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Project 2 for CS 170 Winter 2021, with Dr. Eamonn Keogh

All code is original, except:

Libraries I used for file and terminal output:

1. Iostream
2. Fstream
3. Sstream
4. Iomanip

C++ containers to help store data:

1. Vector
2. Unordered\_set

Misc:

1. String: to store strings
2. Limits: to get max value of double
3. Cmath: to use sqrt() function
4. Ctime: to time my program

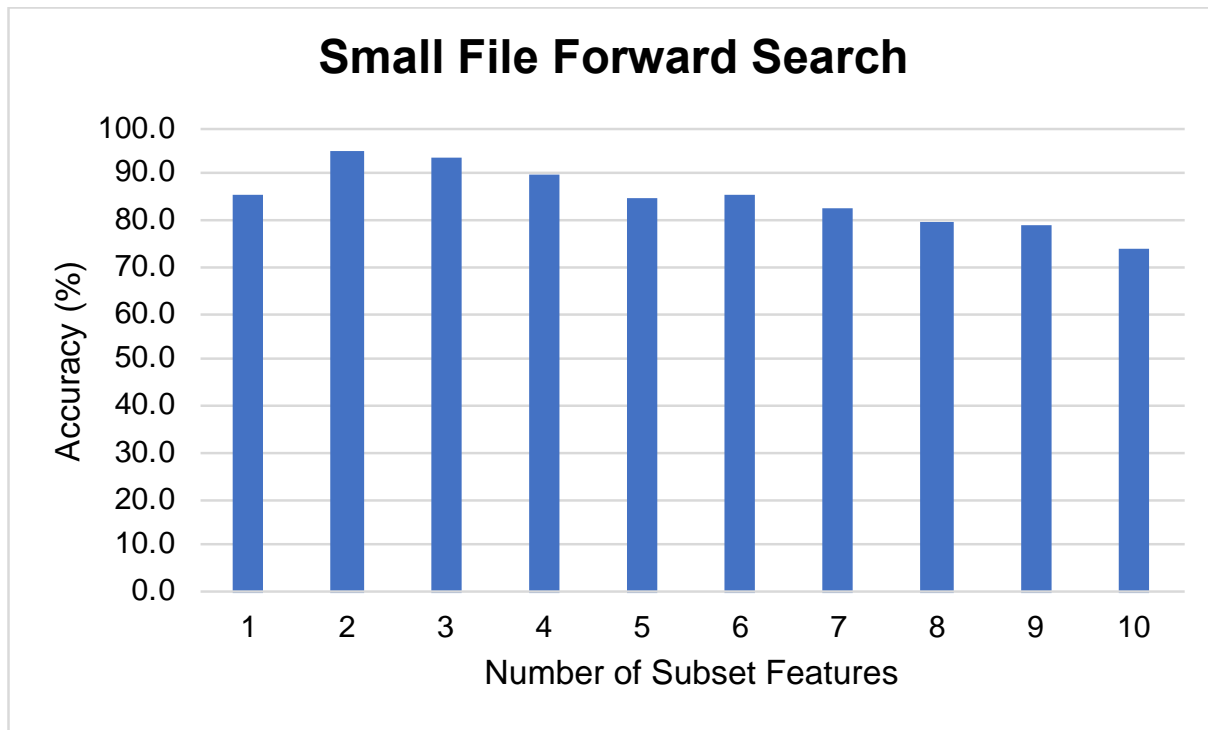
References for help:

1. For help with containers, string manipulation, and line parsing help, I used [www.cplusplus.com](http://www.cplusplus.com).
2. For help with timing my program I used [www.geeksforgeeks.org](http://www.geeksforgeeks.org)

In this project, we were tasked to implement a classification algorithm on a data set. Our goal was to classify data from a file and determine the accuracy of our classifications. The classification algorithm that we used for this project was the k nearest-neighbors algorithm. For this project, we only needed to find the nearest neighbor so k would default to 1. To figure out how accurate our classifications are, we are given test files that already have the correct classification. We compare our classifications with the correct ones and determine our accuracy.

Our next task was to find the best combination of features in our data set that would give us the highest accuracy. We used two different search algorithms to figure this out. For both search algorithms, we used a form of greedy search. We calculate what the accuracy of a combination of features, use the combination that has the best accuracy, and move on with our search. The first algorithm we used was forward selection search. With forward selection search, we start with no features and continuously add features that could increase our accuracy until we tried all possible features. The second algorithm we used was backwards elimination search. With backwards elimination search, we start with all the features and continuously remove features that could increase our accuracy until we have tried all possible features.

