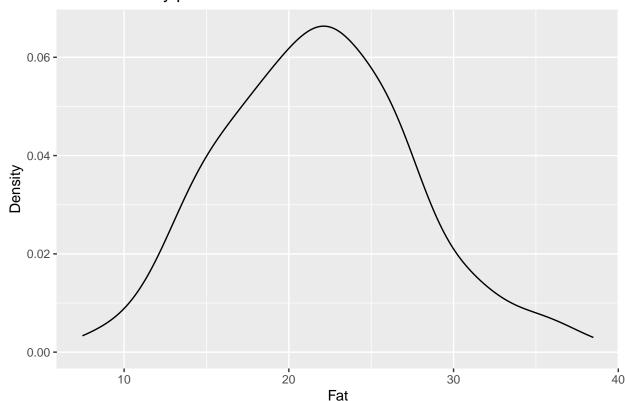
Statistical re-analysis plan: Predicting body fat proportion using anthropometric measures

Mariana Nold

```
library(mfp2)
library(rstanarm)
library(projpred)
library(ggplot2)
library(loo)
library(bayesplot)
library(bayesrules)
library(FBMS)
women <- read.delim("C:/Users/zo95yup/Documents/GitHub/Bayes_for_STRATOS/Task Bodyfat/Datafiles/BodyFat
names(women)
Load R packages
## [1] "Obs"
                  "Fat"
                            "Weight" "Height"
                                                "BMI"
                                                          "Age"
                                                                    "Neck"
## [8] "Chest"
                  "Calf"
                            "Biceps" "Hips"
                                                "Waist"
                                                          "Forearm" "PThigh"
                            "Wrist"
                                      "Knee"
## [15] "MThigh" "DThigh"
                                                "Elbow"
                                                          "Ankle"
PPath2 <- "C:/Users/zo95yup/Nextcloud/Statistik_SoSe24/Forschung/STRATOS/P6/Code_A/Results"
fat_density <- density(women$Fat, na.rm = TRUE)</pre>
ggplot(women, aes(x = Fat)) + geom_density() +
  labs(title = "Kernel-density plot for outcome fat", x = "Fat", y = "Density")
```

Kernel-density plot for outcome fat



```
Prepare data
summary(women$Fat)
##
     Min. 1st Qu.
                 Median
                          Mean 3rd Qu.
                                         Max.
     7.47
           17.61
                  21.64
                          21.76
                                 25.73
                                        38.49
summary(women$Age)
##
     Min. 1st Qu.
                 Median
                          Mean 3rd Qu.
                                         Max.
##
     1.00
           19.00
                  20.00
                          20.39
                                 21.00
                                        25.00
women<- women[women$Age != 1, ]</pre>
women[,3:20] <- scale(women[,3:20])</pre>
head(women)
##
    Obs
         Fat
                 Weight
                           Height
                                        BMI
                                                  Age
                                                           Neck
                                                                    Chest
      1 23.07 -1.29458090 -0.9359529 -0.9574982 0.9702795 -1.7434463 -1.3798033
      2 29.50 0.08151288 -1.5820137
                                  1.0776639
                                            0.9702795 -0.1839318 0.3526427
## 3
      3 26.99 0.35673163 -0.8498114 0.9208569 0.3269420 -0.4438509 -0.2042149
      4 20.25 -0.85423089 0.2269566 -1.0444077 -0.3163955 -0.9636891 -1.0859062
## 5
      5 19.95 -0.08361838 1.0883711 -0.6631153 -0.3163955 0.6608052 -0.1268736
## 6
      6 26.02 0.96221290 -0.9359529 1.6864004
                                            2.2569544
                                                      1.6355018 1.8530647
##
         Calf
                  Biceps
                              Hips
                                       Waist
                                               Forearm
                                                          PThigh
                                                                    MThigh
## 1 -0.9068981 -0.66317114 -1.0960084 -1.0337620 -1.5610578 -1.1012185 -0.5462338
## 4 -0.4052487 -1.15056197 -1.0471407 -0.9251101 -1.2474066 -1.1012185 -0.8417572
## 5 -0.1265545 -0.98809836 -0.6073309 -0.6922846 -1.5610578 -0.4248155 -0.3492182
## 6 0.5144420 1.28639220 1.3148007 1.1392756 0.9481524 1.0407242 0.7589945
```

```
DThigh
                    Wrist
                                 Knee
                                           Elbow
## 1 -0.68363710 -0.6889801 -1.1572958 -1.1260785 -1.2200455
## 2 -0.12699377 0.1614979 -0.4658936 -0.4966577 0.5177452
## 3 -0.40531544 -1.3268386 -0.2930431 0.3215893 -0.9178210
## 4 -0.68363710 -1.2205288 -0.2930431 -0.7484260 -0.9933771
## 5 0.01216707 -0.9015996 -1.1572958 0.3845314 -0.2378160
## 6 0.98629291 1.8624538 1.4354624 1.0139522 0.8955257
model1_f <- formula(Fat ~ fp(Waist, df = 2) + fp(Height, df = 2) + fp(Weight, df = 2))
model1 <- mfp2(model1_f, data = women, verbose=TRUE)</pre>
Derive reference model
##
## i Initial degrees of freedom:
## Waist Height Weight
## df 2
              2
##
## i Visiting order: Weight, Height, Waist
## -----
## i Running MFP Cycle 1
## -----
##
## Variable: Weight (keep = FALSE)
##
                             DF
                                                                Deviance diff.
                   Powers
                                   Deviance
                                               Versus
## FP1
                   0.5
                             6
                                   992.1
## null
                   NA
                                   1013.6
                                               FP1
                                                                21.6
                             4
                                   989.2
                                               FP1
## linear
                   1
                             5
                                                                -2.9
##
                   P-value
## FP1
                   0.0000
## null
## linear
                   1.0000
## Selected: linear
##
## Variable: Height (keep = FALSE)
##
                   Powers
                             DF
                                   Deviance
                                               Versus
                                                                Deviance diff.
## FP1
                             6
                                   988.5
## null
                   NA
                             4
                                   1010.0
                                               FP1
                                                                21.5
                             5
                                   989.2
                                               FP1
## linear
                   1
                                                                0.6
                   P-value
##
## FP1
## null
                   0.0000
## linear
                   0.4315
## Selected: linear
## Variable: Waist (keep = FALSE)
                   Powers
                             DF
                                               Versus
                                                                Deviance diff.
                                   Deviance
## FP1
                             6
                   2
                                   988.8
## null
                             4
                                   999.5
                                               FP1
                                                                10.7
                   NA
## linear
                   1
                             5
                                   989.2
                                               FP1
                                                                0.4
##
                   P-value
```

