

# Anomaly Detection: Wednesday Night Household Global Power Usage

Group 15

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## Objectives:

- Decide on a time window that was consistent across all test sets
- General Data exploration on different time windows and seasonality
- Explain point anomalies using max and min ranges in training set and relating them to moving window averages of test sets
- Explain contextual anomalies using HMMs and normalized log likelihood calculations

*Fig. 1.1 – Wednesday Morning MSE Calculations*

	Mean Error Test 1	Mean Error Test 2	Mean Error Test 3	Mean Error Test 4	Mean Error Test 5	STD Error Test 1	STD Error Test 2	STD Error Test 3	STD Error Test 4	STD Error Test 5
Spring - Season 1	0.287	0.370	0.287	12.943	13.230	0.2558	0.2262	0.2558	5.3846	5.5031
Summer - Season 2	0.128	0.139	0.128	6.666	6.581	0.0952	0.1078	0.0952	3.6175	3.5694
Fall - Season 3	0.385	0.376	0.385	16.507	16.488	0.1782	0.1693	0.1782	5.2776	5.2382
Winter - Season 4	0.176	0.237	0.176	14.279	14.398	0.1462	0.1447	0.1462	5.1911	5.4687

*Fig. 1.2 – Wednesday Night MSE Calculations*

	Mean Error Test 1	Mean Error Test 2	Mean Error Test 3	Mean Error Test 4	Mean Error Test 5	STD Error Test 1	STD Error Test 2	STD Error Test 3	STD Error Test 4	STD Error Test 5
Spring - Season 1	0.210	0.231	0.210	10.238	9.830	0.1093	0.0992	0.1093	3.9950	3.7116
Summer - Season 2	0.246	0.272	0.246	8.413	8.183	0.1125	0.1262	0.1125	4.6450	4.5540
Fall - Season 3	0.139	0.124	0.139	8.733	8.372	0.0972	0.0825	0.0972	4.8271	4.4512
Winter - Season 4	0.185	0.411	0.185	16.468	16.741	0.1265	0.1564	0.1265	6.9111	7.0086

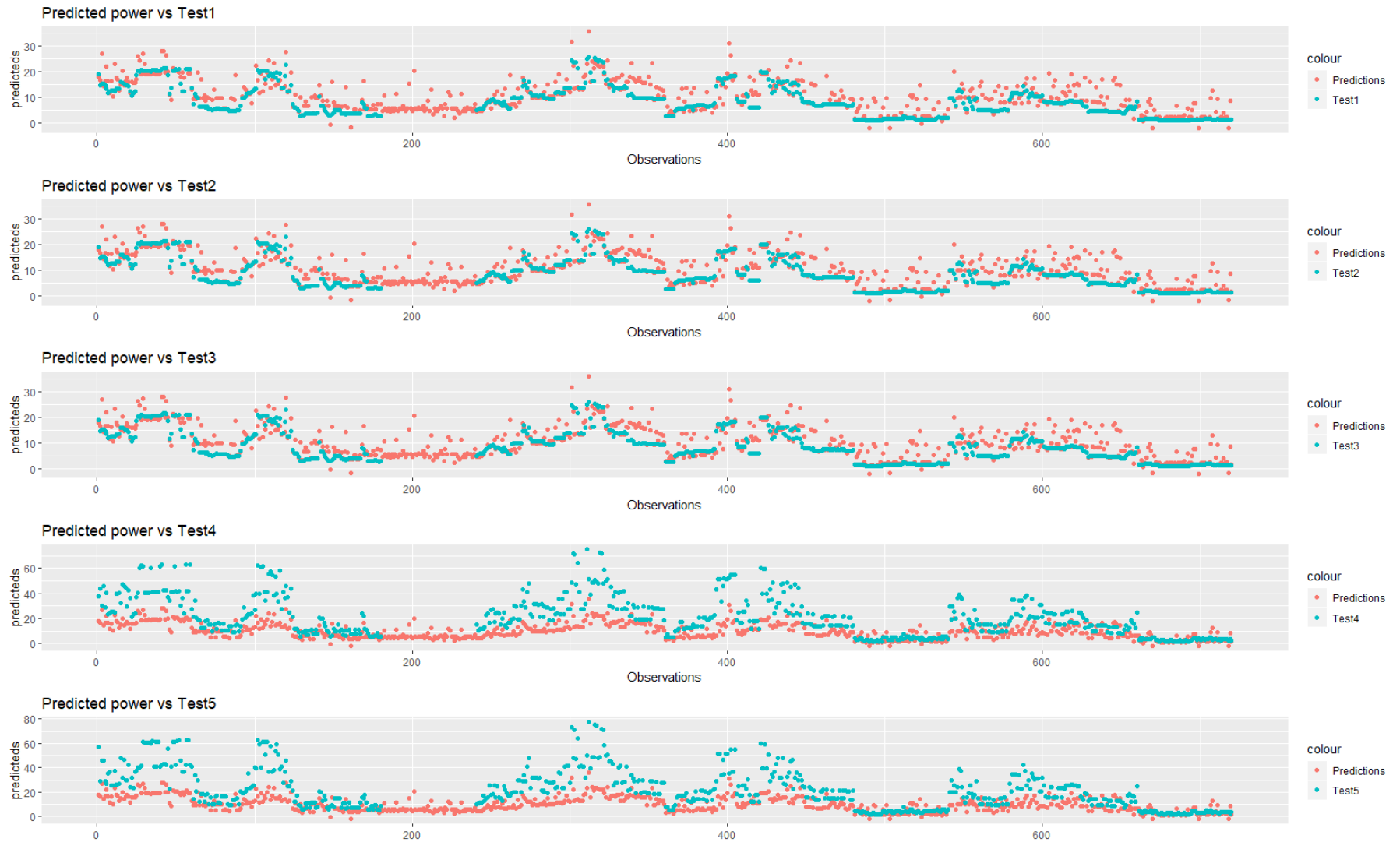
*Fig 1.3 - Correlation between all observations when time was aggregated hourly*

