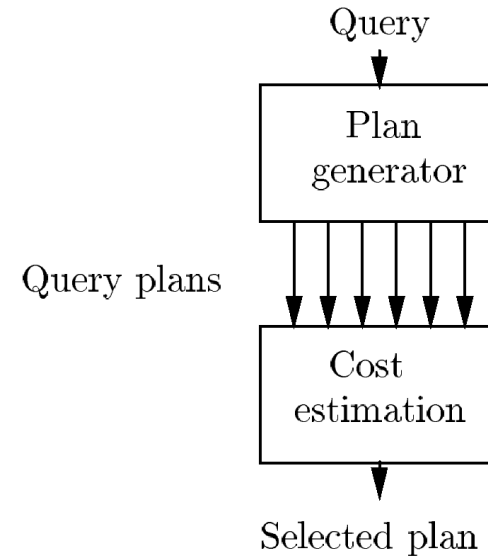


## Query Processing

## Overview Query Processing



WS 23/24  
Frankfurt UAS

Prof. Dr. Justus Klingemann

## Query Plans

Choose operations, e.g.,  $\sigma$ ,  $\bowtie$

Order operations.

Detailed strategy of operations, e.g.:

- Join method.
- Pipelining: consume result of one operation by another, to avoid temporary storage on disk.
- Use of indexes?
- Sort intermediate results?

We focus on relational systems

Implementation of DBMS

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## Example

Select B,D

From R,S

Where R.A = "c" AND S.E = 2 AND R.C=S.C

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R	A	B	C	S	C	D	E
a	1	10	10	x	2		
b	1	20	20	y	2		
c	2	10	30	z	2		
d	2	35	40	x	1		
e	3	45	50	y	3		

Answer

B	D
2	x

## How Do We Execute the Query?

One idea

- Do Cartesian product
- Select tuples
- Do projection

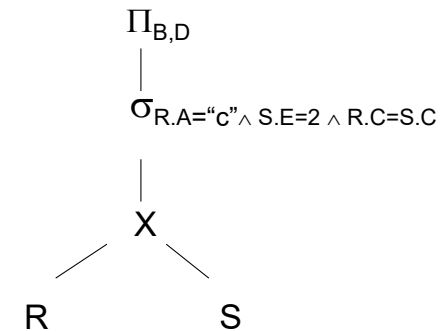
RXS

R.A	R.B	R.C	S.C	S.D	S.E
a	1	10	10	x	2
a	1	10	20	y	2
·					
·					
C	2	10	10	x	2
·					
·					

Bingo!  
Got one...

## Relational Algebra to Describe Plans

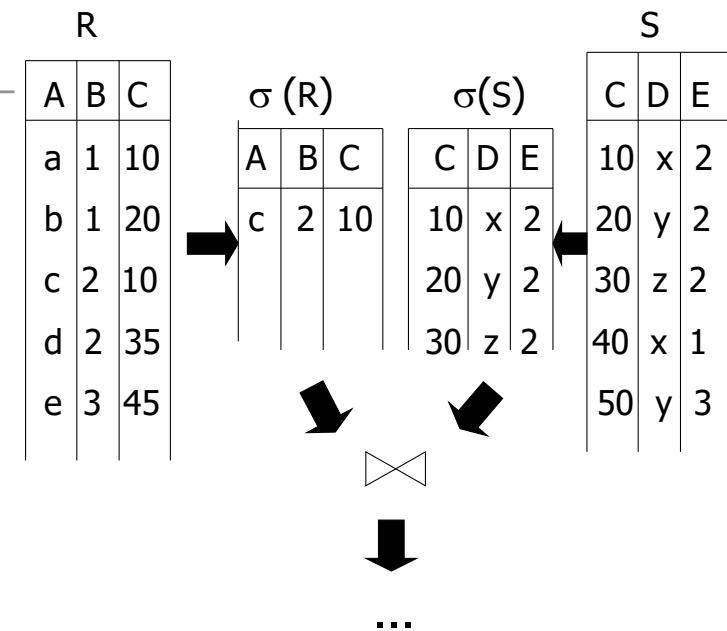
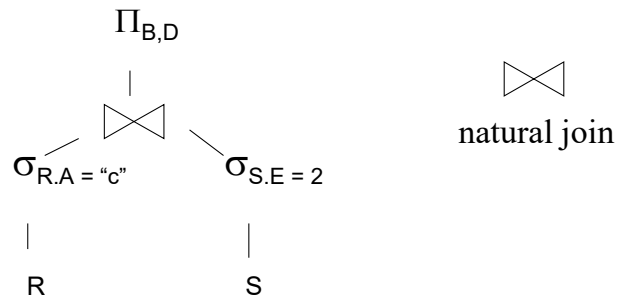
Ex: Plan I



