04:05	23.05%	29.56%	2.0305	1.9423	
0.0010							
2	100	00:05:24	31.84%	38.39%	1.8032	1.6916	
0.0010							
2	150	00:06:45	39.84%	46.04%	1.6340	1.4730	
0.0010							
3	200	00:08:05	48.44%	48.04%	1.4497	1.4095	
0.0010							
4	250	00:09:25	47.46%	52.71%	1.4264	1.3147	
0.0010							
4	300	00:10:45	51.95%	56.84%	1.3355	1.1858	
0.0010							
5	350	00:12:05	56.64%	58.21%	1.1940	1.1769	
0.0010							
5	400	00:13:26	56.05%	60.15%	1.2226	1.1227	
0.0010							
6	450	00:14:45	57.81%	60.47%	1.2050	1.1112	
0.0010							
7	500	00:16:06	64.84%	64.23%	1.0189	1.0050	
0.0010							
7	550	00:17:28	62.89%	64.88%	1.0022	0.9921	
0.0010							
8	600	00:18:49	65.43%	67.41%	1.0184	0.9291	
0.0010							
8	650	00:20:10	68.16%	70.23%	0.9114	0.8688	
0.0010							
9	700	00:21:31	71.48%	68.93%	0.8441	0.9062	
0.0010							
10	750	00:22:52	68.36%	71.39%	0.9565	0.8422	
0.0010							

10	800	00:24:13	67.19%	70.61%	0.9368	0.8515
0.0010						
11	850	00:25:35	67.19%	69.53%	0.9207	0.8781
0.0010						
11	900	00:26:55	71.48%	70.40%	0.8185	0.8636
0.0010						
12	950	00:28:16	71.48%	72.16%	0.8344	0.8269
0.0010						
13	1000	00:29:37	74.41%	73.60%	0.7181	0.7854
0.0010						
13	1050	00:30:57	73.05%	73.35%	0.8046	0.7736
0.0010						
14	1100	00:32:17	72.85%	75.48%	0.8163	0.7243
0.0010						
14	1150	00:33:36	75.78%	74.41%	0.7186	0.7637
0.0010						
15	1200	00:34:56	78.91%	74.48%	0.6884	0.7551
0.0010						
16	1250	00:36:16	76.17%	74.37%	0.7158	0.7408
0.0010						
16	1300	00:37:36	73.83%	76.40%	0.7440	0.7034
0.0010						
17	1350	00:38:56	75.59%	72.89%	0.6730	0.7962
0.0010						
17	1400	00:40:15	77.34%	75.68%	0.6674	0.7034
0.0010						
18	1450	00:41:37	79.69%	75.72%	0.6195	0.7294
0.0010						
19	1500	00:42:57	78.13%	76.39%	0.6104	0.6912
0.0010						
19	1550	00:44:17	77.34%	74.83%	0.7288	0.7506
0.0010						
20	1600	00:45:37	77.15%	78.03%	0.6956	0.6359
0.0010						
20	1650	00:46:56	79.49%	77.44%	0.6096	0.6763
0.0010						
21	1700	00:48:17	78.91%	76.44%	0.6358	0.6896
0.0010						
22	1750	00:49:37	83.59%	76.37%	0.4726	0.7047
0.0010						
22	1800	00:50:58	79.49%	78.59%	0.6246	0.6303
0.0010						
23	1850	00:52:17	79.69%	77.28%	0.6480	0.6792
0.0010						
23	1900	00:53:45	80.86%	78.53%	0.5494	0.6419
0.0010						
24	1950	00:55:05	81.45%	78.51%	0.5932	0.6484
0.0010						
25	2000	00:56:24	82.62%	78.75%	0.5143	0.6555
0.0010						
25	2050	00:57:45	81.45%	77.91%	0.5461	0.6688
0.0010						
26	2100	00:59:04	81.05%	77.41%	0.5522	0.6912
0.0010						
26	2150	01:00:24	83.40%	79.15%	0.5004	0.6260
0.0010						
27	2200	01:01:45	81.05%	79.36%	0.5271	0.6145
0.0010						
28	2250	01:03:05	80.27%	78.72%	0.5737	0.6449
0.0010						
28	2300	01:04:25	79.69%	79.76%	0.5618	0.6105
0.0010						
29	2350	01:05:44	82.62%	78.12%	0.5440	0.6619
0.0010						
29	2400	01:07:04	82.42%	80.03%	0.4902	0.6073
0.0010						
30	2450	01:08:24	83.59%	80.17%	0.5028	0.5901
0.0010						
31	2500	01:09:44	83.40%	79.40%	0.4549	0.6185
0.0010						
31	2550	01:11:04	81.05%	80.09%	0.5590	0.6206
0.0010						
32	2600	01:12:23	83.01%	79.92%	0.4975	0.6255
0.0010						
32	2650	01:13:43	79.10%	80.68%	0.6294	0.5893
0.0010						
33	2700	01:15:03	81.84%	79.11%	0.5202	0.6425
0.0010						
34	2750	01:16:23	86.33%	80.97%	0.4711	0.5894
0.0010						
34	2800	01:17:42	84.57%	80.29%	0.4627	0.6106
0.0010						
35	2850	01:19:02	86.52%	79.55%	0.3983	0.6292
0.0010						
35	2900	01:20:21	84.18%	78.05%	0.4886	0.6640
0.0010						
36	2950	01:21:40	85.55%	80.63%	0.4258	0.6036
0.0010						

	37		3000		01:23:00		86.52%		80.41%		0.3825		0.6077	
	0.0010		37		3050		01:24:21		84.18%		80.53%		0.4640	
	0.0010		38		3100		01:25:40		87.11%		79.97%		0.4125	
	0.0010		38		3150		01:26:59		83.20%		80.95%		0.5435	
	0.0010		39		3200		01:28:18		87.11%		80.52%		0.4022	
	0.0010		40		3250		01:29:38		84.18%		81.56%		0.4500	
	0.0010		40		3300		01:30:57		84.77%		80.25%		0.4485	
	0.0010		40		3320		01:31:32		84.38%		81.37%		0.4713	
	0.0010												0.5919	



## 1.4 Evaluating the Network

Here we use the test partition of the dataset to evaluate the trained network.

### 1.4.1 Loading the Test Set of CIFAR-10

```

1 rootFolder = 'cifar10Test';
2 imds_test = imageDatastore(fullfile(rootFolder, categories), ...
3     'LabelSource', 'foldernames');
4 clear rootFolder
5
6 disp(countEachLabel(imds_test));

```

Label	Count
airplane	1000
automobile	1000
bird	1000
cat	1000
deer	1000
dog	1000
frog	1000
horse	1000
ship	1000
truck	1000

### 1.4.2 Classifying the Test Dataset

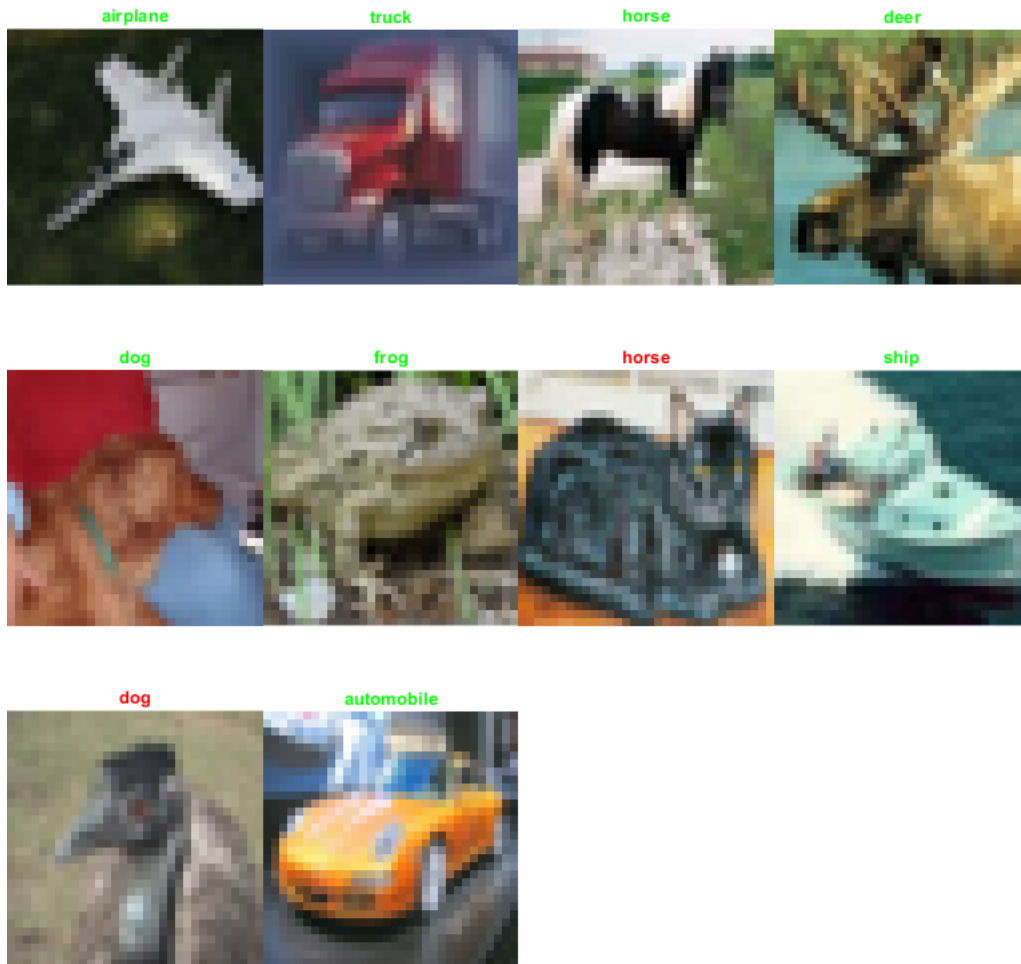
The line below will classify all images in the test dataset.

```
1 predicted_labels_1 = classify(trained_net_1, imds_test);
```

