EE-559 - Deep learning

4b. PyTorch modules, batch processing

François Fleuret
https://fleuret.org/dlc/
[version of: May 17, 2018]





torch.nn

PyTorch provides a vast collection of functions and "modules" which can be combined into complicated architectures. We will look at what is needed to build our first convolutional neural network:

- torch.nn.functional.relu
- torch.nn.functional.max_pool2d
- torch.nn.Conv2d
- torch.nn.Linear
- torch.nn.MSELoss

Elements from torch.nn.functional are autograd-compliant functions which compute a result from provided arguments alone. This is usually imported as F.

Subclasses of torch.nn.Module are losses and network components. The latter embed torch.nn.Parameter s to be optimized during training.

François Fleuret

EE-559 - Deep learning / 4b. PyTorch modules, batch processing

3 / 31



Since they are almost exclusively used with autograd, elements from torch.nn only process Variable s.

The term "tensor" is used for both Tensor's and Variable's in what follows.



Functions and modules from torch.nn process only batches of inputs stored in a tensor with an additional first dimension to index them, and produce a corresponding tensor with an additional dimension.

E.g. a fully connected layer $\mathbb{R}^C \to \mathbb{R}^D$ expects as input a tensor of size $N \times C$ and compute a tensor of size $N \times D$, where N is the number of samples.

François Fleuret

 ${\sf EE\text{-}559-Deep\ learning}\ /\ {\sf 4b.\ PyTorch\ modules,\ batch\ processing}$

5 / 31

```
torch.nn.functional.relu(input, inplace=False)
```

Takes a tensor of any size as input, applies ReLU on each value to produce a result tensor of same size.

```
>>> x = Variable(Tensor(2, 5).normal_())
>>> x
Variable containing:
-0.2066 -1.7997 -0.0653  0.6481  0.0253
1.0239  3.0324  1.6431 -1.8925  0.0890
[torch.FloatTensor of size 2x5]

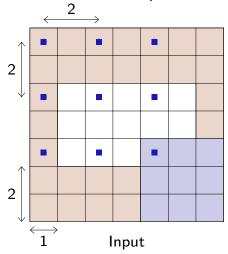
>>> torch.nn.functional.relu(x)
Variable containing:
  0.0000  0.0000  0.0000  0.6481  0.0253
1.0239  3.0324  1.6431  0.0000  0.0890
[torch.FloatTensor of size 2x5]
```

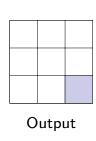
inplace indicates if the operation should modify the argument itself. This may be desirable to reduce the memory footprint of the processing.

For what follows, note that pooling and convolution have two additional standard parameters:

- The padding specifies the size of a zeroed frame added around the input,
- the **stride** specifies a step size when moving the filter across the signal.

Here with $C \times 3 \times 5$ as input, a padding of (2,1), a stride of (2,2), and a kernel of size $C \times 3 \times 3$, the output is $1 \times 3 \times 3$.





Pooling operations have a default stride equal to their kernel size, and convolutions have a default stride of 1. Padding is zero by default, and is useful for instance to generate an output of same size as the input.

François Fleuret

 ${\sf EE\text{-}559-Deep\ learning}\ /\ {\sf 4b.\ PyTorch\ modules,\ batch\ processing}$

7 / 31

Takes as input a $N \times C \times H \times W$ tensor, and a kernel size (h, w) or k interpreted as (k, k), applies the max-pooling on each channel of each sample separately, and produce if the padding is 0 a $N \times C \times |H/h| \times |W/w|$ output.

```
class torch.nn.Linear(in_features, out_features, bias=True)
```

Implements a $\mathbb{R}^C \to \mathbb{R}^D$ fully-connected layer. It takes as input a tensor of size $N \times C$ and produce a tensor of size $N \times D$.

```
>>> f = torch.nn.Linear(in_features = 10, out_features = 4)
>>> f.weight.size()
torch.Size([4, 10])
>>> f.bias.size()
torch.Size([4])
>>> x = Variable(Tensor(523, 10).normal_())
>>> y = f(x)
>>> y.size()
torch.Size([523, 4])
```



The weights and biases are automatically randomized at creation. We will come back to that later.

