EE-559 - Deep learning

7.2. Networks for image classification

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Image classification, standard convnets

The most standard networks for image classification are the LeNet family (leCun et al., 1998), and its modern extensions, among which AlexNet (Krizhevsky et al., 2012) and VGGNet (Simonyan and Zisserman, 2014).

They share a common structure of several convolutional layers seen as a feature extractor, followed by fully connected layers seen as a classifier.

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The performance of AlexNet was a wake-up call for the computer vision community, as it vastly out-performed other methods in spite of its simplicity.

Recent advances rely on moving from standard convolutional layers to local complex architectures to reduce the model size.

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import torchvision
alexnet = torchvision.models.alexnet()

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The networks from PyTorch listed in the coming slides may differ slightly from the reference papers which introduced them historically.

LeNet5 (LeCun et al., 1989). 10 classes, input $1 \times 28 \times 28$.

```
(features): Sequential (
  (0): Conv2d(1, 6, kernel_size=(5, 5), stride=(1, 1))
  (1): ReLU (inplace)
  (2): MaxPool2d (size=(2, 2), stride=(2, 2), dilation=(1, 1))
  (3): Conv2d(6, 16, kernel_size=(5, 5), stride=(1, 1))
  (4): ReLU (inplace)
  (5): MaxPool2d (size=(2, 2), stride=(2, 2), dilation=(1, 1))
)

(classifier): Sequential (
  (0): Linear (256 -> 120)
  (1): ReLU (inplace)
  (2): Linear (120 -> 84)
  (3): ReLU (inplace)
  (4): Linear (84 -> 10)
)
```

Alexnet (Krizhevsky et al., 2012). 1,000 classes, input $3 \times 224 \times 224$.

```
(features): Sequential (
 (0): Conv2d(3, 64, kernel size=(11, 11), stride=(4, 4), padding=(2, 2))
 (1): ReLU (inplace)
 (2): MaxPool2d (size=(3, 3), stride=(2, 2), dilation=(1, 1))
 (3): Conv2d(64, 192, kernel_size=(5, 5), stride=(1, 1), padding=(2, 2))
 (4): ReLU (inplace)
 (5): MaxPool2d (size=(3, 3), stride=(2, 2), dilation=(1, 1))
 (6): Conv2d(192, 384, kernel_size=(3, 3), stride=(1, 1), padding=(1, 1))
 (7): ReLU (inplace)
 (8): Conv2d(384, 256, kernel_size=(3, 3), stride=(1, 1), padding=(1, 1))
 (9): ReLU (inplace)
 (10): Conv2d(256, 256, kernel size=(3, 3), stride=(1, 1), padding=(1, 1))
 (11): ReLU (inplace)
 (12): MaxPool2d (size=(3, 3), stride=(2, 2), dilation=(1, 1))
(classifier): Sequential (
 (0): Dropout (p = 0.5)
 (1): Linear (9216 -> 4096)
 (2): ReLU (inplace)
 (3): Dropout (p = 0.5)
 (4): Linear (4096 -> 4096)
 (5): ReLU (inplace)
 (6): Linear (4096 -> 1000)
```

Krizhevsky et al. used data augmentation during training to reduce over-fitting.

They generated 2,048 samples from every original training example through two classes of transformations:

- crop a 224×224 image at a random position in the original 256×256 , and randomly reflect it horizontally,
- apply a color transformation using a PCA model of the color distribution.

Krizhevsky et al. used data augmentation during training to reduce over-fitting.

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- crop a 224×224 image at a random position in the original 256×256 , and randomly reflect it horizontally,
- apply a color transformation using a PCA model of the color distribution.

During test the prediction is averaged over five random crops and their horizontal reflections.

