

#### Module 2

# Introduction to Neural Networks:

Artificial neural networks are powerful machine learning techniques inspired by the biological nervous system.

They simulate the learning process in living organisms, where neurons communicate through connections called synapses.

The strength of these connections, known as synaptic weights, changes in response to external stimuli, enabling learning.

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# Simulating the Brain: Biological vs. Artificial Neural Neural Networks

#### **Biological Neural Networks**

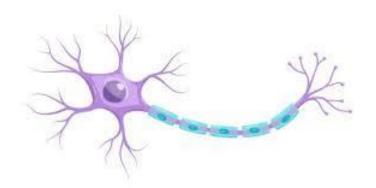
Neurons are connected by axons and dendrites, forming forming synapses.

Synaptic strengths change with stimuli, enabling learning. learning.

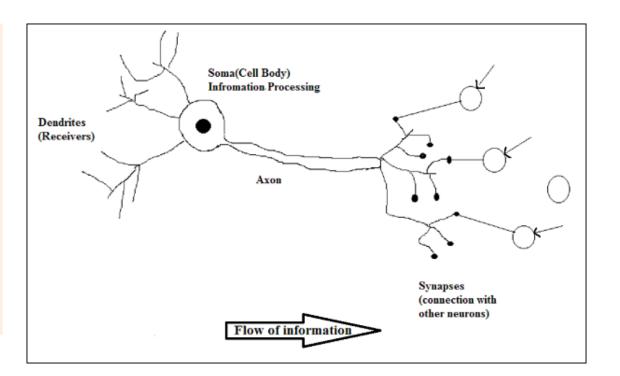
#### **Artificial Neural Networks**

Computational units (neurons) are connected by weights, weights, simulating synaptic strengths.

Learning occurs by adjusting these weights.



- Dendrites They are tree-like branches, responsible for receiving the information from other neurons it is connected to. In other sense, we can say that they are like the ears of neuron.
- **Soma** It is the cell body of the neuron and is responsible for processing of information, they have received from dendrites.
- Axon It is just like a cable through which neurons send the information.
- **Synapses** It is the connection between the axon and other neuron dendrites.



- An artificial neural network (ANN) is an efficient information processing system which resembles in characteristics with a biological neural network.
- ANNs possess large number of highly interconnected processing elements called *nodes* or *units* or *neuron*, which usually operate in parallel and are configured in regular architectures.
- Each neuron is connected with the other by a connection link.
- Each connection link is associated with weights which contain information about the input signal.
- This information is used to solve a particular problem.
- Each neuron has an internal state, which is called an activation signal.
- Output signals, which are produced after combining the input signals and activation rule, may be sent to other units.

# Architecture of Artificial Neural Network

Neural networks are built upon basic computational units inspired by traditional machine learning algorithms like regression.

These units are combined and their weights are learned jointly to minimize prediction errors.

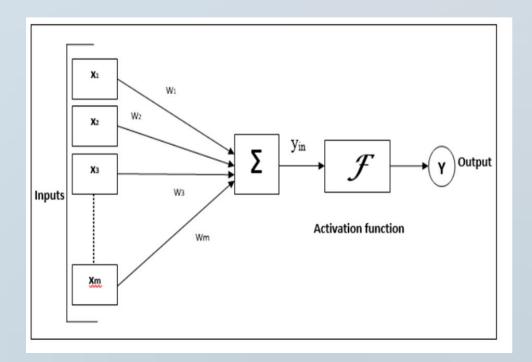
For the above general model of artificial neural network, the net input can be calculated as follows –

$$y_{in} \,=\, x_1.w_1 \,+\, x_2.w_2 \,+\, x_3.w_3\,\ldots\, x_m.w_m$$
 i.e., Net input  $y_{in} \,=\, \sum_i^m\, x_i.w_i$ 

The output can be calculated by applying the activation function over the net input.

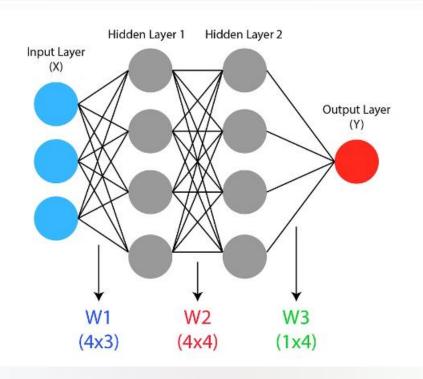
$$Y = F(y_{in})$$

Output = function netinputcalculated

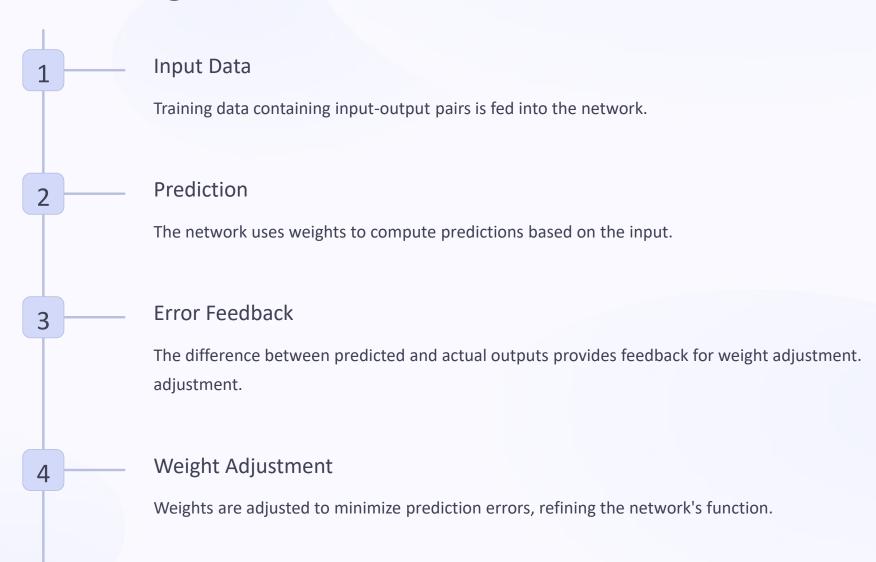


## **ANN vs BNN**

BNN	ANN
Soma	Node
Dendrites	Input
Synapse	Weights or Interconnections
Axon	Output
Massively parallel, slow but superior than ANN	Massively parallel, fast but inferior than BNN
10 <sup>11</sup> neurons and 10 <sup>15</sup> interconnections	10 <sup>2</sup> to 10 <sup>4</sup> nodes mainly depends on the type of application and network designer
They can tolerate ambiguity	Very precise, structured and formatted data is required to tolerate ambiguity
Performance degrades with even partial damage	It is capable of robust performance, hence has the potential to be fault tolerant
Stores the information in the synapse	Stores the information in continuous memory locations