	Global_active_power	Global_reactive_power	Voltage	Global_intensity	Sub_metering_1	Sub_metering_2	Sub_metering_3
Global_active_power	1.0000000	0.2121330	-0.3073528	0.8092017	0.3691985	0.3467608	0.5165714
Global_reactive_power	0.2121330	1.0000000	-0.1544859	0.3346676	0.3541653	0.2567012	0.1124776
Voltage	-0.3073528	-0.1544859	1.0000000	-0.3979771	-0.2099719	-0.1710845	-0.2991657
Global_intensity	0.8092017	0.3346676	-0.3979771	1.0000000	0.5056849	0.4598049	0.6772855
Sub_metering_1	0.3691985	0.3541653	-0.2099719	0.5056849	1.0000000	0.1237429	0.2042420
Sub_metering_2	0.3467608	0.2567012	-0.1710845	0.4598049	0.1237429	1.0000000	0.1372597
Sub_metering_3	0.5165714	0.1124776	-0.2991657	0.6772855	0.2042420	0.1372597	1.0000000

*Fig 1.4 - Correlation between all observations when time was aggregated daily*

	Global_active_power	Global_reactive_power	Voltage	Global_intensity	Sub_metering_1	Sub_metering_2	Sub_metering_3
Global_active_power	1.00000000	-0.09430221	0.15414334	0.86313850	0.39828051	0.38089763	0.60700967
Global_reactive_power	-0.09430221	1.00000000	-0.06300499	0.05077379	0.33947151	0.17856335	0.04455324
Voltage	0.15414334	-0.06300499	1.00000000	0.08135940	-0.07240053	-0.07435111	0.13252725
Global_intensity	0.86313850	0.05077379	0.08135940	1.00000000	0.54520350	0.48912452	0.73306878
Sub_metering_1	0.39828051	0.33947151	-0.07240053	0.54520350	1.00000000	0.24212045	0.32911920
Sub_metering_2	0.38089763	0.17856335	-0.07435111	0.48912452	0.24212045	1.00000000	0.22734383
Sub_metering_3	0.60700967	0.04455324	0.13252725	0.73306878	0.32911920	0.22734383	1.00000000