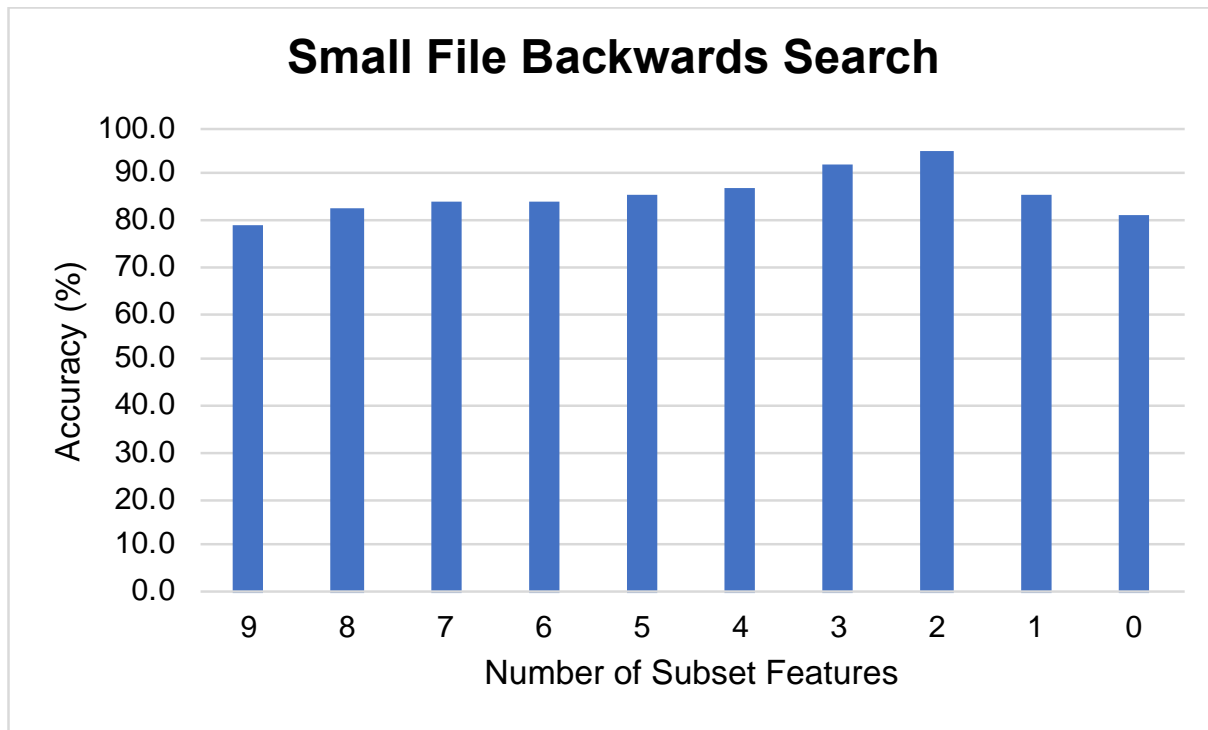
In Figure 1, we see the result of running forward selection search on CS170\_SMALLtestdata\_\_20.txt, which is the small file that was assigned to me.



**Figure 1:** Accuracy of increasing search levels where subset of features increases using forward selection search.

At the beginning of the search, we have no features added. When we add the first best feature, {3}, we start with 85.667% accuracy. From the graph, we can see that the max accuracy of 95.333% accuracy with the feature subset {3,4}. After we add more than 2 features, the accuracy of the classification algorithm decreases. From looking at the graph, it looks like we could have a possible third feature, '8', we can add even though the accuracy is 93.667%. The difference between the two subsets does not seem substantially big. At the end of the search, it seems that we have the lowest accuracy with all features included into our data. This accuracy was 74.000%.

In Figure 2, we see the result of running backwards elimination search on CS170\_SMALLtestdata\_\_20.txt, which is the small file that was assigned to me.



