

R.Y.R

Alice Li

Tue Jul 04 11:31:40 2017

```
rm(list=ls())

#a)
#RY
RY<-read.csv("RY.csv")
x_array <- rep(0,nrow(RY)-1)

for (i in 1:nrow(RY)-1){
  x_array[i] = -100*log(RY$Adj.Close[i+1]/RY$Adj.Close[i])
}

blocksize <- 26
blocks <- floor(length(x_array)/blocksize)

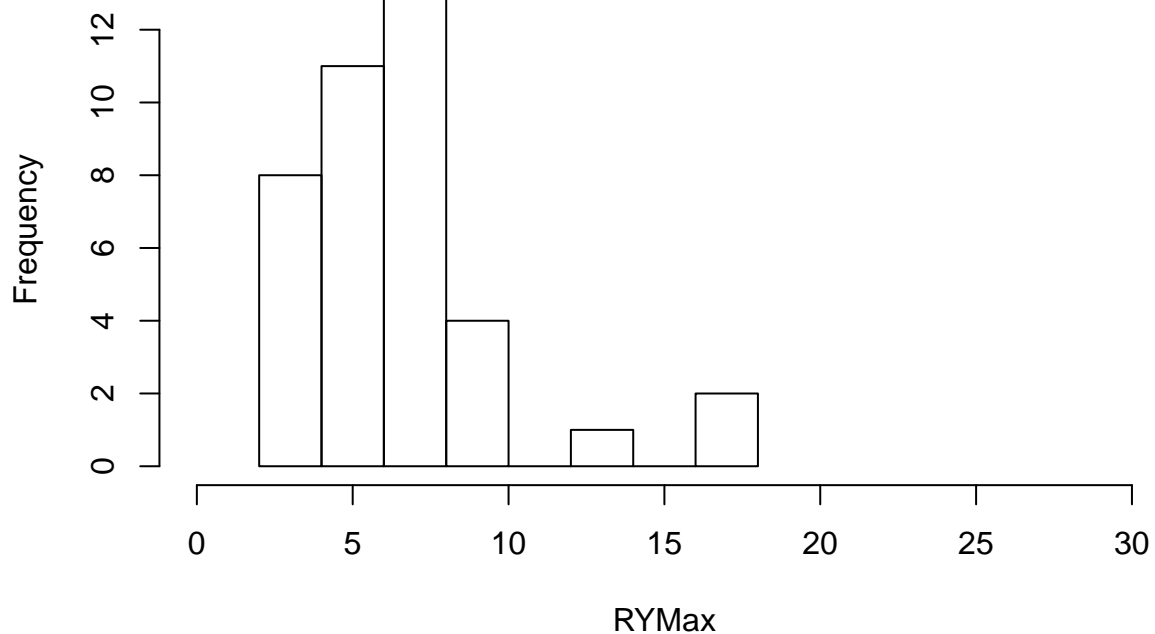
max_array <- rep(0,blocks)

for (i in 1:blocks){
  start_ind <- (i - 1)*26
  end_ind <- start_ind + 25
  max_array[i] = max(x_array[start_ind:end_ind])
}

hist(max_array,
     main="Histogram of RYMax",
     xlab="RYMax",
     xlim=c(0,30)
)

#b)
library(qrmdata) # for the S&P 500 data
```

