

$$R_1 \cup R_2 = (a, b, c, d, e, f, g) = R \quad \textcircled{I}$$

$$R_1 \cap R_2 = (a, e) \neq \emptyset \quad \textcircled{II}$$

①

$$\{R_1 \cap R_2\}^+ = \{a, e\}^+ = R, \quad R_1, R_2 \subset R \quad \textcircled{III}$$

①, ②, ③  $\Rightarrow$  Lossless Decomposition

الف)  $\{a, b, e\}^+ \xrightarrow{ab \rightarrow c} \{a, b, c, e\}^+ \xrightarrow{ce \rightarrow f} \{a, b, c, e, f\}^+ \xrightarrow{f \rightarrow de} \{a, b, c, d, e, f\}^+ = R$

②

Union rule :  $\left. \begin{matrix} \alpha \rightarrow \beta \\ \alpha \rightarrow \gamma \end{matrix} \right\} \Rightarrow \alpha \rightarrow \beta\gamma$

③

$$\left. \begin{matrix} \alpha \rightarrow \beta \Rightarrow \alpha\alpha \rightarrow \alpha\beta \Rightarrow \alpha \rightarrow \alpha\beta \\ \alpha \rightarrow \gamma \Rightarrow \alpha\beta \rightarrow \gamma\beta \end{matrix} \right\} \Rightarrow \alpha \rightarrow \gamma\beta$$

الف)  $\left. \begin{matrix} a \rightarrow bc \Rightarrow a \rightarrow b \\ b \rightarrow cd \Rightarrow b \rightarrow c \end{matrix} \right\} \Rightarrow a \rightarrow c \Rightarrow c \text{ in } a \rightarrow bc$

④

ب)  $\left. \begin{matrix} a \rightarrow c \\ c \rightarrow b \end{matrix} \right\} \Rightarrow a \rightarrow b \Rightarrow b \text{ in } ab \rightarrow de$

د)  $\{de\}^+ = \{ae\}^+ = \{be\}^+ = R$

- )  $a \rightarrow b$ : (X) crn (X) a Superkey  
 $b \rightarrow cd$ : (X) crn (X) b Superkey  
 $de \rightarrow a$ : (X) crn (✓) de Superkey

BCNF:  $R_1 = (a, b)$   $R_2 = (b, cd)$   $R_3 = (d, e, a)$   
 $F_1 = \{a \rightarrow b\}$   $F_2 = \{b \rightarrow cd\}$   $F_3 = \{de \rightarrow a\}$

- ج)  $a \rightarrow b$ : (X) crn (X) a Superkey (✓) b in {be}  
 $b \rightarrow cd$ : (X) crn (X) b Superkey (X) cd in superkey  
 $de \rightarrow a$ : (X) crn (✓) de Superkey (✓) a in {ae}

3NF:  $R_1 = (b, c)$   $R_2 = (a, b, d, e)$   
 $F_1 = \{b \rightarrow c\}$   $F_2 = \{a \rightarrow b, b \rightarrow d, de \rightarrow a\}$

الف)  $\{ag\}^+$

ب)  $\{a \rightarrow b, a \rightarrow d, a \rightarrow e, a \rightarrow c, g \rightarrow h\}$

- ج)  $a \rightarrow e$ : (X) crn (X) a Superkey  
 $a \rightarrow bd$ : (X) crn (X) a Superkey  
 $aed \rightarrow c$ : (X) crn (X) aed Superkey  
 $g \rightarrow gh$ : (X) crn (X) g Superkey

BCNF:  $R_1 = (a, b, c, d, e)$   $R_2 = (g, h)$   $R_3 = (a, f, g)$   
 $F_1 = \{a \rightarrow b, a \rightarrow c, a \rightarrow d, a \rightarrow e\}$   $F_2 = \{g \rightarrow h\}$

- د)  $a \rightarrow e$ : (X) crn (X) a Superkey (X) e in Superkey  
 $a \rightarrow bd$ : (X) crn (X) a Superkey (X) bd in Superkey  
 $aed \rightarrow c$ : (X) crn (X) aed Superkey (X) c in Superkey  
 $g \rightarrow gh$ : (X) crn (X) g Superkey (X) gh in Superkey

3NF:  $R_1 = (a, b, c, d, e)$   $R_2 = (g, h)$   $R_3 = (a, f, g)$

$F_1 = \{a \rightarrow b, a \rightarrow c, a \rightarrow d, a \rightarrow e\}$   $F_2 = \{g \rightarrow h\}$

$R_1 = (a, d)$   $R_2 = (a, b, c)$

$F_1 = \{a \rightarrow d\}$

(7)

الف)  $\pi_{drugName} (\delta_{count \leq 3} (drugName Fcount (*) (\delta_{nameOfDoctor = "Martin"} (($

(8)

$Doctor \bowtie_{Doctor.numberOfDoctor = Appoint.numberOfDoctor} Appoint \bowtie_{Appoint.NA = Prescr.NA} Prescr$

$\bowtie_{Prescr.drugCode = Drugs.drugCode} Drugs))))$

ب)  $\pi_{nameOfPatient, address} (\delta_{nameOfDoctor = "Joe"} (( Appoint \bowtie_{Appoint.numberOfPatient = Patient.numberOfPatient} Patient$

$\bowtie_{Doctor.numberOfDoctor = Appoint.numberOfDoctor} Doctor))$

ج)  $\pi_{drugName} (\delta_{hospital = "Hermes"} (( Appoint \bowtie_{Appoint.numberOfDoctor = Doctor.numberOfDoctor} Doctor$

$\bowtie_{Appoint.NA = Prescr.NA} Prescr \bowtie_{Prescr.drugCode = Drugs.drugCode} Drugs))$

د)  $\pi_{hospital} (\delta_{nameOfDoctor, hospital} (Doctor))$

س: تابع مرتب سازی بر اساس

۹) (a) نام آرایه کنده های که برای آن ها فارسی ثبت شده است.

(b) نام کلاس (های) که بیشترین مقدار را دارند

۱۰) (a) مبدأ (های) که به تمام مقصد های ثبت شده پرواز داشته باشند.

(b) مبدأ مقصد پروازها به همراه پرواز های که مقصد اول یا مبدأ اولی برابر باشند.