FP1 ## null

0.0046

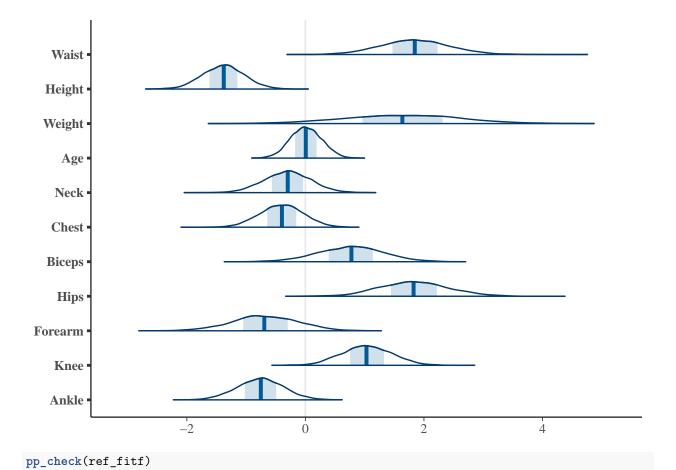
```
## linear
                   0.5445
## Selected: linear
## -----
## i Running MFP Cycle 2
## -----
## Variable: Weight (keep = FALSE)
##
                   Powers
                             DF
                                   Deviance
                                               Versus
                                                                Deviance diff.
## FP1
                   0.5
                             6
                                   992.1
## null
                   NA
                             4
                                   1013.6
                                               FP1
                                                                21.6
                                   989.2
                                               FP1
## linear
                             5
                                                                -2.9
                   1
                   P-value
## FP1
                   0.0000
## null
## linear
                   1.0000
## Selected: linear
## Variable: Height (keep = FALSE)
                   Powers
                             DF
                                   Deviance
                                               Versus
                                                                Deviance diff.
## FP1
                   2
                             6
                                   988.5
## null
                             4
                                   1010.0
                                               FP1
                                                                21.5
                                   989.2
## linear
                             5
                                               FP1
                                                                0.6
                   1
                   P-value
## FP1
## null
                   0.0000
## linear
                   0.4315
## Selected: linear
## Variable: Waist (keep = FALSE)
##
                   Powers
                             DF
                                   Deviance
                                               Versus
                                                                Deviance diff.
## FP1
                   2
                             6
                                   988.8
                                   999.5
## null
                             4
                                               FP1
                                                                10.7
                             5
                                   989.2
                                               FP1
                                                                0.4
## linear
                   1
                   P-value
## FP1
## null
                   0.0046
## linear
                   0.5445
## Selected: linear
## i Fractional polynomial fitting algorithm converged after 2 cycles.
# Summarize the model
summary(model1)
##
## Call:
## glm(formula = y ~ ., family = family, data = data, weights = weights,
      offset = offset, x = TRUE, y = TRUE)
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
                           0.2698 80.527 < 2e-16 ***
## (Intercept) 21.7281
## Weight.1
               3.1648
                           0.6253
                                   5.061 1.03e-06 ***
                           0.3328 -4.646 6.54e-06 ***
## Height.1
               -1.5464
```

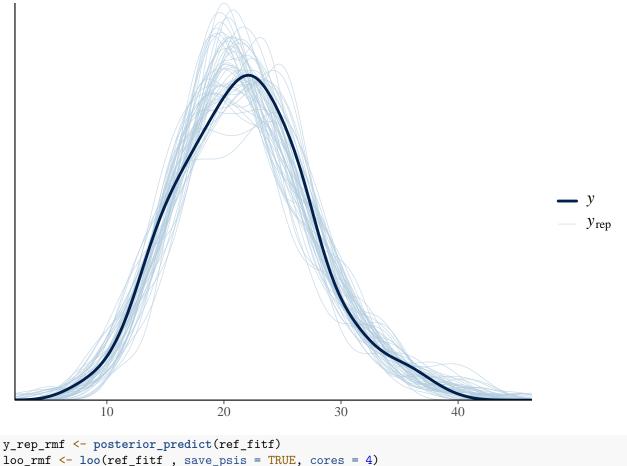
```
0.5724 3.232 0.00146 **
## Waist.1
                1.8501
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for gaussian family taken to be 13.3232)
##
      Null deviance: 6158.0 on 182 degrees of freedom
## Residual deviance: 2384.9 on 179 degrees of freedom
## AIC: 999.17
## Number of Fisher Scoring iterations: 2
print(model1)
## Shifting, Scaling and Centering of covariates
            shift scale center
## Weight 2.230325
                          TRUE
## Height 2.271145
                          TRUE
                      1
## Waist 1.794325
                          TRUE
## Final Multivariable Fractional Polynomial for y
         df_initial select alpha selected df_final power1
## Weight
                  2 0.05 0.05
                                     TRUE
                                                 1
## Height
                  2 0.05 0.05
                                     TRUE
                                                 1
                                                        1
                  2 0.05 0.05
                                     TRUE
## Waist
                                                 1
##
## MFP algorithm convergence: TRUE
## Call: glm(formula = y ~ ., family = family, data = data, weights = weights,
      offset = offset, x = TRUE, y = TRUE)
##
##
## Coefficients:
## (Intercept)
                  Weight.1
                               Height.1
                                             Waist.1
##
       21.728
                     3.165
                                 -1.546
                                               1.850
##
## Degrees of Freedom: 182 Total (i.e. Null); 179 Residual
## Null Deviance:
                       6158
## Residual Deviance: 2385 AIC: 999.2
# Estimate the model
model2 \leftarrow mfp2(Fat \sim fp(Waist, df = 2) + fp(Height, df = 2) + fp(Weight, df = 2)
              + fp(BMI, df = 1), data = women, verbose=TRUE)
##
## i Initial degrees of freedom:
## Waist Height Weight BMI
              2
## df
        2
                      2 1
##
## i Visiting order: Waist, BMI, Height, Weight
## -----
## i Running MFP Cycle 1
##
## Variable: Waist (keep = FALSE)
```

