

1-

$$S_{\text{Coin}} = \{H, T\}$$

$$, S_{\text{die}} = \{1, 2, 3, 4, 5, 6\}$$

$$S = 2 \times 6 = 12$$

$$S = \{(H, 1), (H, 2), (H, 3), (H, 4), (H, 5), (H, 6), (T, 1), (T, 2), (T, 3), (T, 4), (T, 5), (T, 6)\}$$

a - Toss of the Coin

$$S_{\text{Coin}} = \{H, T\}$$

b - the throw of the die.

$$S_{\text{die}} = \{1, 2, 3, 4, 5, 6\}$$

c-

A (the event of head tossed). $\{H\}$

$$P(A) = \frac{N(A)}{N(S)} = \frac{1}{2}$$

B (the event that an odd number is thrown). $\{1, 3, 5\}$

$$P(B) = \frac{N(B)}{N(S)} = \frac{3}{6} = \frac{1}{2}$$

P(A ∩ B) (head and odd number)

$$P(A \cap B) = \frac{3}{12} = \frac{1}{4}$$

$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

$$= \frac{1}{2} + \frac{1}{2} - \frac{1}{4} = 1 - \frac{1}{4} = \frac{3}{4}$$

2-

$$\text{Since } P(S) = 1$$

$$(a) P(S) = P(B) + P(R) + P(Y) + P(G) + P(O) + P(T)$$

$$1 = 0.3 + 0.2 + 0.2 + 0.1 + 0.1 + P(T)$$

$$\boxed{P(T) = 0.1}$$

missing

(b)

i. brown or red one.

U

$$P(B \cup R) = P(B) + P(R) - P(B \cap R) =$$

$$0.3 + 0.2 = \boxed{0.5}$$

They are mutually-exclusive
cannot happen at the
same time

ii. You didn't get a yellow one.

B, R, G, O, T

yellow

$$\boxed{1 - P(Y) = 1 - 0.2 = 0.8}$$

iii. You don't get either an orange one or a tan one.

$$1 - P(O \cap T) = 1 - P(O) \cdot P(T)$$

$$= 1 - 0.1 \times 0.1$$

$$= 1 - 0.01$$

$$\boxed{= 0.99}$$

iv. You get one that is brown or red or yellow or green or orange or tan

$$P(B \cup R \cup Y \cup G \cup O \cup T)$$

$$= 0.3 + 0.2 + 0.2 + 0.1 + 0.1 + 0.1$$

$$= 0.9$$

3. Q, R are independent variables

$$P(Q) = 0.4, P(Q \text{ and } R) = 0.1$$

$$\uparrow$$

$$P(Q \cap R) = 0.1$$

$P(R)$?

Since they are independent, indeed they will be not mutually exclusive

$$P(Q \cap R) = P(Q) \cdot P(R)$$

$$0.1 = 0.4 \cdot P(R)$$

$$P(R) = \frac{0.1}{0.4} = \frac{1}{4}$$

mutually-exclusive events \rightarrow disjoint (अलग-अलग)

(Can't happen at the same time)

they will be dependent, always

\rightarrow because the idea of being can't happen at the same time.

(they are affect each other)

not mutually exclusive events \rightarrow can be (dependent, independent)

dependent \rightarrow drawing a card from a deck without replacement

independent \rightarrow Tossing a coin and rolling a die.

4.

Since $Pr(A)$ not zero, $Pr(B)$ not zero.

(they are Independent (because no one will affect the other).

and IF they Independent they Can't be mutually exclusive, so they will be \rightarrow (not mutually exclusive)

$(I, M) \rightarrow$ impossible.

IF they are Independent (don't Mutually exclusive

(Can't happen at the same time) so they are affecting each other, Independent. (مؤثرين لبعضهما البعض)

$(NI, M) \rightarrow$ Possible, Permissible.

Tossing a Coin

We Can't have both (H, T) at the same time (mutually exclusive).

and they are (NI) because they affect each other, by IF one happen the other can happen at the same time

$(I, NM) \rightarrow$ Possible, Permissible.

rolling 2 dice

The idea of having 1 at the first die, and 2 at the second die is Possible, so they are not mutually exclusive (because they can happen at the same time).

and they are Independent because IF we have 1 at the first die won't affect the second die.

Date: / /

object: _____

(NI, NH) → Possible, Permissible

(A) → Pick a Card without replacement

(B) → " " " " " "

→ They are not mutually exclusive because they can happen at the same time

→ and they are not independent because if one happens will affect the other.

5.

i. P(musician is a female)

$$P(F) = \frac{N(F)}{N(S)} = \frac{72}{130} = \boxed{\frac{36}{65}}$$

ii. P(musician is a male AND had private instruction)

$$= \frac{15}{130} = \boxed{\frac{3}{26}}$$

iii. P(musician is a female or is self-taught)

$$P(F) = \frac{36}{65}$$

$$P(S) = \frac{31}{130}$$

$$P(F \cup S) = \frac{36}{65} + \frac{31}{130} - \frac{12}{130}$$

$$= \boxed{\frac{7}{10}}$$