

A GRASP algorithm for the concrete delivery problem.

Ousmane Ali⁽¹⁾, Jean-François Côté⁽²⁾, Leandro C. Coelho⁽³⁾

(1) `nassoma-wattara-ousmane.ali.1@ulaval.ca`

(2) `Jean-Francois.Cote@fsa.ulaval.ca`

(3) `Leandro.Coelho@fsa.ulaval.ca`

February 13, 2023

Abstract

The concrete delivery problem (CDP) is a combinatorial optimization problem that involves scheduling the delivery of ready-mixed concrete to construction sites while balancing the conflicting goals of minimizing transportation costs and maximizing customer satisfaction. This paper proposes an exact formulation and a heuristic approach based on the Greedy Randomized Adaptive Search Procedure (GRASP) to tackle a new variant of the CDP that incorporates realistic side constraints, such as drivers' working shifts, minimum working time for each driver, and overtime penalties. Additionally, the problem also considers the possibility of customers requiring multiple types of concrete to be delivered within the same time window. The performance of the proposed heuristic is evaluated on real-world and generated CDP instances, and it is compared to another variant to demonstrate its effectiveness.

Keywords: Vehicle scheduling; concrete delivery; GRASP; ready-mixed concrete

1 Introduction

Concrete is a widely used building material in construction projects. It is a perishable product that can be affected by many different factors that impact its quality [Sinha et al., 2021] which is crucial for the durability and strength of the final construction.

Concrete comes in two types: ready-mixed concrete (RMC) and site-mixed concrete (SMC). RMC is manufactured in a batch plant and delivered to the construction site, while SMC is produced on-site using raw materials stored on the construction site. Site-mixed concrete can avoid delays caused by road traffic, but it has a slower and more difficult production process, requires storage for mixing materials and equipment, and is suitable for low amounts of concrete. On the other hand, RMC has better quality and benefits from lower production costs [Muresan, 2019]. However, to take advantage of these benefits, the batch plant manager must ensure efficient and prompt delivery on the construction site, which may require a fleet of high-cost revolving drum trucks (concrete mixers) to dispatch the ready-mixed concrete.

Concrete delivery under the form of RMC is subject to many operational constraints that make it a challenging problem met in Operations Research and addressed by the Concrete Delivery Problem (CDP). In this paper, we study a variant of the Concrete Delivery Problem to schedule the daily production and dispatching of RMC for a company located in the province of Quebec, Canada. This company operates multiple batching plants with varying production rates, using a fleet of concrete mixers with different capacities. Each plant has

its own fleet of trucks, however, the trucks are able to move between plants if necessary. The trucks must return to their home plant at the end of the day. The company owns two types of trucks with different capacities but also has the option to call on an external fleet when needed. They serve construction sites from any of their batch plants, with the first delivery starting at the time specified by the customer. The loading and unloading of a concrete mixer depend on the truck capacity, the loading rate at the plant, and the unloading rate at the construction site. Drivers are allocated based on their daily work schedules. A customer may request several types of concrete to be delivered within the same time window, with no required sequence for the orders, but an order can only start after the completion of the previous order. This constraint generalizes the linked order constraints of Durbin and Hoffman [2008] where some customers place two orders for the same day and request that they are linked (the second order begins only after the first order is completed). The setting of this study is similar to a variant of the Concrete Delivery Problem previously studied in Schmid et al. [2009, 2010]. However, it includes the plant’s production rate and driver shift schedule and does not consider unloading instrumentation in contrast to the previous research. The company uses a centralized dispatcher system to schedule all daily orders, but this system has issues satisfying all daily demands without using an external fleet.

According to Blazewicz et al. [2019], the concrete delivery problem combines vehicle routing with scheduling issues to plan routes to deliver concrete from batch plants (depots) to customers’ construction sites. Ready-mixed concrete is an on-demand product with a short life cycle from production through end use. It cannot be stored and cannot stay too long in a truck, or it will harden. Hence, concrete mixers must deliver RMC at the planned construction site shortly after its production. RMC production and delivery is described by Tommelein and Li [1999] as an example of a Just-In-Time (JIT) production system in construction. A customer quantity requirement is often greater than the truck size and must be fulfilled by multiple deliveries. In that sense, CDP is like the Vehicle Routing Problem (VRP) with split delivery (VRPSD) [Archetti and Speranza, 2008], except that the same truck may visit a customer more than once. Concrete hardens quickly, so when there are multiple deliveries, they must be done back-to-back or at least close in time to avoid the problem of cold joint, which can reduce the strength and durability of the concrete. Customers request to be served within a specific time window, which can complicate truck-loading schedules when a plant can only load one truck at a time. Similarly, only one truck can unload at a time at a customer location, sometimes leading to concrete mixers queuing and waiting their turn to deliver. Furthermore, with trucks of varied sizes, loading, travel, and unloading times that may be uncertain, the Concrete Delivery Problem is a complex problem to solve and has been proven to be NP-hard [Asbach et al., 2009, Kinable et al., 2014].

In this paper, we propose a mathematical model and a Greedy Randomized Search Procedure (GRASP) heuristic solution to solve a new variant for the CDP. Our model takes into consideration the working shifts of the drivers and the scheduling of multiple orders within the same time window at a construction site. To the best of our knowledge, this paper is the first that deals with these specific constraints in the context of the CDP.

The rest of the paper is structured as follows: Section 2 provides a literature review of previous work related to the CDP. Section 3 provides a formal description and mathematical model of the problem. In Section 4, we describe the Greedy Randomized Search Procedure algorithm and the constructive heuristics developed to solve this variant of the CDP. Section 5 presents computational experiments to evaluate the proposed approach, and finally, the conclusions are presented in Section 6.

2 Literature review

A text mining approach by Maghrebi et al. [2015] for reviewing the ready-mixed concrete literature showed that concrete technology and material science are the main core of research in this area. Academic research on concrete batching and delivery began in the late 1990s. Tommelein and Li [1999] described ready-mixed concrete (RMC) as a prototypical example of a Just-In-Time production system in construction and identified two practices for delivering it. One approach is for the customer to haul the product from the batch plant with their concrete mixer, while the other approach is for the batch plant to deliver the concrete directly to the customer's location. This latter approach is the one that has been studied in all related papers found in the literature.

