

Module - getLocalTopology

import mesh

```
In[185]:= DumpGet["C:\\Users\\aliha\\Desktop\\wolfram-vertex-3D\\PREVIOUS  
CODE - slow heuns\\meshGen_noise.mx"];
```

```
In[186]:= yLim[[1]] = 0.;  
edges = SetPrecision[edges, 10];  
faceListCoords = SetPrecision[faceListCoords, 10];  
(*convert faceListCoords into an association*)  
indToPtsAssoc = SetPrecision[indToPtsAssoc, 10];  
ptsToIndAssoc = KeyMap[SetPrecision[#, 10] &, ptsToIndAssoc];  
xLim = SetPrecision[xLim, 10];  
yLim = SetPrecision[yLim, 10];  
faceListCoords = Map[Lookup[indToPtsAssoc, #] &, cellVertexGrouping, {2}];
```

In[194]:=

```

Clear@periodicRules;
With[{xlim1 = xLim[[1]], xlim2 = xLim[[2]], ylim1 = yLim[[1]], ylim2 = yLim[[2]]},
  periodicRules = Dispatch[{
    (*bottom right half*)
    {x_ /; x ≥ xlim2, y_ /; y ≤ ylim1, z_} ⇒ SetPrecision[{x - xlim2, y + ylim2, z}, 10],
    (*right*)
    {x_ /; x ≥ xlim2, y_ /; ylim1 < y < ylim2, z_} ⇒ SetPrecision[{x - xlim2, y, z}, 10],
    (*bottom*)
    {x_ /; xlim1 < x < xlim2, y_ /; y ≤ ylim1, z_} ⇒ SetPrecision[{x, y + ylim2, z}, 10],
    (*bottom left half*)
    {x_ /; x ≤ xlim1, y_ /; y ≤ ylim1, z_} ⇒ SetPrecision[{x + xlim2, y + ylim2, z}, 10],
    (*left half*)
    {x_ /; x ≤ xlim1, y_ /; ylim1 < y < ylim2, z_} ⇒ SetPrecision[{x + xlim2, y, z}, 10],
    (*top-left half*)
    {x_ /; x ≤ xlim1, y_ /; y ≥ ylim2, z_} ⇒ SetPrecision[{x + xlim2, y - ylim2, z}, 10],
    (*top*)
    {x_ /; xlim1 < x < xlim2, y_ /; y ≥ ylim2, z_} ⇒ SetPrecision[{x, y - ylim2, z}, 10],
    (*top-right*)
    {x_ /; x ≥ xlim2, y_ /; y ≥ ylim2, z_} ⇒ SetPrecision[{x - xlim2, y - ylim2, z}, 10]
  }];

transformRules = Dispatch[{
  {x_ /; x ≥ xlim2, y_ /; y ≤ ylim1, _} ⇒ SetPrecision[{-xlim2, ylim2, 0}, 10],
  {x_ /; x ≥ xlim2, y_ /; ylim1 < y < ylim2, _} ⇒ SetPrecision[{-xlim2, 0, 0}, 10],
  {x_ /; xlim1 < x < xlim2, y_ /; y ≤ ylim1, _} ⇒ SetPrecision[{0, ylim2, 0}, 10],
  {x_ /; x ≤ xlim1, y_ /; y ≤ ylim1, _} ⇒ SetPrecision[{xlim2, ylim2, 0}, 10],
  {x_ /; x ≤ xlim1, y_ /; ylim1 < y < ylim2, _} ⇒ SetPrecision[{xlim2, 0, 0}, 10],
  {x_ /; x ≤ xlim1, y_ /; y ≥ ylim2, _} ⇒ SetPrecision[{xlim2, -ylim2, 0}, 10],
  {x_ /; xlim1 < x < xlim2, y_ /; y ≥ ylim2, _} ⇒ SetPrecision[{0, -ylim2, 0}, 10],
  {x_ /; x ≥ xlim2, y_ /; y ≥ ylim2, _} ⇒ SetPrecision[{-xlim2, -ylim2, 0}, 10],
  {___Real} ⇒ SetPrecision[{0, 0, 0}, 10]
}];
];

```

In[196]:=

```

(*
origcellOrient=<|MapIndexed[First[#2]→#1&, faceListCoords]|>;
boundaryCells=
  With[{ylim1=yLim[[1]],ylim2=yLim[[2]],xlim1=xLim[[1]],xlim2=xLim[[2]]},
    Union[First/@Position[origcellOrient,
      {x_ /; x ≥ xlim2, __} | {x_ /; x ≤ xlim1, __} | {_, y_ /; y ≥ ylim2, __} | {_, y_ /; y ≤ ylim1, __}] /.
      Key[x_] ⇒ x]
  ];
*)
wrappedMat = AssociationThread[
  Keys[cellVertexGrouping] → Map[Lookup[indToPtsAssoc, #] /. periodicRules &,
    Lookup[cellVertexGrouping, Keys[cellVertexGrouping]], {2}]]];

```

Miscellaneous F[x]

In[197]:=

```

triangulateFaces[faces_] := Block[{edgelen, ls, mean},
  (ls = Partition[#, 2, 1, 1];
   edgelen = Norm[SetPrecision[First[#] - Last[#], 10]] & /@ ls;
   mean = Total[edgelen * (Midpoint /@ ls)] / Total[edgelen];
   mean = mean ~ SetPrecision ~ 10;
   Map[Append[#, mean] &, ls]) & /@ faces
];

