

# Real time optimization of a FTL transportation system

**N. W. Ousmane Ali, Jean-François Côté, Leandro C. Coelho**

Université Laval

14 Mai 2019



# Outline

1. Introduction
2. Problem definition
3. Mathematical formulation
4. ALNS algorithm
5. Computational experiments
6. Conclusion

# Introduction

## Delivery is a complex problem addressed under several perspectives

- Time windows assignment [?]
- City logistics traffic [Coelho et al., 2016]
- Loading of the truck [?]
- Routing of the vehicles [Toth and Vigo, 2014]
- Customer satisfaction

# Introduction

## Delivery is a complex problem addressed under several perspectives

- Time windows assignment [?]
- City logistics traffic [Coelho et al., 2016]
- Loading of the truck [?]
- Routing of the vehicles [Toth and Vigo, 2014]
- Customer satisfaction
  - Delivery within desired time window [?]

# Introduction

## Delivery is a complex problem addressed under several perspectives

- Time windows assignment [?]
- City logistics traffic [Coelho et al., 2016]
- Loading of the truck [?]
- Routing of the vehicles [Toth and Vigo, 2014]
- Customer satisfaction
  - Delivery within desired time window [?]
  - Reduction of service time [?], [?]

# Introduction

## Delivery is a complex problem addressed under several perspectives

- Time windows assignment [?]
- City logistics traffic [Coelho et al., 2016]
- Loading of the truck [?]
- Routing of the vehicles [Toth and Vigo, 2014]
- Customer satisfaction
  - Delivery within desired time window [?]
  - Reduction of service time [?], [?]
  - Additional services [?]

# Introduction

## Delivery is a complex problem addressed under several perspectives

- Time windows assignment [?]
- City logistics traffic [Coelho et al., 2016]
- Loading of the truck [?]
- Routing of the vehicles [Toth and Vigo, 2014]
- Customer satisfaction
  - Delivery within desired time window [?]
  - Reduction of service time [?], [?]
  - **Installation service**

# Introduction

Logistic companies use the following installation strategies

- Installation/assembly is performed by the deliverymen
- Installation/assembly is performed after delivery by a dedicated crew



# Introduction

Logistic companies use the following installation strategies

- Installation/assembly is performed by the deliverymen
- Installation/assembly is performed after delivery by a dedicated crew
- Installation/assembly can be performed by either a deliveryman or an installer

# Introduction

Logistic companies use the following installation strategies

- Installation/assembly is performed by the deliverymen
- Installation/assembly is performed after delivery by a dedicated crew
- **Installation/assembly can be performed by either a deliveryman or an installer**

# What is the DIRPTW?

The DIRPTW is a VRPTW variant with synchronization constraints

- Installation by either deliverymen or installers
- Deliverymen and installers have different installation times
- Deliverymen have higher installation times
- Installer vehicles are faster, smaller, and cheaper than delivery vehicles

## Constraints

- 1 Each customer is served by exactly one delivery vehicle
- 2 A deliveryman must serve a customer within its time window
- 3 An installer must serve a customer within its time window after the delivery
- 4 Each vehicle can wait at the customer until the time window opens
- 5 Each installation is either performed by a deliveryman or an installer

