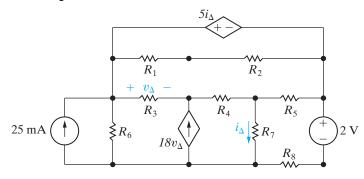
# **Problems**

#### Section 4.1

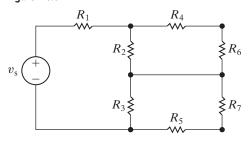
**4.1** For the circuit shown in Fig. P4.1, state the numerical value of the number of (a) branches, (b) branches where the current is unknown, (c) essential branches, (d) essential branches where the current is unknown, (e) nodes, (f) essential nodes, and (g) meshes.

Figure P4.1



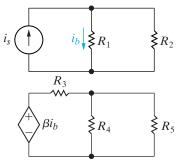
- **4.2** a) If only the essential nodes and branches are identified in the circuit in Fig. P4.1, how many simultaneous equations are needed to describe the circuit?
  - b) How many of these equations can be derived using Kirchhoff's current law?
  - c) How many must be derived using Kirchhoff's voltage law?
  - d) What two meshes should be avoided in applying the voltage law?
- **4.3** Assume the voltage  $v_s$  in the circuit in Fig. P4.3 is known. The resistors  $R_1 R_7$  are also known.
  - a) How many unknown currents are there?
  - b) How many independent equations can be written using Kirchhoff's current law (KCL)?
  - c) Write an independent set of KCL equations.
  - d) How many independent equations can be derived from Kirchhoff's voltage law (KVL)?
  - e) Write a set of independent KVL equations.

Figure P4.3



- **4.4** A current leaving a node is defined as positive.
  - a) Sum the currents at each node in the circuit shown in Fig. P4.3.
  - b) Show that any one of the equations in (a) can be derived from the remaining three equations.
- **4.5** a) How many separate parts does the circuit in Fig. P4.5 have?
  - b) How many nodes?
  - c) How many branches are there?
  - d) Assume that the lower node in each part of the circuit is joined by a single conductor. Repeat the calculations in (a)–(c).

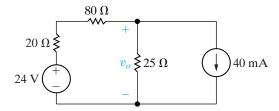
Figure P4.5



## **Section 4.2**

**4.6** Use the node-voltage method to find  $v_o$  in the circuit in Fig. P4.6.

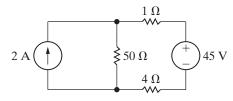
Figure P4.6



- **4.7** a) Find the power developed by the 40 mA current source in the circuit in Fig. P4.6.
  - b) Find the power developed by the 24 V voltage source in the circuit in Fig. P4.6.
  - c) Verify that the total power developed equals the total power dissipated.
- **4.8** A 50  $\Omega$  resistor is connected in series with the 40 mA current source in the circuit in Fig. P4.6.
  - a) Find  $v_o$ .
  - b) Find the power developed by the 40 mA current source.

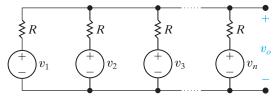
- c) Find the power developed by the 24 V voltage
- d) Verify that the total power developed equals the total power dissipated.
- e) What effect will any finite resistance connected in series with the 40 mA current source have on the value of  $v_o$ ?
- **4.9** Use the node-voltage method to find how much power the 2 A source extracts from the circuit in MULTISIM Fig. P4.9.

Figure P4.9



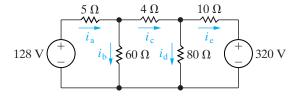
- **4.10** a) Use the node-voltage method to show that the output voltage  $v_o$  in the circuit in Fig. P4.10 is MULTISIM equal to the average value of the source voltages.
  - b) Find  $v_o$  if  $v_1 = 100 \text{ V}$ ,  $v_2 = 80 \text{ V}$ , and  $v_3 = -60 \text{ V}.$

Figure P4.10



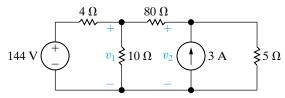
- **4.11** a) Use the node-voltage method to find the **PSPICE** branch currents  $i_a - i_e$  in the circuit shown in MULTISIM Fig. P4.11.
  - b) Find the total power developed in the circuit.

Figure P4.11



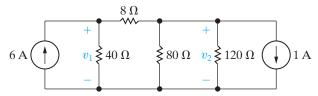
**4.12** Use the node-voltage method to find  $v_1$  and  $v_2$  in the circuit in Fig. P4.12. MULTISIM

Figure P4.12



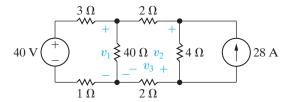
**4.13** Use the node-voltage method to find  $v_1$  and  $v_2$  in PSPICE the circuit shown in Fig. P4.13. MULTISIM

Figure P4.13



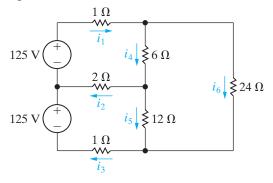
- **4.14** a) Use the node-voltage method to find  $v_1$ ,  $v_2$ , and **PSPICE**  $v_3$  in the circuit in Fig. P4.14.
  - b) How much power does the 40 V voltage source deliver to the circuit?