```

In[218]:=

```

Clear@outerCellsFn;
outerCellsFn::Information = "the function finds the cells at the boundary";
outerCellsFn[faceListCoords_, vertexToCell_, ptsToIndAssoc_] :=
  With[{xlim1 = xLim[[1]], xlim2 = xLim[[2]], ylim1 = yLim[[1]], ylim2 = yLim[[2]]},
    Block[{boundaryCells, bcells, temp, res},
      temp = <|MapIndexed[First[#2] → #1 &, faceListCoords]|>;
      boundaryCells = Union[First /@ Position[temp,
        {x_ /; x ≥ xlim2, __} | {x_ /; x ≤ xlim1, __} |
        {_, y_ /; y ≥ ylim2, __} | {_, y_ /; y ≤ ylim1, __}] /. Key[x_] → x];
      bcells = KeyTake[faceListCoords, boundaryCells];
      res = Union@{Flatten@Lookup[vertexToCell,
        Lookup[ptsToIndAssoc,
          DeleteDuplicates@Cases[bcells,
            {x_ /; x ≥ xlim2, __} | {x_ /; x ≤ xlim1,
              __} | {_, y_ /; y ≥ ylim2, __} | {_, y_ /; y ≤ ylim1, __}, {3}]
          /. periodicRules
        ]
      ] ~Join~ boundaryCells};
      res
    ]
];

```

In[207]:=

```

Clear@boundaryPtsPairing;
boundaryPtsPairing::Information =
  "the function pairs the points at the boundaries with corresponding mirror points";
boundaryPtsPairing[vertexToCell_, indToPtsAssoc_, ptsToIndAssoc_] :=
  Block[{outerpts, mirrorpairs, pt, mirror},
    outerpts = Keys@Select[vertexToCell, Length[#] ≠ 3 &];
    mirrorpairs = <|
      (pt = Lookup[indToPtsAssoc, #];
      If[
        pt[[1]] ≤ xLim[[1]] ||
        pt[[1]] ≥ xLim[[2]] || pt[[2]] ≤ yLim[[1]] || pt[[2]] ≥ yLim[[2]],
        mirror = ptsToIndAssoc[pt /. periodicRules];
        # → mirror,
        Nothing]) & /@ outerpts
    |> // KeySort;
    Map[Sort@*Flatten][List @@@ Normal@GroupBy[Normal@mirrorpairs, Last → First]]
  ];

```

getLocalTopology

In[212]:=

```

D = Rectangle[{First@xLim, First@yLim}, {Last@xLim, Last@yLim}];
getLocalTopology[ptsToIndAssoc_, indToPtsAssoc_, vertexToCell_,
  cellVertexGrouping_, wrappedMat_, facelistCoords_] :=
  Block[{localtopology = <|>, wrappedcelllist = {}, vertcellconns,
    localcellunion, v, wrappedcellpos, vertcs = vertices, r11, r12,
    transVector, wrappedcellCoords, wrappedcells, vertOutOfBounds,
    shiftedPt, transvecList = {}, $faceListCoords = Values@facelistCoords,
    vertexQ, boundsCheck, rules, extractcellkeys, vertind,
    cellsconnected, wrappedcellsrem},
    vertexQ = MatchQ[vertices, {__?NumberQ}];
    If[vertexQ,
      (vertcellconns =
        AssociationThread[{#}, {vertexToCell[ptsToIndAssoc[#]]}] &@vertices;
        vertcs = {vertices};
        localcellunion = Flatten[Values@vertcellconns]),
      (vertcellconns = AssociationThread[#,
        Lookup[vertexToCell, Lookup[ptsToIndAssoc, #]]] &@vertices;
        localcellunion = Union@Flatten[Values@vertcellconns])
    ];

    If[localcellunion ≠ {},
      AppendTo[localtopology,
        Thread[localcellunion →
          Map[Lookup[indToPtsAssoc, #] &, cellVertexGrouping /@ localcellunion, {2}]]
      ]
    ];

```

```

(* condition to be an internal edge: both vertices should have 3 neighbours *)
(* if a vertex has 3 cells in its local neighbourhood then the entire
network topology about the vertex is known → no wrapping required *)
(* else we need to wrap around the vertex because other cells
are connected to it → periodic boundary conditions *)
With[{vert = #},
  vertind = ptsToIndAssoc[vert];
  cellsconnected = vertexToCell[vertind];
  If[Length[cellsconnected] ≠ 3,
    If[(D~RegionMember~Most[vert]),
      (*Print["vertex inside bounds"];*)
      v = vert;
      With[{x = v[[1]], y = v[[2]]}, boundsCheck =
        (x == xLim[[1]] || x == xLim[[2]] || y == yLim[[1]] || y == yLim[[2]])];

      extractcellkeys = If[boundsCheck,
        {r11, r12} = {v, v /. periodicRules};
        rules = Block[{x$},
          With[{r = r11, s = r12},
            DeleteDuplicates[HoldPattern[SameQ[x$, r]] || HoldPattern[SameQ[x$, s]]]
          ]
        ];
        Position@@With[{rule = rules},
          Hold[wrappedMat, x_ /; ReleaseHold@rule, {3}]
        ],
        Position[wrappedMat, x_ /; SameQ[x, v], {3}]
      ];
      (* find cell indices that are attached to the vertex in wrappedMat *)
      wrappedcellpos = DeleteDuplicatesBy[
        Cases[extractcellkeys,
          {Key[p : Except[Alternatives@@
            Join[localcellunion, Flatten@wrappedcellList]], y__} :> {p, y}},
          First];
      (*wrappedcellpos = wrappedcellpos/.
        {Alternatives@@Flatten[wrappedcellList],__} :> Sequence[];*)
      (* if a wrapped cell has not been considered earlier (i.e. is new)
      then we translate it to the position of the vertex *)
      If[wrappedcellpos ≠ {},
        If[vertexQ,
          transVector = SetPrecision[(v - Extract[$faceListCoords,
            Replace[#, {p_, q__} :> {Key[p], q}, {1}]]] & /@wrappedcellpos, 10],
          (* call to function is enquiring an edge and not a vertex*)
          transVector =
            SetPrecision[(v - Extract[$faceListCoords, #]) & /@wrappedcellpos, 10]
        ];
        wrappedcellCoords = MapThread[#1 → Map[Function[x,
          SetPrecision[x + #2, 10]], $faceListCoords[[#1]], {2}] &,
          {First /@ wrappedcellpos, transVector}];
        wrappedcells = Keys@wrappedcellCoords;
        AppendTo[wrappedcellList, Flatten@wrappedcells];

