

A GRASP algorithm for the concrete delivery problem.

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Abstract

The concrete delivery problem (CDP) is a combinatorial optimization problem that involves scheduling the delivery of ready-mixed concrete to construction sites while balancing the conflicting goals of minimizing transportation costs and maximizing customer satisfaction. This paper proposes an exact formulation and a heuristic approach based on the Greedy Randomized Adaptive Search Procedure (GRASP) to tackle a new variant of the CDP that incorporates realistic side constraints, such as drivers' working shifts, minimum working time for each driver, and overtime penalties. Additionally, the problem also considers the possibility of customers requiring multiple types of concrete to be delivered within the same time window. The performance of the proposed heuristic is evaluated on real-world and generated CDP instances, and it is compared to another variant to demonstrate its effectiveness.

Keywords: Vehicle scheduling; concrete delivery; GRASP; ready-mixed concrete

1 Introduction

Concrete is a widely used building material in construction projects. Its perishable nature is affected by many factors that impact its quality [Sinha et al., 2021], which is crucial for the durability and strength of the final construction. Concrete comes in two types: ready-mixed concrete (RMC) and site-mixed concrete (SMC). RMC is manufactured in a batch plant and delivered to the construction site, while SMC is produced on-site using raw materials stored on the construction site. Using SMC can avoid delays caused by road traffic, but it has a slower and more difficult production process, requires storage for mixing materials and equipment, and is suitable for low amounts of concrete. On the other hand, RMC has better quality and benefits from lower production costs [Muresan, 2019]. However, to take advantage of these benefits, the batch plant manager must ensure efficient and prompt delivery on the construction site, which may require a fleet of high-cost revolving drum trucks (concrete mixers) to dispatch the RMC.

Concrete delivery under the form of RMC is subject to many operational constraints that make the Concrete Delivery Problem (CDP) very challenging. In this paper, we study a variant of the CDP to schedule the daily production and dispatching of RMC for a company located in the province of Quebec, Canada. This company operates multiple batching plants with varying production rates, using a fleet of concrete mixers of different capacities. Each plant has its own fleet of trucks; however, under certain conditions, the trucks can move between plants if necessary. The trucks must return to their home plant at the end of the

day. The company owns two types of trucks with different capacities and can call on an external fleet when needed. They serve construction sites from any of their plants, with the first delivery starting at the time specified by the customer. The loading and unloading of a concrete mixer depend on the truck capacity, the loading rate at the plant, and the unloading rate at the construction site. Drivers are allocated based on their daily work schedules. A customer may request several types of concrete to be delivered within the same time window, with no required sequence for the orders, but an order can only start after the completion of the previous order. This constraint generalizes the linked order constraints of Durbin and Hoffman [2008] where some customers place two orders for the same day and request that they are linked (the second order begins only after the first order is completed). The setting of our study is similar to a variant of the CDP previously studied in Schmid et al. [2009, 2010]. However, we include the plant’s production rate and driver shift schedule. The company uses a centralized dispatcher system to schedule all daily orders, but this system has issues satisfying all daily demands without using an external fleet.

According to Blazewicz et al. [2019], the CDP combines vehicle routing with scheduling issues to plan routes to deliver concrete from batch plants (depots) to customers’ construction sites. RMC is an on-demand product with a short life cycle from production through end use. It cannot be stored and cannot stay too long on a truck, or it will harden. Hence, concrete mixers must deliver RMC at the planned construction site shortly after its production. Tommelein and Li [1999] describes RMC production and delivery as an example of a just-in-time (JIT) production system in construction. A customer quantity requirement is often greater than the truck size and must be fulfilled by multiple deliveries. In that sense, CDP is similar to the vehicle routing problem with split delivery [Archetti and Speranza, 2008], except that the same truck may visit a customer more than once. Concrete hardens quickly, so multiple deliveries must be done back-to-back or at least close in time to avoid the problem of cold joint, which can reduce the strength and durability of the concrete. Customers request to be served within a specific time window, which can complicate truck-loading schedules when a plant can only load one truck at a time. Similarly, only one truck can unload at a time at a customer location, sometimes leading to concrete mixers queuing and waiting their turn to deliver. Furthermore, with trucks of varied sizes, loading, travel, and unloading times that may be uncertain, the CDP is a complex and challenging problem.

In this paper, we propose a mathematical model and a Greedy Randomized Search Procedure (GRASP) heuristic solution to solve a new variant of the CDP. Our model takes into consideration the working shifts of the drivers and the scheduling of multiple orders within the same time window at a construction site. To the best of our knowledge, this paper is the first that deals with these specific constraints in the context of the CDP.

The rest of the paper is structured as follows: Section 2 provides a literature review of previous work related to the CDP. Section 3 provides a formal description and mathematical model of the problem. In Section 4, we describe the GRASP algorithm and the constructive heuristics developed to solve this variant of the CDP. Section 5 presents computational experiments to evaluate the proposed approach, and finally, the conclusions are presented in Section 6.

2 Literature review

Academic Research on concrete batching and delivery began in the late 1990s. Tommelein and Li [1999] described RMC as a prototypical example of a JIT production system in construction and identified two practices for delivering it. One approach is for the customer to haul the product from the batch plant with their concrete mixer, while the other is for the

