

Max-HP(A, i):

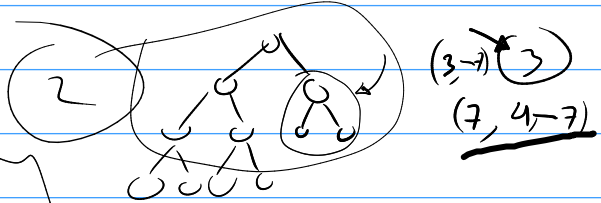
Recebe um heap y su nodo raíz. Tg como maximo  $\Delta$  nodo reemplaza la prop de MaxHeap (Nodo raíz). y Lo maxheapen

$n_l$ : # nodos izq.  
 $n_r$ : # nodos der.

$$n = 1 + n_l + n_r$$

$$T(n) = 1 + T\left(\frac{n}{2}\right) + C$$

$$T(n) \leq$$



$$n \text{ - Heap } h \rightarrow 2^h \leq n \leq 2^{h+1} - 1$$

$$\begin{aligned} \bullet h_l = h_r &\rightarrow n_l = 2^{h_l} - 1, n_r = 2^{h_r} - 1 \rightarrow \frac{n_l + 1}{2} \leq n_r \leq n_l \\ \bullet h_l = h_r + 1 &\rightarrow n_l = 2^{h_l} - 1, n_r = 2^{h_r} - 1 \rightarrow n_{l+1} \leq n_l \leq 2n_{r+1} \end{aligned}$$

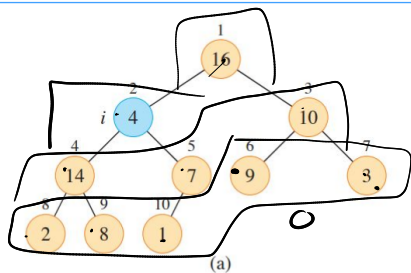
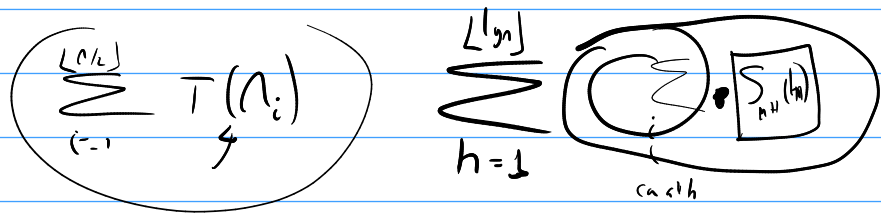
$$n_r \leq n_l \leq 2n_{r+1}$$

$$3n_l \leq 2n_r + 2n_{r+1} = 2n - 1 \rightarrow n_l \leq \frac{2n-1}{3} \leq \frac{2n}{3}$$

$$T(n) \leq T(n_l) + C \leq \frac{1}{3} T\left(\frac{2n}{3}\right) + C \sim O(\log n)$$

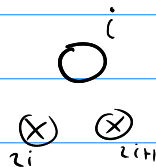
$$T_{\text{path}}(n) = O(\lg n) \iff \underline{S_{\text{path}}(h) = O(h) \leq kh}$$

$\hookrightarrow T_c \text{ n nodes}$



$$\begin{aligned}
 &1 \leq k_0 \\
 &1 \leq k_1 \\
 &\leq 3 \cdot (k_1) \\
 &\leq 5 \cdot k_0
 \end{aligned}$$

$h=0$  # nodes all 0:



$i$  tree all 0

$\leftarrow i$  is valid y  $z_i, z_{i+1}$  no longer



$i \leq n$

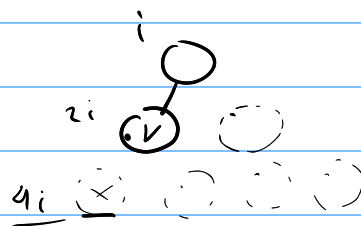
$$z_i, z_{i+1} > n$$

$$\boxed{z_i > n} \quad \boxed{z_i \geq n+1}$$

$$\left\lceil \frac{n+1}{2} \right\rceil \leq i \leq n$$

$$\# \text{ nodes} = n - \left\lceil \frac{n+1}{2} \right\rceil + 1 = \left\lceil \frac{n}{2} \right\rceil$$

$h=1$  #



$i$  all 0

$$z_i \leq n$$

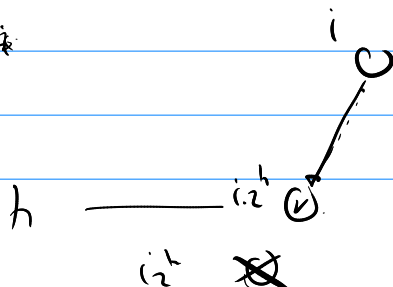
$$z_{i+1} \geq n+1$$

$$\left\lceil \frac{n+1}{4} \right\rceil \leq i \leq \left\lfloor \frac{n}{2} \right\rfloor$$

$$\rightarrow \# \text{ nodes} : \left\lfloor \frac{n}{2} \right\rfloor - \left\lceil \frac{n+1}{4} \right\rceil + 1 = \left\lceil \frac{n}{4} \right\rceil$$

$$\left\lfloor \frac{n}{2} \right\rfloor - \left\lceil \frac{n+1}{4} \right\rceil + 1$$

$h=2$



$$z_i^h \leq n$$

$$z_{i+1}^h \geq n+1$$

$$\left\lceil \frac{n+1}{2^{h+1}} \right\rceil \leq i \leq \left\lfloor \frac{n}{2^h} \right\rfloor$$