

A GRASP algorithm for the concrete delivery problem.

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Abstract

This paper addresses a novel variant of the Concrete Delivery Problem (CDP), which involves the efficient scheduling of ready-mixed concrete deliveries to construction sites while balancing the conflicting goals of minimizing transportation costs and maximizing customer satisfaction. In this study, we propose an exact formulation and a heuristic approach based on the Greedy Randomized Adaptive Search Procedure (GRASP), to tackle this challenging CDP variant. This variant introduces realistic side constraints, including driver working shifts, a minimum driver working time, and overtime penalties. Additionally, it considers the scenario where customers may request multiple types of concrete delivered within the same time window. We assess the performance of our heuristic using new public instances generated for this problem and provide a comparative analysis with another CDP variant to demonstrate its effectiveness.

Keywords: Vehicle scheduling; concrete delivery; GRASP; ready-mixed concrete

1 Introduction

Concrete is a widely used building material in construction projects. Its perishable nature is affected by many factors that impact its quality [Sinha et al., 2021], which is crucial for the durability and strength of the final construction. Concrete comes in two types: ready-mixed concrete (RMC) and site-mixed concrete (SMC). RMC is manufactured in a batch plant and delivered to the construction site, while SMC is produced on-site using raw materials stored on the construction site. Using SMC can avoid delays caused by road traffic, but it has a slower and more difficult production process, requires storage for mixing materials and equipment, and is suitable for low amounts of concrete. On the other hand, RMC has better quality and benefits from lower production costs [Muresan, 2019]. However, to take advantage of these benefits, the batch plant manager must ensure efficient and prompt delivery on the construction site, which may require a fleet of high-cost revolving drum trucks (concrete mixers) to dispatch the RMC.

Concrete delivery under the form of RMC is subject to many operational constraints that make the Concrete Delivery Problem (CDP) very challenging. In this paper, we study a variant of the CDP to schedule the daily production and dispatching of RMC for a company located in the province of Quebec, Canada. This company operates multiple batch plants with varying production rates, using a fleet of concrete mixers of different capacities. Each plant has its own fleet of trucks; however, under certain conditions, the trucks can move

between plants if necessary. The trucks must return to their home plant at the end of the day. The company owns two types of trucks with different capacities and can call on an external fleet when needed. They serve construction sites from any of their plants, with the first delivery starting at the time specified by the customer. The loading and unloading of a concrete mixer depend on the truck capacity, the loading rate at the plant, and the unloading rate at the construction site. Drivers are allocated based on their daily work schedules. A customer may request several types of concrete to be delivered within the same time window, with no required sequence for the orders, but an order can only start after the completion of the previous order. This constraint generalizes the linked order constraints of Durbin and Hoffman [2008] where some customers place two orders for the same day and request that they are linked (the second order begins only after the first order is completed). The setting of our study is similar to a variant of the CDP previously studied in Schmid et al. [2009, 2010]. However, we include the plant’s production rate and driver shift schedule. The company uses a centralized dispatcher system to schedule all daily orders, but this system has issues satisfying all daily demands without using an external fleet or using different plants to serve the same order.

According to Blazewicz et al. [2019], the CDP combines vehicle routing with scheduling issues to plan routes to deliver concrete from batch plants (depots) to customers’ construction sites. RMC is an on-demand product with a short life cycle from production through end use. It cannot be stored and cannot stay too long on a truck, or it will harden. Hence, concrete mixers must deliver RMC at the planned construction site shortly after its production. Tommelein and Li [1999] describes RMC production and delivery as an example of a just-in-time (JIT) production system in construction. A customer quantity requirement is often greater than the truck size and must be fulfilled by multiple deliveries. In that sense, CDP is similar to the vehicle routing problem with split delivery [Archetti and Speranza, 2008], except that the same truck may visit a customer more than once. Concrete hardens quickly, so multiple deliveries must be done back-to-back or at least close in time to avoid the problem of cold joint, which can reduce the strength and durability of the concrete. Customers request to be served within a specific time window, which can complicate truck-loading schedules when a plant can only load one truck at a time. Similarly, only one truck can unload at a time at a customer location, sometimes leading to concrete mixers queuing and waiting their turn to deliver. Furthermore, with trucks of varied sizes, loading, travel, and unloading times that may be uncertain, the CDP is a complex and challenging problem.

In this paper, we propose a mathematical model and a Greedy Randomized Search Procedure (GRASP) heuristic to solve a new variant of the CDP. Our model takes into consideration the working shifts of the drivers and the scheduling of multiple orders within the same time window at a construction site. To the best of our knowledge, this paper is the first that deals with these specific constraints in the context of the CDP.

The rest of the paper is organized as follows: Section 2 provides a literature review of previous work related to the CDP. Section 3 provides a formal description and mathematical model of the problem. Section 4 describes the GRASP algorithm and the constructive heuristics developed to solve this variant of the CDP. Section 5 presents computational experiments and sensitivity analyses to evaluate the proposed approach, and finally, section 6 presents the conclusions.

2 Literature review

Academic Research on concrete batch and delivery began in the late 1990s. Tommelein and Li [1999] described RMC as a prototypical example of a JIT production system in

84 construction and identified two practices for delivering it. One approach is for the customer
 85 to haul the product from the batch plant with their concrete mixer, while the other is for the
 86 batch plant to deliver the concrete directly to the customer’s location. This latter approach
 87 is the one that has been studied in all related papers found in the literature. Several
 88 works to schedule and dispatch concrete production and delivery have mainly focused on
 89 simulation-related methods. These methods can be standalone, such as those used by Zayed
 90 and Halpin [2001], Wang et al. [2001], Tian et al. [2010], Panas and Pantouvakis [2013] and
 91 Galić and Kraus [2016], among others. Alternatively, these methods can be hybridized with
 92 optimization techniques, such as those used by Feng et al. [2004], Lu and Lam [2005], and
 93 Feng and Wu [2006]. Wang et al. [2001] developed a simulation model to reveal the effect
 94 and value of the concrete mixers’ inter-arrival time on the productivity of hired unloading
 95 equipment on site. Feng et al. [2004] used a combination of genetic algorithm (GA) and
 96 simulation process to minimize the total waiting time for trucks at a customer site. The
 97 study focused on loading trucks with identical capacities at the same batch plant, with fixed
 98 loading and unloading durations. The GA was used to find the best loading sequence of RMC
 99 trucks to be assigned to different construction sites. The simulation process determined
 100 the loading, arrival, departure, and waiting time of trucks and thus evaluated the cost of
 101 each dispatching sequence. They evaluated their method using data from a batch plant
 102 in Taiwan with up to nine customers served. Mayteekrieangkrai and Wongthatsanekorn
 103 [2015] addressed the same problem with the same data using a bee algorithm (BA) and
 104 found better solutions than the GA. Lu and Lam [2005] used the same combination of GA
 105 and simulation to determine the optimal number of concrete mixers to be deployed and an
 106 optimal schedule for batching and delivering concrete. Their objective was to minimize the
 107 idle time of the site crew due to late concrete deliveries and truck queuing time. In this
 108 setting, it was also necessary to deliver a batch of mortar on-site to lubricate the unloading
 109 pump before the concrete delivery. As such, the simulation model also included the batch
 110 and delivery of mortar. Finding the best RMC fleet size was also the purpose of the discrete-
 111 event simulation model proposed by Panas and Pantouvakis [2013].

112 In addition to simulation-based methods, several other approaches have been used in the
 113 literature to solve the CDP. These include metaheuristics [Faria et al., 2006, Misir et al.,
 114 2011, Maghrebi et al., 2016b, Yang et al., 2022], exact methods [Yan and Lai, 2007, Asbach
 115 et al., 2009, Kinable et al., 2014], matheuristics [Schmid et al., 2009, 2010], Benders Decom-
 116 position [Maghrebi et al., 2014a], column generation (CG) [Maghrebi et al., 2014b, 2016a],
 117 Lagrangian relaxation [Narayanan et al., 2015], and machine learning approaches such as
 118 those used by Graham et al. [2006], Maghrebi and Waller [2014], Maghrebi et al. [2016c].
 119 Matsatsinis [2004] designed a decision support system (DSS) for the dynamic routing of
 120 both concrete and pumps that may be necessary for some construction sites to aid in the
 121 unloading of concrete. The DSS considered the availability of three plants but stipulated
 122 that vehicles fulfilling the same order must all load at the same plant. Orders that could
 123 not be executed immediately could be postponed for the next day. The routing of the
 124 pumps was modeled as a multi-depot vehicle routing problem with time windows. Naso
 125 et al. [2007] proposed a sequential GA method combined with constructive heuristics to
 126 solve another variant of the CDP. In this problem, the plant’s production schedule must
 127 account for orders for concrete to be delivered to a customer site and orders that customers
 128 must pick up themselves. The algorithm first schedules the plant loading operations before
 129 scheduling truck deliveries. The authors also developed a non-linear model that minimizes
 130 transportation costs, waiting times, outsourced costs, and overtime work. They ran experi-
 131 ments using real-world instances of a concrete supply chain in the Netherlands and found a
 132 reduction in the number of outsourced requests. Yan and Lai [2007] also considered overtime

133 considerations in their paper, which focused on scheduling RMC for one batch plant with
 134 two loading docks. The study took into account that overtime wages are paid for factory
 135 and construction site operations after 4 PM. They developed a mixed-integer programming
 136 (MIP) model on a time-space network to minimize travel times and operating costs at both
 137 normal and overtime working hours at the plant and the construction sites. They tested
 138 the model using real data consisting of three days of operation using a two-stage algorithm.
 139 First, they solved the MIP relaxation with CPLEX. Then, they simplified the original model
 140 by fixing some decision variables before solving it. The algorithm was found to improve the
 141 actual plant operation by 10%. A time-space network is the key component of the real-time
 142 DSS developed by Durbin and Hoffman [2008] to solve a dynamic CDP every five minutes.
 143 The DSS can receive new orders, schedule them on the fly, and handle unexpected events
 144 such as plant closures, truck breakdowns, and delays in transportation times. The authors
 145 combined the DSS with a tabu search (TS) heuristic to warm start CPLEX, which made the
 146 model performant enough to solve instances with up to 1,500 loads per day with up to 250
 147 trucks. The DSS also considers the case of a customer who places two orders, with the first
 148 being completed before the second starts. Further insights on the real-time planning and
 149 monitoring of CDP are available in Garza Cavazos [2021]. Another variant of the CDP is
 150 modeled by Schmid et al. [2009] as an integer multicommodity network flow (MCNF) prob-
 151 lem on a time-space network. In this paper, concrete is delivered using a heterogeneous fleet
 152 of vehicles, and each plant can load an unlimited number of trucks simultaneously. Some
 153 of the trucks have specialized equipment and must arrive first at certain construction sites
 154 to assist in unloading the concrete. The objective is to fulfill all orders, minimize the travel
 155 cost, and avoid delays between two consecutive unloading operations for an order. The
 156 model is typically solved using a matheuristic algorithm that combines the MCNF with a
 157 variable neighborhood search (VNS) heuristic. The method can quickly solve large problem
 158 instances with more than 60 orders per day without encountering any memory issues. The
 159 same problem is addressed by Schmid et al. [2010], who proposed a MIP model combined
 160 with a VNS and a very large neighborhood search (VLNS) to develop two matheuristics
 161 approaches. Comparisons between both matheuristics and a standalone VNS show that the
 162 former methods are much better and suitable for solving larger problem instances. These
 163 methods also provide better solutions for small to medium instances than the matheuristic
 164 used in Schmid et al. [2009]. A pure VNS approach with the same problem but without the
 165 use of instrumentation has been applied by Payr and Schmid [2009].