# Definition of the DIRPTW

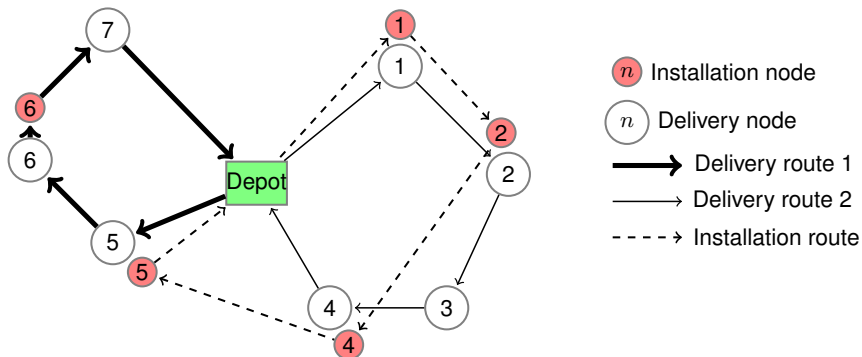


Figure: Solution of a MCDIRP with seven customers

## Variables

- $x_{ijk}$  equal to 1 if a deliveryman travels from  $i$  to  $j$  using vehicle  $k$ , and 0 otherwise
- $y_{ijk}$  equal to 1 if an installer travels from  $i$  to  $j$  using vehicle  $k$ , and 0 otherwise
- $z_i$  equal to 1 if a deliverymen installs at customer  $i$  location, and 0 otherwise

## Subsets

- $D$  is the set of delivery nodes
- $I$  is the set of installation nodes
- $D^I$  is the subset of delivery nodes that require an installation ( $D^I \subseteq D$ )
- $n(i)$  is the delivery node associated with the installation node  $i$
- $l(j)$  is the installation node associated with the delivery node  $j$

# Three-index formulation (1)

$$\begin{aligned}
 & \min \sum_{k \in K^D} \sum_{(i,j) \in A^D} c_{ijk} x_{ijk} + \sum_{k \in K^I} \sum_{(i,j) \in A^I} c_{ijk} y_{ijk} \\
 & \text{Usage of vehicles} \quad \left\{ \begin{aligned} & \sum_{j \in \delta^+(0)} x_{0jk} \leq 1 && k \in K^D, j \in D \\ & \sum_{j \in \delta^+(0)} y_{0jk} \leq 1 && k \in K^I, j \in I \end{aligned} \right. \\
 & \text{Assignment to deliverymen} \quad \left\{ \begin{aligned} & \sum_{k \in K^D} \sum_{j \in \delta^+(i)} x_{ijk} = 1 && i \in D \end{aligned} \right. \\
 & \text{Degree constraints} \quad \left\{ \begin{aligned} & \sum_{j \in \delta^-(i)} x_{jik} - \sum_{j \in \delta^+(i)} x_{ijk} = 0 && i \in N, k \in K^D \\ & \sum_{j \in \delta^-(i)} y_{jik} - \sum_{j \in \delta^+(i)} y_{ijk} = 0 && i \in I, k \in K^I \end{aligned} \right. \\
 & \text{Capacity constraints} \quad \left\{ \begin{aligned} & \sum_{i \in D} q_i \sum_{j \in \delta^+(i)} x_{ijk} \leq Q && k \in K^D \end{aligned} \right. \\
 & \text{Flexibility of installation} \quad \left\{ \begin{aligned} & \sum_{k \in K^I} \sum_{j \in \delta^+(i)} y_{ijk} = 1 - z_i && i \in I \end{aligned} \right.
 \end{aligned}$$

## Three-index formulation (2)

### Timing constraints

$$\begin{aligned}
 S_j &\geq S_i + s_i^D + \sum_{k \in K^D} t_{ijk} x_{ijk} - M \left( 1 - \sum_{k \in K^D} x_{ijk} \right) & (i, j) \in A^D, i \notin D^I \\
 S_j &\geq S_i + s_i^D + \sum_{k \in K^D} (s_{ik}^I + t_{ijk}) x_{ijk} - M \left( 2 - \sum_{k \in K^D} x_{ijk} - z_{l(i)} \right) & (i, j) \in A^D, i \in D^I \\
 S_j &\geq S_i + \sum_{k \in K^I} (s_{ik}^I + t_{ijk}) y_{ijk} - M \left( 1 - \sum_{k \in K^I} y_{ijk} \right) & (i, j) \in A^I \\
 S_i &\geq S_{n(i)} + s_{n(i)} & i \in I \\
 a_i &\leq S_i \leq b_i & i \in N
 \end{aligned}$$

### Domain of variables

$$\begin{aligned}
 x_{ijk} &\in \{0, 1\} & (i, j) \in A, k \in K^D \\
 y_{ijk} &\in \{0, 1\} & (i, j) \in A, k \in K^I \\
 z_i &\in \{0, 1\} & i \in I.
 \end{aligned}$$

