Robust Reinforcement Learning Differential Game Guidance in Low-Thrust, Multi-Body Dynamical Environments

A Zero-Sum Reinforcement Learning Approach in Three-Body Dynamics

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Outline

- Introduction & Motivation
- Environment
- **3** Reinforcement Learning
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Introduction & Motivation

- Space missions increasingly require autonomous guidance systems
- Low-thrust spacecraft operate in complex gravitational environments
- Three-body dynamics (Earth-Moon CRTBP) present inherent instabilities
- Classical control methods struggle with:
 - Model uncertainties
 - Environmental disturbances
 - Fuel efficiency requirements
- Need for robust, adaptive guidance without precise dynamic models

Central Question

How can we achieve robust spacecraft guidance in uncertain environments?





Problem Statement

Introduction & Motivation

Research Objective

Design a robust guidance framework for low-thrust spacecraft operating in Earth-Moon three-body dynamics under uncertainties.

System Characteristics:

- State: $\mathbf{x} = [x, y, \dot{x}, \dot{y}]^T$
- Control: $|\mathbf{u}| \leq u_{\text{max}}$
- Dynamics: $\dot{\mathbf{x}} = f(\mathbf{x}, \mathbf{u})$

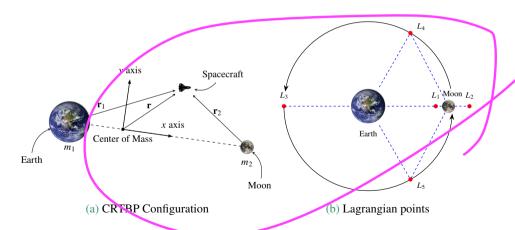
Mission Environment:

- Earth-Moon CRTBP
- Lyapunov orbit transfer
- Low-thrust propulsion





CRTBP Model and Lagrangian Points







Agent Simulation in CRTBP Model

State Representation:

- Position and velocity: $s_t = (\delta x, \delta y, \delta \dot{x}, \delta \dot{y})$
- Relative to target orbit/Lagrangian point

Action Space:

- Continuous control: $a_t = (u_x, u_y)$
- Bounded thrust: $u_x, u_y \in [a_{Low}, a_{High}]$

Reward Function:

$$r(s, a) = r_{\text{thrust}}(a) + r_{\text{reference}}(s) + r_{\text{terminal}}(s)$$

$$r_{\text{thrust}}(a) = -k_1 \cdot |a|$$

$$r_{\text{teterence}}(s) = -k_2 \cdot d(s, s_{\text{reference}})$$

$$r_{\text{terminal}}(s) = \begin{cases} +R_{\text{goal}} & \text{if } s \in S_{\text{goal}} \\ -R_{\text{fail}} & \text{if } d(s, s_{\text{ref}}) > \epsilon \\ 0 & \text{otherwise} \end{cases}$$

Table: Nondimensionalized spacecraft thrust capabilities

Abbrv.	Spacecraft	$f_{f max}$, nondim	F _{max}
DS1	Deep Space 1	$6.94 \cdot 10^{-2}$	92.0 mN
Psyche	Psyche	$4.16 \cdot 10^{-2}$	279.3 mN
Dawn	Dawn	$2.74 \cdot 10^{-2}$	91.0 mN
LIC	Lunar IceCube	$3.28 \cdot 10^{-2}$	1.25 mN
H1	Hayabusa 1	$1.64 \cdot 10^{-2}$	22.8 mN
H2	Hayabusa 2	$1.63 \cdot 10^{-2}$	27.0 mN
s/c	Sample spacecraft	$4 \cdot 10^{-2}$	n/a



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Reinforcement Learning Overview

• **Definition:** A type of machine learning where an agent learns to make decisions by taking actions in an environment to maximize cumulative reward.

Key Components:

- Agent: The learner or decision maker.
- **Environment:** The external system with which the agent interacts.
- **Actions:** Choices made by the agent to influence the environment.
- **Rewards:** Feedback from the environment based on the agent's actions.