166 Regarding objectives, most authors have focused on minimizing travel time and delays
 167 between consecutive deliveries. However, some authors have been more interested in max-
 168 imizing customer satisfaction alone. We find these situations in the works of Durbin and
 169 Hoffman [2008], Kinable et al. [2014], Kinable and Trick [2014], Sulaman et al. [2017]. Kin-
 170 able et al. [2014] introduce a general MIP and constraint programming (CP) models of the
 171 CDP reflecting the main constraints commonly found in all CDP works: time lag and no
 172 overlapping between consecutive deliveries, covering of all customers' demands, delivery time
 173 window, and heterogeneous fleet. However, the model did not include constraints limiting
 174 the time that concrete may reside in a truck. The authors propose a constructive heuristic
 175 that schedules the visits to the customers one by one according to the start time of the
 176 visit and the truck capacity. The procedure is invoked multiple times for different permu-
 177 tations of the customer's order which is determined using the steepest descent (SD) local
 178 search procedure. One of the paper's main contributions is the creation of the first public
 179 test instances for the CDP with up to 50 customers, four batch plants, and 20 concrete
 180 mixers. They found the CP model to be highly effective in finding high-quality solutions in
 181 a relatively short time or improving existing schedules, while the MIP model can be used

to compute bounds, as it seems ineffective in solving large problem instances. Finally, the heuristic often yields good solutions in less than a second. A detailed analysis of the MIP model presented in Kinable et al. [2014] and of two more compact models can be found in the thesis of Hernández López [2020]. In Kinable and Trick [2014], we found an attempt to solve the previous problem with a logic-based Benders' approach. A generalization of the MIP model of Kinable et al. [2014] is addressed in Asbach et al. [2009]. This model simultaneously minimizes the total sum of travel costs and the penalty costs for customers with unfulfilled demand. A customer can request that all concrete deliveries come from the same plant or a subset of plants and that a delivery truck belongs to a subset of the vehicle fleet. The MIP model is used in a local search scheme as a black-box solver to reoptimize an incumbent solution in which a neighborhood operator has unfixed some variables. Tzanetos and Blondin [2023] provide an overview of the various methods used in the literature to address the CDP and categorizes the problem formulations based on the different concepts used in the literature. They also discussed the consistency between industry needs and existing constraints and provided insights into the datasets corresponding to real-world cases, identifying the necessary data for practitioners.

3 Problem description

The focus of this paper is on the distribution of RMC from a Canadian company that operates in the greater Montreal area. When a customer places an order, it is received at a control center and immediately assigned to one of the company's batch plants. These plants produce the concrete and then deliver it to the customer. The problem we are examining involves a set of customer orders, a set of concrete-mixer drivers, and a set of batch plants.

A customer i requests one or more types of concrete to be delivered to their construction site on a specific day, with the delivery service starting at the due time a_i . We call an order o a request for a specific type of concrete. q_i is the sum of the demands q_o of each order o placed, a_i is the desired arrival time of the first concrete mixer, and τ_i^u is the unloading rate for customer i . If the order requires more concrete than a single truck can carry, multiple deliveries are scheduled. We will accept a first delivery if it arrives within a time window of $[a_i, a_i + \tau^w]$, where τ_i^w is a user-defined parameter.

Let O_i be the set of all orders requested by customer i . Each element of O_i must be fully delivered before moving on to another order. Exactly one order $o \in O_i$ must have its first delivery start at a_i , while the others can start at most γ^2 time after o is completed. A plant is assigned to an order, and it must be the supplier of all subsequent deliveries of that order. To avoid cold joint problems with the concrete, subsequent deliveries of the same order must be made in close succession. We define a maximum time delay γ^1 after which no more deliveries are allowed. The customer's unloading rate and the quantity to be unloaded give the time required to unload a truckload. Let \mathcal{C} be the set of construction sites (customers) with a planned delivery for the day, and $\mathcal{O} = \{O_i, i \in \mathcal{C}\}$ be the set of all requested orders for all customers.

The company has two types of concrete mixer trucks with capacities of 8 and 12 cubic meters. Each driver k is assigned to a particular batch plant and is responsible for driving a truck with capacity Q_k . The set of drivers is represented by $K = \cup_{b \in \mathcal{B}} K_b$, where K_b is the set of drivers scheduled to start their shift at batch plant b . t_{ij} is the known time to travel between any two locations i and j . A scheduled driver k is required to start his shift at H_k , work a minimum of M_T hours and a maximum of N_T hours during regular working hours, with the possibility of overtime of up to O_T hours. β_3 and β_4 are the penalties for a driver working less than M_T and more than N_T .

229 A driver typically loads RMC at his assigned batch plant but may be required to drive
 230 to and load at other plants if needed. The batch plant produces concrete on demand using
 231 recipes specific to each order. This means that a truck can only haul RMC for one order,
 232 even if there is spare capacity. After unloading the RMC, driver k takes ρ minutes to clean
 233 the concrete mixer before proceeding.

234 Let n_o be the number of deliveries needed to fulfill the order o . n_o is not known in
 235 advance because we use a fleet of trucks with different capacities. However, we can compute
 236 its lower (n_o^{min}) and upper (n_o^{max}) bounds using the capacities of the largest (Q_{max}) and
 237 smallest (Q_{min}) available trucks.

$$n_o^{min} = \left\lceil \frac{q_o}{Q_{max}} \right\rceil \leq n_o \leq n_o^{max} = \left\lceil \frac{q_o}{Q_{min}} \right\rceil \quad \forall o \in \mathcal{O}. \quad (1)$$

238 Let d_o^j be the j^{th} visit with load q_o^j for order o . We represent the fulfillment of order
 239 o by the visits to the ordered set of delivery nodes $\mathcal{D}_o = (d_o^0, d_o^1, \dots, d_o^{n_o})$. The deliveries
 240 of customer i are the ordered set $\mathcal{D}_i = (\mathcal{D}_{o_1}, \mathcal{D}_{o_2}, \dots, \mathcal{D}_{o_{|O_i|}})$, where o_r is the r^{th} delivered
 241 order. We will refer to $d \in \mathcal{D}_i$ ($d \in \mathcal{D}_o$) as the d^{th} potential delivery of customer i (order
 242 o). $\mathcal{D} = \bigcup_{i \in \mathcal{C}} \mathcal{D}_i$ is the union of all delivery nodes.

243 Each of the company's plants has a single loading dock that can accommodate only one
 244 truck at a time. As a result, trucks often form a queue while waiting for their turn at the
 245 loading dock. Let \mathcal{B} be the set of batch plants. The plants are heterogeneous, as each plant
 246 b has its hourly loading rate, represented by τ_b^l , which affects the duration of the loading
 247 process. After loading the concrete, the driver spends α_b minutes adjusting the concrete in
 248 the truck before heading to the customer site. Each plant has its own assigned fleet of trucks,
 249 but it can borrow trucks from other plants. Let l_j be the loading dock node associated with
 250 delivery node j . After loading RMC at l_j , it must be fully delivered to j at most before Δ
 251 time, which is the concrete lifetime. We denote \mathcal{L}_b as the set of loading dock nodes of plant
 252 b and \mathcal{L} as the set of all loading docks.

253 A solution to the problem involves decisions about truck loading schedules, driver as-
 254 signments to different deliveries, and truck arrival times at construction sites for unloading.
 255 For a batch plant, the decision involves choosing which driver to load, when to load them,
 256 how much to load, and which construction site to deliver. For a driver, the decision is to
 257 determine the sequence of loading depots and delivery sites. And for a construction site,
 258 the decision involves determining the arrival times of all scheduled deliveries for the day.

259 Each driver leaves and returns to their home plant every day. We represent the home
 260 plant of a driver k with a starting depot s_k and an ending depot e_k . S and E are the sets
 261 of starting and ending depots, respectively.

262 We define our problem on a complete directed graph where $V = \{S \cup \mathcal{L} \cup \mathcal{D} \cup E\}$ is the
 263 set of nodes. The arc sets are $A = \{(i, j, k) \mid i, j \in V, k \in K\}$, $A^D = \{(i, j) \mid i, j \in \mathcal{D}\}$,
 264 and $A^L = \{(i, j) \mid i, j \in \mathcal{L}\}$. A corresponds to allowed movements of drivers from node i to
 265 node j . For each driver k , the allowed movements are the following:

- 266 • From the starting depot s_k to a loading dock $l \in \mathcal{L}$ or to the ending depot e_k .
- 267 • From a loading dock $l \in \mathcal{L}$ to a delivery node $d \in \mathcal{D}$.
- 268 • From a delivery node $d \in \mathcal{D}$ to a loading dock $l \in \mathcal{L}$ or to the ending depot e_k .

269 For a customer c , arcs in A^D link consecutive delivery nodes of the same order $\{(i, j) \in$
 270 $\mathcal{D}_o, o \in \mathcal{O}_c, i < j\}$, and pair of delivery nodes of two different orders $\{(i, d_{o_2}^0), i \in \mathcal{D}_{o_1}, i \geq$

271 $n_{o_1}^{min}, o_1, o_2 \in \mathcal{O}_c, o_1 \neq o_2\}$. Arcs in A^L link all pairs of loading docks of the same batch
 272 plant.

273 We define $\delta^+(i) = \{(i, j, k) \in A\}$ and $\delta^-(i) = \{(j, i, k) \in A\}$ as the outgoing and
 274 incoming arc sets of node $i \in V$; $\delta_D^+(i) = \{(i, j) \in A^D\}$ and $\delta_D^-(i) = \{(j, i) \in A^D\}$ are the
 275 outgoing and incoming arc sets of delivery node $i \in \mathcal{D}$. Similarly, $\delta_L^+(i) = \{(i, j) \in A^L\}$
 276 and $\delta_L^-(i) = \{(j, i) \in A^L\}$ are the outgoing and incoming arc sets of loading node $i \in \mathcal{L}$.

277 Let the binary variable x_{ij}^k be 1 if driver k travels from node i to j . Binary variable
 278 y_o is 1 when order o is completely served; v_i and w_i are the start and end of the loading
 279 (unloading) operation at node $i \in \mathcal{L} \cup \mathcal{D}$. Binary variable u_{ij} is 1 if node j is served just after
 280 i , the service being either an unloading or a loading operation. Variable q_j^k is the quantity to
 281 be loaded towards j with vehicle k . Let w_k^1 be a continuous variable indicating the difference
 282 between the driver's work time and the minimum number of hours to be worked in a day,
 283 and w_k^2 indicating the difference between the driver's work time and the normal work time.
 284 Let g_i be the time between the due date and the first service start for customer i .

