

In the Name of GOD



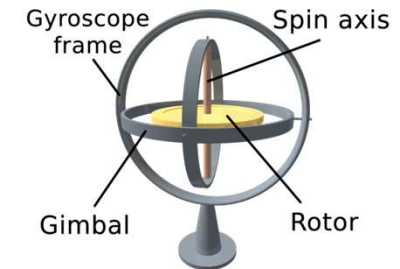
## Guidance and Navigation I: Inertial Sensors

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## Fundamental principles of gyroscopes



- Gyroscopic inertia:** a gyroscopic element tends to maintain the direction of spin axis with respect to the inertial frame



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2

## Fundamental principles of gyroscopes



- Angular momentum

$$H = I\omega_s$$

the angular momentum is chosen to be very high

**Drift:** any undesired deviation of the spin axis

Angular momentum can be increased using a large rotor

=>

- Drift ↓ ☺
- Startup time ↑ ☹
- Bandwidth ↓ ☹

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3

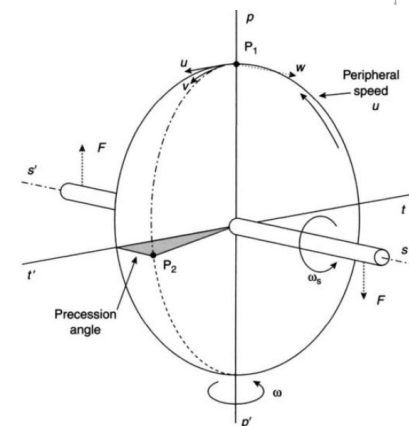
## Fundamental principles of gyroscopes



- Precession:** If the disc is acted upon by a couple, that is, a torque being about the axis  $tt'$ , the spin axis of the disc will be forced to turn about the axis  $pp'$ .

- Law of Gyroscope**

$$\mathbf{T} = \boldsymbol{\omega} \times \mathbf{H}$$

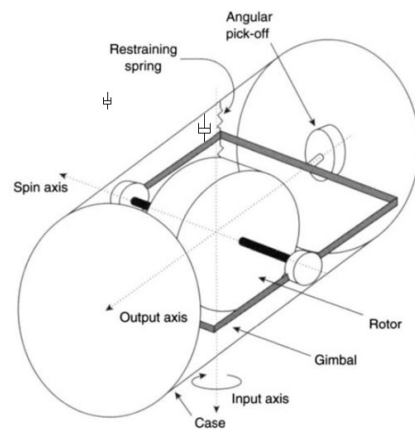


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4

## single-axis rate gyroscope



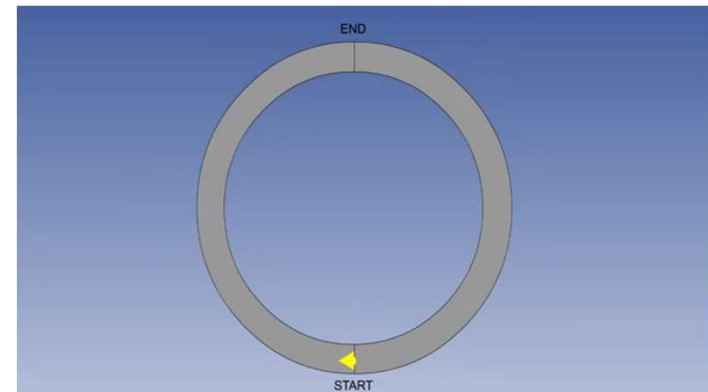
Forced balance?