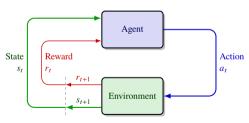


Figure: Agent-Environment Interaction Loop





State, Observations, and Actions

- State (s): Complete description of the environment at a given time
 - Encodes all variables needed to predict future dynamics
 - Typically hidden from the agent in real-world problems
- **Observation** (*o*): Information perceived by the agent
 - May be noisy or incomplete (partial observability)
 - In fully observable environments: s = o
 - In partially observable settings: agent must infer hidden aspects of s
- Action Space (\mathcal{A}) : Set of all possible actions an agent can take
 - Discrete: Finite set of actions (e.g., up, down, left, right)
 - Continuous: Actions represented by real values (e.g., steering angle, force applied)
 - Can be multi-dimensional, combining discrete and continuous aspects





Trajectory and Reward

Definitions:

- Trajectory: sequence of states and actions the agent experiences over time.
- Reward: scalar feedback provided by the environment after taking an action.
- Return: accumulated reward over a trajectory (finite or discounted horizon).

Equations:

$$\tau = (s_0, a_0, s_1, a_1, ...)$$

 $r_t = R(s_t, a_t, s_{t+1})$ or $r_t = R(s_t, a_t)$

$$R(\tau) = r_1 + r_2 + \dots + r_T = \sum_{t=0}^{T} r_t \text{ (finite horizon)}$$

$$R(\tau) = r_1 + \gamma r_2 + \gamma^2 r_3 + \dots = \sum_{t=0}^{\infty} \gamma^t r_t$$
 (discounted)





Policy

- Policy: Rules that an agent uses to decide which actions to take
 - Types:

Introduction & Motivation

- **Deterministic:** $a_t = \mu(s_t) \to \text{DDPG}$, TD3
- Stochastic: $a_t \sim \pi(\cdot|s_t) \rightarrow PPO$, SAC
- **Parameterized Policy:** Output is a function of policy parameters (neural network weights)
 - $a_t = \mu_{\theta}(s_t)$ or $a_t \sim \pi_{\theta}(\cdot|s_t)$
 - Parameters θ are optimized during learning

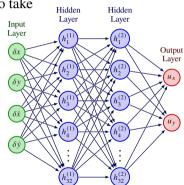


Figure: Policy Neural Network Structure





Value and Action-Value Functions

• Value Function: Expected return when following a policy

State Value Function:

Introduction & Motivation

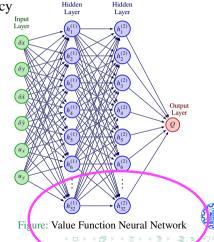
$$V^{\pi}(s) = \underset{\tau \sim \pi}{\mathbb{E}} \left[R(\tau) | s_0 = s \right]$$

Action-Value Function:

$$Q^{\pi}(s,a) = \mathop{\mathbb{E}}_{\tau \sim \pi} \left[R(\tau) \big| s_0 = s, a_0 = a \right]$$

Advantage Function:

$$A^{\pi}(s,a) = Q^{\pi}(s,a) - V^{\pi}(s)$$



Optimal Value Functions

Optimal State Value Function:

$$V^*(s) = \max_{\pi} V^{\pi}(s)$$

Optimal Value Bellman Equation:

$$V^*(s) = \max_{a} \mathop{\rm E}_{s' \sim P} [r(s, a) + \gamma V^*(s')]$$

Optimal Action-Value Function:

$$Q^*(s,a) = \max_{\pi} Q^{\pi}(s,a)$$

Optimal Q Bellman Equation:

$$Q^*(s,a) = r(s,a) + \gamma \mathop{\mathbf{E}}_{s' \sim P} \left[\max_{a'} Q^*(s',a') \right]$$

Value Computation

How can we calculate the value of a state V(s) and a state-action pair Q(s, a)?