### 1.4.3 Plot Some Samples of the Test Dataset with the Predicted Label

Here we plot one sample of every class of the test dataset and display its predicted label on top of it. If it was predicted correctly the title will be in green color otherwise in red.

```
1 rand_nums = randi(size(imds_test.Files, 1)/10) + [0:1000:9000];
2
3 figure('Position', [100, 100, 1000, 1000]);
4 for i = 1:10
5     if predicted_labels_1(rand_nums(i)) == imds_test.Labels(rand_nums(i))
6         colorText = 'g';
7     else
8         colorText = 'r';
9     end
10    subplot(3,4,i);
11    imshow(imread(imds_test.Files{rand_nums(i)}));
12    title(char(predicted_labels_1(rand_nums(i))), 'Color', colorText);
13    hold on;
14 end
15 hold off
```



#### 1.4.4 Classification Performance

As the final step of this section, we plot the confusion matrix. Final performance of the network is 81.0% over the whole test dataset.

```
1 plotconfusion(imds_test.Labels , predicted_labels_1);
```



Output Class	airplane	826	3	60	24	10	12	5	18	29	13	82.6%
		8.3%	0.0%	0.6%	0.2%	0.1%	0.1%	0.1%	0.2%	0.3%	0.1%	17.4%
	automobile	26	951	3	20	4	12	10	11	20	91	82.8%
		0.3%	9.5%	0.0%	0.2%	0.0%	0.1%	0.1%	0.1%	0.2%	0.9%	17.2%
	bird	23	0	681	36	26	22	10	9	8	1	83.5%
		0.2%	0.0%	6.8%	0.4%	0.3%	0.2%	0.1%	0.1%	0.1%	0.0%	16.5%
	cat	12	1	22	533	29	78	17	18	8	6	73.6%
		0.1%	0.0%	0.2%	5.3%	0.3%	0.8%	0.2%	0.2%	0.1%	0.1%	26.4%
	deer	8	1	51	50	807	43	3	35	4	0	80.5%
		0.1%	0.0%	0.5%	0.5%	8.1%	0.4%	0.0%	0.4%	0.0%	0.0%	19.5%
dog	5	3	55	172	18	753	10	38	0	0	71.4%	
	0.1%	0.0%	0.5%	1.7%	0.2%	7.5%	0.1%	0.4%	0.0%	0.0%	28.6%	
frog	8	3	99	104	79	41	938	13	3	5	72.5%	
	0.1%	0.0%	1.0%	1.0%	0.8%	0.4%	9.4%	0.1%	0.0%	0.1%	27.5%	
horse	4	1	15	20	22	30	1	842	2	3	89.6%	
	0.0%	0.0%	0.1%	0.2%	0.2%	0.3%	0.0%	8.4%	0.0%	0.0%	10.4%	
ship	52	9	5	17	2	1	4	3	902	14	89.4%	
	0.5%	0.1%	0.1%	0.2%	0.0%	0.0%	0.0%	0.0%	9.0%	0.1%	10.6%	
truck	36	28	9	24	3	8	2	13	24	867	85.5%	
	0.4%	0.3%	0.1%	0.2%	0.0%	0.1%	0.0%	0.1%	0.2%	8.7%	14.5%	
		82.6%	95.1%	68.1%	53.3%	80.7%	75.3%	93.8%	84.2%	90.2%	86.7%	81.0%
		17.4%	4.9%	31.9%	46.7%	19.3%	24.7%	6.2%	15.8%	9.8%	13.3%	19.0%
	airplane	automobile	bird	cat	deer	dog	frog	horse	ship	truck		

## 2. Deleting Convolutional Layer 5 with Its Max-Pooling

### 2.1 Defining Network Architecture

We define the layers of the network again as below. Convolutional layer 5 is deleted in comparison with question 1.

```
1  image_dim = [32 32 3];
2  kernel_dim = [3 3];
3  maxpool_dim = [2 2];
4  stride_conv_dim = [1 1];
5  stride_maxpool_dim = [2 2];
6
7  layers_2 = [
8      imageInputLayer(image_dim, 'Name', 'data')
9
10     convolution2dLayer(kernel_dim, 48, 'Name', 'conv1', 'BiasLearnRateFactor',
11         2, 'Stride', stride_conv_dim, 'Padding', 'same')
12     reluLayer('Name', 'relu1')
13     maxPooling2dLayer(maxpool_dim, 'Name', 'pool1', 'Stride', stride_maxpool_dim
14         )
15     convolution2dLayer(kernel_dim, 96, 'Name', 'conv2', 'BiasLearnRateFactor',
16         2, 'Stride', stride_conv_dim, 'Padding', 'same')
17     reluLayer('Name', 'relu2')
18     maxPooling2dLayer(maxpool_dim, 'Name', 'pool2', 'Stride', stride_maxpool_dim
19         )
20     convolution2dLayer(kernel_dim, 192, 'Name', 'conv3', 'BiasLearnRateFactor',
21         2, 'Stride', stride_conv_dim, 'Padding', 'same')
22     reluLayer('Name', 'relu3')
23     convolution2dLayer(kernel_dim, 192, 'Name', 'conv4', 'BiasLearnRateFactor',
24         2, 'Stride', stride_conv_dim, 'Padding', 'same')
25     reluLayer('Name', 'relu4')
26     maxPooling2dLayer(maxpool_dim, 'Name', 'pool4', 'Stride', stride_maxpool_dim
27         )
28     fullyConnectedLayer(512, 'Name', 'fc6', 'BiasLearnRateFactor', 2)
29     reluLayer('Name', 'relu6')
30     dropoutLayer(0.5, 'Name', 'drop6')
31     fullyConnectedLayer(256, 'Name', 'fc7', 'BiasLearnRateFactor', 2)
32     reluLayer('Name', 'relu7')
33     dropoutLayer(0.5, 'Name', 'drop7')
34     fullyConnectedLayer(10, 'Name', 'softmax', 'BiasLearnRateFactor', 2)
35     softmaxLayer('Name', 'prob')
```

```

35
36     classificationLayer('Name','output')
37 ];
38
39 clear image_dim kernel_dim maxpool_dim stride_conv_dim stride_maxpool_dim
40
41 disp(layers_2);

```

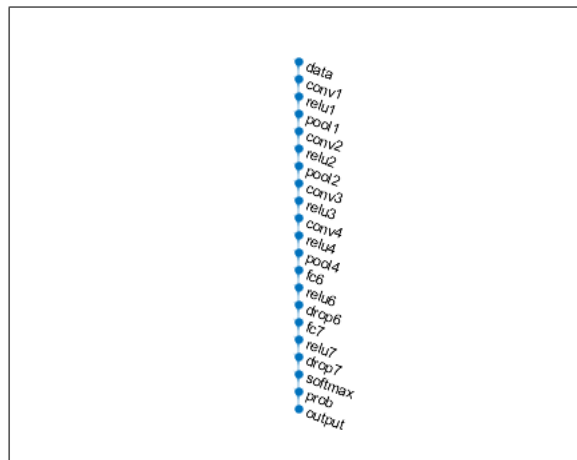
21x1 Layer array with layers:

1	'data'	Image Input	32x32x3 images with 'zerocenter' normalization
2	'conv1'	Convolution	48 3x3 convolutions with stride [1 1] and padding 'same'
3	'relu1'	ReLU	ReLU
4	'pool1'	Max Pooling	2x2 max pooling with stride [2 2] and padding [0 0 0 0]
5	'conv2'	Convolution	96 3x3 convolutions with stride [1 1] and padding 'same'
6	'relu2'	ReLU	ReLU
7	'pool2'	Max Pooling	2x2 max pooling with stride [2 2] and padding [0 0 0 0]
8	'conv3'	Convolution	192 3x3 convolutions with stride [1 1] and padding 'same'
9	'relu3'	ReLU	ReLU
10	'conv4'	Convolution	192 3x3 convolutions with stride [1 1] and padding 'same'
11	'relu4'	ReLU	ReLU
12	'pool4'	Max Pooling	2x2 max pooling with stride [2 2] and padding [0 0 0 0]
13	'fc6'	Fully Connected	512 fully connected layer
14	'relu6'	ReLU	ReLU
15	'drop6'	Dropout	50% dropout
16	'fc7'	Fully Connected	256 fully connected layer
17	'relu7'	ReLU	ReLU
18	'drop7'	Dropout	50% dropout
19	'softmax'	Fully Connected	10 fully connected layer
20	'prob'	Softmax	softmax
21	'output'	Classification Output	crossentropyex

```

1 %analyzeNetwork(layers_2);
2 plot(layerGraph(layers_2));

```



## 2.2 Learning Curves and Training Process

We trained the network on single GPU system and print the results in a table every 50 iterations. Besides, the learning curves are plotted after the table. Finally the network reached 83.59% on training and 81.84%

on validation subset. The training process took about 90 minutes long.