Several works to schedule and dispatch concrete production and delivery have mainly focused on simulation-related methods. These methods can be standalone, such as those used by Zayed and Halpin [2001], Wang et al. [2001], Tian et al. [2010], Panas and Pantouvakis [2013] and Galić and Kraus [2016], among others. Alternatively, these methods can be hybridized with optimization techniques, such as those used by Feng et al. [2004], Lu and Lam [2005], Feng and Wu [2006], etc. Wang et al. [2001] developed a simulation model to reveal the effect and value of the concrete mixers' inter-arrival time on the productivity of hired unloading equipment on site. Feng et al. [2004] used a combination of Genetic Algorithm (GA) and simulation process to minimize the total waiting time for trucks at a customer site. The study focused on loading trucks with identical capacities at the same batch plant, with fixed loading and unloading durations. The GA was used to find the best loading sequence of RMC trucks to be assigned to different construction sites. The simulation process determined the loading, arrival, departure, and waiting time of trucks and thus evaluated the cost of each dispatching sequence. They evaluated their method using data from a batch plant in Taiwan with up to nine customers served. Mayteekriengkrai and Wongthatsanekorn [2015] addressed the same problem with the same data using a bee algorithm (BA) and found better solutions than the GA. Lu and Lam [2005] used the same combination of GA and simulation to determine the optimal number of concrete mixers to be deployed and an optimal schedule for batching and delivering concrete. Their objective was to minimize the idle time of the site crew due to late concrete deliveries and truck queuing time. In this setting, it was also necessary to deliver a batch of mortar on-site to lubricate the unloading pump before the concrete delivery. As such, the simulation model also included the batching and delivery of mortar. Finding the best RMC truck size was also the purpose of the discrete-event simulation model proposed by Panas and Pantouvakis [2013].

In addition to simulation-based methods, several other approaches have been used in the literature to solve the CDP. These include metaheuristics [Faria et al., 2006, Misir et al., 2011, Maghrebi et al., 2016b, Yang et al., 2022], exact methods [Yan and Lai, 2007, Asbach et al., 2009, Kinable et al., 2014], matheuristics [Schmid et al., 2009, 2010], Benders Decomposition [Maghrebi et al., 2014a], Column Generation (CG) [Maghrebi et al., 2014b, 2016a], Lagrangian relaxation [Narayanan et al., 2015], and machine learning approaches such as those used by Graham et al. [2006], Maghrebi and Waller [2014], Maghrebi et al. [2016c]. Matsatsinis [2004] designed a decision support system (DSS) for the dynamic routing of both concrete and pumps that may be necessary for some construction sites to aid in the unloading of concrete. The DSS considered the availability of three plants but stipulated that vehicles fulfilling the same order must all load at the same plant. Orders that could not be executed immediately could be postponed for the next day. The routing of the pumps was modelled as a multi-depot vehicle routing problem with time windows. Naso et al. [2007] proposed a sequential GA method combined with constructive heuristics to solve an-

134 other variant of the CDP. In this problem, the plant’s production schedule must account for
 135 orders for concrete to be delivered to a customer site and orders that customers must pick
 136 up themselves. The algorithm first schedules the plant loading operations before scheduling
 137 truck deliveries. The authors also developed a non-linear model that minimizes transporta-
 138 tion costs, waiting times, outsourced costs, and overtime work. They ran experiments using
 139 real-world instances of a concrete supply chain in the Netherlands and found a reduction in
 140 the number of requests redirected to external companies. Yan and Lai [2007] also considered
 141 overtime considerations in their paper, which focused on scheduling RMC for one batching
 142 plant with two loading docks. The study took into account that overtime wages are paid
 143 for factory and construction site operations after 4 PM. They developed a mixed integer
 144 programming (MIP) model on a time-space network to minimize travel times and operating
 145 costs at both normal and overtime working hours at the plant and the construction sites.
 146 They tested the model using real-data consisting of 3 days of operation using a two-stage
 147 algorithm. First, they solved the MIP relaxation with CPLEX. Then, they simplified the
 148 original model by fixing some decision variables before solving it. The algorithm was found
 149 to improve the actual plant operation by 10%. A time-space network is the key component
 150 of the real-time decision support system (DSS) developed by Durbin and Hoffman [2008] to
 151 solve a dynamic CDP problem every five minutes. The DSS is able to receive new orders,
 152 schedule them on the fly, and handle unexpected events such as plant closures, truck break-
 153 downs, and delays in transportation times. The authors combined the DSS with a Tabu
 154 Search (TS) heuristic to warm start CPLEX, which made the model performant enough to
 155 solve instances with up to 1,500 loads per day with up to 250 trucks. The DSS also considers
 156 the case of a customer who places two orders, with the first being completed before the sec-
 157 ond starts. Further insights on the real-time planning and monitoring of CDP are available
 158 in Garza Cavazos [2021]. Another variant of the CDP is modeled by Schmid et al. [2009] as
 159 an integer multicommodity network flow (MCNF) problem on a time-space network. In this
 160 paper, concrete is delivered using a heterogeneous fleet of vehicles, and each plant can load
 161 an unlimited number of trucks simultaneously. Some of the trucks have specialized equip-
 162 ment and must arrive first at certain construction sites to assist in unloading the concrete.
 163 The objective is to fulfill all orders, minimize the travel cost, and avoid delays between
 164 two consecutive unloading operations for an order. The model is typically solved using
 165 a matheuristic algorithm that combines the MCNF with a variable neighborhood search
 166 (VNS) heuristic. The method can quickly solve large problem instances with more than 60
 167 orders per day without encountering any memory issues. The same problem is addressed
 168 by Schmid et al. [2010] who proposed a mixed integer programming (MIP) model combined
 169 with a VNS and a very large neighborhood search (VLNS) to develop two matheuristics
 170 approaches. Comparisons between both matheuristics and a standalone VNS show that the
 171 former methods are much better and suitable for solving larger problem instances. These
 172 methods also provide better solutions for small to medium instances than the matheuristic
 173 used in Schmid et al. [2009]. A pure VNS approach with the same problem but without the
 174 use of instrumentation has been applied by Payr and Schmid [2009].

175 Regarding objectives, most authors have focused on minimizing travel time and delays
 176 between consecutive deliveries. However, some authors have been more interested in max-
 177 imizing customer satisfaction alone. We find these situations in the works of Durbin and
 178 Hoffman [2008], Kinable et al. [2014], Kinable and Trick [2014], Sulaman et al. [2017]. Kin-
 179 able et al. [2014] introduce a general MIP and constraint programming (CP) models of the
 180 CDP reflecting the main constraints commonly found in all CDP works: time lag and no
 181 overlapping between consecutive deliveries, covering of all customers’ demands, delivery time
 182 window, and heterogeneous fleet. However, the model did not include constraints limiting

the time that concrete may reside in a truck. The authors propose a constructive heuristic that schedules the visits to the customers one by one according to the start time of the visit and the truck capacity. The procedure is invoked multiple times for different permutations of the customer’s order which is determined using the steepest descent (SD) local search procedure. One of the paper’s main contributions is the creation of the first public test instances for the CDP with up to 50 customers, four batching plants, and 20 concrete mixers. They found the CP model to be highly effective in finding high-quality solutions in relatively little time or improving existing schedules, while the MIP model can be used to compute bounds, as it seems ineffective in solving large problem instances. Finally, the heuristic often yields good solutions in less than a second. A detailed analysis of the MIP model presented in citekinable2014concrete and of two more compact models can be found in the thesis of Hernández López [2020]. In Kinable and Trick [2014], we found an attempt to solve the previous problem with a Logic Based Benders’ approach. Sulaman et al. [2017] expand upon the SD heuristic proposed in Kinable et al. [2014], proposing a Simulated Annealing (SA) with a Time-Slot Heuristic (TH). TH mechanism is to look for a slot between existing visits of a truck to schedule a new delivery instead of assigning it to the time slot strictly after the truck’s latest assigned delivery. The goal is to reduce the large time gaps that can be present in a schedule created with SD due to ignoring the intermediate available time slots. Experimental results indicated that SATH outperforms SD in speed and solution quality. A generalization of the MIP model of Kinable et al. [2014] is addressed in Asbach et al. [2009]. This model simultaneously minimizes the total sum of travel costs and the penalty costs for customers with unfulfilled demand. A customer can request that all concrete deliveries come from the same plant or a subset of plants and that a delivery truck belongs to a subset of the vehicle fleet. The MIP model is used in a local search scheme as a black-box solver to reoptimize an incumbent solution in which a neighborhood operator has unfixed some variables. Tzanetos and Blondin [2023] provides an overview of the various methods used in the literature to address the Concrete Delivery Problem and categorizes the problem formulations based on the different concepts used in the literature, such as Integer Programming (IP), time-space network, and job shop model. They also discussed the consistency between industry needs and existing constraints and provided insights into the datasets corresponding to real-world cases, identifying the necessary data for practitioners.

