

Array Problems - II & Time/Space Complexity

Foundation Course on Data Structures & Algorithm - Part I

Questions:

1

Linear Search in an array

T.C
→ $O(n)$

Reverse an Array

→ $O(n)$

find max and min element in an array

→ $O(n)$

Swap Alternates in an array

→ $O(n)$

Sort an Array of 0, 1 and 2

Move all negative number to one side of array

Find union and intersection of 2 sorted arrays

Program to cyclically rotate an array by one

find duplicate in an array of N+1 integers

find the pair that sum to a given value



find the triplet that sum to a given value

Check whether an array is palindrome or not

Minimum swaps required bring elements less equal k together

→ SW

Unique Number of Occurrences - Leetcode

Kadane's Algo

Questions:

~~Find common elements in 3 sorted arrays~~

Find first repeating element in array

Find first non-repeating element in an array

Find subarrays with equal 0s and 1s

Find subarray with 0 Sum in an array

find factorial of a Large Number

Minimum Platforms Problem - GFG

Minimise the Heights II - GFG

Majority Element Problem in array - GFG

Array SubSet of another array

→ Array Problems: - → Largest sum continuous Subarray

→ Kadane Algo: -

→ Brute force

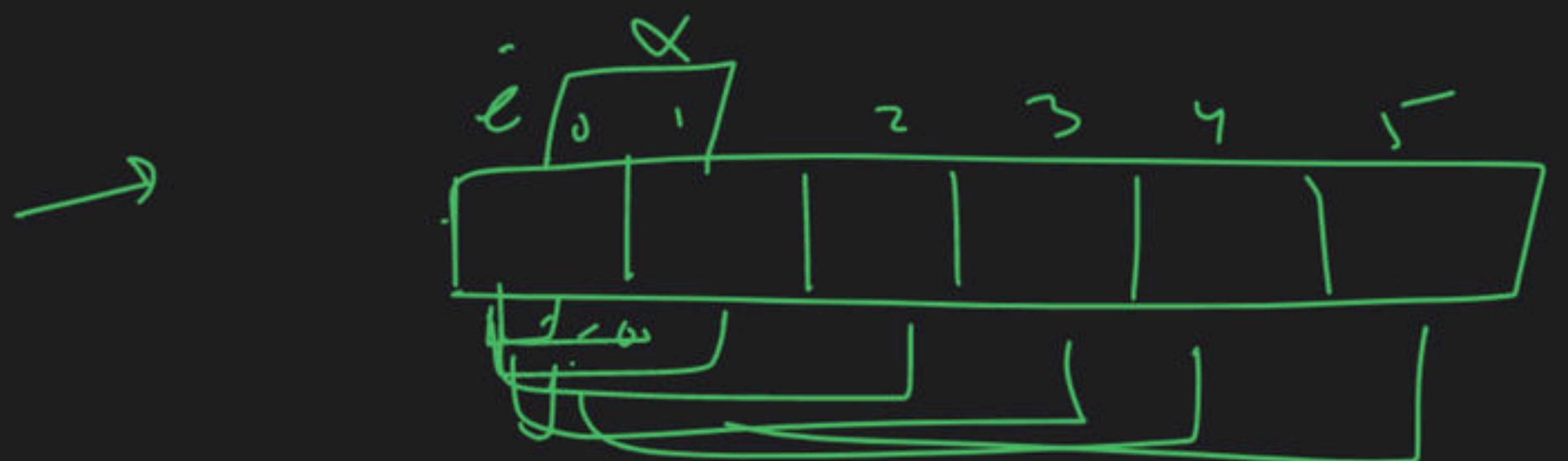
find every subarray

sum 1
sum 2
sum 3

max^m → ans

min sweep → Ques

$$O\left(\frac{n}{2}\right)$$
$$O(n)$$



for $i \rightarrow 0 = \text{loop}$
 for $j \geq i \rightarrow \text{loop}$
 | $\text{sum} + \text{arr}[j]$

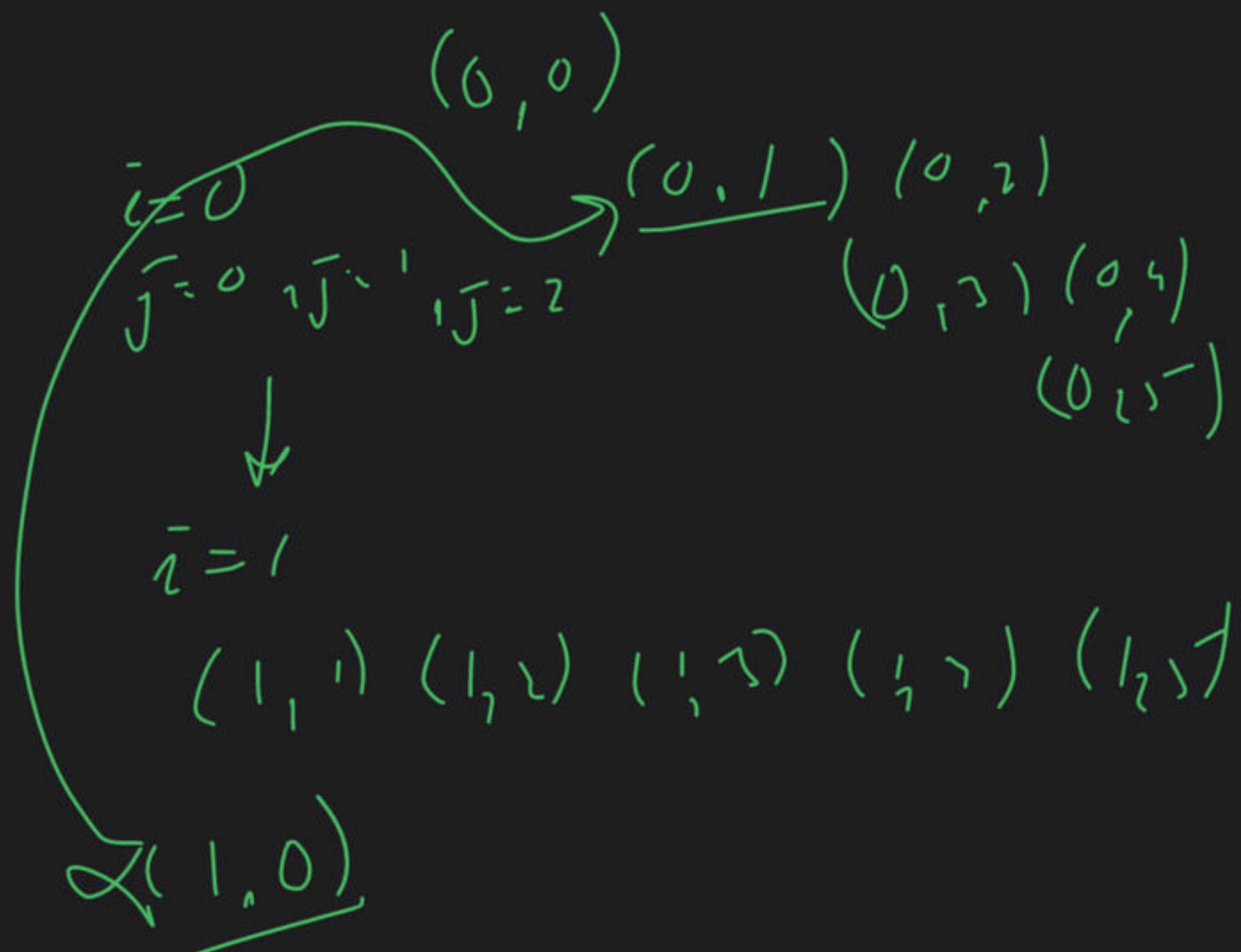
}

$\beta_{\text{max}} \text{ value}$

↑

$i \rightarrow \text{start}$
 $j \rightarrow \text{end}$

T-C / S-C



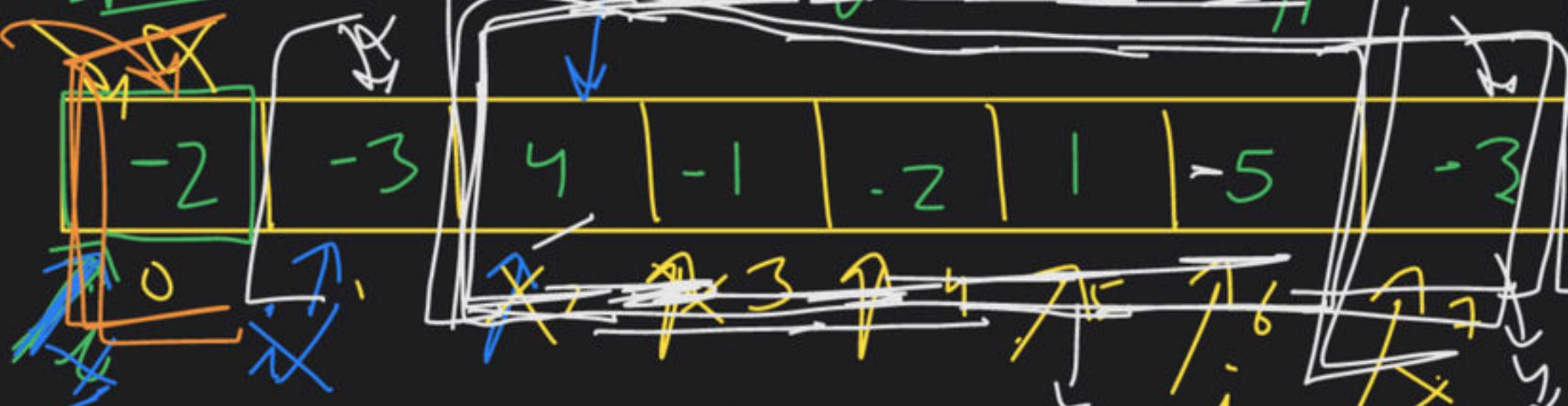
Optimize :->

single traversal

Kadane

Algorithm

arr



i=0

$$\text{sum} = \text{num} + \text{arr}[i]$$

$$\text{sum} = 0 + (-2) = \boxed{-2}$$

I

II

start cond

7)