## Learning in Artificial Neural Networks



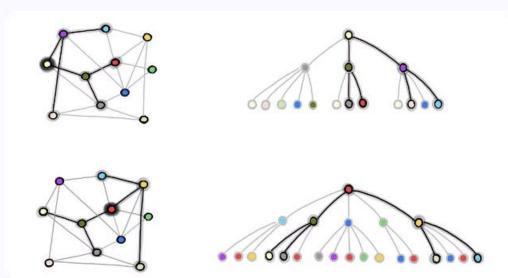
## Generalization: The Power of Neural Networks

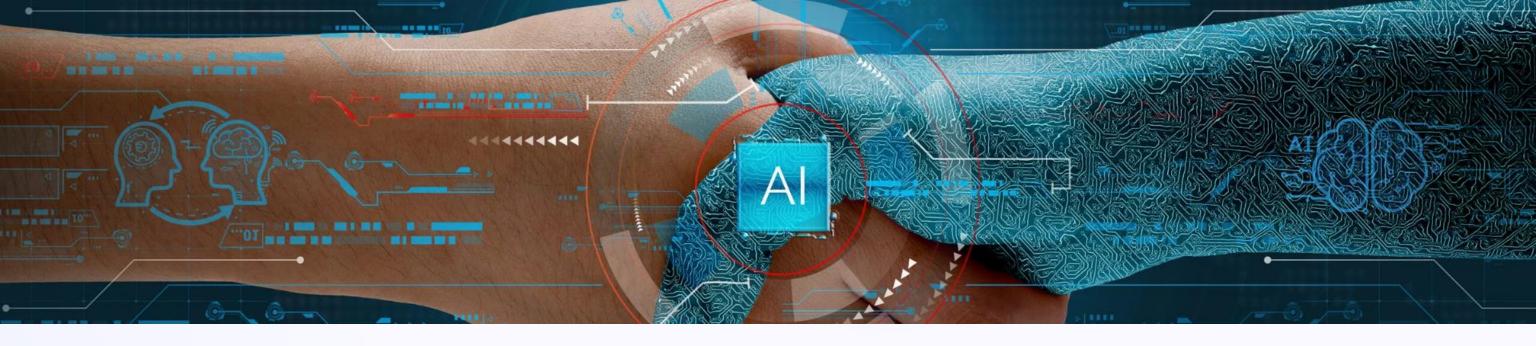
After training on a set of input-output pairs, neural networks can generalize their learning to unseen examples. This ability to accurately predict outputs for new inputs is crucial for their practical applications.

## The Power of Combining Units

The real power of neural networks lies in combining multiple computational units. computational units.

This allows them to learn more complex functions than individual units could could achieve, enabling them to handle intricate data patterns.



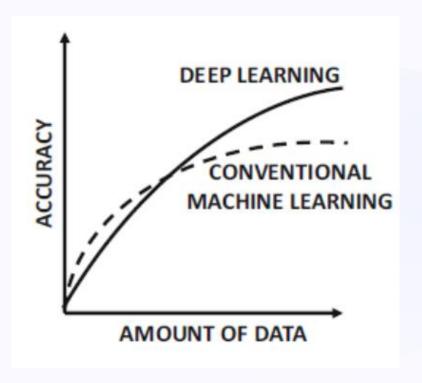


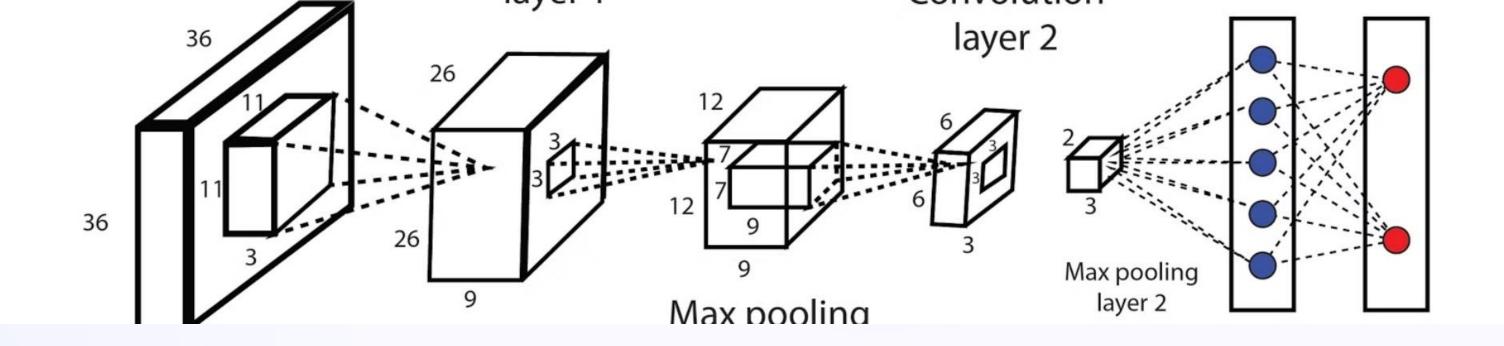
## Humans vs. Computers: The Limits of Al

Humans and computers excel at different tasks.

While computers are adept at complex calculations, humans excel at tasks like image image recognition.

Deep learning has recently surpassed human performance in some image recognition tasks, recognition tasks, highlighting the potential of AI.





# Inspiration from Biology: Convolutional Neural Networks

The success of convolutional neural networks for image recognition is inspired by the structure of the visual cortex in the brain. This architecture, inspired by biological research, demonstrates the potential of leveraging biological insights to improve AI.

#### Neural Networks: Advantages and Disadvantages

Advantages	Disadvantages	
1) The ability to learn by themselves	The black box nature and uncertain prediction rates	
2) The ability to work with insufficient data	Long training processes and limited data efficiency	
The ability of parallel processing	Economically and computationally expensive	

## Advantages of Neural Networks

1 Semantic Insights

Neural networks provide a high-level abstraction for expressing semantic insights about data through their architecture.

2 Flexibility

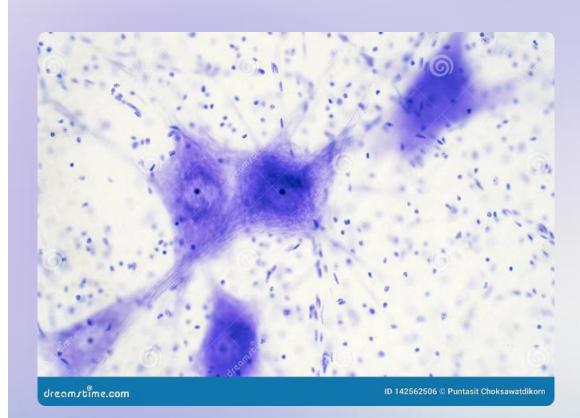
The complexity of a neural network can be easily adjusted by adjusted by adding or removing neurons, adapting to data data availability and computational resources.