```

```

AppendTo[transvecList, transVector];
AppendTo[localtopology, wrappedcellCoords];
],
(* the else clause: vertex is out of bounds *)
(*Print["vertex out of bounds"];*)
vertOutofBounds = vert;
(* translate the vertex back into mesh *)
transVector = vertOutofBounds /. transformRules;
shiftedPt = SetPrecision[vertOutofBounds + transVector, 10];
(* ----- CORE B ----- *)
(* find which cells the
shifted vertex is a part of in the wrapped matrix *)
wrappedcells = Complement[
  Union@Cases[Position[wrappedMat, x_ /; SameQ[x, shiftedPt], {3}],
    x_Key -> Sequence@@x, {2}] /.
  Alternatives@@localcellunion -> Sequence[],
  Flatten@wrappedcellList];

(*forming local topology now that we know the wrapped cells *)
If[wrappedcells != {},
AppendTo[wrappedcellList, Flatten@wrappedcells];
wrappedcellCoords = AssociationThread[wrappedcells,
  Map[Lookup[indToPtsAssoc, #] &,
    cellVertexGrouping[#] & /@ wrappedcells, {2}]];
With[{opt = (vertOutofBounds /. periodicRules)},
Block[{pos, vertref, transvec},
Do[
  With[{cellcoords = wrappedcellCoords[cell]},
    pos = FirstPosition[cellcoords /. periodicRules, opt];
    vertref = Extract[cellcoords, pos];
    transvec = SetPrecision[vertOutofBounds - vertref, 10];
    AppendTo[transvecList, transvec];
    AppendTo[localtopology,
      cell -> Map[SetPrecision[# + transvec, 10] &, cellcoords, {2}]]];
], {cell, wrappedcells}]
];
];
(* to detect wrapped cells not detected by CORE B*)
(* ----- CORE C ----- *)
Block[{pos, celllocs, ls, transvec, assoc, tvecLs = {}, ckey},
ls = Union@Flatten@Join[cellsconnected, wrappedcells];
If[Length[ls] != 3,
pos = Position[faceListCoords, x_ /; SameQ[x, shiftedPt], {3}];
celllocs = DeleteDuplicatesBy[Cases[pos, Except[{Key[Alternatives@@ls],
  __}]], First] /. {Key[x_], z__} -> {Key[x], {z}}];
If[celllocs != {},
celllocs = Transpose@celllocs;
assoc = <|
  MapThread[

```

```

      (transvec = SetPrecision[
        vertOutOfBounds - Extract[faceListCoords[Sequence @@ #1], #2], 10];
      ckey = Identity @@ #1;
      AppendTo[tvecList, transvec];
      ckey → Map[SetPrecision[Lookup[indToPtsAssoc, #] + transvec, 10] &,
        cellVertexGrouping[Sequence @@ #1], {2}]
      ) &, celllocs]
    |>;
    AppendTo[localtopology, assoc];
    AppendTo[wrappedcellList, Keys@assoc];
    AppendTo[transvecList, tvecList];
  ];
];
];
];
];
] & /@ vertcs;

transvecList = Which[
  MatchQ[transvecList, {{{__?NumberQ}}}], First[transvecList],
  MatchQ[transvecList, {{__?NumberQ} ..}], transvecList,
  True, transvecList /. {x___, {p : {__?NumberQ} ..}, y___} => {x, p, y}
];
{localtopology, Flatten@wrappedcellList, transvecList}
];

```

In[]:= (* to fasten speed of pattern matching we
only extract the outermost cells for the wrappedMat *)

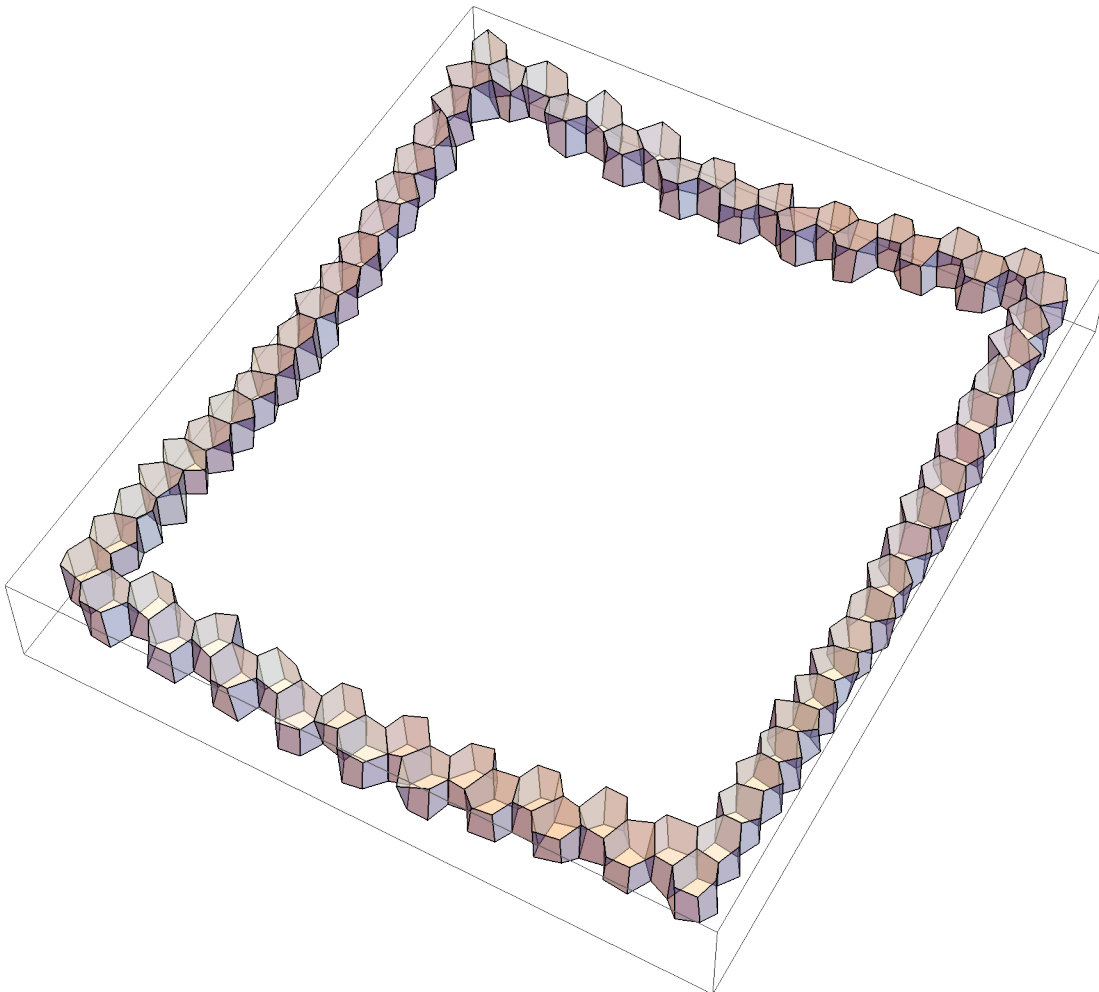
In[221]:= boundarycells = outerCellsFn[faceListCoords, vertexToCell, ptsToIndAssoc]