285 The objective function minimizes total travel cost (TC), penalties associated with unful-
 286 filled orders, first delivery delays (FDD), driver underutilization costs (DUC), and driver
 287 overtime costs (DOC). Together, these components drive the optimization process to find a
 288 solution that efficiently balances travel costs, customer satisfaction, on-time delivery, driver
 289 utilization, and scheduling constraints.

$$\min \sum_{(i,j,k) \in A} t_{ij} x_{ij}^k + \beta_1 \sum_{o \in \mathcal{O}} (1 - y_o) + \beta_2 \sum_{i \in \mathcal{C}} g_i + \sum_{k \in K} (\beta_3 w_k^1 + \beta_4 w_k^2) \quad (2)$$

$$\sum_{j \in \delta^+(i)} x_{ij}^k = 1 \quad \forall i \in S, k \in K \quad (3)$$

$$\sum_{j \in \delta^-(i)} x_{ji}^k = 1 \quad \forall i \in E, k \in K \quad (4)$$

$$v_i \geq w_i - M(1 - x_{ij}^k) \quad i \in S, j \in \delta^+(i), k \in K \quad (5)$$

$$v_j \geq w_i + \alpha_b + t_{ij} - M(1 - x_{ij}^k) \quad \forall b \in \mathcal{B}, i \in \mathcal{L}_b, j \in \delta^+(i), k \in K \quad (6)$$

$$v_j \geq w_i + \rho + t_{ij} - M(1 - x_{ij}^k) \quad \forall i \in \mathcal{D}, j \in \delta^+(i), k \in K \quad (7)$$

$$w_i \geq v_i + \frac{q_j^k}{\tau_b^l} - M(1 - x_{ij}^k) \quad \forall b \in \mathcal{B}, i \in \mathcal{L}_b, j \in \delta^+(i), k \in K \quad (8)$$

$$w_j \geq v_j + \frac{q_j^k}{\tau_c^u} - M(1 - x_{ij}^k) \quad \forall c \in \mathcal{C}, j \in \mathcal{D}_c, i \in \delta^-(j), k \in K \quad (9)$$

$$w_j \leq v_i + \Delta + M(1 - x_{ij}^k) \quad j \in \mathcal{D}, i \in \delta^-(j), k \in K \quad (10)$$

$$v_{d_o^0} \geq a_i \quad \forall i \in \mathcal{C}, \forall o \in \mathcal{O}_i \quad (11)$$

$$g_i \geq v_{d_{o_1}^0} - a_i - M \left(\sum_{j \in \delta_D^-(d_{o_1}^0)} u_{jd_{o_1}^0} \right) \quad \forall i \in \mathcal{C}, \forall o_1 \in \mathcal{O}_i \quad (12)$$

$$g_i - a_i \leq \tau^w \quad \forall i \in \mathcal{C} \quad (13)$$

$$v_{d_{o_1}^0} \geq w_j - M(1 - u_{jd_{o_1}^0}) \quad \forall o_1 \in \mathcal{O}_i, j \in \delta_D^-(d_{o_1}^0) \quad (14)$$

$$v_{d_{o_1}^0} \leq w_j + \gamma^2 + M(1 - u_{jd_{o_1}^0}) \quad \forall o_1 \in \mathcal{O}, j \in \delta_D^-(d_{o_1}^0) \quad (15)$$

$$\sum_{o_1 \in \mathcal{O}_i} \sum_{j \in \delta_D^-(d_{o_1}^0)} u_{j,d_{o_1}^0} = |\mathcal{O}_i| - 1 \quad \forall i \in \mathcal{C}, |\mathcal{O}_i| > 1 \quad (16)$$

$$\sum_{o_1 \in \mathcal{O}_i} \sum_{j \in \delta_D^+(d_{o_1}^0)} u_{d_{o_1}^0,j} = |\mathcal{O}_i| - 1 \quad \forall i \in \mathcal{C}, |\mathcal{O}_i| > 1 \quad (17)$$

$$\sum_{j \in \delta_D^+(d_{o_1}^0)} u_{d_{o_1}^0,j} \leq 1 \quad \forall o_1 \in \mathcal{O} \quad (18)$$

$$\sum_{j \in \delta_D^-(d_{o_1}^0)} u_{j,d_{o_1}^0} \leq 1 \quad \forall o_1 \in \mathcal{O} \quad (19)$$

$$\sum_{j \in \delta_D^+(d_{o_1}^0)} u_{d_{o_1}^0,j} + \sum_{j \in \delta_D^-(d_{o_1}^0)} u_{j,d_{o_1}^0} \geq 1 \quad \forall o_1 \in \mathcal{O} \quad (20)$$

$$v_j \geq w_{j-1} - M(1 - u_{j-1,j}) \quad \forall o \in \mathcal{O}, j \in \mathcal{D}_o, j \geq 1 \quad (21)$$

$$v_j \leq w_{j-1} + \gamma^1 + M(1 - u_{j-1,j}) \quad \forall i \in \mathcal{C}, \forall o \in \mathcal{O}_i, j \in \mathcal{D}_o, j \geq 1 \quad (22)$$

$$u_{j-1,j} \geq u_{j,j+1} \quad \forall o_1 \in \mathcal{O}, j \in \mathcal{D}_{o_1}, 1 \leq j \leq n_{o_1} - 1 \quad (23)$$

$$u_{j-1,j} \geq \sum_{l \in \mathcal{L}} x_{lj} \quad \forall o_1 \in \mathcal{O}, j \in \mathcal{D}_{o_1}, j \geq 1 \quad (24)$$

$$v_j \geq w_i - M(1 - u_{i,j}) \quad \forall i \in \mathcal{L}, j \in \delta_L^+(i) \quad (25)$$

$$\sum_{j \in \delta_L^+(i)} u_{i,j} \leq 1 \quad \forall i \in \mathcal{L} \quad (26)$$

$$\sum_{j \in \delta_L^-(i)} u_{j,i} \leq 1 \quad \forall i \in \mathcal{L} \quad (27)$$

$$\sum_{j \in \delta_L^-(i)} u_{j,i} \geq \sum_{k \in K} \sum_{j \in \delta^-(i)} x_{ji}^k \quad \forall i \in \mathcal{L} \quad (28)$$

$$\sum_{j \in \delta_L^-(i)} u_{j,i} \geq \sum_{j \in \delta_L^-(i+1)} u_{j,i+1} \quad \forall i \in \mathcal{L} \quad (29)$$

$$\sum_{j \in \delta_L^-(i)} u_{j,i} + \sum_{j \in \delta_L^+(i)} u_{i,j} \geq \sum_{k \in K} \sum_{j \in \delta^-(i)} x_{ji}^k \quad \forall i \in \mathcal{L} \quad (30)$$

$$\sum_{k \in K} \sum_{j \in \mathcal{D}_o} q_j^k = q_o \quad \forall o \in \mathcal{O} \quad (31)$$

$$q_j^k \leq \sum_{i \in \delta^-(j)} Q^k x_{ij}^k \quad \forall j \in \mathcal{D}, k \in K \quad (32)$$

$$\sum_{k \in K} \sum_{j \in \delta^+(i)} x_{ij}^k \leq 1 \quad i \in \mathcal{L} \cup \mathcal{D} \quad (33)$$

$$\sum_{k \in K} \sum_{j \in \delta^+(i)} x_{ij}^k = \sum_{k \in K} \sum_{j \in \delta^-(i)} x_{ji}^k \quad i \in \mathcal{L} \cup \mathcal{D} \quad (34)$$

$$w_k^1 \geq M_T + H_k - v_{e_k} \quad \forall k \in K \quad (35)$$

$$w_k^2 \geq (v_{e_k} - H_k) - N_T \quad \forall k \in K \quad (36)$$

$$w_{e_k} \leq H_k + O_T \quad k \in K \quad (37)$$

$$0 \leq q_j^k \leq Q^k \quad j \in \mathcal{D}, k \in K \quad (38)$$

$$x_{ij}^k \in \{0, 1\} \quad (i, j) \in A, k \in K \quad (39)$$

$$u_{ij} \in \{0, 1\} \quad (i, j) \in A^D, k \in K \quad (40)$$

$$y_o \in \{0, 1\} \quad o \in \mathcal{O} \quad (41)$$

$$v_i \geq 0, w_i \geq 0 \quad i \in V \quad (42)$$

$$w_k^1 \geq 0, w_k^2 \geq 0 \quad i \in V \quad (43)$$

$$g_i \geq 0 \quad i \in \mathcal{C}. \quad (44)$$

β_1 to β_4 are the penalty coefficients of each component of the objective function (2). Constraints (3) and (4) state that driver k leaves his start node exactly once a day and returns to his end node. A driver cannot serve a node before the start of his shift with constraints (5). Constraints (6) and (7) set a driver to take some time after loading or unloading to adjust the concrete or clean the truck before moving on to the next node. The duration of the loading operation depends on the plant's loading rate and the amount q_j^k of RMC loaded (8). Similarly, the unloading service depends on the site's rate and q_j^k (9). Unloading operations must end at most Δ minutes after loading begins (10).

Constraints (11) - (15) ensure that the first service of any customer i must start after the due time a_i . This first service may be performed at the first delivery node of any order $\in \mathcal{O}_i$, and one order must be completed before another is started. It also enforces the precedence constraints between the last delivery of an order and the first delivery of the following order. Constraints (16) - (20) find the delivery sequence of all orders $\in \mathcal{O}_i$. With constraints (21) - (24), two trucks cannot unload at the same time for consecutive deliveries of the same order. Additionally, these constraints impose a maximum time delay between the two trucks. Similarly, constraints (25) - (30) ensure that two trucks cannot be loaded at the same time at a plant. Constraints (31) require that the cumulative load of all concrete mixers serving an order must equal the required quantities, and (32) bound a driver load. Constraints (33) require that a driver can only visit a loading/delivery node once. Constraints (34) are degree constraints. Constraints (35) - (36) calculate the difference between a driver's hours of service and the minimum and normal hours of service. Finally, constraints (37) - (44) define the nature and bounds of the variables.

Let us consider the solution of a small instance of our problem shown in Figures 1 and 2. Two batch plants B_1 and B_2 with three drivers serve two construction sites. Customer C_1 requests one order of $q_1^1 = 12 \text{ m}^3$. Customer C_2 requests three orders of $q_2^1 = 3$, $q_2^2 = 11$, and $q_2^3 = 1 \text{ m}^3$ of three different types of concrete. B_1 has two drivers (D_1, D_2) using concrete mixers of capacity 8 m^3 , and B_2 has D_3 with a capacity 12 m^3 . Figure 1 shows the flow of concrete mixers flow in the network. We schedule D_1 and D_2 to deliver 8 and 4 m^3 to C_1 , respectively. We select o_2^2 as the first order of C_2 . D_3 travels to B_1 to load q_2^2 , then visits C_2 before returning to his home plant. Meanwhile, after their first trip, D_1 and D_2 deliver the remaining orders of C_2 .

Figure 2 shows the sequence of loading and unloading operations. The first deliveries of C_1 and C_2 are timely and there is no gap between the two deliveries received by C_1 . There is a delay between the end of the first delivery and the start of the second delivery of C_2 , however, it is less than the maximal time delay of 20 minutes defined for this example.