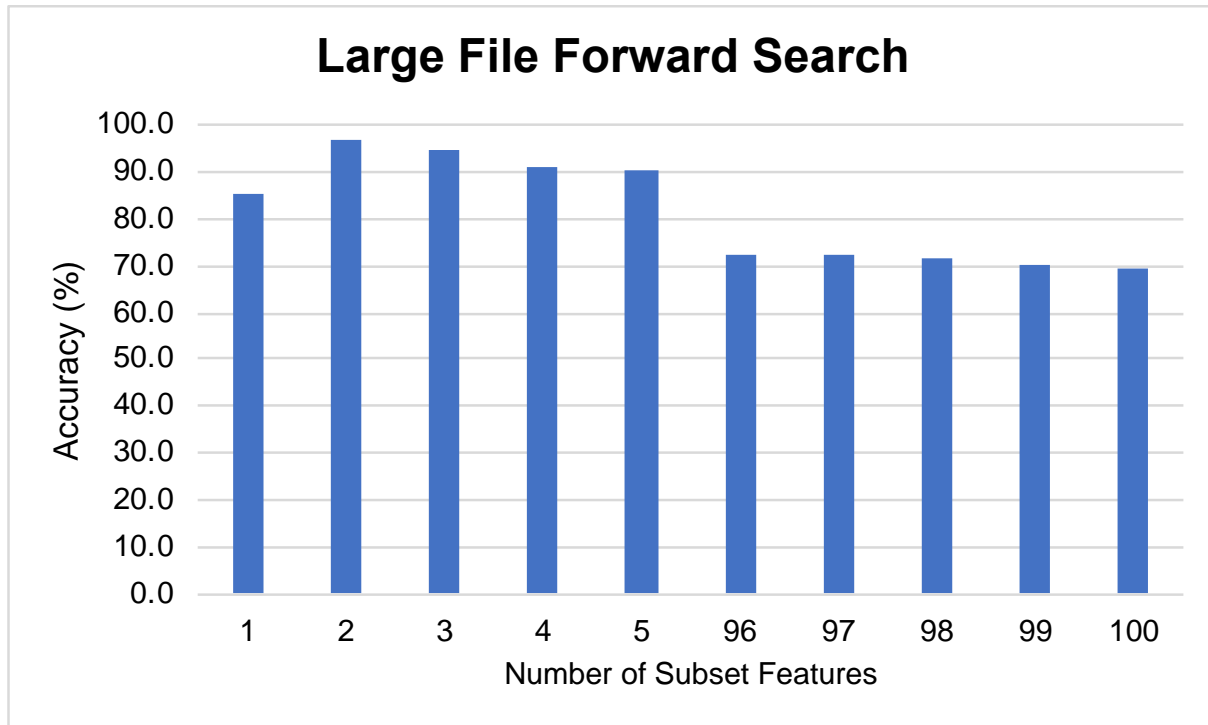
**Figure 2:** Accuracy of increasing search levels where subset of features increases using forward selection search.

At the beginning of the search, we have all features in our subset of features. The accuracy of removing the first feature seems to be 79.000%. As we remove features from the subset of features, we increase our accuracy. There seems to be a significant increase in accuracy when we have 2 features in our subset. When we have 2 features in our subset, {4,3}, we reach a maximum in our accuracy of subset features. The accuracy drastically decreases after removing one of these features.

### **Conclusion for Small Dataset**

From looking at the results from the forward search and backward elimination search algorithms, I can determine that feature '3' and feature '4' are the best subset of features. This is some evidence that feature '8' could also be a useful subset of features but there would need to be more research to see if that is true. The best accuracy for our best subset of features is 95.333%.