84 batch plant to deliver the concrete directly to the customer’s location. This latter approach
 85 is the one that has been studied in all related papers found in the literature. Several
 86 works to schedule and dispatch concrete production and delivery have mainly focused on
 87 simulation-related methods. These methods can be standalone, such as those used by Zayed
 88 and Halpin [2001], Wang et al. [2001], Tian et al. [2010], Panas and Pantouvakis [2013] and
 89 Galić and Kraus [2016], among others. Alternatively, these methods can be hybridized with
 90 optimization techniques, such as those used by Feng et al. [2004], Lu and Lam [2005], and
 91 Feng and Wu [2006]. Wang et al. [2001] developed a simulation model to reveal the effect
 92 and value of the concrete mixers’ inter-arrival time on the productivity of hired unloading
 93 equipment on site. Feng et al. [2004] used a combination of genetic algorithm (GA) and
 94 simulation process to minimize the total waiting time for trucks at a customer site. The
 95 study focused on loading trucks with identical capacities at the same batch plant, with fixed
 96 loading and unloading durations. The GA was used to find the best loading sequence of RMC
 97 trucks to be assigned to different construction sites. The simulation process determined
 98 the loading, arrival, departure, and waiting time of trucks and thus evaluated the cost of
 99 each dispatching sequence. They evaluated their method using data from a batch plant in
 100 Taiwan with up to nine customers served. Mayteekrieangkrai and Wongthatsanekorn [2015]
 101 addressed the same problem with the same data using a bee algorithm (BA) and found better
 102 solutions than the GA. Lu and Lam [2005] used the same combination of GA and simulation
 103 to determine the optimal number of concrete mixers to be deployed and an optimal schedule
 104 for batching and delivering concrete. Their objective was to minimize the idle time of the
 105 site crew due to late concrete deliveries and truck queuing time. In this setting, it was also
 106 necessary to deliver a batch of mortar on-site to lubricate the unloading pump before the
 107 concrete delivery. As such, the simulation model also included the batching and delivery
 108 of mortar. Finding the best RMC fleet size was also the purpose of the discrete-event
 109 simulation model proposed by Panas and Pantouvakis [2013].

110 In addition to simulation-based methods, several other approaches have been used in the
 111 literature to solve the CDP. These include metaheuristics [Faria et al., 2006, Misir et al.,
 112 2011, Maghrebi et al., 2016b, Yang et al., 2022], exact methods [Yan and Lai, 2007, Asbach
 113 et al., 2009, Kinable et al., 2014], matheuristics [Schmid et al., 2009, 2010], Benders Decom-
 114 position [Maghrebi et al., 2014a], column generation (CG) [Maghrebi et al., 2014b, 2016a],
 115 Lagrangian relaxation [Narayanan et al., 2015], and machine learning approaches such as
 116 those used by Graham et al. [2006], Maghrebi and Waller [2014], Maghrebi et al. [2016c].
 117 Matsatsinis [2004] designed a decision support system (DSS) for the dynamic routing of
 118 both concrete and pumps that may be necessary for some construction sites to aid in the
 119 unloading of concrete. The DSS considered the availability of three plants but stipulated
 120 that vehicles fulfilling the same order must all load at the same plant. Orders that could not
 121 be executed immediately could be postponed for the next day. The routing of the pumps
 122 was modeled as a multi-depot vehicle routing problem with time windows. Naso et al. [2007]
 123 proposed a sequential GA method combined with constructive heuristics to solve another
 124 variant of the CDP. In this problem, the plant’s production schedule must account for or-
 125 ders for concrete to be delivered to a customer site and orders that customers must pick
 126 up themselves. The algorithm first schedules the plant loading operations before scheduling
 127 truck deliveries. The authors also developed a non-linear model that minimizes transporta-
 128 tion costs, waiting times, outsourced costs, and overtime work. They ran experiments using
 129 real-world instances of a concrete supply chain in the Netherlands and found a reduction
 130 in the number of outsourced requests. Yan and Lai [2007] also considered overtime con-
 131 siderations in their paper, which focused on scheduling RMC for one batching plant with
 132 two loading docks. The study took into account that overtime wages are paid for factory

133 and construction site operations after 4 PM. They developed a mixed-integer programming
 134 (MIP) model on a time-space network to minimize travel times and operating costs at both
 135 normal and overtime working hours at the plant and the construction sites. They tested
 136 the model using real data consisting of three days of operation using a two-stage algorithm.
 137 First, they solved the MIP relaxation with CPLEX. Then, they simplified the original model
 138 by fixing some decision variables before solving it. The algorithm was found to improve the
 139 actual plant operation by 10%. A time-space network is the key component of the real-time
 140 DSS developed by Durbin and Hoffman [2008] to solve a dynamic CDP every five minutes.
 141 The DSS is able to receive new orders, schedule them on the fly, and handle unexpected
 142 events such as plant closures, truck breakdowns, and delays in transportation times. The
 143 authors combined the DSS with a tabu search (TS) heuristic to warm start CPLEX, which
 144 made the model performant enough to solve instances with up to 1,500 loads per day with
 145 up to 250 trucks. The DSS also considers the case of a customer who places two orders,
 146 with the first being completed before the second starts. Further insights on the real-time
 147 planning and monitoring of CDP are available in Garza Cavazos [2021]. Another variant
 148 of the CDP is modeled by Schmid et al. [2009] as an integer multicommodity network flow
 149 (MCNF) problem on a time-space network. In this paper, concrete is delivered using a
 150 heterogeneous fleet of vehicles, and each plant can load an unlimited number of trucks si-
 151 multaneously. Some of the trucks have specialized equipment and must arrive first at certain
 152 construction sites to assist in unloading the concrete. The objective is to fulfill all orders,
 153 minimize the travel cost, and avoid delays between two consecutive unloading operations
 154 for an order. The model is typically solved using a matheuristic algorithm that combines
 155 the MCNF with a variable neighborhood search (VNS) heuristic. The method can quickly
 156 solve large problem instances with more than 60 orders per day without encountering any
 157 memory issues. The same problem is addressed by Schmid et al. [2010], who proposed a
 158 MIP model combined with a VNS and a very large neighborhood search (VLNS) to develop
 159 two matheuristics approaches. Comparisons between both matheuristics and a standalone
 160 VNS show that the former methods are much better and suitable for solving larger problem
 161 instances. These methods also provide better solutions for small to medium instances than
 162 the matheuristic used in Schmid et al. [2009]. A pure VNS approach with the same problem
 163 but without the use of instrumentation has been applied by Payr and Schmid [2009].