##		Powers	DF	Deviance	Versus	Deviance diff.
	FP1	2	7	986.6		
	null	NA 1	5 6	997.8	FP1	11.2
##	linear	1 P-value	О	987.5	FP1	0.9
	FP1	r value				
	null	0.0036				
	linear	0.3309				
##	Selected: linear					
##						
	Variable: BMI (k	_				
##		Powers		Deviance	Versus	Deviance diff.
	null	NA	5	989.2		
##	linear	1 P-value	6	987.5	null	1.6
	null	P-value				
	linear	0.2005				
	Selected: null	0.200				
##						
##	Variable: Height	(keep = F	ALSE)			
##		Powers	DF	Deviance	Versus	Deviance diff.
	FP1	2	6	988.5	•	•
	null	NA		1010.0	FP1	21.5
	linear	1 D 1	5	989.2	FP1	0.6
##	FP1	P-value				
	null	0.0000				
	linear	0.4315				
##	Selected: linear					
##						
##	Variable: Weight	(keep = F)	ALSE)			
##		Powers	DF	Deviance	Versus	Deviance diff.
	FP1	0.5	6	992.1		
	null linear	NA 1	4 5	1013.6 989.2	FP1 FP1	21.6 -2.9
##	Illiear	P-value	J	909.2	rr1	-2.9
	FP1	· varac				
	null	0.0000				
##	linear	1.0000				
##	Selected: linear					
##						
	· D · MDD G 1 0					
	i Running MFP Cy					
##						
	Variable: Waist	(keep = FA	LSE)			
##		Powers	DF	Deviance	Versus	Deviance diff.
##	FP1	2	6	988.8		•
##	null	NA	4	999.5	FP1	10.7
	linear	1	5	989.2	FP1	0.4
##	ED4	P-value				
	FP1 null					
	nuii linear	0.0046 0.5445				
πĦ	1111001	J.0110				

```
## Selected: linear
##
## Variable: BMI (keep = FALSE)
                                                                  Deviance diff.
                    Powers
                              DF
                                    Deviance
                                                 Versus
## null
                              5
                                    989.2
## linear
                              6
                                    987.5
                                                                  1.6
                                                 null
##
                    P-value
## null
## linear
                    0.2005
## Selected: null
## Variable: Height (keep = FALSE)
                              DF
                                                                  Deviance diff.
                    Powers
                                    Deviance
                                                 Versus
## FP1
                    2
                              6
                                    988.5
## null
                    NA
                              4
                                    1010.0
                                                 FP1
                                                                  21.5
## linear
                    1
                              5
                                    989.2
                                                 FP1
                                                                  0.6
##
                    P-value
## FP1
## null
                    0.0000
## linear
                    0.4315
## Selected: linear
## Variable: Weight (keep = FALSE)
                    Powers
                              DF
                                    Deviance
                                                                  Deviance diff.
                                                 Versus
## FP1
                    0.5
                              6
                                    992.1
## null
                    NA
                              4
                                    1013.6
                                                FP1
                                                                  21.6
## linear
                              5
                                    989.2
                                                 FP1
                                                                  -2.9
                    1
                    P-value
## FP1
## null
                    0.0000
## linear
                    1.0000
## Selected: linear
## i Fractional polynomial fitting algorithm converged after 2 cycles.
# Summarize the model
summary(model2)
##
## Call:
## glm(formula = y ~ ., family = family, data = data, weights = weights,
       offset = offset, x = TRUE, y = TRUE)
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 21.7281
                            0.2698 80.527 < 2e-16 ***
## Waist.1
                1.8501
                            0.5724
                                     3.232 0.00146 **
## Height.1
                -1.5464
                            0.3328
                                    -4.646 6.54e-06 ***
                                    5.061 1.03e-06 ***
## Weight.1
                            0.6253
                 3.1648
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for gaussian family taken to be 13.3232)
##
##
       Null deviance: 6158.0 on 182 degrees of freedom
```

```
## Residual deviance: 2384.9 on 179 degrees of freedom
## ATC: 999.17
##
## Number of Fisher Scoring iterations: 2
print(model2)
## Shifting, Scaling and Centering of covariates
             shift scale center
## Waist 1.794325
                       1
                           TRUE
                           TRUE
## BMI
         2.143166
## Height 2.271145
                       1
                           TRUE
## Weight 2.230325
                           TRUE
## Final Multivariable Fractional Polynomial for y
          df_initial select alpha selected df_final power1
## Waist
                   2
                       0.05 0.05
                                      TRUE
                                                  1
                       0.05 0.05
## BMI
                   1
                                     FALSE
                                                  0
                                                         NA
                   2
                       0.05 0.05
                                      TRUE
                                                         1
## Height
                                                  1
                   2
                       0.05 0.05
                                      TRUE
## Weight
                                                  1
                                                          1
## MFP algorithm convergence: TRUE
## Call: glm(formula = y ~ ., family = family, data = data, weights = weights,
       offset = offset, x = TRUE, y = TRUE)
##
## Coefficients:
## (Intercept)
                    Waist.1
                                Height.1
                                             Weight.1
##
        21.728
                      1.850
                                  -1.546
                                                3.165
##
## Degrees of Freedom: 182 Total (i.e. Null); 179 Residual
## Null Deviance:
                        6158
## Residual Deviance: 2385 AIC: 999.2
#library(rstanarm)
# Use the full model after stept 3 in Georgs task, thus model 1 and all predictors but not BMI
# Only use predictors that are available in the man dataset
# Fat = siri, Age = age, Height = height, Weight = weight, Neck = neck, Chest = chest, Waist = abdomen,
rmf <- as.formula(Fat ~ Waist + Height + Weight + Age + Neck + Chest +
                          Biceps + Hips + Forearm +
                        Knee + Ankle)
# Fit a Bayesian Gaussian regression model using stan_glm
ref_fitf <- stan_glm(rmf, data = women, family = gaussian())</pre>
# Check reference model, MCMC check
summary(ref_fitf)
#shinystan::launch_shinystan(ref_fitf)
mcmc_areas(as.matrix(ref_fitf)[,2:12])
```





```
y_rep_rmf <- posterior_predict(ref_fitf)
loo_rmf <- loo(ref_fitf , save_psis = TRUE, cores = 4)
psis1_rmf <- loo_rmf$psis_object
lw_rmf <- weights(psis1_rmf)
color_scheme_set("red")
#pdf(file.path(PPath2, "/LOOPITrmf.pdf"))
ppc_loo_pit_overlay(y= women$Fat,yrep=y_rep_rmf,lw=lw_rmf)</pre>
```

