The Azinaa Code Notebook

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0.1 Graph

0.1.1 BFS

```
1 #include <bits/stdc++.h>
2 using namespace std;
3 const int SIZE = 100; //Vertex size
4 int main(){
     int source = 0;
     vector < int > Graph[SIZE];
     bool visited[SIZE];
     int distance[SIZE];
     fill(visited, visited+SIZE, 0);
10
     fill(distance, distance+SIZE, INT_MAX);
11
     queue < int > q;
12
     q.push(source);
     visited[source] = true;
13
     distance[source] = 0;
14
15
     while(!q.empty()){
       int u = q.front();
16
17
       q.pop();
       for(int i = 0 ; i < Graph[u].size(); i++){</pre>
18
         if(visited[Graph[u][i]]){
19
20
            continue;
21
         }
22
         visited[Graph[u][i]] = true;
         distance[Graph[u][i]] = distance[u] + 1;
23
24
         q.push(Graph[u][i]);
      }
25
26
     }
27
     return 0;
28 }
```

0.1.2 Topological-Sorting

```
1 #include <bits/stdc++.h>
2 using namespace std;
3 const int SIZE = 100; //Graph Size Vertex
4 int visited[SIZE];
5 vector <int> Graph[SIZE];
6 stack<int> ans;
7 int topolSort(int u)
8 {
     if(visited[u] == 1)
10
     {
```

```
11
       return -1; //cycle
12
13
     if(visited[u] == 2)
14
15
       return 0;
16
17
     visited[u] = 1:
     for(int i = 0 ; i < Graph[u].size() ; i++)</pre>
18
19
20
       topolSort(Graph[u][i]);
21
22
       visited[u] = 2:
23
     ans.push(u);
24
     return 0;
25 }
26
27 int main(){
     return 0;
29 }
   0.1.3 DAG Shortest Path
1 #include <iostream >
2 #include <vector>
3 using namespace std;
4
  const int Gsize=100000;
6
7 int _color[Gsize], _p[Gsize] ,_d[Gsize] ,_f[Gsize] , _time;
8 vector <int > _V;
9 void DFS_visit(vector<int> G[] ,int u)
10 {
11 _time++;
     _d[u]=_time;
13
   _color[u]=1;
14
   int v;
     for(int i=0;i<G[u].size();i++)</pre>
15
16
    {
17
       v=G[u][i];
18
       if(!_color[v])
19
       ₹
20
         _p[v]=u;
21
         DFS_visit(G ,v);
22
       }
23
     }
```

```
_color[u]=2;
                                                                   67
                                                                           int u=arr[i];
25
     _time++;
                                                                          for(int j=0; j < G[u].size(); j++)
                                                                   68
     _f[u]=_time;
                                                                             _Relax(u, G[u][j], W[u][j]);
                                                                   69
     _V.push_back(u);
                                                                       }
27
                                                                   70
28 }
                                                                   71 }
29 void DFS(vector<int>G[])
                                                                   72
30 {
                                                                   73 int main()
31
     for(int i=0;i<Gsize;i++)</pre>
                                                                   74 {
32
                                                                   75
33
       _color[i]=0; _p[i]=0;
                                                                   76
                                                                         return 0;
     }
                                                                   77 }
34
35
     _{time=0};
                                                                      0.1.4 Bellman-Ford
36
     for(int i=0;i<Gsize;i++)</pre>
37
       if(!_color[i])
                                                                    1 // A C++ program for Bellman-Ford's single source
38
         DFS_visit(G ,i);
                                                                    2 #include <bits/stdc++.h>
39 }
                                                                    3
40
                                                                    4 struct Edge
   void Topologival_sort(vector<int> G[], int arr[])
                                                                    5 {
42 {
                                                                    6
                                                                           int src, dest, weight;
43
     _V.clear();
                                                                    7 };
     DFS(G);
44
                                                                    8
     for(int i=0;i<_V.size();i++)
45
                                                                    9 struct Graph
46
       arr[_V.size()-1-i] = _V[i];
                                                                   10 f
47 }
                                                                   11
                                                                           int V, E; //Size Of Graph
48
                                                                   12
                                                                           struct Edge* edge;
49 void _Relax(int u, int v, int w)
                                                                   13 };
50 {
                                                                   14
     if(_d[v]>(_d[u]+w))
51
                                                                   15 struct Graph* createGraph(int V, int E)
52
                                                                   16 {
       _d[v] = _d[u] + w;
53
                                                                   17
                                                                           struct Graph* graph = new Graph;
       _p[v] = u;
54
                                                                   18
                                                                           graph -> V = V;
55
     }
                                                                   19
                                                                           graph -> E = E;
56 }
                                                                   20
                                                                           graph->edge = new Edge[E];
57
                                                                           return graph;
   void DAG_shortest_paths(vector<int> G[], vector<int> W[],
                                                                      }
       s)
                                                                   23
59 {
                                                                   24 void BellmanFord(struct Graph* graph, int src, int* dist)
60
     int arr[Gsize];
                                                                   25 {
     Topologival_sort(G, arr);
                                                                   26
                                                                           int V = graph -> V;
     for(int i=0;i<Gsize;i++)</pre>
                                                                   27
                                                                           int E = graph -> E;
63
      _d[i]=500000000;
                                                                   28
     _d[s] = 0;
                                                                   29
                                                                           for (int i = 0; i < V; i++)
     for(int i=0;i<Gsize;i++)
                                                                   30
                                                                               dist[i]
                                                                                         = INT_MAX;
     {
66
                                                                           dist[src] = 0;
                                                                   31
```

```
32
                                                                   2 using namespace std;
33
                                                                   3 #define endl '\n'
       for (int i = 1; i \le V-1; i++)
34
                                                                   4 #define pii pair <int, int>
35
                                                                   5 #define F first
            for (int j = 0; j < E; j++)
36
                                                                   6 #define S second
37
                int u = graph->edge[j].src;
                                                                   7 #define mp make_pair
                int v = graph->edge[j].dest;
38
                                                                   8 #define pb emplace_back
                int weight = graph->edge[j].weight;
39
40
                if (dist[u] != INT_MAX && dist[u] + weight < dish bool vis[100001];
                   \lceil \mathbf{v} \rceil
                                                                   11 int dis[100001];
                    dist[v] = dist[u] + weight;
                                                                   12 vector <pii> a [100001];
41
42
           }
                                                                   13
       }
43
                                                                   14 class prioritize {
44
                                                                   15 public: bool operator ()(pii &p1 , pii &p2) {
45
                                                                          return p1.S > p2.S;
       for (int i = 0; i < E; i++)
                                                                   16
46
                                                                   17
                                                                      }
47
                                                                   18 };
           int u = graph->edge[i].src;
           int v = graph->edge[i].dest;
48
                                                                   19
49
           int weight = graph->edge[i].weight;
                                                                   20 int Dijkstra(int s, int n) {
                                                                        for (int i = 0; i \le n; i++) {
50
           if (dist[u] != INT_MAX && dist[u] + weight < dist[v]21
                printf("Graph_contains_negative_weight_cycle"); 22
                                                                          vis[i] = false;
51
                   Hint!