Out[221]= {1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 40, 41, 60, 61,
80, 81, 100, 101, 120, 121, 140, 141, 160, 161, 180, 181, 200, 201, 220, 221, 240,
241, 260, 261, 280, 281, 300, 301, 320, 321, 340, 341, 360, 361, 380, 381, 382, 383,
384, 385, 386, 387, 388, 389, 390, 391, 392, 393, 394, 395, 396, 397, 398, 399, 400}

In[222]:= wrappedMatSel = wrappedMat ~ KeyTake ~ boundarycells;

```
In[223]:= plt = Graphics3D[{Opacity[0.5], White, Polyhedron /@ Map[Lookup[indToPtsAssoc, #] &,
    Lookup[cellVertexGrouping, boundarycells], {2}]}], ImageSize -> Large]
```

Out[223]=



```
In[ ]:= (* neighbour-count for vertex *)
```

```
In[224]:= Keys[getLocalTopology[ptsToIndAssoc, indToPtsAssoc, vertexToCell, cellVertexGrouping,
    wrappedMatSel, faceListCoords][indToPtsAssoc[#]] // First] & /@
    Range[Max@ptsToIndAssoc] // Counts@*Map[Length] // AbsoluteTiming
```

Out[224]= {1.14413, <| 3 -> 1760 |>}

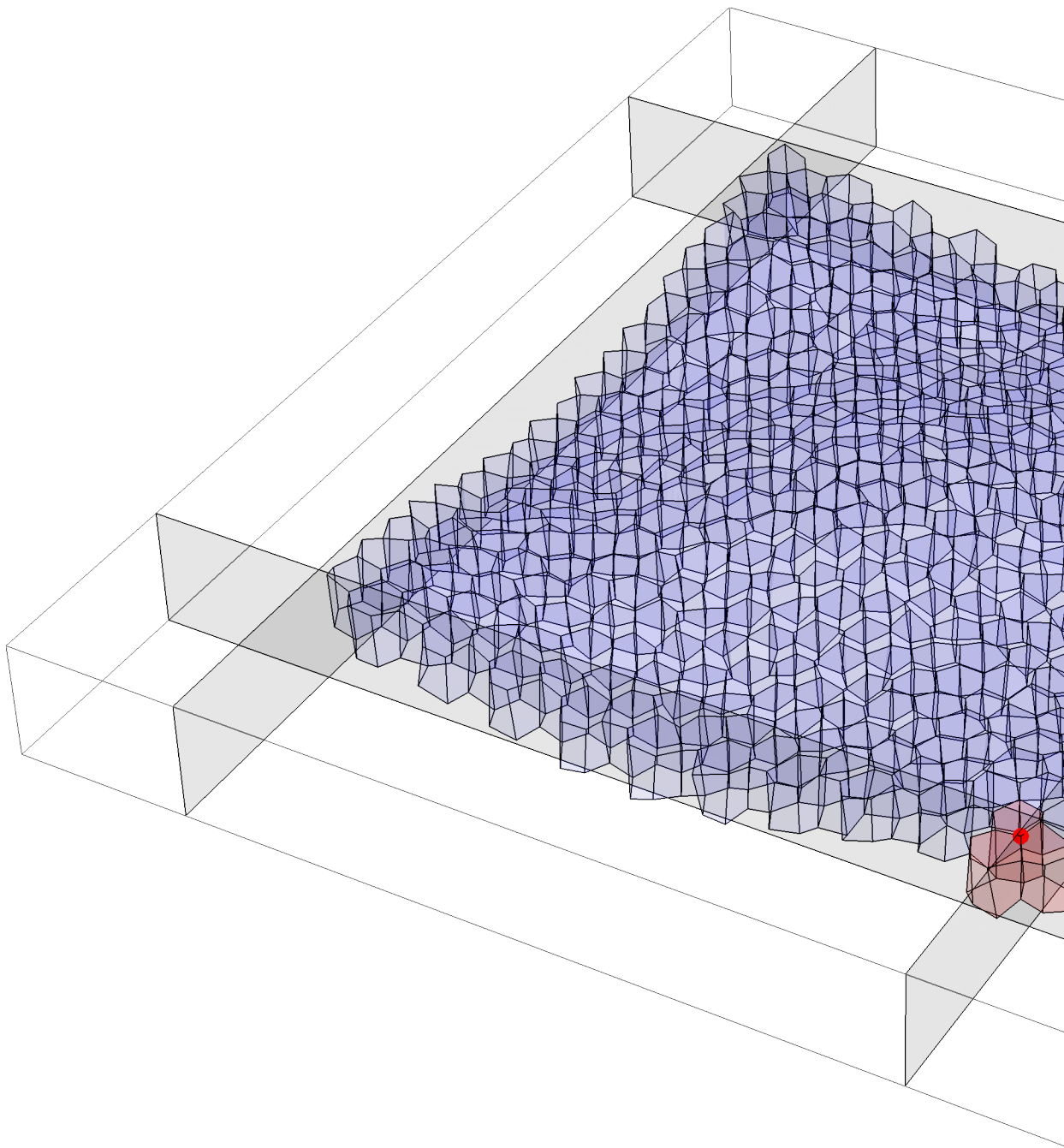
```
In[ ]:= (* neighbour-count for vertex is slow if slightly slower if we use wrappedMat *)
```

```
In[225]:= Keys[getLocalTopology[ptsToIndAssoc, indToPtsAssoc, vertexToCell, cellVertexGrouping,
    wrappedMat, faceListCoords][indToPtsAssoc[#]] // First] & /@
    Range[Max@ptsToIndAssoc] // Counts@*Map[Length] // AbsoluteTiming
```