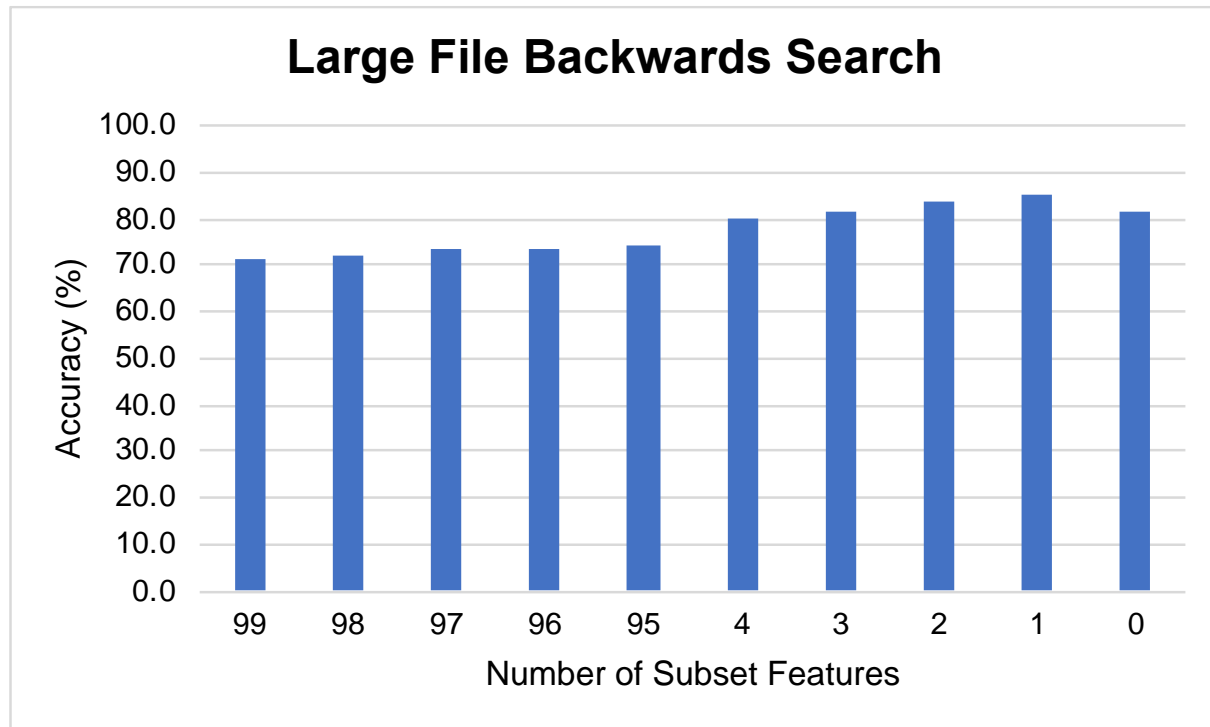
In Figure 3, we move onto a larger dataset. This will be a challenge because it has 100 features. This means there are 100 levels we have to search through to see the best combination of features. We can see here the result of running forward selection search on CS170\_largetestdata\_\_69.txt, which is the large file that was assigned to me.



**Figure 3:** Accuracy of increasing search levels where subset of features increases using forward selection search.

I have omitted the middle 90 levels to save space for the large dataset files. The first feature that I added, '40', turned out to have an 85.4% accuracy. When a second feature was added, our accuracy drastically increased. Our subset was {47, 40} when there were 2 features, with an accuracy of 97.0%. After the second feature was added, the accuracy of the search algorithm decreased slowly. When the third feature was added, for example, the accuracy was 95.0%. We reached the lowest accuracy of 69.4% when all features were in our subset.

In Figure 4, we see the result of running backwards elimination search on CS170\_targettestdata\_\_69.txt, which is the large file that was assigned to me.



**Figure 4:** Accuracy of increasing search levels where subset of features increases using forward selection search.

For Figure 4, I omitted the middle 90 subsets of features for space again. From looking at the chart, the accuracies of the subset of featured increased the more features you removed. With the backwards elimination search algorithm, the max accuracy seemed to be at a subset where there was only one feature. This subset was {40} with an accuracy of 85.4. I believe that this could be a slight mistake. When the subset of features had 2 features, {40, 47}, the accuracy was at 83.4. This could be the true subset because it was the result from the forward selection search.

### Conclusion of Large Dataset

From looking at the results from the forward search and backward elimination search algorithms, I can determine that feature '40' are the best subset of features. This is some evidence that feature '47' could also be a useful subset of features because this was the result subset of features from the forward search. More research would need to be done to determine if this were true. The best accuracy for our best subset of features is 85.4 %.

### Computational Effort for Search

I implemented these search algorithms with the classification algorithm in Python initially but decided to switch to C++. The speed of computations was proving to be too slow in Python. C++ helped me complete the search in less time. I ran all the experiments on a MacBook Pro with a 2.6 GHz 6-Core Intel Core i7. In Table 1, I report the running time for the four times I run the program.