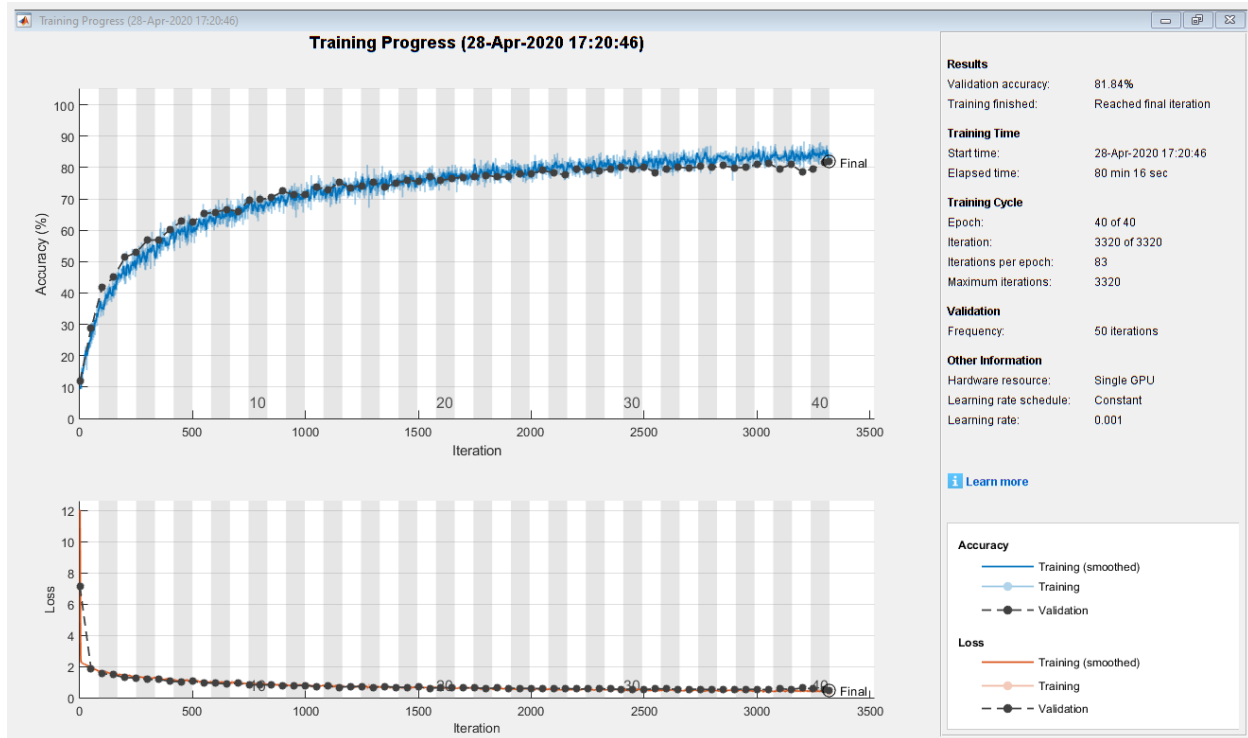
```
1 trained_net_2 = trainNetwork(augimdsTrain, layers_2, opts);
```

Training on single GPU.

Initializing input data normalization.

Epoch Learning	Iteration	Time Elapsed (hh:mm:ss)	Mini-batch Accuracy	Validation Accuracy	Mini-batch Loss	Validation Loss	Base Rate
1	1	00:00:09	9.38%	11.89%	12.0610	7.1610	
0.0010							
1	50	00:01:17	24.61%	28.69%	2.0013	1.9260	
0.0010							
2	100	00:02:27	35.74%	41.84%	1.7440	1.6063	
0.0010							
2	150	00:03:36	38.28%	44.99%	1.6553	1.5126	
0.0010							
3	200	00:04:46	42.77%	51.33%	1.5858	1.3373	
0.0010							
4	250	00:05:56	50.98%	52.97%	1.3348	1.3207	
0.0010							
4	300	00:07:05	48.63%	56.79%	1.3816	1.2178	
0.0010							
5	350	00:08:15	56.45%	56.97%	1.2503	1.2198	
0.0010							
5	400	00:09:25	57.03%	60.29%	1.1812	1.1059	
0.0010							
6	450	00:10:34	58.98%	62.77%	1.1712	1.0679	
0.0010							
7	500	00:11:44	59.96%	62.55%	1.1371	1.1027	
0.0010							
7	550	00:12:54	61.52%	65.28%	1.1597	1.0064	
0.0010							
8	600	00:14:04	61.91%	65.73%	1.0565	0.9785	
0.0010							
8	650	00:15:18	63.48%	66.64%	1.0920	0.9404	
0.0010							
9	700	00:16:28	69.92%	66.04%	0.9164	0.9692	
0.0010							
10	750	00:17:38	66.60%	69.52%	0.9411	0.8815	
0.0010							
10	800	00:18:48	71.48%	69.76%	0.7699	0.8761	
0.0010							
11	850	00:20:00	65.23%	70.47%	0.9358	0.8700	
0.0010							
11	900	00:21:10	70.70%	72.47%	0.9084	0.8083	
0.0010							
12	950	00:22:19	68.36%	71.25%	0.8975	0.8242	
0.0010							
13	1000	00:23:28	68.55%	71.35%	0.8692	0.8445	
0.0010							
13	1050	00:24:38	73.44%	73.73%	0.8148	0.7670	
0.0010							
14	1100	00:25:49	73.63%	72.89%	0.7771	0.7887	
0.0010							
14	1150	00:29:23	76.17%	75.27%	0.7079	0.7233	
0.0010							
15	1200	00:31:07	71.48%	73.53%	0.8016	0.7810	
0.0010							
16	1250	00:32:16	73.24%	74.20%	0.7701	0.7504	
0.0010							
16	1300	00:33:26	75.78%	75.41%	0.6784	0.7155	
0.0010							
17	1350	00:34:35	76.76%	73.65%	0.6671	0.7765	
0.0010							
17	1400	00:35:44	77.54%	75.12%	0.6493	0.7253	
0.0010							
18	1450	00:36:54	74.61%	75.76%	0.7402	0.7145	
0.0010							
19	1500	00:38:03	76.56%	75.68%	0.6916	0.7319	
0.0010							
19	1550	00:39:13	73.83%	77.16%	0.7549	0.6655	
0.0010							
20	1600	00:40:22	76.37%	75.81%	0.6699	0.6971	
0.0010							
20	1650	00:41:32	80.86%	76.53%	0.5834	0.7003	
0.0010							
21	1700	00:42:42	77.15%	76.93%	0.6758	0.6791	