NOTE: The kernel density estimate assumes continuous observations and is not optimal for discrete ob

```
PIT
                                                                                     Unif
                   0.25
                                      0.5
                                                        0.75
#dev.off()
# Summarize the posterior distributions simple model
summary_rmf_cv <- prediction_summary_cv(model = ref_fitf , data = women, k = 3)</pre>
# Print the summary simple model
print(summary_rmf_cv)
## $folds
               mae mae_scaled within_50 within_95
    fold
        1 2.639294 0.7793865 0.4098361 0.8032787
        2 2.227154 0.5941096 0.5737705 0.9672131
## 2
## 3
        3 2.264260 0.6081508 0.6065574 0.9344262
##
## $cv
##
          mae mae_scaled within_50 within_95
               0.660549 0.5300546 0.9016393
## 1 2.376903
pred <- c("Waist" ,"Height" ,"Weight" ,"Age", "Neck" ,"Chest" ,</pre>
                          "Biceps" , "Hips" , "Forearm",
                         "Knee", "Ankle")
# Extract the posterior samples for the estimator
posterior_samples <- as.matrix(ref_fitf, pars = pred)</pre>
```

```
# Define the range
lower_bound <- -0.05</pre>
upper bound <- 0.05
# Apply the condition to each element of the matrix
prob_between <- apply(posterior_samples, 2, function(par) mean(par >= lower_bound & par <= upper_bound)
# Print the result
print(prob_between)
Compute the probabilty for each estimator that it is close to zero
     Waist Height Weight
                                Age
                                       Neck
                                              Chest Biceps
                                                                Hips Forearm
                                                                                Knee
## 0.00000 0.00025 0.00900 0.14825 0.06875 0.06275 0.02500 0.00100 0.03475 0.00350
     Ankle
## 0.01650
print(prob_between[prob_between > 0.25])
## named numeric(0)
set.seed(2341)
vs_cvf <- cv_varsel(ref_fitf)</pre>
Use projpred to downsize model even more
## Warning in warn_pareto(n07 = sum(pareto_k > 0.7), n05 = sum(0.7 >= pareto_k & :
## In the calculation of the reference model's PSIS-LOO CV weights, 1 (out of 183)
## Pareto k-values are in the interval (0.5, 0.7]. Moment matching (see the loo
## package), mixture importance sampling (see the loo package), and `reloo`-ing
## (see the brms package) are not supported by projpred. If these techniques (run
## outside of projpred, i.e., for the reference model only; note that `reloo`-ing
## may be computationally costly) result in a markedly different reference model
## ELPD estimate than ordinary PSIS-LOO CV does, we recommend to use K-fold CV
## within projpred.
save(vs_cvf,file = file.path(PPath2,"vs_cvf"))
#load(file = file.path(PPath2, "vs_cv"))
nsel <- suggest_size(vs_cvf)</pre>
nsel
rank_vs_cvf <- ranking(vs_cvf)</pre>
rank vs cvf
solterms_final_vs_cvf <- head(rank_vs_cvf$fulldata ,suggest_size(vs_cvf))</pre>
solterms_final_vs_cvf
# Print the summary of the variable selection
summary(vs_cvf)
```

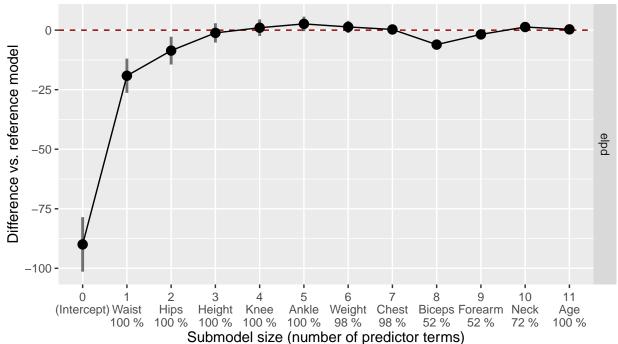
Plot the variable selection

plot(vs_cvf, deltas = TRUE)

#pdf(file.path(PPath2, "cv_valsel_plotf.pdf"))

Predictive performance

Vertical bars indicate 68.3% normal-approximation intervals



Corresponding predictor from full–data predictor ranking
Corresponding main diagonal element from CV ranking proportions matrix

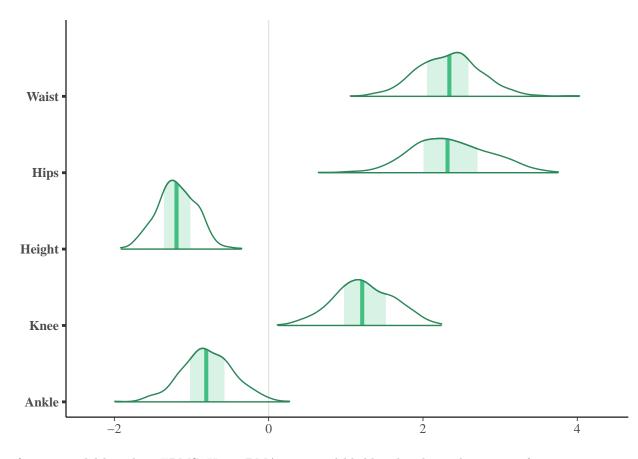
```
#dev.off()
#
solterms_final_fivef <- head(rank_vs_cvf$fulldata, 5)
solterms_final_fivef

## [1] "Waist" "Hips" "Height" "Knee" "Ankle"

# https://cran.r-project.org/web/packages/projpred/vignettes/projpred.html#post-selection-inference
proj_ref_fitf <- project(vs_cvf, predictor_terms = solterms_final_fivef, ns = 4000)</pre>
```

Projected posterior for the selected model

```
color_scheme_set(scheme = "green")
mcmc_areas(as.matrix(proj_ref_fitf), pars = solterms_final_fivef)#
```



Show results

Derive second reference model based on FBMS: Using BMA, marginal likelihoods inherently account for model complexity, and PIPs derived from them reflect this balance.

```
#Marginal likelihoods inherently account for model complexity by integrating over all possible paramete
transforms <- c("p2","p3")# transforms planed in my re-sap</pre>
probs <- gen.probs.gmjmcmc(transforms)</pre>
probs$gen <- c(0,1,0,1) # Only modifications!</pre>
params <- gen.params.gmjmcmc(women[,c("Waist","Height","Weight","Age","Neck","Chest","Biceps","Hips","F</pre>
params$feat$pop.max <- 20 #set the population size to be 20</pre>
params$feat$D <- 1  # Set depth of features to 1</pre>
\#0 Aliaksandr(1): please decide about this options
params$loglik$r <- exp(-2) # to correspond to AIC complexity that Georg uses in mfp
params$loglik$var <- "unknown"</pre>
modelFBMS <- as.formula(Fat ~ Waist + Height + Weight + Age + Neck + Chest +
                           Biceps + Hips + Forearm
                         + Knee + Ankle + BMI)
set.seed(1234)
result <- fbms(modelFBMS, data = women, method = "gmjmcmc.parallel",
                family = "gaussian",
               transforms = transforms, probs = probs, params = params, P = 50,
              runs = 40, cores = 10)
```