Out[225]= {3.38817, <| 3 -> 1760 |>}

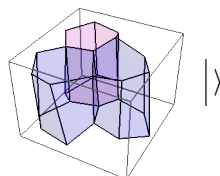
selected vertex

```
In[226]:= Block[{xx, yy, zz, edgelen, edgesel, keys, dset, id = 1680, point},
  point = indToPtsAssoc[id];
  {xx, yy, zz} = getLocalTopology[ptsToIndAssoc, indToPtsAssoc, vertexToCell,
    cellVertexGrouping, wrappedMatSel, faceListCoords][indToPtsAssoc[id]];
  keys = Keys@xx;
  Print@Graphics3D[
    {{Opacity[0.05], Blue, Polyhedron /@ Values@faceListCoords}, Red, PointSize[0.01],
      Point@point, Opacity[0.1], Red, Polyhedron /@ Values@xx},
    Black, InfinitePlane[{{0, 0, 0}, {0, xLim[[2]], 0}, {0, xLim[[2]], 1}}],
    InfinitePlane[
      {{0, yLim[[2]], 0}, {xLim[[2]], yLim[[2]], 0}, {xLim[[2]], yLim[[2]], 1}}],
    InfinitePlane[{{xLim[[2]], yLim[[2]], 0}, {xLim[[2]], yLim[[2]], 1},
      {xLim[[2]], yLim[[1]], 1}}],
    InfinitePlane[{{xLim[[2]], yLim[[1]], 0}, {xLim[[2]], yLim[[1]], 1},
      {0, yLim[[1]], 1}}]],
    ImageSize → 1024];
<|{"vertex" → id,
  "vertices in topology" → Length@DeleteDuplicates@Flatten[Values@xx, 2],
  "cell indices" → keys,
  "translated cell indices" → yy, (*"transvec"→zz,*)
  "localtopology" →
    Graphics3D[{Opacity[0.1], RandomColor[], Polyhedron /@ Lookup[xx, keys],
      Blue, If[yy ≠ {}, Polyhedron /@ Lookup[xx, yy]]}, ImageSize → Tiny]}|>
]
```



Out[226]= $\langle \left| \text{vertex} \rightarrow 1680, \text{vertices in topology} \rightarrow 26, \text{cell indices} \rightarrow \{381, 20, 400\}, \right.$

translated cell indices $\rightarrow \{20, 400\}$, localtopology \rightarrow



\rangle

vertex to cell topology

```

In[ ]:= Manipulate[
  Graphics3D[{{Opacity[0.1], Blue, EdgeForm[{Opacity[0.5], Black}]},
    Values@Map[Polyhedron@* (Flatten[#, 1] &) @* triangulateFaces,
      First@getLocalTopology[ptsToIndAssoc, indToPtsAssoc, vertexToCell,
        cellVertexGrouping, wrappedMatSel, faceListCoords][indToPtsAssoc[i]]]},
    {Red, PointSize[0.04], Point@indToPtsAssoc[i]}}, ImageSize -> Small],
  {i, 1, Max[ptsToIndAssoc], 1}, SaveDefinitions -> True
]

```

Out[]:=



```

In[ ]:= (* checking boundary pt pairing *)