*Fig. 1.5 - Predicted values against recorded values for Global Intensity*



# Point Anomalies

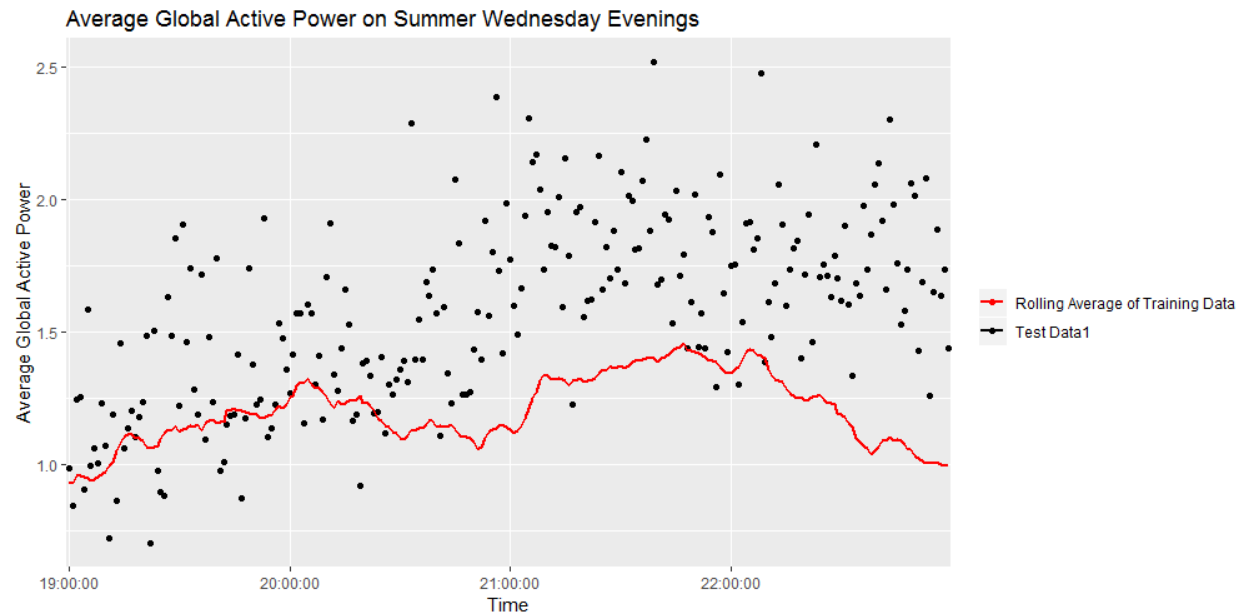
- Shift from Phase 1 to only Wednesday Nights (mainly summer) to explain relationship between test sets
- Used a maximum and minimum bound based on the total training set on Wednesday Nights during each season

*Fig. 1.6 - Training set GAP Max and Min Wednesday nights*

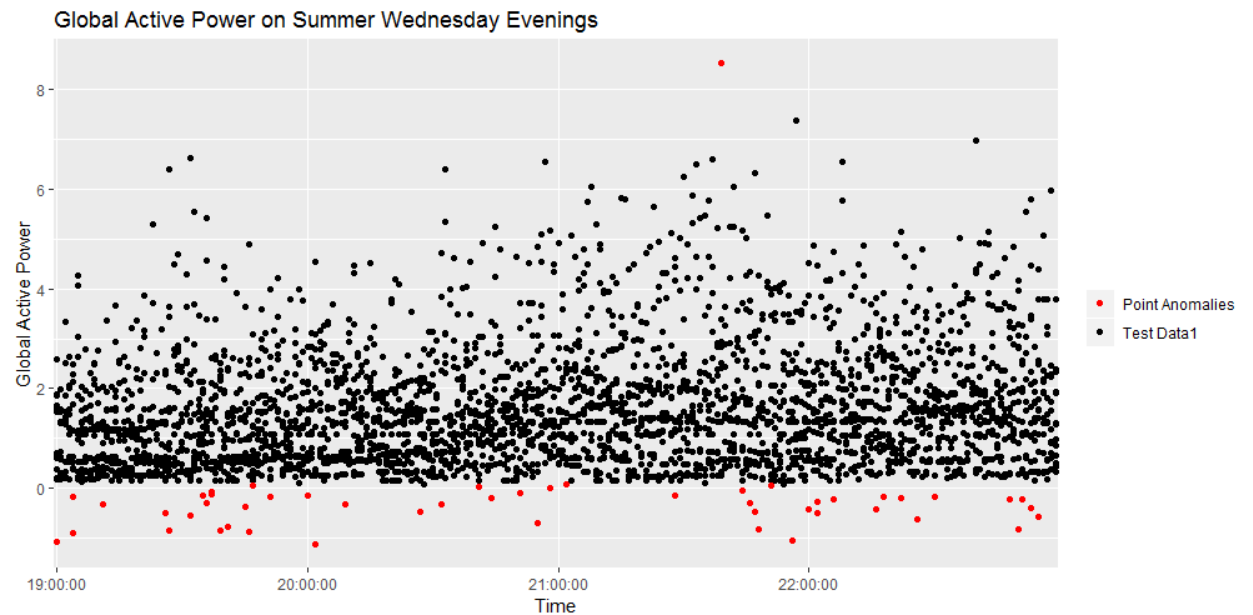
	Max Global Active Power	Min Global Active Power
Spring - Season 1	8.06	0.184
Summer - Season 2	7.436	0.08
Fall - Season 3	7.03	0.188
Winter - Season 4	8.974	0.204

