

## More dynamic memory

In addition to new, we also have delete  
delete - let system know this memory  
is no longer in use.

- Almost always, a call to new  
should have a corresponding call  
to delete somewhere afterward.

Example: allocate array of variable size:

```
int* A = new int[n];
```

```
A[0] = ....
```

```
;
```

```
// done with A; let libc know:
```

```
delete [] A;
```

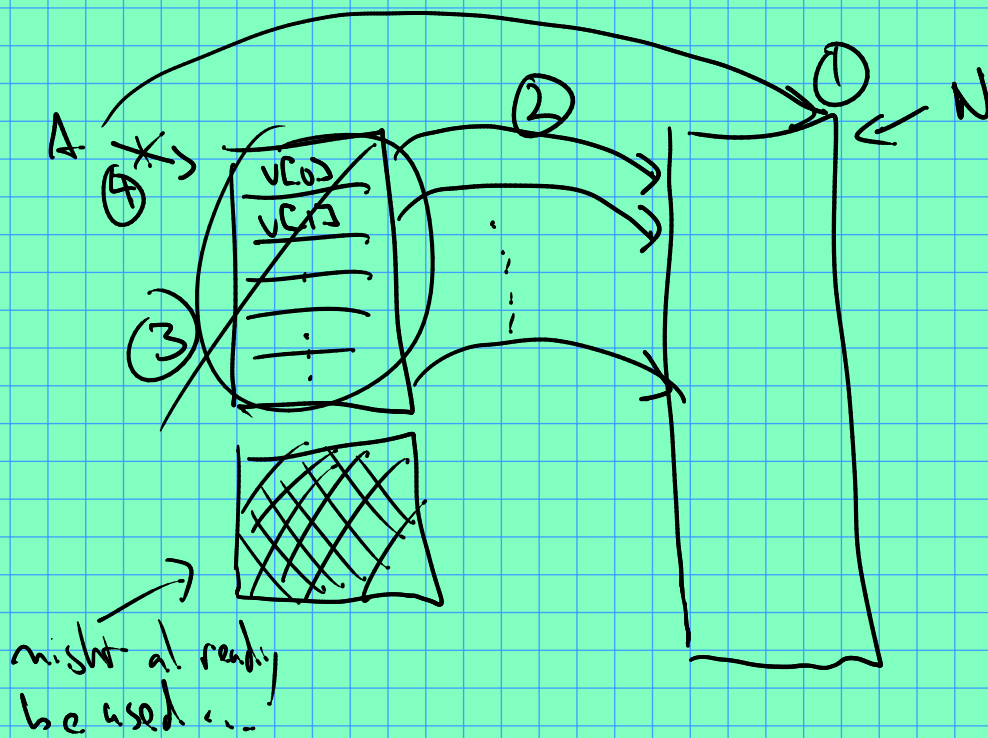
use these whenever you delete an array.

Exercise: how do vectors grow?

Seems to double the allocation (capacity)  
Whenever it runs out of space.

Question: How many steps are required to  
perform  $n$  push-backs into  
an initially empty vector?  
How about if the size only grew  
by 1 (instead of doubling)?

Before we can figure this out, how is the vector being grown?



To allocate more space:

- ① Make a new array.
- ② Copy elements from old to new
- ③ delete the old one!
- ④ redirect pointer  $A$ .

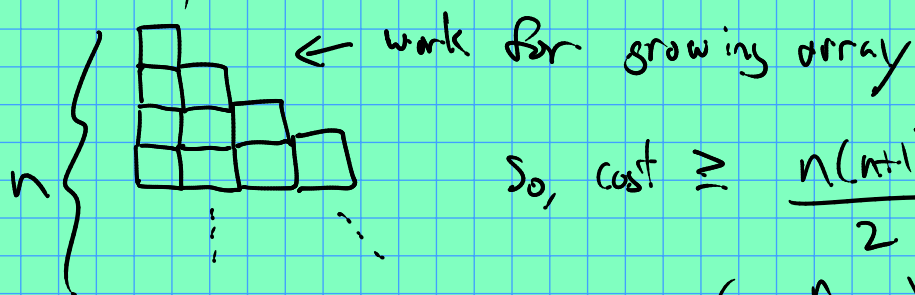
Let's put this into a function:

```
void growArray(int*& A, int size, int newSize)
{
    int* N = new int[newSize]; // ①
    // we assume newSize > size...
    for (int i = 0; i < size; i++) // ②
        N[i] = A[i];
    delete[] A; // ③
    A = N;
}
```

Back to our question:

Cost for  $n$  consecutive push-back?

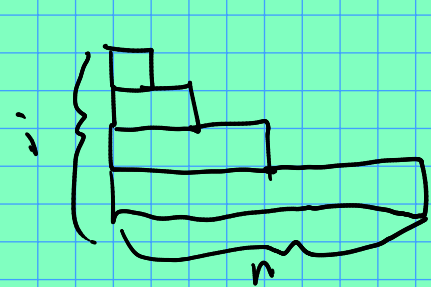
Say we did  $\text{size}++$  instead of  $\text{size} \times 2$ ?



$$\text{So, cost} \geq \frac{n(n+1)}{2}$$

$$\left( = \sum_{i=1}^n i \right)$$

Now what if we do  $\text{size} \times 2$ ?



$$\approx \sum_{i=0}^{\log n} 2^i =$$

$$\frac{(1-2)(1+2+2^2+2^3+\dots+2^k)}{(1-2)}$$

$$= \frac{(1-2) + (2-2^2) + (2^2-2^3) + \dots + (2^k-2^{k+1})}{1-2}$$

$$= \frac{1-2^{k+1}}{1-2} = 2^{k+1} - 1$$

But our  $k \approx \log n$ .

So, cost of reallocation (total, after  $n$  push-back calls)

$$\approx 2^{\log_2 n + 1} - 1 = 2n - 1$$