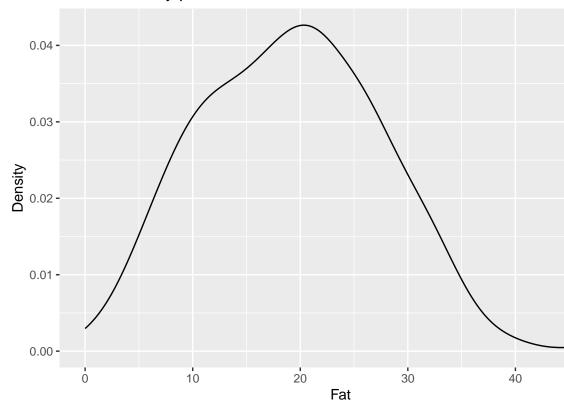
```
summary(result, labels = c("Waist", "Height", "Weight", "Age", "Neck", "Chest", "Biceps", "Hips", "Forearm", "Kn
The final model, which includes five predictors, is identical
##
                     Importance | Feature
##
                                | Forearm
##
                                | Biceps
##
                                | Chest
##
                               #| Weight
##
                              ##| BMI
##
                             ###| Ankle
##
               ######### Knee
##
    ############# Height
##
   ########################## Waist
##
   ############# Hips
##
## Best
         population: 16 thread: 2 log marginal posterior: -499.3607
## Report population: 16 thread: 2 log marginal posterior: -499.3607
     feats.strings marg.probs
## 1
              Hips 0.99540412
## 2
             Waist 0.97552176
## 3
            Height 0.93993647
## 4
              Knee 0.59048472
             Ankle 0.12427203
## 5
## 6
               BMI 0.07414405
## 7
            Weight 0.05028350
## 8
             Chest 0.01719150
## 9
            Biceps 0.01489256
## 10
           Forearm 0.01041275
formula_male <- as.formula(Fat ~ Waist + Hips + Height + Knee + Ankle)</pre>
```

Fit model to male data set and compare the posterior predictive distributions

```
library(mfp)
See Task Bodyfat.qmd
## Warning: Paket 'mfp' wurde unter R Version 4.4.2 erstellt
## Lade nötiges Paket: survival
##
## Attache Paket: 'mfp'
## Das folgende Objekt ist maskiert 'package:mfp2':
##
## fp
data(bodyfat)
bodyfat_corr <- bodyfat
bodyfat_corr[42,"height"] <- 69.5  # one-digit correction of height</pre>
```

```
bodyfat_corr[48,"density"] <- 1.0865 # one-digit correction of density
bodyfat_corr[76,"density"] <- 1.0566 # one-digit correction of density</pre>
bodyfat_corr[96,"density"] <- 1.0591 # one-digit correction of density
# recompute siri formula based on corrected density
bodyfat_corr[,"siri"] <- pmax(round(495 / bodyfat_corr$density - 450, 1) , 0)
bodyfat corr[,"brozek"] <- pmax(round(457/ bodyfat corr$density - 414.2, 1), 0)
Aligning the two data sets
bodyfat corr$height <- bodyfat corr$height * 2.54/100
bodyfat_corr$weight <- bodyfat_corr$weight * 0.454592</pre>
library(tidyverse)
## -- Attaching core tidyverse packages ----
                                                 ----- tidyverse 2.0.0 --
## v dplyr 1.1.4 v readr 2.1.5
## v forcats 1.0.0 v stringr 1.5.1
## v lubridate 1.9.3 v tibble
                                    3.2.1
## v purrr
             1.0.2
                      v tidyr
                                   1.3.1
## -- Conflicts ----- tidyverse_conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag() masks stats::lag()
## i Use the conflicted package (<a href="http://conflicted.r-lib.org/">http://conflicted.r-lib.org/</a>) to force all conflicts to become error
men <- bodyfat_corr %>%
 rename(Fat = siri, Age = age, Height = height, Weight = weight,
        Neck = neck, Chest = chest, Waist = abdomen, Hips = hip,
         Knee = knee, Ankle = ankle, Forearm = forearm,
        Biceps = biceps, Thigh = thigh)
names (men)
## [1] "case"
                 "brozek" "Fat"
                                     "density" "Age"
                                                         "Weight" "Height"
## [8] "Neck" "Chest" "Waist"
                                     "Hips"
                                               "Thigh"
                                                                   "Ankle"
                                                         "Knee"
## [15] "Biceps" "Forearm" "wrist"
# Add BMI
men$BMI <- men$Weight / (men$Height^2)</pre>
men[,4:18] \leftarrow scale(men[,4:18])
fat_density_male <- density(men$Fat, na.rm = TRUE)</pre>
ggplot(men, aes(x = Fat)) + geom_density() +
 labs(title = "Kernel-density plot for outcome fat for males", x = "Fat", y = "Density")
```

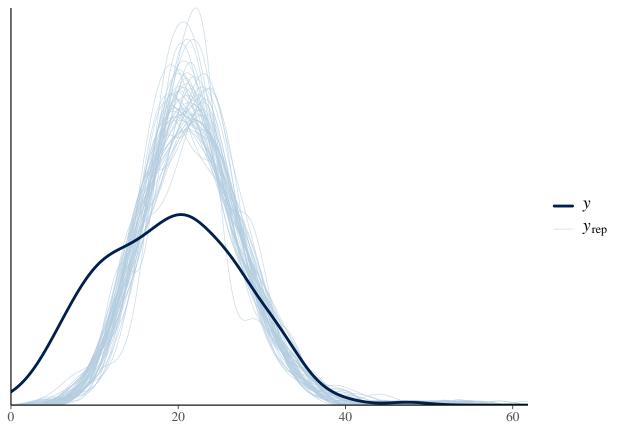
Kernel-density plot for outcome fat for males



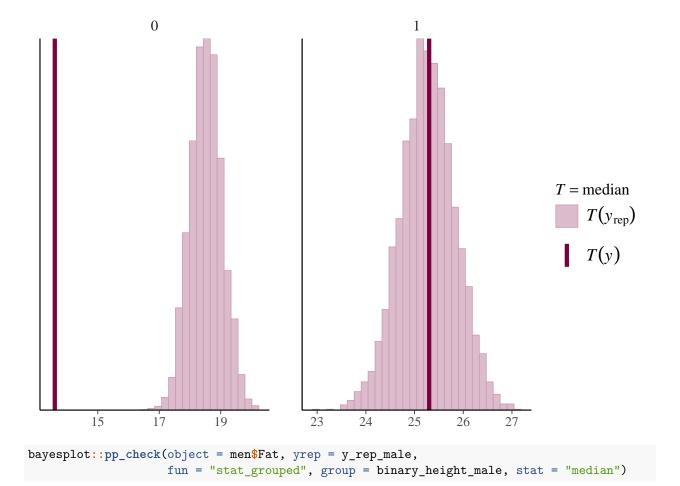
Prepare data for males

```
summary(men$Fat)
```