OR:  $\Pi_{B,D} [\sigma_{R.A='c' \wedge S.E=2 \wedge R.C=S.C} (R \times S)]$

## Another Plan

Plan II

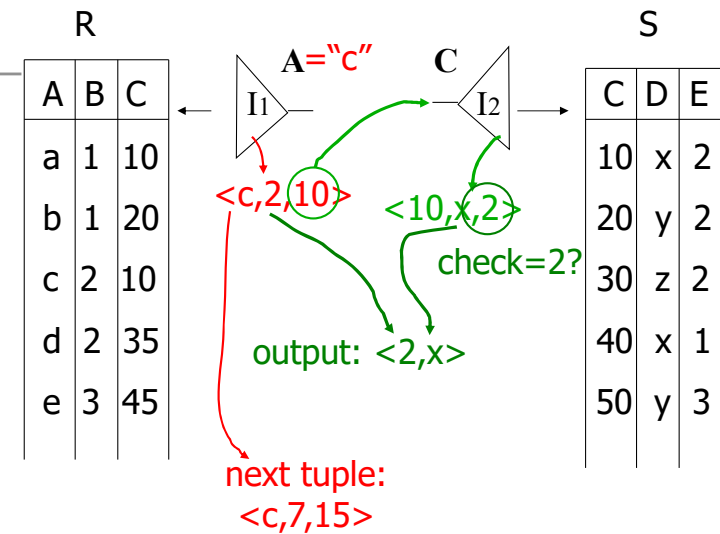


## Plan III

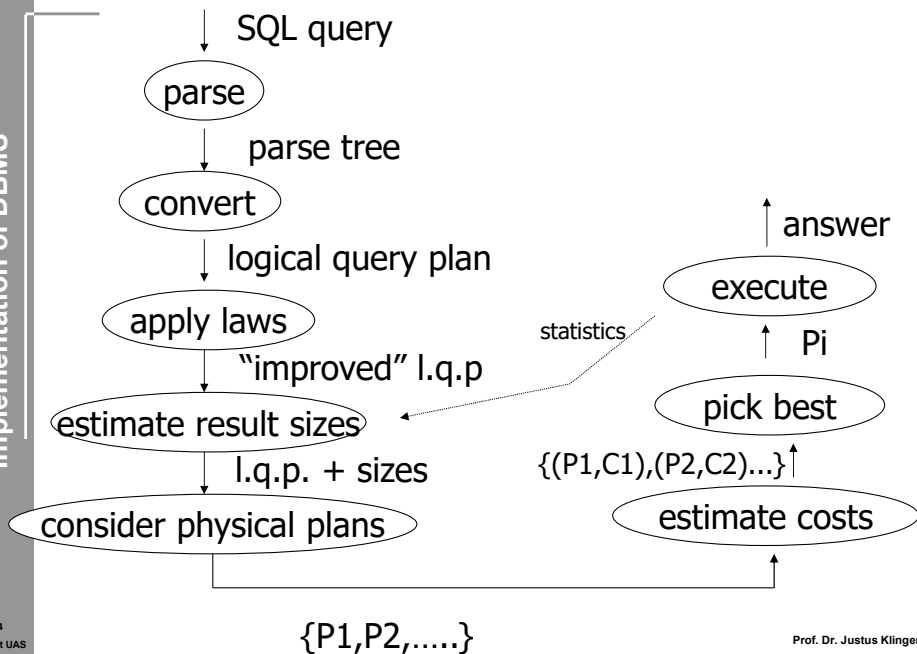
Use R.A and S.C Indexes

- (1) Use R.A index to select R tuples with R.A = "c"
- (2) For each R.C value found, use S.C index to find matching tuples
- (3) Eliminate S tuples with S.E  $\neq$  2
- (4) Join matching R,S tuples,
- (5) Project B,D attributes and place in result

Using the index on R.A to retrieve tuples where R.A = "c".  
 Using the index on S.C to find matching tuples in S for each R.C value found.  