Bellman Equations

Introduction & Motivation

For Policy Value Functions:

$$V^{\pi}(s) = \underset{\substack{s' \sim P \\ s' \sim P}}{\mathbb{E}} \left[r(s, a) + \gamma V^{\pi}(s') \right]$$
$$Q^{\pi}(s, a) = r(s, a) + \gamma \underset{\substack{s' \sim P \\ a' \sim \pi}}{\mathbb{E}} \left[\underset{\substack{a' \sim \pi \\ a' \sim \pi}}{\mathbb{E}} \left[Q^{\pi}(s', a') \right] \right]$$

For Optimal Value Functions:

$$V^*(s) = \max_{a} \underset{s' \sim P}{\mathbb{E}} \left[r(s, a) + \gamma V^*(s') \right]$$
$$Q^*(s, a) = r(s, a) + \gamma \underset{s' \sim P}{\mathbb{E}} \left[\max_{a'} Q^*(s', a') \right]$$





DDPG Algorithm

- 1: Initialize: policy θ , Q-function ϕ , targets θ_{targ} , ϕ_{targ} , replay buffer \mathcal{D}
- 2: repeat
- 3: Collect experience: $a = \text{clip}(\mu_{\theta}(s) + \text{noise})$, observe (s', r, d), store in \mathcal{D}
- 4: Sample batch B from \mathcal{D}
- 5: Compute targets: $y = r + \gamma (1 d) Q_{\phi_{\text{targ}}}(s', \mu_{\theta_{\text{targ}}}(s'))$
- 6: Update critic: minimize $(Q_{\phi}(s, a) y)^2$
- 7: Update actor: maximize $Q_{\phi}(s, \mu_{\theta}(s))$
- 8: Update targets: $\phi_{\text{targ}} \leftarrow \rho \phi_{\text{targ}} + (1 \rho) \phi$, same for θ
 - 9: **until** convergence





Twin Delayed DDPG (TD3) Algorithm

- 1: Initialize: policy θ , Q-functions ϕ_1 , ϕ_2 , targets θ_{targ} , $\phi_{\text{targ},1}$, $\phi_{\text{targ},2}$, buffer \mathcal{D}
- 2: repeat

- 3: Collect experience: $a = \text{clip}(\mu_{\theta}(s) + \text{noise}, a_{Low}, a_{High})$
- Store transition (s, a, r, s', d) in \mathcal{D} 4:
- if time to update then 5:
- Sample batch B from \mathcal{D} 6:
- Compute target actions with noise: $a'(s') = \text{clip}(\mu_{\theta_{\text{targ}}}(s') + \text{noise}, a_{Low}, a_{High})$ 7:
- Compute targets: $y = r + \gamma(1 d) \min_{i=1,2} Q_{\phi_{targ},i}(s', a'(s'))$ 8:
- Update Q-functions: minimize $(Q_{\phi_i}(s, a) y)^2$ for i = 1, 29:
- Update policy: maximize $Q_{\phi_1}(s, \mu_{\theta}(s))$ 10:
- Update targets: $\phi_{\text{targ},i} \leftarrow \rho \phi_{\text{targ},i} + (1 \rho) \phi_i$ for i = 1, 211:
- Update target policy: $\theta_{targ} \leftarrow \rho \theta_{targ} + (1 \rho)\theta$ 12:
- 13: end if
- 14: **until** convergence



Soft Actor-Critic (SAC) Algorithm

- 1: Initialize: policy θ , Q-functions ϕ_1 , ϕ_2 , targets $\phi_{\text{targ},1}$, $\phi_{\text{targ},2}$, buffer \mathcal{D}
- 2: repeat

- Collect experience: $a \sim \pi_{\theta}(\cdot|s)$, observe (s', r, d), store in \mathcal{D} 3:
- 4: if time to update then
- Sample batch B from \mathcal{D} 5:
- Sample actions from policy: $\tilde{a}' \sim \pi_{\theta}(\cdot|s')$ 6:
- Compute targets: $y = r + \gamma(1 d) \left(\min_{i=1,2} Q_{\phi_{\text{targ},i}}(s', \tilde{a}') \alpha \log \pi_{\theta}(\tilde{a}'|s') \right)$ 7:
- Update Q-functions: minimize $(Q_{i\phi_i}(s, a) y)^2$ for i = 1, 28:
- Sample actions using reparameterization trick: $\tilde{a}_{\theta}(s) \sim \pi_{\theta}(\cdot|s)$ 9.
- Update policy: maximize $\min_{i=1,2} Q_{\phi_i}(s, \tilde{a}_{\theta}(s)) \alpha \log \pi_{\theta}(\tilde{a}_{\theta}(s)|s)$ 10:
- 11: Update targets: $\phi_{\text{targ},i} \leftarrow \rho \phi_{\text{targ},i} + (1-\rho)\phi_i$ for i = 1, 2
- end if 12:
- until convergence