3 Problem description

The focus of this paper is the distribution of ready-mixed concrete from a Canadian company that operates in the greater Montreal area. When a customer places an order, it is received at a central center and then assigned to one of the company’s batching plants. These plants produce the concrete and then deliver it to the customer. The problem we are examining involves a set of batching plants, a set of customer orders, and a set of concrete-mixer drivers.

The company owns a total of eight batching plants, located in various geographical regions. Each plant has a loading bay that can only accommodate one truck at a time, which leads to trucks lining up. Let \mathcal{B} be the set of batching plants. The plants are heterogeneous, as each plant has its own hourly loading rate, represented by τ_b^l , which affects the duration of the loading process. After the concrete has been loaded, the driver spends α_b minutes adjusting the concrete in the truck before heading to the customer site. A batching plant can serve a construction site as long as the travel time between the two is less than the concrete’s lifespan, which is represented by Δ . Each plant has its own assigned fleet of trucks, but it can also borrow trucks from other plants or hire external fleets if necessary.

230 A customer i requests a total of q_i of one or several types of concrete to be delivered
 231 to his construction site on a particular day. We call an order a request for a specific type
 232 of concrete. When placing an order o , the customer i specifies the required quantity, q_o ,
 233 the desired arrival time of the first concrete mixer, a_i , and the unloading rate at their
 234 construction site, τ_i^u . If the order requires more concrete than a single truck can carry,
 235 multiple deliveries are scheduled. Let O_i be the unordered set of all orders requested by
 236 customer i . Each element of O_i must be thoroughly delivered before moving on to another
 237 order. One element o of O_i must have its first delivery start at a_i , while the others can
 238 start any time after all deliveries of o . Once a plant is chosen to produce a customer's first
 239 delivery, it must be the provider of all subsequent deliveries of this customer. To prevent cold
 240 joint issues with the concrete, subsequent deliveries must be made just in time, or at least
 241 close in time. We define a maximum time lag γ_i beyond which no next unloading operation
 242 should be allowed. The construction site unloading rate and the quantity to unload give the
 243 time necessary to discharge a truckload. \mathcal{C} is the set of construction sites (customers) with
 244 a planned delivery for the day. \mathcal{O} is the set of all requested orders.

245 The company has two types of concrete mixer trucks with capacities of 8 and 12 cubic
 246 meters. Each driver k is assigned to a specific batching plant and is responsible for driving
 247 a truck with a specific capacity Q_k . The set of drivers is represented by $K = \cup_{b \in \mathcal{B}} K_b$, K_b
 248 being the set of drivers scheduled to start their shift at the batching plant b . t_{ij} is the known
 249 time to travel between any two locations i and j . A scheduled driver k is required to begin
 250 their shift at H_k , work for a minimum of M_T hours and a maximum of N_T hours during
 251 regular working hours, with the possibility of overtime of up to O_T hours.

252 A driver typically loads RMC at their assigned batching plant, but may also be required
 253 to drive to and load at other plants if needed. The batching plant produces concrete on-
 254 demand with recipes specific to each customer. This means that a truck cannot hold orders
 255 for more than one customer, even if there is spare capacity. To fulfill multiple orders, a
 256 driver must refill at a plant between deliveries. After unloading the RMC, a driver takes β_k
 257 minutes to clean the concrete mixer before travelling to his next loading plant.

258 A solution to the problem involves making decisions about truck loading schedules, driver
 259 assignments to different deliveries, and truck arrival times at construction sites for unloading.
 260 For a batching plant, the decision involves choosing which driver to load, when to load
 261 them, and which construction site they should deliver to. For a driver, the decision involves
 262 determining the sequence of loading depots and delivery sites. And for a construction site,
 263 the decision involves determining the arrival times of all scheduled deliveries for the day.

264 We now present a formal definition of our problem. Let n_o be the number of deliveries
 265 needed to fulfill order o . n_o is not known in advance, as we use a fleet of trucks with various
 266 capacities. However, we can compute its lower (n_o^{min}) and upper (n_o^{max}) bounds using the
 267 capacities of the highest (Q_{max}) and smallest (Q_{min}) available trucks. The lower bound is
 268 the number of deliveries needed if we only use trucks of capacity Q_{max} , while the upper
 269 bound is the number of deliveries needed if we only use trucks of capacity Q_{min} .

$$\left\lceil \frac{q_o}{Q_{max}} \right\rceil \leq n_o \leq \left\lceil \frac{q_o}{Q_{min}} \right\rceil \quad \forall o \in \mathcal{O}. \quad (1)$$

270 Let d_o^j be the j_{th} visit with load q_o^j for order o . We represent the delivery of order o by
 271 the visits to the ordered set of nodes $\mathcal{D}_o = (d_o^0, d_o^1, \dots, d_o^{n_o})$. We represent the deliveries
 272 of customer i by the ordered set $\mathcal{D}_i = (\mathcal{D}_{o_1}, \mathcal{D}_{o_2}, \dots, \mathcal{D}_{o_{|O_i|}})$, where o_r is the r_{th} order
 273 delivered. We will refer to $d \in \mathcal{D}_i$ ($d \in \mathcal{D}_o$) as the d_{th} potential delivery of customer i (order
 274 o). $\mathcal{D} = \bigcup_{i \in \mathcal{C}} \mathcal{D}_i$ is the union of all delivery nodes.

275 We represent each plant b by the ordered set $L_b = \{L_{b,1}, L_{b,2}, \dots, L_{b,n(b)}\}$ of loading
 276 docks nodes, with $n(b)$ being the number of delivery nodes at a maximal travel time of Δ of
 277 b . We will refer to $L_{b,l}$ or $l \in L_b$ as the l th potential loading operation at b . $\mathcal{L} = \bigcup_{b \in B} L_b$
 278 is the union of all loading docks.

279 Each driver leaves and returns to his home plant each day. We represent a driver k home
 280 plant with a starting s_k and ending e_k depot. S and E are the sets of starting and ending
 281 depot.