                                                                          dis[i] = INT_MAX;
       }
                                                                        }
52
                                                                   24
53
                                                                   25
                                                                        priority_queue < pii, vector < pii >, prioritize > pq;
54
       //printArr(dist, V);//Finishing Algo
                                                                   26
                                                                        pq.push(mp(s, dis[s] = 0));
55
                                                                   27
                                                                        while (!pq.empty()) {
56
                                                                   28
                                                                          pii cur = pq.top(); pq.pop();
       return;
                                                                          int cv = cur.F, cw = cur.S;
57 }
                                                                   29
58
                                                                   30
                                                                          if (vis[cv]) continue;
59 int main()
                                                                   31
                                                                          vis[cv] = true;
60 {
                                                                   32
                                                                          for (pii x : a[cv]) {
                                                                            if (!vis[x.F] && (cw + x.S) < dis[x.F]) {
61
       int V = 5; // Number of vertices in graph
                                                                   33
62
       int E = 8; // Number of edges in graph
                                                                   34
                                                                               pq.push(mp(x.F, dis[x.F] = cw + x.S));
63
       struct Graph* graph = createGraph(V, E);
                                                                   35
64
       graph -> edge [0] . src = 0;
                                                                   36
                                                                          }
65
       graph -> edge [0] . dest = 1;
                                                                   37
                                                                        }
                                                                   38 }
66
       graph -> edge [0] . weight = -1;
67
       int dist[5];
                                                                   39
68
       BellmanFord(graph, 0, dist);
                                                                   40 int main() {
69
       return 0;
                                                                   41
                                                                        int tc;
70 }
                                                                   42
                                                                        cin >> tc;
                                                                   43
                                                                        while (tc--) {
   0.1.5 Djkstra
                                                                   44
                                                                          int v1, v2, w, n, m;
                                                                   45
                                                                          cin >> n >> m;
1 #include <bits/stdc++.h>
```

```
for (int i = 0; i \le n; i++) {
                                                                  23
                                                                         }
46
                                                                          // All distances -> dist
47
         a[i].clear();
                                                                  24
48
                                                                  25 }
                                                                  26
49
       for (int i = 0; i < m; i++) {
50
         cin >> v1 >> v2 >> w;
                                                                  27 int main()
                                                                  28 {
51
         a[v1].pb(mp(v2, w));
52
       }
                                                                  29
                                                                          /* example Graph:
53
       int s;
                                                                  30
                                                                                  10
                                                                  31
                                                                             (0) ----> (3)
54
       cin >> s;
                                                                  32
55
       Dijkstra(s, n);
                                                                                        //\
       for (int i = 1; i \le n; i++) {
                                                                  33
56
57
         if (dis[i] != INT_MAX) {
                                                                  34
                                                                                          / 1
58
           cout << dis[i] << "";
                                                                  35
                                                                             11/
         } else {
                                                                  36
                                                                             (1) ---->(2)
59
                                                                                  3
60
                                                                  37
           cout << "-1,,";
61
         }
                                                                  38
                                                                          int graph[V][V] =
      }
62
                                                                  39
63
     }
                                                                  40
                                                                            \{0, 5, INF, 10\},\
64
     return 0;
                                                                  41
                                                                            {INF, 0,
                                                                                       3, INF},
65 }
                                                                  42
                                                                            {INF, INF, 0, 1},
                                                                            {INF, INF, INF, 0}
                                                                  43
   0.1.6 Floyd Warshall
                                                                         };
                                                                  44
                                                                  45
1 // C Program for Floyd Warshall Algorithm
                                                                  46
                                                                          // Print the solution
2 #include < stdio.h>
                                                                  47
                                                                          floydWarshall(graph);
3
                                                                  48
                                                                          return 0;
4 #define V 4
                                                                  49 }
  #define INF 9999999
                                                                     0.1.7 Strongly Connected Component
6
  void floydWarshall (int graph[][V])
8
                                                                   1 #include <bits/stdc++.h>
9
     int dist[V][V], i, j, k;
                                                                   2 using namespace std;
     for (i = 0; i < V; i++)
                                                                   3 const int SIZE = 50001;
10
       for (j = 0; j < V; j++)
                                                                   4 bool visited[SIZE];
11
12
         dist[i][j] = graph[i][j];
                                                                   5 //Input: vector < int > Graph, vector < int > Reverce Graph,
13
       for (k = 0; k < V; k++)
                                                                   6 // int Nomber Of vertexces
14
       {
                                                                   7 //Output:
15
         for (i = 0; i < V; i++)
                                                                   8 //Strongly connected componnet Graph ->
16
                                                                   9 //---> SCC_Graph
17
                                                                  10 //List of Each Componnent -->
           for (j = 0; j < V; j++)
18
                                                                  11 //----> ListOfEachSCC
             if (dist[i][k] + dist[k][j] < dist[i][j])</pre>
19
                                                                  12 //to see each node blongs to where
20
                  dist[i][j] = dist[i][k] + dist[k][j];