0.0010													
22		1750		00:43:51		81.05%		77.19%		0.5636		0.6791	
0.0010													
22		1800		00:45:01		75.00%		77.51%		0.7534		0.6539	
0.0010													
23		1850		00:46:10		78.13%		76.97%		0.6281		0.6714	
0.0010													
23		1900		00:47:20		75.39%		77.09%		0.7354		0.6630	
0.0010													
24		1950		00:48:29		80.86%		77.93%		0.5824		0.6567	
0.0010													
25		2000		00:49:38		79.88%		78.03%		0.6081		0.6421	
0.0010													
25		2050		00:50:47		76.37%		79.05%		0.6632		0.6310	
0.0010													
26		2100		00:51:57		81.05%		78.31%		0.5620		0.6360	
0.0010													
26		2150		00:53:06		75.98%		77.65%		0.7153		0.6562	
0.0010													
27		2200		00:54:15		79.69%		79.37%		0.5905		0.6066	
0.0010													
28		2250		00:55:24		80.47%		79.25%		0.5553		0.6123	
0.0010													
28		2300		00:56:33		84.38%		78.88%		0.4753		0.6269	
0.0010													
29		2350		00:57:43		79.30%		79.51%		0.5687		0.6096	
0.0010													
29		2400		00:58:52		79.69%		80.08%		0.5822		0.5920	
0.0010													
30		2450		01:00:01		81.64%		79.64%		0.5390		0.6008	
0.0010													
31		2500		01:01:10		83.40%		80.20%		0.4910		0.5718	
0.0010													
31		2550		01:02:19		82.42%		78.44%		0.5220		0.6315	
0.0010													
32		2600		01:03:28		80.47%		79.51%		0.5769		0.6148	
0.0010													
32		2650		01:04:38		80.08%		80.07%		0.5332		0.5917	
0.0010													
33		2700		01:05:47		81.05%		79.80%		0.5771		0.6039	
0.0010													
34		2750		01:06:56		81.64%		80.25%		0.5067		0.5886	
0.0010													
34		2800		01:08:05		79.10%		80.00%		0.5623		0.5812	
0.0010													
35		2850		01:09:15		84.77%		80.63%		0.4710		0.5896	
0.0010													
35		2900		01:10:24		81.64%		79.89%		0.5543		0.5858	
0.0010													
36		2950		01:11:33		82.81%		80.01%		0.5047		0.6002	
0.0010													
37		3000		01:12:42		83.40%		81.03%		0.4941		0.5815	
0.0010													
37		3050		01:13:52		82.03%		81.28%		0.4730		0.5653	
0.0010													
38		3100		01:15:01		83.20%		79.64%		0.5356		0.6305	
0.0010													
38		3150		01:16:10		85.74%		80.91%		0.4294		0.5786	
0.0010													
39		3200		01:17:19		84.38%		78.64%		0.4582		0.6789	
0.0010													
40		3250		01:18:28		83.40%		79.57%		0.4886		0.6115	
0.0010													
40		3300		01:19:38		83.20%		81.63%		0.4353		0.5549	
0.0010													
40		3320		01:20:10		83.59%		81.84%		0.4765		0.5440	
0.0010													



## 2.3 Evaluating the Network

Here we use the test partition of the dataset to evaluate the trained network.

### 2.3.1 Classifying the Test Dataset

The line below will classify all images in the test dataset.

```
1 predicted_labels_2 = classify(trained_net_2, imds_test);
```

### 2.3.2 Classification Performance

As the final step of this section, we plot the confusion matrix. The final performance of the network is 81.7% over the whole test dataset.

```
1 plotconfusion(imds_test.Labels, predicted_labels_2);
```

Confusion Matrix												
Output Class	airplane	785 7.8%	7 0.1%	26 0.3%	11 0.1%	8 0.1%	7 0.1%	4 0.0%	6 0.1%	41 0.4%	14 0.1%	86.4% 13.6%
	automobile	15 0.1%	923 9.2%	1 0.0%	3 0.0%	1 0.0%	3 0.0%	2 0.0%	0 0.0%	17 0.2%	63 0.6%	89.8% 10.2%
	bird	56 0.6%	2 0.0%	774 7.7%	45 0.4%	52 0.5%	28 0.3%	26 0.3%	23 0.2%	11 0.1%	1 0.0%	76.0% 24.0%
	cat	14 0.1%	2 0.0%	32 0.3%	670 6.7%	40 0.4%	149 1.5%	24 0.2%	40 0.4%	10 0.1%	11 0.1%	67.5% 32.5%
	deer	8 0.1%	0 0.0%	38 0.4%	37 0.4%	763 7.6%	36 0.4%	7 0.1%	26 0.3%	3 0.0%	0 0.0%	83.1% 16.9%
	dog	3 0.0%	1 0.0%	36 0.4%	112 1.1%	12 0.1%	705 7.0%	7 0.1%	35 0.4%	0 0.0%	3 0.0%	77.1% 22.9%
	frog	10 0.1%	7 0.1%	62 0.6%	81 0.8%	66 0.7%	31 0.3%	926 9.3%	5 0.1%	9 0.1%	10 0.1%	76.7% 23.3%
	horse	11 0.1%	0 0.0%	18 0.2%	26 0.3%	50 0.5%	35 0.4%	1 0.0%	856 8.6%	3 0.0%	10 0.1%	84.8% 15.2%
	ship	54 0.5%	14 0.1%	7 0.1%	5 0.1%	5 0.1%	4 0.0%	2 0.0%	2 0.0%	893 8.9%	14 0.1%	89.3% 10.7%
	truck	44 0.4%	44 0.4%	6 0.1%	10 0.1%	3 0.0%	2 0.0%	1 0.0%	7 0.1%	13 0.1%	874 8.7%	87.1% 12.9%
		78.5% 21.5%	92.3% 7.7%	77.4% 22.6%	67.0% 33.0%	76.3% 23.7%	70.5% 29.5%	92.6% 7.4%	85.6% 14.4%	89.3% 10.7%	87.4% 12.6%	81.7% 18.3%
Target Class												
airplane												
automobile												
bird												
cat												
deer												
dog												
frog												
horse												
ship												
truck												

## 3. Deleting Convolutional Layer 4 with Its Max-Pooling

### 3.1 Defining Network Architecture

We define the layers of the network again as below. Convolutional layer 4 is deleted in comparison with question 1.

```
1  image_dim = [32 32 3];
2  kernel_dim = [3 3];
3  maxpool_dim = [2 2];
4  stride_conv_dim = [1 1];
5  stride_maxpool_dim = [2 2];
6
7  layers_3 = [
8      imageInputLayer(image_dim, 'Name', 'data')
9
10     convolution2dLayer(kernel_dim, 48, 'Name', 'conv1', 'BiasLearnRateFactor',
11         2, 'Stride', stride_conv_dim, 'Padding', 'same')
12     reluLayer('Name', 'relu1')
13     maxPooling2dLayer(maxpool_dim, 'Name', 'pool1', 'Stride', stride_maxpool_dim
14         )
15     convolution2dLayer(kernel_dim, 96, 'Name', 'conv2', 'BiasLearnRateFactor',
16         2, 'Stride', stride_conv_dim, 'Padding', 'same')
17     reluLayer('Name', 'relu2')
18     maxPooling2dLayer(maxpool_dim, 'Name', 'pool2', 'Stride', stride_maxpool_dim
19         )
20     convolution2dLayer(kernel_dim, 192, 'Name', 'conv3', 'BiasLearnRateFactor',
21         2, 'Stride', stride_conv_dim, 'Padding', 'same')
22     reluLayer('Name', 'relu3')
23     convolution2dLayer(kernel_dim, 256, 'Name', 'conv5', 'BiasLearnRateFactor',
24         2, 'Stride', stride_conv_dim, 'Padding', 'same')
25     reluLayer('Name', 'relu5')
26     maxPooling2dLayer(maxpool_dim, 'Name', 'pool5', 'Stride', stride_maxpool_dim
27         )
28     fullyConnectedLayer(512, 'Name', 'fc6', 'BiasLearnRateFactor', 2)
29     reluLayer('Name', 'relu6')
30     dropoutLayer(0.5, 'Name', 'drop6')
31     fullyConnectedLayer(256, 'Name', 'fc7', 'BiasLearnRateFactor', 2)
32     reluLayer('Name', 'relu7')
33     dropoutLayer(0.5, 'Name', 'drop7')
34     fullyConnectedLayer(10, 'Name', 'softmax', 'BiasLearnRateFactor', 2)
35     softmaxLayer('Name', 'prob')
```



```

35
36     classificationLayer('Name','output')
37 ];
38
39 clear image_dim kernel_dim maxpool_dim stride_conv_dim stride_maxpool_dim
40
41 disp(layers_3);

```

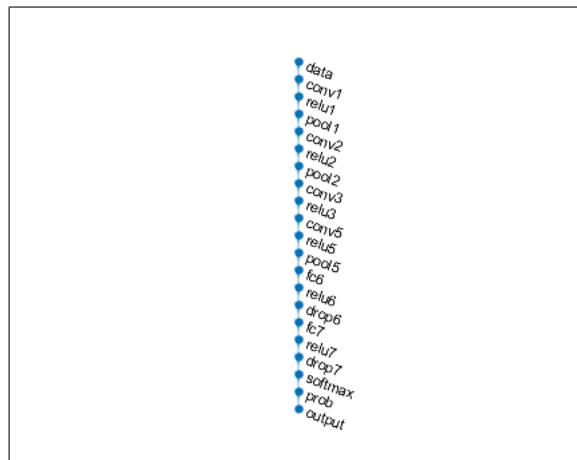
21x1 Layer array with layers:

1	'data'	Image Input	32x32x3 images with 'zerocenter' normalization
2	'conv1'	Convolution	48 3x3 convolutions with stride [1 1] and padding 'same'
3	'relu1'	ReLU	ReLU
4	'pool1'	Max Pooling	2x2 max pooling with stride [2 2] and padding [0 0 0 0]
5	'conv2'	Convolution	96 3x3 convolutions with stride [1 1] and padding 'same'
6	'relu2'	ReLU	ReLU
7	'pool2'	Max Pooling	2x2 max pooling with stride [2 2] and padding [0 0 0 0]
8	'conv3'	Convolution	192 3x3 convolutions with stride [1 1] and padding 'same'
9	'relu3'	ReLU	ReLU
10	'conv5'	Convolution	256 3x3 convolutions with stride [1 1] and padding 'same'
11	'relu5'	ReLU	ReLU
12	'pool5'	Max Pooling	2x2 max pooling with stride [2 2] and padding [0 0 0 0]
13	'fc6'	Fully Connected	512 fully connected layer
14	'relu6'	ReLU	ReLU
15	'drop6'	Dropout	50% dropout
16	'fc7'	Fully Connected	256 fully connected layer
17	'relu7'	ReLU	ReLU
18	'drop7'	Dropout	50% dropout
19	'softmax'	Fully Connected	10 fully connected layer
20	'prob'	Softmax	softmax
21	'output'	Classification Output	crossentropyex

```

1 %analyzeNetwork(layers_3);
2 plot(layerGraph(layers_3));

```



## 3.2 Learning Curves and Training Process

We trained the network on single GPU system and print the results in a table every 50 iterations. Besides, the learning curves are plotted after the table. Finally the network reached 83.59% on training and 81.17%

on validation subset. The training process took about 90 minutes long.

