

Министерство науки и высшего образования Российской Федерации Федеральное государственное бюджетное образовательное учреждение высшего образования

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(национальный исследовательский университет)» (МГТУ им. Н.Э. Баумана)

ФАКУЛЬТЕТ «Информатика и системы управления»
КАФЕДРА «Программное обеспечение ЭВМ и информационные технологии»

Лабораторная работа № 1

По предмету: «Математическая статистика»

Тема: Гистограмма и эмпирическая функция распределения

Вариант 25

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Группа: ИУ7-65Б

Цель и содержание работы

Цель работы: построение гистограммы и эмпирической функции распределения.

Содержание работы:

- 1. Для выборки объема n из генеральной совокупности X реализовать в виде программы на ЭВМ
 - а. вычисление максимального значения M_{max} и минимального значения M_{min} ;
 - b. размаха R выборки;
 - с. вычисление μ и S^2 математического ожидания MX и дисперсии DX;
 - d. группировку значений выборки в $m = [\log_2 n] + 2$ интервала;
 - е. построение на одной координатной плоскости гистограммы и графика функции плотности распределения вероятностей нормальной случайной величины с математическим ожиданием μ и дисперсией S^2 ;
 - f. построение на другой коордитной плоскости графика эмпирической функции распределения и функции распределения нормальной случайной величины с математическим ожиданием μ и дисперсией S^2 ;
- 2. Провести вычисления и построить графики для выборки из индивидуального варианта.

Формулы для вычисления величин

Минимальное значение выборки:

 $M_{min}=\min\{x_1,\ldots,x_n\}$, где (x_1,\ldots,x_n) – реализация случайной выборки.

Максимальное значение выборки:

 $M_{max} = \max\{x_1, ..., x_n\}$, где $(x_1, ..., x_n)$ – реализация случайной выборки.

Размах выборки:

$$R = M_{max} - M_{min}$$

Несмещенная оценка математического ожидания:

$$\hat{\mu}(\overrightarrow{X_n}) = \overline{X} - \frac{1}{n} \sum_{i=1}^n X_i$$

Несмещенная оценка дисперсии:

$$S^{2}(\overrightarrow{X_{n}}) = \frac{1}{n-1} \sum_{i=1}^{n} (X_{i} - \overline{X})^{2}$$

Эмпирическая плотность и гистограмма

Oпределение. Эмпирической плотностью распределения случайной выборки $\overrightarrow{X_n}$ называют функцию $f_n(x) = egin{cases} n_i, & x \in J_i, i = 1, ..., m \\ 0, & \text{иначе} \end{cases}$, где n – количество элементов в выборке.

$$m = \lceil \log_2 n \rceil + 2,$$

$$x_{(1)} = \min \{x_1, ..., x_n\}$$

$$x_{(n)} = \max\{x_1, ..., x_n\}$$

 J_i , i=1,...,m — полуинтервал из $J=[x_{(1)},x_{(n)}]$

$$\Delta = \frac{x_{(n)} - x_{(1)}}{m} = \frac{|J|}{m}$$

$$J_i = [x_{(1)} + (i-1)\Delta, x_{(1)} + i\Delta], i = 1, ..., m-1$$

 n_i — количество элементов выборки в полуинтервале J_i , $i=1,\ldots,m$.

Oпределение. График функции $f_n(x)$ называют гистограммой.

Пусть

- 1. $\overrightarrow{X_n} = (X_1, ..., X_n)$ случайная выборка, 2. $\overrightarrow{x_n} = (x_1, ..., x_n)$ реализация случайной выборки, 3. $n(x, \overrightarrow{x_n})$ количество элементов выборки $\overrightarrow{x_n}$, которые имеют значения меньше x.

Определение. Эмпирической функцией распределения называют функцию

$$F_n$$
: $R \to R$, определенную условием $F_n(x) = \frac{n(x, \overrightarrow{x_n})}{n}$.