                                                                  13 //----SCC_list
21
           }
                                                                  14 //SCC returns the size of SCC graph
22
         }
                                                                  15 vector <int > SCC_Graph[SIZE];
```

```
while(!TopolSorted.empty()){
16 vector<int> ListOfEachSCC[SIZE];
                                                                 59
                                                                             int u = TopolSorted.top();
17 int SCC_List[SIZE];
                                                                 60
18
                                                                 61
                                                                             TopolSorted.pop();
                                                                 62
                                                                             if(visited[u]){
19
   void TopolSort(vector<int> g[],int u, stack<int>& ans){
20
       if(visited[u]){
                                                                 63
                                                                                 continue;
21
                                                                 64
           return:
22
                                                                 65
                                                                             DFSR(graph_reverce, u, counter);
       visited[u] = true;
23
                                                                 66
                                                                             counter++:
       for(int i = 0; i < g[u].size(); i++){
24
                                                                 67
                                                                        }
25
           TopolSort(g,g[u][i],ans);
                                                                         for(int i = 0; i < counter; i++){
                                                                 68
26
                                                                             for(int j = 0 ; j < ListOfEachSCC[i].size() ; j++){</pre>
                                                                 69
                                                                                 int u = ListOfEachSCC[i][j];
27
       ans.push(u);
                                                                 70
                                                                                 for(int k = 0; k < graph[u].size(); k++){
28 }
                                                                 71
                                                                                     int w = graph[u][k];
29
                                                                 72
                                                                                     if(SCC_List[u] != SCC_List[w]){
30
   void DFSR(vector<int> g[],int u, int counter){
                                                                 73
31
       if(visited[u]){
                                                                                         SCC_Graph[SCC_List[u]].push_back(SCC_List
                                                                 74
32
                                                                                             [w];
           return;
33
                                                                 75
       }
                                                                                     }
34
       visited[u] = true;
                                                                 76
                                                                                 }
       for(int i = 0; i < g[u].size(); i++){
                                                                 77
                                                                             }
35
36
           DFSR(g,g[u][i], counter);
                                                                 78
37
                                                                 79
                                                                         return counter;
38
       ListOfEachSCC[counter].push_back(u);
                                                                 80 }
39
       SCC_List[u] = counter;
                                                                    0.1.8 Minimum Spanning Tree
40 }
41
                                                                  1 //C++ program for Prim's Minimum Spanning Tree (MST)
42 int SCC(vector<int> graph[], vector<int> graph_reverce[],int
                                                                        algorithm.
      v){
                                                                  2 #include <stdio.h>
43
       fill(visited, visited+v, false);
                                                                  3 #include <limits.h>
44
       for(int i = 0; i < v; i++){
           SCC_Graph[i].clear();
45
                                                                  5 #define V 5 //Graph Size
46
           ListOfEachSCC[i].clear();
47
           SCC_List[i] = 0;
                                                                  7 int minKey(int key[], bool mstSet[])
48
                                                                  8 {
49
       stack<int> TopolSorted;
                                                                  9
                                                                       int min = INT_MAX, min_index;
       for(int i = 0; i < v; i++){
50
                                                                 10
                                                                        for (int v = 0; v < V; v++)
           if(visited[i]){
51
                                                                 11
                                                                          if (mstSet[v] == false && key[v] < min)</pre>
52
                continue;
                                                                              min = key[v], min_index = v;
                                                                 12
53
           }
                                                                 13
                                                                       return min_index;
54
           TopolSort(graph,i, TopolSorted);
                                                                 14 }
55
                                                                 15
       fill(visited, visited+v, false);
56
                                                                 16 int printMST(int parent[], int n, int graph[V][V])
57
       fill(SCC_List, SCC_List+v, 0);
                                                                 17 {
       int counter = 0;
58
                                                                 18
                                                                        printf("Edge,,,,Weight\n");
```

```
19
      for (int i = 1; i < V; i++)
                                                                     61
                                                                             return 0;
20
          printf("%d_{\square}-_{\square}%d_{\square\square\square\square}%d_{\square}\n", parent[i], i, graph[i][
                                                                     62 }
             parent[i]]);
                                                                        0.1.9 MST Kruskal
21 }
22
                                                                      1 #include <iostream>
   void primMST(int graph[V][V])
                                                                      2 #include <vector>
24 {
                                                                      3 #include <algorithm>
25
       int parent[V];
                                                                        using namespace std;
26
       int key[V];
27
       bool mstSet[V];
                                                                        class Disjoint_set
28
       for (int i = 0; i < V; i++)
                                                                      7 {
29
            key[i] = INT_MAX, mstSet[i] = false;
                                                                           int *id, cnt, *sz;
30
       key[0] = 0;
                                                                      9 public:
31
       parent[0] = -1;
                                                                     10
                                                                           Disjoint_set(int N)
32
       for (int count = 0; count < V-1; count++)
                                                                     11
                                                                           {
33
                                                                     12
                                                                             cnt = N;
34
            int u = minKey(key, mstSet);
                                                                     13
                                                                             id = new int[N];
            mstSet[u] = true;
35
                                                                     14
                                                                             sz = new int[N];
36
            for (int v = 0; v < V; v++)
              if (graph[u][v] \&\& mstSet[v] == false \&\& graph[u][v]
                                                                             for(int i=0; i<N; i++)
37
                                                                             {
                 ] < key[v])
                                                                     17
