

# Eigenfaces & PCA

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## Executive Summary

1. PCA
2. Intro to Facial Recognition
3. Eigenfaces
4. Results
5. Other Methods & Applications
6. Summary
7. Now it's your turn!



**1**

**PCA**



## PCA Review

### What is PCA?

- ◉ Dimensionality reduction tool
- ◉ Good for clustering & predictive analysis
- ◉ Invented by Karl Pearson in 1901
- ◉ Similar to Factor Analysis

### How does PCA work?

- ◉ Performed on a square symmetric matrix such as a covariance matrix
- ◉ Based on orthogonal projections
- ◉ Each subsequent principal component maximizes the proportion of remaining variance explained



## Connecting PCA and SVD

### The Connection:

- PCA is equivalent to finding eigenvalues of a covariance matrix
- $\text{Covariance}(A) = A^T A = \Sigma$
- SVD of  $A = U \Sigma V^T$
- Then  $U$  is an orthogonal matrix, known as the left singular values.
- $U$  will be our eigenfaces (coming soon!)
- We have now avoided the need to calculate the covariance matrix



**SVD MAKES PCA FASTER**

**(SOMETIMES)**



**2**

**Intro to Facial  
Recognition**



# Applications of Facial Recognition



## iPhone

The latest iPhone X, released in 2017, uses facial recognition “Face ID” that allows your face to be your password.



## Android

Android phones introduced the “Trusted Face” feature in 2014 with the release of Android Lollipop.



## Snapchat

Snapchat uses facial recognition to allow its users to have cool filters on their face (dog ears filter).



## Surveillance

Private intelligence agencies were using facial recognition in their surveillance as early as 1964.



## Instagram

Copying Snapchat, Instagram started using facial recognition to also allow their users to have cool filters on their face.



## Digital Cameras

Many digital cameras can recognize human faces that allow for clearer and better portrait photos.



“ This recognition problem is made difficult by the great variability in head rotation and tilt, lighting intensity and angle, facial expression, aging, etc.

— Woody Bledsoe, Father of Facial Recognition, 1966



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Eigenfaces



## Background Information

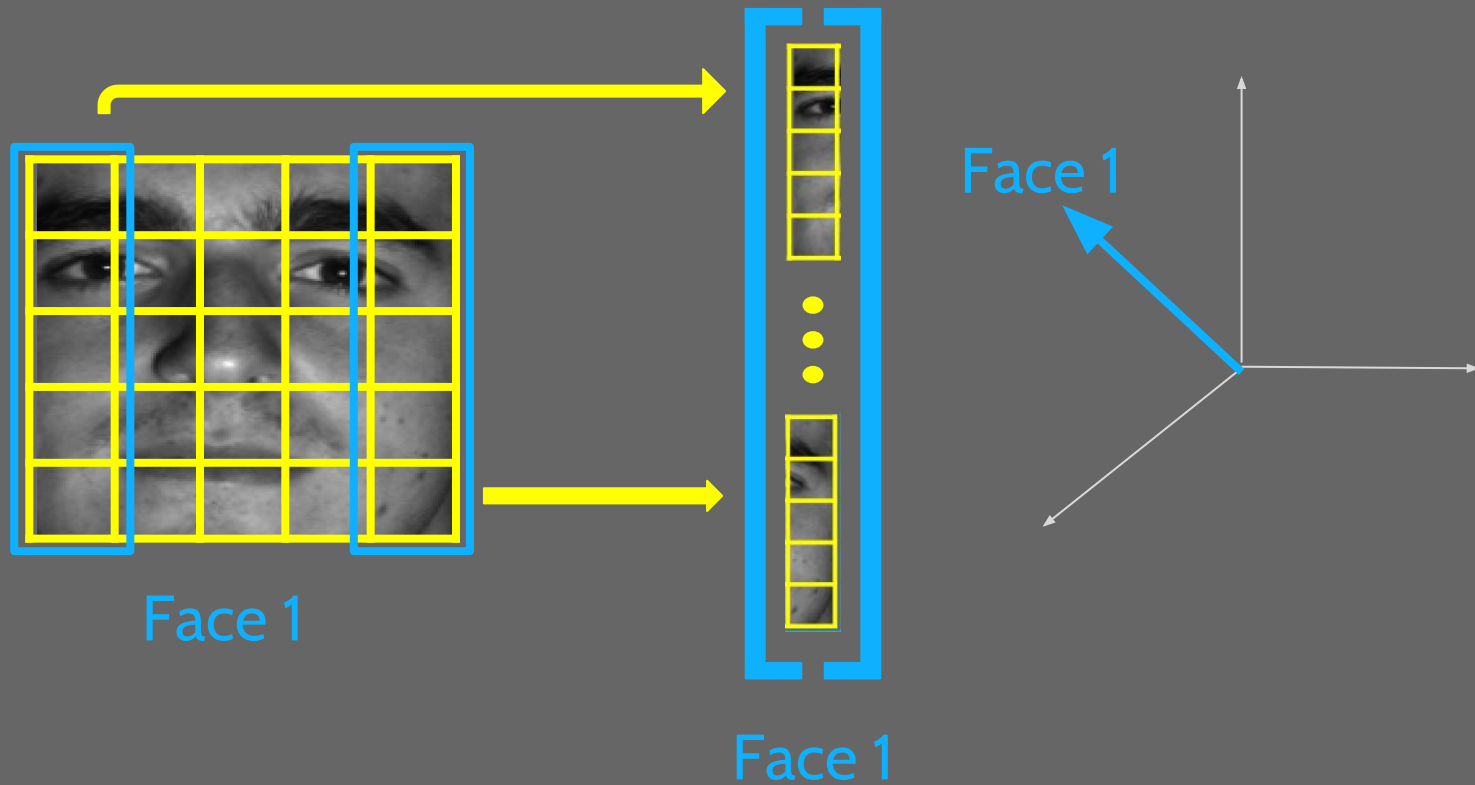
### We will work with Extended Yale Face Database B