## Perceptrons

- Perceptron is one of the simplest\_Artificial neural network architectures.
- It was introduced by Frank Rosenblatt in 1957s.
- It is the simplest type of neural network, consisting of a single layer of input nodes that are fully connected to a layer of output nodes.

#### **Types of Perceptron**

- •Single-Layer Perceptron: This type of perceptron is limited to learning linearly separable patterns. effective for tasks where the data can be divided into distinct categories through a straight line.
- •Multilayer Perceptron: Multilayer perceptrons possess enhanced processing capabilities as they consist of two or more layers, adept at handling more complex patterns and relationships within the data.



#### **Basic Components of Perceptron**

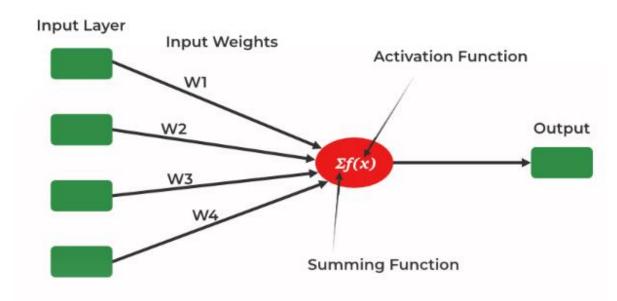
A perceptron, the basic unit of a neural network, comprises essential components that collaborate in information processing.

- •Input Features: The perceptron takes multiple input features, each input feature represents a characteristic or attribute of the input data.
- •Weights: Each input feature is associated with a weight, determining the significance of each input feature in influencing the perceptron's output. During training, these weights are adjusted to learn the optimal values.
- •Summation Function: The perceptron calculates the weighted sum of its inputs using the summation function. The summation function combines the inputs with their respective weights to produce a weighted sum.
- •Activation Function: The weighted sum is then passed through an <u>activation function</u>. Perceptron uses Heaviside step function functions. which take the summed values as input and compare with the threshold and provide the output as 0 or 1.
- •Output: The final output of the perceptron, is determined by the activation function's result. For example, in binary classification problems, the output might represent a predicted class (0 or 1).
- •Bias: A bias term is often included in the perceptron model. The bias allows the model to make adjustments that are independent of the input. It is an additional parameter that is learned during training.
- •Learning Algorithm (Weight Update Rule): During training, the perceptron learns by adjusting its weights and bias based on a learning algorithm. A common approach is the perceptron learning algorithm, which updates weights based on the difference between the predicted output and the true output.

## **Single Layer Perceptrons**

A single layer perceptron (SLP) is a simple type of ANN consisting of a single layer of single layer of neurons.

SLPs can be used for classification tasks, but they are limited in their ability to learn ability to learn complex patterns.



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#### **Linear Separator**

The SLP can only classify data that is linearly separable, meaning that it can draw a straight line to divide the data into two classes.

**Binary Output** 

The SLP outputs a single binary binary value (0 or 1), representing a decision on whether the input belongs to a to a specific class.

The main functionality of the perceptron is:-

- •Takes input from the input layer
- •Weight them up and sum it up.
- •Pass the sum to the nonlinear function to produce the output.

## Perceptron Learning Rule

- The *learning signal* is the difference between the desired and actual response of a neuron.
- The perceptron learning rule is explained as follows:
- Consider a finite "n" number of input training vectors, with their associated target values x(n) and t(n), where "n" ranges from 1 to N.
- The target is either +1 or -1.
- The output "y" is obtained on the basis of the net input calculated and activation function

$$y = f(y_{in}) = \begin{cases} 1 & \text{if } y_{in} > \theta \\ 0 & \text{if } -\theta \le y_{in} \le \theta \\ -1 & \text{if } y_{in} < -\theta \end{cases}$$

$$u(\text{new}) = u(\text{old}) + \alpha tx \quad (\alpha - \text{learning rate})$$

$$u(\text{new}) = u(\text{old})$$

$$u(\text{new}) = u(\text{old})$$

#### Perceptron Training Algorithm for Single Output Classes

Step 0: Initialize the weights and the bias. Also initialize the learning rate  $\alpha(O \le \alpha \le 1)$ . For simplicity  $\alpha$  is set to 1.

**Step 1:**Perform Steps 2-6 until the final stopping condition is false.

**Step 2:** Perform Steps 3-5 for each training pair indicated by s:t.

**Step 3:** The input layer containing input units is applied with identity activation functions:

$$x_i = s_i$$

**Step 4:** Calculate the output of the network. To do so, first obtain the net input:

$$y_{in} = b + \sum_{i=1}^{n} x_i w_i$$

where "n" is the number of input neurons in the input layer. Then apply activations over the netinput calculated to obtain the output:

$$y = f(y_{in}) = \begin{cases} 1 & \text{if } y_{in} > \theta \\ 0 & \text{if } -\theta \le y_{in} \le \theta \\ -1 & \text{if } y_{in} < -\theta \end{cases}$$



## **Limitations of Single Layer Perceptrons**

SLPs are limited in their ability to solve non-linearly separable problems, such as the XOR problem. This is because they can only create linear decision boundaries.

#### **Limited Representation**

SLPs struggle to represent complex patterns and relationships that are not linearly separable.

#### **Inability to Learn Complex Functions**

SLPs cannot learn non-linear functions, hindering their ability to handle real-world data with complex patterns.

## Multi Layer Perceptrons (MLPs)

MLPs overcome the limitations of SLPs by introducing multiple layers of neurons.

This allows them to create non-linear decision boundaries and learn complex patterns.

1 Input Layer

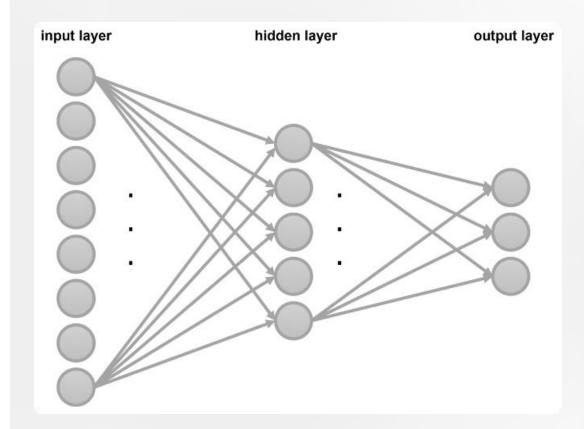
The input layer receives the raw data and passes it to the hidden layers.

**Hidden Layers** 

Hidden layers process the input data through multiple layers of neurons and non-linear activation functions.

3 — Output Layer

The output layer produces the final output, which can be a classification label, a regression value, or a probability distribution.



## Feedforward and Backpropagation in MLPs

The feedforward process involves sending data through the MLP from the input layer to the output layer.