                                                                               id[i] = i;
                 parent[v] = u, key[v] = graph[u][v];
38
                                                                     18
                                                                               sz[i] = 1;
39
                                                                     19
                                                                             }
40
        printMST(parent, V, graph);//print Solution
                                                                     20
                                                                           }
41 }
                                                                     21
                                                                           "Disjoint_set()
42
                                                                     22
                                                                           {
43 int main()
                                                                     23
                                                                             delete [] id;
44 {
                                                                             delete [] sz;
                                                                     24
45
      /* Let us create the following graph
                                                                           }
                                                                     25
46
              2
                    3
                                                                     26
                                                                           int find(int p)
47
          (0) - -(1) - -(2)
                                                                     27
48
               /\ /
                                                                     28
                                                                             int root = p;
49
          61 8/ \5 17
                                                                             while (root != id[root])
                                                                     29
50
           1/ \ /
                                                                     30
                                                                               root = id[root];
51
          (3) ----(4)
                                                                     31
                                                                             while (p != root)
52
                 9
                             */
                                                                     32
                                                                             {
      int graph[V][V] =
53
                                                                     33
                                                                               int newp = id[p];
54
       \{\{0, 2, 0, 6, 0\},
                                                                     34
                                                                               id[p] = root;
       {2, 0, 3, 8, 5},
55
                                                                     35
                                                                               p = newp;
56
       {0, 3, 0, 0, 7},
                                                                     36
                                                                             }
       {6, 8, 0, 0, 9},
57
                                                                     37
                                                                             return root;
58
       \{0, 5, 7, 9, 0\},\
                                                                     38
59
       };
                                                                           void merge(int x, int y)
                                                                     39
60
       primMST(graph);
                                                                     40
                                                                           {
```

```
int i = find(x);
                                                                                second));
41
42
       int j = find(y);
                                                                   83
                                                                             set.merge(E[i].first.first, E[i].first.second);
43
       if (i == j) return;
                                                                   84
                                                                   85 }
44
           (sz[i] < sz[j])
                                                                   86
45
                                                                      void MST_kruskal(vector<pair<int, int>, int> > E)
46
         id[i] = j;
47
         sz[j] += sz[i];
                                                                   88
48
       }
                                                                   89
                                                                        Disjoint_set set(Gsize);
                                                                        _A.clear();
49
       else
                                                                   90
                                                                        sort(E.begin(), E.end(), cmp);
                                                                   91
50
                                                                        for(int i=0;i<E.size();i++)</pre>
                                                                   92
51
         id[j] = i;
52
          sz[i] += sz[j];
                                                                   93
                                                                           if(!set.connected(E[i].first.first, E[i].first.second))
53
       }
                                                                   94
                                                                   95
                                                                             _A.push_back(make_pair(E[i].first.first, E[i].first.
54
       cnt--;
                                                                                second));
55
     bool connected(int x, int y) {return find(x) == find(y);} 96
                                                                             set.merge(E[i].first.first, E[i].first.second);
56
     int count() {return cnt;}
                                                                          }
57
                                                                   97
                                                                   98 }
58 };
59
                                                                   99
   const int Gsize = 9;
                                                                  100
                                                                      int main()
61
                                                                  101 {
   bool cmp(pair<pair<int, int>, int> p1, pair<pair<int, int>,102
      int > p2)
                                                                  103
                                                                        return 0;
63 f
                                                                  104 }
64
     return p1.second < p2.second;
                                                                      0.1.10 Maximum-BPM
65 }
66
                                                                    1 // A C++ program to find maximal Bipartite matching.
   vector < pair < int , int > > _A;
                                                                    2 #include <iostream>
68
                                                                    3 #include <string.h>
   void MST_kruskal(vector<int> G[], vector<int> w[])
                                                                    4 using namespace std;
70 {
71
     Disjoint_set set(Gsize);
                                                                    6 #define M 6 // Size Of Graph M*N
72
     _A.clear();
                                                                     #define N 6
73
     vector<pair<int, int>, int> > E;
     for(int i=0;i<Gsize;i++)</pre>
74
                                                                    9 bool bpm(bool bpGraph[M][N], int u, bool seen[], int matchR
       for(int j=0;j<G[i].size();j++)
75
                                                                          [])
76
         if(i<G[i][i])
            E.push_back(make_pair(make_pair(i, G[i][j]), w[i][j]<sup>10</sup> {
    ):
77
                                                                          for (int v = 0; v < N; v++)
               );
                                                                   12
     sort(E.begin(), E.end(), cmp);
78
                                                                   13
                                                                               if (bpGraph[u][v] && !seen[v])
     for(int i=0;i<E.size();i++)</pre>
79
                                                                   14
                                                                               {
       if(!set.connected(E[i].first.first, E[i].first.second))
80
                                                                                   seen[v] = true; // Mark v as visited
81
       {
                                                                                   if (matchR[v] < 0 || bpm(bpGraph, matchR[v], seen</pre>
82
          _A.push_back(make_pair(E[i].first.first, E[i].first.