Листинг

Листинг 1. Программа на Matlab к лабораторной работе №1

```
function lab1
                                          clear
                                          X = [-17.04, -18.29, -17.38, -18.11, -18.96, -17.65, -17.02, -17.22, -16.25, -17.44, -17.69, -17.69, -17.04, -18.29, -17.38, -18.11, -18.96, -17.65, -17.02, -17.22, -16.25, -17.44, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69, -17.69,
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17.56];
                                            % Пункт а)
                                          Mmax = max(X);
                                          Mmin = min(X);
                                            % Пункт б)
                                          R = Mmax - Mmin;
                                          % Пункт в)
                                          mu = find mu(X);
                                          S2 = find S2(X);
                                          % Пункт г)
                                            % Гистограмма
                                          m = find m(X);
                                            [J, count] = intervalization(X, m);
                                            stairs([J(1) J], [0 count 0]);
                                            % График 1
                                          hold on;
                                          Y1 = f(X, mu, S2);
                                          plot(X, Y1, '.');
                                          legend('Гистограмма', 'Функция плотности распределения нормальной СВ');
                                          hold off;
                                             % График 2
                                            figure;
                                          empF(sort(X));
                                          hold on;
                                          F(sort(X), mu, getS(X), m, R);
                                          legend('Эмпирическая функция распределения', 'Функция распределения нормальной СВ');
                                          hold off;
                                            function [mu] = find mu(X)
                                                                                    mu = sum(X)/size(X,2);
                                            end
                                             function [S2] = find S2(X)
                                                                                     S2 = sum((X - find mu(X)) .* (X - find mu(X))) / (size(X,2) - 1);
                                            end
                                             function sigma = getSigmaSgr(X)
                                                                                        tempMu = find mu(X);
                                                                                        sigma = sum((X - tempMu) .* (X - tempMu)) / size(X,2);
```

```
end
    function Ssqr = getS(X)
       n = size(X, 2);
        Ssqr = n/(n - 1) * getSigmaSqr(X);
    end
    function [m] = find m(X)
        m = floor(log2(size(X, 2))) + 2;
    end
    function [J, count] = intervalization(X, m)
        sortX = sort(X);
        n = size(sortX, 2);
        delta = (sortX(end) - sortX(1)) / m;
        J = sortX(1):delta:sortX(end);
        count = zeros(1, m);
        for i = 1: (size(J, 2) - 1)
            for j = 1:n
                if (sortX(j) >= J(i) \&\& sortX(j) < J(i+1))
                    count(i) = count(i) + 1;
                end
            end
        end
        count(end) = count(end) + sum(sortX==(sortX(end)));
        for i = 1:size(count,2)
           count(i) = count(i)/(n * delta);
        end
    end
    function [Y] = f(X, MX, DX)
        Y = normpdf(X, MX, sqrt(DX));
    end
    function empF(X)
        [yy, xx] = ecdf(X);
        stairs(xx, yy);
    end
    function F(X, MX, DX, m, R)
        delta = R/m;
        Xn = min(X):delta/20:max(X);
        Y = 1/2 * (1 + erf((Xn - MX) / sqrt(2*DX)));
        plot(Xn, Y, '--');
    end
end
```

Результат работы программы

$$M_{max} = -15.27$$

$$M_{min} = -19.47$$

$$R = 4.2$$

$$\hat{\mu} = -17.5894$$

$$S^2 = 0.7286$$

Таблица 1. Интервальная группировка значений выборки при т = 8

[-19.470, -18.945)	[-18.945, -18.419)		[-17.895, -17.369)		-	[-16.320, -15.795)	/
7	12	23	37	18	12	9	2

Графики

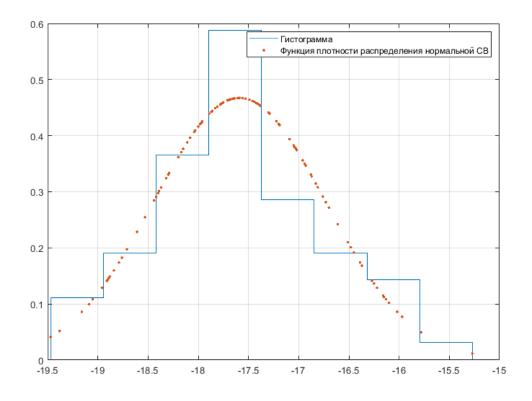


Рисунок 1. Гистограмма и график функции плотности распределения нормальной случайной

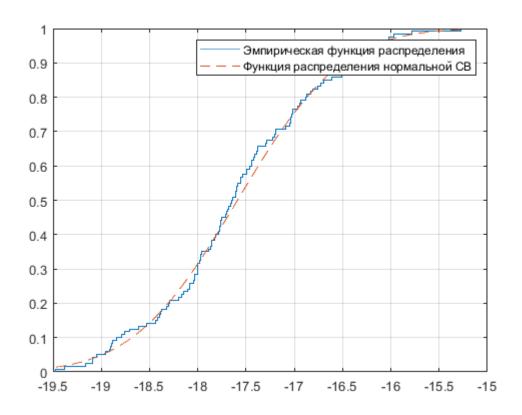


Рисунок 2. График эмпирической функции распределения и функции распределения нормального распределения