# Adaptive Large Neighborhood Search

First introduced in ? for the pickup and delivery routing problem

- Initial solution
- Destroy operators
- Repair operators



# Adaptive Large Neighborhood Search

First introduced in ? for the pickup and delivery routing problem

- Initial solution
- Destroy operators
  - Random delivery removal
  - Related delivery removal
- Repair operators
  - Greedy sequential insertion
  - Regret- $k$  insertion

# Preprocessing procedure for insertion

## Forward time slack [?]

$$F_i = \min_{i \leq k \leq \gamma+1} \sum_{i < p \leq k} W_p + (b_k - B_k) \quad (1)$$

- $\gamma$ : number of nodes in a route
- $A_i$ : arrival time at node  $i$
- $B_i$ : beginning service time at node  $i$
- $W_i$ : waiting time at node  $i$

## Addition of the waiting time at node $i$

$$F_i = \min_{i \leq k \leq \gamma+1} \sum_{i \leq p \leq k} W_p + (b_k - B_k) \quad (2)$$

$W_i = \max \{0, a_i - A_i\}$  for a delivery node  $i$

$W_{l(i)} = \max \{0, B_i + s_i - A_{l(i)}\}$  for its installation node  $l(i)$

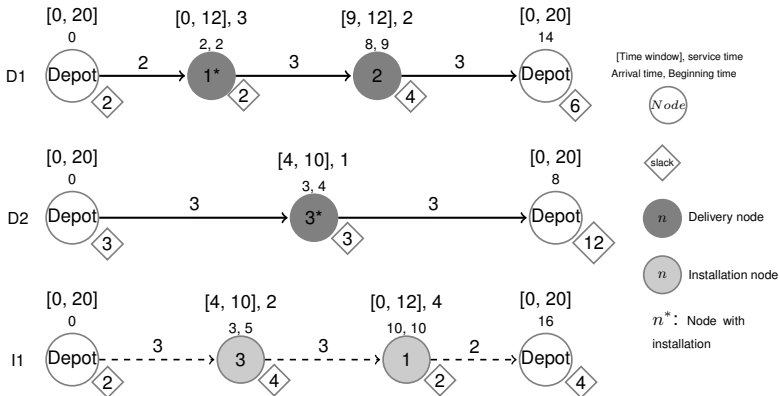
# Preprocessing procedure for insertion

## Delivery and installation on different routes

- compute the arrival time at all delivery nodes of the route
- compute the arrival time at all installation nodes of the route
- compute  $F_{l(i)}$  using equation (2)
- compute  $F_i$  as:

$$F_i = \min \left\{ \min_{i < k \leq \gamma+1} \sum_{i < p \leq k} W_p + (b_k - B_k), b_i - B_i - s_i, F_{l(i)} - W_{l(i)} \right\} + W_i$$

# Illustration of the forward time slack computation



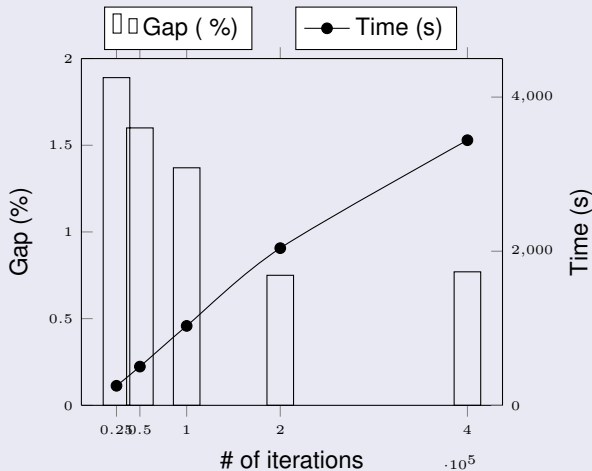
# Instances generation

## Modification of Solomon instances [?] for the VRPTW

- Customers: 15, 25, 50, 100
- Speeds of each delivery/installation vehicle: 1/2
- Costs of the delivery/installation vehicles: 2/1, 5/1 and 10/1
- Efficiency of the deliverymen when installing: [30%, 50%], [60%, 80%]
- Percentage of customers with installation: 20%, 50% and 75%

