

**Q1.**

Write the meaning of these sentences in first order logic. You may ignore temporal and aspectual semantics for the moment.

- (1) a. Every student who is tired is happy.  
b. Every tired student is happy.  
c. Every successful student is tired.  
d. John ate only two apples. (Hint: you can use the two place predicate *notid*, meaning ‘not identical’ or ‘not the same individual as’.)

**Solution:**

- a.  $\forall x. student'x \wedge tired'x \rightarrow happy'x$   
b.  $\forall x. student'x \wedge tired'x \rightarrow happy'x$   
c.  $\forall x. succ' student'x \rightarrow tired'x$   
    *succ'* is a function that maps a property to another property. It's internal semantics is hard to define, but for now we make sure that it is not an intersective adjective like tired.  
d.  $\exists x \exists y. apple'x \wedge apple'y \wedge ate'xjohn' \wedge ate'yjohn' \wedge notid'xy \wedge \forall z. apple'z \wedge ate'zjohn' \rightarrow id'zy \vee id'zx$

**Q2.**

Let the operator  $\circ$  be left associative. (For associativity you can consult the lambda calculus notes Section 3, item B, or the Wikipedia article on ‘operator associativity’.

Eliminate all the eliminable parenthesis in the following:

- (2) a.  $((a \circ b) \circ c)$   
b.  $(a \circ (b \circ (c \circ d)))$   
c.  $(a \circ ((b \circ c) \circ d))$

**Solution:**

- a.  $a \circ b \circ c$   
b.  $a \circ (b \circ (c \circ d))$   
c.  $a \circ (b \circ c \circ d)$

Restore the following to fully parenthesized form.

- (3) a.  $a \circ b \circ c \circ d$   
b.  $a \circ b \circ (c \circ d)$   
c.  $a \circ (b \circ c) \circ d$

**Solution:**

- a.  $((((a \circ b) \circ c) \circ d))$

b.  $((a \circ b) \circ (c \circ d))$

c.  $((a \circ (b \circ c)) \circ d)$