```

```

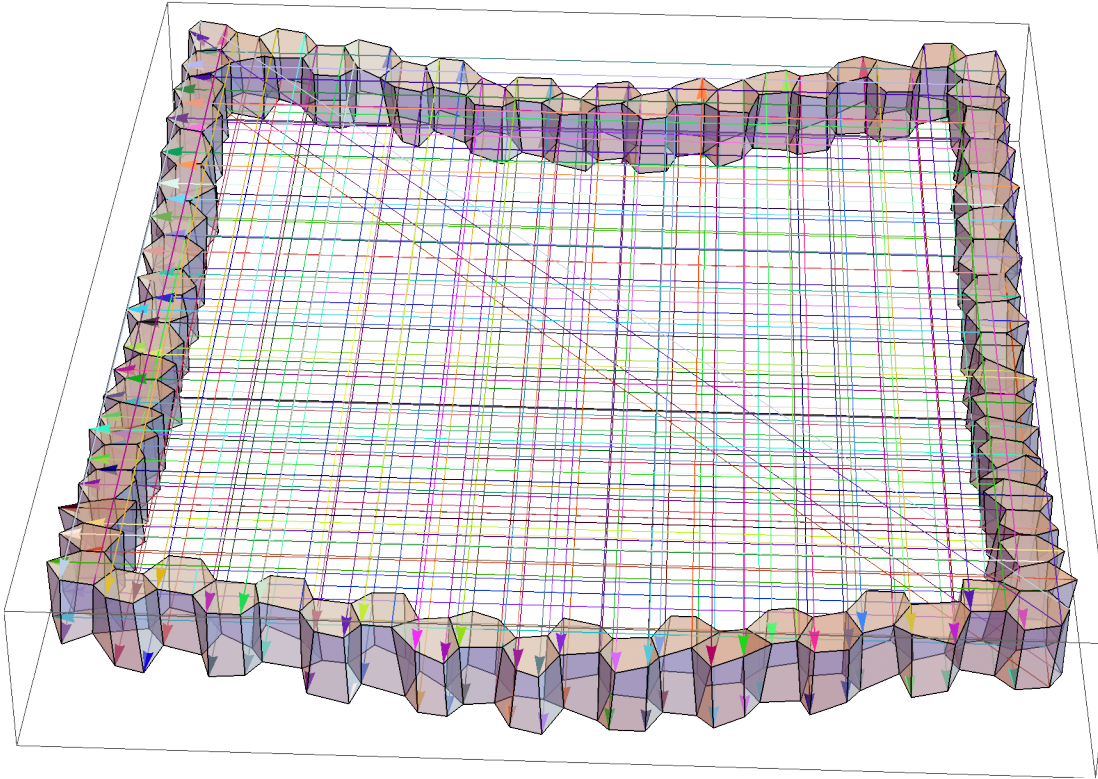
In[227]:= {timing, arrows} =
  boundaryPtsPairing[vertexToCell, indToPtsAssoc, ptsToIndAssoc] // AbsoluteTiming

Out[227]:= {0.0085701, {{4, 1678}, {6, 158}, {10, 1682}, {11, 163, 1681}, {12, 162}, {16, 1686},
  {32, 1694}, {40, 1698}, {52, 1704}, {56, 1706}, {72, 1714}, {84, 1720}, {88, 1722},
  {108, 1732}, {116, 1736}, {120, 1738}, {128, 1742}, {132, 1744}, {136, 1746},
  {140, 1748}, {144, 1750}, {152, 1754}, {5, 159, 1677}, {157, 167}, {168, 246},
  {169, 332}, {161, 171}, {172, 248}, {251, 328}, {165, 329}, {254, 331}, {327, 335},
  {336, 414}, {337, 500}, {330, 339}, {340, 416}, {419, 496}, {422, 499}, {333, 497},
  {495, 503}, {504, 582}, {498, 507}, {508, 584}, {587, 664}, {501, 665}, {590, 667},
  {505, 668}, {669, 833}, {663, 671}, {672, 750}, {666, 675}, {676, 752}, {755, 832},
  {758, 835}, {673, 836}, {831, 839}, {840, 918}, {834, 843}, {844, 920}, {923, 1000},
  {837, 1001}, {926, 1003}, {841, 1004}, {999, 1007}, {1008, 1086}, {1002, 1011},
  {1012, 1088}, {1091, 1168}, {1005, 1169}, {1094, 1171}, {1009, 1172}, {1173, 1337},
  {1167, 1175}, {1176, 1254}, {1177, 1340}, {1170, 1179}, {1180, 1256}, {1259, 1336},
  {1262, 1339}, {1341, 1505}, {1335, 1343}, {1344, 1422}, {1345, 1508}, {1338, 1347},
  {1348, 1424}, {1427, 1504}, {1430, 1507}, {1509, 1673}, {1503, 1511}, {1512, 1590},
  {1506, 1515}, {1516, 1592}, {1595, 1672}, {1598, 1675}, {1513, 1676}, {1671, 1679},
  {160, 1680, 1758}, {1674, 1683}, {164, 1684, 1760}, {3, 1685}, {9, 1687}, {20, 1688},
  {15, 1689}, {24, 1690}, {19, 1691}, {28, 1692}, {23, 1693}, {27, 1695}, {36, 1696},
  {31, 1697}, {35, 1699}, {44, 1700}, {39, 1701}, {48, 1702}, {43, 1703}, {47, 1705},
  {51, 1707}, {60, 1708}, {55, 1709}, {64, 1710}, {59, 1711}, {68, 1712}, {63, 1713},
  {67, 1715}, {76, 1716}, {71, 1717}, {80, 1718}, {75, 1719}, {79, 1721}, {83, 1723},
  {92, 1724}, {87, 1725}, {96, 1726}, {91, 1727}, {100, 1728}, {95, 1729}, {104, 1730},
  {99, 1731}, {103, 1733}, {112, 1734}, {107, 1735}, {111, 1737}, {115, 1739}, {124, 1740},
  {119, 1741}, {123, 1743}, {127, 1745}, {131, 1747}, {135, 1749}, {139, 1751},
  {148, 1752}, {143, 1753}, {147, 1755}, {156, 1756}, {151, 1757}, {155, 1759}}}

```

```
In[229]:= Show[plt, Graphics3D[{Arrowheads[Medium],
  Map[{RandomColor[], Arrow@Lookup[indToPtsAssoc, #]} &, arrows]}], ImageSize → Large]]
```