                                                                                       , matchR))
```

```
₹
17
                                                                    1 // C++ program for implementation of Ford Fulkerson algorithm
18
                    matchR[v] = u;
                                                                    2 #include <iostream>
19
                    return true;
                                                                    3 #include <limits.h>
20
                }
                                                                    4 #include <string.h>
           }
21
                                                                    5 #include <queue>
22
                                                                    6 using namespace std;
23
       return false;
24 }
                                                                       #define V 6
25
                                                                    9
   int maxBPM(bool bpGraph[M][N])
                                                                   10 bool bfs(int rGraph[V][V], int s, int t, int parent[])
27 {
                                                                   11 {
28
                                                                   12
       int matchR[N]; //List Of Matches
                                                                           bool visited[V];
29
                                                                   13
                                                                           memset(visited, 0, sizeof(visited));
30
       memset(matchR, -1, sizeof(matchR));
                                                                   14
                                                                           queue <int> q;
31
                                                                           q.push(s);
                                                                   15
32
                                                                           visited[s] = true;
       int result = 0;
                                                                   16
33
       for (int u = 0; u < M; u++)
                                                                           parent[s] = -1;
                                                                   17
                                                                           while (!q.empty())
34
       {
                                                                   18
35
            bool seen[N];
                                                                   19
                                                                   20
36
            memset(seen, 0, sizeof(seen));
                                                                               int u = q.front();
                                                                   21
37
            if (bpm(bpGraph, u, seen, matchR))
                                                                               q.pop();
                                                                   22
38
                result++;
                                                                   23
39
       }
                                                                               for (int v=0; v<V; v++)
40
       return result;
                                                                   24
                                                                   25
                                                                                    if (visited[v] == false && rGraph[u][v] > 0)
41 }
42
                                                                   26
                                                                                    {
43 int main()
                                                                   27
                                                                                        q.push(v);
44 {
                                                                   28
                                                                                        parent[v] = u;
                                                                                        visited[v] = true;
45
       bool bpGraph[M][N] = \{ \{0, 1, 1, 0, 0, 0\}, \}
                                                                   29
                                                                   30
                                                                                   }
46
                        \{1, 0, 0, 1, 0, 0\},\
47
                                                                   31
                                                                               }
                         \{0, 0, 1, 0, 0, 0\},\
48
                        \{0, 0, 1, 1, 0, 0\},\
                                                                   32
49
                        \{0, 0, 0, 0, 0, 0\},\
                                                                   33
                                                                           return (visited[t] == true);
50
                        \{0, 0, 0, 0, 0, 1\}
                                                                   34 }
51
                      };
                                                                   35
                                                                      int fordFulkerson(int graph[V][V], int s, int t)
52
   cout << "Maximum_Maching_"<< maxBPM(bpGraph);</pre>
                                                                   37 {
                                                                   38
54
                                                                           int u, v;
55 return 0;
                                                                   39
                                                                           int rGraph[V][V];
56 }
                                                                   40
                                                                           for (u = 0; u < V; u++)
                                                                   41
                                                                               for (v = 0; v < V; v++)
        Flow
   0.2
                                                                   42
                                                                                     rGraph[u][v] = graph[u][v];
                                                                   43
                                                                           int parent[V];
   0.2.1 Max-Flow
                                                                           int max_flow = 0;
                                                                   44
```

```
while (bfs(rGraph, s, t, parent))
                                                                   10
45
                                                                   11 int bfs(int rGraph[V][V], int s, int t, int parent[])
46
       {
47
            int path_flow = INT_MAX;
                                                                   12 {
            for (v=t; v!=s; v=parent[v])
                                                                   13
48
                                                                           bool visited[V];
                                                                           memset(visited, 0, sizeof(visited));
49
                                                                   14
                u = parent[v];
                                                                   15
50
51
                path_flow = min(path_flow, rGraph[u][v]);
                                                                   16
                                                                           queue <int> q;
52
            }
                                                                   17
                                                                           q.push(s);
53
                                                                   18
                                                                           visited[s] = true;
                                                                           parent[s] = -1;
54
            for (v=t; v != s; v=parent[v])
                                                                   19
55
                                                                   20
                                                                   21
56
                u = parent[v];
                                                                           while (!q.empty())
57
                rGraph[u][v] -= path_flow;
                                                                   22
                                                                               int u = q.front();
58
                rGraph[v][u] += path_flow;
                                                                   23
59
            }
                                                                   24
                                                                               q.pop();
60
                                                                   25
            max_flow += path_flow;
61
                                                                   26
                                                                               for (int v=0; v<V; v++)
                                                                   27
62
       return max_flow;
                                                                               {
63 }
                                                                   28
                                                                                    if (visited[v] == false && rGraph[u][v] > 0)
64
                                                                   29
65 int main()
                                                                   30
                                                                                        q.push(v);
                                                                                        parent[v] = u;
66
                                                                   31
                                                                   32
                                                                                        visited[v] = true;
67
       int graph[V][V] = \{ \{0, 16, 13, 0, 0, 0\}, \}
68
                             \{0, 0, 10, 12, 0, 0\},\
                                                                   33
                                                                                    }
69
                             \{0, 4, 0, 0, 14, 0\},\
                                                                   34
                                                                               }
                             {0, 0, 9, 0, 0, 20},
70
                                                                   35
71
                             \{0, 0, 0, 7, 0, 4\},\
                                                                   36
                                                                           return (visited[t] == true);
72
                             \{0, 0, 0, 0, 0, 0\}
                                                                   37 }
73
                           };
                                                                   38
74
       cout << "The | maximum | possible | flow | is | "</pre>
                                                                   39 void dfs(int rGraph[V][V], int s, bool visited[])
        << fordFulkerson(graph, 0, 5);</pre>
                                                                   40 {
75
76
       return 0:
                                                                   41
                                                                           visited[s] = true:
77 }
                                                                   42
                                                                           for (int i = 0; i < V; i++)
                                                                   43
                                                                              if (rGraph[s][i] && !visited[i])
   0.2.2 Min-Cut
                                                                   44
                                                                                   dfs(rGraph, i, visited);
                                                                   45 }
1 // C++ program for finding minimum cut using Ford-Fulkerson
2 #include <iostream>
                                                                   47 void minCut(int graph[V][V], int s, int t)
3 #include <limits.h>
                                                                   48 {
4 #include <string.h>
                                                                   49
                                                                           int u, v;
5 #include <queue>
                                                                           int rGraph[V][V];
                                                                   50
6 using namespace std;
                                                                           for (u = 0; u < V; u++)
                                                                   51
                                                                   52
                                                                               for (v = 0; v < V; v++)
8 // Number of vertices in given graph
                                                                   53
                                                                                     rGraph[u][v] = graph[u][v];
9 #define V 6
```

```
int parent[V];
54
55
       while (bfs(rGraph, s, t, parent))
56
57
            int path_flow = INT_MAX;
58
            for (v=t; v!=s; v=parent[v])
59
60
                u = parent[v];
                path_flow = min(path_flow, rGraph[u][v]);
61
62
           }
63
           for (v=t; v != s; v=parent[v])
64
65
                u = parent[v];
                rGraph[u][v] -= path_flow;
66
67
                rGraph[v][u] += path_flow;
           }
68
69
70
       //Finishing...