282 We define our problem on a complete directed graph where $V = \{S \cup \mathcal{L} \cup \mathcal{D} \cup E\}$ is the
 283 set of nodes. The arc sets are $A = \{(i, j, k) \mid i, j \in V, k \in K\}$, and $A^D = \{(i, j) \mid i, j \in \mathcal{D}\}$.
 284 A corresponds to allowed movements of drivers from node i to node j . For each driver k ,
 285 the allowed movements are the following:

- 286 • From the starting depot s_k to a loading dock $l \in \mathcal{L}$ or to the ending depot e_k .
- 287 • From a loading dock $l \in \mathcal{L}$ to a delivery node $d \in \mathcal{D}$.
- 288 • From a delivery node $d \in \mathcal{D}$ to a loading dock $l \in \mathcal{L}$ or to the ending depot e_k .

289 For a customer c , arcs in A^D link consecutive delivery nodes of the same order $\{(i, j) \in$
 290 $\mathcal{D}_o, o \in \mathcal{O}_c, i < j\}$, and pair of delivery nodes of two different orders $\{(i, d_{o_2}^0), i \in \mathcal{D}_{o_1}, i \geq$
 291 $n_{o_1}^{min}, o_1, o_2 \in \mathcal{O}_c, o_1 \neq o_2\}$.

292 $\delta^+(i) = \{(i, j, k) \in A\}$, and $\delta^-(i) = \{(j, i, k) \in A\}$ are the outcoming and incoming arc
 293 sets of any node $i \in V$. Similarly, $\delta_D^+(i) = \{(i, j) \in A^D\}$, and $\delta_D^-(i) = \{(j, i) \in A^D\}$ are the
 294 outcoming and incoming arc sets of delivery node $i \in \mathcal{D}$.

295 Let the binary variable x_{ij}^k be 1 if driver k travels from node i to j . Binary variable
 296 y_i equals 1 if customer i is completely served. v_i is the start of the loading (unloading)
 297 operation at node $i \in L \cup D$. w_i is the end of the loading (unloading) operation at node
 298 $i \in L \cup D$. The binary variable $u_{i,j}$ equals 1 if delivery node j is served just after delivery
 299 i . Binary variable σ_{ib} equals 1 if customer i orders' are loaded from plant b .

300 A driver k leaves his starting node exactly once a day and travels to either a loading
 301 dock or his ending node. When loading at a loading dock i , he takes some time to adjust the
 302 concrete in the truck before travelling to delivery node j to unload. The loading operation
 303 duration depends on the plant loading rate and the quantity q_j^k of RMC to load towards j .
 304 After completing his last unloading operation of the day, he returns to his end node.

$$\sum_{j \in \delta^+(s_k)} x_{s_k j}^k = 1 \quad \forall k \in K \quad (2)$$

$$v_j \geq w_i + \alpha_i + t_{ij} - M(1 - x_{ij}^k) \quad \forall i \in \mathcal{L}, j \in \mathcal{D}, k \in K \quad (3)$$

$$w_i \geq v_i + \frac{q_j^k}{\tau_b^l} - M(1 - x_{ij}^k) \quad \forall b \in \mathcal{B}, i \in L_b, j \in \mathcal{D}, k \in K \quad (4)$$

$$\sum_{j \in \delta^-(e_k)} x_{j e_k}^k = 1 \quad \forall k \in K \quad (5)$$

305 Constraints (4) ensure that two trucks cannot be loaded simultaneously in a plant.

$$w_{l-1} \leq v_l \quad \forall b \in B, l \in L_b, l \geq 1 \quad (6)$$

After completing a delivery at node i , a driver must clean the truck, and travel to the next
 loading depot or end node. The unloading service depends on the construction site's rate

and the received quantity. Unloading operations must finish Δ minutes after the beginning of loading.

$$v_j \geq w_i + \beta_k + t_{ij} - M(1 - x_{ij}^k) \quad \forall i \in \mathcal{D}, j \in \mathcal{L} \cup \{e_k\}, k \in K \quad (7)$$

$$w_j \geq v_j + \frac{q_j^k}{\tau_c^u} - M(1 - x_{ij}^k) \quad \forall c \in \mathcal{C}, j \in \mathcal{D}_c, i \in \mathcal{L}, k \in K \quad (8)$$

$$w_j \leq v_i + \Delta + M(1 - x_{ij}^k) \quad \forall c \in \mathcal{C}, j \in \mathcal{D}_c, i \in \mathcal{L}, k \in K \quad (9)$$

306 The first service of any customer i has to start at the due time a_i . Let g_i be the gap
 307 between the due time and the start of the first service at i . This first service may be
 308 performed at the first delivery node of any order $\in O_i$. Constraints (12–14) are used to find
 309 the delivery sequence of the first delivery node of all orders $\in O_i$.

$$v_{d_o^0} \geq a_i \quad \forall i \in \mathcal{C}, \forall o \in O_i \quad (10)$$

$$g_i \geq v_d - a_i - M \left(\sum_{j \in \delta_D^-(d)} u_{j,d} \right) \quad \forall i \in \mathcal{C}, \forall o_1 \in O_i, d = d_{o_1}^0 \quad (11)$$

$$\sum_{o_1 \in O_i} \sum_{j \in \delta_D^-(d_{o_1}^0)} u_{j,d_{o_1}^0} = |O_i| - 1 \quad \forall i \in \mathcal{C}, |O_i| > 1 \quad (12)$$

$$\sum_{o_1 \in O_i} \sum_{j \in \delta_D^+(d_{o_1}^0)} u_{d_{o_1}^0,j} = |O_i| - 1 \quad \forall i \in \mathcal{C}, |O_i| > 1 \quad (13)$$

$$\sum_{j \in \delta_D^+(d_{o_1}^0)} u_{d_{o_1}^0,j} \leq 1, \sum_{j \in \delta_D^-(d_{o_1}^0)} u_{j,d_{o_1}^0} \leq 1, \sum_{j \in \delta_D^+(d_{o_1}^0)} u_{d_{o_1}^0,j} + \sum_{j \in \delta_D^-(d_{o_1}^0)} u_{j,d_{o_1}^0} \geq 1 \quad \forall i \in \mathcal{C}, \forall o_1 \in O_i \quad (14)$$

310 For a customer, an order must be completed before starting another. Constraints (15–
 311 16) enforce the precedence constraints between the last delivery of an order and the first
 312 delivery of the subsequent order.

$$v_{d_{o_2}^0} \geq w_j - M(1 - u_{j,d_{o_2}^0}) \quad \forall i \in \mathcal{C}, \forall o_1, o_2 \in O_i, j \in \mathcal{D}_{o_1}, (j, d_{o_2}^0) \in \delta_D^-(d_{o_2}^0) \quad (15)$$

$$v_{d_{o_2}^0} \leq w_j + \gamma_i + M(1 - u_{j,d_{o_2}^0}) \quad \forall i \in \mathcal{C}, \forall o_1, o_2 \in O_i, j \in \mathcal{D}_{o_1}, (j, d_{o_2}^0) \in \delta_D^-(d_{o_2}^0) \quad (16)$$

313 Constraints (17–18) enforce the precedence constraints between two consecutive delivery
 314 nodes of the same order.