Out[229]=



checks

```
In[266]:= indToPtsAssocC = indToPtsAssoc;
```

```
In[267]:= indToPtsAssocC[328] = {2.02500000000000035527136788005009293556`10.,
  15.6500000000000003553`10., 0.28026929672068318089017679994867648929`10.};
indToPtsAssocC[329] = {1.57500000000000017763568394002504646778`10.,
  15.6500000000000003553`10., 0.359669334024670883653840292026870884`10.};
indToPtsAssocC[331] = {2.02500000000000035527136788005009293556`10.,
  15.6500000000000003553`10., -0.71973070327931676359867196879349648952`10.};
indToPtsAssocC[332] = {1.57500000000000017763568394002504646778`10.,
  15.6500000000000003553`10., -0.64033066597532917185731093923095613718`10.};
indToPtsAssocC[165] = {1.57500000000000017763568394002504646778`10.,
  0, 0.359669334024670883653840292026870884`10.};
indToPtsAssocC[169] = {1.57500000000000017763568394002504646778`10.,
  0, -0.64033066597532917185731093923095613718`10.};
indToPtsAssocC[251] = {2.02500000000000035527136788005009293556`10.,
  0, 0.28026929672068318089017679994867648929`10.};
indToPtsAssocC[254] = {2.02500000000000035527136788005009293556`10.,
  0, -0.71973070327931676359867196879349648952`10.};
```

```

In[275]:= wrappedMatC = AssociationThread[
    Keys[cellVertexGrouping] → Map[Lookup[indToPtsAssocC, #] /. periodicRules &,
    Lookup[cellVertexGrouping, Keys[cellVertexGrouping]], {2}]];

In[276]:= faceListCoordsC = Map[Lookup[indToPtsAssocC, #] &, cellVertexGrouping, {2}];

In[277]:= ptsToIndAssocC = AssociationMap[Reverse, indToPtsAssocC];

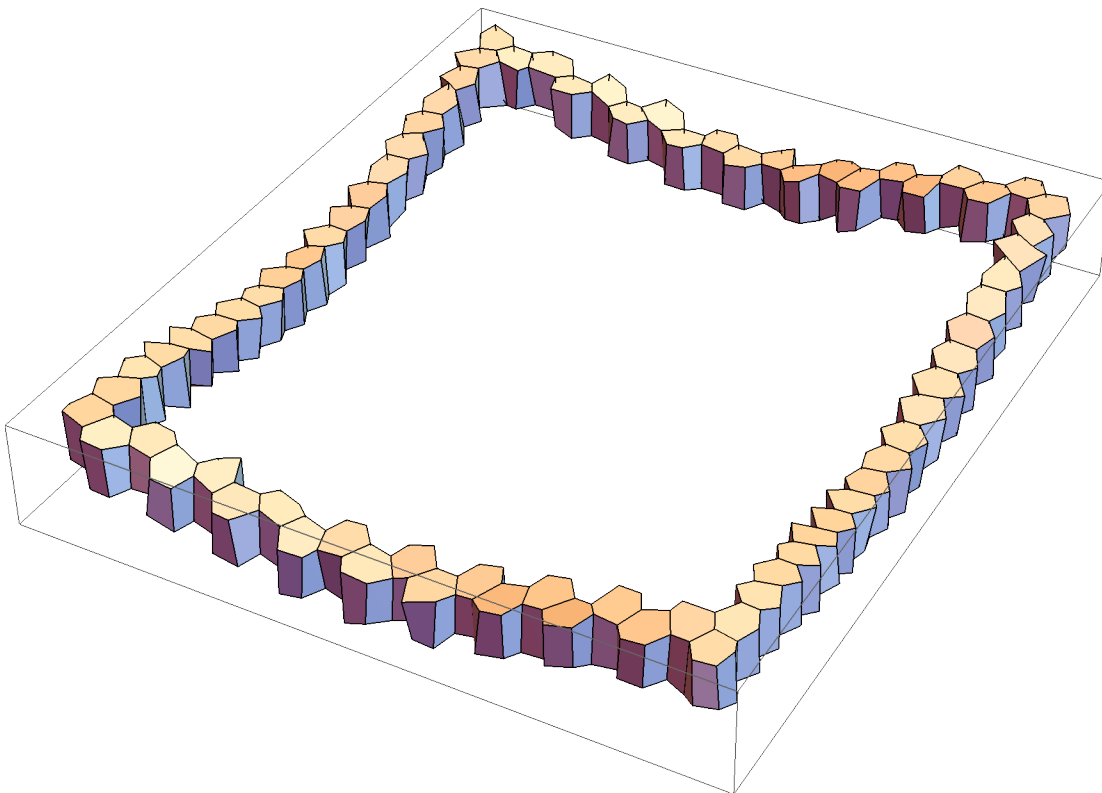
In[278]:= boundarycellsC = outerCellsFn[faceListCoordsC, vertexToCell, ptsToIndAssocC]

Out[278]:= {1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 40, 41, 60, 61,
    80, 81, 100, 101, 120, 121, 140, 141, 160, 161, 180, 181, 200, 201, 220, 221, 240,
    241, 260, 261, 280, 281, 300, 301, 320, 321, 340, 341, 360, 361, 380, 381, 382, 383,
    384, 385, 386, 387, 388, 389, 390, 391, 392, 393, 394, 395, 396, 397, 398, 399, 400}

In[279]:= Graphics3D[Polyhedron /@ Map[Lookup[indToPtsAssoc, #] &,
    Lookup[cellVertexGrouping, boundarycells], {2}], ImageSize → Large]