- ⦿ 32x32 Data file
- ⦿ This contains faces and their labels
- ⦿ 38 individuals
- ⦿ 9 poses
- ⦿ 64 different illuminations per individual.
- ⦿ The eigenfaces are the PCs of this database

<http://vision.ucsd.edu/~leekc/ExtYaleDatabase/ExtYaleB.html>



# Face Vectorization





# Eigenfaces

## What

Eigenfaces are eigenvectors used to help computers perform facial recognition. They are the principal components of a distribution of faces.

## Why

There is a need for low dimensional representation for faces and Eigenfaces do this along with decrease computation time so we get results within a second or two

## How

The eigenfaces are the eigenvectors associated with the largest eigenvalues of the covariance matrix of the training data. The eigenvectors correspond to the least-squares solution.

$$\text{Any Face in Training Set (vector)} = \text{Eigenface 0 (vector)} + C_1 \text{Eigenface 1 (vector)} + C_2 \text{Eigenface 2 (vector)} + \dots$$

Any Face in Training Set  
(vector)

Eigenface 0  
(vector)

Eigenface 1  
(vector)

Eigenface 2  
(vector)

Where  $C_1, C_2, \dots, C_n$  are constants



## Steps to find the Eigenfaces

**Step 1:** Prepare a training set of face images.

**Step 2:** Normalize and grayscale the image, while also centering the data.

**Step 3:** Define the covariance matrix.

**Step 4:** calculating the eigenvectors and eigenvalues of the covariance matrix.

**Step 5:** Perform PCA; Choose the principal components. Sort the eigenvalues in descending order and arrange eigenvectors accordingly.