	Small Dataset (10 features, 300 instances)	Large Dataset (100 features, 500 instances)
Forward Selection	10.408 seconds	2.5019 hours
Backward Search	13.256 seconds	3.4899 hours

**Table 1:** Showing the running time of each experiment.

**Below I show a single trace of my algorithm. I am only showing the forward selection search algorithm on the small dataset.**

```
./prog
Which test data file would you like to try.
    1. Small test data file
    2. Large test data file

1
Which search algorithm would you like to use?
    1. Forward Selection
    2. Backward Elimination

2
Number of features: 10
Number of instances: 300
```

On level 1 of the search tree

- Considering removing feature 1 with 75.333% accuracy.
- Considering removing feature 2 with 76.000% accuracy.
- Considering removing feature 3 with 74.667% accuracy.
- Considering removing feature 4 with 69.000% accuracy.
- Considering removing feature 5 with 74.667% accuracy.
- Considering removing feature 6 with 74.000% accuracy.
- Considering removing feature 7 with 78.667% accuracy.
- Considering removing feature 8 with 75.333% accuracy.
- Considering removing feature 9 with 71.667% accuracy.
- Considering removing feature 10 with 79.000% accuracy.
- Removed feature 10

On level 1 , the best feature subset was { 9 8 7 6 5 4 3 2 1 } . Accuracy was 79.000%

On level 2 of the search tree

- Considering removing feature 1 with 81.000% accuracy.
- Considering removing feature 2 with 74.000% accuracy.
- Considering removing feature 3 with 74.333% accuracy.
- Considering removing feature 4 with 71.667% accuracy.
- Considering removing feature 5 with 82.667% accuracy.
- Considering removing feature 6 with 76.000% accuracy.
- Considering removing feature 7 with 81.667% accuracy.
- Considering removing feature 8 with 77.000% accuracy.
- Considering removing feature 9 with 77.333% accuracy.
- Removed feature 5

On level 2 , the best feature subset was { 9 8 7 6 4 3 2 1 } . Accuracy was 82.667%

**{Here I delete half of the output to save space.}**

On level 8 of the search tree

- Considering removing feature 2 with 95.333% accuracy.
- Considering removing feature 3 with 83.333% accuracy.
- Considering removing feature 4 with 70.333% accuracy.
- Removed feature 2

On level 8 , the best feature subset was { 4 3 } . Accuracy was 95.333%

On level 9 of the search tree

- Considering removing feature 3 with 85.667% accuracy.
- Considering removing feature 4 with 71.333% accuracy.
- Removed feature 3

\*\*\*\* Warning accuracy has decreased! Continuing search in case of local maxima. \*\*\*\*

On level 9 , the best feature subset was { 4 } . Accuracy was 85.667%

On level 10 of the search tree

- Considering removing feature 4 with 81.000% accuracy.



Removed feature 4

\*\*\*\* Warning accuracy has decreased! Continuing search in case of local maxima. \*\*\*\*

On level 10 , the best feature subset was { } . Accuracy was 81.000%

Finished search! The best feature subset is { 3 4 } , which had an accuracy of 95.333%

Search took 13.283 seconds to find best combination of features.

**Code: Below is my code for the project. If you wish to download it for yourself, you can go to my GitHub to download it. [My GitHub](#)**

```
#include <iostream>
#include <fstream>
#include <sstream>
#include <string>
#include <iomanip>
#include <vector>
#include <unordered_set>
#include <limits>
#include <cmath>
#include <ctime>

using namespace std;

void print_menu(int (&choices)[2]);
void get_data(int choice, vector<vector<double> > &arr, int (&data_info)[2]);
void forward_selection_search(const vector<vector<double> > &data);
void backward_elimination_search(const vector<vector<double> > &data);
vector<double> relevant_features_data(const vector<double> &data, const
unordered_set<unsigned> &set_features);
double euclidean_distance(const vector<vector<double> > a, const vector<vector<double> > b);
double leave_one_out_cross_validation(const vector<vector<double> > &data, const
unordered_set<unsigned> &current_features, unsigned k, string alg="fss");
void print_set(const unordered_set<unsigned> &set);
void output_set_to_file(const unordered_set<unsigned> &set);

int main() {
    //      Timer variables
    clock_t start, end;
    double total_time = 0.0;
    //      Will store our user's choices from the menu
    //      choices[0] will be our data file choice
    //      choices[1] will be our algorithm choice
    int choices[2];
    vector<vector<double> > data;
```

```

//      data_info[0] will hold number of features in data data_info[1] will hold number of
instances
int data_info[2];

//      Print our menu and get the user's choices for data file and algorithm choice
print_menu(choices);

//      Get data from our data file
get_data(choices[0], data, data_info);
cout << "Number of features: " << data_info[0] << "\n" << "Number of instances: " <<
data_info[1] << "\n" << endl;

//      Start timer
start = clock();
//      Call our search algorithm
if(choices[1] == 1) {
    forward_selection_search(data);
}
else {
    backward_elimination_search(data);
}
end = clock();
total_time = double(end-start)/(double)(CLOCKS_PER_SEC);
cout << "Search took " << total_time << " seconds to find best combination of features."
<< endl;

}

void print_menu(int (&choices)[2]) {
    string algs[2] = { "Forward Selection Search", "Backward Elimination Search" };
    string alg_name;
    int file_choice = 0, alg_choice = 0;
    int ret[2];

    //      Ask user which test data we would like to try
    cout << "Which test data file would you like to try.\n"
           "\t1. Small test data file\n"
           "\t2. Large test data file\n"
           << endl;
    cin >> file_choice;

    //      Check to see if we were given the right input
    if(file_choice != 1 && file_choice != 2){
        cout << "Your choice can only be \"1\" or \"2\"...exiting";
        exit(0);
    }
}