```

Out[279]=



```

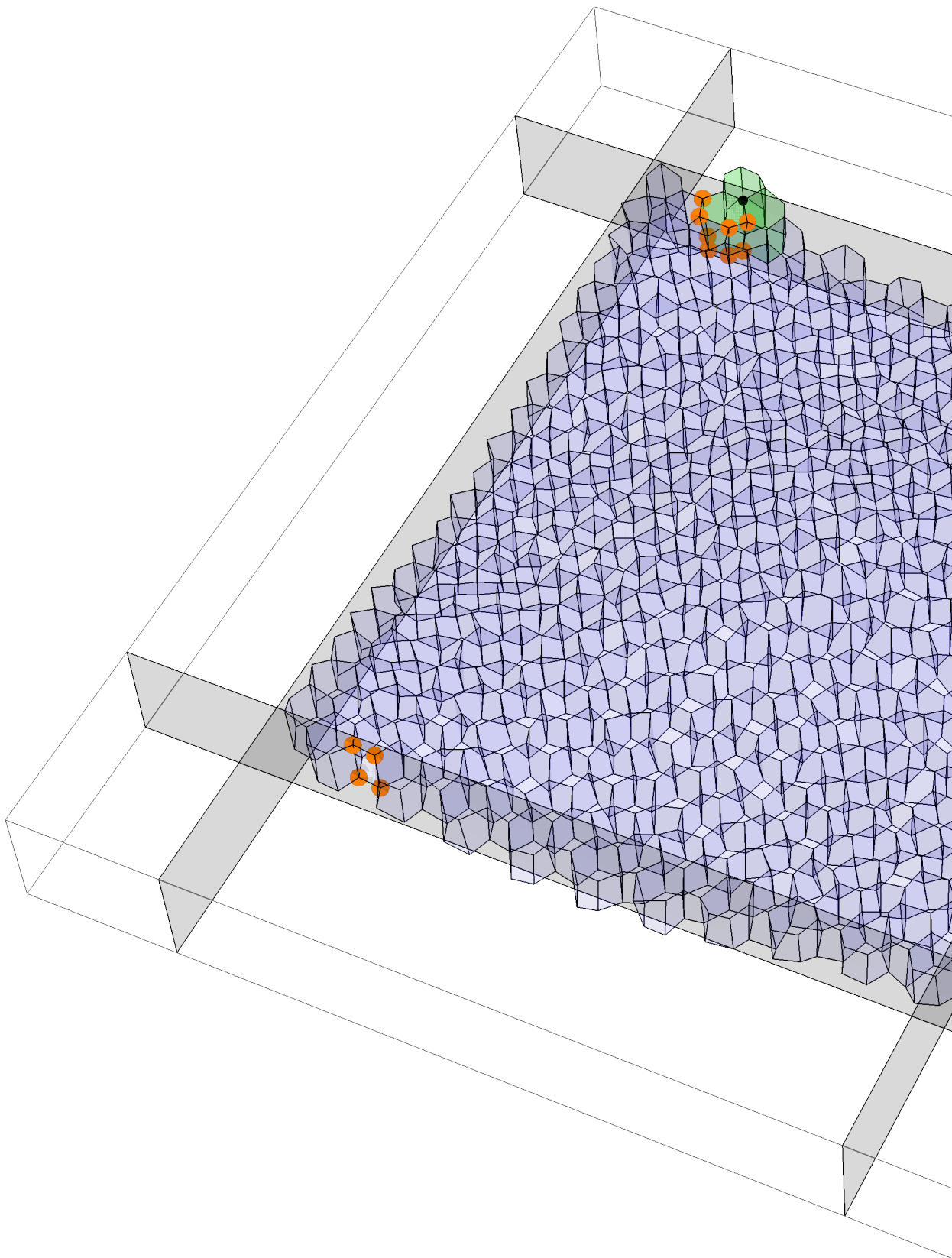
In[280]:= wrappedMatCsel = KeyTake[wrappedMatC, boundarycellsC];

```

```

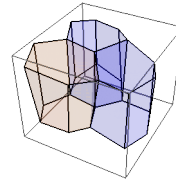
In[281]:= Block[{xx, yy, zz, edgelen, edgesel, keys, dset, id = 328, point},
  point = indToPtsAssocC[id];
  {xx, yy, zz} = getLocalTopology[ptsToIndAssocC, indToPtsAssocC, vertexToCell,
    cellVertexGrouping, wrappedMatCsel, faceListCoordsC][indToPtsAssocC[id]];
  keys = Keys@xx;
  Print@Graphics3D[{Opacity[0.05], Blue, Polyhedron /@ Values@faceListCoordsC},
    Black, PointSize[0.007], Point@point, Green, Point[point /. periodicRules],
    PointSize[0.012], Orange, Map[Point, wrappedMatC[60], {2}],
    Opacity[0.15], Green, Polyhedron /@ Values@xx,
    Black, InfinitePlane[{{0, 0, 0}, {0, xLim[[2]], 0}, {0, xLim[[2]], 1}}],
    InfinitePlane[
      {{0, yLim[[2]], 0}, {xLim[[2]], yLim[[2]], 0}, {xLim[[2]], yLim[[2]], 1}}],
    InfinitePlane[{{xLim[[2]], yLim[[2]], 0}, {xLim[[2]], yLim[[2]], 1},
      {xLim[[2]], yLim[[1]], 1}}],
    InfinitePlane[{{xLim[[2]], yLim[[1]], 0}, {xLim[[2]], yLim[[1]], 1},
      {0, yLim[[1]], 1}}]],
  ImageSize → 1024];
<|{"vertex" → id,
  "vertices in topology" → Length@DeleteDuplicates@Flatten[Values@xx, 2],
  "cell indices" → keys, "translated cell indices" → yy, (*"transvec"→zz,*)
  "localtopology" →
    Graphics3D[{Opacity[0.1], RandomColor[], Polyhedron /@ Lookup[xx, keys],
      Blue, If[yy ≠ {}, Polyhedron /@ Lookup[xx, yy]]}, ImageSize → Tiny]}|>
]

```



Out[281]= \langle vertex \rightarrow 328, vertices in topology \rightarrow 26, cell indices \rightarrow {60, 41, 61},

translated cell indices \rightarrow {41, 61}, localtopology \rightarrow \rangle



In[282]:= **Keys [getLocalTopology [ptsToIndAssocC, indToPtsAssocC, vertexToCell, cellVertexGrouping,**
wrappedMatCsel, faceListCoordsC] [indToPtsAssocC [#]] // First] & /@
Range [Max@ptsToIndAssocC] // Counts*Map [Length] // AbsoluteTiming

Out[282]= {1.00321, \langle 3 \rightarrow 1760 \rangle }