4 Constructive heuristics and GRASP

In this section, we present the heuristic approach we implement to solve this variant of the Concrete Delivery Problem. Our method consists of constructing feasible solutions to the CDP with randomized greedy heuristics and iteratively invoking these heuristics in the

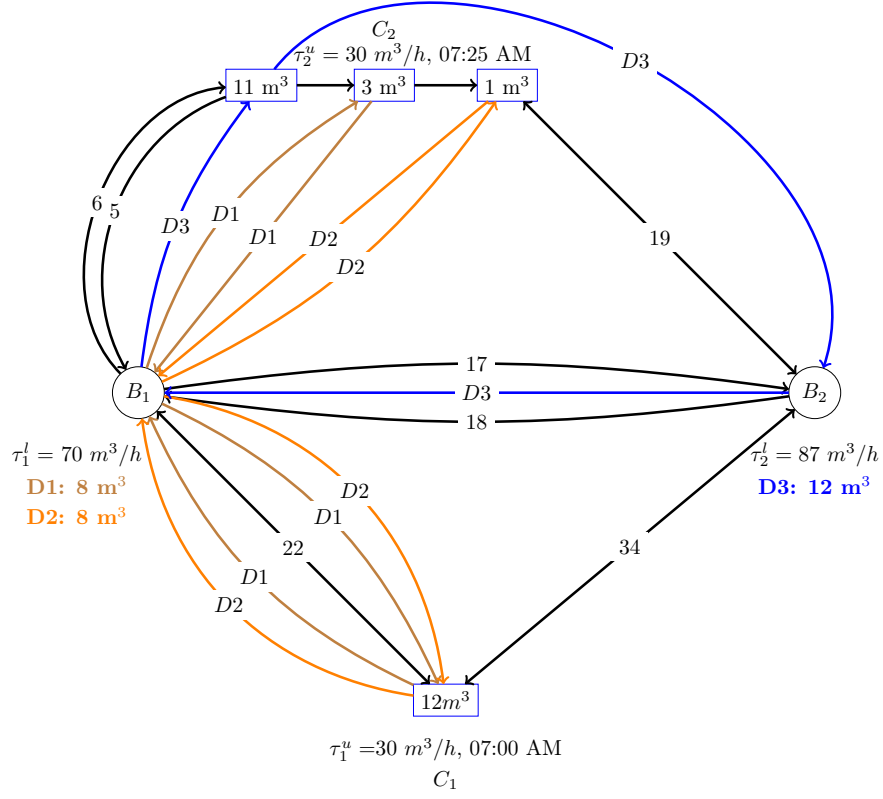


Figure 1: Solution of an instance with two plants, two construction sites, four orders, and three drivers.

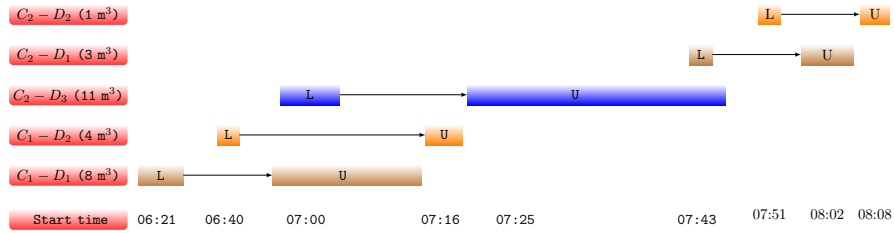


Figure 2: Schedule of the instance of Figure 1.

GRASP metaheuristic. From now on, we represent the scheduling of a delivery node d as the pair (L_d^k, U_d^k) of loading and unloading tasks. $L_d^k = (b, q_d, v_b, w_b)$ indicates that driver k starts loading q_d m^3 of RMC at plant b between $[v_b, w_b]$. $U_d^k = (k, v_d, w_d)$ indicates that driver k serves d between v_d and w_d . We then call a solution $S = \{\cup_{1 \leq j \leq |\mathcal{D}|} (L_j^k, U_j^k), k \in K\}$ the set of all loading and unloading tasks performed on a given day.

4.1 GRASP algorithm

The GRASP algorithm, proposed by Feo and Resende [1989], is a two-phase iterative suite consisting of constructive and local search algorithms. In the construction phase, a feasible solution S is generated using a greedy randomized algorithm. Then, a local search algorithm explores the neighborhood of S to identify a local optimum. Algorithm 1 outlines the pseudocode of the GRASP algorithm. To avoid redundant computations, a hash table H is used to ensure that the local search is not applied multiple times to the same solution. The procedure stops and returns the best overall solution when certain stopping conditions, such as reaching a time limit or a maximum number of iterations, are met.

Algorithm 1 Pseudo-code of the GRASP algorithm

Input: ϕ : number of iterations before path relinking

```

1  $S^* \leftarrow \emptyset$     $T \leftarrow \emptyset$     $Cost(S^*) \leftarrow \infty$ 
2 Initialize an empty hash table  $H$ 
3 while Conditions not met do
4    $S \leftarrow GreedyRandomizedHeuristic()$ 
5   if  $S \notin H$  then
6      $S \leftarrow LocalSearch(S)$ 
7     Add  $S$  to  $H$ 
8   if  $Cost(S) < Cost(S^*)$  then
9      $S^* \leftarrow S$ 
10 return  $S^*$ 

```

For the construction phase, we have developed two greedy randomized heuristics. The first heuristic, called customer-based insertion, schedules customers one at a time. On the other hand, the second heuristic, called delivery-based insertion, does not necessarily complete the scheduling of one customer before starting to plan another customer's schedule.

4.2 Customer-based insertion heuristic

The customer-based insertion heuristic builds a solution from scratch by scheduling all of a customer's orders one at a time. As shown in Algorithm 2, for each customer, we randomly select the first order to schedule. To schedule an order, we iterate over each of its delivery nodes, find a feasible pair of tasks, and add it to the current solution. For a delivery node d , we check if the list of operations $M[d]$ is empty. If it is, for each available driver k we simulate the loading and unloading operations (L_d^k, U_d^k) with the procedure *SimulateVisit*, and if k can serve d , we add k to a candidate list CL and (L_d^k, U_d^k) to $M[d]$.

The *SimulateVisit* procedure takes a partial solution, a delivery node d , a driver k and a numeric value λ as parameters. Its goal is to find the earliest time when an unloading service can start at d and the best position within the route of k . When planning to visit node d of order o and customer i with driver k , we first compute his expected delivery time v_d as follows:

$$v_d = \begin{cases} a_i + \lambda & \text{for the first visited node} \\ w_j + \text{rand}(\lambda, \gamma^1), j \in \mathcal{D}_o, u_{jd} = 1 \\ w_j + \text{rand}(\lambda, \gamma^2), j \notin \mathcal{D}_o, u_{jd} = 1 \end{cases}$$

Then we determine the start loading time v_l of the corresponding dock node l by subtracting the travel time, adjustment time, and loading duration from v_d . Starting from v_l we check when k will be available at an idle loading bay and adjust w_l accordingly. Changing w_l can cause the cold-joint constraints to be violated, especially for a customer's subsequent deliveries, and thus make the schedule infeasible. Once we have v_l , we can check for the best position to insert the visit of d into the route of k .

We extract from CL the restricted candidate list (RCL) of drivers for whom the cost of visiting d falls within a specified range based on the parameter θ . If RCL is empty and a visit to d cannot be scheduled due to cold-joint constraints, we use the *DelayPreviousDelivery* procedure to determine if there is a previous delivery of the same order that we can delay the start of service to visit d feasible. This procedure returns the index of the node and λ , which is the value of the delay. λ is also the same parameter given to *SimulateVisit*. If there is such a previous node, we backtrack to it and restart the scheduling.

If RCL is not empty, we select a random driver from it, insert its corresponding load and unload tasks into S , and update the remaining quantities for the order and customer demands. The algorithm returns at the end the constructed solution S .

Consider the scenario where two customers require their services to start at the same time or within the same time window. In this case, we can either finish scheduling one customer before the other or schedule both simultaneously. If there are sufficient resources available, either option would be feasible. However, when resources are limited, the customer-based insertion heuristic may leave some customers unscheduled. To address this limitation, we introduce the delivery-based insertion heuristic.

4.3 Delivery-based insertion heuristic

The delivery-based insertion heuristic constructs a feasible solution from scratch by scheduling a delivery node one at a time. The pseudocode for this heuristic is outlined in Algorithm 3. It starts with an empty solution S and initially fills CL with the first delivery of a randomly selected order for each customer. Within each iteration of the *while* loop, we filter CL to obtain a reduced candidate list CL' of deliveries from a given neighborhood. With this filtering, we can force the algorithm to schedule nodes with certain criteria first, which could be nodes from customers with the same demand, due date, or geographic area. We can also decide whether to schedule customers with the highest (or lowest) demand or the earliest (latest) due date first.

For each delivery d in CL' , the algorithm determines the best available driver k and adds the corresponding loading and unloading task (L_d^k, U_d^k) to a list of tasks. This is done using the *SimulateVisit* procedure described earlier. Next, the algorithm constructs a RCL from the list of tasks. If it is empty, the algorithm proceeds to the next iteration. Otherwise, it randomly selects a pair of tasks from the RCL , inserts them into S , and updates the remaining order and customer quantities. If an order o is not fulfilled after visiting d_o^j , we add its next delivery node d_o^{j+1} to CL . Otherwise, if the customer has remaining orders, we select the first delivery node $d_{o'}^0$ of another randomly selected order o' and add it to CL .