164 Regarding objectives, most authors have focused on minimizing travel time and delays
 165 between consecutive deliveries. However, some authors have been more interested in max-
 166 imizing customer satisfaction alone. We find these situations in the works of Durbin and
 167 Hoffman [2008], Kinable et al. [2014], Kinable and Trick [2014], Sulaman et al. [2017]. Kin-
 168 able et al. [2014] introduce a general MIP and constraint programming (CP) models of
 169 the CDP reflecting the main constraints commonly found in all CDP works: time lag and
 170 no overlapping between consecutive deliveries, covering of all customers' demands, deliv-
 171 ery time window, and heterogeneous fleet. However, the model did not include constraints
 172 limiting the time that concrete may reside in a truck. The authors propose a constructive
 173 heuristic that schedules the visits to the customers one by one according to the start time
 174 of the visit and the truck capacity. The procedure is invoked multiple times for different
 175 permutations of the customer's order which is determined using the steepest descent (SD)
 176 local search procedure. One of the paper's main contributions is the creation of the first
 177 public test instances for the CDP with up to 50 customers, four batching plants, and 20
 178 concrete mixers. They found the CP model to be highly effective in finding high-quality
 179 solutions in a relatively short time or improving existing schedules, while the MIP model
 180 can be used to compute bounds, as it seems ineffective in solving large problem instances.
 181 Finally, the heuristic often yields good solutions in less than a second. A detailed analysis

of the MIP model presented in Kinable et al. [2014] and of two more compact models can be found in the thesis of Hernández López [2020]. In Kinable and Trick [2014], we found an attempt to solve the previous problem with a logic-based Benders’ approach. Sulaman et al. [2017] expand upon the SD heuristic proposed in Kinable et al. [2014], proposing a simulated annealing (SA) combined with a time-slot Heuristic (SATH). This method looks for a slot between existing visits of a truck to schedule a new delivery instead of assigning it to the time slot strictly after the truck’s latest assigned delivery. The goal is to reduce the large time gaps that can be present in a schedule created with SD due to ignoring the intermediate available time slots. Experimental results indicated that SATH outperforms SD in speed and solution quality. A generalization of the MIP model of Kinable et al. [2014] is addressed in Asbach et al. [2009]. This model simultaneously minimizes the total sum of travel costs and the penalty costs for customers with unfulfilled demand. A customer can request that all concrete deliveries come from the same plant or a subset of plants and that a delivery truck belongs to a subset of the vehicle fleet. The MIP model is used in a local search scheme as a black-box solver to reoptimize an incumbent solution in which a neighborhood operator has unfixed some variables. Tzanetos and Blondin [2023] provide an overview of the various methods used in the literature to address the CDP and categorizes the problem formulations based on the different concepts used in the literature. They also discussed the consistency between industry needs and existing constraints and provided insights into the datasets corresponding to real-world cases, identifying the necessary data for practitioners.

3 Problem description

The focus of this paper is the distribution of RMC from a Canadian company that operates in the greater Montreal area. When a customer places an order, it is received at a central center and assigned to one of the company’s batching plants. These plants produce the concrete and then deliver it to the customer. The problem we are examining involves a set of customer orders, a set of concrete-mixer drivers, and a set of batching plants.

A customer i requests one or more types of concrete to be delivered to his construction site on a particular day, starting at time a_i . We call an order o a request for a specific type of concrete. q_i is the sum of the demand q_o of each order o placed, a_i is the desired arrival time of the first concrete mixer, and τ_i^u is the unloading rate for customer i . If the order requires more concrete than a single truck can carry, multiple deliveries are scheduled.

Let O_i be the set of all orders requested by customer i . Each element of O_i must be fully delivered before moving on to another order. Exactly one order o of O_i must have its first delivery start at a_i , while the others can start at any time after o is completed. Once a plant is selected to produce a customer’s first delivery, it must be the supplier of all subsequent deliveries from that customer. To avoid cold joint problems with the concrete, the subsequent deliveries must be made in close succession. We define a maximum time delay γ_i after which no more deliveries will be allowed. The customer unloading rate and the quantity to be unloaded give the time required to unload a truckload. Let \mathcal{C} be the set of construction sites (customers) with a planned delivery for the day, and $\mathcal{O} = \{O_i, i \in \mathcal{C}\}$ be the set of all requested orders for all customers.

The company has two types of concrete mixer trucks with capacities of 8 and 12 cubic meters. Each driver k is assigned to a particular batch plant and is responsible for driving a truck with capacity Q_k . The set of drivers is represented by $K = \cup_{b \in \mathcal{B}} K_b$, where K_b is the set of drivers scheduled to start their shift at batch plant b . t_{ij} is the known time to travel between any two locations i and j . A scheduled driver k is required to start his shift at H_k ,

work a minimum of M_T hours and a maximum of N_T hours during regular working hours, with the possibility of overtime of up to O_T hours. β_3 and β_4 are the penalties incurred if a driver works less than M_t and more than N_t .

A driver typically loads RMC at his assigned batch plant but may be required to drive to and load at other plants if needed. The batch plant produces concrete on demand using recipes specific to each order. This means that a truck can only haul RMC for one order, even if there is spare capacity. To fill multiple orders, a driver must restock at a plant between deliveries. After unloading the RMC, a driver takes β_k minutes to clean the concrete mixer before proceeding.

Let n_o be the number of deliveries needed to fulfill the order o . n_o is not known in advance because we use a fleet of trucks with different capacities. However, we can compute its lower (n_o^{min}) and upper (n_o^{max}) bounds using the capacities of the largest (Q_{max}) and smallest (Q_{min}) available trucks. The lower bound is the number of deliveries required if we only use trucks with capacity Q_{max} , while the upper bound is the number of deliveries required if we only use trucks with capacity Q_{min} .

$$n_o^{min} = \left\lceil \frac{q_o}{Q_{max}} \right\rceil \leq n_o \leq n_o^{max} = \left\lceil \frac{q_o}{Q_{min}} \right\rceil \quad \forall o \in \mathcal{O}. \quad (1)$$

Let d_o^j be the j_{th} visit with load q_o^j for order o . We represent the fulfillment of order o by the visits to the ordered set of delivery nodes $\mathcal{D}_o = (d_o^0, d_o^1, \dots, d_o^{n_o})$. The deliveries of customer i are the ordered set $\mathcal{D}_i = (\mathcal{D}_{o_1}, \mathcal{D}_{o_2}, \dots, \mathcal{D}_{o_{|O_i|}})$, where o_r is the r_{th} delivered order. We will refer to $d \in \mathcal{D}_i$ ($d \in \mathcal{D}_o$) as the d_{th} potential delivery of customer i (order o). $\mathcal{D} = \bigcup_{i \in \mathcal{C}} \mathcal{D}_i$ is the union of all delivery nodes.