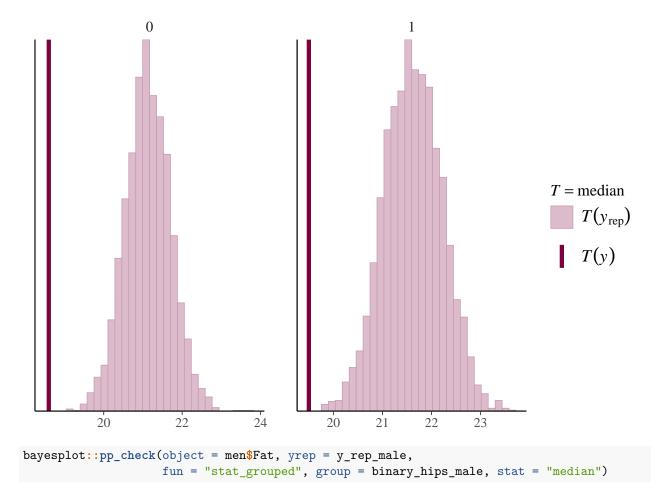
```
Min. 1st Qu. Median
                               Mean 3rd Qu.
##
                                               Max.
##
             12.40
                     19.20
                              19.16
                                      25.30
                                               47.50
# LOOPIT and bayesrules summary for male data based on female model
# Prediction for male data based on female model
fit_female <- stan_glm(formula_male, data = women, family = gaussian())</pre>
#proj_ref_fitf <- project(us_cuf, predictor_terms = solterms_final_fivef, ns = 4000)</pre>
# https://www.rdocumentation.org/packages/projpred/versions/2.0.2/topics/proj-pred
#y_rep_male <- proj_linpred(vs_cvf, solution_terms= solterms_final_fivef, newdata = men)#</pre>
y_rep_male <- posterior_predict(fit_female, newdata = men)</pre>
color_scheme_set("blue")
bayesplot::pp_check(object = men$Fat, yrep = y_rep_male[1:50,],fun = ppc_dens_overlay)
```



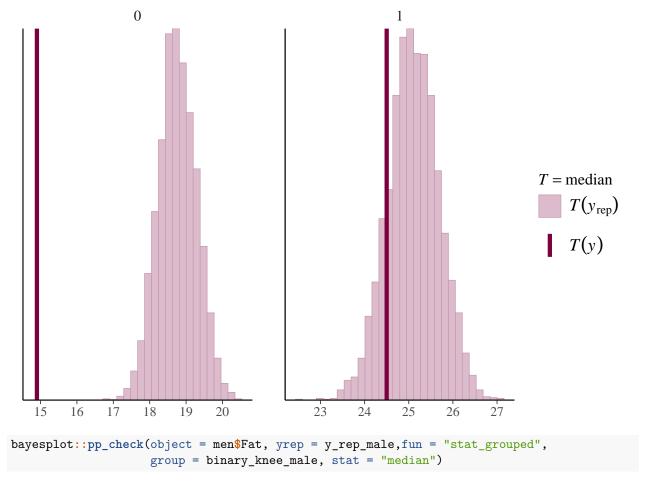
`stat_bin()` using `bins = 30`. Pick better value with `binwidth`.



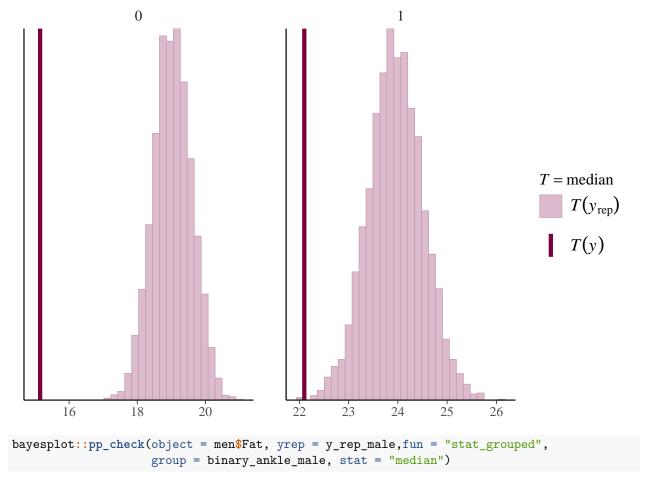
`stat_bin()` using `bins = 30`. Pick better value with `binwidth`.



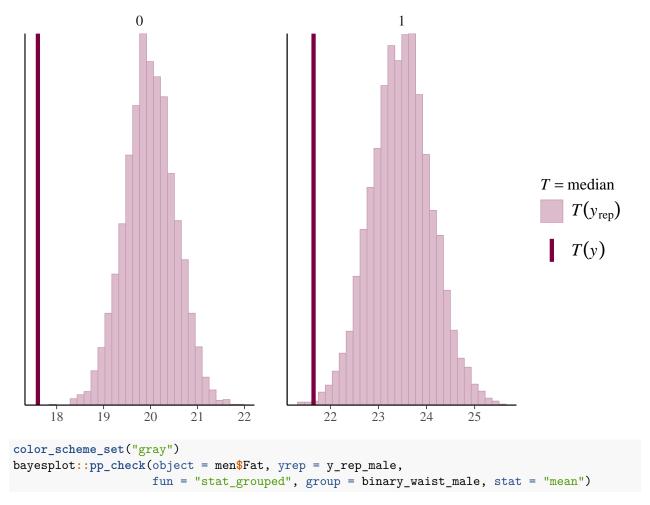
`stat_bin()` using `bins = 30`. Pick better value with `binwidth`.