Using these maximum and minimum bounds we tested each test set for Wednesday nights during the summer to determine point anomalies in each data set

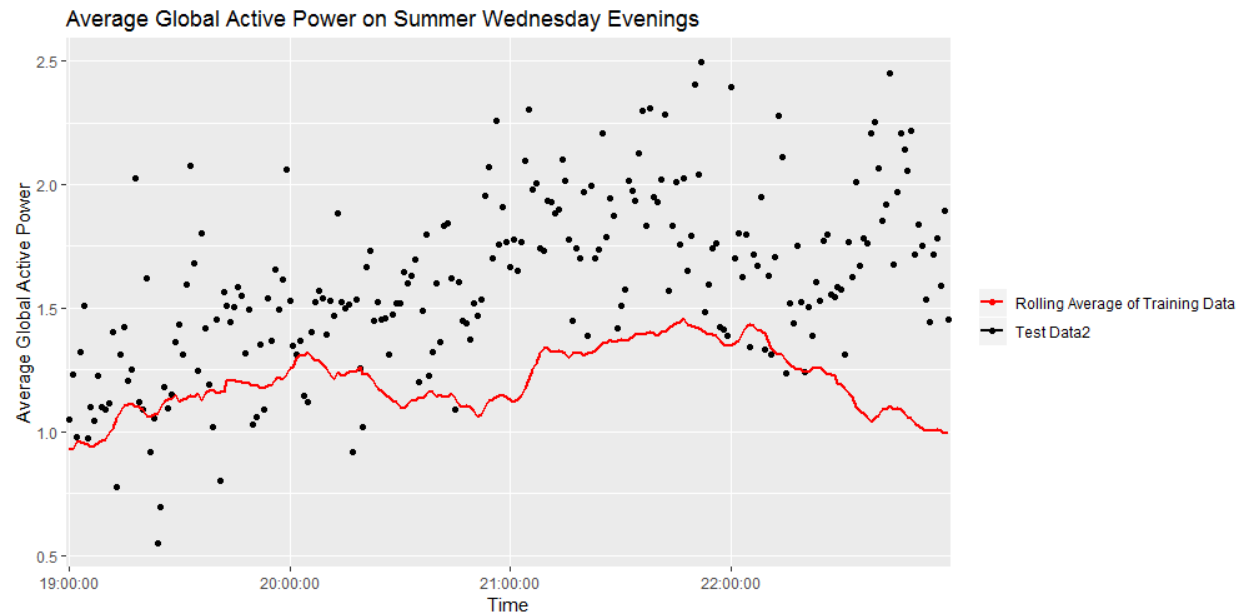
Test set #1  
averages vs  
training set rolling  
average