The company owns a total of eight batching plants located in various geographical regions. Each plant has a loading dock that can only accommodate only one truck at a time, which leads to trucks lining up. Let \mathcal{B} be the set of batching plants. The plants are heterogeneous, as each plant b has its own hourly loading rate, represented by τ_b^l , which affects the duration of the loading process. After loading the concrete, the driver spends α_b minutes adjusting the concrete in the truck before heading to the customer site. Each plant has its own assigned fleet of trucks, but it can borrow trucks from other plants or hire external vehicles if necessary. A batching plant can serve a construction site as long as the travel time between the two is less than the concrete's lifespan, which is represented by Δ . Let $l_{b,j}$ be the loading dock node associated with delivery node j at plant b . We represent each plant b by the set $\mathcal{L}_b = \{l_{b,j}, t_{bj} \leq \Delta, j \in \mathcal{D}\}$ of loading docks nodes. $\mathcal{L} = \bigcup_{b \in \mathcal{B}} \mathcal{L}_b$ is the union of all loading docks.

A solution to the problem involves making decisions about truck loading schedules, driver assignments to different deliveries, and truck arrival times at construction sites for unloading. For a batching plant, the decision involves choosing which driver to load, when to load them, and which construction site they should deliver to. For a driver, the decision involves determining the sequence of loading depots and delivery sites. And for a construction site, the decision involves determining the arrival times of all scheduled deliveries for the day.

Each driver leaves and returns to his home plant every day. We represent the home plant of a driver k with a starting depot s_k and an ending depot e_k . S and E are the sets of starting and ending depots, respectively.

We define our problem on a complete directed graph where $V = \{S \cup \mathcal{L} \cup \mathcal{D} \cup E\}$ is the set of nodes. The arc sets are $A = \{(i, j, k) \mid i, j \in V, k \in K\}$, $A^D = \{(i, j) \mid i, j \in \mathcal{D}\}$, and $A^L = \{(i, j) \mid i, j \in \mathcal{L}\}$. A corresponds to allowed movements of drivers from node i to node j . For each driver k , the allowed movements are the following:

- From the starting depot s_k to a loading dock $l \in \mathcal{L}$ or to the ending depot e_k .

275 • From a loading dock $l \in \mathcal{L}$ to a delivery node $d \in \mathcal{D}$.

276 • From a delivery node $d \in \mathcal{D}$ to a loading dock $l \in \mathcal{L}$ or to the ending depot e_k .

277 For a customer c , arcs in A^D link consecutive delivery nodes of the same order $\{(i, j) \in$
 278 $\mathcal{D}_o, o \in \mathcal{O}_c, i < j\}$, and pair of delivery nodes of two different orders $\{(i, d_{o_2}^0), i \in \mathcal{D}_{o_1}, i \geq$
 279 $n_{o_1}^{min}, o_1, o_2 \in \mathcal{O}_c, o_1 \neq o_2\}$. Arcs in A^L link all pairs of loading docks of the same batching
 280 plant.

281 $\delta^+(i) = \{(i, j, k) \in A\}$, and $\delta^-(i) = \{(j, i, k) \in A\}$ are the outcoming and incoming
 282 arc sets of any node $i \in V$. $\delta_D^+(i) = \{(i, j) \in A^D\}$, and $\delta_D^-(i) = \{(j, i) \in A^D\}$ are the
 283 outcoming and incoming arc sets of delivery node $i \in \mathcal{D}$. Similarly, $\delta_L^+(i) = \{(i, j) \in A^L\}$,
 284 and $\delta_L^-(i) = \{(j, i) \in A^L\}$ are the outcoming and incoming arc sets of loading node $i \in \mathcal{D}$.

285 Let the binary variable x_{ij}^k be 1 if the driver k travels from node i to j . The binary
 286 variable y_o is 1 when the order o is completely served. v_i and w_i are the start and end of
 287 the loading (unloading) operation at node $i \in \mathcal{L} \cup \mathcal{D}$. The binary variable $u_{i,j}$ is 1 if node
 288 j is served just after i , the service being either an unloading or a loading operation. The
 289 binary variable σ_{ib} is equal to 1 if the orders of customer i are loaded by plant b . Variable
 290 q_j^k is the quantity to be loaded towards j with vehicle k . Let w_k^1 be a continuous variable
 291 indicating the difference between the driver's work time and the minimum number of hours
 292 to be worked in a day. w_k^2 is a continuous variable indicating the difference between the
 293 driver's work time and the normal work time. Let g_i be the time between due date and first
 294 service start for customer i .