$$u_{j-1,j} \geq u_{j,j+1} \quad \forall i \in \mathcal{C}, \forall o \in O_i, j \in \mathcal{D}_o, 1 \leq j \leq n_o - 1 \quad (17)$$

$$u_{j-1,j} \geq \sum_{l \in \mathcal{L}} x_{lj} \quad \forall i \in \mathcal{C}, \forall o \in O_i, j \in \mathcal{D}_o, j \geq 1 \quad (18)$$

315 Constraints (19–20) state that it is not possible for two trucks serving consecutive deliv-
 316 eries to be unloaded at the same time and there is a maximum time lag between them.

$$v_j \geq w_{j-1} - M(1 - u_{j-1,j}) \quad \forall i \in \mathcal{C}, \forall o \in O_i, j \in \mathcal{D}_o, j \geq 1 \quad (19)$$

$$v_j \leq w_{j-1} + \gamma_i + M(1 - u_{j-1,j}) \quad \forall i \in \mathcal{C}, \forall o \in O_i, j \in \mathcal{D}_o, j \geq 1 \quad (20)$$

317 With constraints (21) and (22), we respectively impose that the cumulative capacity of
 318 all concrete mixers serving an order and a customer may exceed the required quantities.

$$\sum_{d \in D_o} \sum_{k \in K} q^k \sum_{j \in \mathcal{L}} x_{jd}^k \geq q_o, \forall o \in \mathcal{O} \quad (21)$$

$$\sum_{d \in D_i} \sum_{k \in K} q^k \sum_{j \in \mathcal{L}} x_{jd}^k \geq q_i, \forall i \in \mathcal{C} \quad (22)$$

319 Constraints (23) and (24) impose that a loading or delivery node may only be visited
 320 once by one driver. Constraints (25) and (26) are degree constraints.

$$\sum_{k \in K} \sum_{j \in \mathcal{D}} x_{ij}^k \leq 1 \quad i \in \mathcal{L} \quad (23)$$

$$\sum_{k \in K} \sum_{i \in \mathcal{L}} x_{ij}^k \leq 1 \quad j \in \mathcal{D} \quad (24)$$

$$\sum_{k \in K} \sum_{i \in \mathcal{L}} x_{ij}^k = \sum_{k \in K} \sum_{i \in \mathcal{L}} x_{ji}^k \quad j \in \mathcal{D} \quad (25)$$

$$\sum_{k \in K} \sum_{i \in \mathcal{D}} x_{ij}^k = \sum_{k \in K} \sum_{i \in \mathcal{D}} x_{ji}^k \quad j \in \mathcal{L} \quad (26)$$

321 Constraints (27) and (28) impose that all orders of customer i must be loaded from the
 322 same plant.

$$\sum_{k \in K} \sum_{l \in \mathcal{L}_b} \sum_{d \in \mathcal{D}} x_{ld}^k \leq M * \sigma_{i,b} \quad \forall i \in \mathcal{C}, b \in \mathcal{B} \quad (27)$$

$$\sum_{b \in \mathcal{B}} \sigma_{i,b} \leq 1 \quad \forall i \in \mathcal{C}, b \in \mathcal{B} \quad (28)$$

323 Let w_k^1 be the binary variables indicating if the driver k has reached the minimum number
 324 of hours worked in the day. w_k^2 is a continuous variable indicating the gap between the driver
 325 working time and the normal working time.

$$M_T * w_k^1 \leq v_{e_k} - H_k \quad \forall k \in K \quad (29)$$

$$w_k^2 \geq (v_{e_k} - H_k) - N_T \quad \forall k \in K. \quad (30)$$

The objective function (31) minimizes the travelled distance, the penalty costs incurred when customers' demands are not fully satisfied, the lateness of each customer first delivery, the number of drivers who work under the minimum working time and the total overtime cost when drivers work beyond their scheduled hours.

$$\begin{aligned} \min \sum_{k \in K} \sum_{i \in \mathcal{L}} \sum_{j \in \delta^+(i)} t_{ij} x_{ij}^k &+ \sum_{k \in K} \sum_{i \in \mathcal{D}} \sum_{j \in \delta^+(i)} t_{ij} x_{ij}^k + \sum_{i \in \mathcal{C}} \beta_1 (1 - y_i) \\ &+ \beta_2 \sum_{i \in \mathcal{C}} g_i + \sum_{k \in K} \beta_3 * w_k^1 + \beta_4 * w_k^2 \end{aligned} \quad (31)$$

Let us consider the solution of a small instance of our problem illustrated in Figures 1 and 2. Two batching plants B_1 and B_2 with three drivers serve two construction sites. Customer C_1 requests one order of $q_1^1 = 12 \text{ m}^3$. Customer C_2 requests three orders of $q_2^1 = 3$, $q_2^2 = 11$, and $q_2^3 = 1 \text{ m}^3$ of three different types of concrete. B_1 has two drivers (D_1 , D_2) using concrete mixers of capacity 8 m^3 , and B_2 has D_3 of capacity 12 m^3 . Figure 1 depicts the concrete mixers flow in the network. We schedule D_1 and D_2 to respectively deliver 8 and 4 m^3 to C_1 . We select o_2^2 as the first order of C_2 to deliver. D_3 travels to B_1 to load q_2^2 , then visits C_2 before returning to his home plant. Meanwhile, after their first trip, D_1 and D_2 deliver the remaining orders of C_2 .

Figure 2 shows the sequence of loading and unloading operations. The first deliveries of C_1 and C_2 are timely and there is no gap between the two deliveries received by C_1 . There is a delay between the end of the first delivery and the start of the second delivery of C_2 , however, it is less than the maximal time lag of 20 minutes defined for this example.

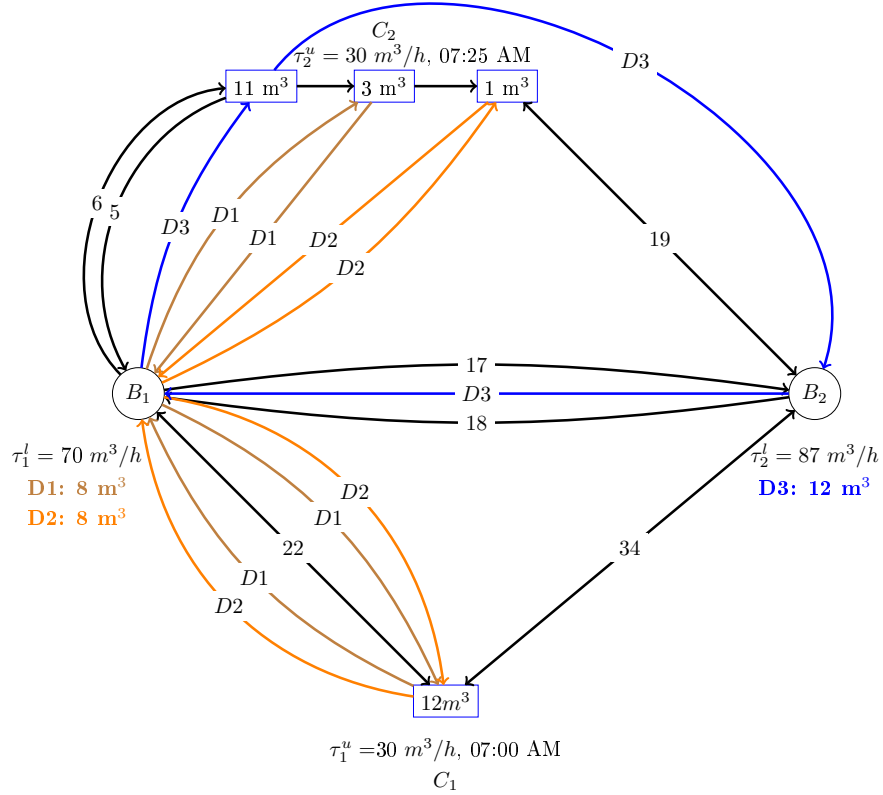


Figure 1: Solution of an instance with two plants, two construction sites, four orders, and three drivers.