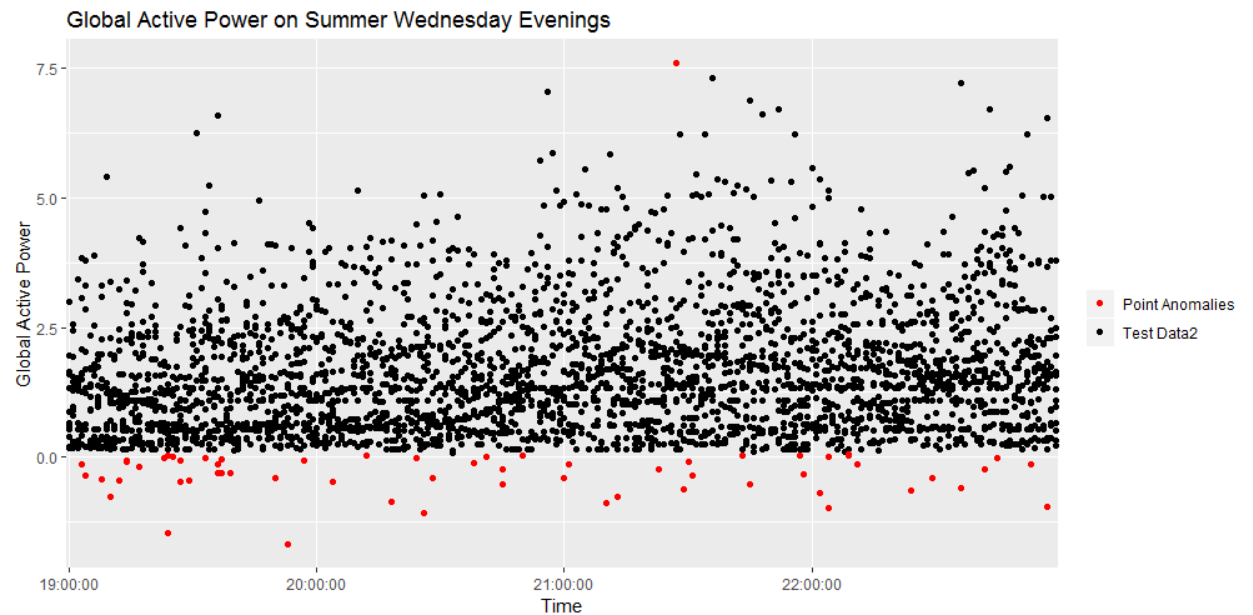
Test set #1 Data with  
point anomalies



Test set #2  
averages vs  
training set rolling  
average

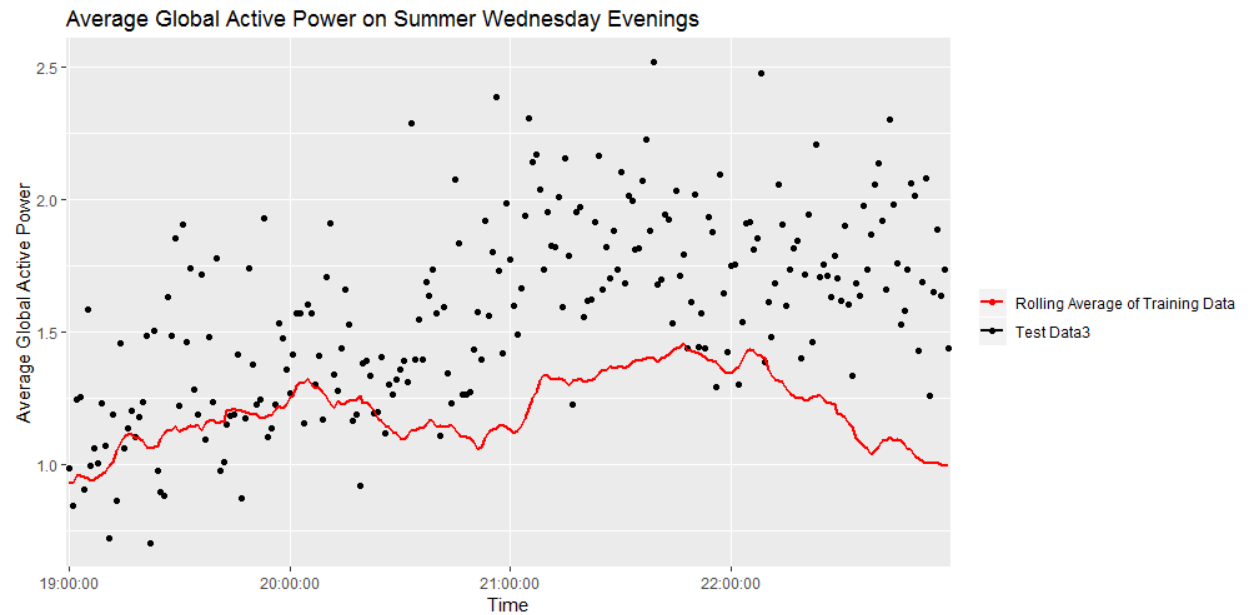