# ALNS parameters tuning

## Number of iterations



# ALNS parameters tuning

## Operators available

- Destroy operators: random and related removal
- Repair operators: greedy sequential (seq), regret-3, regret- $m$ , regret- $3n$ , regret- $mn$

# Operators selection

**Table:** Quality of the solution when combining the operators

Combination of operators	Gap (%)	Time (s)	% of improvement
seq, regret-3, regret- $m$ , regret- $3n$ , regret- $mn$ , related	-1.20	643.7	86.9
seq, regret-3, regret- $m$ , regret- $3n$ , regret- $mn$ , random, related	-1.08	648.5	85.2
seq, regret- $m$ , regret- $mn$ , random	-0.98	690.6	84.3
seq, regret-3, regret- $m$ , regret- $3n$ , regret- $mn$ , random	-0.96	649.5	83.5
seq, regret- $m$ , regret- $mn$ , random, related	-1.10	680.8	82.6
seq, regret-3, regret- $3n$ , related	-0.62	531.1	82.6
seq, regret- $m$ , regret- $mn$ , related	-0.96	667.4	80.9
seq, regret-3, regret- $3n$ , random, related	-0.59	535.9	79.1
regret-3, regret- $mn$ , related	-0.80	708.4	78.3
regret-3, regret- $m$ , related	-0.80	708.6	78.2
regret- $3n$ , regret- $mn$ , related	-0.80	712.2	78.3
seq, random	-0.36	132.3	78.3
seq, related	-0.35	131.1	78.3
seq, regret-3, regret- $3n$ , random	-0.49	534.2	77.4
regret- $m$ , regret- $3n$ , related	-0.71	707.8	75.6
regret-3, regret- $mn$ , random	-0.61	727.5	75.6
regret-3, regret- $m$ , random	-0.60	732.0	75.6
regret-3, regret- $m$ , random, related	-0.82	711.8	74.8
regret- $3n$ , regret- $mn$ , random, related	-0.82	712.6	74.8
regret-3, regret- $mn$ , random, related	-0.82	714.8	74.8
regret- $3n$ , regret- $mn$ , random	-0.58	737.2	74.8
regret- $m$ , regret- $3n$ , random	-0.87	728.5	73.9
regret- $m$ , regret- $3n$ , random, related	-0.80	720.2	73.9
seq, random, related	-0.54	133.4	73.9



# Results

Table: Results for all instances

Del cost	%Inst	[30%, 50%]						[60%, 80%]					
		Best(%)	Avg(%)	Del	Inst	Time(s)	Gap	Best(%)	Avg(%)	Del	Inst	Time(s)	Gap
2	20%	0.0	0.2	3.3	0.2	51.3	16.5	0.0	0.2	3.2	0.1	51.7	15.6
	50%	0.1	0.4	3.5	0.4	126.8	19.5	0.0	0.2	3.5	0.2	128.7	18.5
	75%	0.0	0.4	3.8	0.6	190.2	22.6	0.0	0.4	3.7	0.3	190.2	21.3
5	20%	0.0	0.2	3.3	0.3	50.5	16.6	0.0	0.2	3.2	0.2	52.4	15.7
	50%	0.0	0.3	3.4	0.6	128.5	19.3	0.0	0.3	3.3	0.4	129.1	19.0
	75%	0.0	0.4	3.5	0.9	200.3	21.6	0.0	0.5	3.5	0.7	203.4	21.5
10	20%	0.0	0.2	3.2	0.4	51.0	17.1	0.0	0.2	3.1	0.2	52.5	16.0
	50%	0.0	0.3	3.3	0.9	131.2	18.9	0.0	0.2	3.2	0.6	127.4	18.5
	75%	0.0	0.4	3.4	1.3	200.7	21.2	0.0	0.4	3.3	0.9	197.2	21.0
Average		0.0	0.3	3.4	0.6	125.6	19.2	0.0	0.3	3.3	0.4	125.8	18.6