4 Constructive heuristics and GRASP

We now present the heuristic approach we implement to solve this variant of the Concrete Delivery Problem. Our method consists in constructing feasible solutions for the CDP

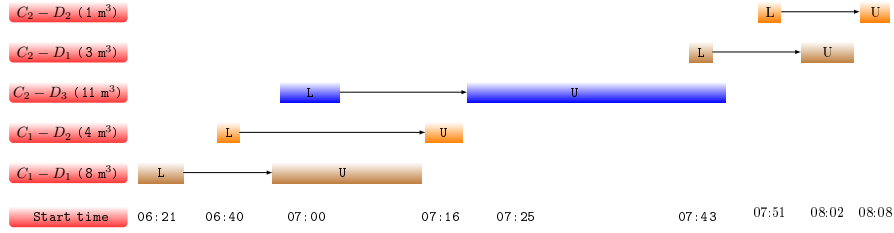


Figure 2: Schedule of the instance of Figure 1.

342 with randomized heuristics and iteratively calling these heuristics in the greedy randomized
 343 adaptive search procedure (GRASP) metaheuristic.

In this section, we represent the scheduling of a delivery node d as a pair of loading L_d and unloading U_d tasks. We then refer to a solution S as a set of loading and unloading tasks performed by a set of drivers during a particular day.

$$\begin{aligned}
 L_d &= \{(b, k, q_d, v_b), b \in \mathcal{B}, k \in K\} \\
 U_d &= (k, v_d, w_d), k \in K \\
 S &= \left\{ \cup_{1 \leq j \leq n_o} (L_{d_o^j}, U_{d_o^j}), \forall o \in \mathcal{O} \right\}
 \end{aligned}$$

344 4.1 GRASP algorithm

345 The GRASP algorithm is an iterative suite of constructive and local search algorithms
 346 introduced by Feo and Resende [1995]. For each iteration, a feasible solution S is built using
 347 a greedy randomized algorithm. Then a local search algorithm investigates the neighborhood
 348 of S to find a local optimum. The pseudo-code of Algorithm 1 shows that the procedure
 349 returns the best overall solution (for a minimization problem) after some stopping conditions
 350 (time limit or a maximal number of iterations) are met.

Algorithm 1 Pseudo-code of the GRASP algorithm

Input: H : List of constructive randomized heuristics

```

1  $S^* \leftarrow \emptyset$     $Cost(S^*) \leftarrow \infty$ 
2 while Conditions not met do
3    $Cost(S') \leftarrow \infty$ 
4   for each  $h \in H$ 
5      $S \leftarrow h(S)$ 
6      $S \leftarrow LocalSearch(S)$ 
7     if  $Cost(S) < Cost(S')$  then
8        $S' \leftarrow S$ 
9       if  $Cost(S') < Cost(S^*)$  then
10         $S^* \leftarrow S'$ 
11 return  $S^*$ 

```

351 4.2 Greedy randomized insertion algorithm

352 As referred to in Resende and Ribeiro [2019], the general outline of a greedy randomized
 353 algorithm used in the GRASP framework works as described in Algorithm 2. At each

iteration, let's consider the set CL of candidate delivery nodes that are not yet scheduled. We note that, for our problem, not all delivery nodes are candidates for insertion at each iteration, since deliveries of the same order are ordered, any order of a customer may be chosen, and it must be satisfied before switching to another order, and the number of visits to a customer is not known beforehand. We first initialize CL with the first delivery of a random order for each customer. We create the set CL' with elements of CL we deem promising for a better solution. We evaluate the increase in the cost function when incorporating each $d \in CL'$ into the incumbent solution S and create a restricted candidate list RCL formed by nodes whose incremental costs are less than a defined threshold. From RCL , we randomly select the next delivery node to be incorporated into the incumbent solution and we determine its loading and unloading schedule with the procedure described in Algorithm 3. Next, we update S and the remaining quantities of the order and customer. Then we add to CL the next delivery node candidate. If an order o is not yet fulfilled after visiting d_o^j , the candidate is the next delivery node d_o^{j+1} . Otherwise, if the customer has remaining orders, the candidate is the first delivery node $d_{o'}^0$ of another randomly selected order o' .

The greedy aspect of the GRASP is the creation of the RCL set, the probabilistic aspect is the random selection in RCL , and the adaptive aspect is the update of CL and the reevaluating of the incremental costs. We use the additional set CL' because we noticed that restricting CL to delivery nodes with the same demand, delivery due time, or overlapping unloading timeslots helps us intensify the search. Using CL' also helps improve the algorithm complexity by reducing the number of nodes to evaluate. To diversify the search we simply remove the filter component. We thus obtain four greedy randomized insertion heuristics for our GRASP framework.

Algorithm 2 Greedy randomized insertion algorithm

Input: S : empty solution S

```

1  $CL \leftarrow \emptyset$ 
2 for each customer  $i$ 
3   | Select a random order  $o_1 \in \mathcal{O}_i$ 
4   |  $CL \leftarrow CL \cup \{d_{o_1}^0\}$ 
5 while  $CL \neq \emptyset$  do
6   |  $CL' \leftarrow \text{Filter}(CL)$ 
7   | for each  $d \in CL'$ 
8     |  $C(d) \leftarrow$  incremental cost of inserting  $d$ 
9   |  $C_{min} \leftarrow \min \{C(d), d \in CL'\}, C_{max} \leftarrow \max \{C(d), d \in CL'\}$ 
10  |  $RCL \leftarrow \{d \in CL, C(d) \leq C_{min} + \alpha(C_{max} - C_{min})\}$ 
11  | Select random delivery node  $d_o^j$  of customer  $i$  from  $RCL$ 
12  |  $L_{d_o^j}, U_{d_o^j} = \text{ScheduleTasks}(d_o^j, S)$ 
13  |  $S \leftarrow S \cup (L_{d_o^j}, U_{d_o^j})$ 
14  |  $q_i \leftarrow q_i - q_{d_o^j}; q_o \leftarrow q_o - q_{d_o^j}$ 
15  | if  $q_o \neq 0$  then
16    |  $CL \leftarrow CL \cup \{d_o^{j+1}\}$ 
17  | else if  $q_i \neq 0$  then
18    | Select another order  $o' \in \mathcal{O}_i$ 
19    |  $CL \leftarrow CL \cup \{d_{o'}^0\}$ 
20  | Update  $CL$ 
21 return  $S$ 