François Fleuret

EE-559 - Deep learning / 4b. PyTorch modules, batch processing

9 / 31

Implements a standard 2d convolutional layer. The kernel size is either a pair (h, w) or a single value k interpreted as (k, k).

It takes as input a $N \times C \times H \times W$ tensor and returns a tensor $N \times D \times (H - h + 1) \times (W - w + 1)$

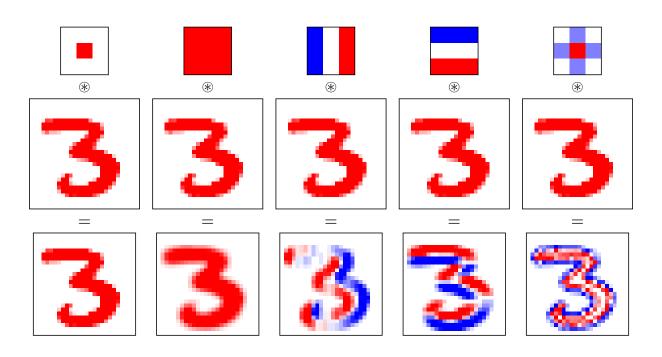
```
>>> l = torch.nn.Conv2d(in_channels = 4, out_channels = 5, kernel_size = (2, 3))
>>> l.weight.size()
torch.Size([5, 4, 2, 3])
>>> l.bias.size()
torch.Size([5])
>>> x = Variable(Tensor(117, 4, 10, 3).normal_())
>>> y = 1(x)
>>> y.size()
torch.Size([117, 5, 9, 1])
```

As for the fully connected layer, weights and biases are randomized.

```
mnist_train = datasets.MNIST('./data/mnist/', train = True, download = True)
# Take the 13th example, shape it as a batch of a single one-channel image
x = mnist_train.train_data[12].float().view(1, 1, 28, 28)
f = torch.nn.Conv2d(1, 5, kernel_size=3)
f.bias.data.zero_()
f.weight.data[0] = Tensor([ [ 0, 0, 0],
                             Ο,
                                 1,
                                     0],
                           [ 0,
                                 0, 0]])
f.weight.data[1] = Tensor([ [ 1, 1, 1],
                           [ 1, 1, 1],
[ 1, 1, 1])
f.weight.data[2] = Tensor([ [ -1, 0, 1 ],
                           [ -1, 0, 1 ],
[ -1, 0, 1 ] )
f.weight.data[3] = Tensor([ [ -1, -1, -1 ],
                           [ 0, 0, 0 ],
[ 1, 1, 1 ] ])
y = f(Variable(x)).data
save_2d_tensor_as_image(f.weight.data[0], 'conv-filters-{:d}.png',
                       signed = True)
save_2d_tensor_as_image(x[0], 'conv-mnist-orig.png', signed = True)
save_2d_tensor_as_image(y[0], 'conv-mnist-results-{:d}.png',
                       signed = True)
```

François Fleuret

EE-559 - Deep learning / 4b. PyTorch modules, batch processing



11 / 31

```
torch.nn.MSELoss()
```

Implements the Mean Square Error loss: the sum of the component-wise squared difference, divided by the total number of components in the tensors.

```
>>> f = torch.nn.MSELoss()
>>> x = Variable(Tensor([[ 3 ]]))
>>> y = Variable(Tensor([[ 0 ]]))
>>> f(x, y)
Variable containing:
9
[torch.FloatTensor of size 1]
>>> x = Variable(Tensor([[ 3, 0, 0, 0 ]]))
>>> f(x, y)
Variable containing:
2.2500
[torch.FloatTensor of size 1]
```

The first parameter of a loss is traditionally called the **input** and the second the **target**. These two quantities may be of different dimensions or even types for some losses (e.g. for classification).

François Fleuret

EE-559 - Deep learning / 4b. PyTorch modules, batch processing

13 / 31

Remember that Module's' inputs and outputs are Variable's. Data Tensor's should be wrapped before forwarding them into a Module.