Figure P4.14



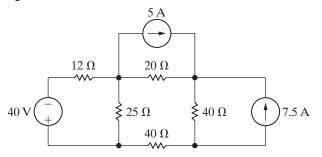
- **4.15** The circuit shown in Fig. P4.15 is a dc model of a PSPICE residential power distribution circuit. MULTISIM
  - a) Use the node-voltage method to find the branch currents  $i_1 - i_6$ .
  - b) Test your solution for the branch currents by showing that the total power dissipated equals the total power developed.

Figure P4.15



**4.16** Use the node-voltage method to find the total power PSPICE dissipated in the circuit in Fig. P4.16. MULTISIN

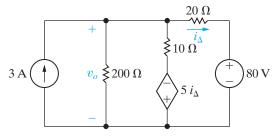
Figure P4.16



PSPICE MULTISIN

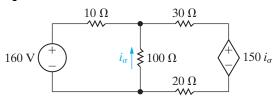
- **4.17** a) Use the node-voltage method to find  $v_o$  in the circuit in Fig. P4.17.
  - b) Find the power absorbed by the dependent source.
  - c) Find the total power developed by the independent sources.

Figure P4.17



**4.18** Use the node-voltage method to calculate the power delivered by the dependent voltage source in the circuit in Fig. P4.18.

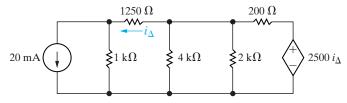
Figure P4.18



4.19 a) Use the node-voltage method to find the total PSPICE power developed in the circuit in Fig. P4.19. MULTISIN

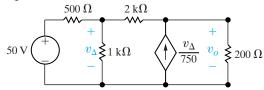
b) Check your answer by finding the total power absorbed in the circuit.

Figure P4.19



- **4.20** a) Use the node voltage method to find  $v_o$  for the circuit in Fig. P4.20.
  - b) Find the total power supplied in the circuit.

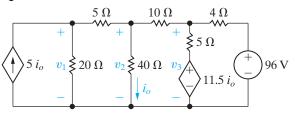
Figure P4.20



**4.21** a) Find the node voltages  $v_1$ ,  $v_2$ , and  $v_3$  in the cir-PSPICE cuit in Fig. P4.21. MULTISIN

b) Find the total power dissipated in the circuit.

Figure P4.21

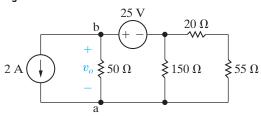


### **Section 4.4**

**PSPICE** MULTISIM

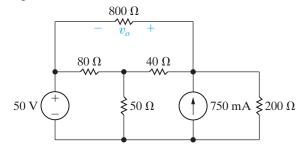
- **4.22** a) Use the node-voltage method to find  $v_o$  and the power delivered by the 2 A current source in the circuit in Fig. P4.22. Use node a as the reference node.
  - b) Repeat part (a), but use node b as the reference node.
  - c) Compare the choice of reference node in (a) and (b). Which is better, and why?

Figure P4.22



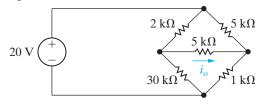
Use the node-voltage method to find the value of  $v_o$ in the circuit in Fig. P4.23. **PSPICE** MULTISIM

Figure P4.23



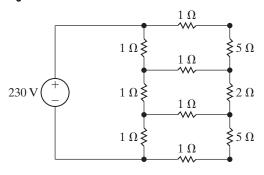
Use the node-voltage method to find  $i_o$  in the cir-4.24 cuit in Fig. P4.24. MULTISIM

Figure P4.24



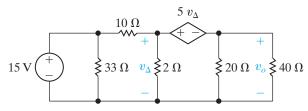
- **4.25** a) Use the node-voltage method to find the power dissipated in the 2  $\Omega$  resistor in the circuit in Fig. P4.25.
  - b) Find the power supplied by the 230 V source.

Figure P4.25



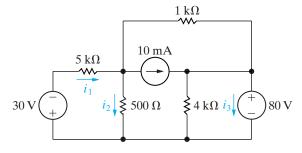
**4.26** Use the node-voltage method to find  $v_o$  in the circuit in Fig. P4.26.

Figure P4.26



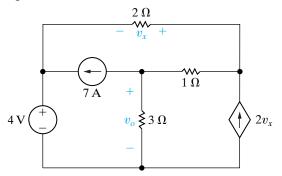
- **4.27** a) Use the node-voltage method to find the branch currents  $i_1$ ,  $i_2$ , and  $i_3$  in the circuit in Fig. P4.27.
  - b) Check your solution for  $i_1$ ,  $i_2$ , and  $i_3$  by showing that the power dissipated in the circuit equals the power developed.