Histogram of RYMax



```
library(xts) # for functions around time series objects
```

```
## Loading required package: zoo
```

```
##
```

```
## Attaching package: 'zoo'
```

```
## The following objects are masked from 'package:base':
```

```
##
```

```
##      as.Date, as.Date.numeric
```

```
library(QRM) # for fit.GEV() and fit.GPD()
```

```
## Loading required package: gsl
```

```
## Loading required package: Matrix
```

```
## Loading required package: mvtnorm
```

```
## Loading required package: numDeriv
```

```
## Loading required package: timeSeries
```

```
## Loading required package: timeDate
```

```
##
```

```
## Attaching package: 'timeSeries'
```

```
## The following object is masked from 'package:zoo':
```

```
##
```

```
##      time<-
```

```

##
## Attaching package: 'QRM'

## The following object is masked from 'package:base':
##
##      lbeta
library(qrmtools) # for returns() <- be RYre to load "qrmtools" last

##
## Attaching package: 'qrmtools'

## The following objects are masked from 'package:QRM':
##
##      dGEV, dGPD, pGEV, pGPD, qGEV, qGPD, rGEV, rGPD

## The following object is masked from 'package:timeSeries':
##
##      returns

fit.week <- fit.GEV(max_array)
(xi.week <- fit.week$par.ests[["xi"]])

## [1] 0.1122853
(mu.week <- fit.week$par.ests[["mu"]])

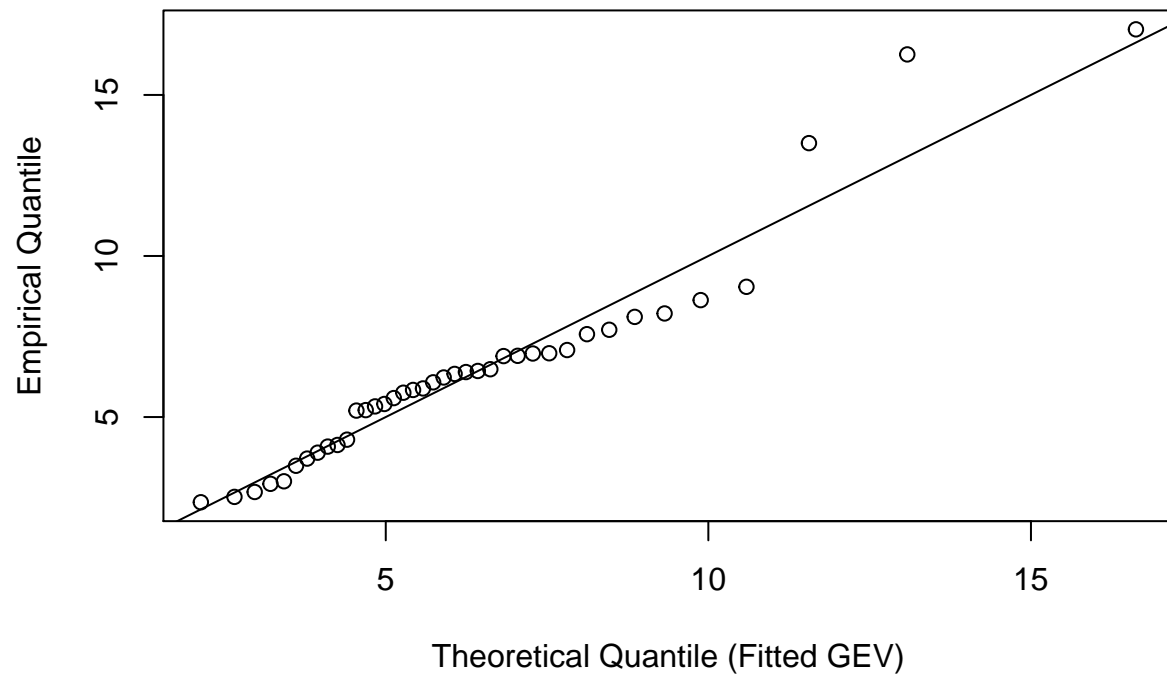
## [1] 4.956501
(sig.week <- fit.week$par.ests[["sigma"]])

## [1] 2.080714
fit.week

## $par.ests
##      xi      mu      sigma
## 0.1122853 4.9565007 2.0807136
##
## $par.ses
##      xi      mu      sigma
## 0.1212678 0.3763374 0.2836944
##
## $varcov
##      [,1]      [,2]      [,3]
## [1,] 0.014705867 -0.01487860 -0.005311442
## [2,] -0.014878596 0.14162988 0.052472686
## [3,] -0.005311442 0.05247269 0.080482486
##
## $converged
## [1] TRUE
##
## $llmax
## [1] -92.52517

#c)
q.week <- qGEV(ppoints(length(max_array)), xi.week, mu.week, sig.week) # contruct theoretical quantiles
qqplot(q.week, as.vector(max_array), xlab = "Theoretical Quantile (Fitted GEV)",
       ylab = "Empirical Quantile") # compare weekly maxima with theoretical quantiles
abline(0,1) # 45 degree line