4.4 Local Search

After the construction phase, the local search phase iteratively invokes five operators using a first-improvement strategy. The first operator (*Swap Load*) exchanges loads between

Algorithm 2 Customer-Based insertion algorithm

Input: S : empty solution S , K : vehicles set

Π : custom sorted customers list

```
1  $M \leftarrow \emptyset$  // List of pair of loading and unloading tasks for all delivery nodes
2  $CL \leftarrow \emptyset$  // Candidate driver list all delivery nodes
3 for each customer  $i \in \Pi$ 
4   Shuffle  $\mathcal{O}_i$ 
5   for each order  $o_1 \in \mathcal{O}_i$ 
6      $\lambda \leftarrow 0$ 
7     for  $j = 0$  to  $n_{o_1}^{max} - 1$  do
8       Delivery  $d = \mathcal{D}_{o_1}^j$ 
9       if  $M[d] == \emptyset$  then
10         for each  $k \in K$ 
11            $(L_d^k, U_d^k) \leftarrow \text{SimulateVisit}(S, d, k, \lambda)$ 
12            $Cost(d, k) \leftarrow \text{Cost of } (L_d^k, U_d^k)$ 
13           Add  $(L_d^k, U_d^k)$  to  $M[d]$ 
14            $CL[d] \leftarrow \{k\}$ 
15        $C_{min} \leftarrow \min \{C(x), x \in M[d]\}, C_{max} \leftarrow \max \{C(x), x \in M[d]\}$ 
16        $RCL \leftarrow \{k \in CL[d], C(d, k) \leq C_{min} + \theta(C_{max} - C_{min})\}$ 
17       if  $RCL == \emptyset$  then
18          $(ind, delay) = \text{DelayPreviousDelivery}(S, d)$ 
19         if  $j$  is none then
20           | break // continue with next customer
21          $j \leftarrow ind, \lambda \leftarrow delay$ 
22         continue // backtrack to  $ind$  position
23       Select from  $RCL$  a random driver  $k$  to visit  $d$  with load  $q_d^k$ 
24        $M[d] \leftarrow M[d] \setminus (L_d^k, U_d^k), CL[d] \leftarrow CL[d] \setminus \{k\}$ 
25        $S \leftarrow S \cup (L_d^k, U_d^k)$ 
26        $q_i \leftarrow q_i - q_d^k; q_{o_1} \leftarrow q_{o_1} - q_d^k$ 
27        $\lambda \leftarrow 0$ 
28       if  $q_{o_1} \neq 0$  then
29         | continue
30       else if  $q_i \neq 0$  then
31         | break
32 return  $S$ 
```

Algorithm 3 Delivery-based insertion algorithm

Input: S : empty solution S

```
1  $CL \leftarrow \emptyset$ 
2 for each customer  $i$ 
3   | Select a random order  $o_1 \in \mathcal{O}_i$ 
4   |  $CL \leftarrow CL \cup \{d_{o_1}^0\}$ 
5 while  $CL \neq \emptyset$  do
6   |  $CL' \leftarrow \text{Filter}(CL)$ 
7   |  $Tasks \leftarrow \emptyset$  // List of loading and unloading tasks
8   | for each  $d \in CL'$ 
9     |  $Tasks \leftarrow (L_d^k, U_d^k)$  //  $k$  is the best available driver to visit  $d$ 
10  |  $C_{min} \leftarrow \min \{Cost(x), x \in Tasks\}$ ,  $C_{max} \leftarrow \max \{Cost(x), x \in Tasks\}$ 
11  |  $RCL \leftarrow \{x \in Tasks, Cost(x) \leq C_{min} + \theta(C_{max} - C_{min})\}$ 
12  | if  $RCL \leftarrow \emptyset$  then
13    | continue
14  | Select random operations  $(L_{d_o^j}^k, U_{d_o^j}^k)$  of customer  $i$  (order  $o$ ) from  $RCL$ 
15  |  $S \leftarrow S \cup (L_{d_o^j}^k, U_{d_o^j}^k)$ 
16  |  $q_i \leftarrow q_i - q_{d_o^j}^k$ ;  $q_o \leftarrow q_o - q_{d_o^j}^k$ 
17  | if  $q_o \neq 0$  then
18    |  $CL \leftarrow CL \cup \{d_o^{j+1}\}$ 
19  | else if  $q_i \neq 0$  then
20    | Select another order  $o' \in \mathcal{O}_i$ 
21    |  $CL \leftarrow CL \cup \{d_{o'}^0\}$ 
22  | Update  $CL$ 
23 return  $S$ 
```

two deliveries of the same order. The *Swap Driver* operator explores alternative driver assignments by swapping drivers assigned to two delivery nodes. The *Relocate* operator removes a delivery node and places it in a different location. The *Consolidate Load* operator assigns an order request initially split between two drivers to a single driver if the driver's capacity allows. The *Remove and Reschedule* operator selects an unscheduled customer, denoted i , within the current solution. It then identifies a set C containing scheduled customers with the same time slot as i . All elements of C are removed and rescheduled along with i . This local search process continues until no further improvements can be made or a timeout is reached.

5 Computational experiments

In this section, we present and discuss the results of computational experiments conducted using the GRASP heuristic described in section 4. The implementation of the GRASP algorithm is coded in C++. We run our experiments on the benchmark data used in Kinable et al. [2014], and on a new dataset extracted from delivery operations records provided by our industry partner.

5.1 Generation of instances

The dataset used in this section was obtained from our partner and contains records representing delivery operations from up to 8 production centers for 36 days. From this historical data, we extract information such as daily orders delivered, plant assignments to orders, and the number of available drivers. We created 36 instances from this data, where each instance corresponds to a daily operation. To maintain confidentiality, we have removed the GPS coordinates of customers and plants, but have included two matrices containing the distances and driving times between all plants and customers. An instance contains information such as each driver’s capacity, associated batch plant, and shift start time (which we generate). For each customer, we have the due time, the total demand, the number of orders (type of concrete) received, and its index in the time (distance) matrix. For each order, we have its demand and the corresponding production plant. Finally, we have the loading capacity for each plant, and also its index in the time matrix. The name of an instance has the format $C_k_n_o_z$, where k is the number of available drivers, n is the number of customers, o is the total number of daily orders, and z is the number of plants. The dataset is divided into small, medium, and large sets according to the total number of daily orders. We have summarized the dataset in Table 1. The dataset is available upon request as a contribution to the CDP literature.

Table 1: Instances summary

	#	Demand (m ³)	#Order	#Client	#Driver	#Depot
Small	8	226.5 - 937.5	7 - 14	4 - 11	13-35	1-3
Medium	14	1,160.5 - 2,971.0	43 - 98	40 - 89	76-137	6-8
Large	14	3,078. - 3,953.5	107 - 136	92 - 127	129-150	8

5.2 Results for the instances of Kinable et al. [2014]

Kinable et al. [2014] provided a benchmark dataset for their variant of the *CDP*. Although their primary objective is to maximize the total load delivered each day, without considering loading operations at a plant and ensuring deliveries within specified time windows, we still use this dataset to analyze and compare the performance of our algorithm under different conditions. Table 2 shows the performance of the GRASP heuristic along with the other methods (CP, MIP, SD-heuristic, and Hybrid) used in Kinable et al. [2014]. For each method, the table shows the average execution time in milliseconds and the corresponding gap between the obtained solution and the upper bound provided by Kinable et al. [2014].

Table 2: Performance of the GRASP heuristic on the CDP benchmark instances

		CP		MIP		SD-heuristic		Hybrid		GRASP	
		Gap (%)	Time (ms)	Gap (%)	Time (ms)	Gap (%)	Time (ms)	Gap (%)	Time (ms)	Gap (%)	Time (ms)
Set A	Avg	4.2	197,012	7.3	13,405,798	9.1	23	7.0	100,765	5.7	13,186
	Opt	40/64		37/64		30/64		35/64		35/64	
Set B	Avg	12.1	357,313	-	-	16.3	1,331	-	-	13.8	574,983
	Opt	55/128		-		40/128		-		44/128	

Overall, the GRASP algorithm shows promise in providing near-optimal solutions in a relatively short time for this benchmark of the CDP, making it a suitable candidate for fur-

ther analysis and real-world application. It outperformed all methods except CP, achieving an average distance of 5.7% (13.8%) with a runtime of 13,186 (574,983) milliseconds for Set A (Set B). The SD-heuristic appears to be much faster, but GRASP provides a better balance between solution quality and computation time. It should also be noted that the exact MIP, CP, and Hybrid are initialized with the results of the SD-heuristic.

5.3 Results for the generated instances

The computational results of our instances solved with the GRASP heuristic are summarized in the tables below. The parameters used in our experiments are listed in Table 3.

Table 3: Parameters of the real-world instances

Parameter	Value
Time window (τ^w)	60 min
Unloading duration (τ_c^u)	2 min/ m^3
Cleaning duration (ρ)	10 min
Adjustment duration (α)	10 min
Max travel time (Δ)	120 min
Min working time (M_T)	180 min
Max working time (N_T)	480 min
Max overtime duration (O_T)	120 min
Max delay between two consecutive deliveries of the same order (γ^1)	20 min
Max delay between two consecutive deliveries of different orders (γ^2)	25 min
Penalty of unfulfilled orders (β_1)	10,000
Penalty of first delivery delay (β_2)	1,000
Penalty for driver underutilization (β_3)	30
Driver overtime penalty (β_4)	20

The table 4 contains the detailed results for all instances with a stop criterion of 3600 seconds. The table shows the demand of each instance, the average, and the best values of the objective function when solving each instance five times. All daily orders of the small instances are completely served by our algorithm within these five iterations, as shown in column UQ , which reports the undelivered quantity. For the medium and large instances, 99.57% and 99.5% of the total demands are delivered. The sum of driver underutilization costs (DUC) is high for medium and large instances. This indicates the underutilization of the scheduled fleet. Some drivers are not scheduled at all or work very little. The sum of driver overtime costs (DOC) is also high for these instances. This can be explained by the fact that the algorithm prefers to put drivers on overtime rather than use a driver who has to travel to another plant for a delivery, which would increase travel costs (TC).

FDD represents the sum of the delays of the first deliveries. In the case of small instances, all but one of the first deliveries are on time. However, for the other instance sets, there is at least one customer with a late first delivery. To provide insight into the actual delay experienced by customers, we report mFDD, which is the maximum delay among all first deliveries. This information reveals that for small instances, the maximum delay ranges between 0 and 35.7 minutes. For medium instances, it varies from 16.8 to 60 minutes, and for large instances, it falls within the range of 56 to 60 minutes.

Table 5 shows that as the algorithm runtime increases, a higher percentage of deliveries are completed. For small instances, all requests are delivered in less than a minute, while for medium and large instances, 99% of requests are delivered.