Figure P4.27



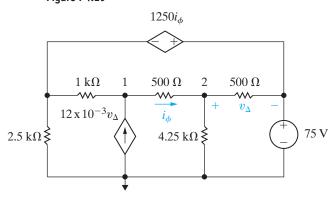
**4.28** Use the node-voltage method to find the value of  $v_o$  in the circuit in Fig. P4.28.

Figure P4.28



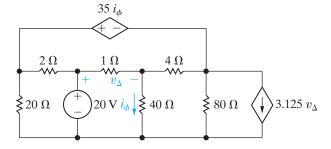
- **4.29** Assume you are a project engineer and one of your staff is assigned to analyze the circuit shown in Fig. P4.29. The reference node and node numbers given on the figure were assigned by the analyst. Her solution gives the values of  $v_1$  and  $v_2$  as 105 V and 85 V, respectively.
  - a) What values did the analyst use for the left-most and right-most node voltages when writing KCL equations at nodes 1 and 2?
  - b) Use the values supplied by the analyst to calculate the total power developed in the circuit and the total power dissipated in the circuit.
  - c) Do you agree with the solution submitted by the analyst?

Figure P4.29



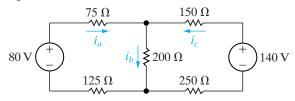
**4.30** Use the node-voltage method to find the power developed by the 20~V source in the circuit in Fig. P4.30.

Figure P4.30



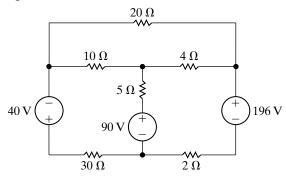
- **4.31** Show that when Eqs. 4.16, 4.17, and 4.19 are solved for  $i_B$ , the result is identical to Eq. 2.25.
- **4.32** a) Use the mesh-current method to find the branch currents  $i_a$ ,  $i_b$ , and  $i_c$  in the circuit in Fig. P4.32.
  - b) Repeat (a) if the polarity of the 140 V source is reversed.

Figure P4.32



- **4.33** Solve Problem 4.11 using the mesh-current method.
- **4.34** Solve Problem 4.15 using the mesh-current method.
- **4.35** Solve Problem 4.24 using the mesh-current method.
- **4.36** a) Use the mesh-current method to find the total power developed in the circuit in Fig. P4.36.
  - b) Check your answer by showing that the total power developed equals the total power dissipated.

Figure P4.36

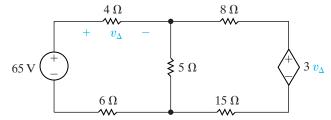


**4.37** Solve Problem 4.25 using the mesh-current method.

#### **Section 4.6**

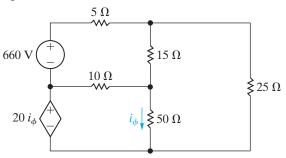
- **4.38** Solve Problem 4.18 using the mesh-current method.
- **4.39** Use the mesh-current method to find the power dissipated in the 15  $\Omega$  resistor in the circuit in Fig. P4.39.

Figure P4.39



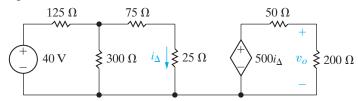
**4.40** Use the mesh-current method to find the power delivered by the dependent voltage source in the circuit seen in Fig. P4.40.

Figure P4.40



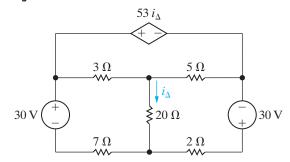
- **4.41** a) Use the mesh-current method to find  $v_o$  in the circuit in Fig. P4.41.
  - b) Find the power delivered by the dependent source.

Figure P4.41



**4.42** Use the mesh-current method to find the power developed in the dependent voltage source in the circuit in Fig. P4.42.

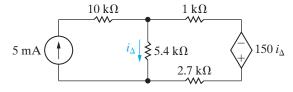
Figure P4.42



### **Section 4.7**

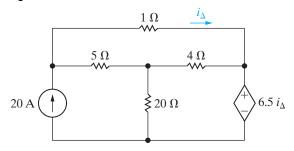
- **4.43** a) Use the mesh-current method to solve for  $i_{\Delta}$  in the circuit in Fig. P4.43.
  - b) Find the power delivered by the independent current source.
  - c) Find the power delivered by the dependent voltage source.

Figure P4.43



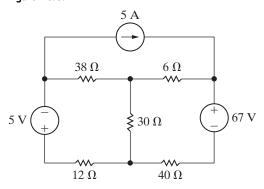
- **4.44** Solve Problem 4.13 using the mesh-current method.
- **4.45** Solve Problem 4.21 using the mesh-current method.
- **4.46** Use the mesh-current method to find the total power developed in the circuit in Fig. P4.46.