ans

num

why

>>>

sum = 0

why

i=1

$$\text{sum} = 0 + (-3) = \boxed{-3}$$

$$\text{ans} = \max(-2, -3) = \boxed{-2}$$

$$\text{sum} = 0$$

i=2

$$\text{sum} = 0 + 4 = \boxed{4}$$

$$\text{ans} = \max(-2, 4) = \boxed{4}$$

$$\text{sum} = 4 > 0$$

sum = 0

maxi = INT_MIN

ans

$$\boxed{i=3}$$

$$\text{sum} = 4$$

$$ans = 4$$

$$\text{sum} \geq 4 + (-1) = 3$$

$$ans = \max(4, 3) = \boxed{4}$$

sum < 0 ↗

$$\boxed{i=4}$$

$$\text{sum} \geq (3) + (-2) = 1$$

$$ans = \max(4, 1) = \boxed{4}$$

$$\text{sum} = 1 > 0$$

Dry run

$$\boxed{i=5}$$

$$\text{sum} \geq 1 + 1 = 2 //$$

$$ans = \max(4, 2) = \boxed{4} //$$

$$\text{sum} = 2 > 0$$

$$\boxed{i=5}$$

$$\text{sum} \geq 2 + 5 = 7$$

$$ans = \max(4, 7) = \boxed{7}$$

$$\text{sum} = 7 > 0$$

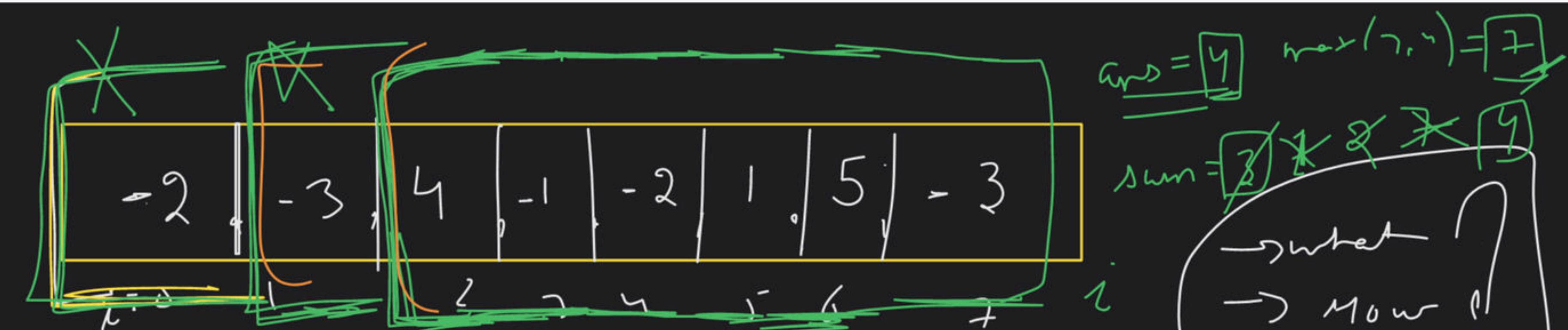
$$\boxed{i=7}$$

$$\text{sum} \geq 7 + (-3) = 4$$

$$ans = \max(7, 4) = \boxed{7}$$

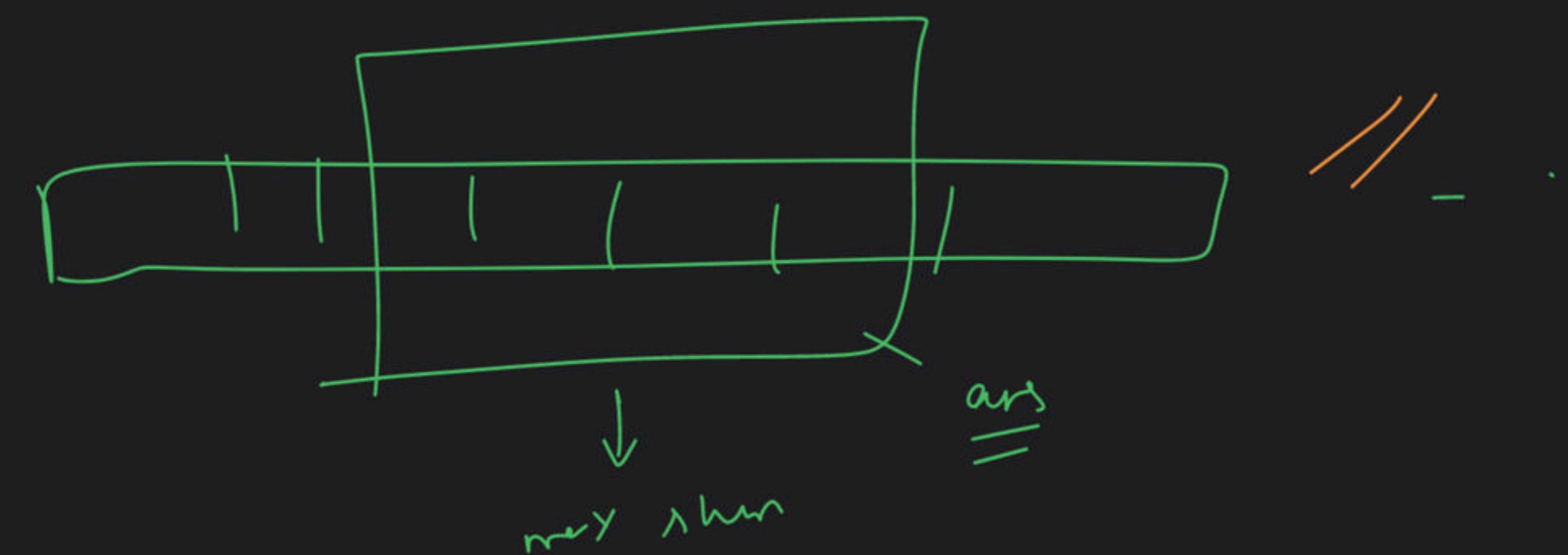
$$\text{sum} = 4 > 0$$

ans \leftarrow ans $+ \text{sum}$



→ largest sum contiguous subarray

→ largest sum contiguous subarray

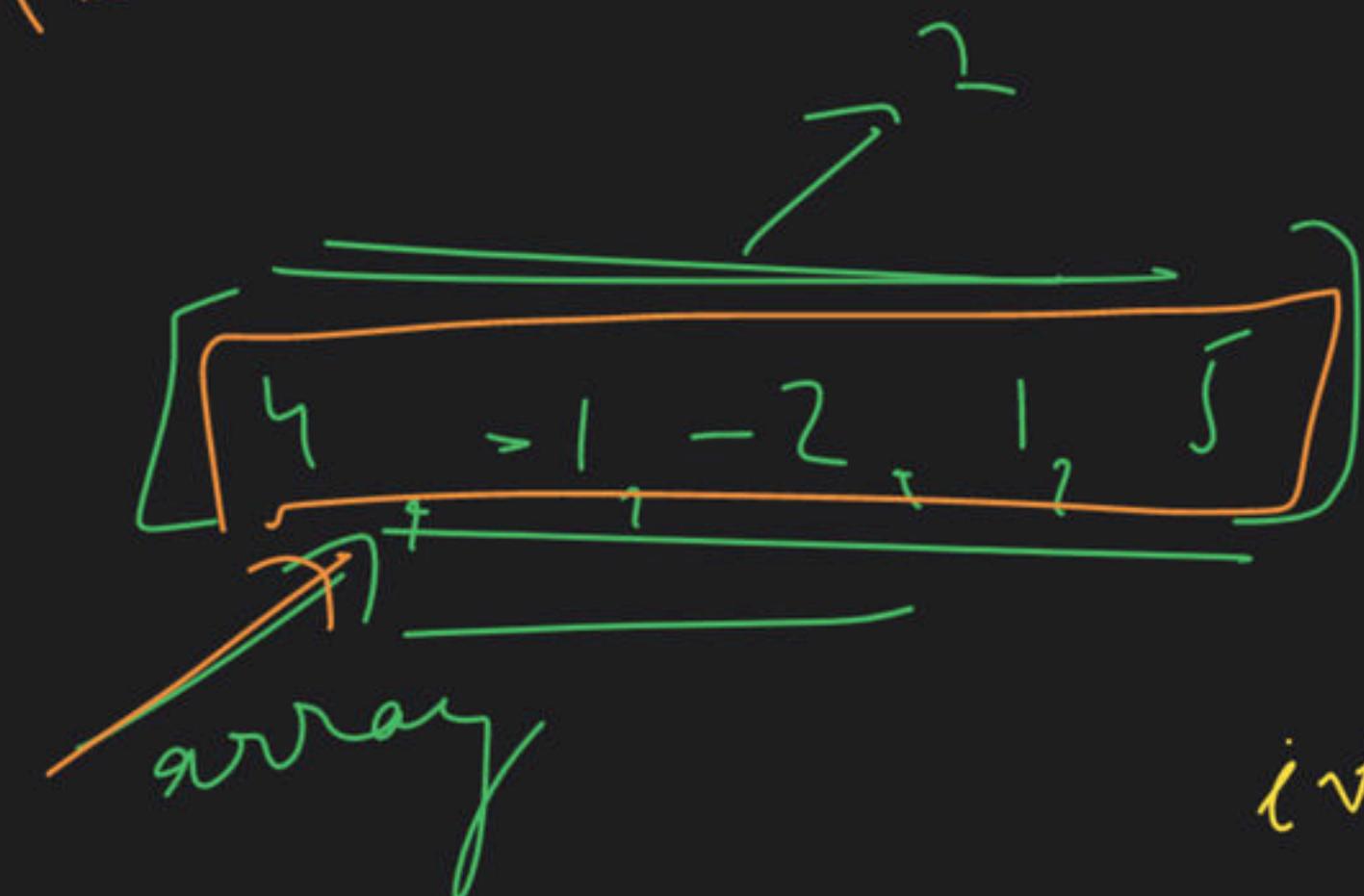


→ target sum

extreme

subarray

sum



→ track → starting index
ending index

→ window

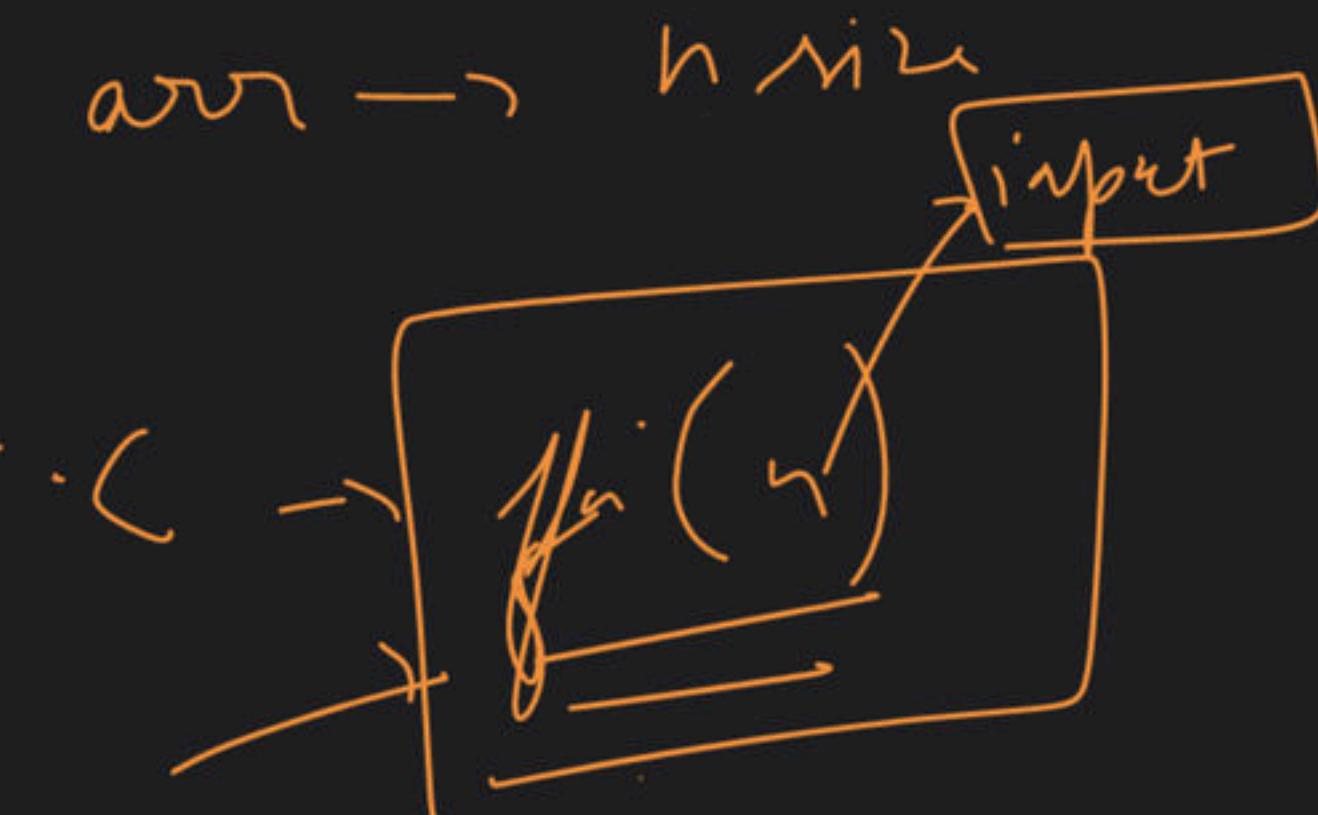
start 2
end :