Table 4: Results with all instances

		Demand (m^3)	Avg						Best						
			TC (min)	UQ (m^3)	FDD (min)	DUC (min)	DOC (min)	Z	TC (min)	UQ (m^3)	FDD (min)	$mFDD$ (min)	DUC (min)	DOC (min)	Z
Small	C_13_11_12_1	226.5	1,243.5	0.0	0.0	10.8	0.0	1,568.3	1,243.5	0.0	0.0	0.0	0.0	0.0	1,243.5
	C_13_5_8_1	267.0	745.1	0.0	0.0	0.0	0.0	745.1	745.1	0.0	0.0	0.0	0.0	0.0	745.1
	C_18_6_11_2	333.5	753.3	0.0	0.0	145.9	0.0	5,130.0	753.3	0.0	0.0	0.0	118.7	0.0	4,315.1
	C_15_4_7_2	375.0	1,015.6	0.0	0.0	148.2	150.5	8,470.9	1,015.4	0.0	0.0	0.0	123.4	110.3	6,924.5
	C_19_7_8_2	388.0	1,747.2	0.0	0.0	349.8	159.0	15,421.6	1,781.8	0.0	0.0	0.0	186.0	0.0	7,361.5
	C_29_10_14_3	613.5	3,510.1	0.0	59.5	194.6	331.9	75,488.1	3,493.4	0.0	59.5	35.7	120.5	60.0	67,810.4
	C_31_8_11_3	776.0	2,314.8	0.0	0.0	804.3	640.7	39,256.8	2,278.2	0.0	0.0	0.0	503.5	617.0	29,722.9
	C_35_9_10_3	937.5	4,175.5	0.0	0.0	222.1	669.3	24,224.7	4,163.1	0.0	0.0	0.0	243.3	570.0	22,863.2
Medium	C_76_40_43_6	1,160.5	6,055.8	0.0	49.1	3,286.4	990.0	173,509.5	5,990.6	0.0	33.9	25.4	3,061.3	788.6	147,510.1
	C_104_42_47_8	1,565.0	8,107.1	12.0	53.3	3,637.1	119.4	1,372,936.3	8,301.9	12.0	54.3	16.8	3,200.5	140.1	1,361,393.1
	C_94_63_70_7	1,746.5	13,783.0	0.0	238.7	983.2	1,554.6	313,077.0	13,673.5	0.0	195.9	59.7	1,025.2	1,407.3	268,524.2
	C_116_67_78_8	1,839.5	13,456.8	0.0	132.7	1,869.0	614.3	214,501.3	13,484.8	0.0	98.0	22.7	1,792.8	622.4	177,710.8
	C_116_71_82_8	2,060.0	11,393.8	9.0	265.1	2,714.8	1,054.6	1,279,068.9	10,793.3	9.0	242.0	41.8	3,197.9	665.2	1,262,000.5
	C_117_57_70_6	2,327.5	14,975.0	0.0	324.1	1,005.5	1,149.6	392,281.0	15,303.5	0.0	295.2	54.6	659.4	1,083.8	351,940.4
	C_137_79_83_7	2,425.0	17,644.3	0.0	553.8	2,320.4	1,993.3	680,888.1	17,379.3	0.0	474.0	55.7	2,964.4	2,016.3	620,601.6
	C_127_66_80_8	2,512.5	14,584.3	0.0	128.3	1,600.0	1,451.5	219,949.8	14,499.2	0.0	127.5	47.3	1,390.2	1,212.8	207,962.2
	C_128_68_74_7	2,595.0	18,450.6	3.7	566.6	1,317.5	2,706.2	1,048,712.1	18,261.4	0.0	473.4	56.0	1,764.7	2,525.6	595,143.5
	C_136_85_97_8	2,673.0	16,831.6	0.0	379.9	2,702.4	2,368.0	525,199.5	17,241.3	0.0	323.7	50.2	2,190.5	2,767.1	461,973.3
	C_128_78_85_8	2,685.5	15,679.8	63.0	474.5	1,399.6	2,394.4	6,880,077.6	15,830.6	63.0	432.7	57.8	1,206.8	2,272.7	6,830,154.3
	C_131_77_85_8	2,893.5	16,988.0	0.0	374.5	1,557.9	1,996.1	478,106.8	16,565.6	0.0	352.1	44.6	1,624.3	1,322.5	443,865.0
	C_137_89_97_7	2,939.5	21,716.4	9.8	924.4	821.0	3,494.4	2,020,622.6	21,311.3	0.0	799.5	51.8	887.3	3,486.7	917,162.4
	C_133_84_98_7	2,971.0	20,435.5	46.1	1,141.3	894.1	2,127.8	5,841,090.1	20,520.4	9.0	1,411.0	59.5	705.0	1,871.9	2,390,157.6
Large	C_132_98_109_8	3,078.5	22,994.6	0.0	465.5	496.5	3,804.8	579,471.0	22,712.7	0.0	351.5	56.2	803.2	4,011.3	478,549.4
	C_129_101_119_8	3,229.0	17,323.1	11.0	657.8	1,577.6	2,375.9	1,869,937.5	17,311.8	11.0	598.8	58.4	1,507.7	1,948.1	1,800,315.9
	C_141_114_136_8	3,350.5	19,891.6	39.1	1,255.8	1,366.2	2,251.9	5,271,698.5	19,556.2	18.0	1,366.7	57.9	1,380.0	2,695.1	3,281,568.6
	C_140_114_132_8	3,401.5	21,917.6	23.8	1,254.1	680.1	3,389.9	3,744,172.5	22,590.2	17.5	1,248.5	58.7	766.3	3,267.6	3,109,441.2
	C_143_101_123_8	3,437.5	23,477.2	0.0	677.7	955.5	4,369.4	817,244.5	23,806.9	0.0	617.3	56.0	1,302.2	5,147.9	783,123.1
	C_137_112_129_8	3,471.0	22,089.2	0.0	546.6	544.8	4,187.3	668,737.0	21,195.2	0.0	456.6	55.0	883.9	3,532.1	574,935.0
	C_142_114_129_8	3,499.5	20,678.2	35.7	1,007.5	1,119.7	4,133.1	4,714,436.9	21,243.7	21.0	907.0	59.8	1,038.0	4,016.6	3,139,750.0
	C_149_98_122_8	3,513.0	19,859.0	28.4	1,141.7	2,154.6	2,649.9	4,119,224.3	19,602.8	21.0	859.2	55.7	2,342.9	2,728.2	3,103,676.6
	C_139_98_108_8	3,541.0	21,060.5	0.0	966.2	684.9	3,585.4	1,079,477.1	21,084.8	0.0	867.2	59.8	834.9	4,133.9	996,046.7
	C_144_108_122_8	3,670.5	23,330.4	2.0	1,123.4	536.2	3,251.6	1,427,866.8	22,882.8	0.0	969.7	57.8	649.7	3,587.1	1,083,850.9
	C_142_92_107_8	3,684.5	23,179.0	0.0	578.3	384.1	4,260.4	698,184.4	23,610.6	0.0	449.2	59.8	315.7	4,257.2	567,403.7
	C_138_114_136_8	3,739.5	23,614.6	11.7	1,225.1	837.4	5,668.6	2,557,166.5	22,859.0	7.5	1,107.0	58.3	1,224.2	5,078.2	2,018,119.1
	C_150_127_136_8	3,946.5	24,940.3	0.0	949.5	775.5	5,384.3	1,105,391.3	24,939.2	0.0	829.0	57.1	805.9	6,166.7	1,001,490.6
	C_148_112_131_8	3,953.5	24,286.0	34.0	1,247.8	657.0	3,009.5	4,752,026.9	24,221.7	24.5	1,118.5	57.1	859.7	3,483.3	3,688,169.1

Table 5: RMC delivery completion within different runtimes of the GRASP

		Runtime (min)				
		1	5	10	30	60
Small	%Load	100.00	100.00	100.00	100.00	100.00
Medium	%Load	99.00	99.29	99.29	99.43	99.57
Large	%Load	99.00	99.21	99.36	99.43	99.50

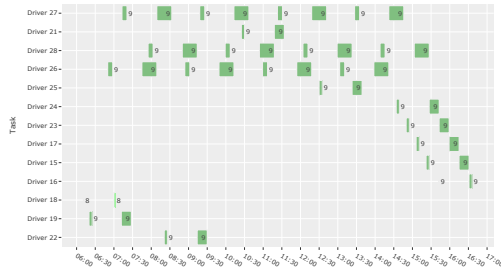
Figure 3 provides a visual representation using Gantt charts of the loading and unloading operations for the orders assigned to each plant in instance $C_{29_10_14_3}$. It also shows the different assignments of each driver throughout the day. This instance has three plants, twenty-nine drivers, and ten customers, with two customers having multiple orders. Customer 8 has two orders (o_8, o_9) assigned to plant 0 while customer 9 has four orders (o_{10} - o_{13}) assigned to plant 2. All the order requirements are in the table 6.

Table 6: Informations of instance $C_{29_10_14_3}$

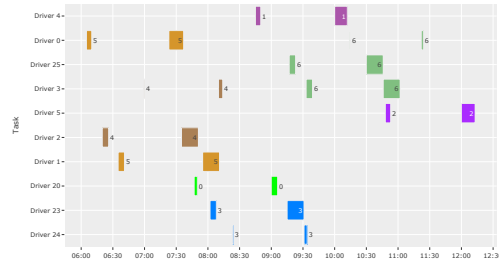
Order	0	1	2	3	4	5	6	7	8	9	10	11	12	13
Customer	0	1	2	3	4	5	6	7	8	8	9	9	9	9
Demand	3.0	6.0	6.5	9.5	10.0	15.0	17.0	118.0	1.0	210.5	1.0	3.0	19.0	194.0
Plant	1	1	1	1	1	1	1	2	0	0	2	2	2	2
TW	09:00	10:00	12:00	09:15	07:00	07:00	10:30	10:00	07:00	07:00	07:25	07:25	07:25	07:25

We can see that the loading operations for each plant do not overlap, and the unloading operations occur sequentially, one after the other, at each worksite. Plant 0 is responsible for both orders from customer 8. In the figure 3a, order o_8 is served before o_9 , starting at the due time. Each row in the figure represents the pairs of loading and unloading tasks performed by a driver. The number next to a task refers to the order. Figure 3c shows how the loading bay is alternately assigned to orders o_{13} and o_7 between 10:00 and 14:00. Driver 26 starts his service at plant 0, serves order o_9 four times, and travels to plant 2 to make the final delivery of order o_{13} . Driver 25 also loads at both plants 0 and 1.

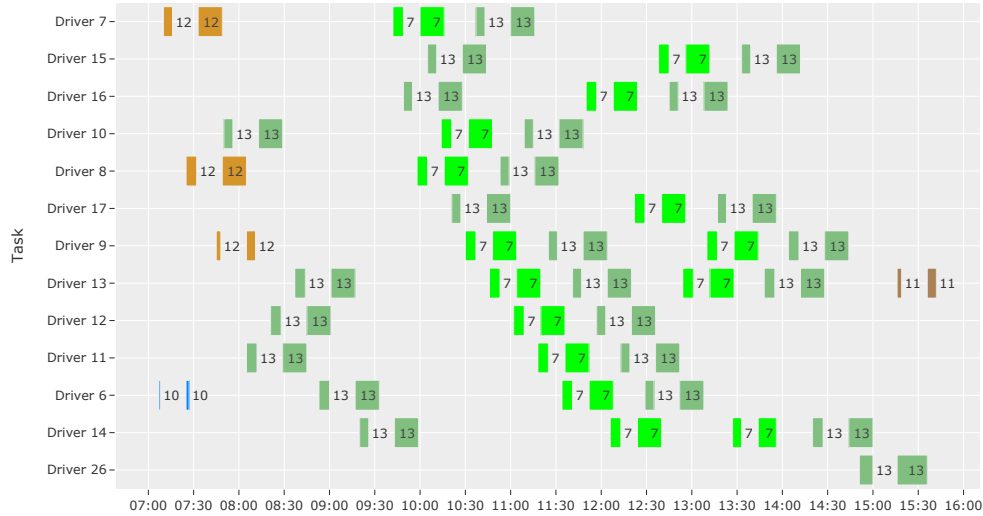
We report a *FDD* of 59.5 minutes for this solution of instance $C29_10_14_3$. The Gantt chart shows that the customers 4 and 5, who need their deliveries at 07:00, have a late first delivery. These delays are due to the work schedules of the drivers assigned to Plant 1. These drivers start their shifts at the earliest at 06:05 and 06 : 20, and it takes them 59 to 63 minutes to reach the customers. This finding suggests that the relatively high *FDD* values in our results may be related to suboptimal scheduling of drivers' hours in our instances.