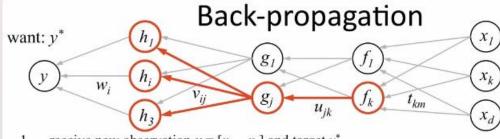
Backpropagation is used to adjust the weights of the connections between neurons to improve the accuracy of the network.

**Feedforward** 

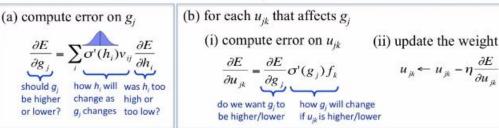
Data is fed forward through the network, with each neuron applying its activation function to the weighted sum of its inputs.

#### **Backpropagation**

The error at the output layer is propagated backward through the network, adjusting weights to reduce the error.



- 1. receive new observation  $\mathbf{x} = [x_1...x_d]$  and target  $\mathbf{y}^*$
- 2. **feed forward:** for each unit  $g_j$  in each layer 1...L compute  $g_j$  based on units  $f_k$  from previous layer:  $g_j = \sigma \left( u_{j0} + \sum u_{jk} f_k \right)$
- 3. get prediction v and error  $(v-v^*)$
- **4.** back-propagate error: for each unit  $g_i$  in each layer L...1



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## **Representation Power of MLPs**

MLPs are capable of representing a wide range of complex functions, including non-linear functions, thanks to their multi-layered structure and non-linear activation functions. This enables them to learn intricate relationships in data.

Non-linearity	Through activation functions, MLPs can learn complex, non-linear relationships that are not possible with linear models.
Hidden Layers	Multiple hidden layers allow MLPs to create hierarchical representations of data, capturing intricate patterns at different levels of abstraction.

## **Approximation Capabilities of MLPs**

MLPs can approximate any continuous function to an arbitrary degree of accuracy, given enough hidden neurons and appropriate training data. This makes them suitable for a wide range of tasks, including function approximation, regression, and classification.



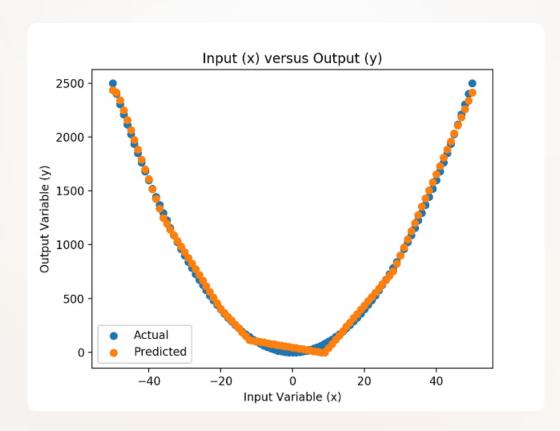
## **Universal Approximation**Theorem

The universal approximation theorem states that a sufficiently large MLP can approximate any continuous function with arbitrary accuracy.



#### **Training Data**

The quality and quantity of the training data significantly impact the MLP's ability to accurately approximate a function.



## **Activation Functions**

- The activation function defines the output of a neuron / node given an input or set of input (output of multiple neurons).
- It's the mimic of the stimulation of a biological neuron.
- Activation function decides, whether a neuron should be activated or not by calculating weighted sum and further adding bias with it.
- The purpose of the activation function is to introduce non-linearity into the output of a neuron.
- The Activation Functions can be basically divided into 2 types-
  - 1. Linear Activation Function
  - 2. Non-linear Activation Function

## **Linear Activation Functions**

- •Equation : Linear function has the equation similar to as of a straight line i.e. y=ax
- •No matter how many layers we have, if all are linear in nature, the final activation function of last layer is nothing but just a linear function of the input of first layer.
- •Range : -inf to +inf
- •Uses: Linear activation function is used at only output layer.
- •Issues: If we will differentiate linear function to bring non-linearity, result will no more depend on input "x" and function will become constant, it won't introduce any ground-breaking behavior to our algorithm.

#### Pros

- •It gives a range of activations, so it is not binary activation.
- •We can definitely connect a few neurons together and if more than 1 fires, we could take the max (or softmax) and decide based on that.

#### Cons

- •For this function, derivative is a constant. That means, the gradient has no relationship with X.
- •It is a constant gradient and the descent is going to be on constant gradient.
- •If there is an error in prediction, the changes made by back propagation is constant and not depending on the change in input delta(x)!

## **Non Linear Activation Functions**

- The Nonlinear Activation Functions are the most used activation functions.
- It makes it easy for the model to generalize or adapt with variety of data and to differentiate between the output.
   The main terminologies needed to understand for nonlinear functions are:

Derivative or Differential: Change in y-axis w.r.t. change in x-axis.It is also known as slope. Monotonic function: A function which is either entirely non-increasing or non-decreasing.

The Nonlinear Activation Functions are mainly divided on the basis of their range or curves

Sigmoid	ReLU	Tanh
The sigmoid function outputs values	The ReLU function is known for its	The tanh function outputs values between
between 0 and 1, making it suitable for	simplicity and efficiency. It outputs the	-1 and 1, making it suitable for both binary
binary classification.	input directly if it's positive, and 0	and multi-class classification.
	otherwise.	

#### 1. Sigmoid or Logistic Activation Function

The Sigmoid Function curve looks like a S-shape.

The main reason why we use sigmoid function is because it exists between (0 to 1). Therefore, it is especially used for models where we have to predict the **probability** as an output.

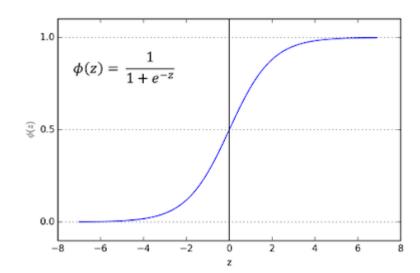
Since probability of anything exists only between the range of 0 and 1, sigmoid is the right choice.

The function is differentiable. That means, we can find the slope of the sigmoid curve at any two points.

The function is monotonic but function's derivative is not.

The logistic sigmoid function can cause a neural network to get stuck at the training time.

- Value Range: 0 to 1
- •Uses: Usually used in output layer of a binary classification, where result is either 0 or 1, as value for sigmoid function lies between 0 and 1 only so, result can be predicted easily to be 1 if value is greater than 0.5 and 0 otherwise.



$$A=rac{1}{(1+e^{-x})}$$

#### **Pros**

- •It is nonlinear in nature. Combinations of this function are also nonlinear!
- •It will give an analog activation unlike step function.
- •It has a smooth gradient too.
- •It's good for a classifier.
- •The output of the activation function is always going to be in range (0,1) compared to (-inf, inf) of linear function. So we have our activations bound in a range. Nice, it won't blow up the activations then.