```

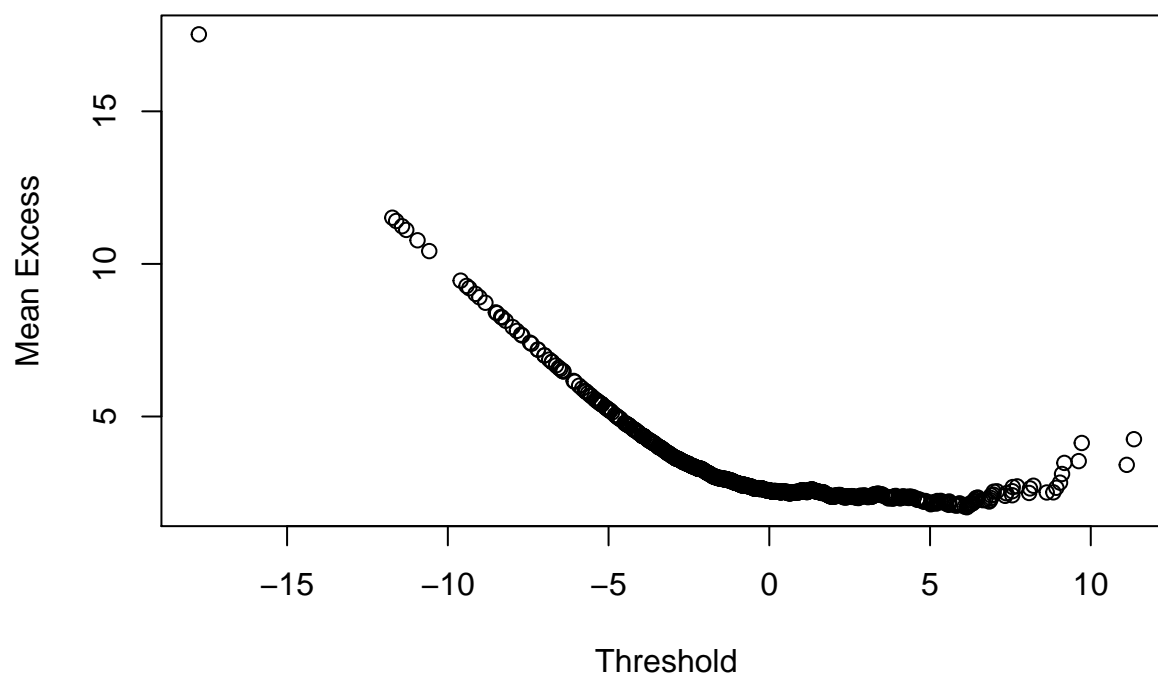


```
#d)
llmax1 <- fit.week$llmax
h.func<-function(M){1/sig.week*exp(-(M-mu.week)/sig.week - exp(-(M-mu.week)/sig.week))}
llmax0 <- sum(log(h.func(max_array)))
D<- 2*(llmax1 - llmax0)
1-pchisq(D,1)

## [1] 0.2536716

#e)
MEplot(x_array, main = "Sample Mean-Excess Plot")
```