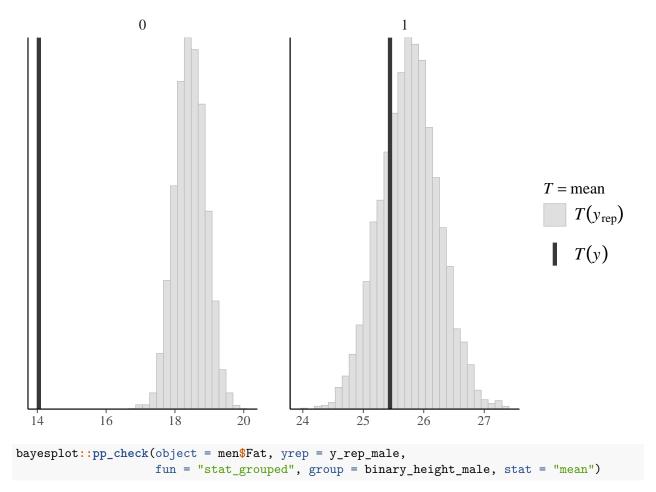
`stat_bin()` using `bins = 30`. Pick better value with `binwidth`.



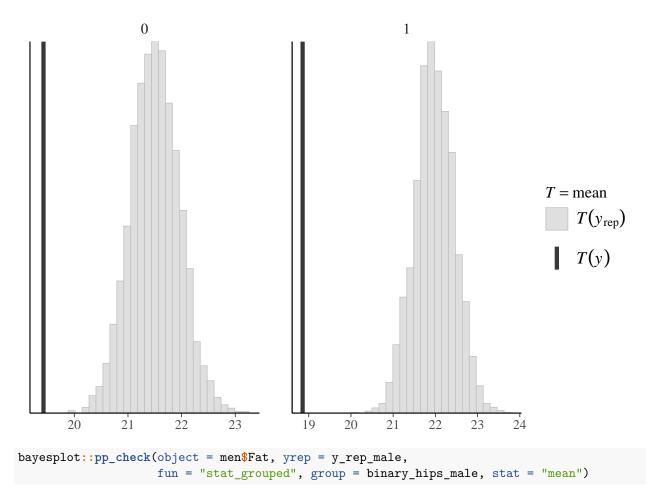
`stat_bin()` using `bins = 30`. Pick better value with `binwidth`.



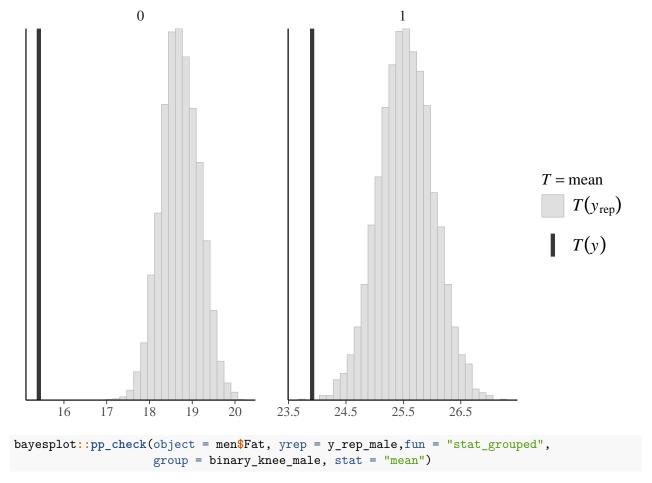
`stat_bin()` using `bins = 30`. Pick better value with `binwidth`.



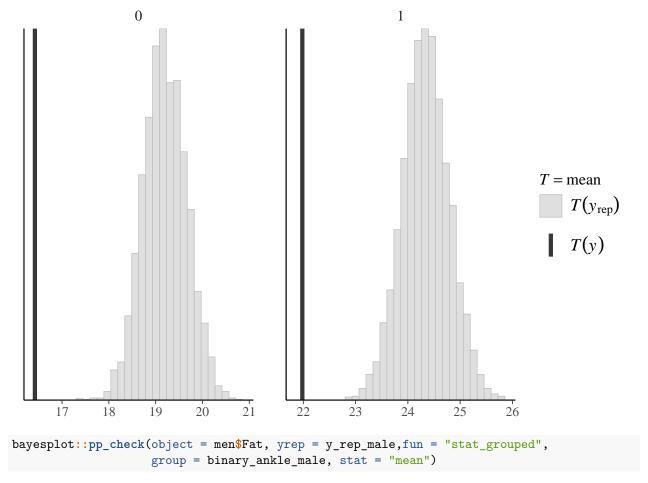
`stat_bin()` using `bins = 30`. Pick better value with `binwidth`.



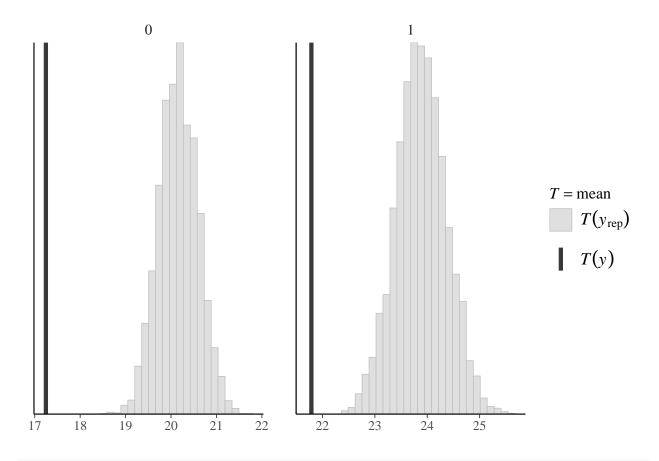
`stat_bin()` using `bins = 30`. Pick better value with `binwidth`.



`stat_bin()` using `bins = 30`. Pick better value with `binwidth`.



`stat_bin()` using `bins = 30`. Pick better value with `binwidth`.



```
# Summarize the posterior distributions
summary_male_cv <- prediction_summary_cv(model = fit_female, data = men, k = 3)
# Print the summary
print(summary_male_cv)</pre>
```