(a) Scheduling of tasks at plant 0



(b) Scheduling of tasks at plant 1



(c) Scheduling of tasks at plant 2

Figure 3: Loading and unloading schedules for the plants of instance $C29_10_14_3$

The medium instance $C_104_42_47_8$ has an unserved customer with a demand of

12 m^3 and a due time of 07 : 00. Upon investigation, we find that even if we have 104 drivers in this case, the number of drivers who start their shift before t07 : 00 is not enough to serve this customer within the 60-minute window we defined. Thus, the value of UQ that we report in the table 4 appears to be optimal given the driver shift schedule given as input to our algorithm. We confirmed this observation by removing the driver start shift and overtime constraints and resolving our instances five more times. All orders are now fully serviced on each run. The table 7 compares the averages of the results from the tables 4 and 8. We found that for small instances the maximum delay dropped to zero, and for medium (large) instances it was reduced by almost 60% (40%) on average. This suggests that when we input a good work schedule, our algorithm works effectively to ensure that all orders are filled and that delays for first deliveries and travel costs are minimized. We can see that the average travel time decreases in all cases except the large one, where the difference is not significant.

Table 7: Comparison of the average results with and without shift and overtime constraints

	Default parameters				$M_T = 0, N_T, O_T = \infty, H_k = 0$			
	TC (min)	UQ (m^3)	FDD (min)	$mFDD$ (min)	TC (min)	UQ (m^3)	FDD (min)	$mFDD$ (min)
Small	1,938.13	0.00	7.44	4.47	1,842.97	0.00	0.00	0.00
Medium	15,007.28	10.26	400.45	46.31	14,879.19	0.00	74.11	17.87
Large	22,045.81	13.26	935.49	56.93	22,454.09	0.00	187.51	34.76

5.4 Sensitivity analyses

In this section, we analyze the effect on the solution when we change some parameters of our problem and how some components of the objective function influence each other.

5.4.1 Influence of the maximum time delay γ^1

We ran additional tests with different values of γ^1 , varying between 5 and 25 minutes, with no shifts or overtime constraints on the drivers. The influence of the value of the maximum time delay between two consecutive deliveries of the same order is shown in figure 4. For small instances, all customers are served on time regardless of the value of γ^1 . For medium (large) instances, all customers are served with γ^1 starting at 15 (20) minutes. The delay of initial delivery decreases as γ^1 increases. These results confirm the fact that when γ^1 is high, plants have more flexibility to delay current deliveries to make room for new ones or to make customers wait until drivers are available. Increasing the maximum delay from 10 to 20 minutes reduces the first delivery delay by over 50% for the medium and large cases. The average delivery time does not change significantly regardless of the value of γ^1 .

5.4.2 Trade-off of the objective function components

We ran five tests on our dataset and obtained two solutions per instance: one that prioritizes the shortest travel time and another that seeks the smallest first delivery delay. Figure 5 visually represents the trade-off between travel time and first delivery delay for these solutions. It is clear that as the first delivery delay decreases, the travel time increases, and conversely when the travel time is minimized, the first delivery delay tends to be longer. This result is expected because drivers assigned to a plant often need to travel to another

Table 8: Results with all instances without shift and overtime constraints

		Demand (m^3)	Avg				Best				
			TC (min)	UQ (m^3)	FDD (min)	Z	TC (min)	UQ (m^3)	FDD (min)	$mFDD$ (min)	Z
Small	C_13_11_12_1	226.5	1,243.5	0.0	0.0	1,243.5	1,243.5	0.0	0.0	0.0	1,243.5
	C_13_5_8_1	267.0	745.1	0.0	0.0	745.1	745.1	0.0	0.0	0.0	745.1
	C_18_6_11_2	333.5	753.3	0.0	0.0	753.3	753.3	0.0	0.0	0.0	753.3
	C_15_4_7_2	375.0	1,013.7	0.0	0.0	1,013.7	1,013.1	0.0	0.0	0.0	1,013.1
	C_19_7_8_2	388.0	1,661.0	0.0	0.0	1,661.0	1,658.2	0.0	0.0	0.0	1,658.2
	C_29_10_14_3	613.5	3,235.5	0.0	0.0	3,235.5	3,198.6	0.0	0.0	0.0	3,198.6
	C_31_8_11_3	776.0	2,257.6	0.0	0.0	2,257.6	2,219.9	0.0	0.0	0.0	2,219.9
	C_35_9_10_3	937.5	3,834.0	0.0	0.0	3,834.0	3,808.8	0.0	0.0	0.0	3,808.8
Medium	C_76_40_43_6	1,160.5	5,262.4	0.0	0.0	5,262.4	5,187.2	0.0	0.0	0.0	5,187.2
	C_104_42_47_8	1,565.0	8,278.0	0.0	0.0	8,278.0	8,209.6	0.0	0.0	0.0	8,209.6
	C_94_63_70_7	1,746.5	12,730.3	0.0	0.0	12,730.3	12,551.9	0.0	0.0	0.0	12,551.9
	C_116_67_78_8	1,839.5	11,884.4	0.0	0.0	11,884.4	11,641.4	0.0	0.0	0.0	11,641.4
	C_116_71_82_8	2,060.0	10,750.9	0.0	0.0	10,750.9	10,697.1	0.0	0.0	0.0	10,697.1
	C_117_57_70_6	2,327.5	14,547.0	0.0	25.8	40,380.4	14,746.8	0.0	16.1	9.1	30,816.0
	C_137_79_83_7	2,425.0	17,822.4	0.0	120.0	137,840.9	17,982.5	0.0	92.0	17.6	110,023.4
	C_127_66_80_8	2,512.5	13,622.2	0.0	0.0	13,622.2	13,565.0	0.0	0.0	0.0	13,565.0
	C_128_68_74_7	2,595.0	18,641.7	0.0	74.1	92,744.7	18,554.8	0.0	43.4	19.0	61,987.5
	C_136_85_97_8	2,673.0	17,336.3	0.0	51.8	69,145.9	17,610.5	0.0	23.1	16.3	40,731.6
	C_128_78_85_8	2,685.5	16,781.2	0.0	55.5	72,294.4	16,658.5	0.0	39.4	12.5	56,076.4
	C_131_77_85_8	2,893.5	17,789.1	0.0	22.0	39,787.5	16,923.5	0.0	0.0	0.0	16,923.5
	C_137_89_97_7	2,939.5	21,831.7	0.0	214.2	236,037.5	22,630.7	0.0	157.1	48.5	179,691.7
	C_133_84_98_7	2,971.0	21,031.1	0.0	474.0	495,073.6	21,179.3	0.0	359.8	59.8	380,980.3
Large	C_132_98_109_8	3,078.5	22,272.3	0.0	7.2	29,438.3	23,294.5	0.0	4.0	1.8	27,252.8
	C_129_101_119_8	3,229.0	18,473.8	0.0	41.6	60,111.3	18,595.2	0.0	28.0	15.7	46,551.2
	C_141_114_136_8	3,350.5	21,237.4	0.0	136.7	157,923.2	20,762.9	0.0	110.7	18.6	131,504.9
	C_140_114_132_8	3,401.5	22,518.4	0.0	174.0	196,489.2	22,537.0	0.0	64.8	10.6	87,390.4
	C_143_101_123_8	3,437.5	23,807.5	0.0	39.1	62,917.8	23,249.3	0.0	30.2	13.8	53,413.3
	C_137_112_129_8	3,471.0	22,457.5	0.0	121.0	143,439.3	21,878.2	0.0	27.9	7.5	49,772.5
	C_142_114_129_8	3,499.5	21,574.4	0.0	362.8	384,413.2	22,591.1	0.0	221.0	52.9	243,564.1
	C_149_98_122_8	3,513.0	20,918.7	0.0	150.6	171,499.5	19,503.4	0.0	94.1	28.6	113,643.5
	C_139_98_108_8	3,541.0	21,548.1	0.0	271.5	293,062.8	22,008.3	0.0	239.9	47.4	261,921.3
	C_144_108_122_8	3,670.5	23,604.0	0.0	169.2	192,821.5	23,200.9	0.0	125.9	42.5	149,122.9
	C_142_92_107_8	3,684.5	21,279.5	0.0	83.8	105,084.6	21,244.2	0.0	36.4	14.4	57,641.8
	C_138_114_136_8	3,739.5	24,385.3	0.0	109.8	134,180.9	25,218.0	0.0	71.7	15.8	96,877.5
	C_150_127_136_8	3,946.5	24,434.2	0.0	391.0	415,476.7	24,732.2	0.0	292.5	52.8	317,191.2
	C_148_112_131_8	3,953.5	25,846.2	0.0	566.8	592,677.4	26,245.8	0.0	383.8	52.7	410,087.8

plant to ensure that the first delivery remains on schedule. This trade-off highlights the challenge decision-makers face in finding the right balance between minimizing operational costs and meeting customer satisfaction.

6 Conclusion

In this paper, we investigated a variant of the concrete delivery problem, where customers can order different types of concrete from different production centers, which must be delivered at the same time. To solve this problem, we introduced a mathematical model and a heuristic solution based on Greedy Randomized Adaptive Search. Our analysis, using a dataset derived from our partner's historical data, demonstrated the effectiveness of our algorithm in making good decisions within a reasonable time. Furthermore, our model incorporates constraints related to working hours, making our heuristic a valuable tool for designing weekly schedules for company drivers. Our GRASP algorithm performed exceptionally well on Kinable et al. [2014] datasets, indicating its reliability. For future work, it would be interesting to address datasets with different unloading times at construction

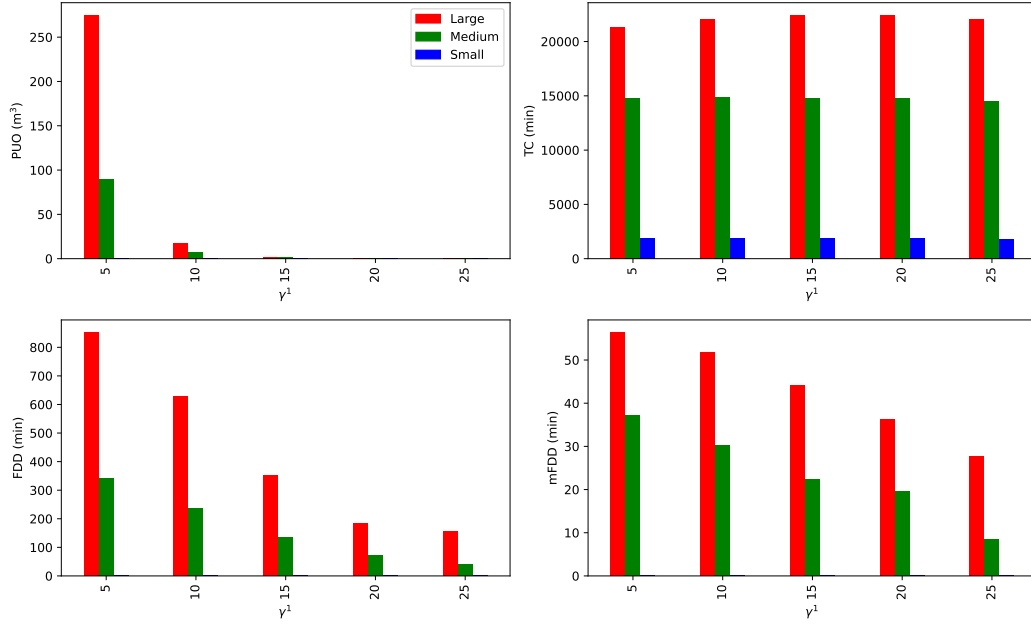


Figure 4: Influence of the maximum time delay (γ^1) between consecutive deliveries of the same order.