295 The objective function minimizes the travel cost, the penalty costs incurred when cus-
 296 tomer demands are not fully met, the lateness of each customer's first delivery, the cost of
 297 drivers working less than the minimum hours, and the total overtime cost of drivers working
 298 beyond their scheduled hours. The mathematical model of this variant of the CDP is as
 299 follows:

$$\min \sum_{(i,j,k) \in A} t_{ij} x_{ij}^k + \beta_1 \sum_{o \in \mathcal{O}} (1 - y_o) + \beta_2 \sum_{i \in \mathcal{C}} g_i + \sum_{k \in K} \beta_3 * w_k^1 + \beta_4 * w_k^2 \quad (2)$$

$$\sum_{j \in \delta^+(s_k)} x_{s_k j}^k = 1 \quad \forall k \in K \quad (3)$$

$$\sum_{j \in \delta^-(e_k)} x_{j e_k}^k = 1 \quad \forall k \in K \quad (4)$$

$$v_j \geq w_i + \alpha_i + t_{ij} - M(1 - x_{ij}^k) \quad \forall i \in \mathcal{L}, j \in \delta^+(i), k \in K \quad (5)$$

$$v_j \geq w_i + \beta_k + t_{ij} - M(1 - x_{ij}^k) \quad \forall i \in \mathcal{D}, j \in \delta^+(i), k \in K \quad (6)$$

$$w_i \geq v_i + \frac{q_j^k}{\tau_b^l} - M(1 - x_{ij}^k) \quad \forall b \in \mathcal{B}, i \in \mathcal{L}_b, j \in \delta^+(i), k \in K \quad (7)$$

$$w_j \geq v_j + \frac{q_j^k}{\tau_c^u} - M(1 - x_{ij}^k) \quad \forall c \in \mathcal{C}, j \in \mathcal{D}_c, i \in \delta^-(j), k \in K \quad (8)$$

$$w_j \leq v_i + \Delta + M(1 - x_{ij}^k) \quad j \in \mathcal{D}, i \in \delta^-(j), k \in K \quad (9)$$

$$v_{d_o^0} \geq a_i \quad \forall i \in \mathcal{C}, \forall o \in \mathcal{O}_i \quad (10)$$

$$g_i \geq v_{d_{o_1}^0} - a_i - M \left(\sum_{j \in \delta_D^-(d_{o_1}^0)} u_{j, d_{o_1}^0} \right) \quad \forall i \in \mathcal{C}, \forall o_1 \in \mathcal{O}_i, d = d_{o_1}^0 \quad (11)$$

$$v_{d_{o_1}^0} \geq w_j - M \left(1 - u_{j,d_{o_1}^0} \right) \quad \forall o_1 \in \mathcal{O}_i, j \in \delta_D^-(d_{o_1}^0) \quad (12)$$

$$v_{d_{o_1}^0} \leq w_j + \gamma_i + M \left(1 - u_{j,d_{o_1}^0} \right) \quad \forall o_1 \in \mathcal{O}, j \in \delta_D^-(d_{o_1}^0) \quad (13)$$

$$\sum_{o_1 \in \mathcal{O}_i} \sum_{j \in \delta_D^-(d_{o_1}^0)} u_{j,d_{o_1}^0} = |\mathcal{O}_i| - 1 \quad \forall i \in \mathcal{C}, |\mathcal{O}_i| > 1 \quad (14)$$

$$\sum_{o_1 \in \mathcal{O}_i} \sum_{j \in \delta_D^+(d_{o_1}^0)} u_{d_{o_1}^0,j} = |\mathcal{O}_i| - 1 \quad \forall i \in \mathcal{C}, |\mathcal{O}_i| > 1 \quad (15)$$

$$\sum_{j \in \delta_D^+(d_{o_1}^0)} u_{d_{o_1}^0,j} \leq 1 \quad \forall o_1 \in \mathcal{O} \quad (16)$$

$$\sum_{j \in \delta_D^-(d_{o_1}^0)} u_{j,d_{o_1}^0} \leq 1 \quad \forall o_1 \in \mathcal{O} \quad (17)$$

$$\sum_{j \in \delta_D^+(d_{o_1}^0)} u_{d_{o_1}^0,j} + \sum_{j \in \delta_D^-(d_{o_1}^0)} u_{j,d_{o_1}^0} \geq 1 \quad \forall o_1 \in \mathcal{O} \quad (18)$$

$$v_j \geq w_{j-1} - M \left(1 - u_{j-1,j} \right) \quad \forall o \in \mathcal{O}, j \in \mathcal{D}_o, j \geq 1 \quad (19)$$

$$v_j \leq w_{j-1} + \gamma_i + M \left(1 - u_{j-1,j} \right) \quad \forall i \in \mathcal{C}, \forall o \in \mathcal{O}_i, j \in \mathcal{D}_o, j \geq 1 \quad (20)$$

$$u_{j-1,j} \geq u_{j,j+1} \quad \forall o_1 \in \mathcal{O}, j \in \mathcal{D}_{o_1}, 1 \leq j \leq n_{o_1} - 1 \quad (21)$$

$$u_{j-1,j} \geq \sum_{l \in \mathcal{L}} x_{lj} \quad \forall o_1 \in \mathcal{O}, j \in \mathcal{D}_{o_1}, j \geq 1 \quad (22)$$

$$v_j \geq w_i - M \left(1 - u_{i,j} \right) \quad \forall i \in \mathcal{L}, j \in \delta_L^+(i) \quad (23)$$

$$\sum_{j \in \delta_L^+(i)} u_{i,j} \leq 1 \quad \forall i \in \mathcal{L} \quad (24)$$

$$\sum_{j \in \delta_L^-(i)} u_{j,i} \leq 1 \quad \forall i \in \mathcal{L} \quad (25)$$

$$\sum_{j \in \delta_L^-(i)} u_{j,i} + \sum_{j \in \delta_L^+(i)} u_{i,j} \geq \sum_{k \in K} \sum_{j \in \delta^-(i)} x_{ji}^k \quad \forall i \in \mathcal{L} \quad (26)$$

$$\sum_{k \in K} \sum_{j \in \mathcal{D}_o} q_j^k = q_o \quad \forall o \in \mathcal{O} \quad (27)$$

$$\sum_{k \in K} \sum_{j \in \delta^+(i)} x_{ij}^k \leq 1 \quad i \in \mathcal{L} \cup \mathcal{D} \quad (28)$$

$$\sum_{k \in K} \sum_{j \in \delta^+(i)} x_{ij}^k = \sum_{k \in K} \sum_{j \in \delta^-(i)} x_{ji}^k \quad i \in \mathcal{L} \cup \mathcal{D} \quad (29)$$