Figure P4.46



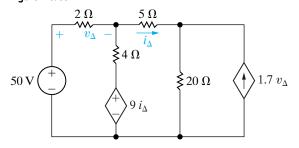
- **4.47** a) Use the mesh-current method to find how much power the 5 A current source delivers to the circuit in Fig. P4.47.
  - b) Find the total power delivered to the circuit.
  - c) Check your calculations by showing that the total power developed in the circuit equals the total power dissipated

Figure P4.47



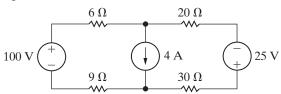
- **4.48** a) Use the mesh-current method to determine which sources in the circuit in Fig. P4.48 are generating power.
  - b) Find the total power dissipated in the circuit.

Figure P4.48



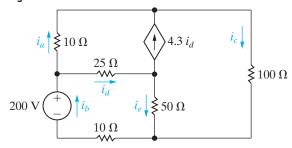
**4.49** Use the mesh-current method to find the total power dissipated in the circuit in Fig. P4.49.

Figure P4.49



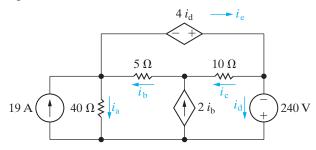
- **4.50** a) Assume the 100 V source in the circuit in Fig. P4.49 is changed to 67.5 V. Find the total power dissipated in the circuit.
  - b) Repeat (a) with the 4 A current source replaced by a short circuit.
  - c) Explain why the answers to (a) and (b) are the same.
  - c) Now assume you wish to change the value of the 25 V source, instead of the 100 V source, in the circuit in Fig. P4.49 to get the same power dissipated by the current source that you found in (a) and (b). Use the results in part (c) to calculate the new value of this voltage source.
- **4.51** Solve Problem 4.27 using the mesh-current method.
- **4.52** a) Use the mesh-current method to find the branch currents in  $i_a i_e$  in the circuit in Fig. P4.52.
  - b) Check your solution by showing that the total power developed in the circuit equals the total power dissipated.

Figure P4.52



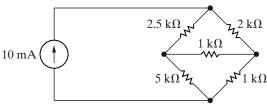
- **4.53** a) Find the branch currents  $i_a i_e$  for the circuit shown in Fig. P4.53.
  - b) Check your answers by showing that the total power generated equals the total power dissipated.

Figure P4.53



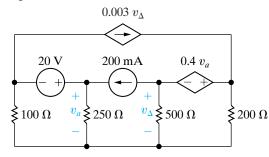
- **4.54** Assume you have been asked to find the power dissipated in the horizontal  $1 k\Omega$  resistor in the MULTISIM circuit in Fig. P4.54.
  - a) Which method of circuit analysis would you recommend? Explain why.
  - b) Use your recommended method of analysis to find the power dissipated in the horizontal 1 k $\Omega$ resistor.
  - c) Would you change your recommendation if the problem had been to find the power developed by the 10 mA current source? Explain.
  - d) Find the power delivered by the 10 mA current source.

Figure P4.54



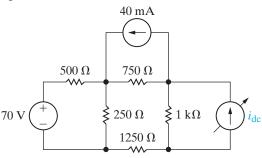
- **4.55** A 4 k $\Omega$  resistor is placed in parallel with the 10 mA current source in the circuit in Fig. P4.54. Assume you have been asked to calculate the power developed by the current source.
  - a) Which method of circuit analysis would you recommend? Explain why.
  - b) Find the power developed by the current source.
- PSPICE MULTISIM
- **4.56** a) Would you use the node-voltage or mesh-current method to find the power absorbed by the 20 V source in the circuit in Fig. P4.56? Explain your choice.
  - b) Use the method you selected in (a) to find the power.

Figure P4.56



- **4.57** The variable dc current source in the circuit in Fig. P4.57 is adjusted so that the power developed MULTISIM by the 40 mA current source is zero. You want to find the value of  $i_{dc}$ .
  - a) Would you use the node-voltage or mesh-current method to find  $i_{dc}$ ? Explain your choice.
  - b) Use the method selected in (a) to find  $i_{dc}$ .

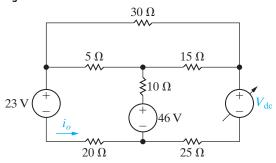
Figure P4.57



The variable dc voltage source in the circuit in PSPICE Fig. P4.58 is adjusted so that  $i_o$  is zero. MULTISIM

- a) Would you use the node-voltage or mesh-current method to find  $V_{dc}$ ? Explain your choice.
- b) Find the value of  $V_{\rm dc}$ , using the method selected
- c) Check your solution by showing the power developed equals the power dissipated.

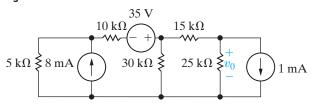
Figure P4.58



#### **Section 4.9**

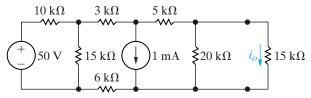
- **4.59** a) Make a series of source transformations to find the voltage  $v_0$  in the circuit in Fig. P4.59.
  - b) Verify your solution using the mesh-current method.