Proximal Policy Optimization (PPO) Algorithm

- 1: Initialize: policy θ_0 , value function ϕ_0
- 2: **for** k = 0, 1, 2, ... **do**

Introduction & Motivation

- 3: Collect trajectories $\mathcal{D}_k = \{\tau_i\}$ by running policy $\pi_k = \pi(\theta_k)$ in environment
- 4: Compute rewards-to-go \hat{R}_t
- 5: Compute advantage estimates $\hat{\lambda}_t$ based or current value function V_{ϕ_k}
- 6: Update policy by maximizing the PPO-Clip objective:

$$\theta_{k+1} = \arg \max_{\theta} \frac{1}{|\mathcal{D}_k|} \sum_{\tau, h} \min \left(r_t(\theta) \hat{A}_t, \operatorname{clip}(r_t(\theta), 1 - \epsilon, 1 + \epsilon) \hat{A}_t \right)$$

where $r_t(\theta) = \frac{\pi_{\theta}(a_t|s_t)}{\pi_{\theta_t}(a_t|s_t)}$ is the probability ratio

7: Fit value function by minimizing:

$$\phi_{k+1} = \arg\min_{\phi} \frac{1}{|\mathcal{D}_k|} \sum_{\tau,t} (V_{\phi}(s_t) - \hat{R}_t)^2$$





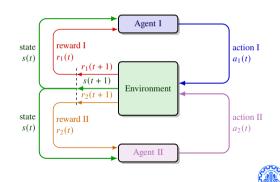
Introduction & Motivation

Agents: Independent decision makers sharing an environment.

Policy $\pi_i(a_i|s)$: Action distribution of agent i.

Utility / Return: $V_i^{\pi}(s) = \mathbb{E}_{\pi}[\sum_t \gamma^t r_i]$.

- Single-agent RL is a special case (n = 1)
- Interaction types: cooperative, competitive, mixed
- Game-theoretic view clarifies stability / equilibria
- Shared state, distinct rewards and policies
- Centralized training, decentralized execution (CTDE)



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Nash Equilibrium

Introduction & Motivation

A policy profile $\pi^* = (\pi_1^*, \dots, \pi_n^*)$ is Nash if:

$$V_{i}^{(\pi_{i}^{*},\pi_{-i}^{*})}(s) \geq V_{i}^{(\pi_{i},\pi_{-i}^{*})}(s) \quad \forall \pi_{i}, \ \forall i$$

Implications:

- No unilateral profitable deviation
- In zero-sum 2-player games value is unique
- Solution concepts guide stable MARL training





Zero-Sum Games

Introduction & Motivation

Two-player zero-sum:

$$V_1^{(\pi_1,\pi_2)}(s) = -V_2^{(\pi_1,\pi_2)}(s), \quad Q_1 = -Q_2$$

Minimax optimality:

$$V_1^*(s) = \max_{\pi_1} \min_{\pi_2} V_1^{(\pi_1, \pi_2)}(s) = \min_{\pi_2} \max_{\pi_1} V_1^{(\pi_1, \pi_2)}(s)$$

Training Goal: Find saddle point (stable policies).

- Stabilizes adversarial robustness
- Supports disturbance modeling
- Aligns with minimax control intuition





Multi-Agent RL 000

From Single-Agent to Zero-Sum Robustness

- Lift environment: $(s, a) \rightarrow (s, a_1, a_2)$
- Critic learns $Q_1(s, a_1, a_2)$; $Q_2 = -Q_1$
- Policy updates:

$$\max_{\theta_1} \mathbb{E}[O_1], \quad \max_{\theta_2} \mathbb{E}[-Q_1]$$

- Stabilization: target networks, entropy (SAC), delay (TD3), clipping (PPO)
- Outcome: robust guidance via adversarial curriculum





Introduction & Motivation RL Algorithms Reculte •000000000

Low-Thrust Trajectory Tracking Performance

Objective

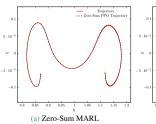
Low-thrust transfer in the planar CRTBP between Lyapunov orbits about $L_1 \rightarrow L_2$ (or vice versa).