VGGNet19 (Simonyan and Zisserman, 2014). 1,000 classes, input $3 \times 224 \times 224$. 16 convolutional layers + 3 fully connected layers.

```
(features): Sequential (
    (0): Conv2d(3, 64, kernel size=(3, 3), stride=(1, 1), padding=(1, 1))
    (1): ReLU (inplace)
    (2): Conv2d(64, 64, kernel size=(3, 3), stride=(1, 1), padding=(1, 1))
    (3): ReLU (inplace)
    (4): MaxPool2d (size=(2, 2), stride=(2, 2), dilation=(1, 1))
    (5): Conv2d(64, 128, kernel_size=(3, 3), stride=(1, 1), padding=(1, 1))
    (6): ReLU (inplace)
    (7): Conv2d(128, 128, kernel_size=(3, 3), stride=(1, 1), padding=(1, 1))
    (8): ReLU (inplace)
    (9): MaxPool2d (size=(2, 2), stride=(2, 2), dilation=(1, 1))
    (10): Conv2d(128, 256, kernel_size=(3, 3), stride=(1, 1), padding=(1, 1))
    (11): ReLU (inplace)
    (12): Conv2d(256, 256, kernel_size=(3, 3), stride=(1, 1), padding=(1, 1))
    (13): ReLU (inplace)
    (14): Conv2d(256, 256, kernel_size=(3, 3), stride=(1, 1), padding=(1, 1))
    (15): ReLU (inplace)
    (16): Conv2d(256, 256, kernel_size=(3, 3), stride=(1, 1), padding=(1, 1))
    (17): ReLU (inplace)
    (18): MaxPool2d (size=(2, 2), stride=(2, 2), dilation=(1, 1))
    (19): Conv2d(256, 512, kernel_size=(3, 3), stride=(1, 1), padding=(1, 1))
    (20): ReLU (inplace)
    (21): Conv2d(512, 512, kernel_size=(3, 3), stride=(1, 1), padding=(1, 1))
    (22): ReLU (inplace)
    (23): Conv2d(512, 512, kernel_size=(3, 3), stride=(1, 1), padding=(1, 1))
    (24): ReLU (inplace)
   (25): Conv2d(512, 512, kernel size=(3, 3), stride=(1, 1), padding=(1, 1))
    (26): ReLU (inplace)
   (27): MaxPool2d (size=(2, 2), stride=(2, 2), dilation=(1, 1))
1.../
```

VGGNet19 (cont.)

```
(classifier): Sequential (
  (0): Linear (25088 -> 4096)
  (1): ReLU (inplace)
  (2): Dropout (p = 0.5)
  (3): Linear (4096 -> 4096)
  (4): ReLU (inplace)
  (5): Dropout (p = 0.5)
  (6): Linear (4096 -> 1000)
```

We can illustrate the convenience of these pre-trained models on a simple image-classification problem.



To be sure this picture did not appear in the training data, it was not taken from the web.

```
import PIL, torch, torchvision
# Imagenet class names
class_names = eval(open('imagenet1000_clsid_to_human.txt', 'r').read())
# Load and normalize the image
to_tensor = torchvision.transforms.ToTensor()
img = to_tensor(PIL.Image.open('example_images/blacklab.jpg'))
img = img.view(1, img.size(0), img.size(1), img.size(2))
img = 0.5 + 0.5 * (img - img.mean()) / img.std()
```

```
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img = 0.5 + 0.5 * (img - img.mean()) / img.std()
# Load and evaluate the network
alexnet = torchvision.models.alexnet(pretrained = True)
alexnet.eval()
output = alexnet(img)
# Prints the classes
scores, indexes = output.view(-1).sort(descending = True)
for k in range(15):
    print('%.02f' % scores[k].item(), class_names[indexes[k].item()])
```



- 12.26 Weimaraner
- 10.95 Chesapeake Bay retriever
- 10.87 Labrador retriever
- 10.10 Staffordshire bullterrier, Staffordshire bull terrier
- 9.55 flat-coated retriever
- 9.40 Italian greyhound
- 9.31 American Staffordshire terrier, Staffordshire terrier, American pit bull terrier, pit bull terrier
- 9.12 Great Dane
- 8.94 German short-haired pointer
- 8.53 Doberman, Doberman pinscher
- 8.35 Rottweiler
- 8.25 kelpie
- 8.24 barrow, garden cart, lawn cart, wheelbarrow
- 8.12 bucket, pail
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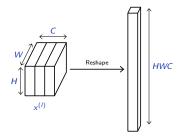
Weimaraner

