

# PARTY PLANNING ALGORITHM

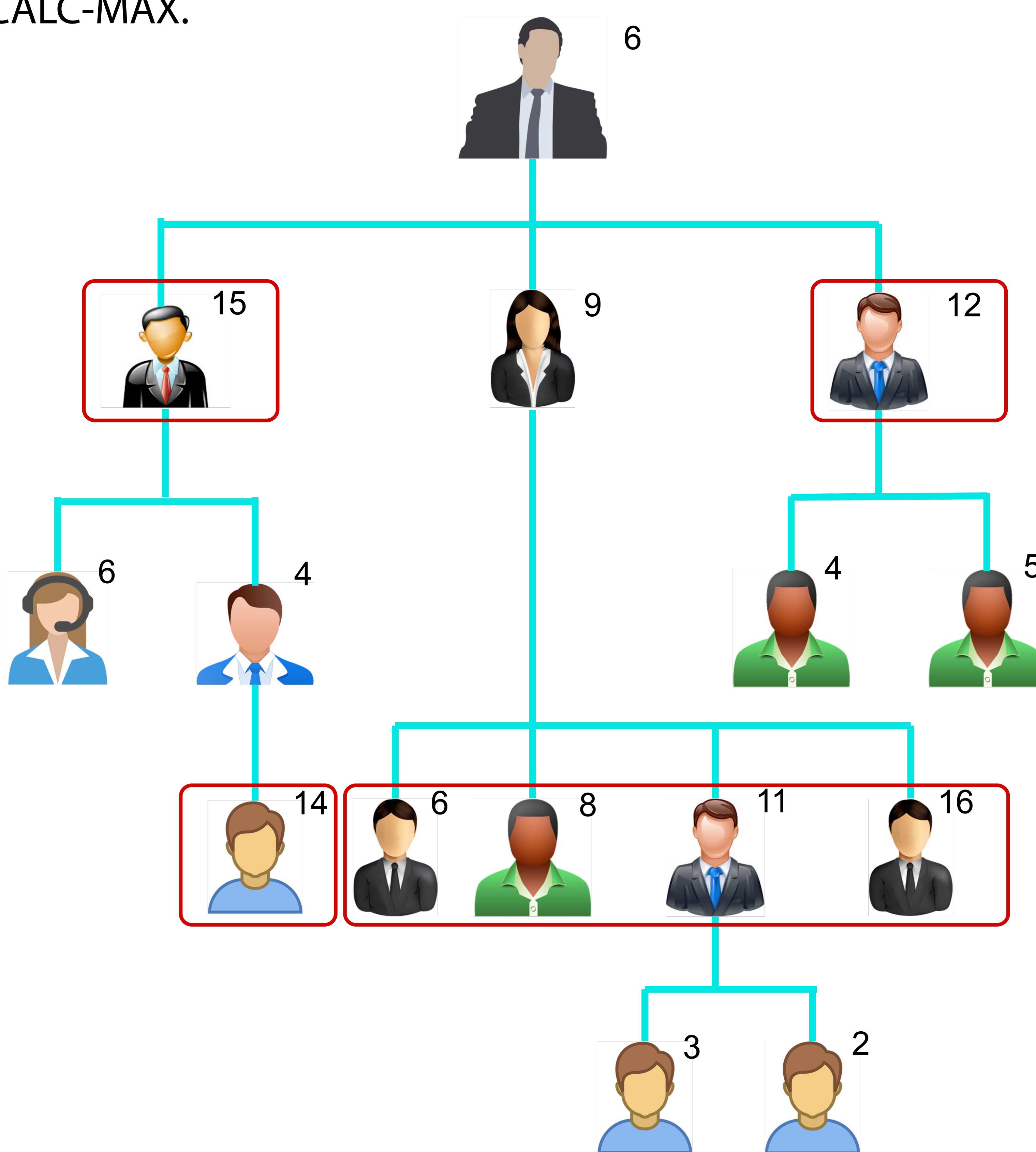
## INTRODUCTION

In order to make the party fun for all attendees, the president doesn't want both an employee & his/her immediate supervisor to attend. Professor Stewart is consulting for the president of a corporation that is planning a company party.

## EXAMPLE

Add three fields to each node:  $a[i]$  and  $p[i]$  which stores the optimal value in the subtree rooted at  $i$  if  $i$  is absent and present respectively and  $g[i]$  which indicates whether  $i$  is a guest. Finding the optimal sum can be done by running the following algorithm CALC-MAX from the root and checking whether  $a[\text{root}]$  or  $p[\text{root}]$  is larger.

To fill in the  $g[i]$  field, run LIST-GUEST from the root after CALC-MAX.



### CALC-MAX(x)

```

1  $a[x] = 0, p[x] = \text{conviviality}[x]$ 
2  $y = \text{left-child}[x]$ 
3 while  $y \neq \text{null}$ 
4   Calc-Max( $y$ )
5    $y = \text{right-sibling}[y]$ 
6 if  $x$  is not the root
7    $a[\text{parent}[x]] = a[\text{parent}[x]] + \max\{a[x], p[x]\}$ 
8    $p[\text{parent}[x]] = p[\text{parent}[x]] + a[x]$ 
```

### LIST-GUEST(x)

```

1 if  $x = \text{root}$ 
2 if  $p[x] > a[x]$ 
3    $g[x] = \text{true}$ 
4 else
5    $g[x] = \text{false}$ 
6 else
7   if  $g[\text{parent}[x]] = \text{true}$ 
8      $g[x] = \text{false}$ 
9 else
10  if  $p[x] > a[x]$ 
11     $g[x] = \text{true}$ 
12 else
13   $g[x] = \text{false}$ 
14  $y = \text{left-child}[x]$ 
15 while  $y \neq \text{null}$ 
16   List-Guest( $y$ )
17    $y = \text{right-sibling}[y]$ 
```

Since each node is processed once and all operations in the processing run in constant time, the running time is  $O(n)$ .

## RUN TIME