Test set #2 Data with  
point anomalies

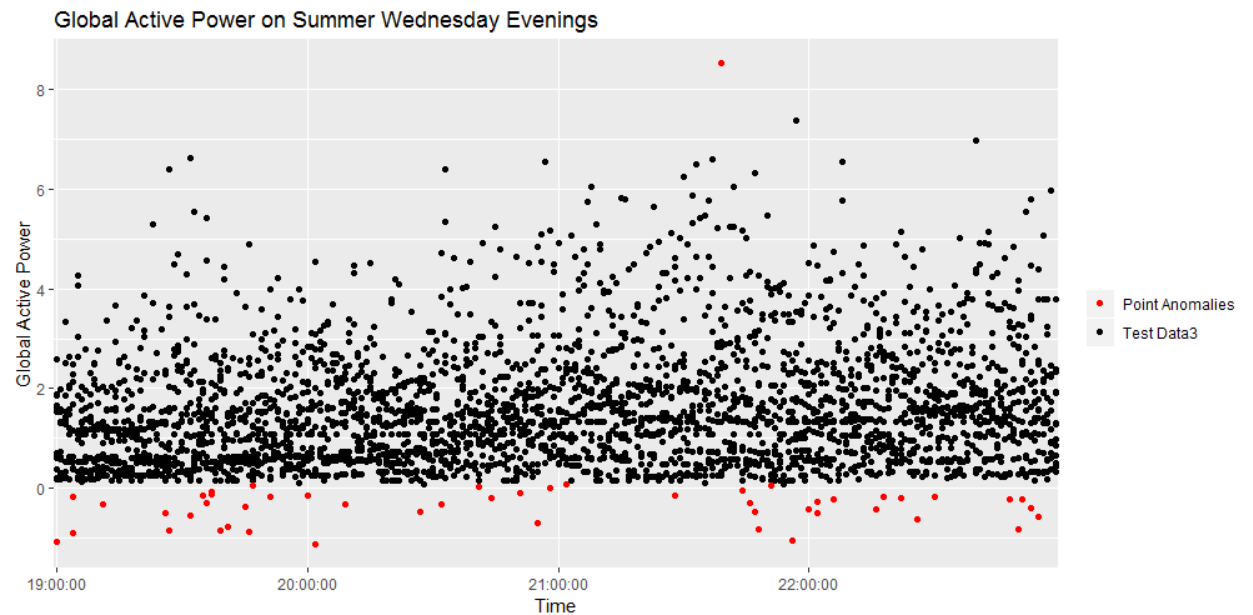




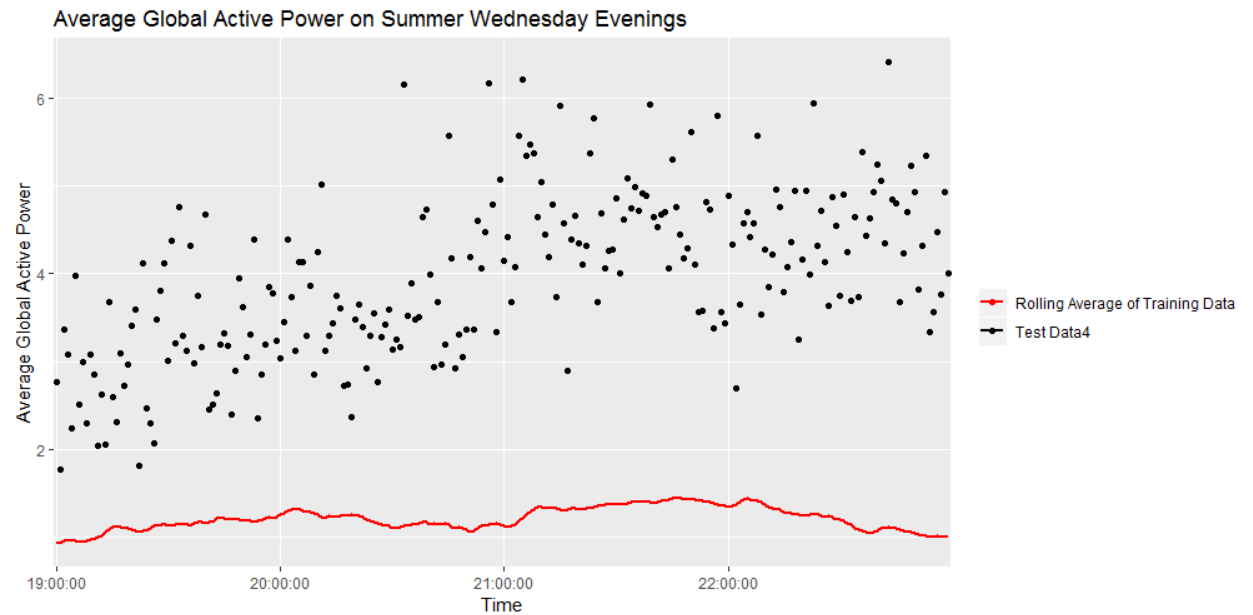
Test set #3  
averages vs  
training set rolling  
average