#### Cons

- •Towards either end of the sigmoid function, the Y values tend to respond very less to changes in X.
- •It gives rise to a problem of "vanishing gradients".
- •Its output isn't zero centered. It makes the gradient updates go too far in different directions. 0 < output < 1, and it makes optimization harder.
- •Sigmoids saturate and kill gradients.
- •The network refuses to learn further or is drastically slow (depending on use case and until gradient /computation gets hit by floating point value limits).
- •The softmax function is a more generalized logistic activation function which is used for multiclass classification.

#### 2. Softmax Function

The softmax function is also a type of sigmoid function but is handy when we are trying to handle classification problems.

Nature:- non-linear

Uses :- Usually used when trying to handle multiple classes. The softmax function would squeeze the outputs for each class between 0 and 1 and would also divide by the sum of the outputs.

Output:- The softmax function is ideally used in the output layer of the classifier where we are actually trying to attain the probabilities to define the class of each input.

Softmax is an activation function that scales numbers/logits into probabilities. The output of a Softmax is a vector (say v) with probabilities of each possible outcome. The probabilities in vector v sums to one for all possible outcomes or classes.

Mathematically, Softmax is defined as,

$$S(y)_i = rac{exp(y_i)}{\sum_{j=1}^n exp(y_j)}$$
  $n$ - is the number of classes ( possible outcomes)  $y_i$  is the input  $exp(y_i)$  is the standard exponential function applied on  $y_i$ 

#### 3. Tanh or Hyperbolic Tangent Activation Function

tanh is also like logistic sigmoid but better. The range of the tanh function is from (-1 to 1).

tanh is also sigmoidal (s - shaped).

Tanh function also knows as Tangent Hyperbolic function.

It's actually mathematically shifted version of the sigmoid function.

Both are similar and can be derived from each other.

Tanh squashes a real-valued number to the range [-1, 1].

It's non-linear. But unlike Sigmoid, its output is zero-centered.

Therefore, in practice the tanh non-linearity is always preferred to the sigmoid nonlinearity.

The advantage is that the negative inputs will be mapped strongly negative and the zero inputs will be mapped near zero in the tanh graph.



The function is monotonic while its derivative is not monotonic.

The tanh function is mainly used classification between two classes.

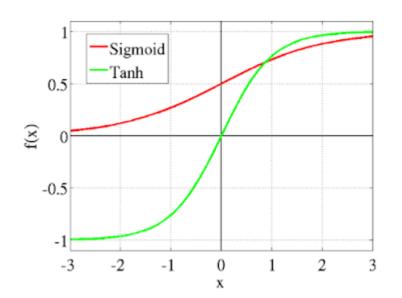
Both tanh and logistic sigmoid activation functions are used in feed-forward nets.



The gradient is stronger for tanh than sigmoid (derivatives are steeper).

#### Cons

Tanh also has the vanishing gradient problem.

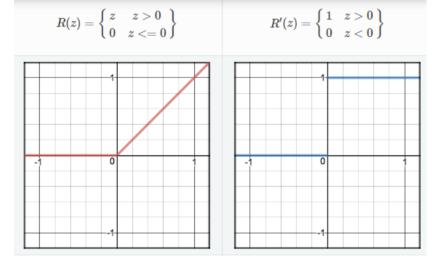


$$f(x) = tanh(x) = rac{2}{(1+e^{-2x})} - 1$$
 OR  $tanh(x) = 2*sigmoid(2x) - 1$ 

#### 4. ReLU (Rectified Linear Unit) Activation Function

A recent invention which stands for **Rectified Linear Units**.

The formula is deceptively simple: max(0,z) Despite its name and appearance, it's not linear and provides the same benefits as Sigmoid (i.e. the ability to learn nonlinear functions), but with better performance. it is used in almost all the convolutional neural networks or deep learning



A(x) = max(0,x)

Uses :- ReLu is less computationally expensive than tanh and sigmoid because it involves simpler mathematical operations. At a time only a few neurons are activated making the network sparse making it efficient and easy for computation.

In simple words, ReLU learns much faster than sigmoid and Tanh function.

#### **Pros**

- •It avoids and rectifies vanishing gradient problem.
- •ReLu is less computationally expensive than tanh and sigmoid because it involves simpler mathematical operations.

#### Cons

- •One of its limitations is that it should only be used within hidden layers of a neural network model.
- •Some gradients can be fragile during training and can die. It can cause a weight update which will makes it never activate on any data point again. In other words, ReLu can result in dead neurons.
- •In another words, For activations in the region (x<0) of ReLu, gradient will be 0 because of which the weights will not get adjusted during descent. That means, those neurons which go into that state will stop responding to variations in error/ input (simply because gradient is 0, nothing changes). This is called the dying ReLu problem.

The range of ReLu is  $[0,\infty)[0,\infty)$ . This means it can blow up the activation.

#### **Advantages of ReLU**

#### **Computational Speed**

**Vanishing Gradient -** ReLU only saturates when the input is less than 0.

**Convergence Speed -** ReLU provides Better performance and faster convergence.

### **Conclusion and Future Directions**

Artificial neural networks, particularly MLPs, have revolutionized machine learning, enabling solutions for complex problems. Future research focuses on improving training efficiency, exploring new architectures, and developing methods for explainability and interpretability.





#### **Robotics**

ANNs are used to control robots and enable them to perform complex tasks, such as grasping objects and navigating environments.

#### **Autonomous Vehicles**

ANNs are used to power self-driving cars, enabling them to perceive their surroundings and make safe driving decisions.



## **Training Multilayer Perceptrons with Backpropagation**

# Forward Pass Input data is fed through the network, activating nodes and propagating signals forward. The error signal is propagated backward through the network, adjusting weights and biases to minimize loss. 2 3 4

The output layer computes the loss function, measuring the difference between predicted and actual outputs.

**Loss Calculation** 

## The algorithm modifies the network's parameters based on the calculated gradients, optimizing for

**Weight Update** 

based on the calculated gradients, optimizing for better performance.

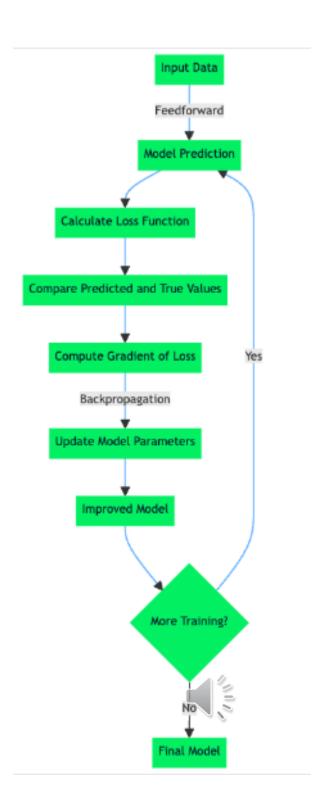


# Neural Network Training: Risk Minimization and Challenges

This topic explores the fundamental concepts of risk minimization and the practical challenges encountered when training neural networks. We will delve into the core principles of loss functions, backpropagation algorithms, and common pitfalls like overfitting and vanishing/exploding gradients. By understanding these aspects, we can develop effective strategies to optimize model performance.