$$\sum_{k \in K} \sum_{i \in \mathcal{D}_c} \sum_{j \in \delta^-(i)} x_{ji}^k \leq M * \sigma_{c,b} \quad \forall c \in \mathcal{C}, b \in \mathcal{B} \quad (30)$$

$$\sum_{b \in \mathcal{B}} \sigma_{c,b} \leq 1 \quad \forall c \in \mathcal{C}, b \in \mathcal{B} \quad (31)$$

$$w_k^1 \geq M_T + H_k - v_{e_k} \quad \forall k \in K \quad (32)$$

$$w_k^2 \geq (v_{e_k} - H_k) - N_T \quad \forall k \in K \quad (33)$$

$$w_{e_k} \leq H_k + O_T \quad k \in K \quad (34)$$

$$0 \leq q_j^k \leq Q^k \quad j \in \mathcal{D}, k \in K \quad (35)$$

$$x_{ij}^k \in \{0, 1\} \quad (i, j) \in A, k \in K \quad (36)$$

$$u_{ij} \in \{0, 1\} \quad (i, j) \in A^D, k \in K \quad (37)$$

$$\sigma_{ib} \in \{0, 1\} \quad i \in \mathcal{C}, b \in \mathcal{B} \quad (38)$$

$$y_o \in \{0, 1\} \quad o \in \mathcal{O} \quad (39)$$

$$v_i \geq 0, w_i \geq 0 \quad i \in V \quad (40)$$

$$w_k^1 \geq 0, w_k^2 \geq 0 \quad i \in V \quad (41)$$

$$g_i \geq 0 \quad i \in \mathcal{C}. \quad (42)$$

β_1 to β_4 are the penalty coefficients of each component of the objective function (2). Constraints (3–4) state that a driver k leaves his start node exactly once a day and returns to his end node after completing his last unloading operation of the day. Constraints (5–6) set a driver to take some time after loading or unloading to adjust the concrete or clean the truck before moving on to the next node. The duration of the loading operation depends on the plant’s loading rate and the amount q_j^k of RMC loaded (Eq. 7). Similarly, the unloading service depends on the site’s rate and q_j^k (Eq. 8). Unloading operations must end Δ minutes after loading begins (Eq. 9).

Constraints (10–13) ensure that the first service of any customer i must start at the due time a_i . This first service may be performed at the first delivery node of any order $\in \mathcal{O}_i$, and one order must be completed before another is started. It also enforces the precedence constraints between the last delivery of an order and the first delivery of the following order. Constraints (14–18) find the delivery sequence of all orders $\in \mathcal{O}_i$. Constraints (19–22) prohibit two trucks serving consecutive deliveries of the same order from unloading at the same time and enforce a maximum time delay between them. Similarly, constraints (23–26) ensure that two trucks cannot be loaded at the same time at a plant. Constraints (27) require that the cumulative load of all concrete mixers serving an order must equal the required quantities. Constraints (28) require that a driver can only visit a loading/delivery node once. Constraints (29) are degree constraints. Constraints (30) and (31) require that all orders from customer i must be loaded from the same plant. Constraints (32–33) calculate the difference between a driver’s hours of service and the minimum and normal hours of service. Finally, constraints (34)–(42) define the nature and bounds of the variables.

Let us consider the solution of a small instance of our problem shown in Figures 1 and 2. Two batching plants B_1 and B_2 with three drivers serve two construction sites. Customer C_1 requests one order of $q_1^1 = 12 \text{ m}^3$. Customer C_2 requests three orders of $q_2^1 = 3$, $q_2^2 = 11$, and $q_2^3 = 1 \text{ m}^3$ of three different types of concrete. B_1 has two drivers (D_1, D_2) using concrete mixers of capacity 8 m^3 , and B_2 has D_3 with a capacity 12 m^3 . Figure 1 shows the flow of concrete mixers flow in the network. We schedule D_1 and D_2 to deliver 8 and 4 m^3 to C_1 , respectively. We select o_2^2 as the first order of C_2 to deliver. D_3 travels to B_1 to load q_2^2 , then visits C_2 before returning to his home plant. Meanwhile, after their first trip, D_1 and D_2 deliver the remaining orders of C_2 .

Figure 2 shows the sequence of loading and unloading operations. The first deliveries of C_1 and C_2 are timely and there is no gap between the two deliveries received by C_1 . There is a delay between the end of the first delivery and the start of the second delivery of C_2 , however, it is less than the maximal time delay of 20 minutes defined for this example.

4 Constructive heuristics and GRASP

We now present the heuristic approach we implement to solve this variant of the Concrete Delivery Problem. Our method consists of constructing feasible solutions to the CDP with

