Statistical Pattern Recognition
Assignment 2

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Abstract

In this assignment, we'll be focusing on the *Bayes Classifier*. We'll work with *Bayesian Discriminators* and *Bayes Error*. The *Bhattacharyya* error bound is also analyzed as an upper bound for the *Bayes Classifier* error. The detailed computations of *Bayesian Discriminators* are also given in an exact definition. Finally, we'll be going through a more practical example of a linear discriminator by classifying the flowers in the *Iris* dataset.

Keywords. *Linear Discriminator, Quadratic Discriminator, Bayes Classification, Bayes Error, Optimal Classification, Bhattacharyya Distance, Bhattacharyya Upper Bound, Iris Dataset, Iris Classification.*

1 Quadratic & Linear Discriminant Analysis

We consider a classification problem in dimension $d = 2$, with $k = 3$ classes where:

$$p(x \mid w_i) \sim N(\mu_i, \Sigma_i), \quad i = 1, 2, 3$$

and

$$\mu_1 = \begin{bmatrix} 0 \\ 2 \end{bmatrix}, \ \mu_2 = \begin{bmatrix} 3 \\ 1 \end{bmatrix}, \ \mu_3 = \begin{bmatrix} 1 \\ 0 \end{bmatrix}, \Sigma_i = \Sigma \begin{bmatrix} 1 & 0 \\ 0 & \frac{1}{3} \end{bmatrix},$$

(a) Calculate the discriminant function $g_i(x)$ for each class.

(b) Express your discriminant functions in the form of linear discriminant functions.

(c) Determine and plot the decision boundaries.

Solution

(a) The general form of a Bayesian discriminator is given in .

$$g_i(\underline{x}) = \tag{1.1}$$