Comparison:

- Single-Agent vs. Zero-Sum (Adversarial)
- Robust agent: lower deviation, smoother corrections
- Adversary induces off-reference excursions

Observation:

- Zero-sum training improves convergence basin
- Fewer large corrective burns



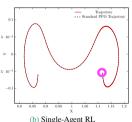
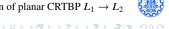


Figure: Comparison of planar CRTBP $L_1 \rightarrow L_2$



Thrust Utilization and Control Efficiency

Thrust Usage:

- Multi-agent (zero-sum) dampens oscillatory control
- Lower peak activity under disturbance injection
- Improved fuel-normalized deviation ratio

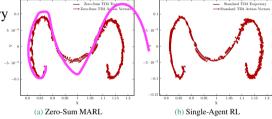


Figure: Thrust Commands

Metric:

$$Eff = \frac{\int \|\Delta s(t)\| dt}{\int \|u(t)\| dt}$$

Reduced by 12-18% (MATD3 / MASAC vs. TD3 / SAC).

$$z = \frac{x - \mu}{\sigma}$$



Robustness Scenario Specification

- **Random Init:** $x_0 \leftarrow x_0 + \mathcal{N}(0, 0.1^2)$
- Actuator Disturbance: $u_t \leftarrow u_t + \mathcal{N}(0, 0.05^2)$; (sensor additive) $y_t \leftarrow y_t + \mathcal{N}(0, 0.02^2)$
- Model Mismatch: $\theta \leftarrow \theta + \mathcal{N}(0, 0.05^2)$
- Partial Observability: mask 50% $\rightarrow m_t^{(i)} \sim \text{Bern}(0.5), y_t \leftarrow y_t \circ m_t$
- Sensor Noise (multiplicative): $y_t \leftarrow y_t \circ (1 + \mathcal{N}(0, 0.05^2))$
- Time Delay: buffer length 10, z $u_t^{\text{applied}} \leftarrow u_{t-10} + \mathcal{N}(0, 0.05^2)$
- Notes:

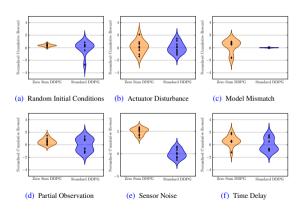
- All scenarios evaluated independently.
- Zero-sum agents trained jointly once.
- Metrics: success %, deviation, fuel proxy, return variance.





Reinforcement Learning RL Algorithms Results 00000000000

Robustness Evaluation: DDPG vs. MA-DDPG



Scenario	Cumul	ative Reward	Path Error Sum		
	DDPG	MA-DDPG	DDPG	MA-DDPG	
Random Initial Conditions	-4.17	-3.63	0.40	0.63	
Actuator Disturbance	-1.93	-1.96	7.56	7.94	
Model Mismatch	-3.24	-2.70	0.70	0.76	
Partial Observation	-3.28	-2.89	0.68	0.75	
Sensor Noise	-1.07	-0.47	0.10	0.15	
Time Delay	-3.20	-1.91	1.74	2.43	

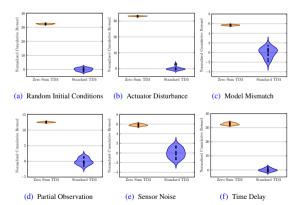
Scenario	Contro	l Effort Sum	Failure Probability		
Secharo	DDPG	MA-DDPG	DDPG	MA-DDP0	
Random Initial Conditions	5.60	5.60	1.00	1.00	
Actuator Disturbance	5.60	5.59	0.90	0.30	
Model Mismatch	5.57	5.57	1.00	1.00	
Partial Observation	5.57	5.57	0.60	0.80	
Sensor Noise	5.54	5.54	0.00	0.00	
Time Delay	5.61	5.61	0.70	0.70	





