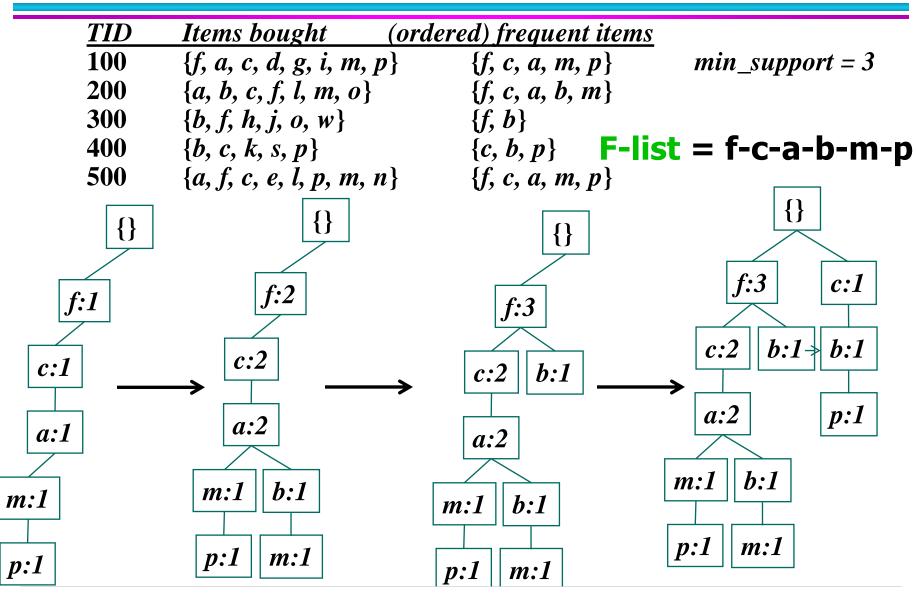
Association Rule Mining

Dr. Faisal Kamiran

FP-growth Algorithm

- Use a compressed representation of the database using an FP-tree
- Once an FP-tree has been constructed, it uses a recursive divide-and-conquer approach to mine the frequent itemsets
- Steps:
 - FP tree construction
 - Conditional pattern base construction
 - Conditional FP-trees
 - Frequent pattern generation

FP-Tree Construction



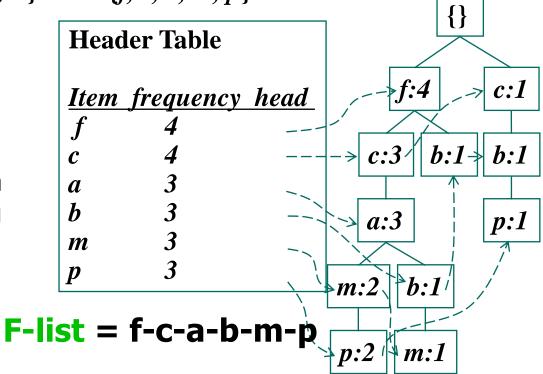
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FP-Tree Construction

<u>TID</u>	Items bought (ordered) frequent items	
100	$\{f, a, c, d, g, i, m, p\}$	$\{f, c, a, m, p\}$	
200	$\{a, b, c, f, l, m, o\}$	$\{f, c, a, b, m\}$	
300	$\{b, f, h, j, o, w\}$	{ <i>f</i> , <i>b</i> }	min_support = 3
400	$\{b, c, k, s, p\}$	$\{c, b, p\}$	
500	$\{a, f, c, e, \overline{l}, p, m, n\}$	$\{f, c, a, m, p\}$	\square

- Scan DB once, find frequent 1-itemset (single item pattern)
- 2. Sort frequent items in frequency descending order, f-list
- 3. Scan DB again, construct FP-tree

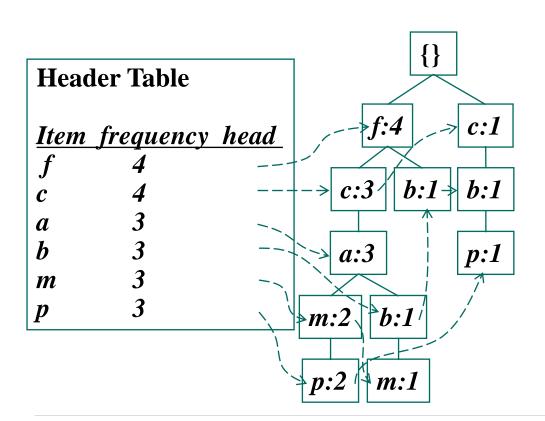


Partition Patterns and Databases

- Frequent patterns can be partitioned into subsets according to f-list
 - F-list = f-c-a-b-m-p
 - Patterns containing p
 - Patterns having m but no p
 - **–** ...
 - Patterns having c but no a nor b, m, p
 - Pattern f
- Completeness and non-redundency

Conditional Pattern Base Construction

Conditional Pattern Base is a sub-database which consists of the set of prefix paths in the FP tree co-occurring with the suffix pattern or item. For example prefix paths (fcam, cb) of item p to form p's conditional pattern base.