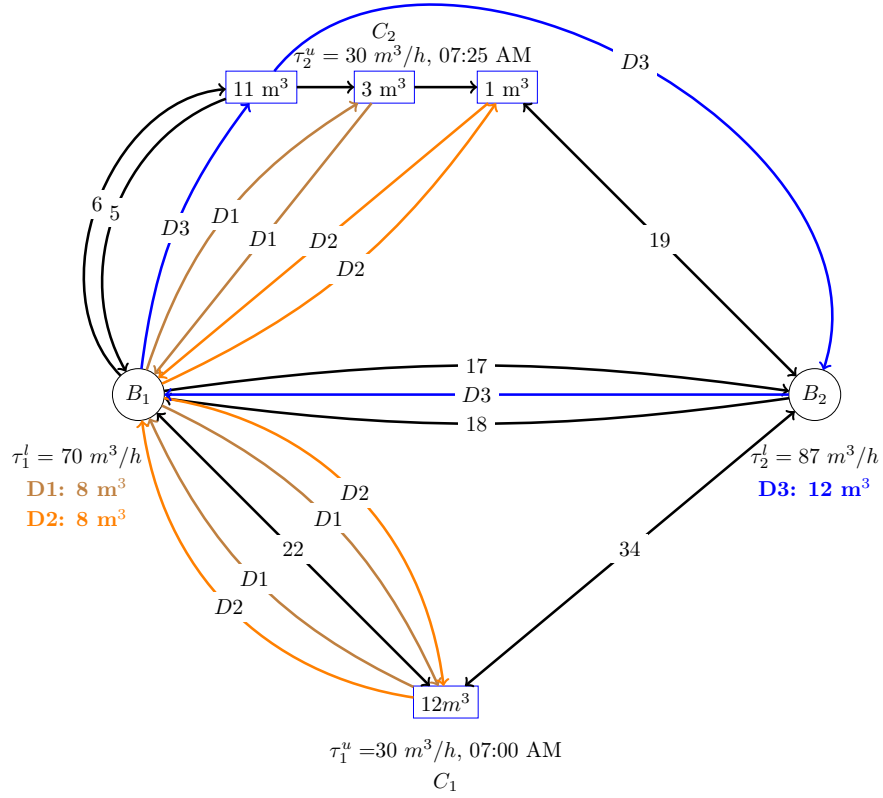


Figure 1: Solution of an instance with two plants, two construction sites, four orders, and three drivers.

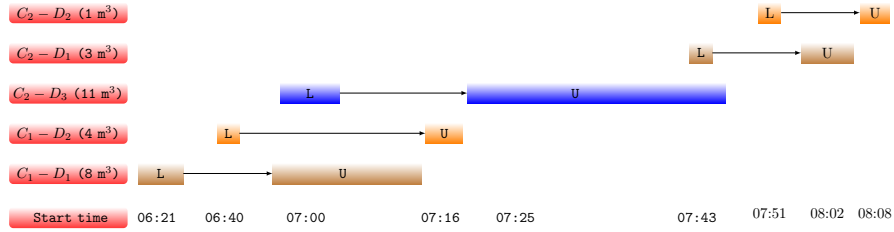


Figure 2: Schedule of the instance of Figure 1.

338 randomized heuristics and iteratively invoking these heuristics in the GRASP metaheuristic.
 339 In this section, we represent the scheduling of a delivery node d as a pair of loading (L_d)
 340 and unloading (U_d) tasks. $L_d = (b, k, q_d, v_b)$ indicates that driver k starts loading $q_d \text{ m}^3$ of
 341 RMC at plant b at time v_b . $U_d = (k, v_d, w_d)$ indicates that driver k is serving d between
 342 v_d and w_d . We then call a solution $S = \left\{ \cup_{1 \leq j \leq n_o} (L_{d_o^j}, U_{d_o^j}), \forall o \in \mathcal{O} \right\}$ the set of all loading
 343 and unloading tasks performed on a given day.

344 4.1 GRASP algorithm

345 The GRASP algorithm is an iterative suite of constructive and local search algorithms in-
 346 troduced by Feo and Resende [1995]. A feasible solution S is constructed using a greedy
 347 randomized algorithm at each iteration. Then a local search algorithm explores the neigh-
 348 borhood of S to find a local optimum. The pseudocode of the algorithm 1 shows that the
 349 procedure returns the best overall solution (for a minimization problem) after some stopping
 350 conditions (time limit or a maximum number of iterations) are met. In our implementa-
 351 tion, we introduce at line 13 an additional local search step using the solutions found by all
 352 heuristics in the current iteration.

Algorithm 1 Pseudo-code of the GRASP algorithm

Input: H : List of constructive randomized heuristics

```

1  $S^* \leftarrow \emptyset$   $T \leftarrow \emptyset$   $Cost(S^*) \leftarrow \infty$ 
2 while Conditions not met do
3    $Cost(S') \leftarrow \infty$ 
4    $T \leftarrow \emptyset$ 
5   for each  $h \in H$ 
6      $S \leftarrow h(S)$ 
7      $S \leftarrow LocalSearch(S)$ 
8      $T \leftarrow T \cup \{S\}$ 
9     if  $Cost(S) < Cost(S')$  then
10        $S' \leftarrow S$ 
11       if  $Cost(S') < Cost(S^*)$  then
12          $S^* \leftarrow S'$ 
13    $S^* \leftarrow LocalSearch(T)$ 
14 return  $S^*$ 

```

353 4.2 Greedy randomized insertion algorithm

354 As mentioned in Resende and Ribeiro [2019], the general outline of a greedy randomized
 355 algorithm used in the GRASP framework works as described in Algorithm 2. Let's consider
 356 the set CL of candidate delivery nodes that have not yet been scheduled. We first initialize
 357 CL with the first delivery node of a randomly selected order, for each customer.

358 At each iteration, we create the set CL' with elements of CL from a given neighborhood.
 359 We then evaluate the increase in the cost function of incorporating each $d \in CL'$ into the
 360 incumbent solution S and construct a restricted candidate list RCL consisting of nodes
 361 whose incremental cost is less than a given threshold. From RCL , we randomly select the
 362 next delivery node to be incorporated into the incumbent solution and determine its loading
 363 and unloading schedule using the procedure described in Algorithm 3. Next, we update S
 364 and the remaining order and customer quantities. Then we add the next candidate delivery
 365 node to CL . If an order o is not yet fulfilled after visiting d_o^j , the candidate is the next
 366 delivery node d_o^{j+1} . Otherwise, if the customer has remaining orders, the candidate is the
 367 first delivery node $d_{o'}^0$ of another randomly selected order o' . Note that for our problem,
 368 not all unscheduled delivery nodes are candidates at each iteration, since deliveries of the
 369 same order are ordered, any order of a customer can be chosen and must be satisfied before
 370 switching to another order, and the number of visits to a customer is not known in advance.

371 Consider two customers whose services are required to start at the same time or in the
 372 same time slot. We could either finish scheduling one before the other, or schedule both

at the same time. Obviously, each of these choices would result in a different solution. Similarly, in some cases, it would be better to schedule a customer that has a high demand and therefore requires more resources first. That's why we added the filtering part to impose some criteria on the algorithm. We can limit CL' to delivery nodes with the same demand, the same due date, or from the same customer. We can also decide if we want to schedule customers with the highest (or lowest) demand or the earliest (latest) due time first. In fact, this helps us to intensify the search in specific neighborhoods of the solution. To diversify the search, we simply remove the filter component. The greedy aspect of GRASP is the creation of the set RCL , the probabilistic aspect is the random selection in RCL , and the adaptive aspect is the updating of CL and the re-evaluation of the incremental costs.

