

## MATHEMATICAL QUESTIONS

### Question 1

If the two networks shown in each of Figs. 1 and 2 are equivalent, specify values for  $L_a$ ,  $L_b$ , and  $L_c$ . For each equivalent circuit, show that  $L_a$ ,  $L_b$ , and  $L_c$  can be non-negative by a proper choice of  $n$

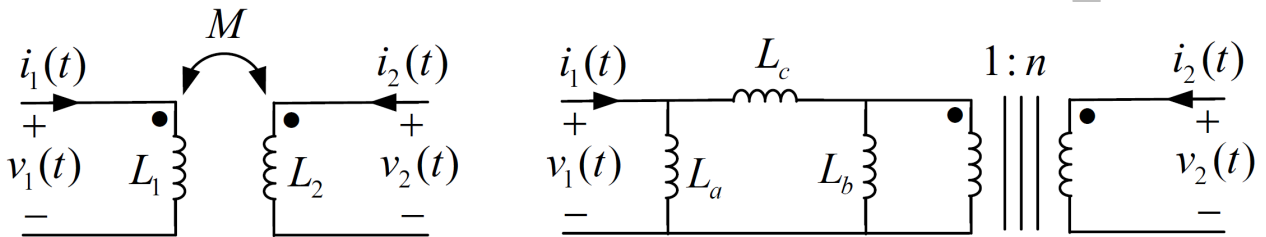


Figure 1: A pair of coupled inductors and its T equivalent circuit.

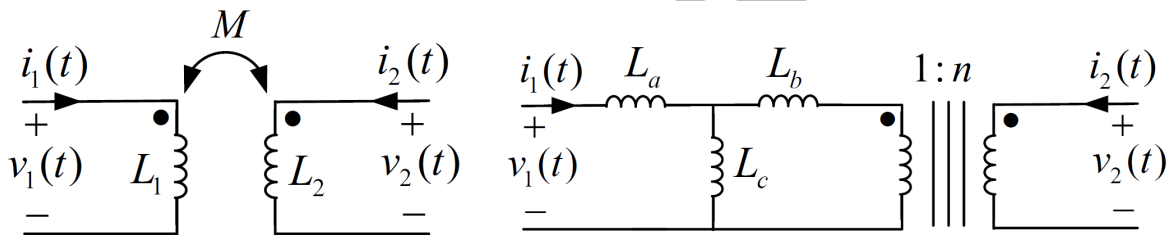


Figure 2: A pair of coupled inductors and its  $\pi$  equivalent circuit.

### Question 2

Find the frequency response  $H(j\omega) = \frac{V_o(j\omega)}{V_s(j\omega)}$  of the double-tuned circuit shown in Fig. 3.

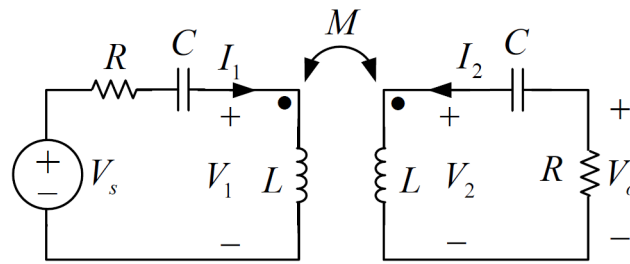


Figure 3: Double-tuned circuit.

### Question 3

For the circuit of Fig. 4, find the input impedance  $Z_{in}$  seen from the source terminals.

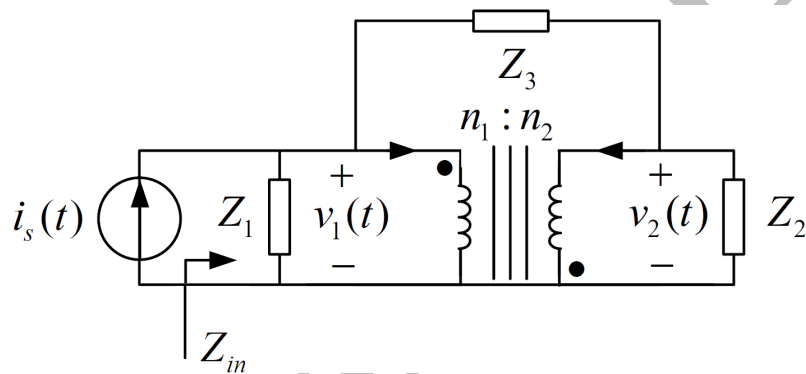


Figure 4: A circuit for which the input impedance is required.

