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CS180 Spring 2010 - Midterm

Wednesday, April 28, 2010

You will have 110 minutes to take this exam. This exam is closed-book and closed-notes. There are 5 questions for a total of 100 points. Please write your name and student ID on every page of your solutions. Please use separate pages for each question.

Question	Points
1	18
2	18
3	20
4	7
5	17
Total	80

Llass Average (mean): 50.2

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1. [20 points] Suppose we are given n men and n women along with their preference lists. Recall that a valid partnership is a pair (m, w) consisting of a man and a woman such that there is some stable matching which contains (m, w). Describe a polynomial time algorithm in high-level pseudocode to determine if there is a stable matching which simultaneously pairs each man with his best valid partner and each woman with her best valid partner. Prove that your algorithm is correct and give its running time (you may use the Gale-Shapley algorithm as a subroutine).

The sple-shapley olgorithm alvers favors the person being the matched and alvers gives lie Teast preference watched to the preson thosen for the person being matched.

In order to seest there is a mothing which give both genders their best valled partner, we weed to run the algorithms liner. Once with the new being the choosers and ence with the women being the choosers

running time?

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2. [20 points] We are given a set of n jobs, each with a processing time p_i and a weight w_i , where the weight represents the job's priority. Let C_i denote the completion time of job i. For example, if job j is the first job to be completed, then its completion time is $C_j = p_j$. If job j completes right after job i, then j's completion time is $C_j = C_i + p_j$. Design an efficient algorithm in high-level pseudocode to determine an ordering of the jobs so as to minimize the weighted sum of completion times $\sum_{i=1}^{n} w_i C_i$. Prove that your algorithm is correct and state its running time.

The optimal algorithm is to take all the jobs and find out what their rates of weight to processing time is (wilpi). Then soit the jobs from largest tismaliest. This ensures that the weight per unit time is always decreasing them; if you routine sobs in this order, you wilged the lowest weight som

Let us look at inversions to prove that our solution is rorrect.

Take any two adjacent jobs and assume that job a your before

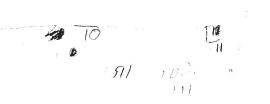
Job b, but Job b has a higher weight to line to the (Fi) than a.

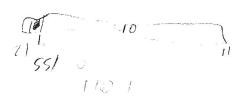
So, Ca & Cb and rakeb. Then, total case is (x+pa). rapa + (x+pa+pb) rape

(a=(x+pa and (b=(x+pa+pb)))

In normal english this will always be more thank the intersement was received because a higher cost times more time will always be more than a lover of the same amount of the same and of the same are that all inversions are voise than it they were santched. So, the optimal solution must have no inversions, so the optimal solution and the form inghest places of a pine.

Prove cost after swap = cost before swap





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3. [20 points] In the Maximum Tri-Partition problem, we are given an undirected graph G = (V, E) along with an integer k. We are asked to determine whether there exist disjoint sets V_1, V_2 , and V_3 whose union is V such that there are at least k edges of E whose endpoints are not in the same set V_i . Prove that this problem is NP-Complete.

This problem is No because to check the solution, ac would only have to whick each edge and keep a tally of how many edges straddled the sets. It that tally was greater than or equal to 15, then we could verify that the solution was correct.

3 Glar Ep Tri Partition

we will construct a graph where each node stands lower of and what needs to be idealed and couch edge connects had adjusted areas on the stand.

Then we pass this araph into the partition with the value K equal to the lotal number of edges in the graph. It it succeeds, that mens we have three disjoint sets where each node is not touching any other node in the set. Thus, we can pack one color for each set and be grapenized that we had adjacent areas have the same color.

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4. [20 points] You are given a minimum spanning tree T of an undirected graph G = (V, E) with weights on the edges. Now, you have been told that the weight of a particular edge e in G has all of a sudden been increased, giving us a new graph G'. Describe, in high-level pseudocode, an algorithm to compute a minimum spanning tree T' in G' that runs in time O(|V| + |E|). You may assume that all edge weights in G and G' are distinct.

The only edges we may need to change are with mac agreety.

The only edges we may need to change are

Those edges larger than e before its size

So, be each edge larger than convened to see It it

sty we need to remove e and all edges larger than e before adds site was increased. Then we need to run the minimum spanning free algorithm again starting at piece ellold sites and continuing assist if had left off there.

not linear.

It e \$7, do nothing.

If e \$7, do nothing.

If e \$7, remove e. This creates a cat (segments the graph). Add the 19 htest edge that rejoins the graph. spanning tree.

The two segments of the graphero \$5,0 V-S.

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5. (a) [10 points] For any problem $B \in \mathbb{NP}$, give an algorithm which solves B in time $O(2^{p(n)})$, where n is the size of the input and p(n) is some polynomial which may depend on B.

(b) [10 points] Consider the following decision version of the Minimum Spanning Tree problem, which we will call D-MST: Given an undirected graph G with weights on the edges and an integer k, is there a Minimum Spanning Tree of total weight at most k. A friend of yours comes to you and claims they have a proof that D-MST reduces to the Traveling Salesman Problem (i.e. TSP) in polynomial time. That is, they claim D-MST ≤_p TSP. Your friend plans on writing up his solution very carefully and sending it to the most prestigious conference in computer science. Assuming your friend has not made any mistakes, do you feel that this result is important enough to get published? Explain your answer in detail.

A. All NP problems are about finding some combination of values to content finding some combination of values to come up ustill curry possible combination of the inputs and give them to the verifier. They all possible combinations will be checked and it will take Irla time to complete.

where do we get pln)?

b. No, this is not important. We already know that minimum spanning tree can be solved in polynomial time or less without being reduced to anything else. There is already a deterministic algorithm to solve it the way to solve the decision, problem is losole the minimum spanning tree then see of the total writing. The minimum spanning tree then see of the total writing. It was then K. Since this can already be done faster than Irse than K. Since this can already be done faster than