The FarshadBazi Code Notebook

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0.1 Graph

0.1.1 BFS

```
1 #include <bits/stdc++.h>
2 using namespace \operatorname{\mathtt{std}};
3 const int SIZE = 100; //Vertex size
4 int main(){
5
     int source = 0;
     vector < int > Graph [SIZE];
6
7
     bool visited[SIZE];
     int distance[SIZE];
9
     fill(visited, visited+SIZE, 0);
     fill(distance, distance+SIZE, INT_MAX);
10
11
     queue < int > q;
     q.push(source);
12
13
     visited[source] = true;
14
     distance[source] = 0;
15
     while(!q.empty()){
16
       int u = q.front();
17
       q.pop();
       for(int i = 0 ; i < Graph[u].size(); i++){</pre>
18
19
          if (visited [Graph [u][i]]) {
20
            continue;
21
          }
22
          visited[Graph[u][i]] = true;
23
          distance[Graph[u][i]] = distance[u] + 1;
24
          q.push(Graph[u][i]);
25
       }
26
     }
27
     return 0;
28 }
   0.1.2
          Topological-Sorting
1 #include <bits/stdc++.h>
2 using namespace std;
3 const int SIZE = 100;//Graph Size Vertex
4 int visited[SIZE];
5 vector <int> Graph[SIZE];
6 stack<int> ans;
   int topolSort(int u)
7
9
     if(visited[u] == 1)
10
     {
       return -1; //cycle
11
12
     if(visited[u] == 2)
13
14
     {
15
       return 0;
16
17
     visited[u] = 1;
18
     for(int i = 0; i < Graph[u].size(); i++)
19
     {
20
        topolSort(Graph[u][i]);
21
22
        visited[u] = 2;
23
     ans.push(u);
24
     return 0;
25 }
26
27 int main(){
28
     return 0;
29 }
```