→ Time Complexity

Amount of time taken
taken by algo / code / program
as a function of input

algo

fast → avg
slow



Notation

Big O

$O(n)$

Upper bound

Theta

$\Theta(n)$

avg - avg complexity

Omega

$\Omega(n)$

worst lower bound

Distance

km

Big-O notation:-

Ex ->

$$O(n)$$

linear time



$O(1)$ → constant time

$O(n^2)$ → quadratic



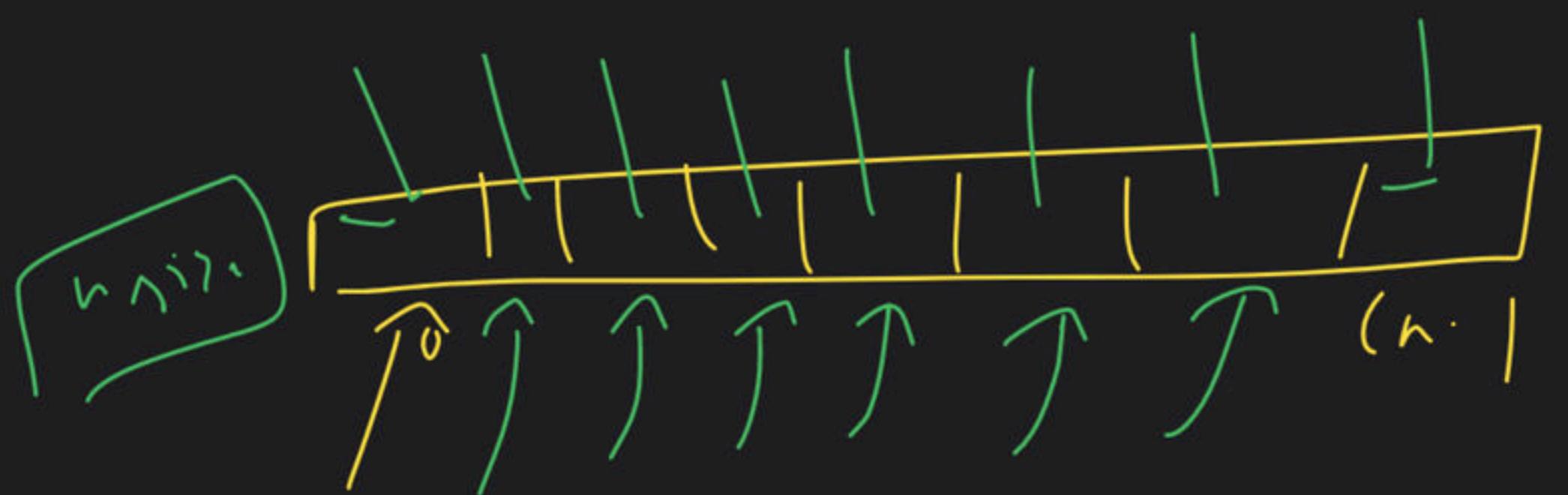
$O(n^3)$ → cubic

$O(\log n)$ → logarithmic

→

```
for (int i=0 ; i<n ; i++)  
{  
    cout << arr[i];  
}
```

$T.C \Rightarrow \underline{\underline{O(n)}}$



total no. of
operation = n

\rightarrow for (int $i = 0$; $i < 10$; $i++$)
 {
 $\quad \quad \quad$
 }
10

2^0

2^{000}

$| \Phi 0 |$
 10^{600}

10^{100}

constant
 $T.C \rightarrow O(1)$
 $O(|v|)$

\rightarrow `int i = 10;`
`while (i - -)` $\rightarrow \underline{\underline{T}} \leq \underline{\underline{O(1)}}$

~~`cout << "mira behai"`~~

`xcount {` \rightarrow `for (int i = 0; i < n)`
 `{` \rightarrow `for (j = 0; j < n)`
 `{` \rightarrow `cout << "habibur",`
 `}` \rightarrow $\underline{\underline{T}} \leq \underline{\underline{O(n^2)}}$

`xcount \`

`101` \rightarrow `constant`

`501`
`501`

```

    for (i=0 → n)
    {
        for (j=0 → n)
        {
            for (k=0 → n)
        }
    }

```

$\hookrightarrow 1 \cdot \hookrightarrow O(n^3)$

$O(1) \rightarrow$

$i = 0 \rightarrow j = 0, 1, 2, \dots, n-1$
 $i = 1 \rightarrow j = 0, 1, 2, \dots, n-1$
 \vdots
 $i = (n-1) \rightarrow j = 0, 1, 2, \dots, (n-1)$

$$n \times n = n^2$$

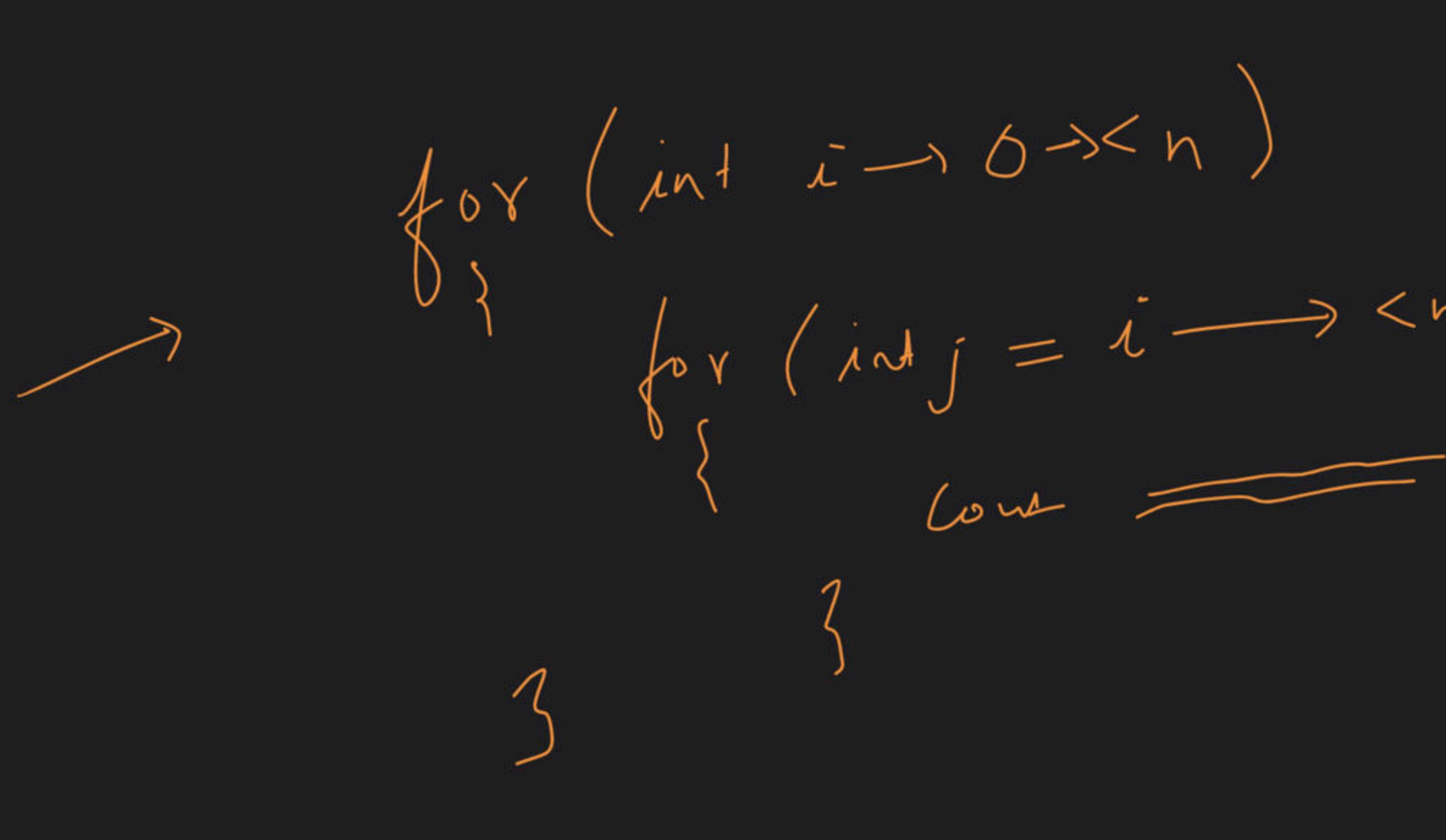
$$n \times n \times n \rightarrow n^3$$

$O(n^3)$

→ why we need $T \cdot C^9$
↳ comparison b/w algo 

→

```
for (int i = 0 < n)
{
    for (int j = i < n)
        cout <<
```



$i=0$	$j \rightarrow 0 \dots (n-1)$
$i=1$	$j \rightarrow 1 \dots (n-1)$
$i=2$	$j \rightarrow 2 \dots (n-1)$
$i=3$	$j \rightarrow 3 \dots (n-1)$
\vdots	\vdots
$i=(n-1)$	$j \rightarrow (n-1)$

\rightarrow Kadane's $\hookrightarrow T.C \rightarrow O(n)$, $n = \text{size of array}$

$$f(n) = ? + 3n \rightarrow 4n \rightarrow O(\cancel{4n}) \rightarrow \underline{\underline{O(n)}}$$

$$f(n) = \frac{n^2}{5} \rightarrow O\left(\frac{n^2}{5}\right) = O(n^2)$$

$$f(n) = n^3 - 2n \rightarrow n^3 \rightarrow O(n^3)$$

$$f(n) \rightarrow \underline{3n^3} \rightarrow O(1)$$
$$f(n) \rightarrow n^3 + \frac{n^3}{5} \rightarrow \cancel{n^3(1+\frac{1}{5})} = O(n^3)$$

$$f(n) \rightarrow n^3 + n^6 + n^{2/3} \rightarrow O(n^6)$$

$$f(n) \rightarrow \cancel{n^2} \rightarrow O(n^2)$$

$$\rightarrow 2^n \rightarrow O(\cancel{2^n}) \underset{\equiv}{=} O(n)$$

```
int main ()
```

```
{
```

```
    for (int i = 0; i < n; i++)
```

```
}
```

```
    for (int j = 0; j < m; j++)
```

```
}
```

```
}
```

$T \rightarrow O(n)$

+

$O(m)$

n

0

\sim

$O(\max(n, m))$

$=$

$O(n + m)$

R/W

Right or wrong

for (int i=0 & $i < \sqrt{n+m}$; $i++$)
 \sum
)

$$O(\sqrt{n+m})$$

$O(i^c)$

$O(n+m)$

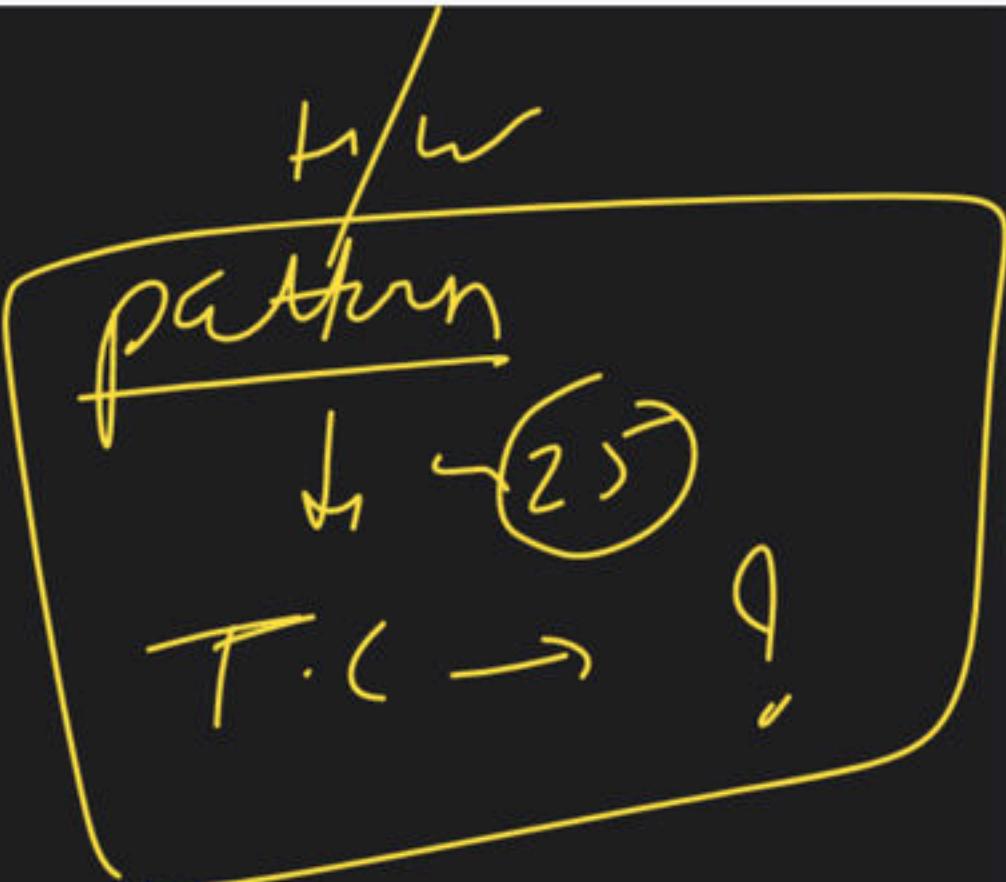
Space Complexity



space taken by p/g



```
int i=0  
for ( ; i<n ; i++)  
{  
    cout << i;  
}  
→ S.C → O(1)  
= constant  
space
```