### Question 4

Calculate  $I_x$  and  $V_2$  as labeled in Fig. 5.

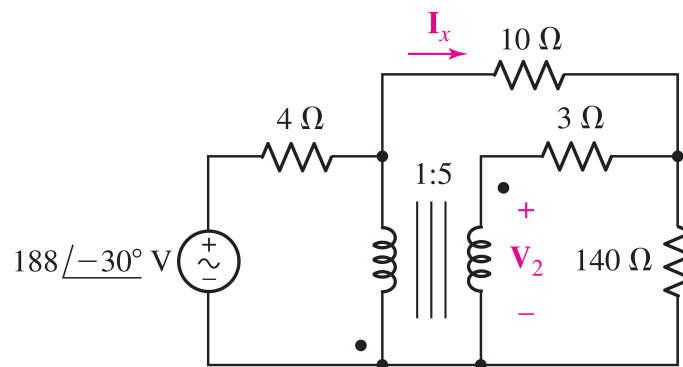


Figure 5: A simple circuit having an ideal transformer.

### Question 5

With respect to the circuit depicted in Fig. 6,

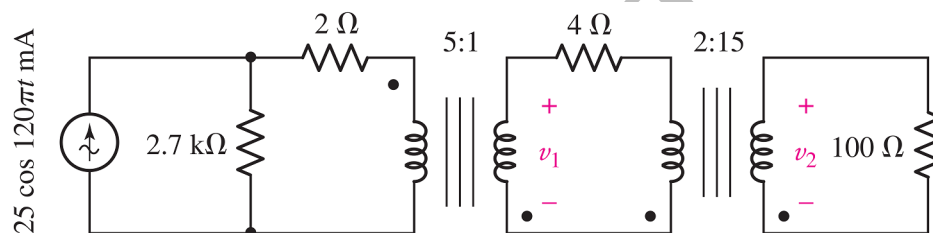


Figure 6: A circuit with two ideal transformers.

(a) Calculate the voltages  $v_1$  and  $v_2$ .

(b) Compute the average power delivered to each resistor.

## SOFTWARE QUESTIONS

## Question 6

A real transformer is usually modeled as the circuit of Fig. 6, where  $L_p$  is the primary leakage inductance,  $R_p$  is the primary copper loss,  $R_c$  is the core losses due to eddy currents and hysteresis,  $L_m$  is the magnetization inductance,  $L_s$  is the secondary leakage inductance, and  $R_s$  is the secondary copper loss. Use [CircuitLab](#), which is an online circuit simulation platform, to investigate the impact of  $L_p$ ,  $R_p$ ,  $R_c$ ,  $L_m$ ,  $L_s$ , and  $R_s$  on the transformer performance. You may plot the voltages of the primary and secondary versus time to investigate the impact of each item.

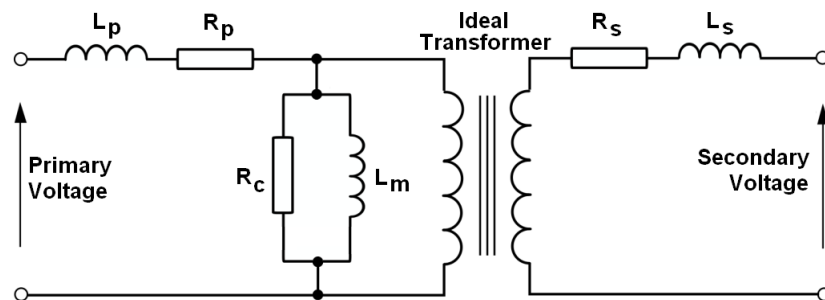


Figure 7: Real transformer equivalent circuits.

## BONUS QUESTIONS

## Question 7

Return your answers by filling the  $\text{\LaTeX}$  template of the assignment. If you want to add a circuit schematic, you can draw it directly using TikZ package, or draw it in a secondary application such as Microsoft Visio and then, import it as a figure.

## EXTRA QUESTIONS

## Question 8

Feel free to solve the following questions from the book *"Engineering Circuit Analysis"* by W. Hayt, J. Kemmerly, and S. Durbin.

1. Chapter 13, question 5.
2. Chapter 13, question 18.
3. Chapter 13, question 21.
4. Chapter 13, question 22.
5. Chapter 13, question 44.
6. Chapter 13, question 48.

Mohammad Hadi