0.1.3 DAG Shortest Path

```
#include <iostream >
2 #include <vector>
3 using namespace \operatorname{\mathtt{std}};
   const int Gsize=100000;
6
7
   int _color[Gsize], _p[Gsize] ,_d[Gsize] ,_f[Gsize] , _time;
8 vector<int> _V;
  void DFS_visit(vector<int> G[] ,int u)
10
11
      _time++;
12
      _d[u]=_time;
      _color[u]=1;
13
      int v;
14
15
     for(int i=0;i<G[u].size();i++)
16
17
        v=G[u][i];
18
        if(!_color[v])
19
20
          _p[v]=u;
21
          DFS_visit(G ,v);
22
        }
     }
23
      _color[u]=2;
24
25
      _time++;
26
      _f[u]=_time;
27
      _V.push_back(u);
28
   }
29
   void DFS(vector<int>G[])
30 {
     for(int i=0;i<Gsize;i++)</pre>
31
32
33
        _color[i]=0; _p[i]=0;
34
35
      _{time}=0;
36
     for(int i=0;i<Gsize;i++)</pre>
37
        if(!_color[i])
38
          DFS_visit(G ,i);
39
   }
40
41
   void Topologival_sort(vector<int> G[], int arr[])
42
43
      _V.clear();
44
      DFS(G);
     for(int i=0;i<_V.size();i++)</pre>
45
46
        arr[_V.size()-1-i] = _V[i];
47
   }
48
49
   void _Relax(int u, int v, int w)
50
51
      if(\underline{d}[v]>(\underline{d}[u]+w))
52
53
        _d[v] = _d[u] + w;
54
        _p[v] = u;
      }
55
56 }
57
   void DAG_shortest_paths(vector<int> G[], vector<int> W[], int s)
58
59
60
      int arr[Gsize];
61
     Topologival_sort(G, arr);
62
      for(int i=0;i<Gsize;i++)</pre>
63
        _d[i]=500000000;
```

```
64
      _d[s] = 0;
65
     for(int i=0;i<Gsize;i++)</pre>
66
67
        int u=arr[i];
        for(int j=0; j < G[u].size(); j++)</pre>
68
69
          _Relax(u, G[u][j], W[u][j]);
70
71
   }
72
73 int main()
74
75
76
     return 0;
77 }
   0.1.4 Bellman-Ford
   // A C++ program for Bellman-Ford's single source
  #include <bits/stdc++.h>
3
   struct Edge
5
   {
6
        int src, dest, weight;
   };
9
   struct Graph
10
11
        int V, E; //Size Of Graph
12
        struct Edge* edge;
13
   };
14
15
   struct Graph* createGraph(int V, int E)
16
17
        struct Graph* graph = new Graph;
        graph \rightarrow V = V;
18
19
        graph \rightarrow E = E;
20
        graph -> edge = new Edge [E];
21
        return graph;
22
  }
23
24
   void BellmanFord(struct Graph* graph, int src, int* dist)
25
26
        int V = graph \rightarrow V;
27
        int E = graph->E;
28
29
        for (int i = 0; i < V; i++)
30
            dist[i] = INT_MAX;
31
        dist[src] = 0;
32
33
        for (int i = 1; i \le V-1; i++)
34
35
            for (int j = 0; j < E; j++)
36
37
                 int u = graph->edge[j].src;
                 int v = graph->edge[j].dest;
38
39
                 int weight = graph->edge[j].weight;
40
                 if (dist[u] != INT_MAX && dist[u] + weight < dist[v])</pre>
                     dist[v] = dist[u] + weight;
41
42
            }
43
        }
44
45
        for (int i = 0; i < E; i++)
46
47
            int u = graph->edge[i].src;
48
            int v = graph->edge[i].dest;
```

```
49
            int weight = graph->edge[i].weight;
50
            if (dist[u] != INT_MAX && dist[u] + weight < dist[v])</pre>
51
                printf("Graph_contains_negative_weight_cycle");//Hint!
       }
52
53
54
       //printArr(dist, V);//Finishing Algo
55
56
       return;
57
   }
58
59 int main()
60 {
61
       int V = 5; // Number of vertices in graph
62
       int E = 8; // Number of edges in graph
       struct Graph* graph = createGraph(V, E);
63
64
       graph -> edge [0] .src = 0;
65
       graph -> edge [0] . dest = 1;
66
       graph \rightarrow edge[0].weight = -1;
67
       int dist[5];
68
       BellmanFord(graph, 0, dist);
69
       return 0;
70 }
   0.1.5 Djkstra
1 #include <bits/stdc++.h>
2 using namespace std;
3 #define endl '\n'
4 #define pii pair <int,int>
5 #define F first
6 #define S second
7 #define mp make_pair
8 #define pb emplace_back
9
10 bool vis[100001];
   int dis[100001];
12
  vector < pii > a [100001];
13
14
   class prioritize {
   public: bool operator ()(pii &p1 , pii &p2) {
16
       return p1.S > p2.S;
17
   };
18
19
20
  int Dijkstra(int s, int n) {
21
     for (int i = 0; i \le n; i++) {
22
       vis[i] = false;
23
       dis[i] = INT_MAX;
24
25
     priority_queue < pii, vector < pii >, prioritize > pq;
26
     pq.push(mp(s, dis[s] = 0));
27
     while (!pq.empty()) {
28
       pii cur = pq.top(); pq.pop();
29
       int cv = cur.F, cw = cur.S;
30
       if (vis[cv]) continue;
31
       vis[cv] = true;
32
       for (pii x : a[cv]) {
33
          if (!vis[x.F] && (cw + x.S) < dis[x.F]) {
34
            pq.push(mp(x.F, dis[x.F] = cw + x.S));
35
36
       }
37
     }
38 }
39
40 int main() {
```

```
41
     int tc;
42
      cin >> tc;
43
      while (tc--) {
44
        int v1, v2, w, n, m;
45
        cin >> n >> m;
        for (int i = 0; i \le n; i++) {
46
47
          a[i].clear();
48
        }
49
        for (int i = 0; i < m; i++) {
50
          cin >> v1 >> v2 >> w;
51
          a[v1].pb(mp(v2, w));
        }
52
53
        int s;