 Eliminating tuples in S where S.E  $\neq$  2.  
 Joining matching tuples from R and S.  
 Projecting attributes B and D into the result.



## Overview of Query Optimization



## Example: SQL Query

Implementation of DBMS

```

SELECT title
FROM StarsIn
WHERE starName IN (
    SELECT name
    FROM MovieStar
    WHERE birthdate LIKE '%1960'
);

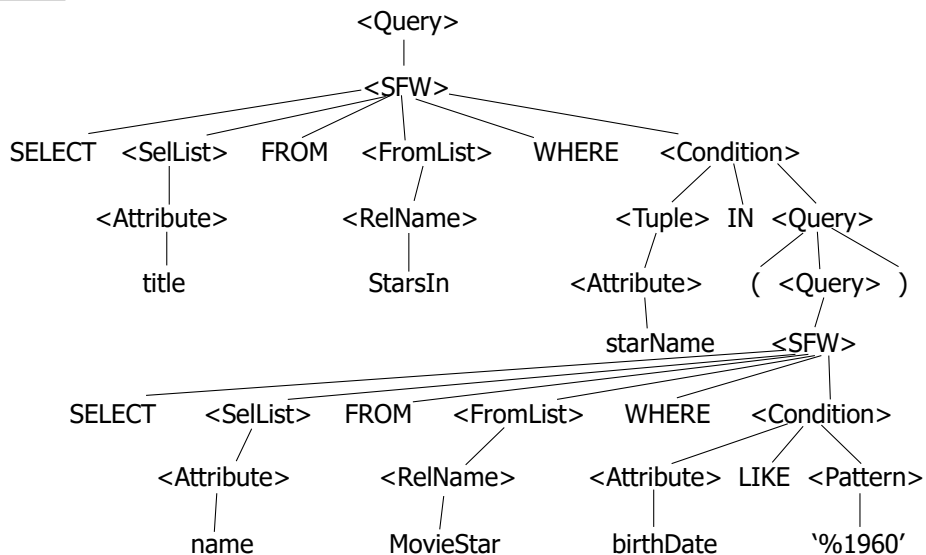
```

(Find the movies with stars born in 1960)

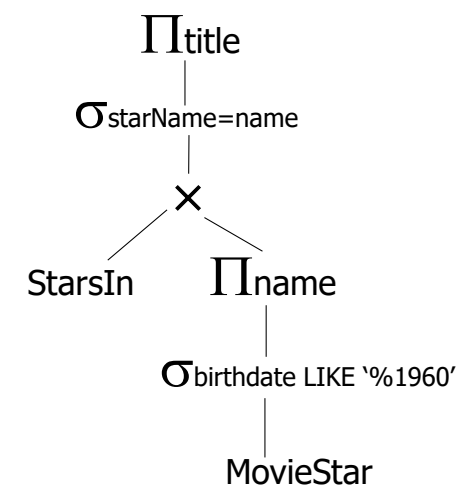
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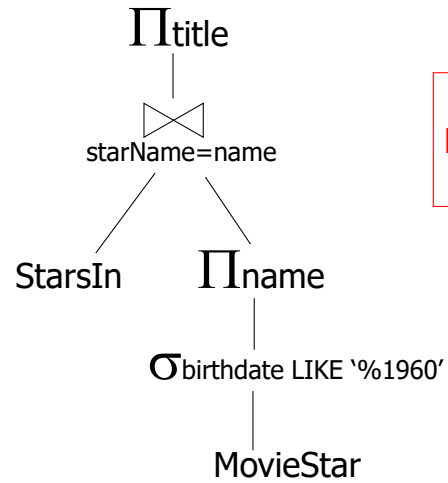
## Example: Parse Tree