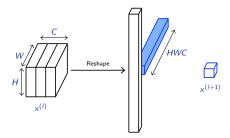


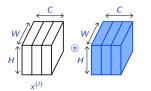
Chesapeake Bay retriever

Fully convolutional networks

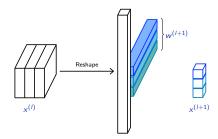


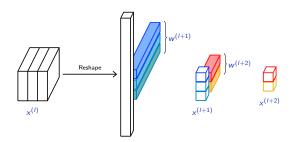


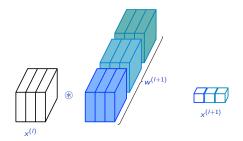


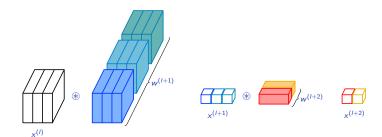




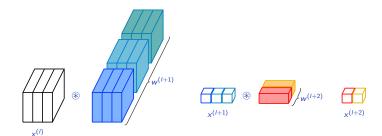




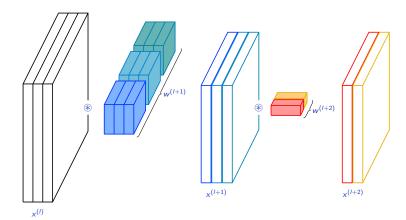




This "convolutionization" does not change anything if the input size is such that the output has a single spatial cell, but it fully re-uses computation to get a prediction at multiple locations when the input is larger.



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We can write a routine that transforms a series of layers from a standard convnets to make it fully convolutional:

```
def convolutionize(layers, input_size):
   result_layers = []
   x = torch.zeros((1, ) + input_size)
   for m in layers:
        if isinstance(m. torch.nn.Linear):
            n = torch.nn.Conv2d(in_channels = x.size(1),
                                out channels = m.weight.size(0).
                                kernel_size = (x.size(2), x.size(3)))
            with torch.no_grad():
                n.weight.view(-1).copy_(m.weight.view(-1))
                n.bias.view(-1).copy_(m.bias.view(-1))
            m = n
        result_layers.append(m)
        x = m(x)
    return result_layers
```



This function makes the [strong and disputable] assumption that only nn. Linear has to be converted.

To apply this to AlexNet

```
model = torchvision.models.alexnet(pretrained = True)
print(model)

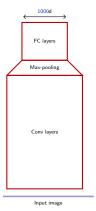
layers = list(model.features) + list(model.classifier)

model = nn.Sequential(*convolutionize(layers, (3, 224, 224)))
print(model)
```

```
AlexNet (
  (features): Sequential (
    (0): Conv2d(3, 64, kernel_size=(11, 11), stride=(4, 4), padding=(2, 2))
    (1): ReLU (inplace)
    (2): MaxPool2d (size=(3, 3), stride=(2, 2), dilation=(1, 1))
    (3): Conv2d(64, 192, kernel_size=(5, 5), stride=(1, 1), padding=(2, 2))
    (4): ReLU (inplace)
    (5): MaxPool2d (size=(3, 3), stride=(2, 2), dilation=(1, 1))
    (6): Conv2d(192, 384, kernel size=(3, 3), stride=(1, 1), padding=(1, 1))
    (7): ReLU (inplace)
    (8): Conv2d(384, 256, kernel_size=(3, 3), stride=(1, 1), padding=(1, 1))
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    (10): Conv2d(256, 256, kernel_size=(3, 3), stride=(1, 1), padding=(1, 1))
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```
Sequential (
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  (11): ReLU (inplace)
  (12): MaxPool2d (size=(3, 3), stride=(2, 2), dilation=(1, 1))
  (13): Dropout (p = 0.5)
  (14): Conv2d(256, 4096, kernel size=(6, 6), stride=(1, 1))
  (15): ReLU (inplace)
  (16): Dropout (p = 0.5)
  (17): Conv2d(4096, 4096, kernel_size=(1, 1), stride=(1, 1))
  (18): ReLU (inplace)
  (19): Conv2d(4096, 1000, kernel size=(1, 1), stride=(1, 1))
```

In their "overfeat" approach, Sermanet et al. (2013) combined this with a stride $\bf 1$ final max-pooling to get multiple predictions.