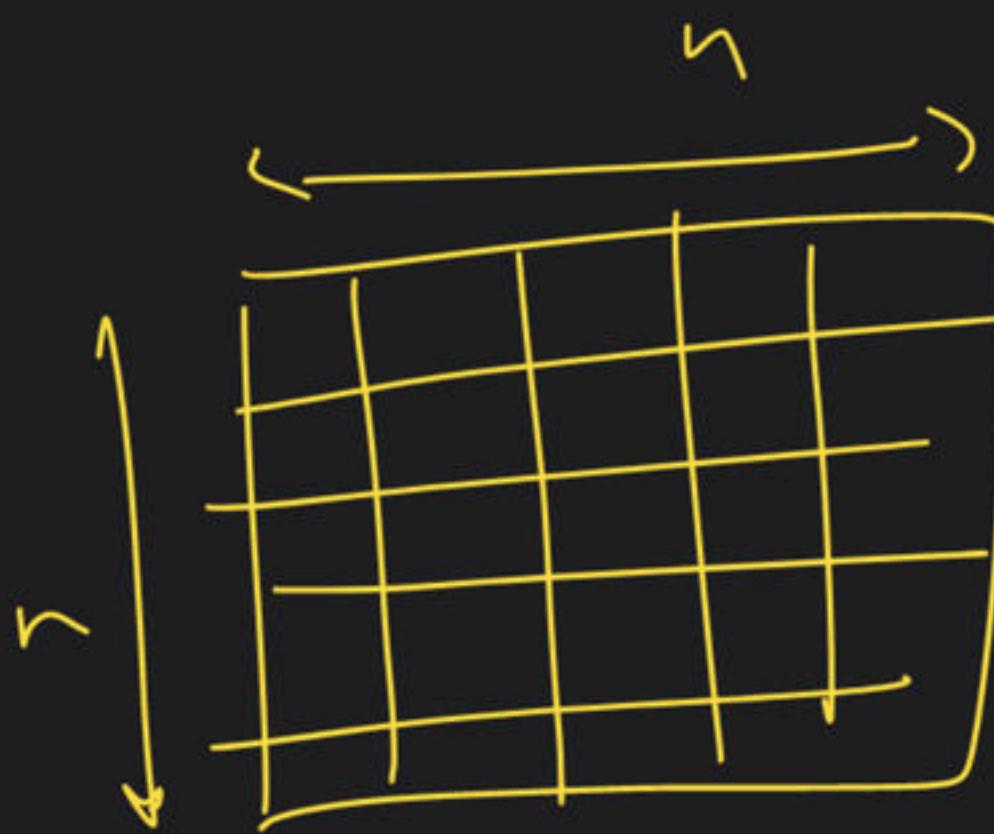
\rightarrow

f

$\text{int arr}[n] \rightarrow$

$\sum_{i=1}^n O(n)$

\exists



$\rightarrow \text{Nested} \rightarrow n \otimes n$

$\sum_{i=1}^n O(n^2)$

\rightarrow

$\{$

int arr[n]



\sim



\sim

$\mathcal{O}(n+m)$

$\frac{n+m}{2}$

int arr[m]

$\}$

\rightarrow

{ int arr[$n+m$];

$\rightarrow \mathcal{O}(\cancel{(m+n)})$

~~$(m+n)$~~

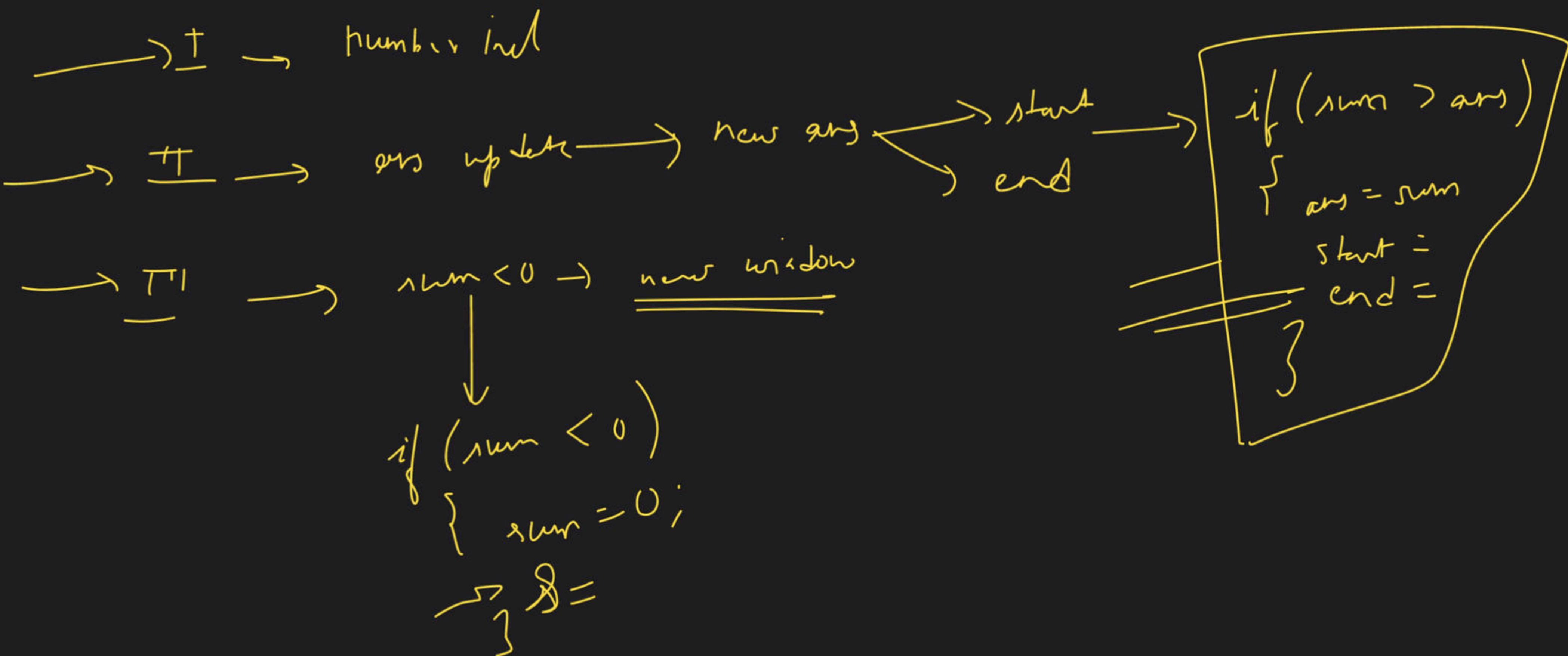
int arr2[$n+m$];

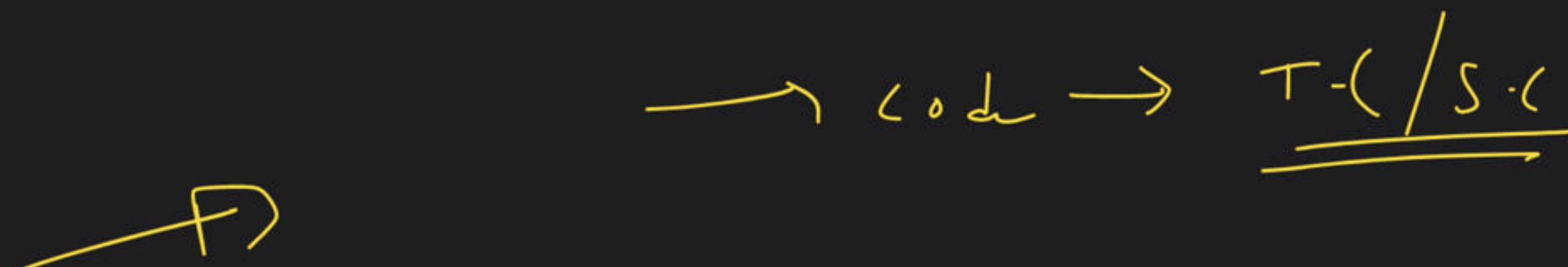
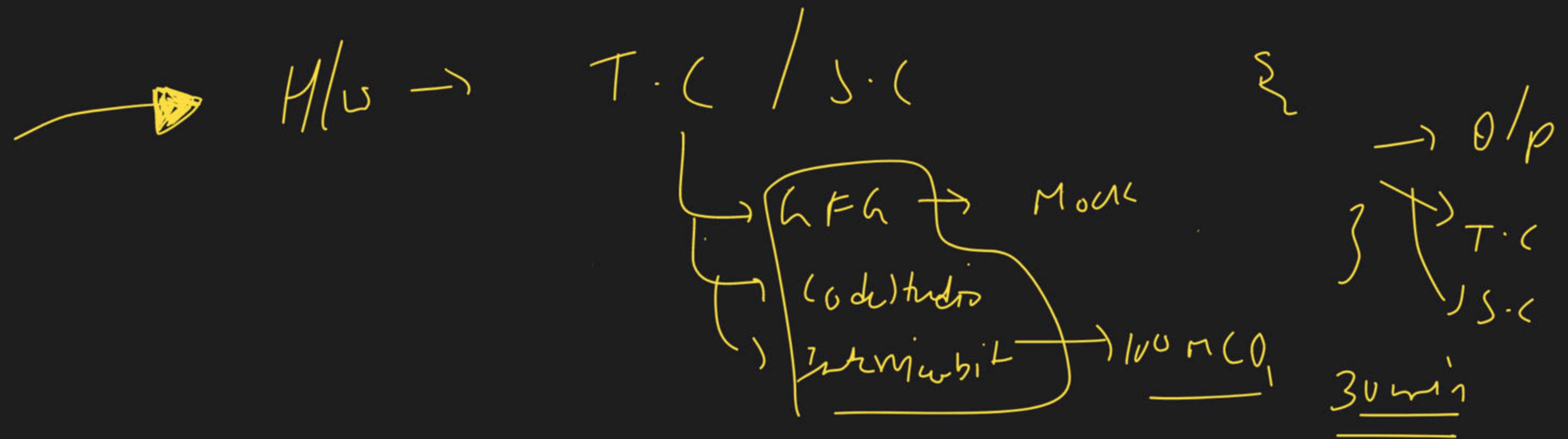
$\rightarrow \mathcal{O}(m+n)$