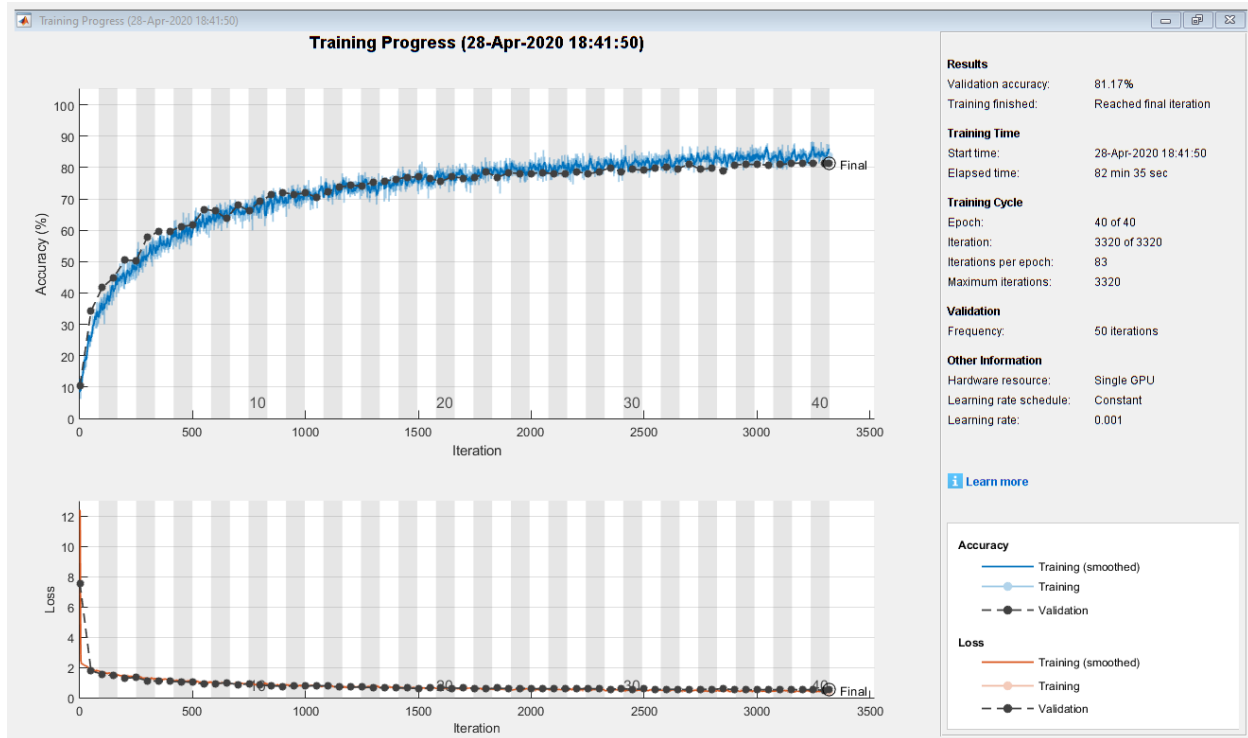
```
1 trained_net_3 = trainNetwork(augimdsTrain, layers_3, opts);
```

Training on single GPU.

Initializing input data normalization.

Epoch Learning	Iteration	Time Elapsed (hh:mm:ss)	Mini-batch Accuracy	Validation Accuracy	Mini-batch Loss	Validation Loss	Base Rate
1	1	00:00:09	8.40%	10.51%	12.4558	7.5910	
0.0010							
1	50	00:01:22	25.98%	34.25%	1.9766	1.8403	
0.0010							
2	100	00:02:36	33.20%	41.79%	1.7935	1.6030	
0.0010							
2	150	00:03:50	37.50%	44.89%	1.7270	1.5264	
0.0010							
3	200	00:05:04	44.34%	50.48%	1.5197	1.3583	
0.0010							
4	250	00:06:18	49.61%	50.32%	1.4239	1.3820	
0.0010							
4	300	00:07:32	50.00%	57.88%	1.3442	1.1852	
0.0010							
5	350	00:08:46	56.45%	59.64%	1.2219	1.1483	
0.0010							
5	400	00:10:02	57.03%	59.75%	1.2362	1.1274	
0.0010							
6	450	00:11:17	56.64%	61.13%	1.2024	1.1178	
0.0010							
7	500	00:12:31	61.91%	61.68%	1.1280	1.0773	
0.0010							
7	550	00:13:46	64.06%	66.67%	1.0673	0.9591	
0.0010							
8	600	00:15:00	65.04%	66.17%	1.0417	0.9873	
0.0010							
8	650	00:16:15	65.63%	63.72%	1.0807	1.0454	
0.0010							
9	700	00:17:30	67.19%	68.00%	0.9540	0.9266	
0.0010							
10	750	00:18:44	67.19%	66.24%	0.9907	0.9674	
0.0010							
10	800	00:19:59	67.19%	69.32%	0.9006	0.8895	
0.0010							
11	850	00:21:13	68.55%	71.21%	1.0141	0.8429	
0.0010							
11	900	00:22:28	67.19%	72.00%	0.9094	0.8113	
0.0010							
12	950	00:23:42	72.07%	71.45%	0.7779	0.8314	
0.0010							
13	1000	00:24:56	69.53%	71.87%	0.8481	0.8128	
0.0010							
13	1050	00:26:11	71.29%	70.47%	0.7981	0.8714	
0.0010							
14	1100	00:27:25	74.02%	72.20%	0.7570	0.8164	
0.0010							
14	1150	00:28:40	73.24%	73.76%	0.7977	0.7711	
0.0010							
15	1200	00:29:54	73.63%	74.25%	0.7361	0.7520	
0.0010							
16	1250	00:31:08	77.73%	74.15%	0.6777	0.7562	
0.0010							
16	1300	00:32:22	72.66%	75.37%	0.8078	0.7201	
0.0010							
17	1350	00:33:36	75.59%	75.68%	0.7724	0.7068	
0.0010							
17	1400	00:34:50	75.98%	76.27%	0.7133	0.7029	
0.0010							
18	1450	00:36:04	75.20%	76.87%	0.7074	0.6885	
0.0010							
19	1500	00:37:18	71.48%	77.04%	0.7779	0.6740	
0.0010							
19	1550	00:38:32	75.98%	76.57%	0.6821	0.6965	
0.0010							
20	1600	00:39:46	78.71%	75.57%	0.6723	0.7495	
0.0010							
20	1650	00:41:00	76.17%	77.03%	0.6501	0.6822	
0.0010							
21	1700	00:42:14	77.73%	76.61%	0.6755	0.6961	

