

## Using a Python Script in Spyder:

### 1. Explore and Read the Data File

Load the attached dataset file, "data\_mass\_raw.txt", into the script. Store its contents in appropriate NumPy variables.

*Hint:* This file contains time-series data (in days) of a mass-related quantity, referred to as  $x$ .

### 2. Data Analysis

- Determine the number of time data points.
- Display the following in the console:
  - Number of data points.
  - Minimum and maximum values of  $x$ .
  - The final time value (ensuring it is less than 500 days).

### 3. Data Visualization

Create a well-designed 1D plot to illustrate the data described above.

### 4. Model Implementation

Analyze the data using the given model:

$$\frac{dx}{dt} = a \cdot x \cdot \ln \left( \frac{K}{x} \right)$$

- Start with the constants  $a=0.07$  and  $K=700$ .
- Numerically solve  $x(t)$  using the algorithm :

$$x_{k+1} = x_k + \Delta t \cdot a \cdot x_k \cdot \ln \left( \frac{K}{x_k} \right)$$

- Parameters:
  - Time step:  $\Delta t=0.05$ .
  - Initial value:  $x_0=16$ .
- Compute  $x(t)$  values until the time matches the last point in the dataset.
- Overlay the approximation  $x(t)$  on the known data in a graph.

### 5. Interpolation

- With thousands of computed  $x$  values, use Scipy to interpolate them onto a less refined grid matching the dataset's time points.
- Ensure the interpolation creates a smooth curve with second derivative continuity.
- Plot the original data, the computed approximation, and the interpolated curve for comparison.

### 6. Solver Function

- Implement a function `mon_solver` that automates the numerical solution:
  - Inputs:  $a$ ,  $K$ ,  $x_0$ ,  $\Delta t$ .
  - Outputs: Approximated  $x$  values sampled at the dataset's time points.
- Test the function with the parameters  $a=0.07$ ,  $K=700$ ,  $x_0=16$ ,  $\Delta t=0.05$ .
- Plot the original data and the function's result for verification.