## Example: Logical Query Plan

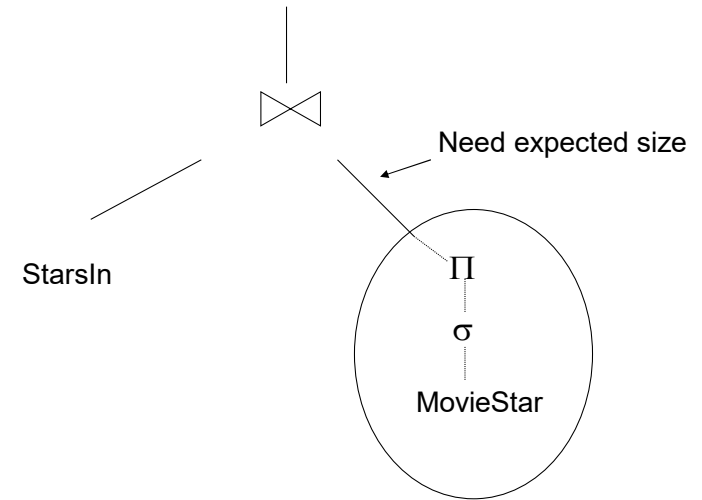


## Example: Improved Logical Query Plan

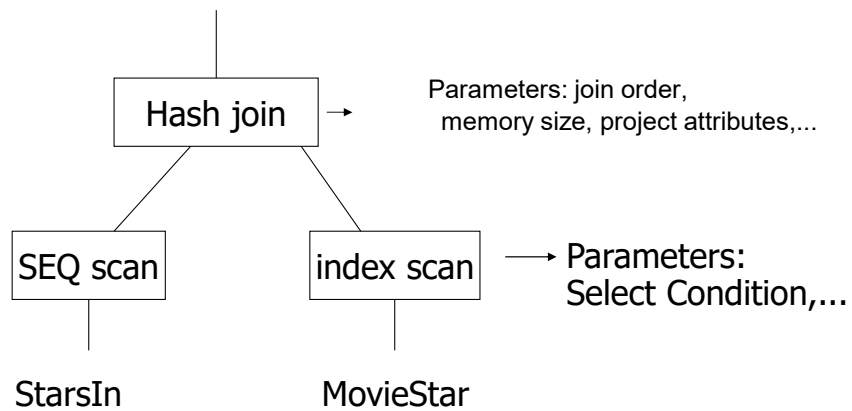


Question:  
Push project to  
StarsIn?

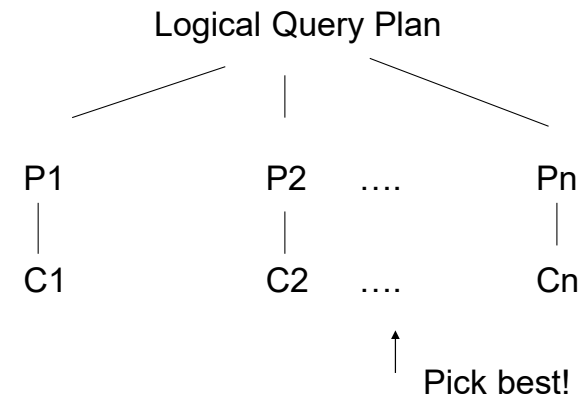
## Example: Estimate Result Sizes



## Example: One Physical Plan



## Example: Estimate Costs



# Algebraic Transformations

## Generating Plans

- Start with query definition.
  - A plan, but usually a terrible one.
- Apply algebraic transformations to find other plans.
- Relational algebra is a good start, but we need also to consider: GROUP BY, duplicate elimination, HAVING, ORDER BY.