0.0010													
22		1750		00:43:29		80.47%		76.69%		0.5903		0.6787	
0.0010													
22		1800		00:44:43		78.71%		78.53%		0.6083		0.6350	
0.0010													
23		1850		00:45:57		76.76%		76.88%		0.7153		0.6905	
0.0010													
23		1900		00:47:11		76.56%		78.25%		0.6748		0.6467	
0.0010													
24		1950		00:48:25		81.84%		78.13%		0.5674		0.6835	
0.0010													
25		2000		00:49:39		78.71%		78.07%		0.5549		0.6560	
0.0010													
25		2050		00:50:53		80.86%		78.41%		0.5516		0.6459	
0.0010													
26		2100		00:52:08		79.69%		77.97%		0.6324		0.6510	
0.0010													
26		2150		00:53:22		78.32%		78.12%		0.6190		0.6611	
0.0010													
27		2200		00:54:36		81.64%		78.71%		0.5365		0.6301	
0.0010													
28		2250		00:55:51		77.73%		77.92%		0.6132		0.6678	
0.0010													
28		2300		00:57:05		80.66%		78.64%		0.5374		0.6289	
0.0010													
29		2350		00:58:19		81.05%		79.95%		0.6034		0.6107	
0.0010													
29		2400		00:59:34		85.74%		78.45%		0.4658		0.6574	
0.0010													
30		2450		01:00:48		80.66%		79.41%		0.5758		0.6080	
0.0010													
31		2500		01:02:03		82.81%		79.09%		0.5239		0.6284	
0.0010													
31		2550		01:03:17		82.42%		79.73%		0.5658		0.6017	
0.0010													
32		2600		01:04:31		81.05%		80.19%		0.5426		0.6025	
0.0010													
32		2650		01:05:46		82.03%		79.59%		0.5275		0.6171	
0.0010													
33		2700		01:07:00		82.81%		81.12%		0.5312		0.5785	
0.0010													
34		2750		01:08:15		80.47%		79.36%		0.5784		0.6150	
0.0010													
34		2800		01:09:29		79.69%		79.77%		0.5607		0.6057	
0.0010													
35		2850		01:10:43		82.42%		78.88%		0.4991		0.6532	
0.0010													
35		2900		01:11:58		81.45%		80.77%		0.5652		0.5843	
0.0010													
36		2950		01:13:12		82.03%		81.05%		0.5043		0.5763	
0.0010													
37		3000		01:14:26		85.16%		80.87%		0.4620		0.5881	
0.0010													
37		3050		01:15:40		81.84%		80.83%		0.5218		0.5819	
0.0010													
38		3100		01:16:56		85.35%		80.88%		0.4086		0.5834	
0.0010													
38		3150		01:18:10		83.79%		81.27%		0.4887		0.5780	
0.0010													
39		3200		01:19:25		81.25%		81.44%		0.5146		0.6004	
0.0010													
40		3250		01:20:40		82.03%		81.45%		0.4769		0.5755	
0.0010													
40		3300		01:21:54		84.38%		81.43%		0.4589		0.5587	
0.0010													
40		3320		01:22:28		83.59%		81.17%		0.4991		0.5806	
0.0010													



### 3.3 Evaluating the Network

Here we use the test partition of the dataset to evaluate the trained network.

#### 3.3.1 Classifying the Test Dataset

The line below will classify all images in the test dataset.

```
1 predicted_labels_3 = classify(trained_net_3, imds_test);
```

#### 3.3.2 Classification Performance

As the final step of this section, we plot the confusion matrix. The final performance of the network is 80.8% over the whole test dataset.

```
1 plotconfusion(imds_test.Labels, predicted_labels_3);
```

Confusion Matrix												
Output Class	airplane	863 8.6%	4 0.0%	78 0.8%	39 0.4%	25 0.3%	16 0.2%	12 0.1%	23 0.2%	51 0.5%	14 0.1%	76.7% 23.3%
	automobile	18 0.2%	926 9.3%	5 0.1%	11 0.1%	2 0.0%	7 0.1%	5 0.1%	8 0.1%	35 0.4%	77 0.8%	84.6% 15.4%
	bird	17 0.2%	1 0.0%	680 6.8%	50 0.5%	28 0.3%	26 0.3%	13 0.1%	10 0.1%	4 0.0%	3 0.0%	81.7% 18.3%
	cat	7 0.1%	1 0.0%	26 0.3%	549 5.5%	22 0.2%	101 1.0%	23 0.2%	20 0.2%	4 0.0%	2 0.0%	72.7% 27.3%
	deer	7 0.1%	1 0.0%	57 0.6%	55 0.5%	774 7.7%	31 0.3%	10 0.1%	29 0.3%	2 0.0%	1 0.0%	80.0% 20.0%
	dog	3 0.0%	2 0.0%	38 0.4%	120 1.2%	17 0.2%	739 7.4%	6 0.1%	21 0.2%	1 0.0%	1 0.0%	78.0% 22.0%
	frog	6 0.1%	3 0.0%	69 0.7%	86 0.9%	78 0.8%	28 0.3%	923 9.2%	9 0.1%	3 0.0%	5 0.1%	76.3% 23.7%
	horse	4 0.0%	0 0.0%	26 0.3%	33 0.3%	43 0.4%	34 0.3%	3 0.0%	867 8.7%	1 0.0%	6 0.1%	85.3% 14.7%
	ship	42 0.4%	6 0.1%	10 0.1%	31 0.3%	6 0.1%	9 0.1%	3 0.0%	3 0.0%	880 8.8%	10 0.1%	88.0% 12.0%
	truck	33 0.3%	56 0.6%	11 0.1%	26 0.3%	5 0.1%	9 0.1%	2 0.0%	10 0.1%	19 0.2%	881 8.8%	83.7% 16.3%
		86.3% 13.7%	92.6% 7.4%	68.0% 32.0%	54.9% 45.1%	77.4% 22.6%	73.9% 26.1%	92.3% 7.7%	86.7% 13.3%	88.0% 12.0%	88.1% 11.9%	80.8% 19.2%
	airplane	automobile	bird	cat	deer	dog	frog	horse	ship	truck		

## 4. Deleting Fully-Connected Layer 6

### 4.1 Defining Network Architecture

We define the layers of the network again as below. Fully-Connected layer 6 is deleted in comparison with question 1.

```
1  image_dim = [32 32 3];
2  kernel_dim = [3 3];
3  maxpool_dim = [2 2];
4  stride_conv_dim = [1 1];
5  stride_maxpool_dim = [2 2];
6
7  layers_4 = [
8      imageInputLayer(image_dim, 'Name', 'data')
9
10     convolution2dLayer(kernel_dim, 48, 'Name', 'conv1', 'BiasLearnRateFactor',
11         2, 'Stride', stride_conv_dim, 'Padding', 'same')
12     reluLayer('Name', 'relu1')
13     maxPooling2dLayer(maxpool_dim, 'Name', 'pool1', 'Stride', stride_maxpool_dim
14         )
15
16     convolution2dLayer(kernel_dim, 96, 'Name', 'conv2', 'BiasLearnRateFactor',
17         2, 'Stride', stride_conv_dim, 'Padding', 'same')
18     reluLayer('Name', 'relu2')
19     maxPooling2dLayer(maxpool_dim, 'Name', 'pool2', 'Stride', stride_maxpool_dim
20         )
21
22     convolution2dLayer(kernel_dim, 192, 'Name', 'conv3', 'BiasLearnRateFactor',
23         2, 'Stride', stride_conv_dim, 'Padding', 'same')
24     reluLayer('Name', 'relu3')
25
26     convolution2dLayer(kernel_dim, 192, 'Name', 'conv4', 'BiasLearnRateFactor',
27         2, 'Stride', stride_conv_dim, 'Padding', 'same')
28     reluLayer('Name', 'relu4')
29     maxPooling2dLayer(maxpool_dim, 'Name', 'pool4', 'Stride', stride_maxpool_dim
30         )
31
32     convolution2dLayer(kernel_dim, 256, 'Name', 'conv5', 'BiasLearnRateFactor',
33         2, 'Stride', stride_conv_dim, 'Padding', 'same')
34     reluLayer('Name', 'relu5')
35     maxPooling2dLayer(maxpool_dim, 'Name', 'pool5', 'Stride', stride_maxpool_dim
36         )
37
38     fullyConnectedLayer(256, 'Name', 'fc7', 'BiasLearnRateFactor', 2)
39     reluLayer('Name', 'relu7')
40     dropoutLayer(0.5, 'Name', 'drop7')
41 ]
```

```

33     fullyConnectedLayer(10, 'Name', 'softmax', 'BiasLearnRateFactor', 2)
34     softmaxLayer('Name', 'prob')
35
36     classificationLayer('Name', 'output')
37 ];
38
39 clear image_dim kernel_dim maxpool_dim stride_conv_dim stride_maxpool_dim
40
41 disp(layers_4);

```

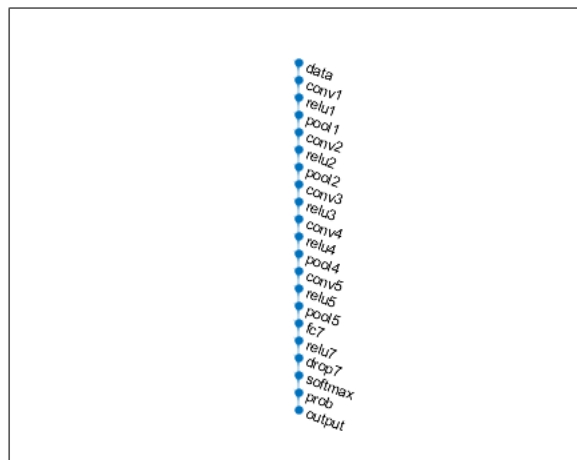
21x1 Layer array with layers:

1	'data'	Image Input	32x32x3 images with 'zerocenter' normalization
2	'conv1'	Convolution	48 3x3 convolutions with stride [1 1] and padding 'same'
3	'relu1'	ReLU	ReLU
4	'pool1'	Max Pooling	2x2 max pooling with stride [2 2] and padding [0 0 0 0]
5	'conv2'	Convolution	96 3x3 convolutions with stride [1 1] and padding 'same'
6	'relu2'	ReLU	ReLU
7	'pool2'	Max Pooling	2x2 max pooling with stride [2 2] and padding [0 0 0 0]
8	'conv3'	Convolution	192 3x3 convolutions with stride [1 1] and padding 'same'
9	'relu3'	ReLU	ReLU
10	'conv4'	Convolution	192 3x3 convolutions with stride [1 1] and padding 'same'
11	'relu4'	ReLU	ReLU
12	'pool4'	Max Pooling	2x2 max pooling with stride [2 2] and padding [0 0 0 0]
13	'conv5'	Convolution	256 3x3 convolutions with stride [1 1] and padding 'same'
14	'relu5'	ReLU	ReLU
15	'pool5'	Max Pooling	2x2 max pooling with stride [2 2] and padding [0 0 0 0]
16	'fc7'	Fully Connected	256 fully connected layer
17	'relu7'	ReLU	ReLU
18	'drop7'	Dropout	50% dropout
19	'softmax'	Fully Connected	10 fully connected layer
20	'prob'	Softmax	softmax
21	'output'	Classification Output	crossentropyex

```

1 %analyzeNetwork(layers_4);
2 plot(layerGraph(layers_4));

```



## 4.2 Learning Curves and Training Process

We trained the network on single GPU system nad print the results in a table every 50 iterations. Besides, the learning curves are plotted after the table. Finally the network reached 85.16% on training and 81.56% on validation subset. The training process took about 88 minutes long.

```
1 trained_net_4 = trainNetwork(augimdsTrain, layers_4, opts);
```

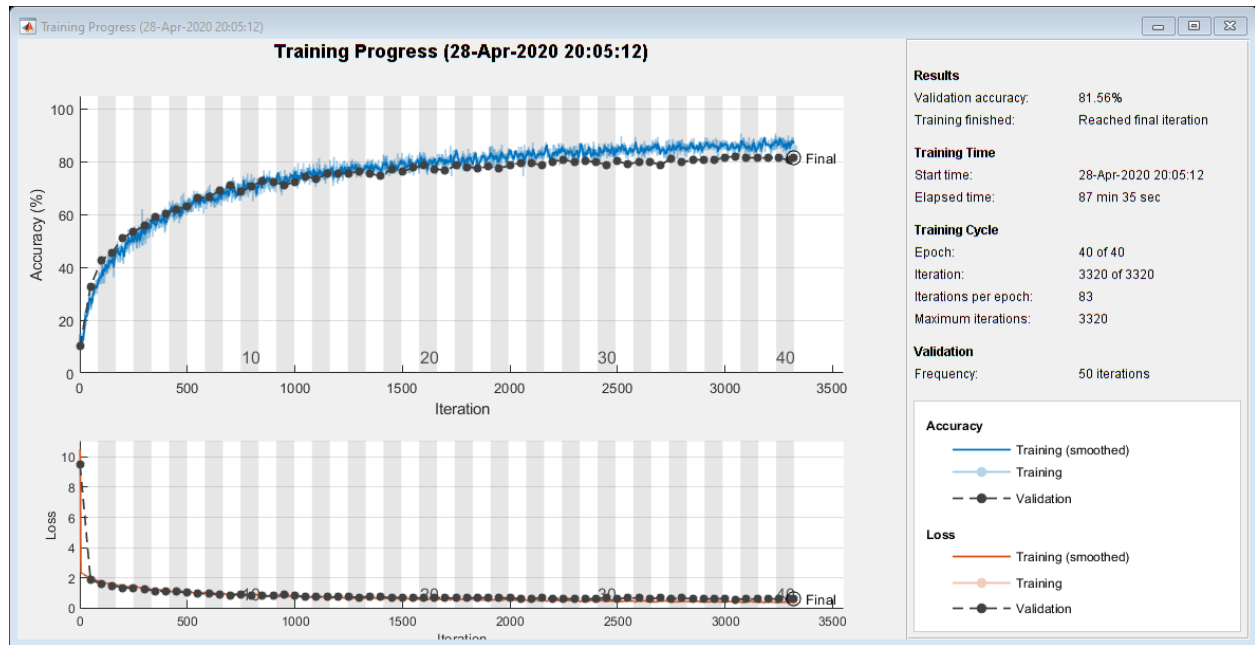
Training on single GPU.

Initializing input data normalization.

Epoch Learning	Iteration	Time Elapsed (hh:mm:ss)	Mini-batch Accuracy	Validation Accuracy	Mini-batch Loss	Validation Loss	Base Rate
1	1	00:00:09	11.72%	10.12%	10.5038	9.4881	
0.0010							
1	50	00:01:26	23.83%	32.83%	2.1314	1.8730	
0.0010							
2	100	00:02:44	38.28%	42.65%	1.7415	1.5924	
0.0010							
2	150	00:04:03	43.16%	45.68%	1.6198	1.4808	
0.0010							
3	200	00:05:23	43.95%	51.21%	1.5060	1.3415	
0.0010							
4	250	00:06:44	50.39%	53.56%	1.3679	1.3049	
0.0010							
4	300	00:08:03	53.32%	55.84%	1.3522	1.2311	
0.0010							
5	350	00:09:23	56.64%	59.04%	1.2368	1.1214	
0.0010							
5	400	00:10:42	55.86%	60.37%	1.2420	1.0968	
0.0010							
6	450	00:12:02	64.65%	62.09%	1.0527	1.0670	
0.0010							
7	500	00:13:21	65.63%	63.21%	1.0031	1.0294	
0.0010							
7	550	00:14:40	64.45%	66.41%	1.0214	0.9567	
0.0010							
8	600	00:15:59	66.80%	66.57%	0.9318	0.9426	
0.0010							
8	650	00:17:17	66.41%	69.12%	0.9867	0.8769	
0.0010							
9	700	00:18:36	71.29%	71.09%	0.8586	0.8371	
0.0010							
10	750	00:19:55	70.12%	68.80%	0.8572	0.8933	
0.0010							
10	800	00:21:13	69.53%	70.80%	0.8742	0.8329	
0.0010							
11	850	00:22:32	70.90%	72.91%	0.8471	0.7851	
0.0010							
11	900	00:23:50	74.22%	72.27%	0.7121	0.7916	
0.0010							
12	950	00:25:09	73.24%	71.33%	0.7878	0.8584	
0.0010							
13	1000	00:26:27	77.93%	72.17%	0.6161	0.8177	
0.0010							
13	1050	00:27:46	75.00%	74.36%	0.7175	0.7403	
0.0010							
14	1100	00:29:04	76.17%	73.64%	0.7260	0.7520	
0.0010							
14	1150	00:30:22	76.76%	75.37%	0.6979	0.7155	
0.0010							
15	1200	00:31:40	76.17%	75.59%	0.6442	0.7154	
0.0010							
16	1250	00:32:59	76.95%	75.53%	0.6579	0.7148	
0.0010							
16	1300	00:34:17	75.78%	76.36%	0.7088	0.7086	
0.0010							
17	1350	00:35:35	79.49%	75.55%	0.6131	0.7544	
0.0010							
17	1400	00:36:53	75.78%	74.63%	0.6773	0.7344	
0.0010							
18	1450	00:38:11	80.08%	77.29%	0.6093	0.6770	
0.0010							
19	1500	00:39:29	80.66%	76.27%	0.5871	0.6974	
0.0010							