# Results

Table: Results for all optimal instances

% of inst	Perf	2				5				10			
		Opt	Best (%)	Time	Gap	Opt	Best (%)	Time	Gap	Opt	Best (%)	Time	Gap
20	[30%, 50%]	30	0.1	9	37	29	0.1	5.9	37.6	26	0.1	8.5	36.7
	[60%, 80%]	30	0.1	5.3	33.7	30	0.0	9.6	34.7	28	0.0	8.8	34.6
50	[30%, 50%]	27	0.2	10	43.8	24	0.2	13.9	41.8	22	0.1	13.5	39.2
	[60%, 80%]	25	0.1	8.1	39.2	21	0.2	7.2	38.8	23	0.1	8.4	39
75	[30%, 50%]	18	0.0	13.4	45.1	18	0.0	14.5	43.5	16	0.0	24.6	41.1
	[60%, 80%]	22	0.0	14.5	44.5	17	0.0	11.2	43	18	0.0	13.2	42.4
Solved		152				139				133			

# Results

$$\sum_{k \in K^I} \sum_{j \in \delta^+(i)} y_{ijk} = 1 - z_i \quad i \in I$$

Comparison when deliverymen efficiency are within [30%, 50%]

Del cost	20%				50%				75%			
	Opt	$z_i = 1$	$z_i = 0$	DIRPTW	Opt	$z_i = 1$	$z_i = 0$	DIRPTW	Opt	$z_i = 1$	$z_i = 0$	DIRPTW
2	28	909.6	908.6	<b>864.2</b>	26	722.6	803.3	<b>696.1</b>	17	896.1	1106.9	<b>855.2</b>
5	29	2247.8	2014.7	<b>1972.4</b>	24	2481.6	2107.0	<b>2020.0</b>	28	2107.9	1860.2	<b>1709.8</b>
10	26	4507.6	3875.3	<b>3838.4</b>	22	5008.6	3985.3	<b>3899.5</b>	16	5887.6	4174.9	<b>4051.2</b>

Comparison when deliverymen efficiency are within [60%, 80%]

Del cost	20%				50%				75%			
	Opt	$z_i = 1$	$z_i = 0$	DIRPTW	Opt	$z_i = 1$	$z_i = 0$	DIRPTW	Opt	$z_i = 1$	$z_i = 0$	DIRPTW
2	27	635.0	719.9	<b>633.4</b>	24	<b>619.6</b>	794.6	640.3	21	<b>913.2</b>	1268.8	920.7
5	30	2256.3	2275.2	<b>2182.8</b>	21	1589.9	1724.3	<b>1574.6</b>	17	1446.8	1630.2	<b>1424.9</b>
10	28	4066.8	3868.1	<b>3795.7</b>	23	3052.3	3112.8	<b>2972.6</b>	18	3429.5	3299.0	<b>3182.9</b>

# Results

$$\sum_{k \in K^I} \sum_{j \in \delta^+(i)} y_{ijk} = 0 \quad i \in I \quad \text{Deliverymen make all installations}$$

Comparison when deliverymen efficiency are within [30%, 50%]

Del cost	20%				50%				75%			
	Opt	$z_i = 1$	$z_i = 0$	DIRPTW	Opt	$z_i = 1$	$z_i = 0$	DIRPTW	Opt	$z_i = 1$	$z_i = 0$	DIRPTW
2	28	909.6	908.6	<b>864.2</b>	26	722.6	803.3	<b>696.1</b>	17	896.1	1106.9	<b>855.2</b>
5	29	2247.8	2014.7	<b>1972.4</b>	24	2481.6	2107.0	<b>2020.0</b>	28	2107.9	1860.2	<b>1709.8</b>
10	26	4507.6	3875.3	<b>3838.4</b>	22	5008.6	3985.3	<b>3899.5</b>	16	5887.6	4174.9	<b>4051.2</b>

Comparison when deliverymen efficiency are within [60%, 80%]