54
        cin >> s;
55
        Dijkstra(s, n);
        for (int i = 1; i \le n; i++) {
56
57
          if (dis[i] != INT_MAX) {
58
            cout << dis[i] << "";
59
          } else {
60
            cout << "-1<sub>\(\sigma\)</sub>;
61
        }
62
63
     }
64
      return 0;
65
          Floyd Warshall
   0.1.6
   // C Program for Floyd Warshall Algorithm
2 #include < stdio.h>
3
4 #define V 4
5 #define INF 9999999
   void floydWarshall (int graph[][V])
8
9
      int dist[V][V], i, j, k;
10
      for (i = 0; i < V; i++)
11
        for (j = 0; j < V; j++)
12
          dist[i][j] = graph[i][j];
13
        for (k = 0; k < V; k++)
14
          for (i = 0; i < V; i++)
15
16
17
            for (j = 0; j < V; j++)
18
19
               if (dist[i][k] + dist[k][j] < dist[i][j])</pre>
20
                   dist[i][j] = dist[i][k] + dist[k][j];
21
            }
22
          }
23
24
        // All distances -> dist
25 }
26
27
   int main()
28
29
        /* example Graph:
30
                10
           (0) ---->(3)
31
                       //\
32
            1
33
            - /
                        1
34
                         / 1
            1
                        1
35
           11/
36
           (1) ---
                   --->(2)
37
                 3
```

```
int graph[V][V] =
39
       {
40
         {0,
               5, INF, 10},
41
         {INF, 0, 3, INF},
         {INF, INF, 0, 1},
42
         {INF, INF, INF, 0}
43
44
       };
45
       // Print the solution
46
47
       floydWarshall(graph);
48
       return 0;
49 }
         Strongly Connected Component
1 #include <bits/stdc++.h>
2 using namespace std;
3 const int SIZE = 50001;
4 bool visited[SIZE];
  //Input: vector < int > Graph, vector < int > Reverce Graph,
  // int Nomber Of vertexces
  //Output:
8 //Strongly connected componnet Graph ->
9 //--->SCC\_Graph
10 //List of Each Componnent -->
  //---->ListOfEachSCC
11
12 //to see each node blongs to where
13 //----SCC_list
14 //SCC returns the size of SCC graph
15 vector<int> SCC_Graph[SIZE];
16 vector < int > ListOfEachSCC[SIZE];
17 int SCC_List[SIZE];
19
  void TopolSort(vector<int> g[],int u, stack<int>& ans){
20
       if(visited[u]){
21
           return;
22
       }
23
       visited[u] = true;
24
       for(int i = 0; i < g[u].size(); i++){
25
           TopolSort(g,g[u][i],ans);
26
27
       ans.push(u);
28 }
29
30 void DFSR(vector<int> g[],int u, int counter){
31
       if(visited[u]){
32
           return;
33
       visited[u] = true;
34
       for(int i = 0; i < g[u].size(); i++){
35
36
           DFSR(g,g[u][i], counter);
37
38
       ListOfEachSCC[counter].push_back(u);
39
       SCC_List[u] = counter;
40 }
41
  int SCC(vector<int> graph[], vector<int> graph_reverce[],int v){
42
       fill(visited, visited+v, false);
43
       for(int i = 0; i < v; i++){
44
           SCC_Graph[i].clear();
45
46
           ListOfEachSCC[i].clear();
47
           SCC_List[i] = 0;
48
49
       stack<int> TopolSorted;
50
       for(int i = 0; i < v; i++){
```

```
if(visited[i]){
51
52
                continue;
            }
53
54
            TopolSort(graph,i, TopolSorted);
       }
55
56
       fill(visited, visited+v, false);
       fill(SCC_List, SCC_List+v, 0);
57
58
       int counter = 0;
59
       while(!TopolSorted.empty()){
            int u = TopolSorted.top();
60
61
            TopolSorted.pop();
62
            if(visited[u]){
63
                continue;
64
            }
65
            DFSR(graph_reverce, u, counter);
66
            counter++;
67
       }
68
       for(int i = 0; i < counter; i++){
69
            for(int j = 0 ; j < ListOfEachSCC[i].size() ; j++){</pre>
70
                int u = ListOfEachSCC[i][j];
71
                for(int k = 0; k < graph[u].size(); k++){
                    int w = graph[u][k];
72
                    if(SCC_List[u] != SCC_List[w]){
73
74
                         SCC_Graph[SCC_List[u]].push_back(SCC_List[w]);
75
                    }
76
                }
77
           }
78
       }
79
       return counter;
80 }
          Minimum Spanning Tree
   0.1.8
   //C++ program for Prim's Minimum Spanning Tree (MST) algorithm.
  #include <stdio.h>
   #include <limits.h>
4
  #define V 5 //Graph Size
5
6
7
   int minKey(int key[], bool mstSet[])
8
9
      int min = INT_MAX, min_index;
10
      for (int v = 0; v < V; v++)
11
        if (mstSet[v] == false && key[v] < min)</pre>
12
             min = key[v], min_index = v;
13
      return min_index;
14
  }
15
   int printMST(int parent[], int n, int graph[V][V])
16
17
18
      printf("Edge___Weight\n");
19
      for (int i = 1; i < V; i++)
20
         printf("%du-u%duuuu%du\n", parent[i], i, graph[i][parent[i]]);
21
   }
22
23
   void primMST(int graph[V][V])
24
25
       int parent[V];
26
       int key[V];
27
       bool mstSet[V];
28
       for (int i = 0; i < V; i++)
29
           key[i] = INT_MAX, mstSet[i] = false;
30
       key[0] = 0;
31
       parent[0] = -1;
32
