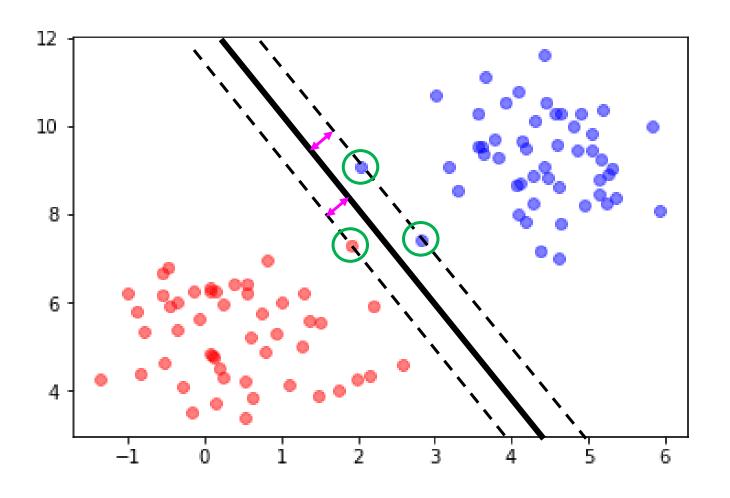


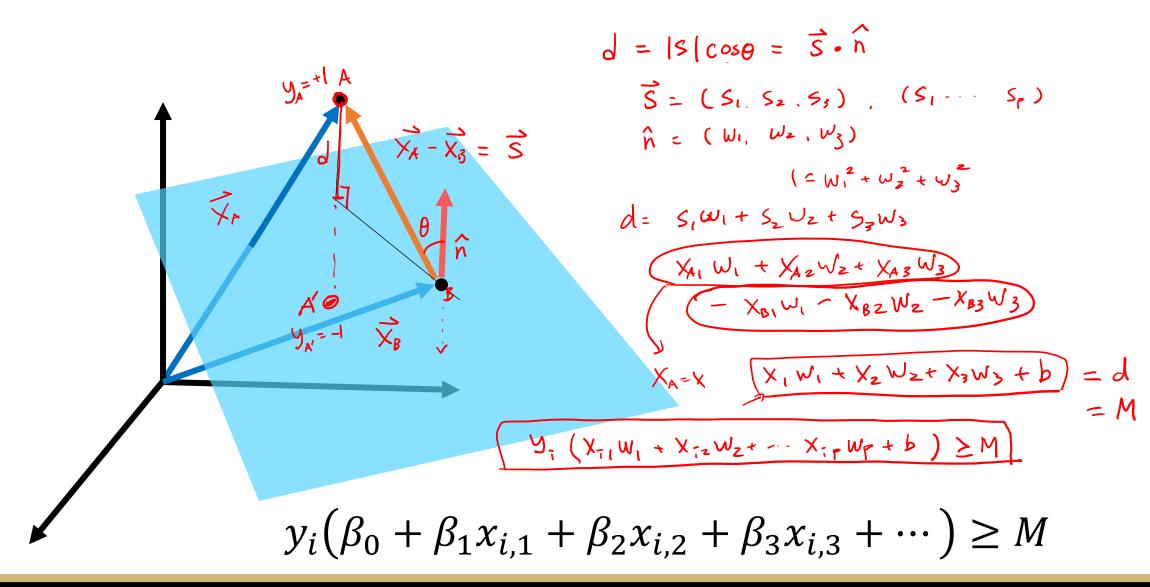
Maximum margin classifier



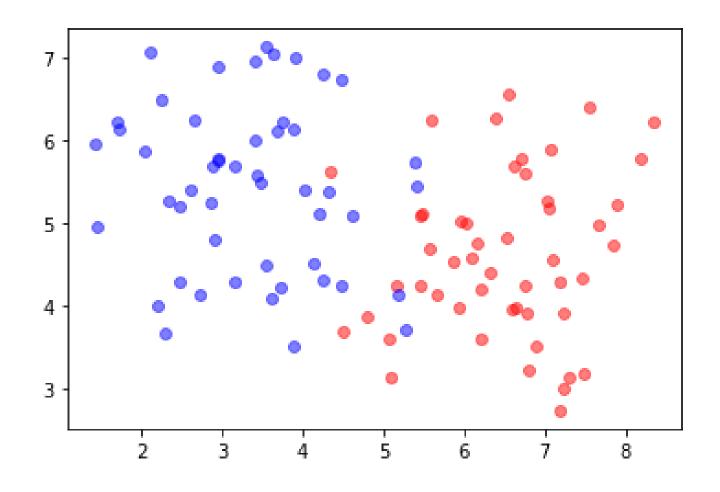
Support

Margin

Maximum margin classifier

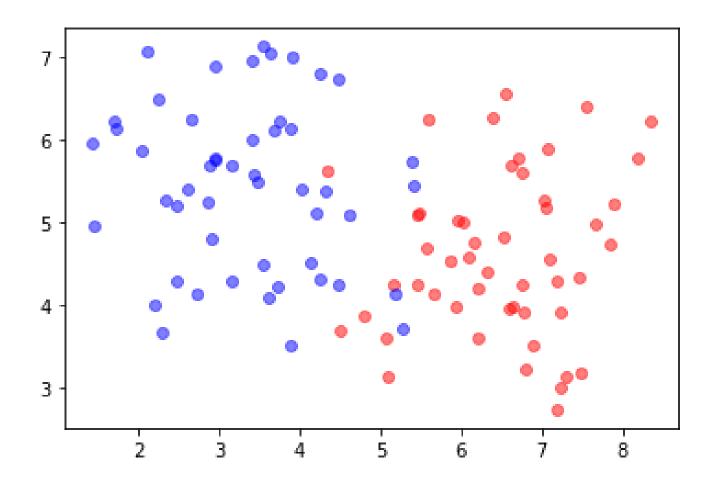


The impossible case...



Can you separate this with a hyperplane?

How to deal with an inseparable case



We'll have to accept some errors by softening the margin

"soft margin classifier"

or called "support vector classifier"

Soft margin classifier

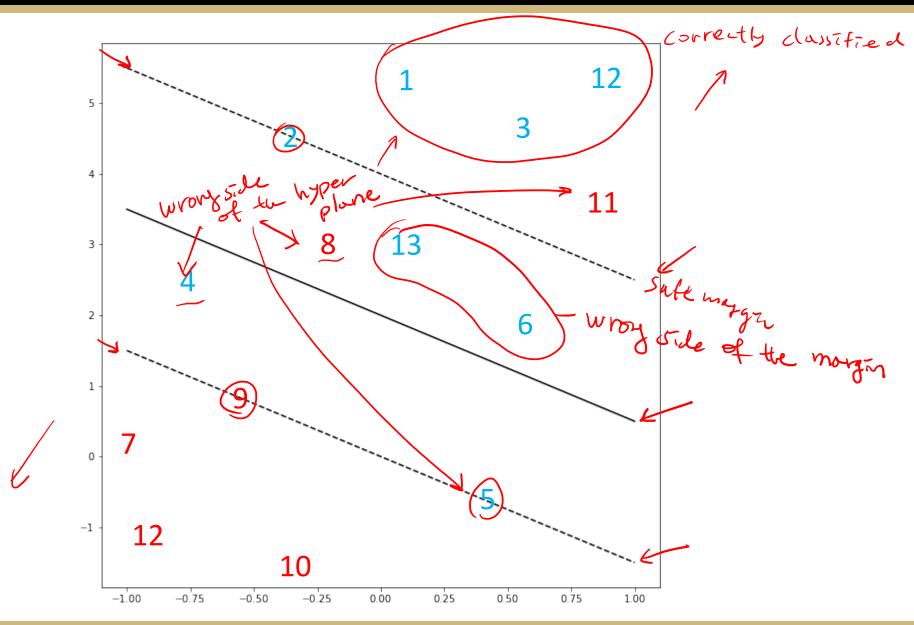
$$y_{i}(\beta_{0} + \beta_{1}x_{i,1} + \beta_{2}x_{i,2} + \beta_{3}x_{i,3} + \cdots) \geq M(1 - \epsilon_{i})$$

$$\sum_{j}^{p} \beta_{j}^{2} = 1$$