$\}$

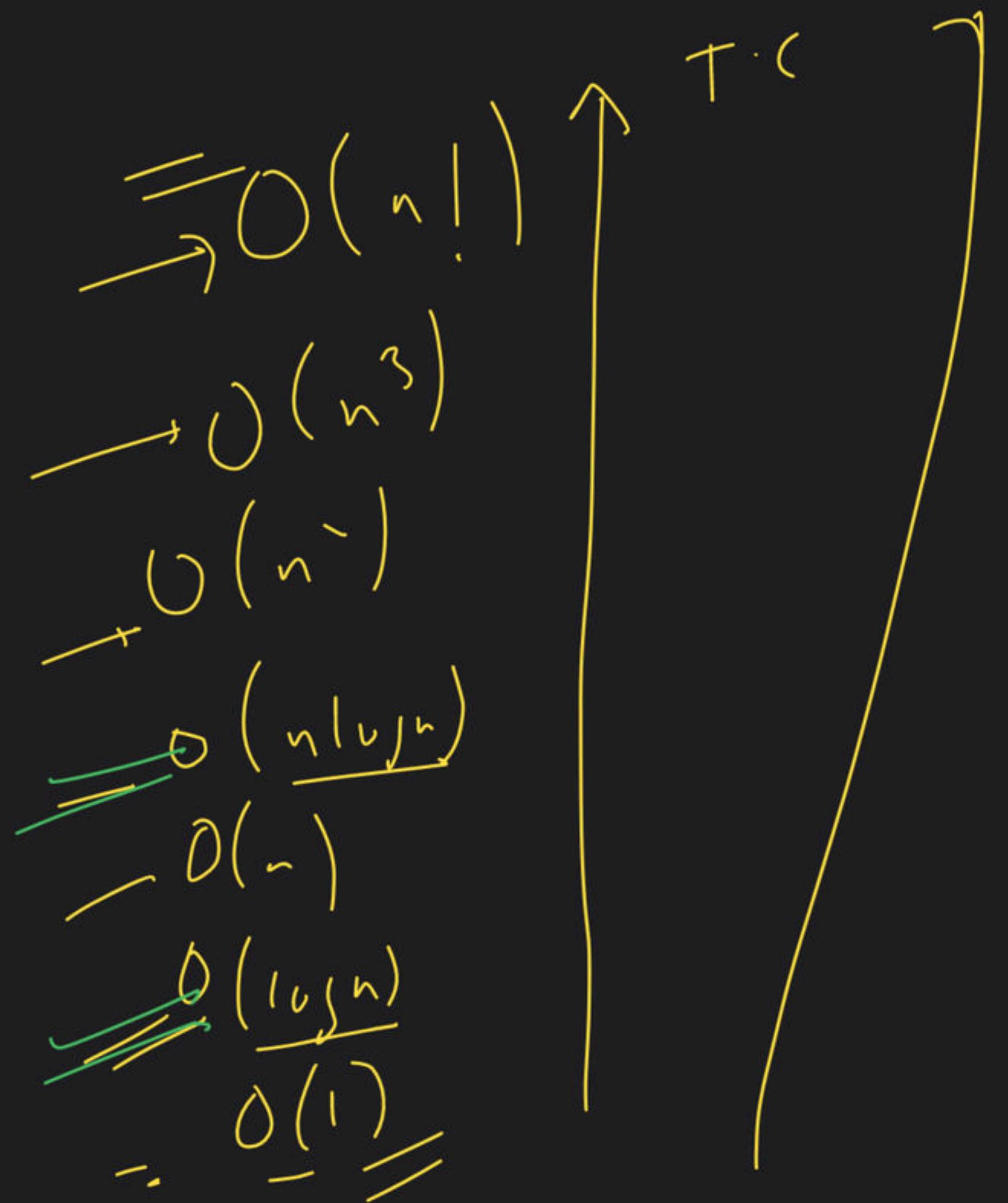
$\rightarrow \{$ func ()
int arr [115] ; $\rightarrow S.C \rightarrow \frac{O(1)}{\text{constant}}$

$\rightarrow \{$ ()
int v1, v2, v3, v4 $\rightarrow O(1)$
vector v
func LL





\rightarrow

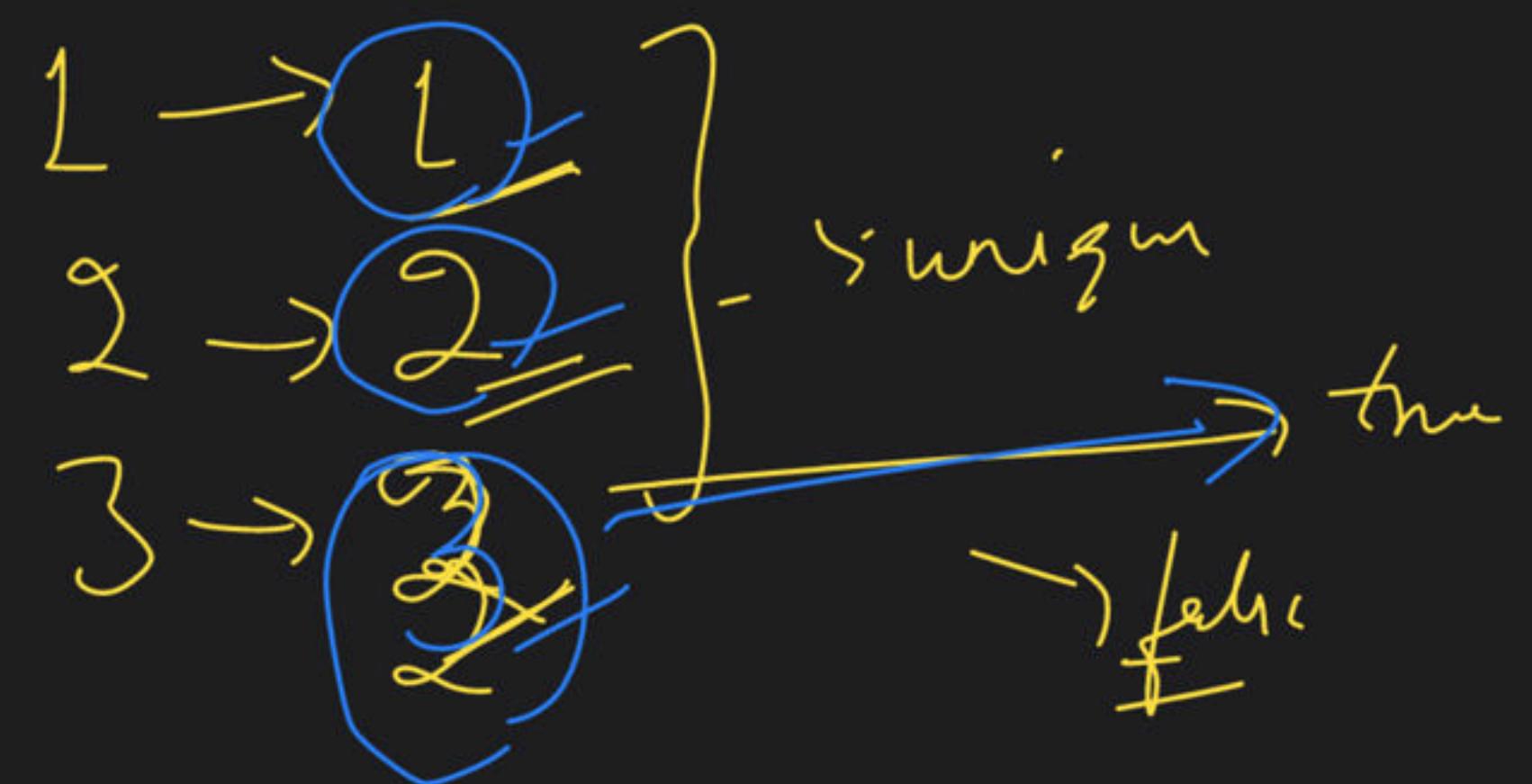


arr
arr $(\text{arr}, \text{arr} + \text{arr})$

\downarrow
 $T \cdot C - \sqrt{n \log n}$

B.S $\rightarrow O(\log n)$

\rightarrow if $p \rightarrow \text{arr} \rightarrow \{ 3, 2, 2, 1, 3, 3 \}$



\rightarrow approach:-

- sort $\{ 1, 2, 2, 3, 3, 3 \}$
- count occurrence
- check element

~~map~~

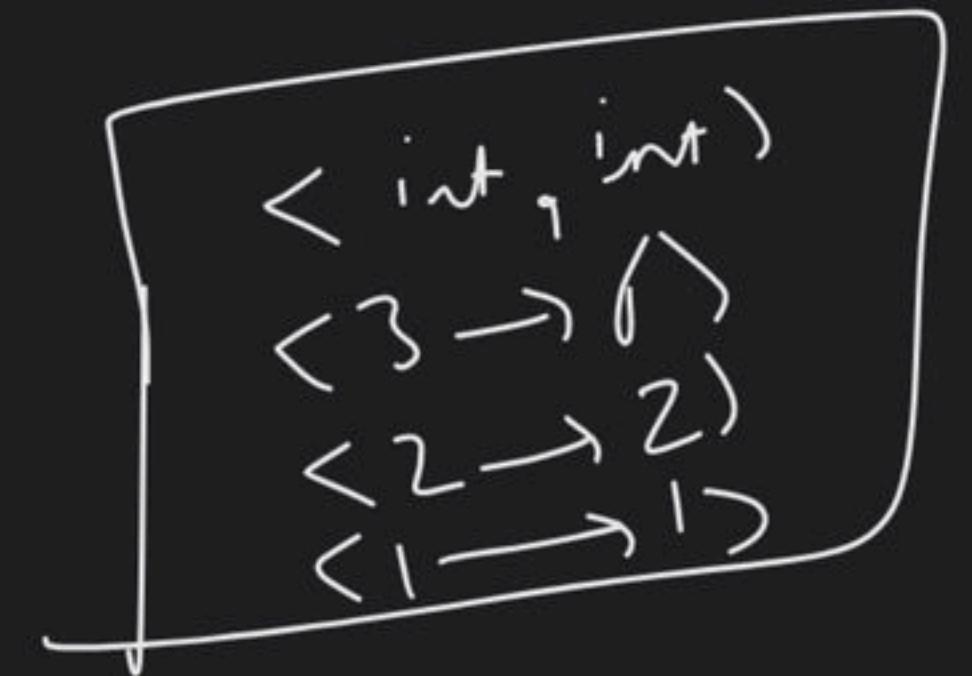
$1 \rightarrow 1$
 $2 \rightarrow 2$
 $3 \rightarrow 3$