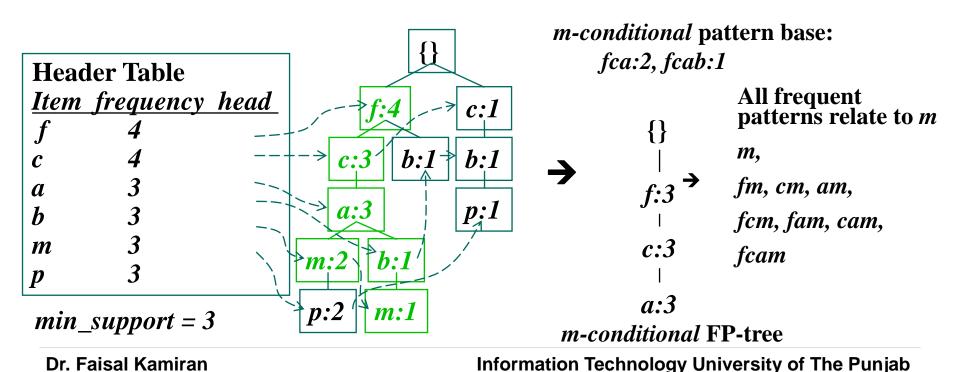


Conditional pattern bases

<u>item</u>	cond. pattern base
c	<i>f</i> :3
a	fc:3
b	fca:1, f:1, c:1
m	fca:2, fcab:1
p	fcam:2, cb:1

From Conditional Pattern-bases to Conditional FP-trees

- For each pattern-base
 - Accumulate the count for each item in the base
 - Construct the FP-tree for the frequent items of the pattern base



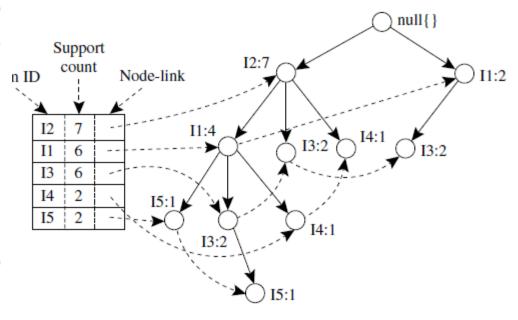
FP Growth: Example

Min supp=2

Data:

TID List of item_IDs T100 11, 12, 15 T200 I2, I4 12, 13 T300 T400 11, 12, 14 T500 I1, I3 T600 I2, I3 T700 I1, I3 T800 11, 12, 13, 15 11, 12, 13 T900

FP Tree:



Mining the FP-Tree

Item	Conditional Pattern Base	Conditional FP-tree	Frequent Patterns Generated
I5	{{I2, I1: 1}, {I2, I1, I3: 1}}	⟨I2: 2, I1: 2⟩	{I2, I5: 2}, {I1, I5: 2}, {I2, I1, I5: 2}
I 4			
I3			
I1			

Benefits of the FP-tree Structure

Completeness

- Preserve complete information for frequent pattern mining
- Never break a long pattern of any transaction
- Compactness
 - Reduce irrelevant info—infrequent items are gone
 - Items in frequency descending order: the more frequently occurring, the more likely to be shared
 - Never be larger than the original database (not count node-links and the *count* field)

ECLAT

For each item, store a list of transaction ids (tids)

Horizontal Data Layout

TID	Items
1	A,B,E
2	B,C,D
3	C,E
4	A,C,D
5	A,B,C,D
6	A,E
7	A,B
8	A,B,C
9	A,C,D
10	В

Vertical Data Layout

Α	В	С	D	Е
1	1	2	2	1
4	2	2 3 4	2 4 5 9	3 6
5	5		5	6
6	2 5 7 8	8 9	9	
7	8	9		
4 5 6 7 8 9	10			
9				

† TID-list

ECLAT

Determine support of any k-itemset by intersecting tid-lists of two of its (k-1) subsets.

Α		В		AB
1		1		1
4		2		5
5	^	5	\rightarrow	7
6		7		8
7		8		
8		10		
9				

- □ 3 traversal approaches:
 - top-down, bottom-up and hybrid
- Advantage: very fast support counting
- Disadvantage: intermediate tid-lists may become too large for memory

Rule Generation

- □ Given a frequent itemset L, find all non-empty subsets f ⊂ L such that f → L − f satisfies the minimum confidence requirement
 - If {A,B,C,D} is a frequent itemset, candidate rules:

ABC
$$\rightarrow$$
D, ABD \rightarrow C, ACD \rightarrow B, BCD \rightarrow A, A \rightarrow BCD, B \rightarrow ACD, C \rightarrow ABD, D \rightarrow ABC AB \rightarrow CD, AC \rightarrow BD, AD \rightarrow BC, BC \rightarrow AD, BD \rightarrow AC, CD \rightarrow AB,

