Q 1. (40%)

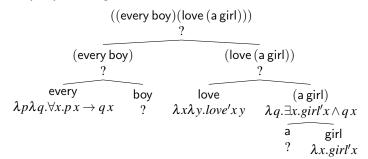
In the following, you are required to give the lambda term that needs to replace? so that the reduction results as given. Note that the given expressions are meant to be lambda terms rather than syntactic objects.

- (a) ? a b = b a
- (b) ?abc = acb
- (c) ?abc = a(cb)
- (d) $?ab = \lambda x.ax(bx)$
- (e) $?(\lambda x.ax)c = ac$
- (f) $?(\lambda x.ax)c = \lambda y.a(yc)$
- (g) $?(\lambda x.sleeps'x) = sleeps'john'$
- (h) ? sleeps' = sleeps' john'

Q 2. (60%)

Complete the missing entries in the following trees:

(a) Every boy loves a girl.



(b) Every boy walks or talks.

$$((\mathsf{every}\,\mathsf{boy})(\mathsf{walk}\,(\mathsf{or}\,\mathsf{talk})))\\ \forall x. boy' x \to walk' x \lor talk' x\\ (\mathsf{every}\,\mathsf{boy}) \qquad (\mathsf{walk}\,(\mathsf{or}\,\mathsf{talk}))\\ ? \qquad ?\\ \mathsf{every} \qquad \mathsf{boy} \qquad \mathsf{walk} \qquad (\mathsf{or}\,\mathsf{talk})\\ \lambda p \lambda q. \forall x. p \, x \to q \, x \qquad ? \qquad ? \qquad ?\\ \mathsf{or} \qquad \mathsf{talk}\\ ? \qquad ?$$