Conversely, results are also Variable s, so to retrieve a loss as an actual standard python float, one has to do

```
>>> f = torch.nn.L1Loss()
>>> u = f(Variable(Tensor([1, 2, 3])), Variable(Tensor([1, 2, 9])))
>>> u
Variable containing:
2
[torch.FloatTensor of size 1]
>>> u.data[0]
2.0
```

François Fleuret

EE-559 - Deep learning / 4b. PyTorch modules, batch processing

15 / 31



Criteria do not compute the gradient with respect to the target, and will not accept a Variable with requires_grad to True as the target.

We can use the MSE loss for training, even though this is classification.

To do so, given a training set

$$(x_n, y_n) \in \mathbb{R}^D \times \{1, \dots, C\}, \ n = 1, \dots, N,$$

we will consider an output with as many units as there are classes, and the target will be a tensor $z \in \mathbb{R}^{N \times C}$, with -1 everywhere but for the correct labels:

$$\forall n, z_{n,m} = \begin{cases} 1 & \text{if } m = y_n \\ -1 & \text{otherwise.} \end{cases}$$

For instance, with N=5 and C=3, we would have

$$\begin{pmatrix} 2\\1\\1\\3\\2 \end{pmatrix} \Rightarrow \begin{pmatrix} -1 & 1 & -1\\1 & -1 & -1\\1 & -1 & -1\\-1 & 1 & 1 \end{pmatrix}.$$

Although MSE is a regression loss, using it like this gives excellent results.

François Fleuret

EE-559 - Deep learning / 4b. PyTorch modules, batch processing

17 / 31

Both the convolutional and pooling layers take as input batches of samples, each one being itself a 3d tensor $C \times H \times W$.

The output has the same structure, and tensors have to be explicitly reshaped before being forwarded to a fully connected layer.

```
>>> mnist = datasets.MNIST('./data/mnist/', train = True, download = True)
>>> d = mnist.train_data
>>> d.size()
torch.Size([60000, 28, 28])
>>> x = d.view(d.size(0), 1, d.size(1), d.size(2))
>>> x.size()
torch.Size([60000, 1, 28, 28])
>>> x = x.view(x.size(0), -1)
>>> x.size()
torch.Size([60000, 784])
```

We can now put all this together and define our first convolutional network for MNIST, with two convolutional layers, and two fully-connected layers:

Input sizes / operations	Nb. parameters	Nb. products
$1 \times 28 \times 28$		
nn.Conv2d(1, 32, kernel_size=5)	$32 \times (5^2 + 1) = 832$	$32 \times 24^2 \times 5^2 = 460,800$
$32 \times 24 \times 24$		
<pre>F.max_pool2d(x, kernel_size=3)</pre>	0	0
$32 \times 8 \times 8$		
F.relu	0	0
$32 \times 8 \times 8$		
nn.Conv2d(32, 64, kernel_size=5)	$64 \times (32 \times 5^2 + 1) = 51,264$	$32 \times 64 \times 4^2 \times 5^2 = 819,200$
$64 \times 4 \times 4$		
<pre>F.max_pool2d(x, kernel_size=2)</pre>	0	0
$64 \times 2 \times 2$		
F.relu	0	0
$64 \times 2 \times 2$		
x.view(-1, 256)	0	0
256		
nn.Linear(256, 200)	$200 \times (256 + 1) = 51,400$	$200 \times 256 = 51,200$
200		
F.relu	0	0
200		
nn.Linear(200, 10)	$10 \times (200+1) = 2{,}010$	$10 \times 200 = 2,000$
10		

Total 105,506 parameters and 1,333,200 products for the forward pass.