$$\epsilon_{i} \geq 0 \qquad \sum_{i}^{n} \epsilon_{i} \leq C$$

$$\beta_{i} \leq C$$

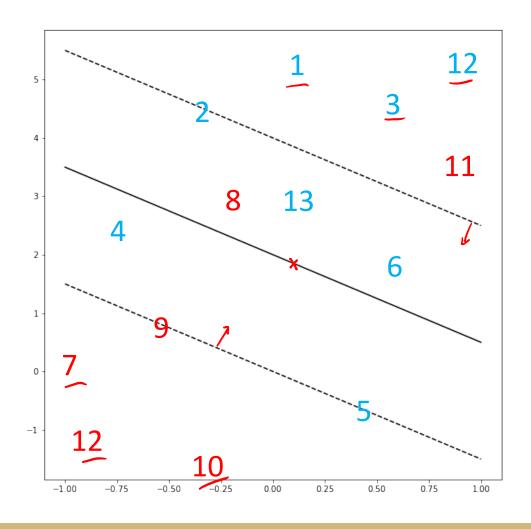
Soft margin classifier



Quiz: Soft margin classifier

$$y_i(\beta_0 + \beta_1 x_{i1} + \beta_2 x_{i2} + \ldots + \beta_p x_{ip}) \ge M(1 - \epsilon_i)$$

$$\epsilon_i \ge 0$$



Correct side of the margin
 \(\xi_1 = \circ\)

wrong side of the hyperplane
 1<2;

$$y_i(\beta_0 + \beta_1 x_{i1} + \beta_2 x_{i2} + \dots + \beta_p x_{ip}) \ge M(1 - \epsilon_i)$$

$$\epsilon_i \ge 0$$

$$\underline{n}$$

$$\sum_{i=1}^{n} \epsilon_i \le C$$

C is an error budget

C bounds both number and severity of violations

C is a hyperparameter

Q1. What's the maximum number of supports on the wrong side the hyperplane given C?

