Exponentiation

Finite cyclic group G (for example $G = \mathbb{Z}_p^*$)

Goal: given g in G and x compute g^x

Example: suppose $x = 53 = (110101)_2 = 32+16+4+1$

Then:
$$g^{53} = g^{32+16+4+1} = g^{32} \cdot g^{16} \cdot g^4 \cdot g^1$$

$$g \longrightarrow g^2 \longrightarrow g^4 \longrightarrow g^8 \longrightarrow g^{16} \longrightarrow g^{32}$$
 g^{53}