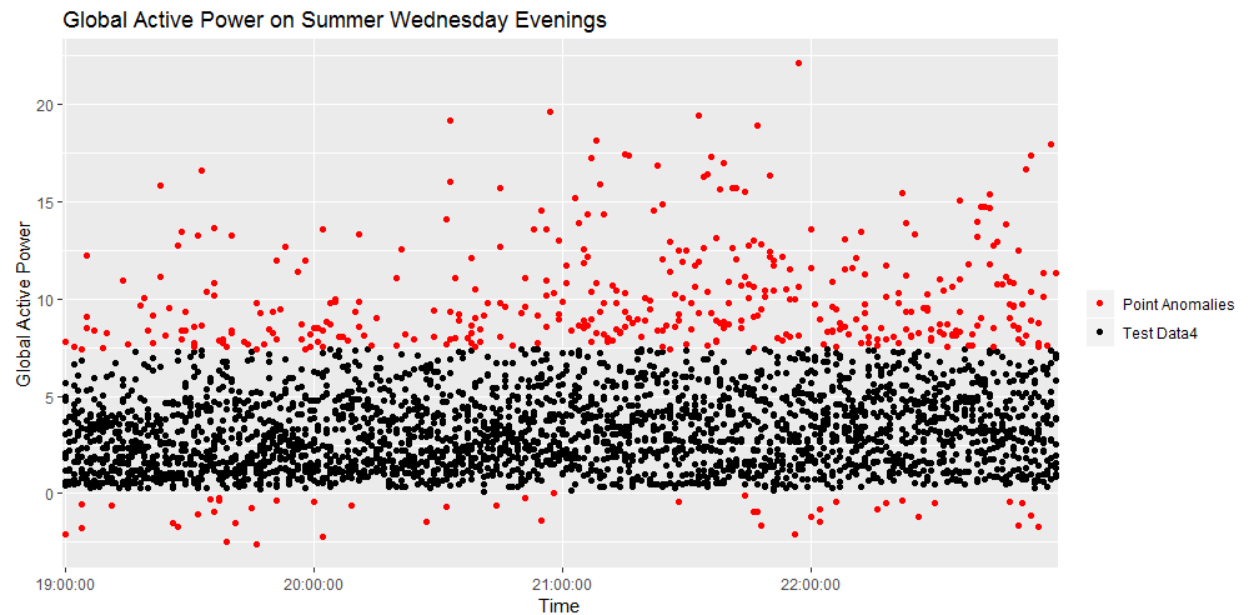
Test set #3 Data with  
point anomalies



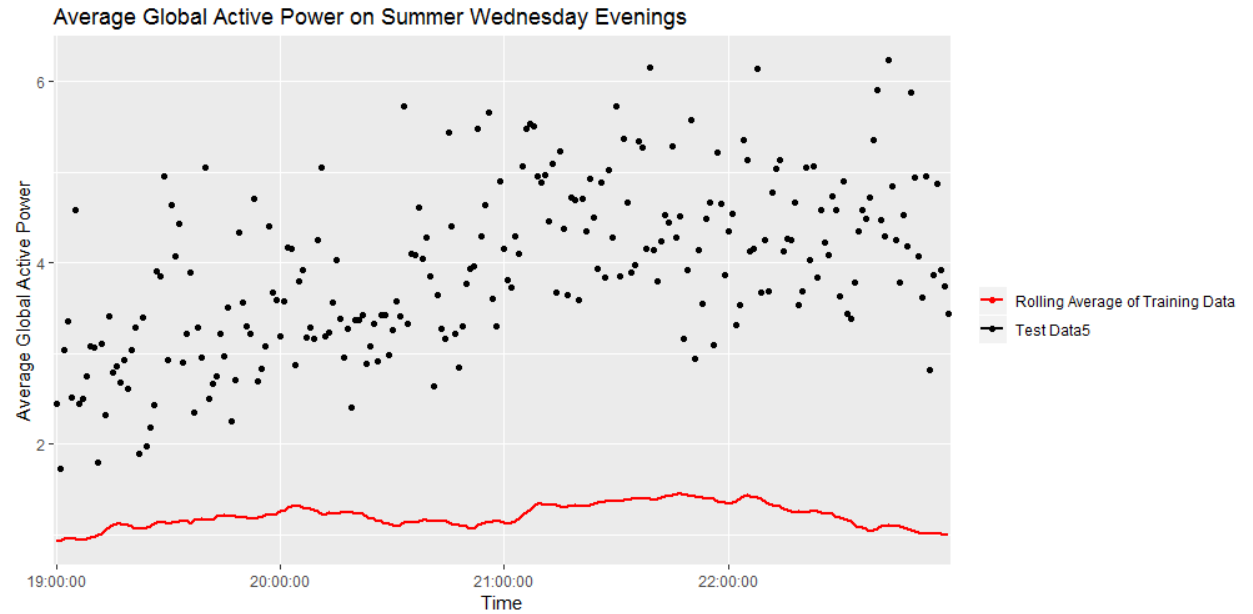
Test set #4  
averages vs  
training set rolling  
average