**Step 6:** We obtain then obtain a matrix that contains the eigenfaces.



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**Results**





## Our process

Capture Image

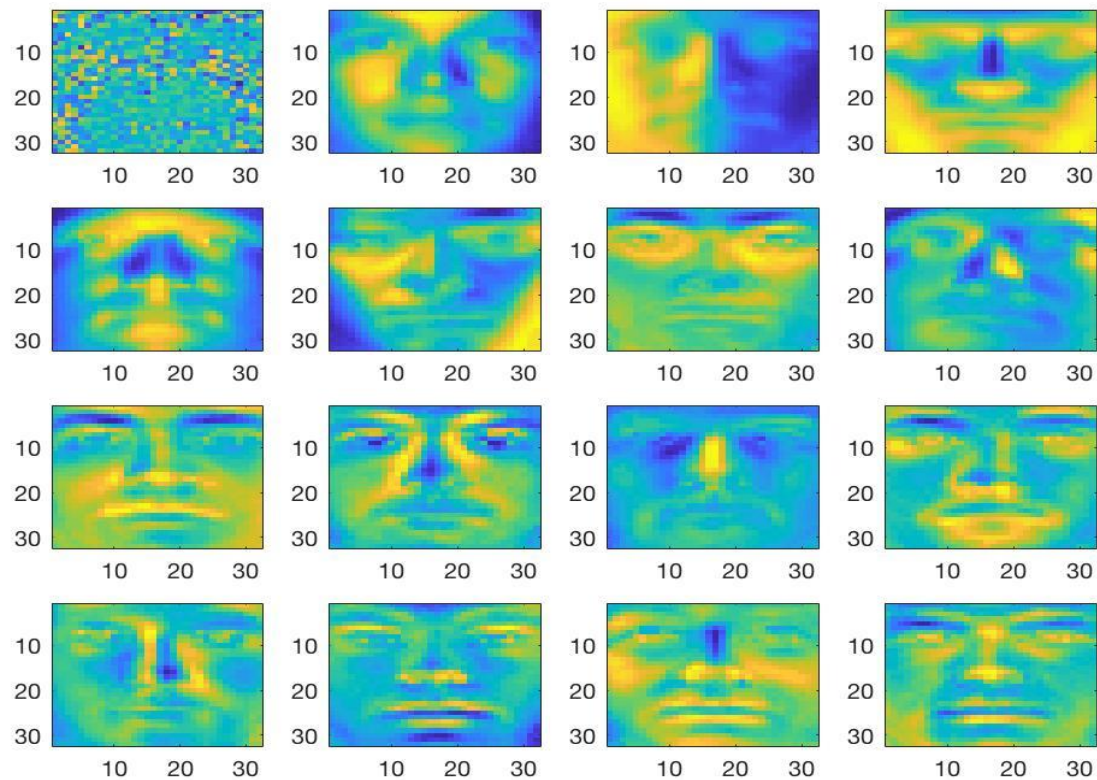
Greyscale,  
Align, and  
Crop  
Image

Run  
MATLAB  
code

Output  
closest  
face in  
database

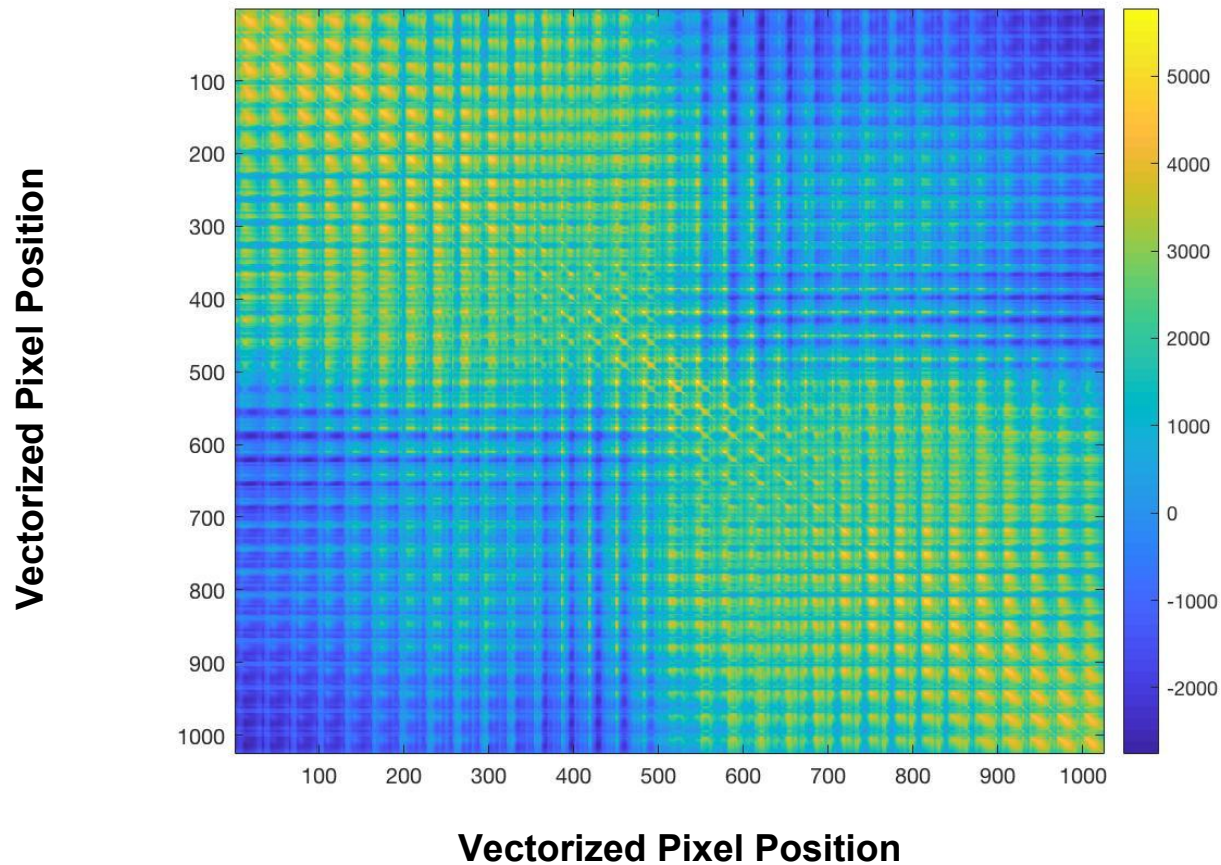
## Top 15 Eigenfaces

Y Pixel Coordinate



X Pixel Coordinate

**Covariance Matrix for Extended Yale Database B**



# 1.33 Seconds

for computing eigenfaces with a  
covariance matrix

# 1.86 Seconds

for computing eigenfaces with  
