

$$7. \int_0^1 (x^3 - 3x^2 + 2x) + \int_1^2 (x^3 - 3x^2 + 2x)$$

$$\left[ \frac{1}{4}x^4 - x^3 + x^2 \right]_0^1 + \left[ \frac{1}{4}x^4 - x^3 + x^2 \right]_1^2$$

$$\left( \frac{1}{4}(1)^4 - (1)^3 + (1)^2 \right) - \left( \frac{1}{4}(0)^4 - (0)^3 + (0)^2 \right)$$

$$= \frac{1}{4} \text{ square unit}$$

$$\left( \frac{1}{4}(2)^4 - (2)^3 + (2)^2 \right) - \left( \frac{1}{4}(1)^4 - (1)^3 + (1)^2 \right)$$

$$\left| -\frac{1}{4} \right| = \frac{1}{4} \text{ square unit}$$

$$\text{Area} = \frac{1}{4} + \frac{1}{4}$$

$$= \frac{1}{2} \text{ square units}$$



$$2. \int \frac{x^2}{(x^3+1)^2} dx$$

$$\text{let } u = x^3 + 1$$

$$\frac{du}{dx} = 3x^2$$

$$dx = \frac{du}{3x^2}$$

$$= \int \frac{x^2}{u^2} \cdot \frac{du}{3x^2}$$

$$\frac{1}{3} \int \frac{1}{u^2} du$$

$$\frac{1}{3} \int u^{-2} du$$

$$= -\frac{1}{3u} + C$$

$$= -\frac{1}{3(x^3+1)} + C$$