Del cost	20%				50%				75%			
	Opt	$z_i = 1$	$z_i = 0$	DIRPTW	Opt	$z_i = 1$	$z_i = 0$	DIRPTW	Opt	$z_i = 1$	$z_i = 0$	DIRPTW
2	27	635.0	719.9	<b>633.4</b>	24	<b>619.6</b>	794.6	640.3	21	<b>913.2</b>	1268.8	920.7
5	30	2256.3	2275.2	<b>2182.8</b>	21	1589.9	1724.3	<b>1574.6</b>	17	1446.8	1630.2	<b>1424.9</b>
10	28	4066.8	3868.1	<b>3795.7</b>	23	3052.3	3112.8	<b>2972.6</b>	18	3429.5	3299.0	<b>3182.9</b>

# Results

$$\sum_{k \in K^I} \sum_{j \in \delta^+(i)} y_{ijk} = 1 \quad i \in I \quad \text{Deliverymen never install}$$

Comparison when deliverymen efficiency are within [30%, 50%]

Del cost	20%				50%				75%			
	Opt	$z_i = 1$	$z_i = 0$	DIRPTW	Opt	$z_i = 1$	$z_i = 0$	DIRPTW	Opt	$z_i = 1$	$z_i = 0$	DIRPTW
2	28	909.6	908.6	<b>864.2</b>	26	722.6	803.3	<b>696.1</b>	17	896.1	1106.9	<b>855.2</b>
5	29	2247.8	2014.7	<b>1972.4</b>	24	2481.6	2107.0	<b>2020.0</b>	28	2107.9	1860.2	<b>1709.8</b>
10	26	4507.6	3875.3	<b>3838.4</b>	22	5008.6	3985.3	<b>3899.5</b>	16	5887.6	4174.9	<b>4051.2</b>

Comparison when deliverymen efficiency are within [60%, 80%]

Del cost	20%				50%				75%			
	Opt	$z_i = 1$	$z_i = 0$	DIRPTW	Opt	$z_i = 1$	$z_i = 0$	DIRPTW	Opt	$z_i = 1$	$z_i = 0$	DIRPTW
2	27	635.0	719.9	<b>633.4</b>	24	<b>619.6</b>	794.6	640.3	21	<b>913.2</b>	1268.8	920.7
5	30	2256.3	2275.2	<b>2182.8</b>	21	1589.9	1724.3	<b>1574.6</b>	17	1446.8	1630.2	<b>1424.9</b>
10	28	4066.8	3868.1	<b>3795.7</b>	23	3052.3	3112.8	<b>2972.6</b>	18	3429.5	3299.0	<b>3182.9</b>

# Results

$$\sum_{k \in K^I} \sum_{j \in \delta^+(i)} y_{ijk} = 1 - z_i \quad i \in I \quad \text{Both can install}$$

Comparison when deliverymen efficiency are within [30%, 50%]

Del cost	20%				50%				75%			
	Opt	$z_i = 1$	$z_i = 0$	DIRPTW	Opt	$z_i = 1$	$z_i = 0$	DIRPTW	Opt	$z_i = 1$	$z_i = 0$	DIRPTW
2	28	909.6	908.6	<b>864.2</b>	26	722.6	803.3	<b>696.1</b>	17	896.1	1106.9	<b>855.2</b>
5	29	2247.8	2014.7	<b>1972.4</b>	24	2481.6	2107.0	<b>2020.0</b>	28	2107.9	1860.2	<b>1709.8</b>
10	26	4507.6	3875.3	<b>3838.4</b>	22	5008.6	3985.3	<b>3899.5</b>	16	5887.6	4174.9	<b>4051.2</b>

Comparison when deliverymen efficiency are within [60%, 80%]