D.S
map

unidim



$\xrightarrow{\text{unidim}}$ $\text{map} < \text{int}, \text{int} > m;$

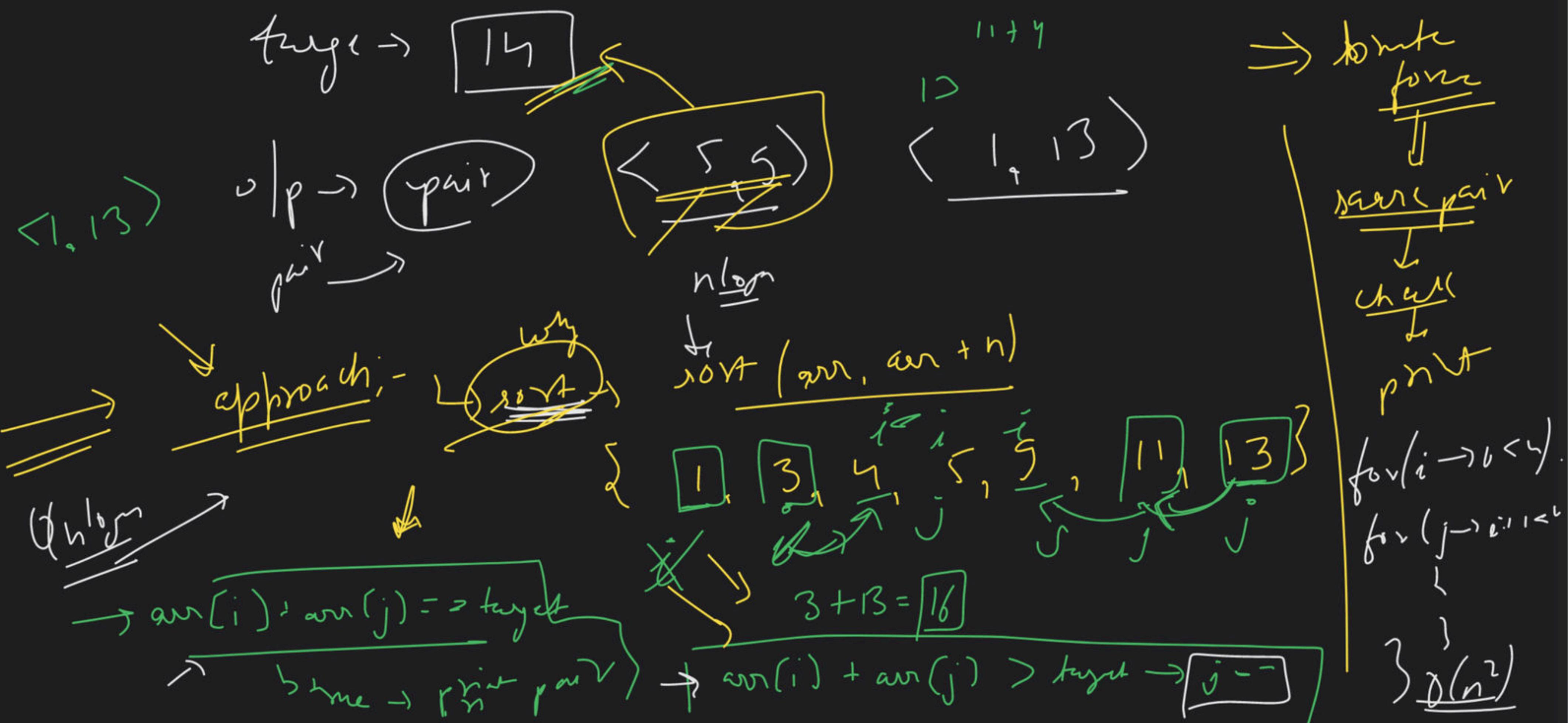


$\xrightarrow{\text{unidim}}$ $\text{map} < \text{int}, \text{int} > m;$

$O(1)$

$\xrightarrow{\text{multidim}}$ $\text{sort} (\text{arr}, \text{arr} + n);$

$$\rightarrow \text{arr} = \{ 3, 1, 4, 5, 9, 2, 10, 11 \} \quad 3+11=\boxed{14}$$



$$arr[i] + arr[j] < target$$

$i \leftarrow i + 1$

$j \leftarrow j - 1$

$\langle 5, 11 \rangle$

ans

target = 20

1	3	5	7	9	11	13
---	---	---	---	---	----	----

$i \rightarrow 1 \rightarrow 3 \rightarrow 5 \rightarrow 7 \rightarrow 9 \rightarrow 11 \rightarrow 13 \rightarrow j$

$$\begin{aligned} 3 &= w \text{ F} \\ &\rightarrow w \rightarrow \top \\ &= w \rightarrow + \end{aligned}$$

$$3 + 13 = 20 \text{ F}$$

$$3 + 11 > 20 \rightarrow \text{F}$$

$$3 + 11 < 20 \rightarrow \top$$

$$w < 20$$

$$w + 13 = 20 \rightarrow \text{F}$$

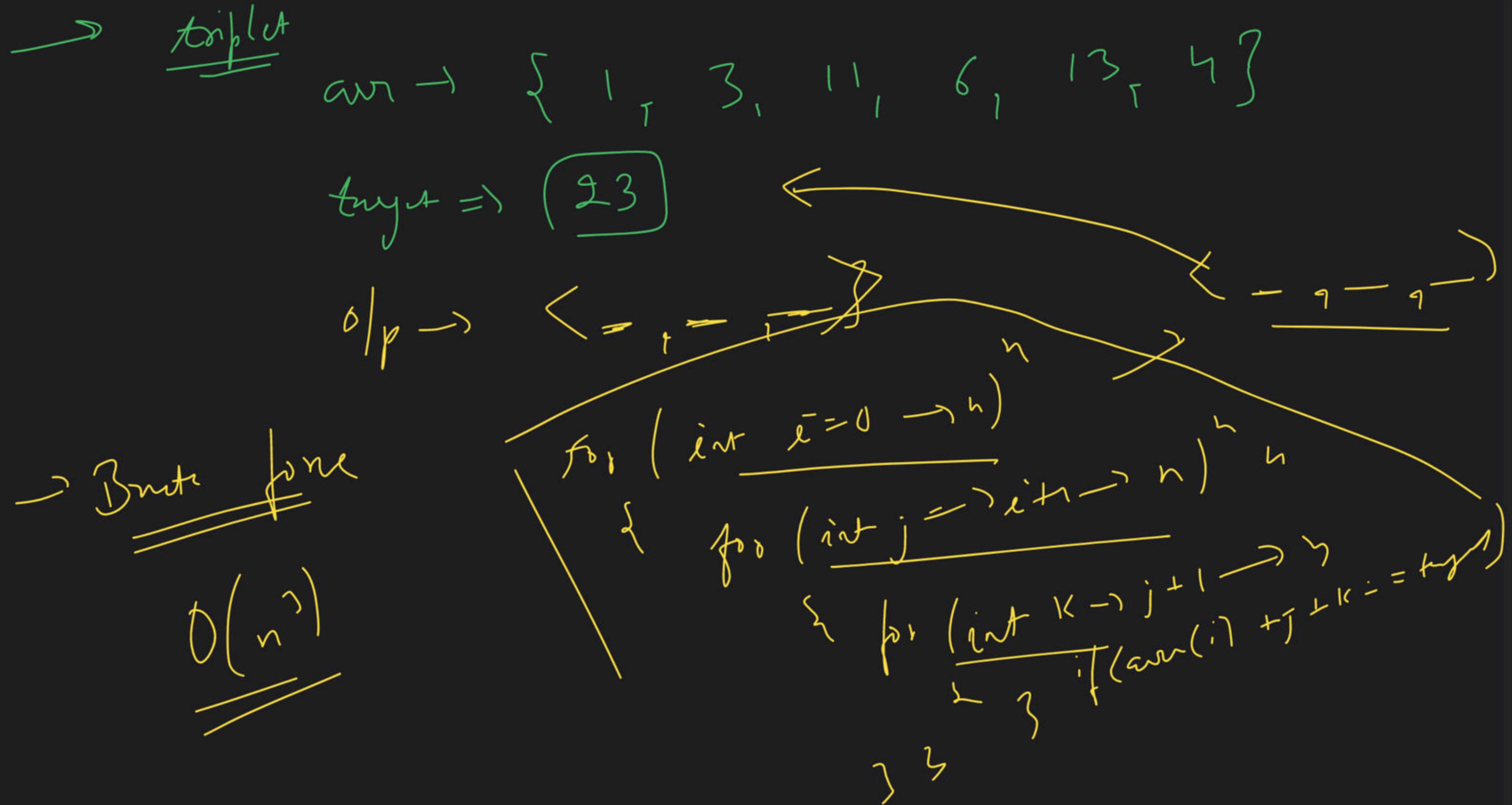
$$w + 13 > 20 \rightarrow \text{F}$$

$$w + 13 < w \rightarrow \top$$

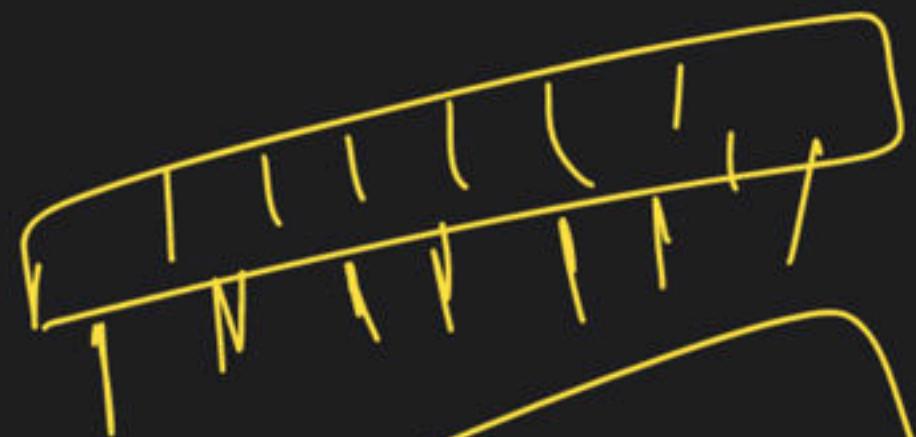
$$5 + 13 = w \text{ F}$$

$$5 + 11 > w \rightarrow \text{F}$$

$$5 + 11 < w \rightarrow \top$$



Optimize
target



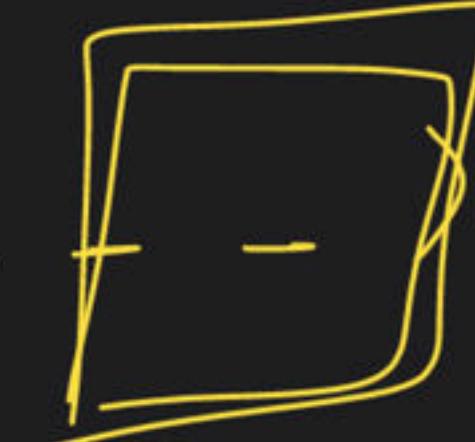
$n^2 \log n$

$n^2 \log n$

for {
int $i = 0$; $i < n$; $i++$)

int fint = \boxed{i}

int newTarget = target - fint



$n \log n$

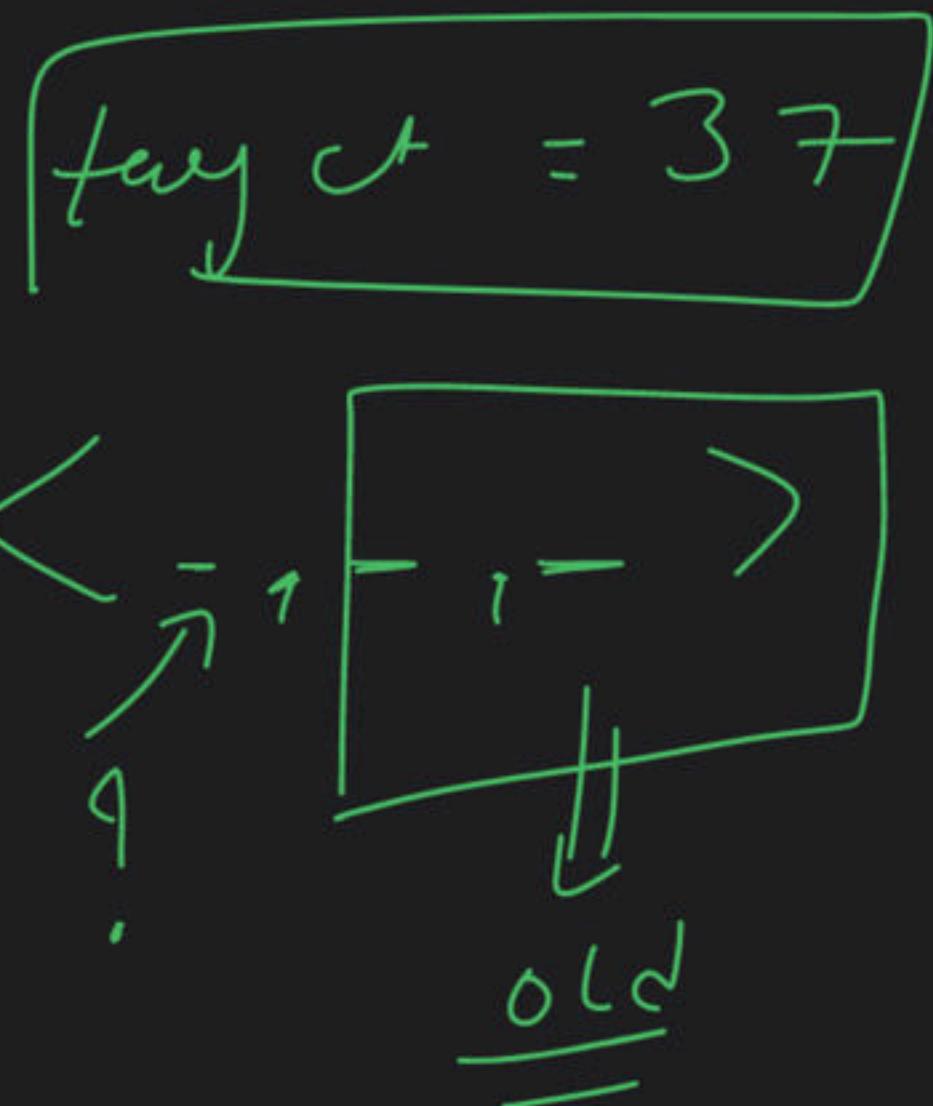
$i=0$	$\boxed{1}$	$\boxed{3}$	$\boxed{5}$	$\boxed{7}$	$\boxed{11}$	$\boxed{12}$	$\boxed{14}$	$\boxed{18}$	$\boxed{19}$
-------	-------------	-------------	-------------	-------------	--------------	--------------	--------------	--------------	--------------