François Fleuret EE-559 – Deep learning / 4b. PyTorch modules, batch processing

19 / 31

Creating a module

To create a Module, one has to inherit from the base class and implement the constructor $__init__(self, ...)$ and the forward pass forward(self, x).

```
class Net(nn.Module):
    def __init__(self):
        super(Net, self).__init__()
        self.conv1 = nn.Conv2d(1, 32, kernel_size=5)
        self.conv2 = nn.Conv2d(32, 64, kernel_size=5)
        self.fc1 = nn.Linear(256, 200)
        self.fc2 = nn.Linear(200, 10)

def forward(self, x):
        x = F.relu(F.max_pool2d(self.conv1(x), kernel_size=3, stride=3))
        x = F.relu(F.max_pool2d(self.conv2(x), kernel_size=2, stride=2))
        x = x.view(-1, 256)
        x = F.relu(self.fc1(x))
        x = self.fc2(x)
        return x
```

As long as you use autograd-compliant operations, the backward pass is implemented automatically.

François Fleuret

EE-559 - Deep learning / 4b. PyTorch modules, batch processing

21 / 31

Module's added as attributes are seen by Module.parameters(), which returns an iterator over the model's parameters for optimization.

```
class Net(nn.Module):
    def __init__(self):
        super(Net, self).__init__()
        self.conv1 = nn.Conv2d(1, 32, kernel_size=5)
        self.conv2 = nn.Conv2d(32, 64, kernel_size=5)
        self.fc1 = nn.Linear(256, 200)
        self.fc2 = nn.Linear(200, 10)

model = Net()

for k in model.parameters():
    print(k.size())
```

prints

```
torch.Size([32, 1, 5, 5])
torch.Size([32])
torch.Size([64, 32, 5, 5])
torch.Size([64])
torch.Size([200, 256])
torch.Size([200])
torch.Size([10, 200])
torch.Size([10])
```

Parameter's added as attributes are also seen by Module.parameters().



prints

prints

torch.Size([21])

Parameters added in dictionaries or arrays are not seen.

```
class Buggy(nn.Module):
    def __init__(self):
        super(Buggy, self).__init__()
        self.conv = nn.Conv2d(1, 32, kernel_size=5)
        self.param = Parameter(Tensor(123, 456))
        self.ouch = {}
        self.ouch[0] = nn.Linear(543, 21)

model = Buggy()

for k in model.parameters():
    print(k.size())

torch.Size([123, 456])
torch.Size([32, 1, 5, 5])
torch.Size([32])
```

François Fleuret

EE-559 - Deep learning / 4b. PyTorch modules, batch processing

23 / 31

The proper policy then is to use Module.add_module(name, module)

```
class NotBuggyAnymore(nn.Module):
    def __init__(self):
        super(NotBuggyAnymore, self).__init__()
        self.conv = nn.Conv2d(1, 32, kernel_size=5)
        self.param = Parameter(Tensor(123, 456))
        self.add_module('ahhh_0', nn.Linear(543, 21))

model = NotBuggyAnymore()

for k in model.parameters():
    print(k.size())

torch.Size([123, 456])
torch.Size([32], 1, 5, 5])
torch.Size([32])
torch.Size([31])
```

These modules are added as attributes, and can be accessed with getattr.

Module.register_parameter(name, parameter) allows to similarly register Parameter s explicitly.

Another option is to add modules in a field of type nn.ModuleList, which is a list of modules properly dealt with by PyTorch's machinery.

```
class AnotherNotBuggy(nn.Module):
    def __init__(self):
        super(AnotherNotBuggy, self).__init__()
        self.conv = nn.Conv2d(1, 32, kernel_size=5)
        self.param = Parameter(Tensor(123, 456))
        self.other_stuff = nn.ModuleList()
        self.other_stuff.append(nn.Linear(50, 75))
        self.other_stuff.append(nn.Linear(125, 999))

model = AnotherNotBuggy()

for k in model.parameters():
    print(k.size())
```

prints

```
torch.Size([123, 456])
torch.Size([32, 1, 5, 5])
torch.Size([32])
torch.Size([75, 50])
torch.Size([75])
torch.Size([999, 125])
torch.Size([999])
```

François Fleuret

EE-559 - Deep learning / 4b. PyTorch modules, batch processing

25 / 31

Batch processing

We saw that elements from torch.nn take as input a batch of samples, that is a tensor whose first index is the sample's index.

