A Comparative Study of Generative Adversarial Networks Towards Automatic Image Colorization

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1 Introduction

Deep learning has recently shown impressive results towards various problems in multiple domains such as speech recognition, image classification, image segmentation, and reinforcement learning []. Until recently, much of the focus was towards discriminative models, which aim to map a high-dimensional input, such as an image, to a class label. Deep generative models, such as Deep Botlzmann Machines, Deep Belief Networks, and Autoencoders have not had the same level of success. Generative Adversarial Networks (GANs)[1] are a class of generative models that have shown great success in generatig realistic images. Despite their success, they are known to be very difficult to train, and are extremely sensitive to modifications. For this reason it is not yet straightforward to directly apply them towards different problems or problems of a different domain.

Since their introduction in 2014, there have been several large contributions made towards stabalizing and understanding the training process of GANs. I will be focusing on implementing and comparing four different methods used for training GANs towards the original problem of image generation. With these implemented, I apply their methods towards our goal to automatically colorize grayscale images. The four different variants of GANs I will be focusing on are the original GAN formulation [1], Least Squares GANs (LSGANs) [6], Energy-Based GANs (EBGANs) [4], and Wasserstein GAN (WGAN) [5]. The papers I will be discussing are [1,2,3,4,5,6], with additional references to others not listed here. The original GANs paper [1] provides a novel method towards generating images with the use of an adversarial loss, where both the generator and discriminator networks are multilayer perceptrons. Deep Convolutional GANs (DCGANs) [2] bridge the gap between recent advances in deep learning and GANs by introducing deep convolutional generative adversarial networks. The architechture they contribute is used in "pix2pix" [3], which approaches the problem of translating images from one domain to the other, in [4] which views the discriminator as an energy function, in [5] which proposes to minimize an approximation of the Earth Mover distance, and in [6], which adopt the least squares loss function in attepmt to overcome the vanishing gradient problem commonly seen with GANs.

2 Background and Related Work

2.1 Deep Learning

Deep learning is a class of machine learning algorithms that use one or more *hidden layers* between the input and output to learn a heirarchy of concepts, often referred to as *deep neural networks* (DNN). In a feedforward network, or multilayer perceptron (MLP), each successive layer uses the output from the previous layer as input, and uses an activation function, such as a logistic function, to obtain a new representation of the input. To learn the set of weights and biases connecting successive layers, the error is propagated backwards through the network in order to optimize a given objective function. This process is known as *backpropogation*. Backpropogation is used in conjunction with an optimization method, such as gradient descent, to effeciently compute the gradients by propogation from the output to input. This allows multi-layer networks to learn a non-linear mapping from copious amounts of data. Because of the large amount of data needed to effectively train DNNs, *stochastic gradient descent* is often used via batches of data, which amounts to computing the gradient on a mini-batch of training samples. Recent advances in GPUs have provided massive speedups in training due to

their ability to parallelize the many operations in a DNN.

2.2 Convolutional Neural Networks

The most common type of DNN for visual data is the Convolutional Neural Network (CNN), which is designed specifically for multidimensional data such as images. CNNs incorporate three powerful techniques in order to achieve some degree of scale and shift invariance. The first is the use of shared weights, which stems from the idea that a feature detector used in one part of an image is almost certainly useful in other parts of the image. This also allows networks to reduce the number of parameters to avoid the curse of dimensionality. The second is the use of local receptive fields. A kernel or filter is *convolved* across the entire image to produce a *feature map*. Each pixel in the resulting feature map is the result of the kernel convolved with a small area in the input. The use of local receptive fields allow earlier layers in the network to learn low-level features such as edges or corners, which can then be combined in successive layers throughout the network to learn high-level features. The third technique is various forms of subsampling, such as the use of pooling layers, which provide a form of nonlinear downsampling. Subsampling is performed to reduce the dimensionality of the internal representation.

While the size of the output in a MLP is independent of the size of its input, the height and width of the resulting feature maps are dependent on the size and stride of the kernel. The number of feature maps or *depth* of the resulting layer (which corresponds to the *width* of the network as a whole) however, is arbitrary. Clearly, there are many different opitions to be chosen, such as the size of the kernel, the stride of the kernel, depth of the . When designing a CNN, many rely on heuristics, as well as theorectical design principles as shown in [inception paper]. An example CNN architecture is shown in Figure 1.

2.3 Deep Generative Models

Much focus has been put on CNNs as a discriminative model, learning a function to map some input data to some desired output label. In other words, they learn the conditional distribution $P(y|x)$. The rest of this paper is focused on *generative* models, which instead learn the joint probability of the input data and labels. They attempt to model the data directly by learning $P(x, y)$. Autoencoders, Deep Boltzmann Machines, and Deep Belief Nets are some examples of these class of models. Generative models are usually based on some generator network G, that takes as input a random variable z sampled from some distribution, e.g $z \sim \mathcal{N}(0, 1)$, and outputs a sample x.