       for (int count = 0; count < V-1; count++)
```

```
{
33
34
            int u = minKey(key, mstSet);
35
            mstSet[u] = true;
36
            for (int v = 0; v < V; v++)
37
              if (graph[u][v] && mstSet[v] == false && graph[u][v] < key[v])</pre>
38
                 parent[v] = u, key[v] = graph[u][v];
39
40
       printMST(parent, V, graph);//print Solution
41
42
43 int main()
44
45
      /* Let us create the following graph
46
              2 3
          (0) --(1) --(2)
47
          1 / 1
48
          6| 8/ \5 |7
| / \ |
49
50
51
          (3) ----(4)
               9
52
      int graph[V][V] =
53
       {{0, 2, 0, 6, 0},
54
       {2, 0, 3, 8, 5},
55
56
       {0, 3, 0, 0, 7},
57
       {6, 8, 0, 0, 9},
58
       \{0, 5, 7, 9, 0\},\
59
60
        primMST(graph);
61
       return 0;
62 }
   0.1.9 MST Kruskal
1 #include <iostream>
2 #include <vector>
3 #include <algorithm>
4 using namespace std;
5
   class Disjoint_set
     int *id, cnt, *sz;
9
   public:
10
     Disjoint_set(int N)
11
12
       cnt = N;
13
       id = new int[N];
14
       sz = new int[N];
15
       for (int i=0; i<N; i++)
16
17
         id[i] = i;
18
         sz[i] = 1;
19
20
21
     ~Disjoint_set()
22
23
       delete [] id;
24
       delete [] sz;
25
26
     int find(int p)
27
28
       int root = p;
29
        while (root != id[root])
30
         root = id[root];
31
        while (p != root)
32
        {
```

```
33
          int newp = id[p];
34
          id[p] = root;
35
          p = newp;
36
        }
37
       return root;
38
     }
39
     void merge(int x, int y)
40
       int i = find(x);
41
42
        int j = find(y);
43
        if (i == j) return;
44
             (sz[i] < sz[j])
45
        ₹
46
          id[i] = j;
47
          sz[j] += sz[i];
        }
48
49
       else
50
        {
51
          id[j] = i;
52
          sz[i] += sz[j];
53
       }
54
        cnt --;
     }
55
56
     bool connected(int x, int y) {return find(x) == find(y);}
57
     int count() {return cnt;}
58
   };
59
   const int Gsize = 9;
60
61
   bool cmp(pair<pair<int, int>, int> p1, pair<pair<int, int>, int> p2)
62
63
64
     return p1.second < p2.second;</pre>
65
66
67
   vector<pair<int, int> > _A;
68
   void MST_kruskal(vector<int> G[], vector<int> w[])
69
70
71
     Disjoint_set set(Gsize);
72
     _A.clear();
73
     vector < pair < int , int > , int > > E;
74
     for(int i=0;i<Gsize;i++)</pre>
75
       for(int j=0;j<G[i].size();j++)</pre>
76
          if(i<G[i][j])</pre>
            E.push_back(make_pair(make_pair(i, G[i][j]), w[i][j]));
77
78
     sort(E.begin(), E.end(), cmp);
79
     for(int i=0;i<E.size();i++)</pre>
80
        if(!set.connected(E[i].first.first, E[i].first.second))
81
        {
82
          _A.push_back(make_pair(E[i].first.first, E[i].first.second));
83
          set.merge(E[i].first.first, E[i].first.second);
84
        }
85
   }
86
87
   void MST_kruskal(vector<pair<pair<int, int>, int> > E)
88
   {
89
     Disjoint_set set(Gsize);
90
     _A.clear();
91
     sort(E.begin(), E.end(), cmp);
92
     for(int i=0;i<E.size();i++)</pre>
93
        if(!set.connected(E[i].first.first, E[i].first.second))
94
95
          _A.push_back(make_pair(E[i].first.first, E[i].first.second));
96
          set.merge(E[i].first.first, E[i].first.second);
97
        }
```

```
98
99
100
    int main()
101
102
103
      return 0;
104 }
    0.1.10 Maximum-BPM
   // A C++ program to find maximal Bipartite matching.
 2 #include <iostream>
 3 #include <string.h>
 4 using namespace std;
 5
 6 #define M 6 // Size Of Graph M*N
 7 #define N 6
 8
 9 bool bpm(bool bpGraph[M][N], int u, bool seen[], int matchR[])
 10
         for (int v = 0; v < N; v++)
 11
 12
             if (bpGraph[u][v] && !seen[v])
 13
 14
 15
                 seen[v] = true; // Mark v as visited
                 if (matchR[v] < 0 || bpm(bpGraph, matchR[v], seen, matchR))</pre>
 16
 17
 18
                      matchR[v] = u;
 19
                      return true;
 20
                 }
             }
 21
 22
         }
 23
        return false;
 24 }
 25
 26
    int maxBPM(bool bpGraph[M][N])
 27
    {
 28
         int matchR[N];//List Of Matches
 29
 30
        memset(matchR, -1, sizeof(matchR));
 31
 32
        int result = 0;
         for (int u = 0; u < M; u++)
 33
 34
 35
             bool seen[N];
 36
             memset(seen, 0, sizeof(seen));
 37
             if (bpm(bpGraph, u, seen, matchR))
 38
                 result++;
 39
        }
 40
        return result;
 41
    }
 42
 43
    int main()
 44
    {
 45
         bool bpGraph[M][N] = \{ \{0, 1, 1, 0, 0, 0\}, \}
 46
                          {1, 0, 0, 1, 0, 0},
 47
                          \{0, 0, 1, 0, 0, 0\},\
                          {0, 0, 1, 1, 0, 0},
 48
                          \{0, 0, 0, 0, 0, 0\},\
 49
 50
                          {0, 0, 0, 0, 0, 1}
51
                        };
52
 53
    cout << "Maximum Maching "<< maxBPM(bpGraph);</pre>
54
55 return 0;
```