19	1550	00:40:47	77.15%	77.79%	0.6782	0.6573
0.0010						
20	1600	00:42:05	79.10%	78.64%	0.6255	0.6601
0.0010						
20	1650	00:43:23	81.25%	77.33%	0.6001	0.6815
0.0010						
21	1700	00:44:42	77.93%	76.87%	0.6048	0.6655
0.0010						
22	1750	00:46:00	82.81%	78.67%	0.4991	0.6453
0.0010						
22	1800	00:47:25	77.73%	78.15%	0.6271	0.6564
0.0010						
23	1850	00:48:44	76.76%	77.64%	0.6390	0.6833
0.0010						
23	1900	00:50:03	82.42%	78.17%	0.5483	0.6655
0.0010						
24	1950	00:51:23	79.88%	77.65%	0.5369	0.6748
0.0010						
25	2000	00:52:43	82.42%	78.63%	0.5254	0.6525
0.0010						
25	2050	00:54:03	83.98%	79.60%	0.4554	0.6171
0.0010						
26	2100	00:55:22	83.59%	79.52%	0.4978	0.6169
0.0010						
26	2150	00:56:41	83.20%	78.80%	0.4724	0.6680
0.0010						
27	2200	00:57:59	82.81%	80.08%	0.5037	0.6214
0.0010						
28	2250	00:59:18	86.52%	80.93%	0.3928	0.6083
0.0010						
28	2300	01:00:37	86.13%	79.84%	0.4347	0.5991
0.0010						
29	2350	01:01:56	79.88%	80.29%	0.5154	0.6146
0.0010						
29	2400	01:03:14	83.20%	80.00%	0.5069	0.6028
0.0010						
30	2450	01:04:34	85.16%	78.81%	0.4108	0.6991
0.0010						
31	2500	01:05:53	83.01%	80.20%	0.4772	0.5975
0.0010						
31	2550	01:07:12	81.05%	79.15%	0.5888	0.6645
0.0010						
32	2600	01:08:31	84.57%	79.93%	0.4370	0.6453
0.0010						
32	2650	01:09:49	85.94%	80.13%	0.4144	0.6194
0.0010						
33	2700	01:11:08	85.55%	78.76%	0.4232	0.6549
0.0010						
34	2750	01:12:26	83.79%	81.27%	0.4577	0.5956
0.0010						
34	2800	01:13:45	84.57%	79.92%	0.4605	0.6482
0.0010						
35	2850	01:15:04	85.16%	80.64%	0.4686	0.6112
0.0010						
35	2900	01:16:23	85.35%	80.91%	0.4015	0.5787
0.0010						
36	2950	01:17:42	84.77%	80.65%	0.4368	0.6163
0.0010						
37	3000	01:19:01	86.52%	81.67%	0.3710	0.6021
0.0010						
37	3050	01:20:19	84.38%	82.09%	0.4289	0.5681
0.0010						
38	3100	01:21:38	87.11%	81.64%	0.3445	0.5873
0.0010						
38	3150	01:22:57	85.55%	81.47%	0.4172	0.5899
0.0010						
39	3200	01:24:15	86.13%	81.55%	0.4324	0.5927
0.0010						
40	3250	01:25:35	86.13%	81.41%	0.4079	0.6028
0.0010						
40	3300	01:26:53	84.96%	80.73%	0.4284	0.6104
0.0010						
40	3320	01:27:29	85.16%	81.56%	0.4182	0.6244
0.0010						



## 4.3 Evaluating the Network

Here we use the test partition of the dataset to evaluate the trained network.

### 4.3.1 Classifying the Test Dataset

The line below will classify all images in the test dataset.

```
1 predicted_labels_4 = classify(trained_net_4, imds_test);
```

### 4.3.2 Classification Performance

As the final step of this section, we plot the confusion matrix. The final performance of the network is 81.2% over the whole test dataset.

```
1 plotconfusion(imds_test.Labels, predicted_labels_4);
```

Confusion Matrix												
Output Class	airplane	872 8.7%	5 0.1%	39 0.4%	23 0.2%	11 0.1%	5 0.1%	5 0.1%	12 0.1%	72 0.7%	31 0.3%	81.1% 18.9%
	automobile	16 0.2%	939 9.4%	3 0.0%	4 0.0%	1 0.0%	5 0.1%	2 0.0%	1 0.0%	18 0.2%	104 1.0%	85.9% 14.1%
	bird	39 0.4%	1 0.0%	705 7.0%	39 0.4%	29 0.3%	27 0.3%	21 0.2%	13 0.1%	10 0.1%	6 0.1%	79.2% 20.8%
	cat	9 0.1%	2 0.0%	43 0.4%	600 6.0%	37 0.4%	102 1.0%	19 0.2%	20 0.2%	4 0.0%	6 0.1%	71.3% 28.7%
	deer	8 0.1%	2 0.0%	52 0.5%	54 0.5%	790 7.9%	33 0.3%	10 0.1%	34 0.3%	3 0.0%	1 0.0%	80.0% 20.0%
	dog	2 0.0%	2 0.0%	37 0.4%	135 1.4%	24 0.2%	734 7.3%	7 0.1%	23 0.2%	2 0.0%	2 0.0%	75.8% 24.2%
	frog	9 0.1%	6 0.1%	76 0.8%	93 0.9%	62 0.6%	45 0.4%	927 9.3%	9 0.1%	11 0.1%	8 0.1%	74.4% 25.6%
	horse	11 0.1%	3 0.0%	34 0.3%	37 0.4%	39 0.4%	46 0.5%	4 0.0%	882 8.8%	4 0.0%	16 0.2%	82.0% 18.0%
	ship	31 0.3%	16 0.2%	10 0.1%	9 0.1%	4 0.0%	3 0.0%	5 0.1%	2 0.0%	871 8.7%	25 0.3%	89.2% 10.8%
	truck	3 0.0%	24 0.2%	1 0.0%	6 0.1%	3 0.0%	0 0.0%	0 0.0%	4 0.0%	5 0.1%	801 8.0%	94.6% 5.4%
		87.2% 12.8%	93.9% 6.1%	70.5% 29.5%	60.0% 40.0%	79.0% 21.0%	73.4% 26.6%	92.7% 7.3%	88.2% 11.8%	87.1% 12.9%	80.1% 19.9%	81.2% 18.8%
	airplane	automobile	bird	cat	deer	dog	frog	horse	ship	truck		

## Appendix

### A.1 Saving Workspace Variables for Future Use

```
1 save('HW8_code_workspace.mat')
```

### A.2 Definition of Auxiliary Functions

```
1 function saveCIFAR10AsFolderOfImages(inputPath, outputPath, varargin)
2
3 % Check input directories are valid
4 if(~isempty(inputPath))
5     assert(exist(inputPath, 'dir') == 7);
6 end
7 if(~isempty(outputPath))
8     assert(exist(outputPath, 'dir') == 7);
9 end
10
11 % Check if we want to save each set with the same labels to its own
12 % directory.
13 if(isempty(varargin))
14     labelDirectories = false;
15 else
16     assert(nargin == 3);
17     labelDirectories = varargin{1};
18 end
19
20 % Set names for directories
21 trainDirectoryName = 'cifar10Train';
22 testDirectoryName = 'cifar10Test';
23 % Create directories for the output
24 mkdir(fullfile(outputPath, trainDirectoryName));
25 mkdir(fullfile(outputPath, testDirectoryName));
26
27 if(labelDirectories)
28     labelNames = {'airplane', 'automobile', 'bird', 'cat', 'deer', 'dog', 'frog', '
        horse', 'ship', 'truck'};
29     iMakeTheseDirectories(fullfile(outputPath, trainDirectoryName), labelNames);
30     iMakeTheseDirectories(fullfile(outputPath, testDirectoryName), labelNames);
31     for i = 1:5
32         iLoadBatchAndWriteAsImagesToLabelFolders(fullfile(inputPath, ['
            data_batch_' num2str(i) '.mat']), fullfile(outputPath,
            trainDirectoryName), labelNames, (i-1)*10000);
33     end
34     iLoadBatchAndWriteAsImagesToLabelFolders(fullfile(inputPath, 'test_batch.mat')
```

```

        ), fullfile(outputPath, testDirectoryName), labelNames, 0);
35 else
36     for i = 1:5
37         iLoadBatchAndWriteAsImages(fullfile(inputPath, ['data_batch_' num2str(i)
38             '.mat']), fullfile(outputPath, trainDirectoryName), (i-1)*10000);
39     end
40     iLoadBatchAndWriteAsImages(fullfile(inputPath, 'test_batch.mat'), fullfile(
41         outputPath, testDirectoryName), 0);
42 end
43 function iLoadBatchAndWriteAsImagesToLabelFolders(fullInputBatchPath,
44     fullOutputDirectoryPath, labelNames, nameIndexOffset)
45 load(fullfile(inputBatchPath));
46 data = data'; %ok<NODEF>
47 data = reshape(data, 32,32,3,[]);
48 data = permute(data, [2 1 3 4]);
49 for i = 1:size(data,4)
50     imwrite(data(:,:, :, i), fullfile(fullOutputDirectoryPath, labelNames{labels(i
51         )+1}, ['image' num2str(i + nameIndexOffset) '.png']));
52 end
53 end
54 function iLoadBatchAndWriteAsImages(fullInputBatchPath, fullOutputDirectoryPath,
55     nameIndexOffset)
56 load(fullfile(inputBatchPath));
57 data = data'; %ok<NODEF>
58 data = reshape(data, 32,32,3,[]);
59 data = permute(data, [2 1 3 4]);
60 for i = 1:size(data,4)
61     imwrite(data(:,:, :, i), fullfile(fullOutputDirectoryPath, ['image' num2str(i
62         + nameIndexOffset) '.png']));
63 end
64 end
65 function iMakeTheseDirectories(outputPath, directoryNames)
66 for i = 1:numel(directoryNames)
67     mkdir(fullfile(outputPath, directoryNames{i}));
68 end
69 end
70 function h = subplottight(n,m,i)
71 [c,r] = ind2sub([m n], i);
72 ax = subplot('Position', [(c-1)/m, 1-(r)/n, 1/m, 1/n]);
73 if(nargout > 0)
74     h = ax;
75 end
end

```