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5

## Fiber Optic Gyroscope (FOG)

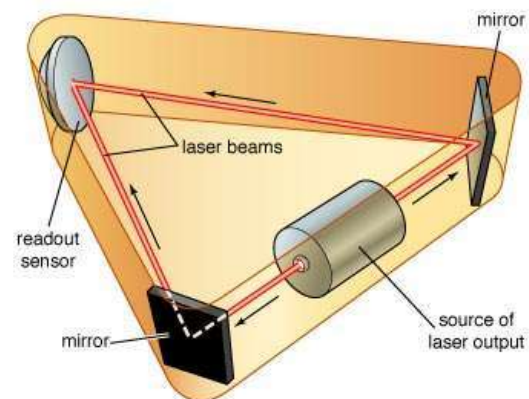


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6

## Ring Laser Gyro (RLG)

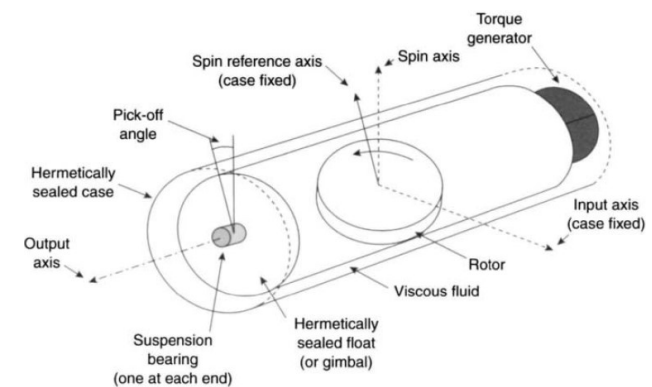


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7

## Rate-integrating gyroscope

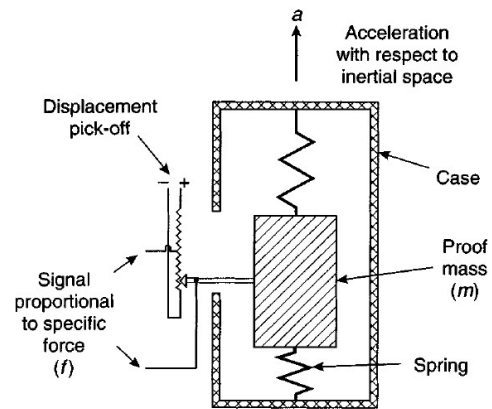


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8

### Spring-mass accelerometer

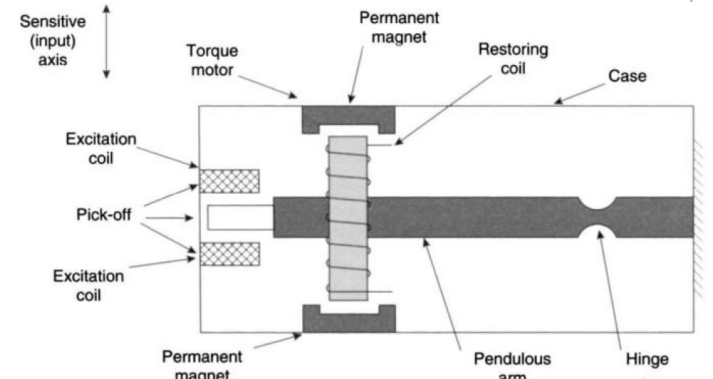


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9

### Force-feedback pendulous accelerometer

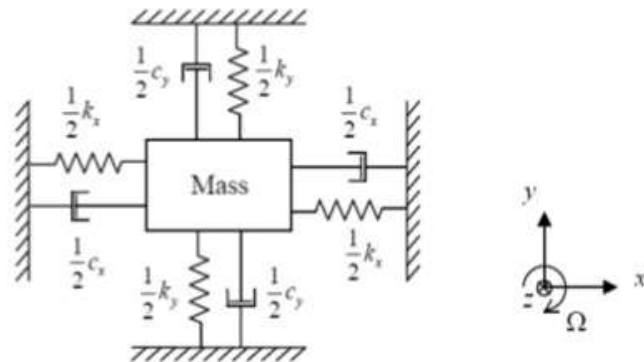


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10

### MEMS Gyroscope

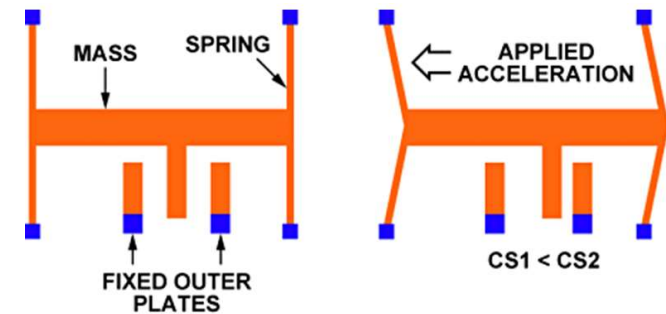


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11

### MEMS Accelerometer



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12

## Errors of a gyroscopic



- **Fixed bias ( $^{\circ}/h$ ):** the sensor output which is present even in the absence of an applied input rotation
- **Acceleration/g-dependent bias ( $^{\circ}/h/g$ ):** Biases which are proportional to the magnitude of the applied acceleration (as a result of mass unbalance in the rotor suspension)
- **$g^2$ -dependent bias ( $^{\circ}/h/g^2$ ):** Biases which are proportional to the product of acceleration along orthogonal pairs of axes
- **Scale-factor errors (ppm):** Errors in the ratio relating the change in the output signal to a change in the input rate which is to be measured and compensated.
- **Cross-coupling errors (ppm):** sensitivity to turn rates about other axes (due to non-orthogonality of the sensor axes)

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13

## Rate Table



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## Tilt and Index Table



- Accelerations less than  $g$  can be exerted to the accelerometer using a tilt table



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15

## Centrifuge Turn Table



- A centrifuge turn table is used to calibrate an accelerometer.
- The accelerometer is installed in a given distance from the axis of rotation.
- $a = r\omega^2$
- The output is measured in different turn rates and ...



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16