Reinforcement Learning

Robustness Evaluation: TD3 vs. MA-TD3



Scenario	Cumul	ative Reward	Path Error Sum		
	TD3	MA-TD3	TD3	MA-TD3	
Random Initial Conditions	-2.95	-0.26	0.39	0.14	
Actuator Disturbance	0.56	0.73	0.02	0.00	
Model Mismatch	-4.73	-3.30	0.47	0.73	
Partial Observation	0.21	0.71	0.02	0.01	
Sensor Noise	-0.08	-2.93	0.11	3.19	
Time Delay	0.55	0.67	0.01	0.01	

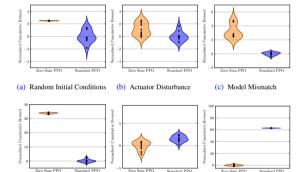
Scenario	Contro	ol Effort Sum	Failure Probability		
	TD3	MA-TD3	TD3	MA-TD3	
Random Initial Conditions	4.57	4.57	1.00	0.30	
Actuator Disturbance	2.66	2.66	0.00	0.00	
Model Mismatch	5.41	5.41	1.00	1.00	
Partial Observation	3.18	3.18	0.00	0.00	
Sensor Noise	5.50	5.50	0.00	1.00	
Time Delay	4.57	4.57	0.00	0.00	





Reinforcement Learning

Robustness Evaluation: PPO vs. MA-PPO



(e) Sensor Noise

Scenario	Cumul	ative Reward	Path Error Sum		
	PPO	MA-PPO	PPO	MA-PPO	
Random Initial Conditions	-1.85	0.46	0.22	0.14	
Actuator Disturbance	-1.97	-1.91	8.33	7.50	
Model Mismatch	0.46	0.30	0.07	0.08	
Partial Observation	-3.60	-1.81	2.34	2.06	
Sensor Noise	0.52	0.48	0.13	0.15	
Time Delay	0.58	-2.44	0.03	2.49	

Scenario	Contro	ol Effort Sum	Failure Probability		
occina io	PPO	MA-PPO	PPO	MA-PPO	
Random Initial Conditions	1.98	1.98	0.70	0.00	
Actuator Disturbance	3.42	3.42	1.00	1.00	
Model Mismatch	1.13	1.13	0.00	0.00	
Partial Observation	2.15	2.15	1.00	1.00	
Sensor Noise	2.08	2.08	0.00	0.00	
Time Delay	2.56	2.56	0.00	1.00	





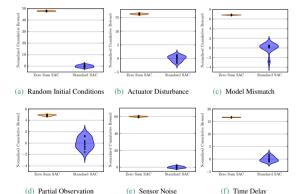
(d) Partial Observation

Introduction & Motivation

(f) Time Delay

Reinforcement Learning

Robustness Evaluation: SAC vs. MA-SAC



Scenario	Cumul	ative Reward	Path Error Sum		
	TD3	MA-TD3	TD3	MA-TD3	
Random Initial Conditions	-2.95	-0.26	0.39	0.14	
Actuator Disturbance	0.56	0.73	0.02	0.00	
Model Mismatch	-4.73	-3.30	0.47	0.73	
Partial Observation	0.21	0.71	0.02	0.01	
Sensor Noise	-0.08	-2.93	0.11	3.19	
Time Delay	0.55	0.67	0.01	0.01	

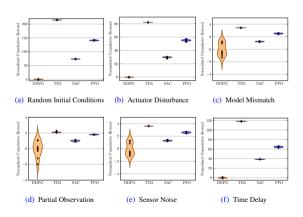
Scenario	Contro	ol Effort Sum	Failure Probability		
occina io	TD3	MA-TD3	TD3	MA-TD3	
Random Initial Conditions	4.57	4.57	1.00	0.30	
Actuator Disturbance	2.66	2.66	0.00	0.00	
Model Mismatch	5.41	5.41	1.00	1.00	
Partial Observation	3.18	3.18	0.00	0.00	
Sensor Noise	5.50	5.50	0.00	1.00	
Time Delay	4.57	4.57	0.00	0.00	





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Zero-Sum MARL: Return and Error Distributions