Figure P4.59



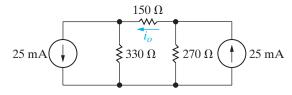
- a) Find the current  $i_0$  in the circuit in Fig. P4.60 PSPICE by making a succession of appropriate source MULTISIM transformations.
  - b) Using the result obtained in (a), work back through the circuit to find the power developed by the 50 V source.

Figure P4.60



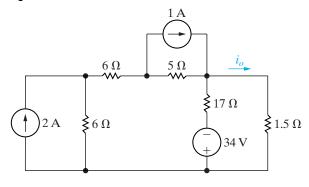
- MULTISIM
- **4.61** a) Use source transformations to find the current  $i_o$ in the circuit in Fig. P4.61.
  - b) Verify your solution by using the node-voltage method to find  $i_o$ .

Figure P4.61



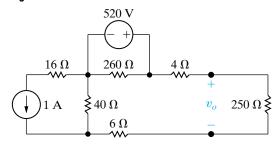
- MULTISIM
- **4.62** a) Use a series of source transformations to find  $i_0$ in the circuit in Fig. P4.62.
  - b) Verify your solution by using the mesh-current method to find  $i_o$ .

Figure P4.62



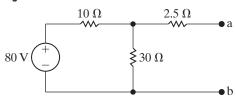
- **PSPICE** MULTISIM
- **4.63** a) Use source transformations to find  $v_o$  in the circuit in Fig. P4.63.
  - b) Find the power developed by the 520 V source.
  - c) Find the power developed by the 1 A current source.
  - d) Verify that the total power developed equals the total power dissipated.

Figure P4.63



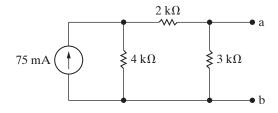
**4.64** Find the Thévenin equivalent with respect to the **PSPICE** terminals a,b for the circuit in Fig. P4.64. MULTISIM

Figure P4.64



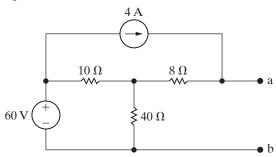
4.65 Find the Norton equivalent with respect to the terminals a,b for the circuit in Fig. P4.65.

Figure P4.65



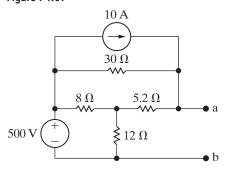
**4.66** Find the Norton equivalent with respect to the terpspice minals a,b for the circuit in Fig. P4.66.

Figure P4.66



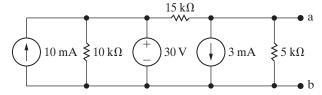
Find the Thévenin equivalent with respect to the **PSPICE** terminals a,b for the circuit in Fig. P4.67. MULTISIM

Figure P4.67



Find the Norton equivalent with respect to the ter-4.68 **PSPICE** minals a,b in the circuit in Fig. P4.68. MULTISIM

Figure P4.68



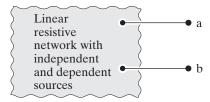
4.69 A Thévenin equivalent can also be determined from measurements made at the pair of terminals of interest. Assume the following measurements were made at the terminals a,b in the circuit in Fig. P4.69.

> When a 20  $\Omega$  resistor is connected to the terminals a,b, the voltage  $v_{\rm ab}$  is measured and found to be 100 V.

> When a 50  $\Omega$  resistor is connected to the terminals a,b, the voltage is measured and found to be 200 V.

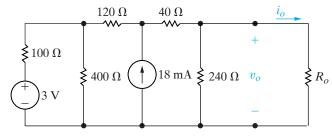
> Find the Thévenin equivalent of the network with respect to the terminals a,b.

Figure P4.69



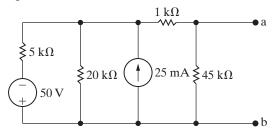
- **4.70** An automobile battery, when connected to a car radio, provides 12.5 V to the radio. When connected to a set of headlights, it provides 11.7 V to the headlights. Assume the radio can be modeled as a 6.25  $\Omega$ resistor and the headlights can be modeled as a  $0.65~\Omega$  resistor. What are the Thévenin and Norton equivalents for the battery?
- **4.71** Determine  $i_o$  and  $v_o$  in the circuit shown in Fig. P4.71 when  $R_o$  is a resistor from Appendix H MULTISIM such that  $100 \Omega \leq R_o < 200 \Omega$ .