71
       bool visited[V];
72
       memset(visited, false, sizeof(visited));
73
       dfs(rGraph, s, visited);
74
       for (int i = 0; i < V; i++)
75
         for (int j = 0; j < V; j++)
76
             if (visited[i] && !visited[j] && graph[i][j])
77
                  cout << i << "u-u" << j << endl;
78
79
       return;
80 }
81
82 int main()
83 {
       int graph[V][V] = \{ \{0, 16, 13, 0, 0, 0\}, \}
84
85
                             {0, 0, 10, 12, 0, 0},
86
                             \{0, 4, 0, 0, 14, 0\},\
                             \{0, 0, 9, 0, 0, 20\},\
87
88
                             {0, 0, 0, 7, 0, 4},
89
                             \{0, 0, 0, 0, 0, 0\}
90
                          };
91
92
       minCut(graph, 0, 5);
93
94
       return 0;
95 }
```

0.3 Geometry

0.3.1 Convex-Hull

```
1 // A C++ program to find convex hull of a set of points.
       Refer
2 #include <iostream>
3 #include <stack>
4 #include <stdlib.h>
5 using namespace std;
6
7 struct Point
8 {
9
       int x, y;
10 };
11
12 Point p0;
13
14 Point nextToTop(stack<Point> &S)
15 {
16
       Point p = S.top();
17
       S.pop();
18
       Point res = S.top();
19
       S.push(p);
20
       return res;
21 }
22
23 int swap(Point &p1, Point &p2)
24 {
25
       Point temp = p1;
       p1 = p2;
26
27
       p2 = temp;
28 }
30 int distSq(Point p1, Point p2)
31 {
32
       return (p1.x - p2.x)*(p1.x - p2.x) +
33
             (p1.y - p2.y)*(p1.y - p2.y);
34 }
35
36 int orientation(Point p, Point q, Point r)
37 f
38
       int val = (q.y - p.y) * (r.x - q.x)
           -(q.x - p.x) * (r.y - q.y);
39
```

```
40
       if (val == 0) return 0;
                                                                   83
41
       return (val > 0)? 1: 2;
                                                                   84
                                                                          stack < Point > S;
42 }
                                                                   85
                                                                          S.push(points[0]);
                                                                   86
                                                                          S.push(points[1]);
44 int compare(const void *vp1, const void *vp2)
                                                                   87
                                                                          S.push(points[2]);
45 {
                                                                   88
      Point *p1 = (Point *) vp1;
46
                                                                   89
                                                                          for (int i = 3: i < m: i++)
47
      Point *p2 = (Point *)vp2;
                                                                   90
48
                                                                   91
                                                                             while (orientation(nextToTop(S), S.top(), points[i]) !=
49
      int o = orientation(p0, *p1, *p2);
                                                                                  2)
                                                                                S.pop();
50
      if (o == 0)
                                                                   92
51
        return (distSq(p0, *p2) >= distSq(p0, *p1))?
                                                                   93
                                                                             S.push(points[i]);
                                                                         }
52
                     -1 : 1:
                                                                   94
53
                                                                   95
54
      return (o == 2)? -1: 1;
                                                                   96
                                                                          while (!S.empty()) // List Of The Points In The Convex
55 }
                                                                             Hull
56
                                                                   97
                                                                         {
57 void convexHull(Point points[], int n)
                                                                   98
                                                                              Point p = S.top();
                                                                              cout << "(" << p.x << ", " << p.y <<")" << endl;
58 {
                                                                   99
59
      int ymin = points[0].y, min = 0;
                                                                  100
                                                                              S.pop();
      for (int i = 1; i < n; i++)
                                                                         }
60
                                                                  101
61
                                                                  102 }
        int y = points[i].y;
62
                                                                  103
63
        if ((v < vmin) || (vmin == v &&
                                                                  104 int main()
            points[i].x < points[min].x))</pre>
                                                                  105 - {}
64
65
           ymin = points[i].y, min = i;
                                                                  106
                                                                           Point points[] = \{\{0, 3\}, \{1, 1\}, \{2, 2\}, \{4, 4\},
66
      }
                                                                  107
                                                                                            \{0, 0\}, \{1, 2\}, \{3, 1\}, \{3, 3\}\};
67
                                                                  108
                                                                           int n = sizeof(points)/sizeof(points[0]);
                                                                          /* N is The Number of Points And points is
68
      swap(points[0], points[min]);
                                                                  109
69
                                                                  110
                                                                           the list Of points */
      p0 = points[0];
                                                                  111
                                                                           convexHull(points, n);
70
71
      gsort(&points[1], n-1, sizeof(Point), compare);
                                                                  112
                                                                           return 0:
72
                                                                  113 }
73
      int m = 1; // Initialize size of modified array
                                                                      0.3.2 Shoelace Formula (python)
74
      for (int i=1; i < n; i++)
75
          while (i < n-1 && orientation(p0, points[i], points[i] def PolygonArea(corners):
76
                                                                           n = len(corners) # of corners
              +1]) == 0)
                                                                           area = 0.0
77
             <u>i</u>++:
                                                                           for i in range(n):
78
           points[m] = points[i];
                                                                               i = (i + 1) \% n
79
           m++;
                                                                    6
                                                                               area += corners[i][0] * corners[j][1]
80
      }
                                                                               area -= corners[j][0] * corners[i][1]
81
                                                                           area = abs(area) / 2.0
82
      if (m < 3) return;
                                                                           return area
```

```
10
                                                                   6
                                                                          bool type; // Type of event: 0 = Lower-left; 1 = Upper-
11 # examples
                                                                             right
12 \text{ corners} = [(2.0, 1.0), (4.0, 5.0), (7.0, 8.0)]
                                                                         event(){};
                                                                         event(int ind, int type) : ind(ind), type(type){};
13 print (PolygonArea(corners))
                                                                   9 };
   0.3.3 Swap Line
                                                                  10 struct point
                                                                  11 {
1 #include <bits/stdc++.h>
                                                                  12
                                                                          int x, y;
2 #define px second
                                                                  13 }:
3 #define py first
                                                                  14 point rects[MAX][12];
4 typedef pair < long long, long long > pairll;
                                                                  15 // Each rectangle consists of 2 points: [0] = lower-left;
5 pairll pnts [MAX];
                                                                         \lceil 1 \rceil = upper - right
6 int compare(pairll a, pairll b)
                                                                  16 bool compare_x(event a, event b)
7 {
                                                                  17 {
 8
           return a.px < b.px;</pre>
                                                                  18
                                                                         return rects[a.ind][a.type].x < rects[b.ind][b.type].x;</pre>
9 }
                                                                  19 }
   double closest_pair(pairll pnts[],int n)
                                                                  20 bool compare_y(event a, event b)
11 {
                                                                  21 {
12
           sort(pnts,pnts+n,compare);
                                                                  22
                                                                         return rects[a.ind][a.type].y < rects[b.ind][b.type].y;</pre>