## Algebraic Transformations

- Rules give equivalent expressions. meaning that whatever relations are substituted for variables, the results are the same.

# Rules: Natural joins & cross products & union

$$R \bowtie S = S \bowtie R$$

$$(R \bowtie S) \bowtie T = R \bowtie (S \bowtie T)$$

$$R \times S = S \times R$$

$$(R \times S) \times T = R \times (S \times T)$$

$$R \cup S = S \cup R$$

$$R \cup (S \cup T) = (R \cup S) \cup T$$

But beware of thetajoins (join condition different from =)

- associative law does not hold.

# Rules: Selects

$$\sigma_{p_1 \wedge p_2}(R) = \sigma_{p_1} [\sigma_{p_2}(R)]$$

$$\sigma_{p_1 \vee p_2}(R) = [\sigma_{p_1}(R)] \cup [\sigma_{p_2}(R)]$$

# Rules: Project

Let: X = set of attributes

Y = set of attributes

$$XY = X \cup Y$$

$$\pi_{xy}(R) = \pi_x[\pi_y(R)]$$

## Rules: $\sigma + \bowtie$ combined

Let  $p$  = predicate with only R attributes

$q$  = predicate with only S attributes

$m$  = predicate with only R,S attributes

$$\sigma_p(R \bowtie S) = [\sigma_p(R)] \bowtie S$$

$$\sigma_q(R \bowtie S) = R \bowtie [\sigma_q(S)]$$

## Rules: $\sigma + \bowtie$ combined

Some rules can be derived:

$$\sigma_{p \wedge q}(R \bowtie S) = [\sigma_p(R)] \bowtie [\sigma_q(S)]$$

$$\sigma_{p \wedge q \wedge m}(R \bowtie S) = \sigma_m[(\sigma_p(R) \bowtie (\sigma_q(S))]$$

$$\sigma_{p \vee q}(R \bowtie S) = [(\sigma_p(R) \bowtie S)] \cup [R \bowtie (\sigma_q(S))]$$

## Rules: $\pi, \sigma$ combined

Let  $x$  = subset of R attributes

$z$  = attributes in predicate P  
(subset of R attributes)

$$\pi_x[\sigma_p(R)] = \pi_x \left\{ \sigma_p \left[ \overset{\pi_{xz}}{\pi_x(R)} \right] \right\}$$