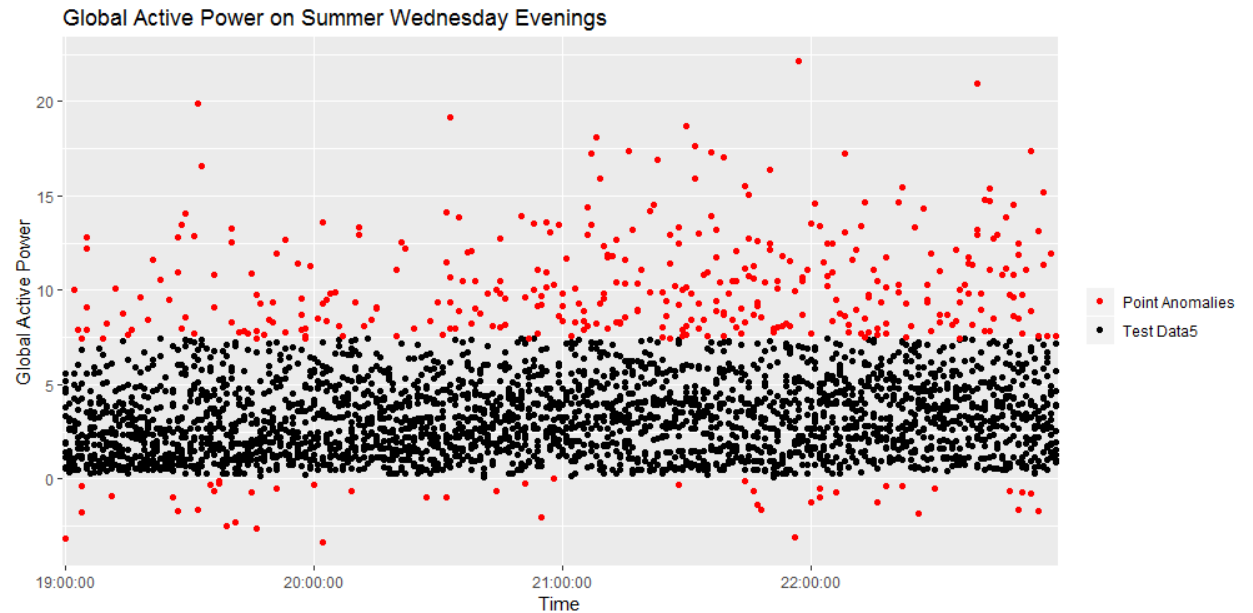
Test set #4 Data with  
point anomalies



Test set #5  
averages vs  
training set rolling  
average

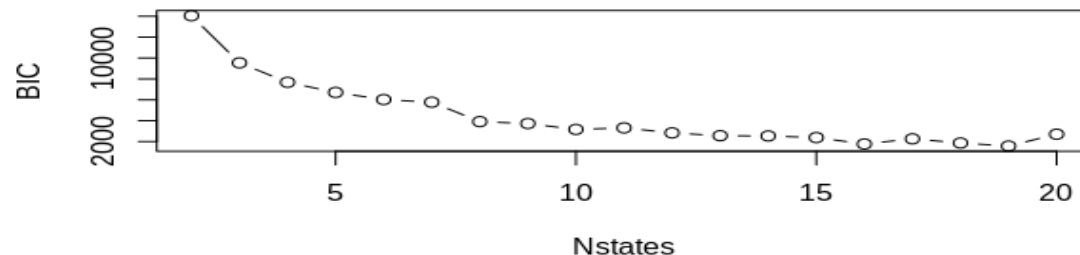


Test set #5 Data with  
point anomalies



# Contextual Anomalies

Training data BIC per  
Nstates



Normalized log likelihoods using 39 observations for training data  
and 13 observations per training set

	Training set (training original)	Test set #1	Test set #2	Test set #3	Test set #4	Test set #5
Normalized Log Likelihood	185.6229 (556.8686)	-5208.521	-5538.565	-5208.823	-16194.67	-15983.83

## **Key Findings**

- Test sets #1 and #3 included exactly the same data points for Wednesday nights during the summer when doing point anomalies and we assume one is just a copy based on error calculations and contextual anomalies
- Test sets #4 and #5 were highly anomalous with very high values compared to the expected behaviour of the training set and had very high log likelihoods
- Global active power and Global reactive power had the closest correlation constants which we expected because they are a function of one another

## **Future applications**

- Using a live max and min point anomaly detection techniques could potentially give a first response to malicious or unexpected behaviour
- Contextual anomaly detection can be used to determine normal behaviours across long spans of time to make better reporting of power consumption in the past when compared to the present.