0.2 Flow

0.2.1 Max-Flow

```
// C++ program for implementation of Ford Fulkerson algorithm
2 #include <iostream>
3 #include <limits.h>
4 #include <string.h>
5 #include <queue>
6 using namespace std;
7
8
   #define V 6
9
10
   bool bfs(int rGraph[V][V], int s, int t, int parent[])
11
   {
12
       bool visited[V];
13
       memset(visited, 0, sizeof(visited));
14
       queue <int> q;
15
       q.push(s);
16
       visited[s] = true;
17
       parent[s] = -1;
18
       while (!q.empty())
19
       {
20
            int u = q.front();
21
            q.pop();
22
23
            for (int v=0; v<V; v++)
24
25
                if (visited[v] == false && rGraph[u][v] > 0)
26
                {
27
                    q.push(v);
28
                    parent[v] = u;
29
                    visited[v] = true;
30
                }
            }
31
32
       }
33
       return (visited[t] == true);
34 }
35
36 int fordFulkerson(int graph[V][V], int s, int t)
37
   {
       int u, v;
38
39
       int rGraph[V][V];
40
       for (u = 0; u < V; u++)
            for (v = 0; v < V; v++)
41
42
                 rGraph[u][v] = graph[u][v];
43
       int parent[V];
44
       int max_flow = 0;
45
       while (bfs(rGraph, s, t, parent))
46
            int path_flow = INT_MAX;
47
48
            for (v=t; v!=s; v=parent[v])
49
50
                u = parent[v];
51
                path_flow = min(path_flow, rGraph[u][v]);
52
            }
53
54
            for (v=t; v != s; v=parent[v])
55
56
                u = parent[v];
57
                rGraph[u][v] -= path_flow;
58
                rGraph[v][u] += path_flow;
59
            }
```

```
60
            max_flow += path_flow;
61
       }
62
       return max_flow;
63 }
64
65
  int main()
66
67
       int graph[V][V] = \{ \{0, 16, 13, 0, 0, 0\}, \}
                             {0, 0, 10, 12, 0, 0},
68
69
                             {0, 4, 0, 0, 14, 0},
70
                             \{0, 0, 9, 0, 0, 20\},\
71
                             \{0, 0, 0, 7, 0, 4\},\
72
                             {0, 0, 0, 0, 0, 0}
73
                           };
74
       cout << "The maximum possible flow is"
75
        << fordFulkerson(graph, 0, 5);
76
       return 0;
77 }
   0.2.2 Min-Cut
  // C++ program for finding minimum cut using Ford-Fulkerson
2 #include <iostream>
3 #include <limits.h>
4 #include <string.h>
5 #include <queue>
6 using namespace std;
8
   // Number of vertices in given graph
9
  #define V 6
10
11
  int bfs(int rGraph[V][V], int s, int t, int parent[])
12
13
       bool visited[V];
14
       memset(visited, 0, sizeof(visited));
15
16
       queue <int> q;
17
       q.push(s);
18
       visited[s] = true;
19
       parent[s] = -1;
20
21
       while (!q.empty())
22
            int u = q.front();
23
24
           q.pop();
25
26
            for (int v=0; v<V; v++)
27
            {
28
                if (visited[v] == false && rGraph[u][v] > 0)
29
                {
30
                    q.push(v);
31
                    parent[v] = u;
32
                    visited[v] = true;
33
                }
34
            }
35
       }
36
       return (visited[t] == true);
37
   }
38
39
   void dfs(int rGraph[V][V], int s, bool visited[])
40
       visited[s] = true;
41
       for (int i = 0; i < V; i++)
42
43
           if (rGraph[s][i] && !visited[i])
               dfs(rGraph, i, visited);
44
```

```
45
46
47
   void minCut(int graph[V][V], int s, int t)
48
49
       int u, v;
50
       int rGraph[V][V];
51
       for (u = 0; u < V; u++)
52
            for (v = 0; v < V; v++)
53
                 rGraph[u][v] = graph[u][v];
54
       int parent[V];
55
       while (bfs(rGraph, s, t, parent))
56
57
            int path_flow = INT_MAX;
58
            for (v=t; v!=s; v=parent[v])
59
                u = parent[v];
60
                path_flow = min(path_flow, rGraph[u][v]);
61
62
            }
63
            for (v=t; v != s; v=parent[v])
64
            {
65
                u = parent[v];
66
                rGraph[u][v] -= path_flow;
                rGraph[v][u] += path_flow;
67
68
69
       }
70
       //Finishing...
71
       bool visited[V];
72
       memset(visited, false, sizeof(visited));
73
       dfs(rGraph, s, visited);
74
       for (int i = 0; i < V; i++)
75
         for (int j = 0; j < V; j++)
76
             if (visited[i] && !visited[j] && graph[i][j])
77
                  cout << i << "u-u" << j << endl;
78
79
       return;
80
  }
81
82
   int main()
83
84
       int graph[V][V] = \{ \{0, 16, 13, 0, 0, 0\}, \}
85
                             {0, 0, 10, 12, 0, 0},
86
                             {0, 4, 0, 0, 14, 0},
87
                             {0, 0, 9, 0, 0, 20},
                             \{0, 0, 0, 7, 0, 4\},\
88
89
                             {0, 0, 0, 0, 0, 0}
90
91
92
       minCut(graph, 0, 5);
93
94
       return 0;
95 }
   0.3
         Geometry
   0.3.1 Convex-Hull
  // A C++ program to find convex hull of a set of points. Refer
2 #include <iostream>
3 #include <stack>
4 #include <stdlib.h>
5 using namespace std;
6
7
   struct Point
8 {
```