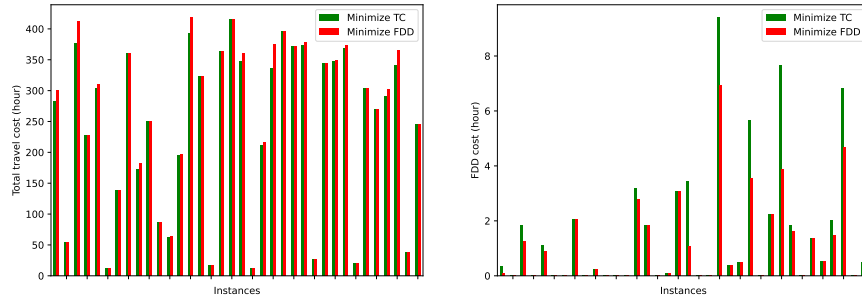


Figure 5: Trade-off between minimizing travel cost VS minimizing first delivery delay

547 sites or to explore different scenarios regarding the number of simultaneous deliveries and
548 the maximum time between two consecutive deliveries at a construction site. We can also
549 study the problem using a stochastic or robust methodology to account for the uncertainty
550 of the parameters in a real-world setting. As a contribution to the literature on CDP, we
551 provide a mathematical formulation for our variant, contribute a dataset, and demonstrate
552 the application of GRASP to solve both our problem and the one studied by Kinable et al.
553 [2014].

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References

- C. Archetti and M. G. Speranza. The split delivery vehicle routing problem: A survey. In *The vehicle routing problem: Latest advances and new challenges*, pages 103–122. Springer, 2008.
- L. Asbach, U. Dorndorf, and E. Pesch. Analysis, modeling and solution of the concrete delivery problem. *European Journal of Operational Research*, 193(3):820–835, 2009.
- J. Blazewicz, K. H. Ecker, E. Pesch, G. Schmidt, M. Sterna, and J. Weglarz. *Handbook on scheduling: From theory to practice*. Springer, 2019.
- M. Durbin and K. Hoffman. Or practice—the dance of the thirty-ton trucks: Dispatching and scheduling in a dynamic environment. *Operations Research*, 56(1):3–19, 2008.
- J. M Faria, C. A. Silva, J. MC Sousa, M. Surico, and U. Kaymak. Distributed optimization using ant colony optimization in a concrete delivery supply chain. In *2006 IEEE International Conference on Evolutionary Computation*, pages 73–80. IEEE, 2006.
- C.-W. Feng and H.-T. Wu. Integrating fmGA and CYCLONE to optimize the schedule of dispatching RMC trucks. *Automation in Construction*, 15(2):186–199, 2006.
- C.-W. Feng, T.-M. Cheng, and H.-T. Wu. Optimizing the schedule of dispatching rmc trucks through genetic algorithms. *Automation in Construction*, 13(3):327–340, 2004.
- T. A. Feo and M. GC Resende. A probabilistic heuristic for a computationally difficult set covering problem. *Operations research letters*, 8(2):67–71, 1989.
- M. Galić and I. Kraus. Simulation model for scenario optimization of the ready-mix concrete delivery problem. *Selected Scientific Papers-Journal of Civil Engineering*, 11(2):7–18, 2016.
- J. Garza Cavazos. *Dynamic planning and real-time monitoring of ready-mixed concrete delivery problem*. PhD thesis, Universidad Autónoma de Nuevo León, 2021.
- L. D. Graham, D. R. Forbes, and S. D. Smith. Modeling the ready mixed concrete delivery system with neural networks. *Automation in construction*, 15(5):656–663, 2006.
- O. A. Hernández López. *Study of mixed integer programming models for the concrete delivery problem*. PhD thesis, Universidad Autónoma de Nuevo León, 2020.
- J. Kinable and M. Trick. A logic based benders’ approach to the concrete delivery problem. In *International Conference on Integration of Constraint Programming, Artificial Intelligence, and Operations Research*, pages 176–192. Springer, 2014.
- J. Kinable, T. Wauters, and G. V. Berghé. The concrete delivery problem. *Computers & Operations Research*, 48:53–68, 2014.

- 592 M. Lu and H.-C. Lam. Optimized concrete delivery scheduling using combined simulation
593 and genetic algorithms. In *Proceedings of the Winter Simulation Conference*. IEEE, 2005.
- 594 M. Maghrebi and S. T. Waller. Exploring experts decisions in concrete delivery dispatching
595 systems using bayesian network learning techniques. In *2014 2nd International Conference*
596 *on Artificial Intelligence, Modelling and Simulation*, pages 103–108. IEEE, 2014.
- 597 M. Maghrebi, V. Periaraj, S. T. Waller, and C. Sammut. Using benders decomposition for
598 solving ready mixed concrete dispatching problems. In *The 31st International Symposium*
599 *on Automation and Robotics in Construction and Mining*, 2014a.
- 600 M. Maghrebi, V. Periaraj, S. T. Waller, and Claude Sammut. Solving ready-mixed concrete
601 delivery problems: Evolutionary comparison between column generation and robust ge-
602 netic algorithm. In *Computing in Civil and Building Engineering (2014)*, pages 1417–1424.
603 2014b.
- 604 M. Maghrebi, V. Periaraj, S. T. Waller, and C. Sammut. Column generation-based approach
605 for solving large-scale ready mixed concrete delivery dispatching problems. *Computer-*
606 *Aided Civil and Infrastructure Engineering*, 31(2):145–159, 2016a.
- 607 M. Maghrebi, S. Travis Waller, and Claude Sammut. Sequential meta-heuristic approach
608 for solving large-scale ready-mixed concrete–dispatching problems. *Journal of Computing*
609 *in Civil Engineering*, 30(1):04014117, 2016b.
- 610 M. Maghrebi, T. Waller, and C. Sammut. Matching experts’ decisions in concrete deliv-
611 ery dispatching centers by ensemble learning algorithms: Tactical level. *Automation in*
612 *Construction*, 68:146–155, 2016c.
- 613 N. F. Matsatsinis. Towards a decision support system for the ready concrete distribution
614 system: A case of a greek company. *European Journal of Operational Research*, 152(2):
615 487–499, 2004.
- 616 N. Mayteekrieangkrai and W. Wongthatsanekorn. Optimized ready mixed concrete truck
617 scheduling for uncertain factors using bee algorithm. *Songklanakarin Journal of Science*
618 *& Technology*, 37(2), 2015.
- 619 M. Misir, W. Vancroonenburg, K. Verbeeck, and G. V. Berghe. A selection hyper-heuristic
620 for scheduling deliveries of ready-mixed concrete. In *Proceedings of the metaheuristics*
621 *international conference (MIC 2011)*, pages 289–298. Udine, Italy, 2011.
- 622 F. Muresan. Comparing ready-mix concrete and site-mixed
623 concrete, 2019. URL [https://www.ny-engineers.com/blog/](https://www.ny-engineers.com/blog/ready-mix-concrete-and-site-mixed-concrete)
624 [ready-mix-concrete-and-site-mixed-concrete](https://www.ny-engineers.com/blog/ready-mix-concrete-and-site-mixed-concrete).
- 625 P. K. Narayanan, D. Rey, M. Maghrebi, and S. T. Waller. Using lagrangian relaxation to
626 solve ready mixed concrete dispatching problems. *Transportation Research Record*, 2498
627 (1):84–90, 2015.
- 628 D. Naso, M. Surico, B. Turchiano, and U. Kaymak. Genetic algorithms for supply-chain
629 scheduling: A case study in the distribution of ready-mixed concrete. *European Journal*
630 *of Operational Research*, 177(3):2069–2099, 2007.
- 631 A. Panas and J.-P. Pantouvakis. Simulation-based Concrete Truck-Mixers Fleet Size Deter-
632 mination for On-Site Batch Plant Operation. *Procedia - Social and Behavioral Sciences*,
633 74:459–467, 2013.

- 634 F. Payr and V. Schmid. Optimizing deliveries of ready-mixed concrete. In *2009 2nd Inter-*
635 *national Symposium on Logistics and Industrial Informatics*, pages 1–6, 2009.
- 636 V. Schmid, K. F. Doerner, M. W.P. Hartl, R. F. .and Savelsbergh, and W. Stoecher. A
637 hybrid solution approach for ready-mixed concrete delivery. *Transportation Science*, 43
638 (1):70–85, 2009.
- 639 V. Schmid, K F. Doerner, R. F. Hartl, and J-J. Salazar-González. Hybridization of very
640 large neighborhood search for ready-mixed concrete delivery problems. *Computers &*
641 *Operations Research*, 37(3):559–574, 2010.
- 642 A. Sinha, N. Singh, G. Kumar, and S. Pal. Quality factors prioritization of ready-mix
643 concrete and site-mix concrete: A case study in indian context. In D. Singh, A. K.
644 Awasthi, I. Zelinka, and K. Deep, editors, *Proceedings of International Conference on*
645 *Scientific and Natural Computing*, Algorithms for Intelligent Systems, pages 179–187,
646 Singapore, 2021. Springer.
- 647 M. Sulaman, X. Cai, M. Misir, and Z. Fan. Simulated annealing with a time-slot heuristic
648 for ready-mix concrete delivery. In *Asia-Pacific Conference on Simulated Evolution and*
649 *Learning*, pages 39–50. Springer, 2017.
- 650 X. Tian, Y. Mohamed, and S. AbouRizk. Simulation-based aggregate planning of batch plant
651 operations. *Canadian Journal of Civil Engineering*, 37(10):1277–1288, 2010. Publisher:
652 NRC Research Press.
- 653 I.D. Tommelein and A. Li. Just-in-time concrete delivery: mapping alternatives for vertical
654 supply chain integration. In *Proceedings of the 7th Annual Conference of the International*
655 *Group for Lean Construction*, volume 7, pages 97–108, University of California, 1999.
656 Berkeley.
- 657 A. Tzanetos and M. Blondin. Systematic search and mapping review of the concrete delivery
658 problem (cdp): Formulations, objectives, and data. *Automation in Construction*, 145:
659 104631, 2023.
- 660 S. Q. Wang, C. L. Teo, and G. Ofori. Scheduling the truckmixer arrival for a ready mixed
661 concrete pour via simulation with @risk. *Journal of Construction Research*, 2(2):169–179,
662 2001.
- 663 S. Yan and W. Lai. An optimal scheduling model for ready mixed concrete supply with
664 overtime considerations. *Automation in Construction*, 16(6):734–744, 2007.
- 665 J. Yang, B. Yue, F. Feng, J. Shi, H. Zong, J. Ma, L. Shangguan, and S. Li. Concrete vehicle
666 scheduling based on immune genetic algorithm. *Mathematical Problems in Engineering*,
667 2022.
- 668 T. M. Zayed and D. Halpin. Simulation of concrete batch plant production. *Journal of*
669 *Construction Engineering and Management*, 127(2):132–141, 2001.