singular value decomposition

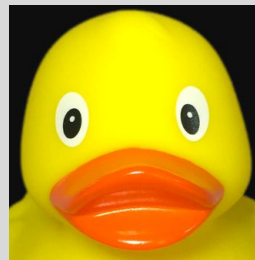
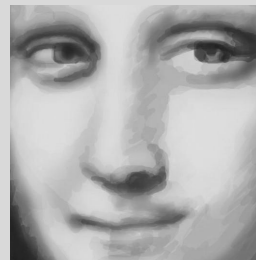
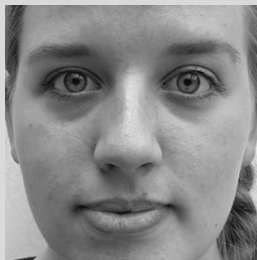
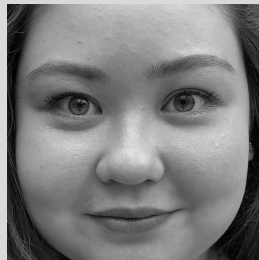


## Error Calculation

- ◉ We can define weights
- ◉  $\mathbf{M}$  is the mean vector
- ◉ Let  $\mathbf{C}$  be the vector of weights that represent a face image as a linear combination of eigenfaces.
- ◉  $\mathbf{C} = \text{transpose}(\mathbf{V})(\mathbf{U} - \mathbf{M})$
- ◉ The distance (error) between two faces is the euclidean norm of the difference between the two weight vectors.