int x, y;

```
10 };
11
12
  Point p0;
13
14 Point nextToTop(stack<Point> &S)
15
       Point p = S.top();
16
17
       S.pop();
18
       Point res = S.top();
19
       S.push(p);
20
       return res;
21 }
22
23 int swap(Point &p1, Point &p2)
24
25
       Point temp = p1;
26
       p1 = p2;
27
       p2 = temp;
28
  }
29
30
  int distSq(Point p1, Point p2)
31
32
       return (p1.x - p2.x)*(p1.x - p2.x) +
33
              (p1.y - p2.y)*(p1.y - p2.y);
34
35
36
  int orientation(Point p, Point q, Point r)
37
38
       int val = (q.y - p.y) * (r.x - q.x)
39
           -(q.x - p.x) * (r.y - q.y);
40
       if (val == 0) return 0;
41
       return (val > 0)? 1: 2;
42 }
43
44
   int compare(const void *vp1, const void *vp2)
45
46
      Point *p1 = (Point *) vp1;
      Point *p2 = (Point *) vp2;
47
48
49
      int o = orientation(p0, *p1, *p2);
50
      if (o == 0)
51
        return (distSq(p0, *p2) >= distSq(p0, *p1))?
52
                     -1:1;
53
      return (o == 2)? -1: 1;
54
55 }
56
57
   void convexHull(Point points[], int n)
58
59
      int ymin = points[0].y, min = 0;
60
      for (int i = 1; i < n; i++)
61
62
        int y = points[i].y;
        if ((y < ymin) || (ymin == y &&
63
64
             points[i].x < points[min].x))</pre>
65
            ymin = points[i].y, min = i;
      }
66
67
68
      swap(points[0], points[min]);
69
70
      p0 = points[0];
      qsort(&points[1], n-1, sizeof(Point), compare);
71
72
73
      int m = 1; // Initialize size of modified array
74
      for (int i=1; i < n; i++)
```

```
75
       {
 76
           while (i < n-1 && orientation(p0, points[i], points[i+1]) == 0)
 77
 78
           points[m] = points[i];
 79
           m++;
 80
       }
 81
 82
       if (m < 3) return;
 83
 84
       stack < Point > S;
 85
       S.push(points[0]);
 86
       S.push(points[1]);
 87
       S.push(points[2]);
 88
 89
       for (int i = 3; i < m; i++)
 90
          while (orientation(nextToTop(S), S.top(), points[i]) != 2)
 91
 92
              S.pop();
 93
          S.push(points[i]);
 94
 95
 96
       while (!S.empty()) // List Of The Points In The Convex Hull
 97
 98
           Point p = S.top();
99
            cout << "(" << p.x << ", " << p.y <<")" << endl;
100
           S.pop();
101
       }
102 }
103
104 int main()
105
106
        Point points[] = {{0, 3}, {1, 1}, {2, 2}, {4, 4},
107
                          \{0, 0\}, \{1, 2\}, \{3, 1\}, \{3,3\}\};
108
        int n = sizeof(points)/sizeof(points[0]);
109
        /* N is The Number of Points And points is
        the list Of points */
110
111
        convexHull(points, n);
112
        return 0;
113 }
    0.3.2 Shoelace Formula (python)
    def PolygonArea(corners):
 2
        n = len(corners) # of corners
 3
        area = 0.0
 4
        for i in range(n):
 5
             j = (i + 1) \% n
 6
             area += corners[i][0] * corners[j][1]
 7
             area -= corners[j][0] * corners[i][1]
 8
        area = abs(area) / 2.0
 9
        return area
 10
 11
   # examples
    corners = [(2.0, 1.0), (4.0, 5.0), (7.0, 8.0)]
 12
 13 print (PolygonArea(corners))
    0.3.3
           Swap Line
 1 #include <bits/stdc++.h>
 2 #define px second
 3 #define py first
 4 typedef pair < long long, long long > pairll;
 5 pairll pnts [MAX];
 6 int compare(pairll a, pairll b)
 7 {
 8
             return a.px < b.px;
```

```
9 }
  double closest_pair(pairll pnts[],int n)
10
11
12
           sort(pnts,pnts+n,compare);
13
           double best=INF;
           set < pairll > box;
14
15
           box.insert(pnts[0]);
16
           int left = 0;
17
           for (int i=1; i < n; ++i)
18
19
                while (left<i && pnts[i].px-pnts[left].px > best)
20
                    box.erase(pnts[left++]);
21
                for(typeof(box.begin()) it=box.lower_bound(make_pair(pnts[i].py-best,
                   pnts[i].px-best));it!=box.end() && pnts[i].py+best>=it->py;it++)
                    best = min(best, sqrt(pow(pnts[i].py - it->py, 2.0)+pow(pnts[i].px -
22
                        it->px, 2.0)));
23
                box.insert(pnts[i]);
24
           }
25
           return best;
26 }
   0.3.4 Union Of Rectangles
1 #include <bits/stdc++.h>
2 #define MAX 1000
3 struct event
4 {
5
                   // Index of rectangle in rects
6
       bool type; // Type of event: 0 = Lower-left; 1 = Upper-right
7
       event(){};
       event(int ind, int type) : ind(ind), type(type){};
8
9 };
  struct point
10
11
12
       int x, y;
13
  };
14
   point rects[MAX][12];
15
   // Each rectangle consists of 2 points: [0] = lower-left; [1] = upper-right
   bool compare_x(event a, event b)
17
       return rects[a.ind][a.type].x < rects[b.ind][b.type].x;</pre>
18
19
  }
20
   bool compare_y(event a, event b)
21
22
       return rects[a.ind][a.type].y < rects[b.ind][b.type].y;</pre>
23
24
  int union_area(event events_v[], event events_h[], int n, int e)
25
26
       /*n is the number of rectangles, e=2*n , e is the number of