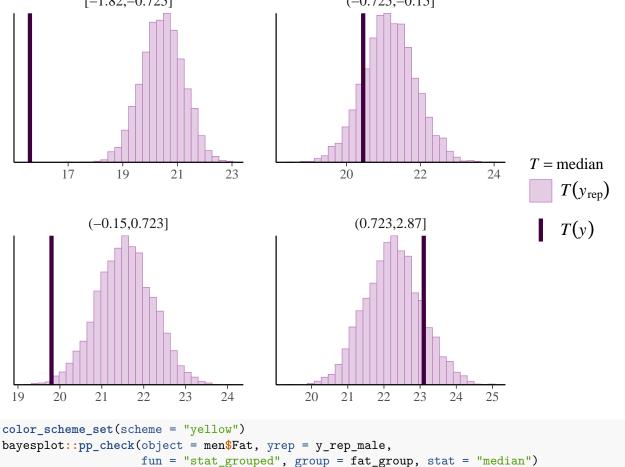
Summarize the posterior distributions

1 4.316417

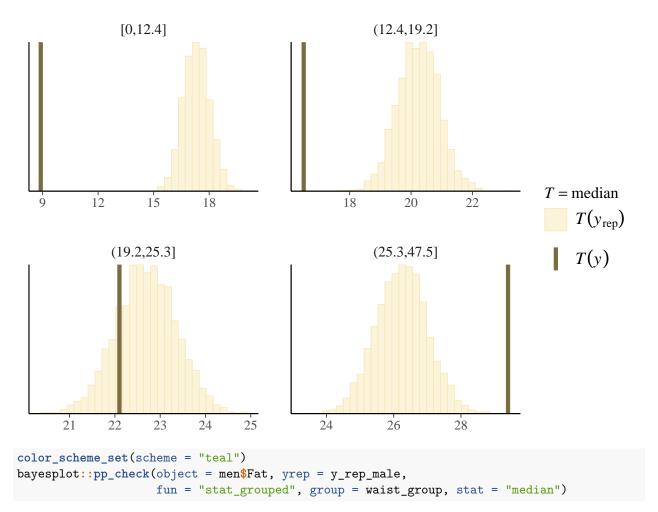
```
## $folds
##
    fold
               mae mae_scaled within_50 within_95
        1 3.696158  0.7896502  0.4285714  0.9761905
## 1
        2 2.835573  0.5887821  0.5714286  0.9642857
        3 3.459173 0.7612981 0.4523810 0.9523810
## 3
##
## $cv
##
          mae mae_scaled within_50 within_95
## 1 3.330301 0.7132435 0.484127 0.9642857
summary_male <- prediction_summary(model = fit_female, data = men)</pre>
# Print the summary
print(summary_male)
          mae mae_scaled within_50 within_95
```

1.225886 0.297619 0.7301587

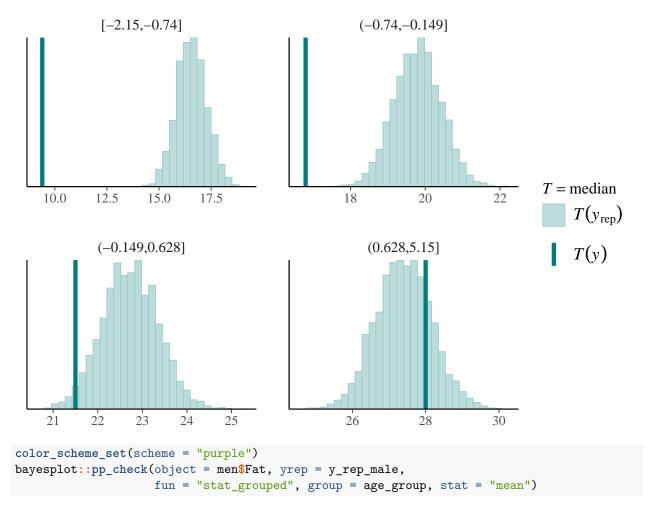
```
age_group <- cut(men$Age, breaks = quantile(men$Age, probs = seq(0, 1, by = 0.25)), include.lowest = TR
table(age_group)
Identify the groups where the prediction performs effectively
## age_group
## [-1.82,-0.725] (-0.725,-0.15] (-0.15,0.723]
                                                   (0.723, 2.87]
##
fat_group <- cut(men$Fat, breaks = quantile(men$Fat, probs = seq(0, 1, by = 0.25)), include.lowest = TR
table(fat_group)
## fat_group
      [0,12.4] (12.4,19.2] (19.2,25.3] (25.3,47.5]
##
##
waist_group <- cut(men$Waist, breaks = quantile(men$Waist, probs = seq(0, 1, by = 0.25)), include.lowes</pre>
color_scheme_set(scheme = "purple")
bayesplot::pp_check(object = men$Fat, yrep = y_rep_male,
                    fun = "stat_grouped", group = age_group, stat = "median")
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
            [-1.82, -0.725]
                                                  (-0.725, -0.15]
```



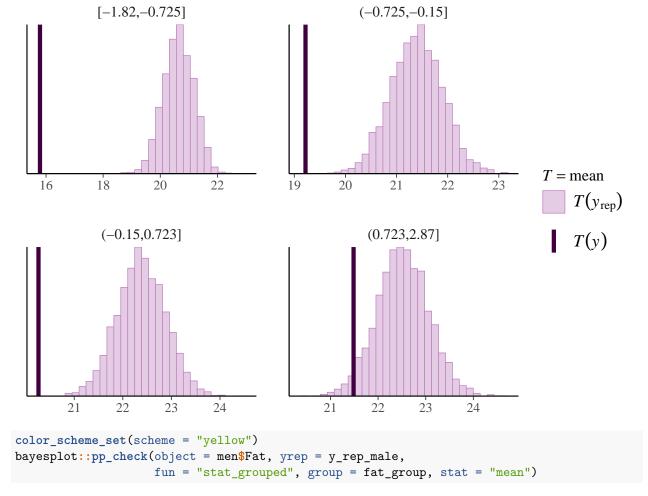
`stat_bin()` using `bins = 30`. Pick better value with `binwidth`.



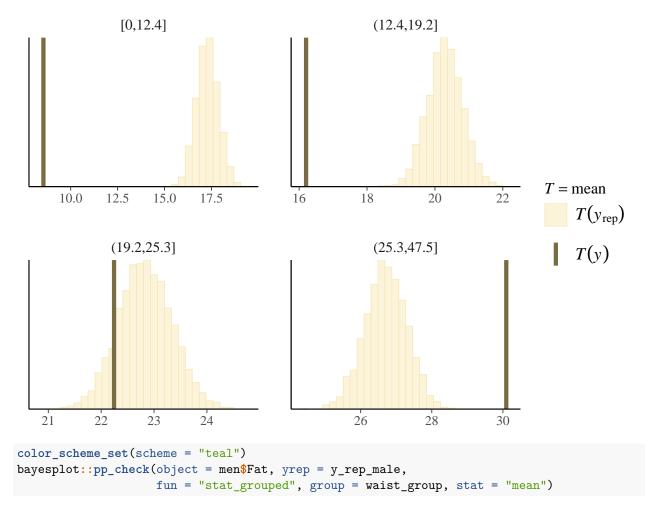
`stat_bin()` using `bins = 30`. Pick better value with `binwidth`.



`stat_bin()` using `bins = 30`. Pick better value with `binwidth`.



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