## Guess Who?



Error: 1364



Error: 1041



Error: 809



Error: 1101

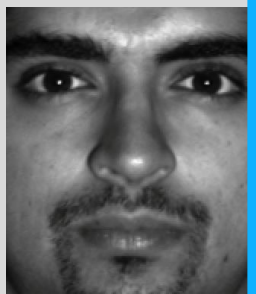
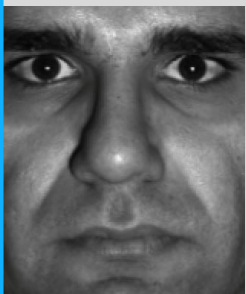
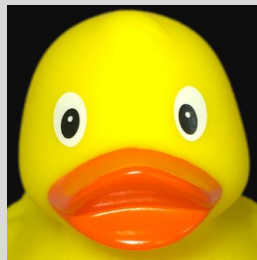
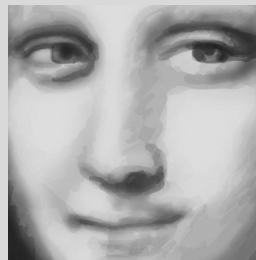
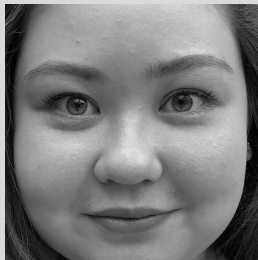


Error: 1874



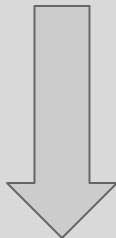
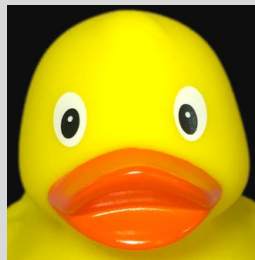
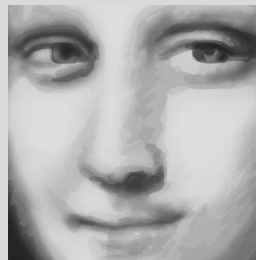
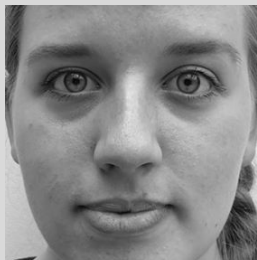
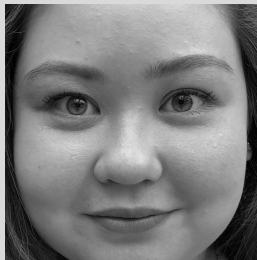


Guess Who?





Guess Who?







## Limitations

- ⦿ Faces must be very well centered and adjusted for accurate results
- ⦿ Small training set
- ⦿ Need more data to set error bounds  $e_1$ , and  $e_2$
- ⦿ Not much racial diversity in the training set

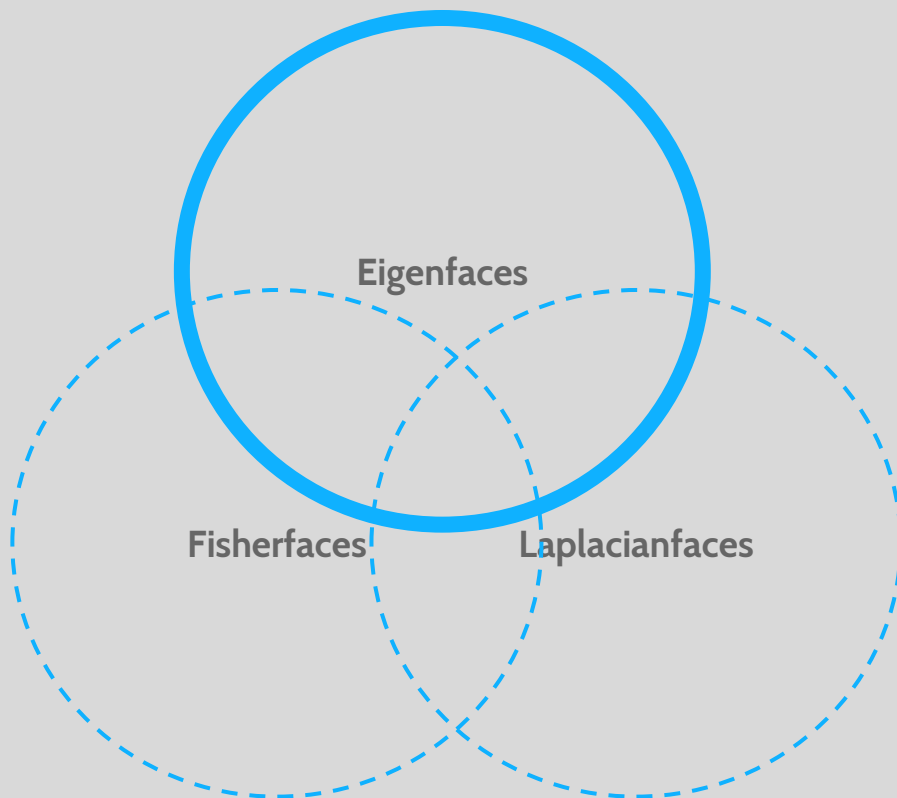


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**Other Methods  
& Applications**