27
       points (each rectangle has two points as described in
28
       declaration of rects)
29
       */
       bool in_set[MAX] = {0};
30
31
       int area = 0;
32
       sort(events_v, events_v + e, compare_x);
33
       //Pre-sort of vertical edges
34
       sort(events_h, events_h + e, compare_y);
35
       // Pre-sort set of horizontal edges
36
       in_set[events_v[0].ind] = 1;
37
       for (int i = 1; i < e; ++i)
38
39
            event c = events_v[i];
40
           int cnt = 0; // Counter to indicate how many
41
           //rectangles are currently overlapping
42
            // Delta_x: Distance between current
```

```
43
            // sweep line and previous sweep line
44
            int delta_x = rects[c.ind][c.type].x - rects[events_v[i - 1].ind]\
45
            [events_v[i - 1].type].x;
46
            int begin_y;
            if (delta_x == 0)
47
48
            {
49
                 in_set[c.ind] = (c.type == 0);
50
                continue;
            }
51
52
            for (int j = 0; j < e; ++ j)
53
                if (in_set[events_h[j].ind] == 1)
54
55
                     if (events_h[j].type == 0)
56
                         if (cnt == 0)
57
58
                              begin_y = rects[events_h[j].ind][0].y;
59
                         ++cnt;
60
                     }
61
                     else
62
                     {
63
                         --cnt;
                         if (cnt == 0)
64
65
                              int delta_y = (rects[events_h[j].ind][13].y - begin_y);
66
67
                              area += delta_x * delta_y;
68
                         }
                     }
69
70
71
            in_set[c.ind] = (c.type == 0);
72
        }
73
        return area;
74 }
   0.4
          String
   0.4.1
         LCS
   /* Dynamic Programming C/C++ implementation of LCS problem */
   #include < bits / stdc ++.h>
3
4 int max(int a, int b)
5
6
        return (a > b)? a : b;
7
   }
8
9
    int lcs( char *X, char *Y, int m, int n )
10
   {
      int L[m+1][n+1];
11
12
      int i, j;
13
14
      for (i=0; i \le m; i++)
15
16
         for (j=0; j \le n; j++)
17
18
           if (i == 0 || j == 0)
19
             L[i][j] = 0;
20
21
           else if (X[i-1] == Y[j-1])
22
             L[i][j] = L[i-1][j-1] + 1;
23
24
             L[i][j] = max(L[i-1][j], L[i][j-1]);
25
26
         }
27
      }
      return L[m][n];
28
```

```
29 }
30
31
  int main()
32 {
     char X[] = "AGGTAB";
33
     char Y[] = "GXTXAYB";
34
35
36
     int m = strlen(X);
37
     int n = strlen(Y);
38
39
     printf("Length_of_LCS_is_%dn", lcs( X, Y, m, n ) );
40
41
     return 0;
42 }
   0.4.2 LIS
1 typedef vector <int> VI;
2 typedef pair < int , int > PII;
3 typedef vector <PII > VPII;
  #define STRICTLY_INCREASNG
7
   VI LongestIncreasingSubsequence(VI v) {
8
     VPII best;
9
     VI dad(v.size(), -1);
10
     for (int i = 0; i < v.size(); i++) {
11
12 #ifdef STRICTLY_INCREASNG
13
       PII item = make_pair(v[i], 0);
14
       VPII::iterator iter = lower_bound(best.begin(), best.end(), item);
15
       item.second = i;
16 #else
17
       PII item = make_pair(v[i], i);
18
       VPII::iterator iter = upper_bound(best.begin(), best.end(), item);
19
  #endif
20
       if (iter == best.end()) {
         dad[i] = (best.size() == 0 ? -1 : best.back().second);
21
22
         best.push_back(item);
23
       } else {
24
         dad[i] = dad[iter->second];
25
         *iter = item;
26
       }
27
     }
28
29
     VI ret;
30
     for (int i = best.back().second; i >= 0; i = dad[i])
31
       ret.push_back(v[i]);
32
     reverse(ret.begin(), ret.end());
33
     return ret;
34 }
   0.4.3 KMP
1 /*
2 Finds all occurrences of the pattern string p within the
3 text string t. Running time is \mathit{O(n+m)}, where n and m
  are the lengths of p and t, respectively.
5
   */
  #include <iostream>
7
8 #include <string>
9 #include <vector>
10
11
  using namespace std;
12
```

```
15
   void buildPi(string& p, VI& pi)
16
17
     pi = VI(p.length());
     int k = -2;
18
     for(int i = 0; i < p.length(); i++) {</pre>
19
20
       while (k \ge -1 \&\& p[k+1] != p[i])
         k = (k == -1) ? -2 : pi[k];
21
22
       pi[i] = ++k;
23
     }
24 }
25
26
  int KMP(string& t, string& p)
27
28
     VI pi;
     buildPi(p, pi);
29
30
     int k = -1;
31
     for(int i = 0; i < t.length(); i++) {
32
       while (k \ge -1 \&\& p[k+1] != t[i])
33
          k = (k == -1) ? -2 : pi[k];
34
       k++;
       if(k == p.length() - 1) {
35
36
          // p matches t[i-m+1, \ldots, i]
37
         cout << "matcheduatuindexu" << i-k << ":u";
38
         cout << t.substr(i-k, p.length()) << endl;</pre>
39
          k = (k == -1) ? -2 : pi[k];
40
41
     }
42
     return 0;
43
   }
44
45
   int main()
46
47
     string a = "AABAACAADAABAABA", b = "AABA";
48
     KMP(a, b); // expected matches at: 0, 9, 12
     return 0;
49
50 }
```