Sample Mean-Excess Plot

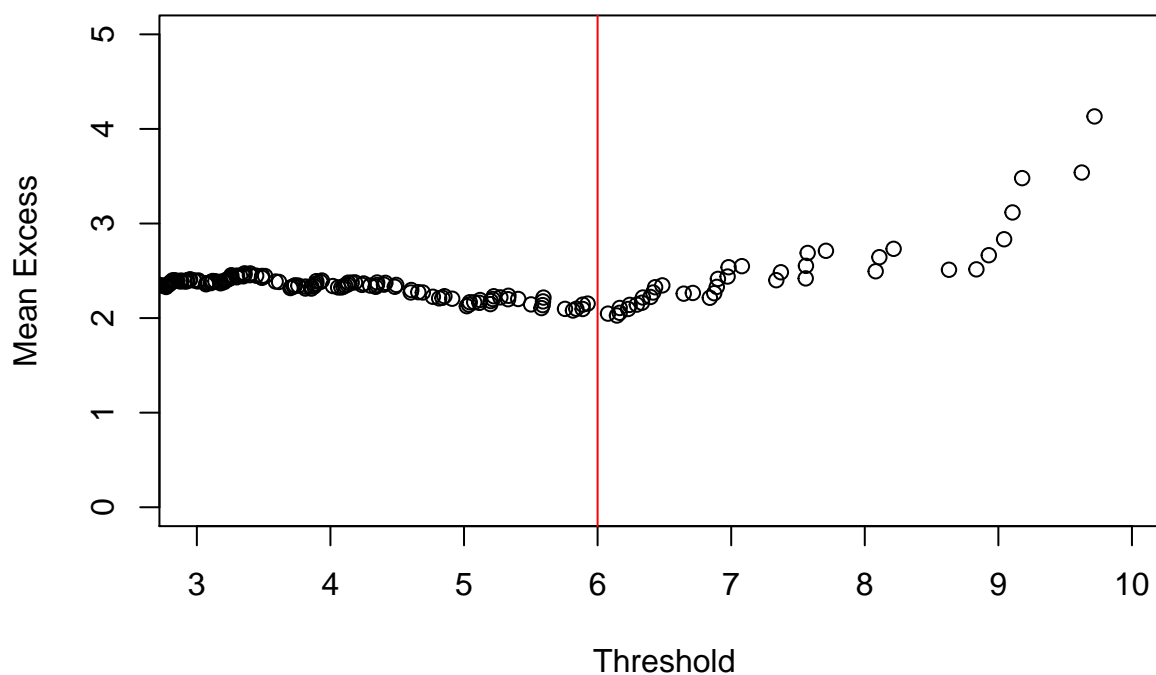


```
quantile(x_array,0.9)
```

```
##      90%  
## 3.880546
```

```
MEplot(x_array, main = "Sample Mean-Excess Plot", xlim = c(3,10), ylim = c(0,5)) #zoom in  
#pick d1 = 6  
d1 <- 6  
abline(v = d1, col = 2)
```

Sample Mean–Excess Plot



```
#f)
fitGPD <- fit.GPD(x_array, threshold = d1)

xi2 <- fitGPD$par.ests[["xi"]]
beta2 <- fitGPD$par.ests[["beta"]]
lmax1 <- fitGPD$ll.max

#g)
g.func<-function(X){1/beta2 * exp(-X/beta2)}
lmax0 <- sum(log(g.func(x_array[x_array>d1] - d1)))
lmax1

## [1] -75.49648

lmax0

## [1] -77.19716
D2<- 2*(lmax1 - lmax0)
1-pchisq(D2,1)

## [1] 0.06514294

#h)
Sxd <- length(x_array[x_array>d1])/length(x_array)
Q99<- d1 + beta2/xi2 * ((Sxd / (1 - 0.99))^xi2 - 1)
Q995<- d1 + beta2/xi2 * ((Sxd / (1 - 0.995))^xi2 - 1)
Q99
```

```

## [1] 8.854395
Q995

## [1] 10.51019
CTE99 <- (Q99 + beta2 - xi2*d1)/(1-xi2)
CTE995 <- (Q995 + beta2 - xi2*d1)/(1-xi2)
CTE99

## [1] 11.61486
CTE995

## [1] 13.66035
#empirical
Q99e <- quantile(x_array,0.99)
Q995e <- quantile(x_array,0.995)
Q99e

##      99%
## 8.912565
Q995e

##      99.5%
## 9.711564
CTE99e <-mean(x_array[x_array > Q99e])
CTE995e <- mean(x_array[x_array > Q995e])

CTE99e

## [1] 11.35086
CTE995e

## [1] 13.16329

```