Generative models, as the name suggest, attempt to generate new data similar to existing data. Generative models have been shown to perform well on many tasks such as inpainting, image denoising, and video generation. Autoencoders have been a popular form of generative model because of their ability to approximate some distribution of observed data, such as imagery. A simple autoencoder setup may be to learn an encoding z over a set of images, $\mathcal{X}$, with z being of a much lower dimension than that of $X \in \mathcal{X}$. A training procedure for a setup such as this is as follows. An image $X \in \mathbb{R}^{m \times n}$ is encoded through an encoder CNN to some latent variable $z \in \mathbb{R}^d$, which is then used as input to a decoder CNN to produce $X' \in \mathbb{R}^{m \times n}$. A loss function, such as L_2 is then used to compare the two, and the error is propogated back through the networks. To produce a new sample, a random variable $z' \sim \mathcal{N}$ can be used as input to the generator network in place of an encoded z. An open research problem is to determine an appropriate loss function. L_2 and L_1 often result in blurry images, and may not be a correct metric for visual quality. A recent class of generative models proposes to instead use an *adversarial* loss in place of existing loss functions in the form of a network.

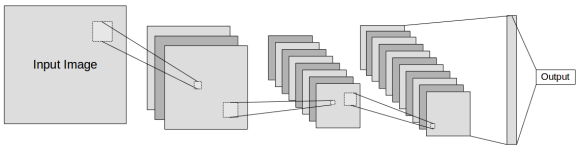

Figure 1: An example of a Convolutional Neural Network

3 Generative Adversarial Networks

Generative Adversarial Networks (GANs) [1] are a recent class of generative models that are based on a game theory scenario in which a generator network is competing against an adversary. The goal is to train a generator network to generate samples that are indistinguishable from the true data, p_{data}, by mapping a random input variable $z \sim p_z$ to some some $\boldsymbol{x}$. This mapping can be represented as $G(z; \theta_g)$, where G is a MLP with weights θ_g, and z is a random variable sampled from some distribution, e.g $z \sim \mathcal{N}(0, 1)$. The discriminator, $D(\boldsymbol{x}; \theta_d)$ is represented by a second MLP with weights θ_d, and outputs a scalar representing the probability that a sample $\boldsymbol{x}$ came from p_{data} rather than from G. The two networks are trained simultaneously, with D being trained to maximize the probability of correctly distinguishing whether or not a sample came from p_{data} or from G, and G being trained to fool D by minimizing $log(1 - D(G(z)))$. This can be represented by the following objective function:

$$\min_G \max_D \mathbb{E}_{x \sim p_{data(x)}}[logD(\boldsymbol{x})] + \mathbb{E}_{z \sim p_z(z)}[log(1 - D(G(z)))]$$

In practice however, D will be able to discriminate between real and generate samples with ease early in learning, due to the fact that generated images will clearly look very different than those from the training set upon initialization. As extensively shown in [7], as D gets better, the gradient begins to vanish. This means early in learning when D is often perfect, it provides little or no gradients to G, so G cannot improve. To help avoid this issue, G is trained to maximize $logD(G(z))$, rather than minimize $log(1 - D(G(z)))$, which is able to provide much stronger gradients. To validate the results in [1], I trained adversarial networks on the MNIST dataset. The two networks were simple MLP. Full details can be found in the appendix. Figure 2 shows some non-cherry picked samples from the model.

Conditional GANs (cGANs) introduce a simple method to condition image generation on some extra information y (e.g a class label). This is done by simply feeding y to the generator and discriminator networks. The new objective function then becomes:

$$\min_G \max_D \mathbb{E}_{x \sim p_{data(x)}}[logD(\boldsymbol{x}|y)] + \mathbb{E}_{z \sim p_z(z)}[log(1 - D(G(z|y)))]$$

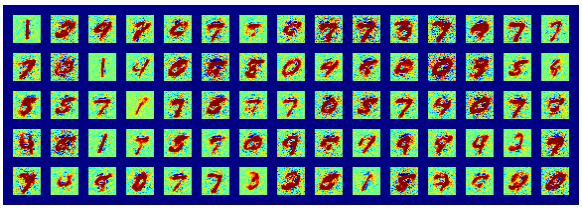

Figure 2: Results from training a GAN on MNIST after about 65 epochs.