Figure P4.71



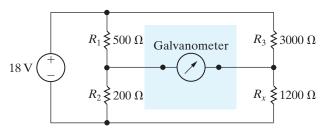
- **4.72** A voltmeter with a resistance of 85.5 k $\Omega$  is used to PSPICE measure the voltage  $v_{\rm ab}$  in the circuit in Fig. P4.72. MULTISIM
  - a) What is the voltmeter reading?
  - b) What is the percentage of error in the voltmeter reading if the percentage of error is defined as  $[(measured - actual)/actual] \times 100?$

Figure P4.72



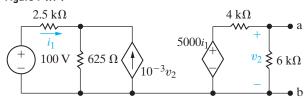
**4.73** The Wheatstone bridge in the circuit shown in **PSPICE** Fig. P4.73 is balanced when  $R_3$  equals 3000  $\Omega$ . If the MULTISIN galvanometer has a resistance of 50  $\Omega$ , how much current will the galvanometer detect, when the bridge is unbalanced by setting  $R_3$  to 3003  $\Omega$ ? (Hint: Find the Thévenin equivalent with respect to the galvanometer terminals when  $R_3 = 3003 \Omega$ . Note that once we have found this Thévenin equivalent, it is easy to find the amount of unbalanced current in the galvanometer branch for different galvanometer movements.)

Figure P4.73



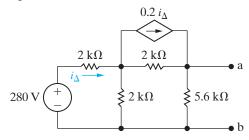
**4.74** Determine the Thévenin equivalent with respect to the terminals a,b for the circuit shown in MULTISIM Fig. P4.74.

Figure P4.74



**4.75** Find the Norton equivalent with respect to the terminals a,b for the circuit seen in Fig. P4.75.

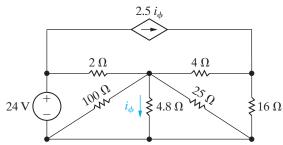
Figure P4.75



**4.76** When an ammeter is used to measure the current  $i_{\phi}$  in the circuit shown in Fig. P4.76, it reads 6 A.

- a) What is the resistance of the ammeter?
- b) What is the percentage of error in the current measurement?

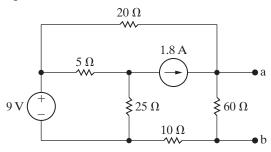
Figure P4.76



## **Section 4.11**

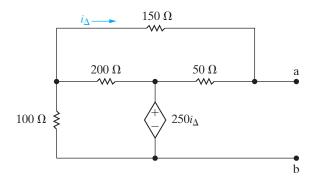
- **4.77** a) Find the Thévenin equivalent resistance with respect to the terminals a,b in the circuit in Fig. P4.64 without finding either the open circuit voltage or the short circuit current.
  - b) Find the Norton equivalent resistance with respect to the terminals a,b in the circuit in Fig. P4.66 without finding either the open circuit voltage or the short circuit current.
- **4.78** a) Find the Thévenin equivalent with respect to the terminals a,b for the circuit in Fig. P4.78 by finding the open-circuit voltage and the short-circuit current.
  - b) Solve for the Thévenin resistance by removing the independent sources. Compare your result to the Thévenin resistance found in (a).

Figure P4.78



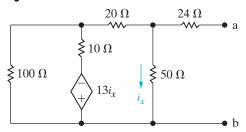
**4.79** Find the Thévenin equivalent with respect to the terminals a,b in the circuit in Fig. P4.79.

Figure P4.79



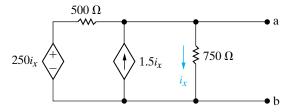
**4.80** Find the Thévenin equivalent with respect to the terminals a,b in the circuit in Fig. P4.80.

Figure P4.80



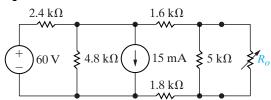
**4.81** Find the Norton equivalent with respect to the terminals a,b for the circuit seen in Fig. P4.81.

Figure P4.81



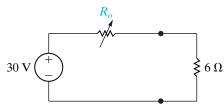
- **4.82** The variable resistor in the circuit in Fig. P4.82 is adjusted for maximum power transfer to  $R_o$ .
  - a) Find the value of  $R_o$ .
  - b) Find the maximum power that can be delivered to  $R_o$ .
  - c) Find a resistor in Appendix H closest to the value in part (a). How much power is delivered to this resistor?

Figure P4.82



- **4.83** What percentage of the total power developed in the circuit in Fig. P4.82 is delivered to  $R_o$  when  $R_o$  is set for maximum power transfer?
- **4.84** a) Calculate the power delivered for each value of  $R_o$  used in Problem 4.71.
  - b) Plot the power delivered to  $R_o$  versus the resistance  $R_o$ .
  - c) At what value of  $R_o$  is the power delivered to  $R_o$  a maximum?
- **4.85** a) Find the value of the variable resistor  $R_o$  in the circuit in Fig. P4.85 that will result in maximum power dissipation in the 6  $\Omega$  resistor. (*Hint:* Hasty conclusions could be hazardous to your career.)
  - b) What is the maximum power that can be delivered to the 6  $\Omega$  resistor?