However we have formalized the fully connected layers and back-prop with column vectors *e.g.*

$$\forall I, n, \ w^{(I)} \in \mathbb{R}^{d_I \times d_{I-1}}, \ x_n^{(I-1)} \in \mathbb{R}^{d_{I-1}}, \ s_n^{(I)} = w^{(I)} x_n^{(I-1)}.$$

From now on, we will use row vectors, so that we can represent a series of samples as a 2d array with the first index being the sample's index.

$$x = \begin{pmatrix} x_{1,1} & \dots & x_{1,D} \\ \vdots & \ddots & \vdots \\ x_{N,1} & \dots & x_{N,D} \end{pmatrix} = \begin{pmatrix} (x_1)^T \\ \vdots \\ (x_N)^T \end{pmatrix},$$

which is an element of $\mathbb{R}^{N \times D}$.

François Fleuret

 ${\sf EE\text{-}559-Deep\ learning}\ /\ {\sf 4b.\ PyTorch\ modules,\ batch\ processing}$

27 / 31

To make all sample row vectors and apply a linear operator, we want

$$\forall n, \ s_n^{(l)} = \left(w^{(l)} \left(x_n^{(l-1)}\right)^T\right)^T = x_n^{(l-1)} \left(w^{(l)}\right)^T$$

which gives a tensorial expression for the full batch

$$s^{(l)} = x^{(l-1)} \left(w^{(l)} \right)^T.$$

And in torch/nn/functional.py

```
def linear(input, weight, bias=None):
   if input.dim() == 2 and bias is not None:
      # fused op is marginally faster
      return torch.addmm(bias, input, weight.t())

output = input.matmul(weight.t())
if bias is not None:
      output += bias
return output
```

Similarly for the backward pass of a linear layer we get

$$\left[\!\left[\frac{\partial \mathcal{L}}{\partial w^{(l)}}\right]\!\right] = \left[\!\left[\frac{\partial \mathcal{L}}{\partial x^{(l)}}\right]\!\right]^T x^{(l-1)},$$

and

$$\left[\left[\frac{\partial \mathcal{L}}{\partial x^{(l)}}\right]\right] = \left[\left[\frac{\partial \ell}{\partial x^{(l+1)}}\right]\right] w^{(l+1)}.$$

François Fleuret

 ${\sf EE\text{-}559-Deep\ learning}\ /\ {\sf 4b.\ PyTorch\ modules},\ {\sf batch\ processing}$

29 / 31

Batch processing allows to use efficient matrix product implementations, which in particular deal properly with cache memory

```
import torch, time
def timing(x, w, nb = 51):
    t = torch.FloatTensor(nb)
    for u in range(t.size(0)):
         t0 = time.perf_counter()
         # Batch processing
         y = x.mm(w.t())
         y.is_cuda and torch.cuda.synchronize()
         t[u] = time.perf_counter() - t0
    tb = t.median()[0][0]
    for u in range(t.size(0)):
         t0 = time.perf_counter()
         # Ugly loop
         for k in range(y.size(0)): y[k] = w.mv(x[k])
         y.is_cuda and torch.cuda.synchronize()
t[u] = time.perf_counter() - t0
    t1 = t.median()[0][0]
    print('\{:s\} batch vs. loop speed ratio \{:.01f\}'
           .format((y.is_cuda and 'GPU') or 'CPU', tl / tb))
x = torch.FloatTensor(2500, 1000).normal_()
w = torch.FloatTensor(1500, 1000).normal_()
timing(x, w)
x = torch.cuda.FloatTensor(2500, 1000).normal_()
w = torch.cuda.FloatTensor(1500, 1000).normal_()
timing(x, w)
```

Prints:

```
CPU batch vs. loop speed ratio 10.0 GPU batch vs. loop speed ratio 80.7
```

Practical session:

https://fleuret.org/dlc/dlc-practical-4.pdf

François Fleuret

EE-559 - Deep learning / 4b. PyTorch modules, batch processing

31 / 31