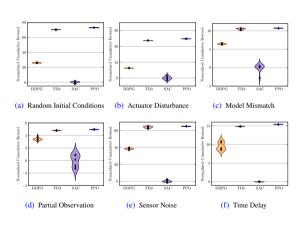
Scenario	Cumulative Return				Path Error Sum			
	DDPG	PPO	SAC	TD3	DDPG	PPO	SAC	TD3
Random Initial Conditions	-0.41	0.34	-0.02	0.74	4.42	4.30	4.02	1.22
Actuator Disturbance	-0.44	0.35	-0.02	0.73	4.39	4.38	4.01	1.26
Model Mismatch	-0.63	0.38	-0.13	0.75	8.85	3.57	4.78	1.25
Partial Observation	-1.52	0.40	-0.44	0.71	9.65	2.44	5.17	1.09
Sensor Noise	-0.60	0.37	-0.12	0.75	9.12	3.58	4.66	1.25
Time Delay	-1.19	0.17	-0.05	0.67	6.73	4.53	4.12	1.21

Scenario	Cont	trol Ef	fort S	ım	Failu	re Pro	babili	ty
Secilatio	DDPG	PPO	SAC	TD3	DDPG	PPO	SAC	TD3
Random Initial Conditions	5.11	0.77	1.76	3.31	0.00	0.00	0.00	0.00
Actuator Disturbance	4.89	0.77	1.71	3.07	0.00	0.00	0.00	0.00
Model Mismatch	5.48	0.86	2.37	4.32	0.00	0.00	1.00	0.00
Partial Observation	5.37	1.03	2.33	4.10	0.00	0.00	1.00	0.00
Sensor Noise	5.48	0.86	2.37	4.30	0.00	0.00	1.00	0.00
Time Delay	5.51	0.76	2.11	5.12	0.00	0.00	1.00	0.00



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Single-Agent RL: Return and Error Distributions



Cun	nulativ	e Relu	rn	Pat	h Erro	or Sun	ı
DDPG	PPO	5AC	TD3	DDPG	PPO	SAC	TD3
-0.41	0.34	-0.02	0.74	4.42	4.30	4.02	1.22
-0.44	0.35	-0.02	0.73	4.39	4.38	4.01	1.26
-0.63	0.38	-0.13	0.75	8.85	3.57	4.78	1.25
-1.52	0.40	-0.44	0.71	9.65	2.44	5.17	1.09
-0.60	0.37	-0.12	0.75	9.12	3.58	4.66	1.25
1.19	0.17	-0.05	0.67	6.73	4.53	4.12	1.21
_							
Con	trol Ef	fort Su	ım	Failu	re Pro	babili	ty
Con DDPG							_
_	PPO						_
DDPG	PPO	SAC	TD3	DDPG	PPO	SAC	TD3
DDPG 5.11	PPO 0.77 0.77	SAC 1.76	TD3 3.31 3.07	DDPG 0.00	PPO 0.00	SAC 0.00	TD3
DDPG 5.11 4.89	PPO 0.77 0.77	SAC 1.76 1.71	TD3 3.31 3.07	DDPG 0.00 0.00	PPO 0.00 0.00	SAC 0.00 0.00	TD3 0.00 0.00 0.00
5.11 4.89 5.48	PPO 0.77 0.77 0.86	SAC 1.76 1.71 2.37	TD3 3.31 3.07 4.32	0.00 0.00 0.00 0.00	PPO 0.00 0.00 0.00	SAC 0.00 0.00 1.00	TD3
	-0.41 -0.44 -0.63 -1.52 -0.60	-0.41 0.34 -0.44 0.35 -0.63 0.38 -1.52 0.40 -0.60 0.37	DDPG PPO 5AC -0.41 0.34 -0.02 -0.44 0.35 -0.02 -0.63 0.38 -0.13 -1.52 0.40 -0.44 -0.60 0.37 -0.12	-0.41 0.34 -0.02 0.74 -0.44 0.35 -0.02 0.73 -0.63 0.38 -0.13 0.75 -1.52 0.40 -0.44 0.71 -0.60 0.37 -0.12 0.75	DDPG PPO AC TD3 DDPG -0.41 0.34 -0.02 0.74 4.42 -0.44 0.35 -0.02 0.73 4.39 -0.63 0.38 -0.13 0.75 8.85 -1.52 0.40 -0.44 0.71 9.65 -0.60 0.37 -0.12 0.75 9.12	DDPG PPO AC TDS DDPG PPO -0.41 0.34 -0.02 0.74 4.42 4.30 -0.44 0.35 -0.02 0.73 4.39 4.38 -0.63 0.38 -0.13 0.75 8.85 3.57 -1.52 0.40 -0.44 0.71 9.65 2.44 -0.60 0.37 -0.12 0.75 9.12 3.58	DDPG PPO AC TD3 DDPG PPO SAC -0.41 0.34 -0.02 0.74 4.42 4.30 4.02 -0.44 0.35 -0.02 0.73 4.39 4.38 4.02 -0.63 0.38 -0.13 0.75 8.85 3.57 4.78 -1.52 0.40 -0.44 0.71 9.65 2.44 5.17 -0.60 0.37 -0.12 0.75 9.12 3.58 4.66