AlexNet random cropping

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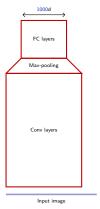
AlexNet random cropping



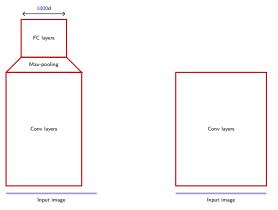
AlexNet random cropping



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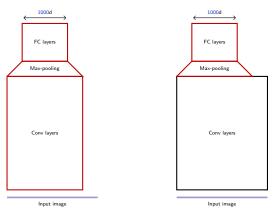


AlexNet random cropping



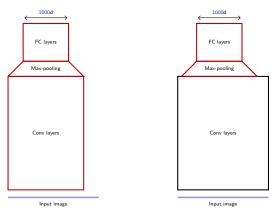
AlexNet random cropping

Overfeat dense max-pooling



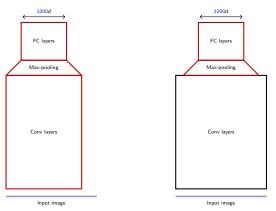
AlexNet random cropping

Overfeat dense max-pooling



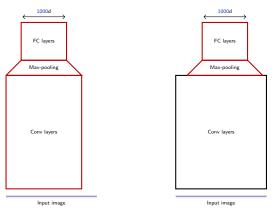
AlexNet random cropping

Overfeat dense max-pooling



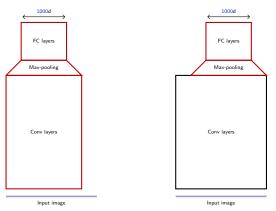
AlexNet random cropping

Overfeat dense max-pooling



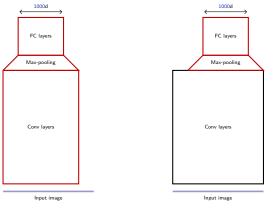
AlexNet random cropping

Overfeat dense max-pooling



AlexNet random cropping

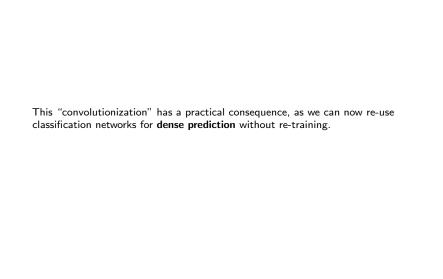
Overfeat dense max-pooling

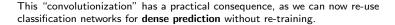


AlexNet random cropping

Overfeat dense max-pooling

Doing so, they could afford parsing the scene at 6 scales to improve invariance.





Also, and maybe more importantly, it blurs the conceptual boundary between "features" and "classifier" and leads to an intuitive understanding of convnet activations as gradually transitioning from appearance to semantic.

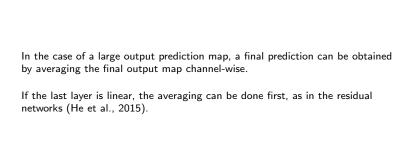
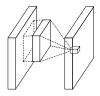
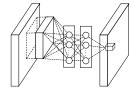


Image classification, network in network

Lin et al. (2013) re-interpreted a convolution filter as a one-layer perceptron, and extended it with an "MLP convolution" (aka "network in network") to improve the capacity vs. parameter ratio.

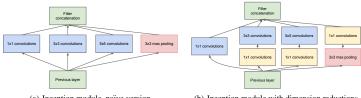




(Lin et al., 2013)

As for the fully convolutional networks, such local MLPs can be implemented with 1×1 convolutions.