$$i=0, \text{av}(\cdot) = 1$$

$$\text{newTarget} = 37 - 1 = \boxed{36} \quad <-, ->$$

$$i=1, \text{av}(\cdot) = 3$$

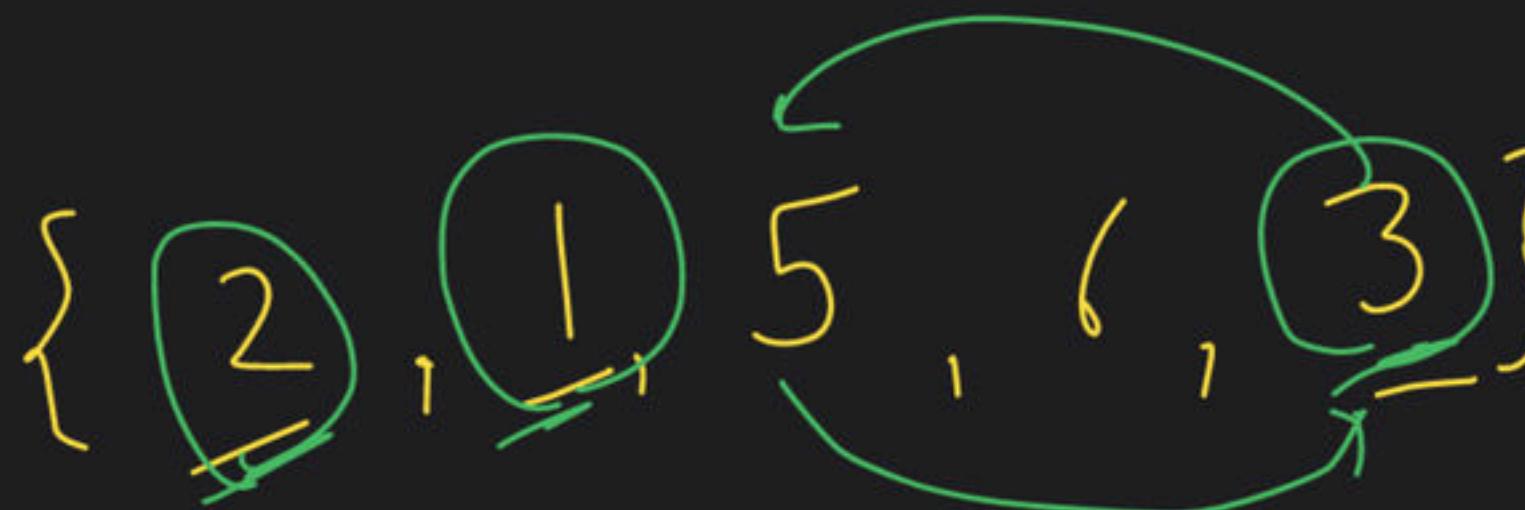
$$\text{newTarget} = 37 - 3 = \boxed{34} \quad <\!\!\! \circlearrowleft \circlearrowright \!\!\! >$$



Code, dry run

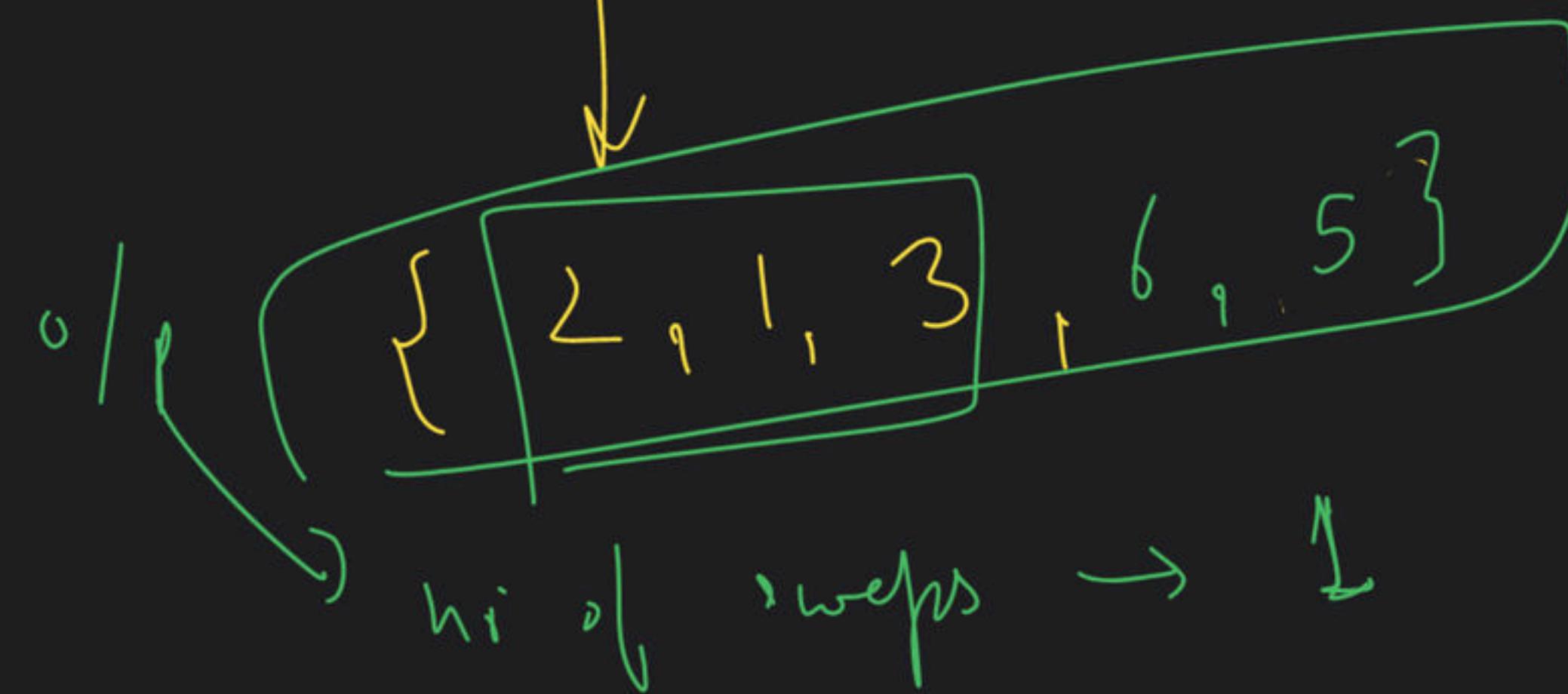
optimization
explore

Min swaps



$$K = 3$$

$$\leq K$$



Count = 3

for (int i=0; i<locA

to find minimum no. of swaps
reg to bring elements together

$100!$ \rightarrow \checkmark

150 digits

$$5! = [5 \times 4] \times 3 \times 2 \times 1$$

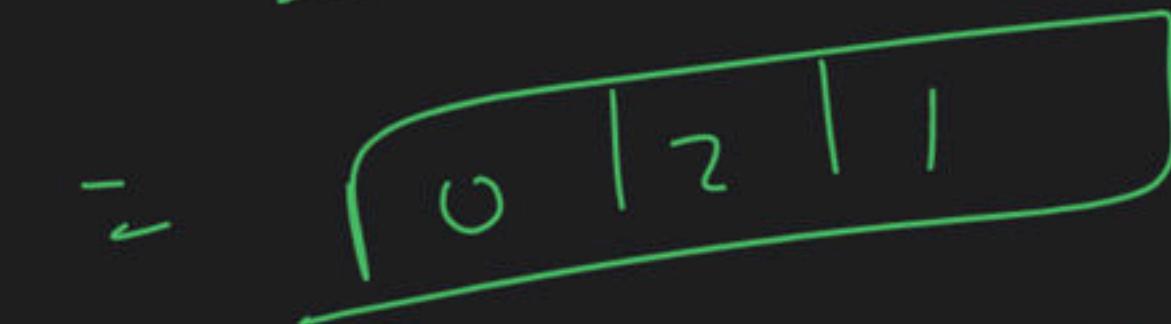
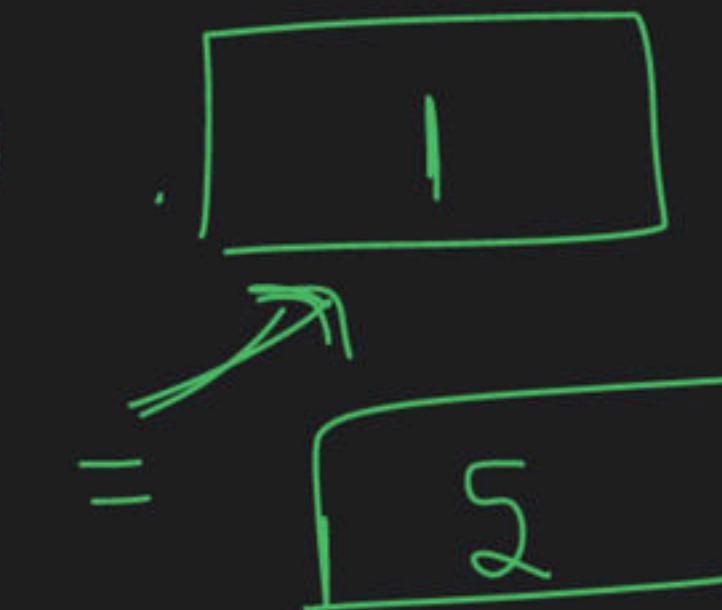
int carry = 0

int ans = $\underbrace{arr[i] \times num}_{+} + carry$

int digit = ans $\cdot\cdot\cdot 10;$

carry = ans $\cdot\cdot\cdot 10$

arrays



100 b

carry = 0

int ans = arr[0] * num

int digit = ans % 10

carry = ans / 10

$$\begin{array}{r}
 & 9 \\
 & 2 \\
 \times & 3 \\
 \hline
 2 & 1 & 7
 \end{array}$$