```

378 Algorithm 3 takes as parameters a delivery node d_o^i of the customer i and a partial
 379 solution and looks for a plant and a driver available for loading and unloading operations.
 380 For each driver k and plant b we simulate the loading and unloading operations while
 381 checking the concrete lifespan constraints, and the plant and driver availability. For each
 382 node, we first determine the start loading time SLT by subtracting t_{bi} , α_b , and the loading
 383 duration $LD_{d_o^i}^b$ to the expected delivery time EDT . EDT is either the arrival time a_i for
 384 the first delivery of a customer or the end of the unloading of the precedent delivery. At line
 385 15, we ensure with the procedure *FindDriverLoadingSlot* that the loading starts only if the
 386 driver is present at the depot. The presence of the driver does not guarantee that the loading
 387 dock is available, thus we use the procedure *FindDepotLoadingSlot* at line 16 to ensure that.
 388 Once we know SLT , we can easily deduce the arrival time (AT), start unloading time
 389 (SUT), driver waiting time ($W_{d_o^i}^k$), and client waiting time ($W_{d_o^i}$). We also keep track of the
 390 driver's work duration. The algorithm returns the best loading and unloading operations
 391 with the least cost. We keep track of all timeslots for a plant when its loading dock is
 392 busy, and for a driver when he starts loading until the end of the unloading service. Within
 393 *FindDepotLoadingSlot* (*FindDriverLoadingSlot*), we iterate through the timeslots of a depot
 394 (driver) to schedule the current operation at a free timeslot. These allow us to insert the
 395 scheduling of a node between existing schedules.

Algorithm 3 Schedule loading and unloading tasks

Input: Partial solution S , delivery node d_o^j

```
1 Function ScheduleTask( $d_o^j, S$ )
2    $n_i$ : last node visited for the customer  $i$ 
3    $\mathcal{LS}$ : Partial solutions list
4    $bestSol$   $Cost(bestSol) = +\infty$ 
5   for each driver  $k$ 
6      $n_k$ : current location of  $k$  (plant or delivery node)
7     for each plant  $b$ 
8       if  $t_{bi} \geq \delta$  then continue
9        $EDT = SUT = a_i$ 
10      if  $n_i \neq null$  then
11         $SUT = rand(EUt_{n_i} - \gamma/3, EUt_{n_i})$ 
12         $EDT = EUt_{n_i}$ 
13       $q_o^j = \min\{Q_k, q_o\} // q_o$  remaining demand of order  $o$ 
14       $SLT = EDT - t_{bi} - \alpha_b - LD_{d_o^j}^b$ 
15       $SLT = FindDriverLoadingSlot(b, n_k, SLT, LD_{d_o^j}^b)$ 
16       $SLT = FindDepotLoadingSlot(b, SLT, LD_{d_o^j}^b)$ 
17       $AT = SLT + LD_{d_o^j}^b + \alpha_b + t_{bi}$ 
18       $SUT = \max\{AT, EDT\}$ 
19       $W_{d_o^j}^k = \max\{0, SUT - AT\}$ 
20       $W_{d_o^j} = \max\{0, AT - EDT - \lambda_i\}$ 
21       $EUT = SUT + UD_{d_{ij}^p}$ 
22       $WT = WT_k + (EUT + \beta_k - SLT) + t_{n_k b} + t_{i,k}$ 
23       $TC = t_{n_k, b} + t_{b, i}$ 
24      if  $Cost(bestSol) < Cost(S) + TC$  then
25         $bestSol = (j, b, k, SLT) \cup (j, b, k, SUT)$ 
26         $Cost(bestSol) = Cost(S) + TC$ 
27  return  $bestSol$ 
```

396 **Local Search**397 **5 Experimental results**398 **5.1 Data sets**399 **6 Conclusion**400 **Acknowledgments**

401 Financial support for this work was provided by the Canadian Natural Sciences and
402 Engineering Research Council (NSERC) under grants 2015-04893 and 2019-00094. This
403 support is gratefully acknowledged.

References

- C. Archetti and M. G. Speranza. The split delivery vehicle routing problem: A survey. In *The vehicle routing problem: Latest advances and new challenges*, pages 103–122. Springer, 2008.
- L. Asbach, U. Dorndorf, and E. Pesch. Analysis, modeling and solution of the concrete delivery problem. *European Journal of Operational Research*, 193(3):820–835, 2009.
- J. Blazewicz, K. H. Ecker, E. Pesch, G. Schmidt, M. Sterna, and J. Weglarz. *Handbook on scheduling: From theory to practice*. Springer, 2019.
- M. Durbin and K. Hoffman. Or practice—the dance of the thirty-ton trucks: Dispatching and scheduling in a dynamic environment. *Operations Research*, 56(1):3–19, 2008.
- J. M Faria, C. A. Silva, J. MC Sousa, M. Surico, and U. Kaymak. Distributed optimization using ant colony optimization in a concrete delivery supply chain. In *2006 IEEE International Conference on Evolutionary Computation*, pages 73–80. IEEE, 2006.
- C.-W. Feng and H.-T. Wu. Integrating fmGA and CYCLONE to optimize the schedule of dispatching RMC trucks. *Automation in Construction*, 15(2):186–199, 2006.
- C.-W. Feng, T.-M. Cheng, and H.-T. Wu. Optimizing the schedule of dispatching rmc trucks through genetic algorithms. *Automation in Construction*, 13(3):327–340, 2004.
- T. A. Feo and M. GC Resende. Greedy randomized adaptive search procedures. *Journal of global optimization*, 6(2):109–133, 1995.
- M. Galić and I. Kraus. Simulation model for scenario optimization of the ready-mix concrete delivery problem. *Selected Scientific Papers-Journal of Civil Engineering*, 11(2):7–18, 2016.
- J. Garza Cavazos. *Dynamic planning and real-time monitoring of ready-mixed concrete delivery problem*. PhD thesis, Universidad Autónoma de Nuevo León, 2021.
- L. D. Graham, D. R. Forbes, and S. D. Smith. Modeling the ready mixed concrete delivery system with neural networks. *Automation in construction*, 15(5):656–663, 2006.
- O. A. Hernández López. *Study of mixed integer programming models for the concrete delivery problem*. PhD thesis, Universidad Autónoma de Nuevo León, 2020.
- J. Kinable and M. Trick. A logic based benders’ approach to the concrete delivery problem. In *International Conference on Integration of Constraint Programming, Artificial Intelligence, and Operations Research*, pages 176–192. Springer, 2014.
- J. Kinable, T. Wauters, and G. V. Berghe. The concrete delivery problem. *Computers & Operations Research*, 48:53–68, 2014.
- M. Lu and H.-C. Lam. Optimized concrete delivery scheduling using combined simulation and genetic algorithms. In *Proceedings of the Winter Simulation Conference*. IEEE, 2005.
- M. Maghrebi and S. T. Waller. Exploring experts decisions in concrete delivery dispatching systems using bayesian network learning techniques. In *2014 2nd International Conference on Artificial Intelligence, Modelling and Simulation*, pages 103–108. IEEE, 2014.

