AINT351 - Clustering

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K-Means clustering

Clustering

- Idea of clustering is to group patterns so that patterns are similar to one another within the same cluster
- Patterns are dissimilar to those in other clusters
- Need some sort of metric to determine how similar things are

Hierarchical clustering

- Breaks down the dataset into a series of nested clusters
- Single cluster at the top with all data
- N clusters at the bottom for each point
- Can be displayed as a dendrogram

K-means algorithm

- K-means as a simple clustering algorithm
- Implementing K-means is easy
- K is the number of clusters
- Often K is set by hand
- Assign the data to k clusters
- Calculate the centroids (means)
- Loop until convergence and do the following:
 - 1. For each point, put the point into the cluster whose centroid it is closest
 - 2. Recompute the cluster centroids
 - 3. Repeat loop until there is no change in clusters between two consecutive iterations

Mixture of Gaussians

limitations of simple Gaussian and PCA models

- They're a convenient way to reduce dimensionality of high dimensional data sets
- The problem is that they make very strong assumptions about the distribution of the data
 - Only the mean and variance of the data are teken into account

Mixture of models

- Clusters can overlap
- Data may exhibit non-binary strength of association to all clusters
- Probabilistic method
- Each cluster is a generative model
- Clusters have parameters (means & covarience)
- Can have different Gaussians for capturing different parts of the data sets

Recall K-means algorithm

- How is MoG implemented?
- Randomly assign Kdata points at the centroids
- Loop to find centres
- Mixture of guassians operates in an analogous fashion

EM algorithm

- Need to know the Guassian parameters (mean & variance) for each cluster to estimate data point cluster membership
- But need to know data assignments to estimate the parameters
- Solution is to use EM algorithm
- What's the value of prob that it has come from each class
- Have to compute the prob of how it came from a class

E-step:

 Look at each data point and calculate how likely it came from a given cluster

M-step:

- Re-estimate Gaussian paremeters to fit the assigned points
- Repeat until convergence achieved

NB: sensitive to starting point

- $\bullet\,$ The probability goes up when it is closer to the mean
- If it is at the tail end of a guassian curve that isn't near another, the probability becomes more certain