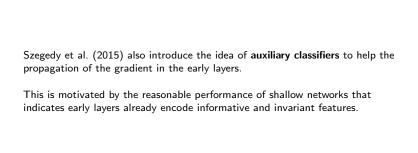
The same notion was generalized by Szegedy et al. (2015) for their GoogLeNet, through the use of module combining convolutions at multiple scales to let the optimal ones be picked during training.



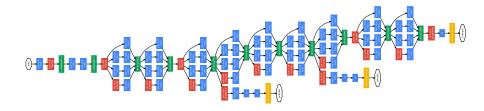
(a) Inception module, naïve version

(b) Inception module with dimension reductions

(Szegedy et al., 2015)



The resulting GoogLeNet has 12 times less parameters than AlexNet and is more accurate on ILSVRC14 (Szegedy et al., 2015).



(Szegedy et al., 2015)

It was later extended with techniques we are going to see in the next slides: batch-normalization (loffe and Szegedy, 2015) and pass-through à la resnet (Szegedy et al., 2016).

Image classification, residual networks

We already saw the structure of the residual networks and how well they perform on CIFAR10 (He et al., 2015).

The default residual block proposed by He et al. is of the form



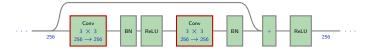
and as such requires $2 \times (3 \times 3 \times 64 + 1) \times 64 \simeq 73k$ parameters.

To apply the same architecture to ImageNet, more channels are required, e.g.



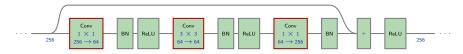
However, such a block requires $2 \times (3 \times 3 \times 256 + 1) \times 256 \simeq 1.2 m$ parameters.

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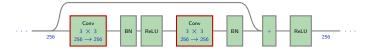
However, such a block requires $2 \times (3 \times 3 \times 256 + 1) \times 256 \simeq 1.2 m$ parameters.

They mitigated that requirement with what they call a bottleneck block:



$$256 \times 64 + (3 \times 3 \times 64 + 1) \times 64 + 64 \times 256 \simeq 70k$$
 parameters.

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However, such a block requires $2 \times (3 \times 3 \times 256 + 1) \times 256 \simeq 1.2m$ parameters.

They mitigated that requirement with what they call a **bottleneck** block:



$$256 \times 64 + (3 \times 3 \times 64 + 1) \times 64 + 64 \times 256 \simeq 70k$$
 parameters.

The encoding pushed between blocks is high-dimensional, but the "contextual reasoning" in convolutional layers is done on a simpler feature representation.