Del cost	20%				50%				75%			
	Opt	$z_i = 1$	$z_i = 0$	DIRPTW	Opt	$z_i = 1$	$z_i = 0$	DIRPTW	Opt	$z_i = 1$	$z_i = 0$	DIRPTW
2	27	635.0	719.9	<b>633.4</b>	24	<b>619.6</b>	794.6	640.3	21	<b>913.2</b>	1268.8	920.7
5	30	2256.3	2275.2	<b>2182.8</b>	21	1589.9	1724.3	<b>1574.6</b>	17	1446.8	1630.2	<b>1424.9</b>
10	28	4066.8	3868.1	<b>3795.7</b>	23	3052.3	3112.8	<b>2972.6</b>	18	3429.5	3299.0	<b>3182.9</b>

# Managerial insights

- The proposed strategy is better than the traditional strategies
- No need for installation fleet in the following cases:
  - A small number of customers with very few having an installation regardless of the cost or the performance of the deliveryman
  - Low deliveryman cost, higher efficiency, medium size of customers
- Use a distinct installation fleet is better when:
  - Deliverymen efficiency are low and the cost range from medium to high
  - Deliverymen efficiency and cost are both high

# Performance on the VRPMS instances set I

## ? studied the delivery and installation of large items

- Two distinct fleets are used
- A deliveryman and its installer arrival must be synchronized at a certain number of customer locations
- The installer must visit the customer within **ten** units of time after the start of the delivery service



# Results on the VRPMS instances set

## Performance on the VRPMS instances

	?				ALNS				
	Best(%)	Del	Inst	Time (s)	Best(%)	Avg (%)	Del	Inst	Time (s)
Average	6.9	8.4	3.7	63681.0	0.0	0.3	7.6	3.4	170.7

# Results on the VRPMS instances set

## Performance on the VRPMS instances

	?				ALNS				
	Best(%)	Del	Inst	Time (s)	Best(%)	Avg (%)	Del	Inst	Time (s)
Average	6.9	8.4	3.7	63681.0	0.0	0.3	7.6	3.4	170.7

## Results for instances solved optimally with CPLEX

	?				ALNS					Exact method				
	Best (%)	Del	Inst	Time (s)	Best (%)	Avg (%)	Del	Inst	Time (s)	Opt	Gap(%)	Del	Inst	Time (s)
Average	3.0	9.1	4.3	33319.8	0.2	0.3	8.5	4.1	72.7	20.3	34.2	8.5	4.1	505.7
Solved	44				122					139				

# Performance on the VRPTWDST instances set I

?

- Drivers have different efficiency with their customers
- Drivers have specific travel and service times in order to model their familiarity with the customers to visit
- No synchronization constraints

# Performance on the VRPTWDST instances set II

**Table:** Lower and upper bounds for the VRPTWDST for the secondary objective of minimizing travelled distance

	?			ALNS			Exact	
	Best (%)	Opt	Time	Best (%)	Opt	Time	Gap(%)	Opt
C1	0.0	28/90	6.9	0.0	28/90	33.7	22.0	28/90
C2	0.0	24/80	10.5	0.0	24/80	46.8	4.1	24/80
R1	2.4	0/120	94.7	0.2	4/120	37.6	28.7	8/120
R2	6.6	0/110	45.3	0.1	0/110	73.2	19.6	0/110
RC1	3.8	0/80	53.1	0.3	0/80	32.6	40.2	0/80
RC2	10.7	0/80	67.4	0.1	0/80	54.1	28.6	0/80
Average	3.9	-	52.8	0.1	-	46.9	24.0	-
Solved	52/560			56/560			60/560	

# Conclusion

- Novel distribution strategy proposed
- Insights about existing distribution and installation strategies
- An exact and heuristic algorithm to solve the DIRPTW
- New best-know and optimal solutions for the VRPMS and the VRPTWDST

## Applications of the DIRPTW

Choose between a specialist and a generalist in the home care staff scheduling problem

# References I

- L.C. Coelho, J. Renaud, and G. Laporte. Road-based goods transportation: a survey of real-world logistics applications from 2000 to 2015. INFOR: Information Systems and Operational Research, 54(2):79–96, 2016.
- P. Toth and D. Vigo, editors. Vehicle Routing. Monographs on Discrete Mathematics and Applications. MOS-SIAM Series on Optimization, Philadelphia, 2014.