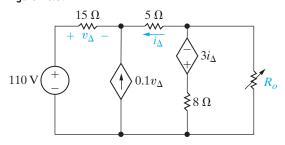
Figure P4.85



- **4.86** A variable resistor  $R_o$  is connected across the terminals a,b in the circuit in Fig. P4.75. The variable resistor is adjusted until maximum power is transferred to  $R_o$ .
  - a) Find the value of  $R_o$ .
  - b) Find the maximum power delivered to  $R_o$ .
  - c) Find the percentage of the total power developed in the circuit that is delivered to  $R_o$ .

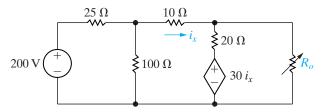
- d) Find the resistor from Appendix H closest in value to the  $R_o$  from part (a).
- e) Find the percentage of the total power developed in the circuit that is delivered to the resistor in part (d).
- **4.87** The variable resistor  $(R_o)$  in the circuit in Fig. P4.87 is adjusted until it absorbs maximum power from the circuit.
  - a) Find the value of  $R_o$ .
  - b) Find the maximum power.
  - c) Find the percentage of the total power developed in the circuit that is delivered to  $R_o$ .

Figure P4.87



**4.88** The variable resistor  $(R_o)$  in the circuit in Fig. P4.88 is adjusted until the power dissipated in the resistor is 250 W. Find the values of  $R_o$  that satisfy this condition.

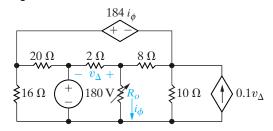
Figure P4.88



**4.89** The variable resistor in the circuit in Fig. P4.89 is adjusted for maximum power transfer to  $R_o$ .

- a) Find the numerical value of  $R_o$ .
- b) Find the maximum power delivered to  $R_o$ .
- c) How much power does the 180 V source deliver to the circuit when  $R_o$  is adjusted to the value found in (a)?

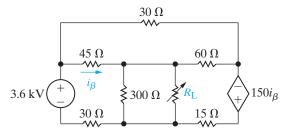
Figure P4.89



**4.90** The variable resistor  $(R_{\rm L})$  in the circuit in Fig. P4.90 is adjusted for maximum power transfer to  $R_{\rm L}$ .

- a) Find the numerical value of  $R_{\rm L}$ .
- b) Find the maximum power transferred to  $R_{\rm L}$ .

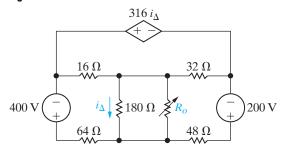
Figure P4.90



**4.91** The variable resistor  $(R_o)$  in the circuit in Fig. P4.91 is adjusted for maximum power transfer to  $R_o$ .

- a) Find the value of  $R_o$ .
- b) Find the maximum power that can be delivered to  $R_o$ .
- c) What percentage of the total power developed in the circuit is delivered to  $R_o$  found in part(a)?
- d) If  $R_o$  is selected from Appendix H, which resistor value will result in the greatest amount of power delivered to  $R_o$ ?

Figure P4.91

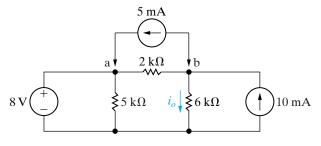


#### Section 4.13

**4.92** a) In the circuit in Fig. P4.92, before the 5 mA current source is attached to the terminals a,b, the current  $i_o$  is calculated and found to be 3.5 mA. Use superposition to find the value of  $i_o$  after the current source is attached.

b) Verify your solution by finding  $i_o$  when all three sources are acting simultaneously.

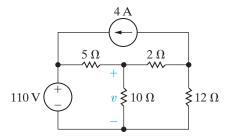
Figure P4.92



**4.93** a) Use the principle of superposition to find the voltage v in the circuit of Fig. P4.93.

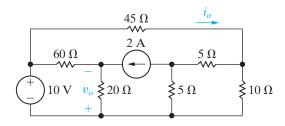
b) Find the power dissipated in the 10  $\Omega$  resistor.

Figure P4.93



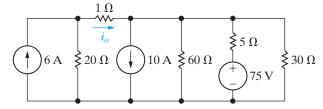
**4.94** Use superposition to solve for  $i_o$  and  $v_o$  in the circuit in Fig. P4.94.

Figure P4.94



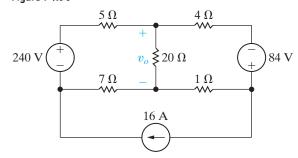
**4.95** Use the principle of superposition to find the current  $i_o$  in the circuit shown in Fig. P4.95.

Figure P4.95



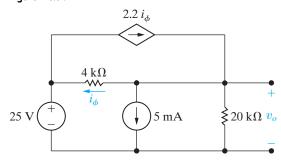
**4.96** Use the principle of superposition to find the voltage  $v_o$  in the circuit in Fig. P4.96.

Figure P4.96



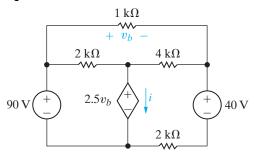
**4.97** Use the principle of superposition to find  $v_o$  in the circuit in Fig. P4.97.