## Rules: $\pi, \bowtie$ combined

Let  $x$  = subset of R attributes

$y$  = subset of S attributes

$z$  = intersection of R, S attributes

$$\pi_{xy}(R \bowtie S) = \pi_{xy}\{[\pi_{xz}(R)] \bowtie [\pi_{yz}(S)]\}$$

Rules:  $\pi$ ,  $\bowtie$ , and  $\sigma$  combined

$$\pi_{xy} \{ \sigma_p (R \bowtie S) \} =$$

$$\pi_{xy} \{ \sigma_p [ \pi_{xz'} (R) \bowtie \pi_{yz'} (S) ] \}$$

$$z' = z \cup \{ \text{attributes used in P} \}$$

Rules:  $\sigma$ ,  $\cup$  combined

$$\sigma_p(R \cup S) = \sigma_p(R) \cup \sigma_p(S)$$

$$\sigma_p(R - S) = \sigma_p(R) - S = \sigma_p(R) - \sigma_p(S)$$

## Which are “good” transformations?

$$\sigma_{p1 \wedge p2} (R) \rightarrow \sigma_{p1} [ \sigma_{p2} (R) ]$$

$$\sigma_p (R \bowtie S) \rightarrow [ \sigma_p (R) ] \bowtie S$$

$$R \bowtie S \rightarrow S \bowtie R$$

$$\pi_x [ \sigma_p (R) ] \rightarrow \pi_x \{ \sigma_p [ \pi_{xz} (R) ] \}$$

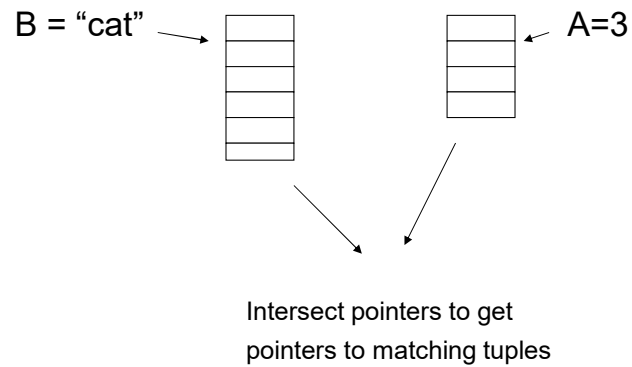
## Conventional wisdom: do projects early

Example:  $R(A,B,C,D,E)$   $x=\{E\}$   
 $P: (A=3) \wedge (B=\text{“cat”})$

$$\pi_x \{ \sigma_p (R) \} \quad \text{vs.} \quad \pi_E \{ \sigma_p \{ \pi_{ABE}(R) \} \}$$



## What if we have A, B indexes?



## Bottom line

There is no transformation that is good in any case

Usually good: early selections

- Variant: move selection up to the root and then down on multiple path

## Selections Should Go Up Then Down

StarsIn(title, year, starName)

Movie(title, year, studioName)

CREATE VIEW MoviesOf1996 AS

SELECT \*

FROM Movie

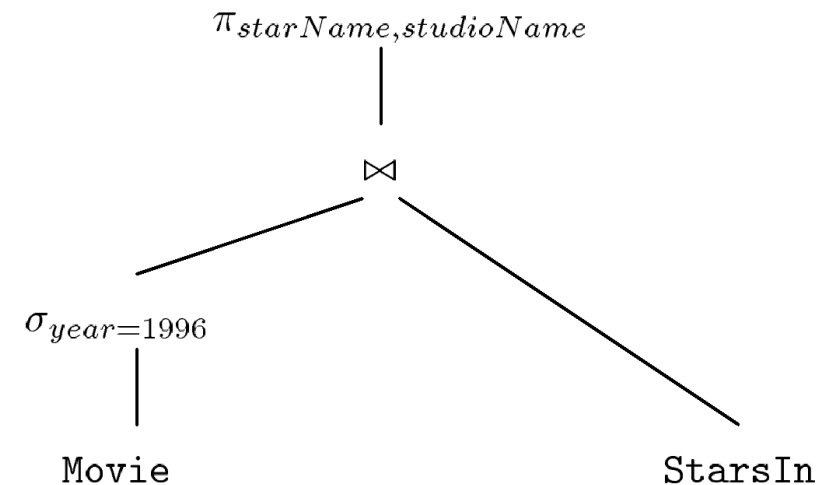
WHERE year = 1996;

SELECT starName, studioName

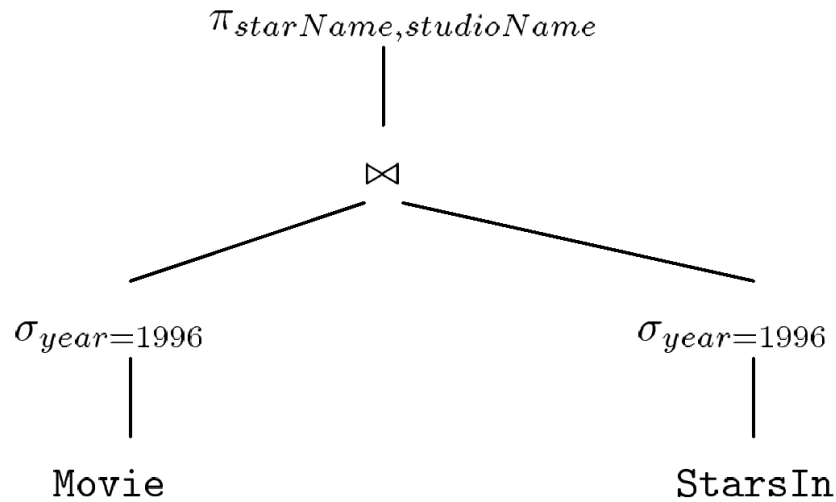
FROM MoviesOf1996 NATURAL JOIN StarsIn;