Algorithm 2 Greedy randomized insertion algorithm

Input: S : empty solution S

```

1  $CL \leftarrow \emptyset$ 
2 for each customer  $i$ 
3   | Select a random order  $o_1 \in \mathcal{O}_i$ 
4   |  $CL \leftarrow CL \cup \{d_{o_1}^0\}$ 
5 while  $CL \neq \emptyset$  do
6   |  $CL' \leftarrow \text{Filter}(CL)$ 
7   | for each  $d \in CL'$ 
8     |  $C(d) \leftarrow$  incremental cost of inserting  $d$ 
9   |  $C_{min} \leftarrow \min \{C(d), d \in CL'\}, C_{max} \leftarrow \max \{C(d), d \in CL'\}$ 
10  |  $RCL \leftarrow \{d \in CL', C(d) \leq C_{min} + \alpha(C_{max} - C_{min})\}$ 
11  | Select random delivery node  $d_o^j$  of customer  $i$  from  $RCL$ 
12  |  $L_{d_o^j}, U_{d_o^j} = \text{ScheduleTasks}(d_o^j, S)$ 
13  |  $S \leftarrow S \cup (L_{d_o^j}, U_{d_o^j})$ 
14  |  $q_i \leftarrow q_i - q_{d_o^j}; q_o \leftarrow q_o - q_{d_o^j}$ 
15  | if  $q_o \neq 0$  then
16    |  $CL \leftarrow CL \cup \{d_o^{j+1}\}$ 
17  | else if  $q_i \neq 0$  then
18    | Select another order  $o' \in \mathcal{O}_i$ 
19    |  $CL \leftarrow CL \cup \{d_{o'}^0\}$ 
20  | Update  $CL$ 
21 return  $S$ 

```

Algorithm 3 takes as parameters a delivery node d_o^j of the customer i and a partial solution and looks for a plant and a driver available for loading and unloading operations. For each driver k and plant b we simulate the loading and unloading operations while checking the concrete lifespan and cold joint constraints, and the plant and driver availability. For each node, we first determine the start loading time SLT by subtracting t_{bi} , α_b , and the loading duration $LD_{d_o^j}^b$ to the expected delivery time EDT . EDT is either the arrival time a_i for the first delivery of a customer or the end of the unloading of the precedent delivery. At line 15, we ensure with the procedure *FindDriverLoadingSlot* that the loading starts only if the driver is present at the depot. The presence of the driver does not guarantee that the loading dock is available, thus we use the procedure *FindDepotLoadingSlot* at line 16 to ensure that. Once we know SLT , we can easily deduce the arrival time (AT), start unloading time (SUT), driver waiting time ($W_{d_o^j}^k$), and client waiting time ($W_{d_o^j}$). We also keep track of the driver's work duration. The algorithm returns the best loading and unloading operations

396 with the least cost. We keep track of all timeslots for a plant when its loading dock is busy,
 397 and for a driver when he starts loading until the end of the unloading service. Within
 398 *FindDepotLoadingSlot* (*FindDriverLoadingSlot*), we iterate through the timeslots of a depot
 399 (driver) to schedule the current operation at a free timeslot. These allow us to insert the
 400 scheduling of a node between existing schedules.

Algorithm 3 Schedule loading and unloading tasks

Input: Partial solution S , delivery node d_o^j

```

1 Function ScheduleTask( $d_o^j, S$ )
2    $n_i$ : last node visited for the customer  $i$ 
3    $\mathcal{LS}$ : Partial solutions list
4    $bestSol$   $Cost(bestSol) = +\infty$ 
5   for each driver  $k$ 
6      $n_k$ : current location of  $k$  (plant or delivery node)
7     for each plant  $b$ 
8       if  $t_{bi} \geq \delta$  then continue
9        $EDT = SUT = a_i$ 
10      if  $n_i \neq null$  then
11         $SUT = rand(EUt_{n_i} - \gamma/3, EUt_{n_i})$ 
12         $EDT = EUt_{n_i}$ 
13       $q_o^j = \min\{Q_k, q_o\}$  //  $q_o$  remaining demand of order  $o$ 
14       $SLT = EDT - t_{bi} - \alpha_b - LD_{d_o^j}^b$ 
15       $SLT = FindDriverLoadingSlot(b, n_k, SLT, LD_{d_o^j}^b)$ 
16       $SLT = FindDepotLoadingSlot(b, SLT, LD_{d_o^j}^b)$ 
17       $AT = SLT + LD_{d_o^j}^b + \alpha_b + t_{bi}$ 
18       $SUT = \max\{AT, EDT\}$ 
19       $W_{d_o^j}^k = \max\{0, SUT - AT\}$ 
20       $W_{d_o^j} = \max\{0, AT - EDT - \lambda_i\}$ 
21       $EUT = SUT + UD_{d_{ij}^p}$ 
22       $WT = WT_k + (EUT + \beta_k - SLT) + t_{n_k b} + t_{i, k}$ 
23       $TC = t_{n_k, b} + t_{b, i}$ 
24      if  $Cost(bestSol) < Cost(S) + TC$  then
25         $bestSol = (j, b, k, SLT) \cup (j, b, k, SUT)$ 
26         $Cost(bestSol) = Cost(S) + TC$ 
27  return  $bestSol$ 

```

401 4.3 Local Search

402 5 Experimental results

403 5.1 Generation of instances

404 5.2 Data sets

405 5.2.1 Results for the generated instances

406 5.2.2 Results for the real-world datasets

407 5.2.3 Results for the instances of Kinable et al. [2014]

408 We run our algorithm on the dataset provided in Kinable et al. [2014].

409 6 Conclusion

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