## **Loss Functions for Machine Learning**

- The **loss function** is a mathematical process that quantifies the error margin between a model's prediction and the actual target value.
- Loss function applies to a single training example and is part of the overall model's learning process.
- The learning algorithm and mechanisms in a machine learning model are optimized to minimize the prediction error.
- The learning algorithm leverages this information to conduct weight and parameter updates which in effect during the next training pass leads to a lower prediction error.
- Empirical Risk Minimization(ERM) is an approach to selecting the optimal parameters of a machine learning algorithm that minimizes the empirical risk.
- The empirical risk, in this case, is the training dataset.



## **Importance of Loss Functions**

#### **1** Quantifying Error

Loss functions measure the discrepancy between predicted and actual outputs, providing a quantitative measure of model performance.

#### **Diverse Functions**

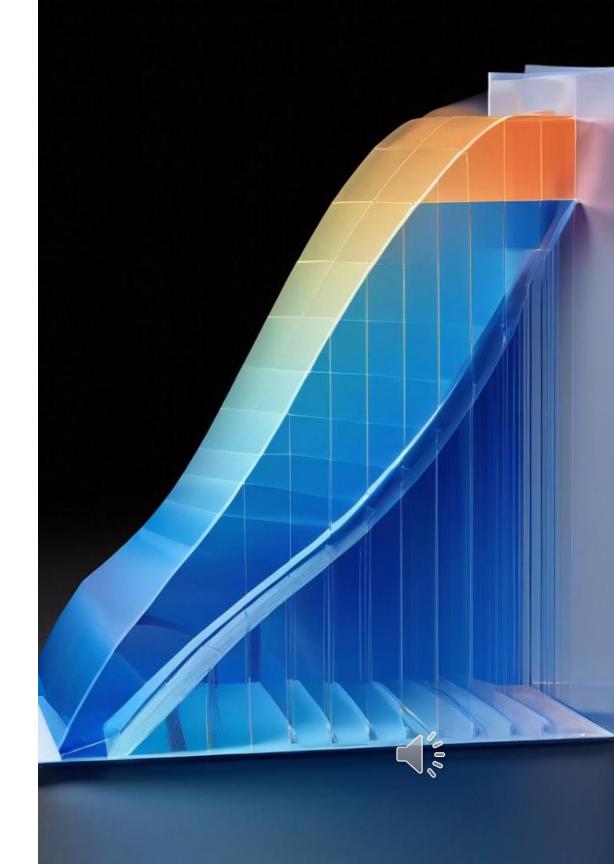
Various loss functions are available, each tailored to specific problem domains and model architectures.

#### **2** Guiding Optimization

By minimizing the loss function, we aim to adjust model parameters, minimizing errors and improving accuracy.

#### Model Evaluation

Loss values provide insights into model performance, allowing for comparisons and selection of optimal models.



## **Types of Loss Functions**

- Loss functions in machine learning can be categorized based on the machine learning tasks to which they are applicable.
- Most loss functions apply to regression and classification machine learning problems.

Loss Function	Applicability to Classification	Applicability to Regression
Mean Square Error (MSE) / L2 Loss	×	•
Mean Absolute Error (MAE) / L1 Loss	×	~
Binary Cross-Entropy Loss / Log Loss	<b>~</b>	×
Categorical Cross-Entropy Loss	<b>✓</b>	×
Hinge Loss	•	×
Huber Loss / Smooth Mean Absolute Error	×	~
Log Loss	<b>~</b>	× dis

## **Loss Functions for Regression**

#### Mean Square Error (MSE) / L2 Loss

- The Mean Square Error(MSE) or L2 loss is a loss function that quantifies the magnitude of the error between a machine learning algorithm prediction and an actual output by taking the average of the squared difference between the predictions and the target values.
- Squaring the difference between the predictions and actual target values results in a higher penalty assigned to more significant deviations from the target value.
- A mean of the errors normalizes the total errors against the number of samples in a dataset or observation.
- MSE is a standard loss function utilized in most regression tasks since it directs the model to optimize to minimize
  the squared differences between the predicted and target values.
- The mathematical equation for Mean Square Error (MSE) or L2 Loss is:

MSE = 
$$(1/n) * \Sigma (y_i - \bar{y})^2$$

#### Where:

- •n is the number of samples in the dataset
- •y<sub>i</sub> is the predicted value for the i-th sample
- ȳ is the target value for the i-th sample



#### Mean Absolute Error (MAE) / L1 Loss

- Mean Absolute Error (MAE), also known as L1 Loss,
- It is a loss function used in regression tasks that calculates the average absolute differences between predicted values from a machine learning model and the actual target values.
- Unlike Mean Squared Error (MSE), MAE does not square the differences, treating all errors with equal weight regardless of their magnitude.
- An outlier's influence on the overall error metric is minimal when using MAE as a loss function.
- The mathematical equation for Mean Absolute Error (MAE) or L1 Loss is:

$$MAE = (1/n) * \Sigma | y_i - \overline{y} |$$

#### Where:

- •n is the number of samples in the dataset
- •y<sub>i</sub> is the predicted value for the i-th sample
- $\bar{y}$  is the target value for the i-th sample



#### **Huber Loss / Smooth Mean Absolute Error**

- Huber Loss or Smooth Mean Absolute Error is a loss function that takes the advantageous characteristics of the Mean Absolute Error and Mean Squared Error loss functions and combines them into a single loss function.
- The hybrid nature of Huber Loss makes it less sensitive to outliers, just like MAE, but also penalizes minor errors within the data sample, similar to MSE.
- The Huber Loss function is also utilized in regression machine learning tasks.
- The mathematical equation for Huber Loss is as follows:

```
 L(\delta, y, f(x)) = (1/2) * (f(x) - y)^2 if |f(x) - y| \le \delta   = \delta * |f(x) - y| - (1/2) * \delta^2 if |f(x) - y| > \delta
```



## **Loss Functions for Classification Binary Cross-Entropy Loss / Log Loss**

- Binary Cross-Entropy Loss(BCE) is a performance measure for classification models that outputs a
  prediction with a probability value typically between 0 and 1, and this prediction value corresponds
  to the likelihood of a data sample belonging to a class or category. In the case of Binary CrossEntropy Loss, there are two distinct classes.
- Binary Cross Entropy Loss (or Log Loss) is a quantification of the difference between the
  prediction of a machine learning algorithm and the actual target prediction that is calculated
  from the negative value of the summation of the logarithm value of the probabilities of the
  predictions made by the machine learning algorithm against the total number of data samples.
- BCE is found in machine learning use cases that are logistic regression problems and in training
  artificial neural networks designed to predict the likelihood of a data sample belonging to a class
  and leverage the <u>sigmoid activation function</u> internally.