Figure P4.97



**4.98** Use the principle of superposition to find the Current i in the circuit of Fig. P4.98.

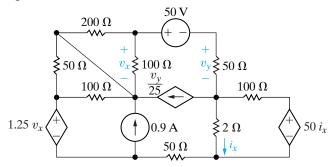
Figure P4.98



## **Sections 4.1–4.13**

- **4.99** Assume your supervisor has asked you to determine the power developed by the 50 V source in the circuit in Fig. P4.99. Before calculating the power developed by the 50 V source, the supervisor asks you to submit a proposal describing how you plan to attack the problem. Furthermore, he asks you to explain why you have chosen your proposed method of solution.
  - a) Describe your plan of attack, explaining your reasoning.
  - b) Use the method you have outlined in (a) to find the power developed by the 50 V source.

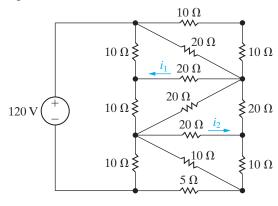
Figure P4.99



**4.100** Find  $i_1$  and  $i_2$  in the circuit in Fig. P4.100.

PSPICE MULTISIM

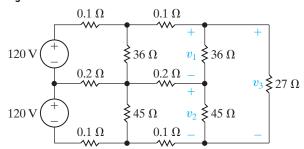
Figure P4.100



**4.101** Find  $v_1$ ,  $v_2$ , and  $v_3$  in the circuit in Fig. P4.101.

PSPICE MULTISIM

Figure P4.101



- **4.102** Two ideal dc voltage sources are connected by electrical conductors that have a resistance of r  $\Omega/m$ , as shown in Fig. P4.102. A load having a resistance of R  $\Omega$  moves between the two voltage sources. Let x equal the distance between the load and the source  $v_1$ , and let L equal the distance between the sources.
  - a) Show that

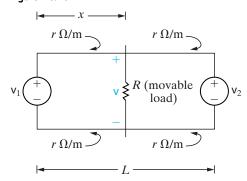
$$v = \frac{v_1 RL + R(v_2 - v_1)x}{RL + 2rLx - 2rx^2}.$$

b) Show that the voltage v will be minimum when

$$x = \frac{L}{v_2 - v_1} \left[ -v_1 \pm \sqrt{v_1 v_2 - \frac{R}{2rL} (v_1 - v_2)^2} \right].$$

- c) Find x when L=16 km,  $v_1=1000$  V,  $v_2=1200$  V, R=3.9  $\Omega$ , and  $r=5\times 10^{-5}$   $\Omega/\mathrm{m}$ .
- d) What is the minimum value of v for the circuit of part (c)?

Figure P4.102



4.103 Laboratory measurements on a dc voltage source yield a terminal voltage of 75 V with no load connected to the source and 60 V when loaded with a  $20~\Omega$  resistor.

- a) What is the Thévenin equivalent with respect to the terminals of the dc voltage source?
- b) Show that the Thévenin resistance of the source is given by the expression

$$R_{\rm Th} = \left(\frac{v_{\rm Th}}{v_o} - 1\right) R_{\rm L},$$

where

 $v_{\rm Th}$  = the Thévenin voltage,

 $v_o$  = the terminal voltage corresponding to the load resistance  $R_{\rm L}$ .

**4.104** For the circuit in Fig. 4.69 derive the expressions for the sensitivity of  $v_1$  and  $v_2$  to changes in the source currents  $I_{g1}$  and  $I_{g2}$ .

**4.105** Assume the nominal values for the components in the circuit in Fig. 4.69 are:  $R_1 = 25~\Omega$ ;  $R_2 = 5~\Omega$ ;  $R_3 = 50~\Omega$ ;  $R_4 = 75~\Omega$ ;  $I_{g1} = 12~\mathrm{A}$ ; and  $I_{g2} = 16~\mathrm{A}$ . Predict the values of  $v_1$  and  $v_2$  if  $I_{g1}$  decreases to 11 A and all other components stay at their nominal values. Check your predictions using a tool like PSpice or MATLAB.

**4.106** Repeat Problem 4.105 if  $I_{g2}$  increases to 17 A, and all other components stay at their nominal values. Check your predictions using a tool like PSpice or MATLAB.

**4.107** Repeat Problem 4.105 if  $I_{g1}$  decreases to 11 A and Perspective PSPICE  $I_{g2}$  increases to 17 A. Check your predictions using a tool like PSpice or MATLAB.

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**4.108** Use the results given in Table 4.2 to predict the values of  $v_1$  and  $v_2$  if  $R_1$  and  $R_3$  increase to 10% above their nominal values and  $R_2$  and  $R_4$  decrease to 10% below their nominal values.  $I_{g1}$  and  $I_{g2}$  remain at their nominal values. Compare your predicted values of  $v_1$  and  $v_2$  with their actual values.