13
           double best=INF;
                                                                  23
14
           set < pairll > box;
                                                                  24 int union_area(event events_v[], event events_h[], int n, int
           box.insert(pnts[0]);
15
                                                                          e )
16
           int left = 0;
                                                                  25 {
17
           for (int i=1; i < n; ++ i)
                                                                  26
                                                                          /*n is the number of rectangles, e=2*n, e is the number
18
           {
19
                while (left<i && pnts[i].px-pnts[left].px > bestn)
                                                                          points (each rectangle has two points as described in
20
                    box.erase(pnts[left++]);
                                                                  28
                                                                          declaration of rects)
                for(typeof(box.begin()) it=box.lower_bound(
21
                                                                          */
                   make_pair(pnts[i].py-best, pnts[i].px-best)) 30
                                                                          bool in_set[MAX] = {0};
                   it!=box.end() && pnts[i].py+best>=it->py;it 31
                                                                          int area = 0;
                   ++)
                                                                  32
                                                                          sort(events_v, events_v + e, compare_x);
                    best = min(best, sqrt(pow(pnts[i].py - it->pg
22
                                                                          //Pre-sort of vertical edges
                       , 2.0) + pow(pnts[i].px - it -> px, 2.0))); 34
                                                                          sort(events_h, events_h + e, compare_y);
23
                box.insert(pnts[i]);
                                                                  35
                                                                          // Pre-sort set of horizontal edges
24
           }
                                                                  36
                                                                          in_set[events_v[0].ind] = 1;
25
           return best;
                                                                  37
                                                                         for (int i = 1; i < e; ++i)
26 }
                                                                  38
                                                                  39
                                                                              event c = events_v[i];
   0.3.4 Union Of Rectangles
                                                                  40
                                                                              int cnt = 0; // Counter to indicate how many
                                                                  41
                                                                              //rectangles are currently overlapping
1 #include <bits/stdc++.h>
                                                                  42
                                                                              // Delta_x: Distance between current
 2 #define MAX 1000
                                                                  43
                                                                              // sweep line and previous sweep line
 3 struct event
                                                                  44
                                                                              int delta_x = rects[c.ind][c.type].x - rects[events_v
4 {
                                                                                 [i - 1].ind]\
       int ind:
                   // Index of rectangle in rects
```

```
[events_v[i - 1].type].x;
                                                                   8
45
46
           int begin_y;
                                                                       int lcs( char *X, char *Y, int m, int n)
47
           if (delta_x == 0)
                                                                   10 {
48
           {
                                                                   11
                                                                         int L[m+1][n+1];
                                                                         int i, j;
49
                in_set[c.ind] = (c.type == 0);
                                                                   12
50
                continue:
                                                                   13
51
           }
                                                                   14
                                                                         for (i=0; i \le m; i++)
52
           for (int j = 0; j < e; ++ j)
                                                                   15
53
                if (in_set[events_h[j].ind] == 1)
                                                                   16
                                                                            for (j=0; j <= n; j++)
                {
                                                                   17
54
                                                                              if (i == 0 || j == 0)
                                                                   18
55
                    if (events_h[j].type == 0)
                                                                   19
                                                                                L[i][j] = 0;
56
57
                        if (cnt == 0)
                                                                   20
                                                                              else if (X[i-1] == Y[j-1])
58
                             begin_v = rects[events_h[j].ind][0].24
                                                                   22
                                                                                L[i][j] = L[i-1][j-1] + 1;
                                                                   23
59
                        ++cnt;
                    }
                                                                   24
60
                                                                              else
                                                                   25
                                                                                L[i][j] = max(L[i-1][j], L[i][j-1]);
61
                    else
62
                                                                   26
63
                                                                   27
                        --cnt;
                        if (cnt == 0)
64
                                                                   28
                                                                         return L[m][n];
65
                                                                   29 }
66
                             int delta_y = (rects[events_h[j].ind30
                                ][13].y - begin_y);
                                                                   31 int main()
67
                             area += delta_x * delta_y;
                                                                   32 {
68
                        }
                                                                   33
                                                                        char X[] = "AGGTAB";
69
                    }
                                                                   34
                                                                        char Y[] = "GXTXAYB";
70
                                                                   35
71
            in_set[c.ind] = (c.type == 0);
                                                                   36
                                                                        int m = strlen(X);
72
       }
                                                                   37
                                                                        int n = strlen(Y);
                                                                   38
73
       return area;
74 }
                                                                   39
                                                                        printf("Length_of_LCS_is_%dn", lcs( X, Y, m, n ) );
                                                                   40
   0.4 String
                                                                   41
                                                                        return 0;
                                                                   42 }
   0.4.1 LCS
                                                                      0.4.2 LIS
1 /* Dynamic Programming C/C++ implementation of LCS problem */ typedef vector<int> VI;
2 #include <bits/stdc++.h>
                                                                   2 typedef pair < int, int > PII;
                                                                   3 typedef vector <PII > VPII;
4 int max(int a, int b)
5 f
                                                                      #define STRICTLY_INCREASNG
6
       return (a > b)? a : b;
7 }
                                                                   7 VI LongestIncreasingSubsequence(VI v) {
```

```
14
     VPII best:
9
     VI dad(v.size(), -1);
                                                                 15 void buildPi(string& p, VI& pi)
10
                                                                 16 {
11
     for (int i = 0; i < v.size(); i++) {
                                                                 17
                                                                       pi = VI(p.length());
   #ifdef STRICTLY_INCREASNG
                                                                 18
                                                                     int k = -2;
13
       PII item = make_pair(v[i], 0);
                                                                      for(int i = 0; i < p.length(); i++) {
       VPII::iterator iter = lower_bound(best.begin(), best.end20