$$L(y, f(x)) = -[y * log(f(x)) + (1 - y) * log(1 - f(x))]$$



#### **Hinge Loss**

- Hinge Loss is a loss function utilized within machine learning to train classifiers that optimize to increase the margin between data points and the **decision boundary**.
- Hence, it is mainly used for **maximum margin** classifications.
- To ensure the maximum margin between the data points and boundaries, hinge loss penalizes predictions from the machine learning model that are wrongly classified, which are predictions that fall on the wrong side of the **margin boundary** and also predictions that are correctly classified but are within close proximity to the decision boundary.

$$L(y, f(x)) = max(0, 1 - y * f(x))$$

#### Where:

- •L represents the Hinge Loss
- •y is the true label or target value (-1 or 1)
- •f(x) is the predicted value or decision function output



#### **Choosing the Right Loss Function**

- Selecting the appropriate loss function to apply to a machine learning algorithm is essential, as
  the model's performance heavily depends on the algorithm's ability to learn or adapt its internal
  weights to fit a dataset.
- A machine learning model or algorithm's performance is defined by the loss function utilized, mainly because the loss function component affects the learning algorithm used to minimize the model's error loss or cost function value.
- Essentially, the loss function impacts the model's ability to learn and adapt the value of its internal weights to fit the patterns within a dataset.
- When appropriately selected, the loss function enables the learning algorithm to effectively converge to an optimal loss during its training phase and generalize well to unseen data samples.
- An appropriately selected loss function acts as a guide, steering the learning algorithm towards
  accuracy and reliability, ensuring that it captures the underlying patterns in the data while
  avoiding overfitting or underfitting.



### Factors to consider when selecting a loss function

Factor	Description
Type of Learning Problem	Classification vs Regression; Binary vs Multiclass Classification.
Model Sensitivity to Outliers	Some loss functions are more sensitive to outliers (e.g., MSE), while others are more robust (e.g., MAE).
Desired Model Behavior	Influences how the model behaves, e.g., hinge loss in SVMs focuses on maximizing the margin.
Computational Efficiency	Some loss functions are more computationally intensive, impacting the choice based on available resources.
Convergence Properties	The smoothness and convexity of a loss function can affect the ease and speed of training.
The scale of the Task	For large-scale tasks, a loss function that scales well and can be efficiently optimized is crucial.



## Practical issues in neural network training

Training MLPs can be challenging, often requiring careful selection of hyperparameters, optimization algorithms, and data preprocessing techniques to preprocessing techniques to avoid overfitting and achieve optimal performance.

These challenges are primarily related to several practical problems associated with training, the most important one of which is overfitting.

1 Overfitting

3

The MLP can overfit the training data, leading to poor performance on unseen data. **Difficulties in Convergence** 

Fast convergence of the optimization optimization process is difficult to achieve with very deep networks.

5

The Vanishing and **Exploding Gradient Problems** 

The updates in earlier layers can either either be negligibly small (vanishing (vanishing gradient) or they can be increasingly large (exploding gradient) gradient) in certain types of neural network architectures

**Local and Spurious Optima** 

The optimization function of a neural neural network is highly nonlinear, which has lots of local optima

**Computational Challenges** 

A significant challenge in neural network design is the running time time required to train the network.



## 1. The Problem of Overfitting

#### **High Variance**

The model learns the training data too well, capturing noise and outliers, leading to poor generalization.

#### **Low Bias**

The model fits the training data closely, but fails to generalize to unseen data, leading to poor prediction accuracy.

#### Consequences

Overfitting results in models that perform well on the training data but poorly on new, unseen data.



#### **Techniques to Prevent Overfitting in Neural Networks**

- 1. Simplifying The Model
- 2. Early stopping is a form of regularization while training a model with an iterative method, such as gradient descent
- 3. Use **Data augmentation** which means increasing size of the data which helps in better generalization. Some of the popular image augmentation techniques are flipping, translation, rotation, scaling, changing brightness, adding noise etc.
- **4. Use Regularization** Regularization is a technique to reduce the complexity of the model. It does so by adding a penalty term to the loss function.
- **5. Use Dropouts** Dropout is a regularization technique that prevents neural networks from overfitting. It randomly drops neurons from the neural network during training in each iteration.



# Vanishing and Exploding Gradient Problems

#### **Gradient Descent**

1

The core principle of backpropagation involves adjusting model parameters based on the gradient of the loss function.

#### **Vanishing Gradients**

2

When gradients become extremely small, the learning process slows down, hindering effective weight updates.

#### **Exploding Gradients**

3

Extremely large gradients can cause instability, leading to chaotic weight updates and divergence.



#### Solutions to address vanishing and exploding gradient problems

- A **sigmoid** activation often encourages the vanishing gradient problem, because its derivative is less than 0.25 at all values of its argument, and is extremely small at saturation.
- A **ReLU** activation unit is known to be less likely to create a vanishing gradient problem because its derivative is always 1 for positive values of the argument.
- Aside from the use of the ReLU, a whole host of gradient-descent tricks are used to improve the convergence behavior of the problem.
- In particular, the use of adaptive learning rates and conjugate gradient methods can help in many cases.
- Furthermore, a recent technique called batch normalization is helpful in addressing some of these issues.



## **Difficulties in Convergence**

- Sufficiently fast convergence of the optimization process is difficult to achieve with very deep networks, as depth leads to increased resistance to the training process in terms of letting the gradients smoothly flow through the network.
- This problem is somewhat related to the vanishing gradient problem, but has its own unique characteristics
- Therefore, some "tricks" have been proposed in the literature for these cases, including the use of gating networks and residual networks

gradient is ction is not g a challenge lgorithms.
loss function eading to d potential timization
•

## **Local and Spurious Optima**

When the parameter space is large, and there are many local optima, it makes sense to spend some effort in picking good initialization points. One such method for improving neural network initialization is referred to as **pretraining**.

#### **Local Optima**

Points where the loss function is minimized within a limited region, but not globally.

#### **Spurious Optima**

False minima that do not represent actual optimal solutions, often caused by noise or data irregularities.

#### Challenges

Reaching the global minimum is crucial for optimal performance, but local and spurious optima can hinder convergence.

## Computational Challenges in Neural Network Training



#### **Time Complexity**

Training large neural networks can require significant computational resources and time, especially for complex architectures.



#### **Memory Requirements**

Storing and processing large datasets and model parameters necessitate substantial memory capacity.



#### **Power Consumption**

Training deep neural networks consumes considerable power, requiring optimized hardware and energy management strategies.