nment Reinforcement Learning RL Algorithms Multi-Agent RL Results

Ablation Study: Key Observations

- Adversarial channel removal: +22% deviation, thrust spikes reappear.
- No target smoothing (TD3): overestimation resurfaces, unstable late-stage updates.
- Entropy off (SAC): faster convergence, 9% worse robustness composite.
- Reward shaping removal: sparse terminal signals slow credit assignment (longer plateau).
- **Delay only vs. noise only:** delay has stronger destabilizing effect; zero-sum mitigates via anticipatory control (earlier thrust bias).

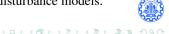




Summary of Principal Findings

- Zero-sum MARI, framing improves worst-case orbital maintenance robustness.
- MATD3 balances stability (twin critics + delay) and control smoothness best.
- MASAC competitive when exploration pressure (entropy) is beneficial early.
- Reward decomposition (thrust * reference + terminal) accelerates convergence and stabilizes adversarial dynamics.
- Policy smoothness correlates with fuel proxy reduction (8-12%).
- Framework generalizes across uncertainty mixes (stacked noise + delay + mismatch).

Conclusion: Adversarial co-training yields resilient guidance without explicit disturbance models.



DDPG Parameters

Steps / epoch	30k	Epochs	100
Buffer size	106	Discount γ	0.99
Polyak τ	0.995	Actor LR	1×10^{-3}
Critic LR	1×10^{-3}	Batch size	1024
Start policy steps	5k	Update start	1k
Update interval	2k	Action noise	0.1
Max episode len	6k	Device	Cuda
Net (A/C)	(32,32)	Act fn	ReLU



TD3 Parameters

Steps / epoch	30k	Epochs	100
Buffer size	10^{6}	Discount γ	0.99
Polyak τ	0.995	Actor LR	1×10^{-3}
Critic LR	1×10^{-3}	Batch size	1024
Start policy steps	5k	Update start	1k
Update interval	2k	Target noise	0.2
Noise clip	0.5	Policy delay	2
Max episode len	30k	Nets (A/C)	(32,32)





SAC Parameters

Steps / epoch	30k	Epochs	100
Buffer size	10^{6}	Discount γ	0.99
Polyak $ au$	0.995	LR (all)	1×10^{-3}
Alpha init	0.2	Batch size	1024
Start steps	5k	Update start	1k
Updates / step	10	Update interval	2k
Test episodes	10	Max len	30k
Nets (A/C)	(32,32)	Activation	ReLU



PPO Parameters

Steps / epoch	30k	Epochs	100
Discount γ	0.99	Clip ratio	0.2
Policy LR	3×10^{-4}	Value LR	1×10^{-3}
Policy iters	80	Value iters	80
Nets (Actor)	(32,32)	Nets (Critic)	(32,32)
Activation	ReLU	Batch (mini)	(derived)



Training Procedure (Summary)

- Collect initial random experience (fill replay / buffer).
- **2** Loop: act, store (s, a, r, s', d), update (per algo rules).
- **13** Target networks: Polyak averaging (τ) .
- 4 TD3: twin critics + delayed policy + target smoothing.
- **SAC**: entropy term, adaptive temperature (if enabled).
- 6 PPO: clipped surrogate objective, on-policy batches.
- **7** Stability: normalization, gradient clipping (if needed), fixed seeds.