0.5 Other

13 typedef vector <int> VI;

14

0.5.1 Date Transformation

```
//Dates (C++)
1
2
  // Routines for performing computations on dates. In these routines,
  // months are expressed as integers from 1 to 12, days are expressed
  // as integers from 1 to 31, and years are expressed as 4-digit
  // integers.
8
  string dayOfWeek[] = {"Mo", "Tu", "We", "Th", "Fr", "Sa", "Su"};
9
10
  // converts Gregorian date to integer (Julian day number)
11
12
  int DateToInt (int m, int d, int y){
13
     return
14
       1461 * (y + 4800 + (m - 14) / 12) / 4 +
       367 * (m - 2 - (m - 14) / 12 * 12) / 12 -
       3 * ((y + 4900 + (m - 14) / 12) / 100) / 4 +
16
       d - 32075;
17
18
19
20
  // converts integer (Julian day number) to Gregorian date: month/day/year
21
22 void IntToDate (int jd, int &m, int &d, int &y) {
```

```
23
     int x, n, i, j;
24
25
     x = jd + 68569;
     n = 4 * x / 146097;
     x = (146097 * n + 3) / 4;
     i = (4000 * (x + 1)) / 1461001;
     x = 1461 * i / 4 - 31;
29
30
      = 80 * x / 2447;
     d = x - 2447 * j / 80;
31
32
     x = j / 11;
33
     m = j + 2 - 12 * x;
     y = 100 * (n - 49) + i + x;
35 }
36
37
   // converts integer (Julian day number) to day of week
38
39
  string IntToDay (int jd){
40
     return dayOfWeek[jd % 7];
41
   0.6
         Specific
   0.6.1 Max Flow:
1 #include <bits/stdc++.h>
2 using namespace std;
3 #define MAXSIZE 502
4
5 #define LL long long
7
   // s-> source, d -> sink, n = |V|, e = |E|
  int n, e, s, d, c; // s--, d--
9
10
  vector < int > graph [MAXSIZE];
  LL capacity[MAXSIZE][MAXSIZE];
   int parent[MAXSIZE];
13
14
15
   inline int bfs(vector<int>& parent) {
16
       fill(begin(parent), end(parent), -1);
17
       parent[s] = -2;
18
       queue <pair <int, LL>> q;
19
       q.emplace(s, __LONG_LONG_MAX__);
20
21
       while (!q.empty()){
22
           int cur = q.front().first;
23
           auto flow = q.front().second;
24
           q.pop();
25
26
           for (auto v: graph[cur]) {
         if (parent[v] == -1 && capacity[cur][v]) {
27
28
           parent[v] = cur;
29
           LL new_flow = min(flow, capacity[cur][v]);
30
           if (v == d) return new_flow; // done
31
           q.emplace(v, new_flow);
32
         }
33
           }
34
35
       return 0;
36 }
37
```

38 LL maxFlow(){

LL flow {0};

vector < int > parent(n);

39

40

41

```
42
     while(int new_flow = bfs(parent)) {
43
       flow += new_flow;
44
       int cur = d;
       for (int prev; cur != s; cur = prev) {
45
46
         prev = parent[cur];
         capacity[prev][cur] -= new_flow;
47
         capacity[cur][prev] += new_flow;
48
       }
49
50
51
     return flow;
52 }
```

0.6.2 MCST: Kruskal

```
1 #include <iostream >
2 #include <utility >
3 #include <algorithm >
4 using namespace std;
6 typedef pair<int, int>
7
   typedef pair<int, pair<int, int> > EDGE;
8
9
   constexpr int maxn = 1e4, maxm = 1e4;
10
11
   EDGE edge[maxm];
   int n, m, mcstSize, mcstCost, rankk[maxn], par[maxn];
12
13
14
   int ds_find(int u){
15
        if(par[u] == u) return u;
16
       return par[u] = ds_find(par[u]);
17
   }
18
   void ds_union(int u, int v){
19
20
       int uu = ds_find(u), vv = ds_find(v);
21
       if(rankk[uu] == rankk[vv]){
22
            ++rankk[uu];
23
            par[uu] = vv;
24
25
       else if(rankk[uu] < rankk[vv])</pre>
26
            par[vv] = uu;
27
        else // same height, select one at random
28
            par[uu] = vv;
29 }
30
31
   void kruskal(){
32
       generate(par, par+n, [n=0]() mutable {return n++;});
33
       sort(edge, edge+m);
34
       for(int i=0; i<m && mcstSize<n-1; i++){</pre>
35
            int u = edge[i].second.first, v = edge[i].second.second;
36
            if(ds_find(u) != ds_find(v)){
37
                ds_union(u, v);
38
                mcstCost += edge[i].first;
39
                ++mcstSize;
40
            }
       }
41
42 }
43
44
   int main()
45
   {
46
        cin >> n>> m;
47
        for(int i=0; i < m; i++){
48
            cin >> edge[i].second.first
49
                >> edge[i].second.second
50
                >> edge[i].first;
            edge[i].second.first--,edge[i].second.second--;
51
52
53
54
55
       kruskal();
56
57
       cout << mcstCost << endl;</pre>
58 }
```

0.6.3 Articulation Point

```
1 #include <bits/stdc++.h>
2 using namespace std;
3 #define MaxSize 10001
4
5 vector <int> graph[MaxSize];
6 bool visited[MaxSize];
7
  vector<int> art_point;
8 int low[MaxSize],disc[MaxSize],parent[MaxSize];
9 int timeii = 0;
10
11
   void dfs_art_point(int v) {
       int ch = 0; visited[v] = true;
12
       disc[v] = low[v] = ++timeii;
13
14
       for (auto c: graph[v]) {
15
            if (!visited[c]) {
16
                ch++;
17
                parent[c] = v;
18
                dfs_art_point(c);
19
                low[v] = min(low[c], low[v]);
20
21
                if (parent[v] == -1 && ch > 1)art_point.push_back(v);
                if (parent[v] != -1 && low[c]>=disc[v])art_point.push_back(v);
22
23
            }
24
            else if (c != parent[v])
25
                low[v] = min(low[v], disc[c]);
26
       }
27 }
28
29
   int main() {
30
       int n, m; cin >> n >> m;
31
32
       fill(parent, parent+n+2, -1);
33
       fill(disc, disc+n+2, -1);
       fill(low, low+n+2, -1);
34
35
       for (int j = 0; j < m; j++) {
36
37
            int a, b; cin >> a >> b;
38
            graph[a].push_back(b);
39
            graph[b].push_back(a);
40
41
       for (int j = 1; j \le n; j++)
42
            if (!visited[j])dfs_art_point(j);
43
       for(auto a: art_point)cout << a << "u";
44 }
```