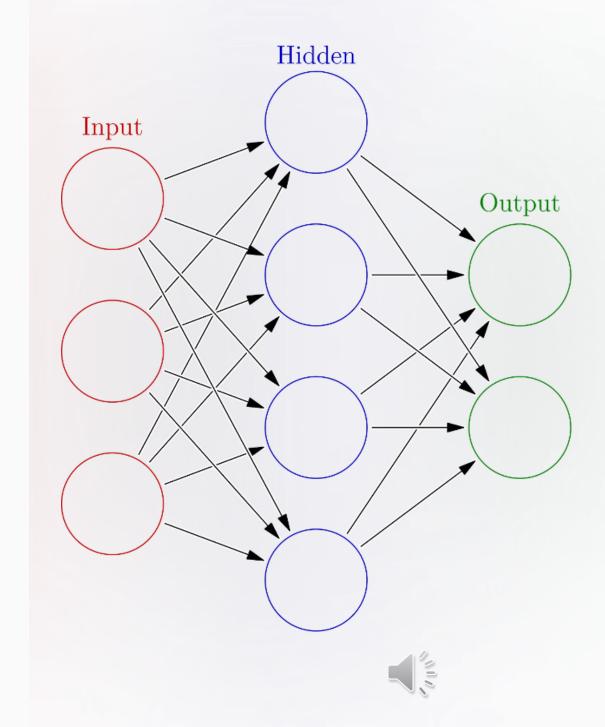
# Applications of Neural Networks

Neural networks have revolutionized various fields of computer science and artificial intelligence, finding applications in areas ranging from speech recognition to image processing.

These networks, inspired by the structure and function of the human brain, have the ability to learn from data and adapt their behavior accordingly.

The core concept involves interconnected nodes, or neurons, arranged in layers.

Each connection between neurons has a weight associated with it, and these weights are adjusted during the learning process to improve the network's performance.



## Speech Recognition

#### Challenges

Speech recognition systems face challenges such as limited vocabulary, grammatical complexities, and the need for retraining for different speakers and conditions.

Acoustic variations, background noise, and speaker-specific accents add further complexity.

#### Role of Neural Networks

Artificial Neural Networks (ANNs) have significantly contributed to advancing speech recognition.

ANNs are trained on vast datasets of speech samples, allowing them to learn complex patterns and model the intricacies of human speech.

Deep learning architectures, such as recurrent neural networks (RNNs) and convolutional neural networks (CNNs), have further enhanced speech recognition capabilities.

#### Applications

Speech recognition finds applications in various areas, including voice assistants, dictation software, speech-to-text conversion, and automated transcription. It enables users to interact with computers using their voice, creating a more natural and intuitive user experience.



## Character Recognition

1 Handwritten Text Recognition

Neural networks excel in recognizing handwritten characters, making them valuable for applications involving handwritten input, such as data entry, signature verification, and document processing.

3 Character Segmentation

Neural networks play a crucial role in segmenting characters from images, effectively isolating individual characters for accurate recognition. This is particularly important in scenarios where characters are densely packed or handwritten styles vary greatly.

2 Optical Character Recognition (OCR)

OCR systems, powered by neural networks, enable the conversion of images containing text into machine-readable format. This has significant implications for digitizing documents, automating data extraction, and accessibility for visually impaired individuals.

4 Applications

Character recognition has widespread applications, including digitalizing historical documents, processing bank checks, translating handwritten notes, and creating accessibility tools for the visually impaired.

## Human Face Recognition

1

#### **Face Detection**

The first step in face recognition is identifying regions within an image that contain faces. Neural networks trained on extensive datasets of faces can effectively distinguish faces from non-face regions.

#### **Feature Extraction**

Once faces are detected, neural networks extract key features from them, such as the distance between eyes, nose shape, and jawline. These features are then represented as numerical vectors.

Face Matching

3

Finally, the extracted feature vectors are compared against a database of known faces. Neural networks are adept at matching these vectors, enabling accurate identification of individuals.

Q

## Image Compression

Neural Network	Traditional Methods
Can learn complex patterns in images, leading to higher compression ratios.	Often rely on pre-defined patterns, leading to lower compression ratios.
Can adapt to different image types, resulting in better compression quality.	May not perform well with diverse image types.
Can handle noise and distortions in images effectively.	May struggle with noisy or distorted images.

#### Stock Market Prediction

\_\_\_\_ Data Collection

Neural networks are trained on historical stock market data, including price trends, company financials, economic indicators, and news sentiment. This data provides insights into market behavior.

—— Pattern Recognition

Neural networks analyze the vast amount of collected data, identifying complex patterns and relationships that might be missed by traditional methods. This allows them to learn from historical trends.

3 Prediction

2

Based on the learned patterns, neural networks predict future stock prices. However, it's important to note that stock market prediction is inherently complex and even the most advanced models have limitations.

## Traveling Salesman Problem

#### **Problem Definition**

The Traveling Salesman Problem (TSP) involves finding the shortest possible route that visits a set of cities exactly once and returns to the starting city. It's a classic optimization problem with applications in logistics and transportation.

#### Neural Network Approach

Neural networks can provide approximate solutions to the TSP by learning to estimate the optimal route based on the distances between cities. However, they may not always find the absolute shortest route.

#### Limitations

The performance of neural networks for TSP depends on the size and complexity of the problem. For very large sets of cities, finding an optimal solution remains computationally challenging.



## Natural Language Processing



#### Natural Language Generation (NLG)

Neural networks can generate coherent and grammatically correct text based on input data or instructions. This enables applications like chatbots, text summarization, and creative writing.



#### Machine Translation

Neural networks have significantly improved machine translation accuracy. They learn the complex relationships between languages, enabling more natural and fluent translations.



#### Sentiment Analysis

Neural networks analyze text to determine the underlying sentiment or emotion expressed. This has applications in customer feedback analysis, brand monitoring, and social media analytics.



## Image Processing

#### Remote Sensing

Neural networks are used for analyzing satellite imagery, identifying land cover changes, monitoring natural disasters, and supporting agricultural planning.

#### Medical Imaging

Neural networks assist in analyzing medical images, such as X-rays, MRI scans, and CT scans, to detect abnormalities and aid in diagnosis.

#### Security

Image processing using neural networks enables facial recognition for security purposes, object detection in surveillance systems, and automated identification of individuals.

## Miscellaneous Applications

1 Self-Driving Cars

Neural networks are critical for autonomous vehicles, enabling them to perceive their surroundings, navigate roads, and make real-time decisions.

2 Social Media

Neural networks power content recommendation engines, personalize user experiences, and detect harmful content on social media platforms.

3 Marketing and Sales

Neural networks analyze customer data, predict buying behavior, and optimize marketing campaigns to improve targeting and conversion rates.

4 Personal Assistants

Neural networks enable personal assistants like Siri and Alexa to understand natural language, respond to queries, and perform tasks based on user requests.