- 442 M. Maghrebi, V. Periaraj, S. T. Waller, and C. Sammut. Using benders decomposition for
443 solving ready mixed concrete dispatching problems. In *The 31st International Symposium*
444 *on Automation and Robotics in Construction and Mining*, 2014a.
- 445 M. Maghrebi, V. Periaraj, S. T. Waller, and Claude Sammut. Solving ready-mixed concrete
446 delivery problems: Evolutionary comparison between column generation and robust ge-
447 netic algorithm. In *Computing in Civil and Building Engineering (2014)*, pages 1417–1424.
448 2014b.
- 449 M. Maghrebi, S. T. Waller, and C. Sammut. Text mining approach for reviewing the
450 ready mixed concrete literature. In *2nd International Conference on Civil and Building*
451 *Engineering Informatics, University of Osaka, Tokyo, Japan*, pages 105–109, 2015.
- 452 M. Maghrebi, V. Periaraj, S. T. Waller, and C. Sammut. Column generation-based approach
453 for solving large-scale ready mixed concrete delivery dispatching problems. *Computer-*
454 *Aided Civil and Infrastructure Engineering*, 31(2):145–159, 2016a.
- 455 M. Maghrebi, S. Travis Waller, and Claude Sammut. Sequential meta-heuristic approach
456 for solving large-scale ready-mixed concrete–dispatching problems. *Journal of Computing*
457 *in Civil Engineering*, 30(1):04014117, 2016b.
- 458 M. Maghrebi, T. Waller, and C. Sammut. Matching experts’ decisions in concrete deliv-
459 ery dispatching centers by ensemble learning algorithms: Tactical level. *Automation in*
460 *Construction*, 68:146–155, 2016c.
- 461 N. F. Matsatsinis. Towards a decision support system for the ready concrete distribution
462 system: A case of a greek company. *European Journal of Operational Research*, 152(2):
463 487–499, 2004.
- 464 N. Mayteekrieangkrai and W. Wongthatsanekorn. Optimized ready mixed concrete truck
465 scheduling for uncertain factors using bee algorithm. *Songklanakarin Journal of Science*
466 *& Technology*, 37(2), 2015.
- 467 M. Misir, W. Vancroonenburg, K. Verbeeck, and G. V. Berghe. A selection hyper-heuristic
468 for scheduling deliveries of ready-mixed concrete. In *Proceedings of the metaheuristics*
469 *international conference (MIC 2011)*, pages 289–298. Udine, Italy, 2011.
- 470 F. Muresan. Comparing ready-mix concrete and site-mixed
471 concrete, 2019. URL [https://www.ny-engineers.com/blog/](https://www.ny-engineers.com/blog/ready-mix-concrete-and-site-mixed-concrete)
472 [ready-mix-concrete-and-site-mixed-concrete](https://www.ny-engineers.com/blog/ready-mix-concrete-and-site-mixed-concrete).
- 473 P. K. Narayanan, D. Rey, M. Maghrebi, and S. T. Waller. Using lagrangian relaxation to
474 solve ready mixed concrete dispatching problems. *Transportation Research Record*, 2498
475 (1):84–90, 2015.
- 476 D. Naso, M. Surico, B. Turchiano, and U. Kaymak. Genetic algorithms for supply-chain
477 scheduling: A case study in the distribution of ready-mixed concrete. *European Journal*
478 *of Operational Research*, 177(3):2069–2099, 2007.
- 479 A. Panas and J.-P. Pantouvakis. Simulation-based Concrete Truck-Mixers Fleet Size Deter-
480 mination for On-Site Batch Plant Operation. *Procedia - Social and Behavioral Sciences*,
481 74:459–467, 2013.
- 482 F. Payr and V. Schmid. Optimizing deliveries of ready-mixed concrete. In *2009 2nd Inter-*
483 *national Symposium on Logistics and Industrial Informatics*, pages 1–6, 2009.

- 484 M. G.C Resende and C. C Ribeiro. Greedy randomized adaptive search procedures: advances
485 and extensions. In *Handbook of metaheuristics*, pages 169–220. Springer, 2019.
- 486 V. Schmid, K. F. Doerner, M. W.P. Hartl, R. F. and Savelsbergh, and W. Stoecher. A
487 hybrid solution approach for ready-mixed concrete delivery. *Transportation Science*, 43
488 (1):70–85, 2009.
- 489 V. Schmid, K F. Doerner, R. F. Hartl, and J-J. Salazar-González. Hybridization of very
490 large neighborhood search for ready-mixed concrete delivery problems. *Computers &
491 Operations Research*, 37(3):559–574, 2010.
- 492 A. Sinha, N. Singh, G. Kumar, and S. Pal. Quality factors prioritization of ready-mix
493 concrete and site-mix concrete: A case study in indian context. In D. Singh, A. K.
494 Awasthi, I. Zelinka, and K. Deep, editors, *Proceedings of International Conference on
495 Scientific and Natural Computing*, Algorithms for Intelligent Systems, pages 179–187,
496 Singapore, 2021. Springer.
- 497 M. Sulaman, X. Cai, M. Misir, and Z. Fan. Simulated annealing with a time-slot heuristic
498 for ready-mix concrete delivery. In *Asia-Pacific Conference on Simulated Evolution and
499 Learning*, pages 39–50. Springer, 2017.
- 500 X. Tian, Y. Mohamed, and S. AbouRizk. Simulation-based aggregate planning of batch plant
501 operations. *Canadian Journal of Civil Engineering*, 37(10):1277–1288, 2010. Publisher:
502 NRC Research Press.
- 503 I.D. Tommelein and A. Li. Just-in-time concrete delivery: mapping alternatives for vertical
504 supply chain integration. In *Proceedings of the 7th Annual Conference of the International
505 Group for Lean Construction*, volume 7, pages 97–108, University of California, 1999.
506 Berkeley.
- 507 A. Tzanetos and M. Blondin. Systematic search and mapping review of the concrete delivery
508 problem (cdp): Formulations, objectives, and data. *Automation in Construction*, 145:
509 104631, 2023.
- 510 S. Q. Wang, C. L. Teo, and G. Ofori. Scheduling the truckmixer arrival for a ready mixed
511 concrete pour via simulation with @risk. *Journal of Construction Research*, 2(2):169–179,
512 2001.
- 513 S. Yan and W. Lai. An optimal scheduling model for ready mixed concrete supply with
514 overtime considerations. *Automation in Construction*, 16(6):734–744, 2007.
- 515 J. Yang, B. Yue, F. Feng, J. Shi, H. Zong, J. Ma, L. Shangguan, and S. Li. Concrete vehicle
516 scheduling based on immune genetic algorithm. *Mathematical Problems in Engineering*,
517 2022.
- 518 T. M. Zayed and D. Halpin. Simulation of concrete batch plant production. *Journal of
519 Construction Engineering and Management*, 127(2):132–141, 2001.