# Methods for Facial Recognition





**Eigenface**  
**Fisherface**  
**Laplacianfaces**

## Fisherface

- ◉ Fisherface uses Linear Discriminant Analysis (LDA).
- ◉ Used when the goal is classification rather than representation.
- ◉ To compute these, we assume the data in each class is Normally distributed with a mean and covariance matrix and probability density function

## Laplacianfaces

- ◉ Laplacian faces are an appearance-based approach to human face representation and recognition.
- ◉ Uses Locality Preserving Projection (LPP) which seeks to capture the details in the geometry of the data as well as the local structure
- ◉ Truncates the unnecessary information



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Summary



## Final Summary

- ⦿ Facial Recognition has many applications
- ⦿ Eigenfaces form a basis for a set of faces
- ⦿ Eigenface algorithm can find closest face
- ⦿ Eigenfaces, Fisherfaces, and Laplacianfaces method all do facial recognition



<https://github.com/aliceroberts10/SciProgWorkshop-Eigenfaces>



## Bibliography

<https://en.wikipedia.org/wiki/Eigenface>  
<http://www.cad.zju.edu.cn/home/dengcai/Data/FaceData.html>  
[http://www.scholarpedia.org/article/Eigenfaces#Computing\\_the\\_Eigenfaces](http://www.scholarpedia.org/article/Eigenfaces#Computing_the_Eigenfaces)  
[http://www.scholarpedia.org/article/Fisherfaces#Computing\\_the\\_Fisherfaces](http://www.scholarpedia.org/article/Fisherfaces#Computing_the_Fisherfaces)  
[http://www.scholarpedia.org/article/Laplacianfaces#Locality\\_Preserving\\_Projection.28LPP.29](http://www.scholarpedia.org/article/Laplacianfaces#Locality_Preserving_Projection.28LPP.29)

## Images

<http://www.cad.zju.edu.cn/home/dengcai/Data/FaceData.html>  
<http://diylogodesigns.com/blog/apple-logo/>  
[https://commons.wikimedia.org/wiki/File:Android\\_robot.svg](https://commons.wikimedia.org/wiki/File:Android_robot.svg)  
<https://www.edigitalagency.com.au/instagram/new-instagram-logo-png/>  
<https://www.shareicon.net/snapchat-snapchat-logo-logo-ghost-886532>  
<https://github.com/blackducksoftware>  
<https://ducksinthewindow.com/yellow>  
<https://www.queeky.com/gallery/image/mona-lisa-close-up/>

## Slide Template

<https://www.slidescarnival.com/>





**Eigenface**  
**Fisherface**  
**Laplacianfaces**

## Laplacianfaces

- ⦿ Laplacian faces are an appearance-based approach to human face representation and recognition.
- ⦿ Uses Locality Preserving Projection (LPP) which seeks to capture the details in the geometry of the data as well as the local structure
- ⦿ Extract the low-dimensional manifold structure.
- ⦿ Truncates the unnecessary information



Eigenface  
Fisherface  
Laplacianfaces

## Fisherface

- ⦿ Fisherface uses Linear Discriminant Analysis (LDA).
- ⦿ Used when the goal is classification rather than representation.
- ⦿ To compute these, we assume the data in each class is Normally distributed with a mean and covariance matrix and probability density function
- ⦿ Problem with fisherfaces is we need to compute the inverse of the within-class scatter matrix. If the sample feature vectors are defined in a  $p$ -dimensional space and  $p \gg n$  then  $S$  is singular and problems arise.
- ⦿ Generalization with large training sample sets