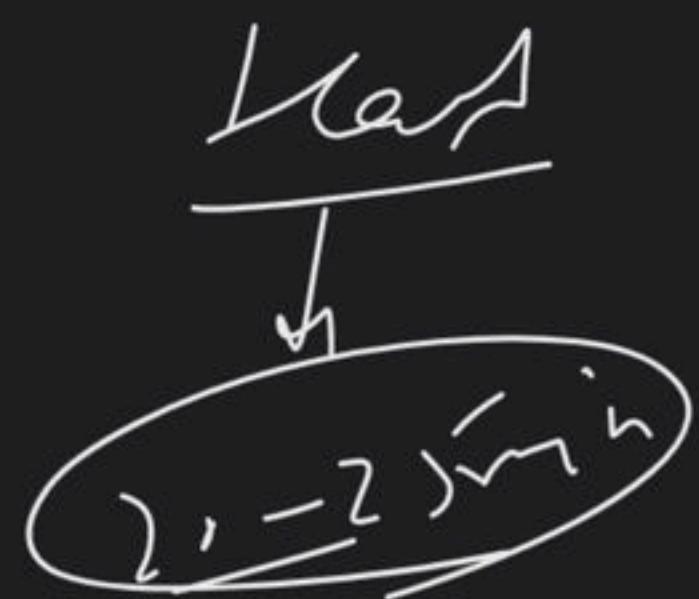
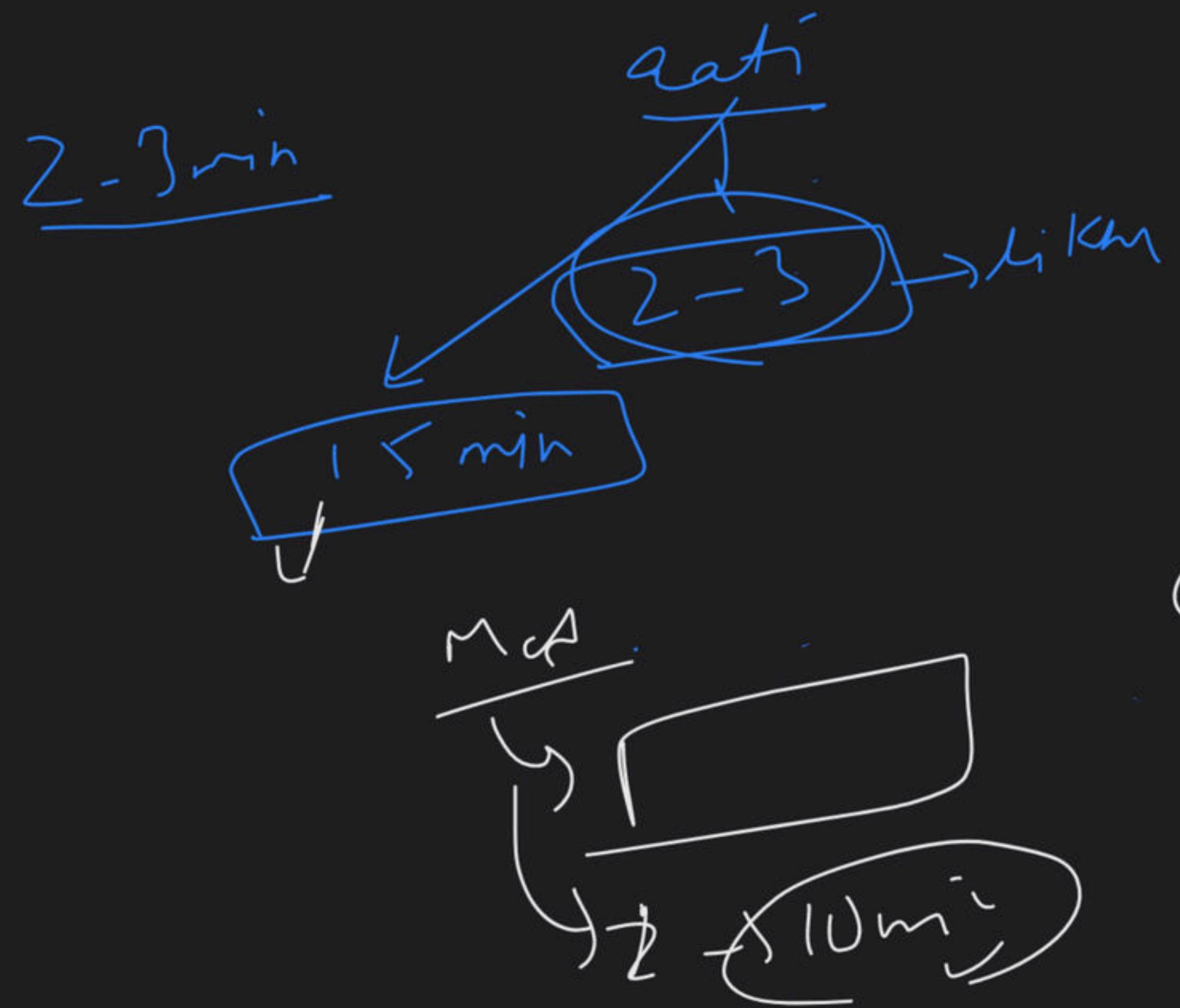
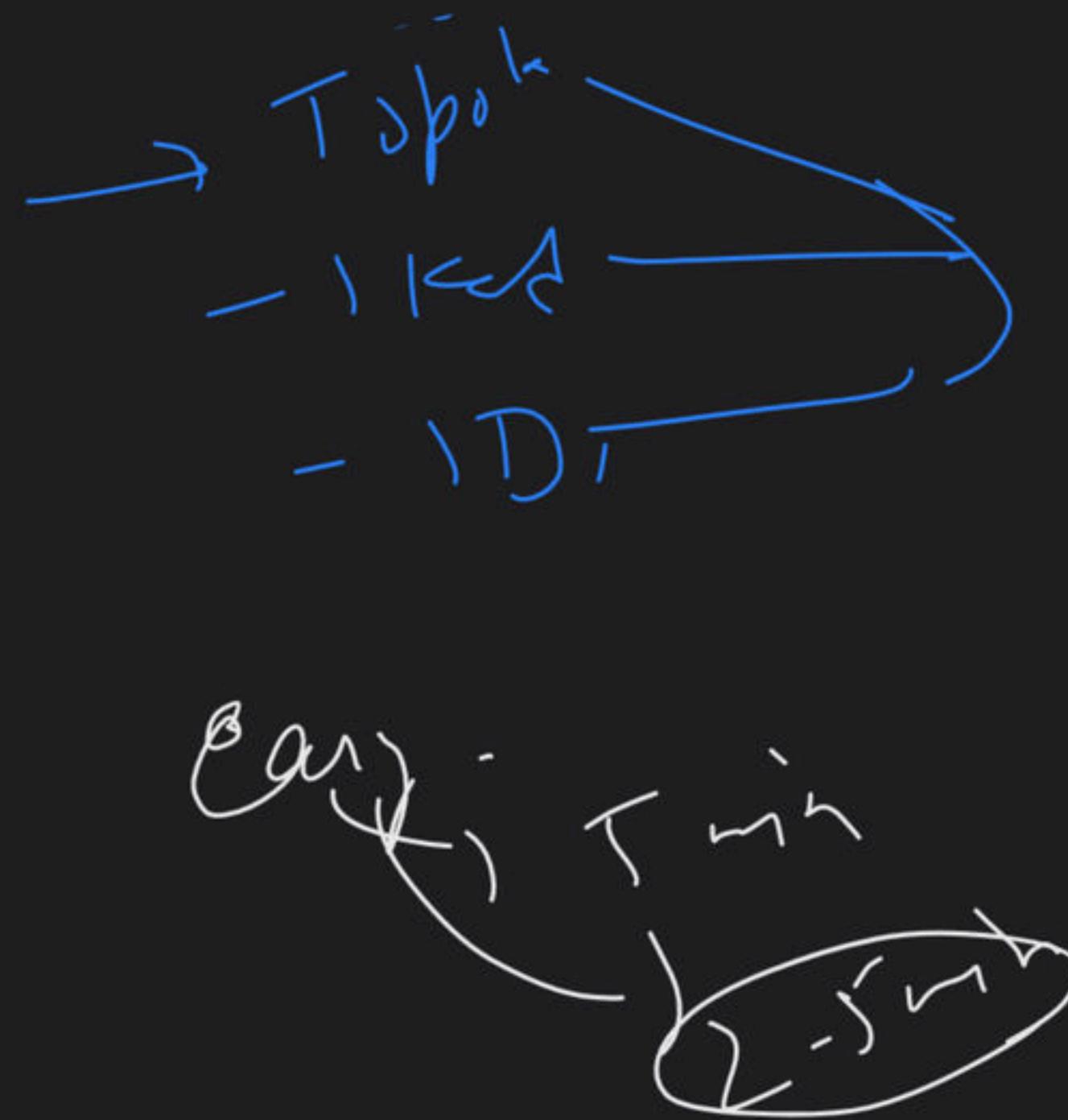
~~927~~

$$\begin{array}{r}
 9 \times 3 = 27 \\
 3 \boxed{0}
 \end{array}$$

$$\begin{array}{r}
 38 \\
 \hline
 10
 \end{array} = 3 - \frac{2}{10} = 2$$

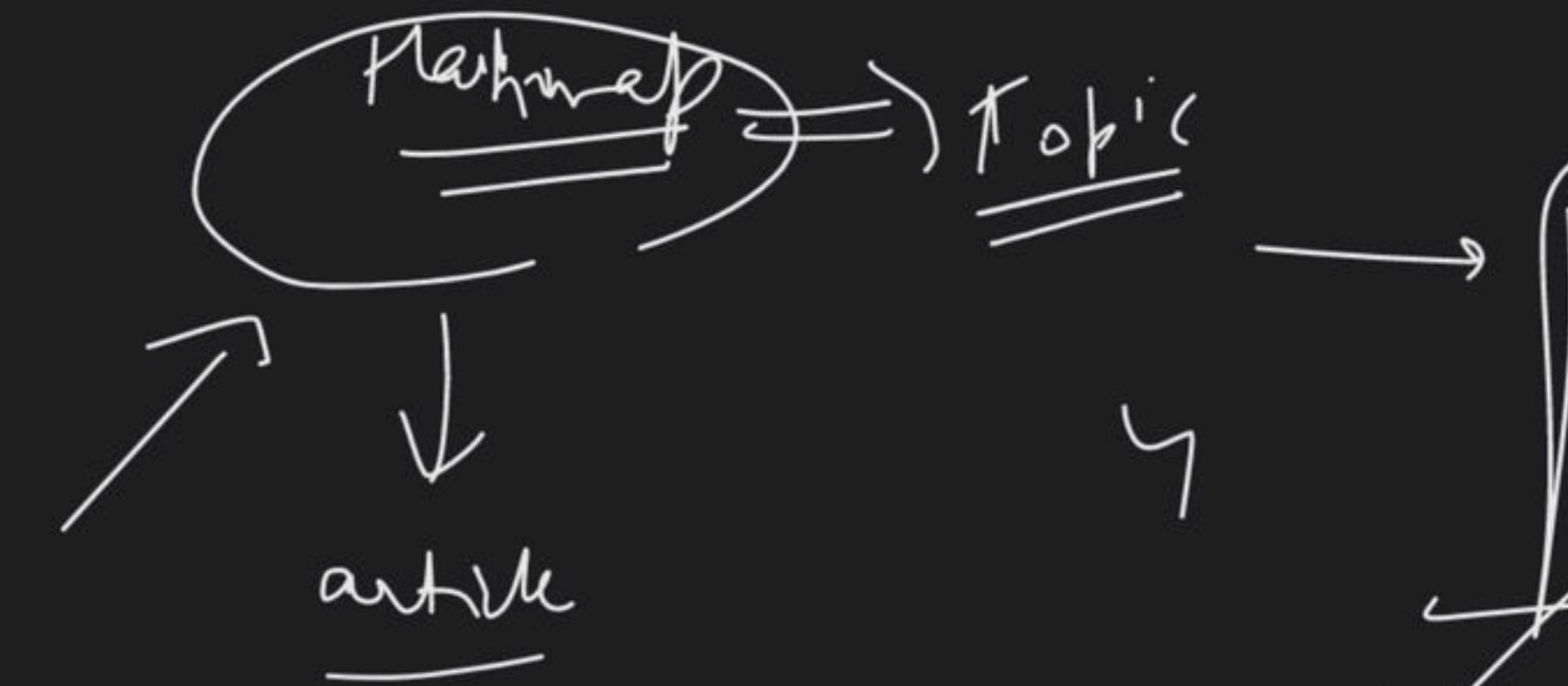
$$\begin{array}{r}
 3253 \\
 \times 87 \\
 \hline
 2675 \\
 240 \\
 \hline
 27791
 \end{array}$$

int arr[1000];



$\rightarrow \text{2:12}$

(1.5 bits)



int ->

(char ->

(string ->

$O(1)$

H W

$\rightarrow D_{HW}$

line

$\rightarrow MS$

$\rightarrow PMS$

\rightarrow

$\rightarrow SW$

$\rightarrow NYD$