                                                                         while (k \ge -1 \&\& p[k+1] != p[i])
           (), item);
                                                                 21
                                                                          k = (k == -1) ? -2 : pi[k];
       item.second = i;
15
                                                                         pi[i] = ++k;
                                                                 23
                                                                       }
16 #else
                                                                 24 }
17
       PII item = make_pair(v[i], i);
18
       VPII::iterator iter = upper_bound(best.begin(), best.en@5
           (), item);
                                                                 26 int KMP(string& t, string& p)
                                                                 27 {
19 #endif
20
       if (iter == best.end()) {
                                                                 28
                                                                     VI pi;
21
         dad[i] = (best.size() == 0 ? -1 : best.back().second) 29
                                                                       buildPi(p, pi);
                                                                      int k = -1;
         best.push_back(item);
                                                                 30
23
      } else {
                                                                 31
                                                                       for(int i = 0; i < t.length(); i++) {
24
         dad[i] = dad[iter->second];
                                                                 32
                                                                         while (k \ge -1 \&\& p[k+1] != t[i])
25
         *iter = item;
                                                                 33
                                                                          k = (k == -1) ? -2 : pi[k];
      }
26
                                                                 34
                                                                         k++;
27
     }
                                                                 35
                                                                        if(k == p.length() - 1) {
28
                                                                 36
                                                                          // p matches t[i-m+1, \ldots, i]
29
                                                                 37
                                                                           cout << "matched_iat_index_i" << i-k << ":";</pre>
     VI ret:
     for (int i = best.back().second; i >= 0; i = dad[i])
                                                                           cout << t.substr(i-k, p.length()) << endl;</pre>
30
                                                                 38
31
       ret.push_back(v[i]);
                                                                           k = (k == -1) ? -2 : pi[k];
                                                                 39
32
     reverse(ret.begin(), ret.end());
                                                                        }
                                                                 40
33
     return ret;
                                                                 41
                                                                       }
34 }
                                                                 42
                                                                       return 0;
                                                                 43 }
   0.4.3 KMP
                                                                 44
                                                                 45 int main()
1 /*
                                                                 46 {
2 Finds all occurrences of the pattern string p within the
                                                                 47
                                                                       string a = "AABAACAADAABAABA", b = "AABA";
3 text string t. Running time is O(n + m), where n and m
                                                                 48
                                                                       KMP(a, b); // expected matches at: 0, 9, 12
4 are the lengths of p and t, respectively.
                                                                 49
                                                                       return 0;
5 */
                                                                 50 }
7 #include <iostream>
                                                                    0.5 Other
8 #include <string>
9 #include <vector>
                                                                     0.5.1 Disjoint Set
10
11 using namespace std;
                                                                  1 // To represent Disjoint Sets
                                                                  2 struct DisjointSets
13 typedef vector <int > VI;
```

```
3 {
                                                                        diqit
       int *parent, *rnk;
                                                                  6 // integers.
       int n;
                                                                 8 string dayOfWeek[] = {"Mo", "Tu", "We", "Th", "Fr", "Sa", "Su
       DisjointSets(int n)
8
                                                                  9
9
                                                                   // converts Gregorian date to integer (Julian day number)
           this -> n = n:
10
           parent = new int[n+1];
                                                                 11
11
           rnk = new int[n+1];
                                                                 12 int DateToInt (int m, int d, int y) {
12
           for (int i = 0; i \le n; i++)
                                                                 13
                                                                      return
                                                                        1461 * (y + 4800 + (m - 14) / 12) / 4 +
13
                                                                 14
14
               rnk[i] = 0;
                                                                 15
                                                                        367 * (m - 2 - (m - 14) / 12 * 12) / 12 -
15
                                                                 16
                                                                        3 * ((y + 4900 + (m - 14) / 12) / 100) / 4 +
16
               parent[i] = i;
                                                                        d - 32075;
                                                                 17
                                                                 18 }
17
           }
       }
                                                                 19
18
19
                                                                 20 // converts integer (Julian day number) to Gregorian date:
20
                                                                        month/day/year
       int find(int u)
21
                                                                 21
22
           if (u != parent[u])
                                                                    void IntToDate (int jd, int &m, int &d, int &y){
               parent[u] = find(parent[u]);
23
                                                                 23
                                                                      int x, n, i, j;
24
           return parent[u];
                                                                 24
25
                                                                 25
                                                                      x = id + 68569;
26
       void merge(int x, int y)
                                                                 26
                                                                      n = 4 * x / 146097;
27
                                                                 27
                                                                      x = (146097 * n + 3) / 4;
28
           x = find(x), y = find(y);
                                                                 28
                                                                      i = (4000 * (x + 1)) / 1461001;
29
           if (rnk[x] > rnk[y])
                                                                 29
                                                                      x = 1461 * i / 4 - 31;
30
               parent[y] = x;
                                                                      i = 80 * x / 2447;
                                                                 30
31
           else
                                                                 31
                                                                      d = x - 2447 * j / 80;
32
                                                                 32
                                                                      x = i / 11;
               parent[x] = y;
33
                                                                 33
                                                                      m = i + 2 - 12 * x:
           if (rnk[x] == rnk[y])
34
                                                                 34
                                                                      y = 100 * (n - 49) + i + x;
               rnk[y]++;
35
                                                                 35 }
36
       }
                                                                 36
37 };
                                                                 37 // converts integer (Julian day number) to day of week
                                                                 38
   0.5.2 Date Transformation
                                                                    string IntToDay (int jd){
                                                                      return dayOfWeek[jd % 7];
1 //Dates (C++)
                                                                 41 }
                                                                    0.5.3 make CIN and COUT Run Faseter
3 // Routines for performing computations on dates. In these
      routines,
4 // months are exprsesed as integers from 1 to 12, days are 1 ios_base::sync_with_stdio(false);
5 // as integers from 1 to 31, and years are expressed as 4-
```