□ If |L| = k, then there are $2^k - 2$ candidate association rules (ignoring $L \to \emptyset$ and $\emptyset \to L$)

Rule Generation

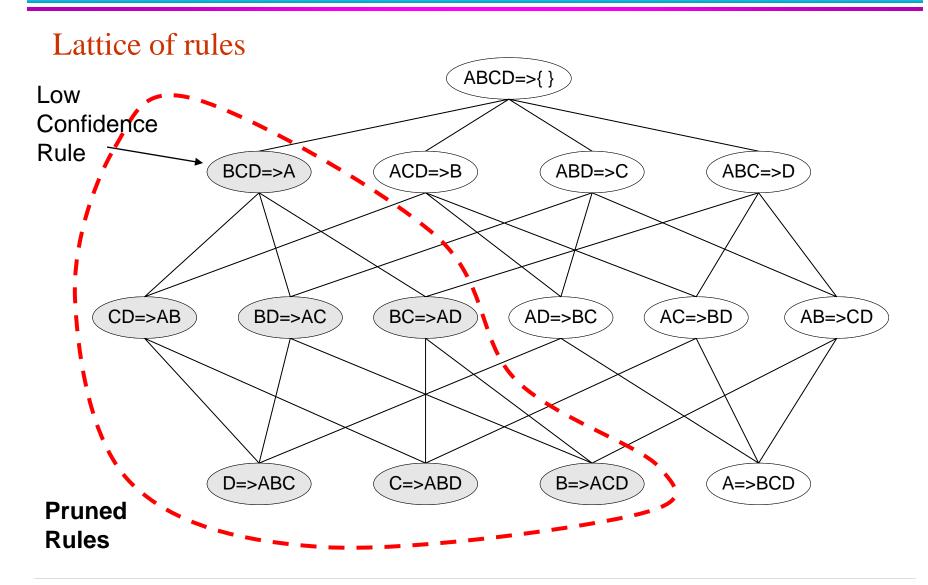
- How to efficiently generate rules from frequent itemsets?
 - In general, confidence does not have an antimonotone property

 $c(ABC \rightarrow D)$ can be larger or smaller than $c(AB \rightarrow D)$

- But confidence of rules generated from the same itemset has an anti-monotone property
- e.g., L = {A,B,C,D}:

$$c(ABC \rightarrow D) \ge c(AB \rightarrow CD) \ge c(A \rightarrow BCD)$$

Rule Generation for Apriori Algorithm

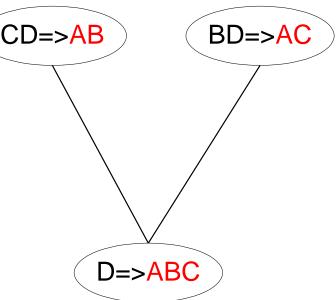


Rule Generation for Apriori Algorithm

 Candidate rule is generated by merging two rules that share the same prefix in the rule consequent

i join(CD=>AB,BD=>AC)
would produce the candidate
rule D => ABC

 Prune rule D=>ABC if its subset CD=>AB does not have high confidence



Pattern Evaluation

- Association rule algorithms tend to produce too many rules
 - many of them are uninteresting or redundant
 - Redundant if {A,B,C} → {D} and {A,B} → {D} have same support & confidence
- Interestingness measures can be used to prune/rank the derived patterns

In the original formulation of association rules, support & confidence are the only measures used

Computing Interestingness Measure

 \square Given a rule X \rightarrow Y, information needed to compute rule interestingness can be obtained from a contingency table

Contingency table for $X \rightarrow Y$

	Υ	$\overline{\gamma}$	
X	f ₁₁	f ₁₀	f ₁₊
X	f ₀₁	f ₀₀	f _{o+}
	f ₊₁	f ₊₀	Τ

f₁₁: support of X and Y

 f_{10} : support of X and \overline{Y}

f₀₁: support of X and Y

f₀₀: support of X and Y

Used to define various measures

support, confidence, lift, Gini, J-measure, etc.

Drawback of Confidence

	Coffee	Coffee	
Tea	15	5	20
Tea	75	5	80
	90	10	100

Association Rule: Tea → Coffee

- Confidence= P(Coffee|Tea) = 0.75
- but P(Coffee) = 0.9
- Although confidence is high, rule is misleading
- P(Coffee|Tea) = 0.9375

Statistical-based Measures

Measures that take into account statistical dependence

$$Lift = \frac{P(Y \mid X)}{P(Y)}$$

Example: Lift/Interest

	Coffee	Coffee	
Tea	15	5	20
Tea	75	5	80
	90	10	100

Association Rule: Tea → Coffee

Confidence = P(Coffee|Tea) = 0.75

but P(Coffee) = 0.9

 \Rightarrow Lift = 0.75/0.9= 0.8333 (< 1, therefore is negatively associated)