3.1 Deep Convolutional GANs

I now turn towards Deep Convolutional GANs (DCGANs) [2], and discuss their success in bridging the gap between CNNs and GANs. Three modifications are demonstrated throughout their network architecture. The first is the replacement of downsampling layers such as max or average pooling with strided convolutions. While both perform downsampling, the all convnet architecture allows the network to learn its own downsampling, as opposed to a harsh cut such as max pooling. The second modification is the elimination of fully connected layers on top of convolutional layers, as often seen in models designed for classification. The final modification is the use of Batch Normalization [9], which normalizes the input to each node to have zero mean and unit variance. This showed to help prevent the generator from collapsing to generate a single sample. Batch normalization is *not* applied to the generator output and the discriminator input, as they resulted in model instability. As opposed to the *maxout* [10] activation used for the discriminator in [1], DCGANs use a LeakyReLU activation for all layers. As for the generator, the ReLU [11] activation is used in all layers except the output layer, which

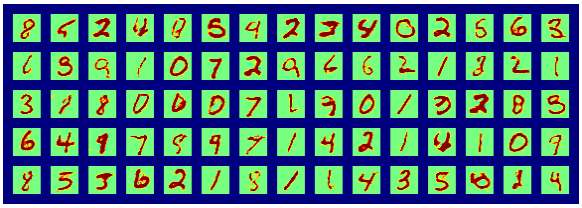

Figure 3: Results from training DCGANs on MNIST after only 3 epochs.

uses *tanh* to match with the input range of z, $[-1, 1]$.

The experiments provided show that their model acts as a very powerful generator for images in several domains. They evaluate their model on the LSUN bedrooms dataset, as well as human faces. To show the capabilities of their model beyond image generation, they successfully used it as a feature extractor for classification. Their DCGAN model was trained on Imagenet-1k [12], and the features are then used for classification on CIFAR-10 images, achieving an accuracy of 82.8%. A very impressive result is shown by modifying the latent vector z. Figure 3 shows how modifications in the latent space affect the generated images. This is further explored in [13], which combines cGANs with an autoencoder to control the attributes contained in generated images in a more explicit manner. To compare with the results I obtained from [1], I trained a DCGAN on MNIST. Results can be seen in Figure 3, and cleary contain much less noise [1].

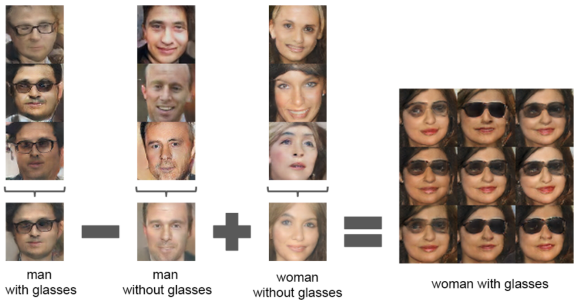

Figure 4: Modifications to the latent vectors z. For each column, the z vector used to generate the samples are averaged to produce the bottom image. Vector arithmetic is then performed to produce a z that is used to generate the center image on the right. The extra images are the results of small modifications made to z in the form of noise. This image comes directly from [2].

3.2 Least Squares GANs

Least Squares GANs (LSGANs) attempt to overcome the problem of the vanishing gradient seen in the original GAN formulation by using the least squares loss function for the discriminator. This is motivated by the idea that because [1] uses a cross entropy loss function for the discriminator, it is possible that generated samples on the correct side of the decision boundry may still be far from the true data. The least squares loss is able to penalize samples that lie far from the decision boundry, and pull fake samples towards the true data. The objective function for D and G are defined as:

$$\min_D \frac{1}{2}\mathbb{E}_{x\sim p_{data(x)}}[(D(\boldsymbol{x}) - b)^2] + \frac{1}{2}\mathbb{E}_{z\sim p_z(z)}[(D(G(z)) - a)^2]$$

$$\min_G \frac{1}{2}\mathbb{E}_{x\sim p_{data(x)}}[(D(G(\boldsymbol{x})) - c)^2]$$

[1] Code for GAN and DCGAN results can be found at https://github.com/cameronfabbri/DCGANs-Tensorflow

where $a = 0$ to denote the fake data, $b = 1$ to denote the true data, and $c = 1$ in order to try and fool D. The authors note that other values may be used, such as setting $c = b$ in order to push G to generate samples as real as possible, or by setting $b - c = 1$ and $b - a = 2$ to minimize the Pearson $\mathcal{X}^2$ divergence between $p_{data} + p_g$ and $2p_g$, as opposed to minimizing the Jensen-Shannon divergence (JSD) as seen in the original GAN formulation. In practice however, all show similar performance.

Their experiments show sharp images generated at size 128×128, as opposed to the 64×64 images generated in [2]. Despite doubling the resolution, the images are much clearer. Evaluations were done on multiple classes from the LSUN dataset. The architecture for both the discriminator and generator are very similar to those used in DCGANs. Layers were added to account for the difference in resolution. I trained LSGANs on the churches class of LSUN. Results can be seen in Figure 5. [2] One important thing to note is the extreme diversity seen in the results, showing that LSGANs are able to avoid mode collapse for the generator.

Figure 5: Results from training LSGANs on churches from the LSUN dataset.

3.3 Energy-Based GANs

3.4 Wasserstein GANs

4 Colorization

We now show how adversarial networks can be used for generating a plausible color version of a grayscale image. The problem is set up as a cGAN, where the generator and descriminator are both conditioned on the grayscale image.

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[2] More results on other LSUN classes and code can be found at https://github.com/cameronfabbri/LSGANs-Tensorflow

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A Appendix

Here we show