## Example Cont.

Initial query:



## Probably Better



## Estimating the Cost of a Query Plan

Goal is to count disk I/O's.

But we first have to estimate sizes of intermediate results.

Keep statistics for relation R

- $T(R)$  : # tuples in R
- $S(R)$  : # of bytes in each R tuple
- $B(R)$  : # of blocks to hold all R tuples
- $V(R, A)$  : # distinct values in R for attribute A
- $DOM(R, A)$  : # possible distinct values for attribute A (size of domain for A)

## Example

R

A	B	C	D
cat	1	10	a
cat	1	20	b
dog	1	30	a
dog	1	40	c
bat	1	50	d

A: 20 byte string

B: 4 byte integer

C: 8 byte date

D: 5 byte string

$$T(R) = 5$$

$$V(R, A) = 3$$

$$V(R, B) = 1$$

$$S(R) = 37$$

$$V(R, C) = 5$$

$$V(R, D) = 4$$

## Size estimates for $W = R1 \times R2$

$$T(W) = T(R1) \times T(R2)$$

$$S(W) = S(R1) + S(R2)$$

## Size estimate for $W = \sigma_{A=a}(R)$

$$S(W) = S(R)$$

$$T(W) = ?$$

## Estimate Depends on Assumption

R

A	B	C	D
cat	1	10	a
cat	1	20	b
dog	1	30	a
dog	1	40	c
bat	1	50	d

$$V(R,A)=3$$

$$V(R,B)=1$$

$$V(R,C)=5$$

$$V(R,D)=4$$

$$W = \sigma_{Z=val}(R) \quad T(W) = \frac{T(R)}{V(R,Z)}$$

Assumption: Values in select expression  $Z = val$  are uniformly distributed over possible  $V(R,Z)$  values.

## Alternate Assumption

R

A	B	C	D
cat	1	10	a
cat	1	20	b
dog	1	30	a
dog	1	40	c
bat	1	50	d

Alternate assumption

$$V(R,A)=3 \quad \text{DOM}(R,A)=10$$

$$V(R,B)=1 \quad \text{DOM}(R,B)=10$$

$$V(R,C)=5 \quad \text{DOM}(R,C)=10$$

$$V(R,D)=4 \quad \text{DOM}(R,D)=10$$

$$W = \sigma_{Z=val}(R) \quad T(W) = \frac{T(R)}{\text{DOM}(R,Z)}$$

Assumption: Values in select expression  $Z = val$  are uniformly distributed over possible  $\text{DOM}(R,Z)$  values.

## Selections Involving Inequality

What about  $W = \sigma_{Z \geq val}(R)$  ?

$$T(W) = ?$$

Solution # 1:  $T(W) = T(R)/2$

- Assumption: All split values are equally likely

Solution # 2:  $T(W) = T(R)/3$

- Assumption: Queries involving inequality ask more likely for a small fraction of possible tuples
- This assumption is usually preferred

## Selections Involving Inequality (cont.)

Solution # 3: Estimate values in range

Example R

	Z

Min=1



Max=20

$W = \sigma_{z \geq 15}(R)$

$$f = \frac{20-15+1}{20-1+1} = \frac{6}{20} \quad (\text{fraction of range})$$

$$T(W) = f \times T(R)$$