Q2. What happens to the margin M when C decreases?

Q3. What happens to the bias and variance when C is small?

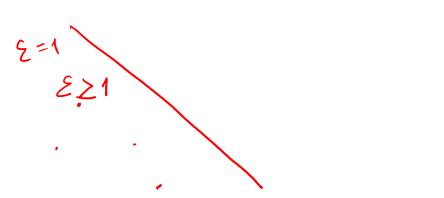
Q1. What's the maximum number of supports on the wrong side the hyperplane given C?

ANS: C

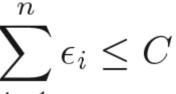
$$y_i(\beta_0 + \beta_1 x_{i1} + \beta_2 x_{i2} + \ldots + \beta_p x_{ip}) \ge M(1 - \epsilon_i)$$

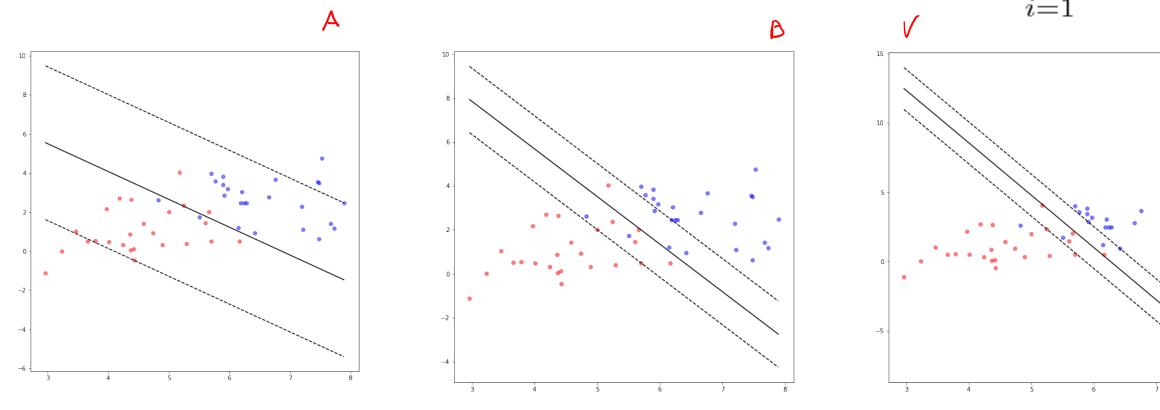
$$\epsilon_i \ge 0$$

$$\sum_{i=1}^{n} \epsilon_i \le C$$



Q2. What happens to the margin when C decreases?



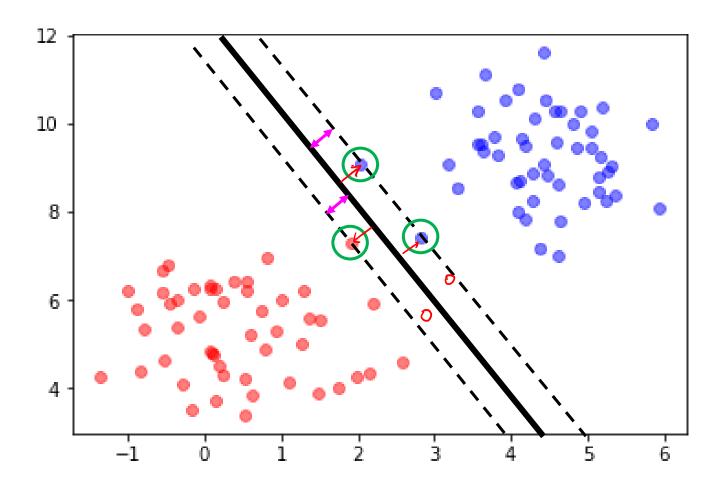


ANS: the margin becomes narrower

Q3. What happens to the bias and variance when C is small?

ANS: small C gives lower bias and higher variance

Recap



Support

Margin

$$y_i(\beta_0 + \beta_1 x_{i,1} + \beta_2 x_{i,2} + \beta_3 x_{i,3} + \cdots) \ge M(1 - \epsilon_i)$$

$$\epsilon_i \ge 0$$

$$\sum_{i=1}^{n} \epsilon_i \le C$$

Beyond linearly separable data

How can we separate this kind of data with SVC?