layer name	output size	18-layer	34-layer	50-layer	101-layer	152-layer
conv1	112×112	7×7, 64, stride 2				
				3×3 max pool, stric	le 2	
conv2_x	56×56	[3×3, 64]×2	$\left[\begin{array}{c} 3\times3,64\\ 3\times3,64 \end{array}\right]\times3$	$\begin{bmatrix} 1 \times 1, 64 \\ 3 \times 3, 64 \\ 1 \times 1, 256 \end{bmatrix} \times 3$	$\begin{bmatrix} 1 \times 1, 64 \\ 3 \times 3, 64 \\ 1 \times 1, 256 \end{bmatrix} \times 3$	\[\begin{array}{c} 1 \times 1, 64 \\ 3 \times 3, 64 \\ 1 \times 1, 256 \end{array} \times 3
conv3_x	28×28	$\left[\begin{array}{c} 3\times3,128\\ 3\times3,128 \end{array}\right]\times2$	$\left[\begin{array}{c} 3{\times}3,128 \\ 3{\times}3,128 \end{array}\right]{\times}4$	\[\begin{array}{c} 1 \times 1, 128 \\ 3 \times 3, 128 \\ 1 \times 1, 512 \end{array} \] \times 4	\[\begin{array}{c} 1 \times 1, 128 \\ 3 \times 3, 128 \\ 1 \times 1, 512 \end{array} \times 4	\[\begin{array}{c} 1 \times 1, 128 \\ 3 \times 3, 128 \\ 1 \times 1, 512 \end{array} \times 8
conv4_x	14×14	$\left[\begin{array}{c} 3\times3,256\\ 3\times3,256 \end{array}\right]\times2$	$\left[\begin{array}{c} 3 \times 3, 256 \\ 3 \times 3, 256 \end{array}\right] \times 6$	\[\begin{array}{c} 1 \times 1, 256 \\ 3 \times 3, 256 \\ 1 \times 1, 1024 \end{array} \] \times 6	\[\begin{array}{c} 1 \times 1, 256 \\ 3 \times 3, 256 \\ 1 \times 1, 1024 \end{array} \] \times 23	\[\begin{array}{c} 1 \times 1, 256 \\ 3 \times 3, 256 \\ 1 \times 1, 1024 \end{array} \times 36
conv5_x	7×7	$\left[\begin{array}{c} 3\times3,512\\ 3\times3,512 \end{array}\right]\times2$	$\left[\begin{array}{c} 3\times3,512\\ 3\times3,512 \end{array}\right]\times3$	\[\begin{array}{c} 1 \times 1, 512 \\ 3 \times 3, 512 \\ 1 \times 1, 2048 \end{array} \] \times 3	\[\begin{array}{c} 1 \times 1, 512 \\ 3 \times 3, 512 \\ 1 \times 1, 2048 \end{array} \] \times 3	\[\begin{array}{c} 1 \times 1, 512 \\ 3 \times 3, 512 \\ 1 \times 1, 2048 \end{array} \times 3
	1×1			erage pool, 1000-d fc,		
FLOPs		1.8×10 ⁹	3.6×10^{9}	3.8×10^{9}	7.6×10 ⁹	11.3×10 ⁹

Table 1. Architectures for ImageNet. Building blocks are shown in brackets (see also Fig. 5), with the numbers of blocks stacked. Downsampling is performed by conv3_1, conv4_1, and conv5_1 with a stride of 2.

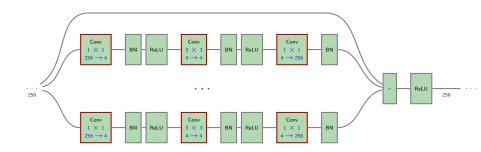
(He et al., 2015)

method	top-5 err. (test)	
VGG [41] (ILSVRC'14)	7.32	
GoogLeNet [44] (ILSVRC'14)	6.66	
VGG [41] (v5)	6.8	
PReLU-net [13]	4.94	
BN-inception [16]	4.82	
ResNet (ILSVRC'15)	3.57	

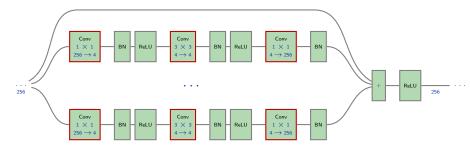
Table 5. Error rates (%) of **ensembles**. The top-5 error is on the test set of ImageNet and reported by the test server.

(He et al., 2015)

This was extended to the ResNeXt architecture by Xie et al. (2016), with blocks with similar number of parameters, but split into 32 "aggregated" pathways.



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When equalizing the number of parameters, this architecture performs better than a standard resnet.

Image classification, summary

To summarize roughly the evolution of convnets for image classification:

- standard ones are extensions of LeNet5,
- everybody loves ReLU,
- state-of-the-art networks have 100s of channels and 10s of layers,

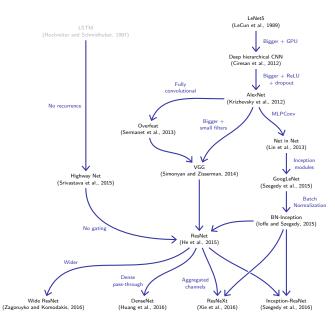
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- standard ones are extensions of LeNet5,
- everybody loves ReLU.
- state-of-the-art networks have 100s of channels and 10s of layers,
- they can (should?) be fully convolutional,
- pass-through connections allow deeper "residual" nets,
- bottleneck local structures reduce the number of parameters,
- aggregated pathways reduce the number of parameters.

Image classification networks





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