```

```

//      Ask user which test data we would like to try
cout << "Which search algorithm would you like to use?\n"
      "\t1. Forward Selection\n"
      "\t2. Backward Elimination\n"
      << endl;
cin >> alg_choice;

//      Check to see if we were given the right input
if(alg_choice != 1 && alg_choice != 2){
    cout << "Your choice can only be \"1\" or \"2\"...exiting";
    exit(0);
}

choices[0] = file_choice;
choices[1] = alg_choice;

//      Output filename to file
alg_name = algs[alg_choice-1];
ofstream accuracy_file("./large_file_accuracy_cpp.txt", ios_base::app);
accuracy_file << alg_name << endl;
accuracy_file.close();
}

void get_data(int choice, vector<vector<double>> &arr, int (&data_info)[2]) {
    string files[2] = { "CS170_SMALLtestdata__20.txt", "CS170_largetestdata__69.txt" };
    string filename = files[choice-1];
    ifstream data_file(filename);
    stringstream ss;
    string line;
    string str_num;
    double num = 0;

    //      Check if we opened file
    if(data_file.is_open()) {
        //      First look at file line by line
        while(getline(data_file, line)) {
            //      vector to hold our columns
            vector<double> cols;
            //      Parse the numbers from each line
            istringstream scientific_string(line);
            while(scientific_string >> num) {
                //      Place our numbers in our vector of columns
                cols.push_back(num);
            }
        }
    }
}

```

```

        //      Place our vector of columns into our vector of vectors
        arr.push_back(cols);
    }

    //      close data file
    data_file.close();
}
else {
    cout << "Error opening file...exiting" << endl;
    exit(0);
}

//      Number of features
data_info[0] = arr[0].size() - 1;
//      Number of instances
data_info[1] = arr.size();

//      Output filename to file
ofstream accuracy_file("./large_file_accuracy_cpp.txt", ios_base::app);
accuracy_file << filename << endl;
accuracy_file.close();
}

void forward_selection_search(const vector<vector<double> > &data) {
    //      Size of Second dimension in the 2D array
    unsigned size = data[0].size();
    //      This set will have our current set of features
    unordered_set<unsigned> current_features;
    double best_accuracy_overall = 0.0;
    //      This set will have our best set of features
    unordered_set<unsigned> best_features_overall;
    //      Feature we would like to add to this level
    unsigned feature_to_add;
    //      This will track our best accuracy so far
    double best_accuracy;
    //      This will track our accuracy for each cross validation
    double accuracy;
    //      Iterator for unordered set
    unordered_set<unsigned>::const_iterator iter;

    //      Skip first column because the data is just the class label.
    for(unsigned i = 1; i < size; i++) {

        feature_to_add = 0;
        best_accuracy = 0.0;
    }
}

```

```

        cout << "On level " << i << " of the search tree" << endl;
        for(unsigned k = 1; k < size; k++) {
            //      Check if feature has not been added yet. Check if we should add
this one
            iter = current_features.find(k);
            //      If iter is end, that means feature is not in the set
            if(iter == current_features.end()) {
                accuracy = leave_one_out_cross_validation(data, current_features,
k);
                cout << "\tConsidering adding feature " << k << " with " << fixed
<< setprecision(3) << (accuracy*100) << "% accuracy." << endl;

                if(accuracy > best_accuracy) {
                    best_accuracy = accuracy;
                    feature_to_add = k;
                }
            }

            current_features.insert(feature_to_add);
            cout << "\tAdded feature " << feature_to_add << endl;

            if(best_accuracy > best_accuracy_overall) {
                best_accuracy_overall = best_accuracy;
                best_features_overall = current_features;
            }
            else{
                cout << "**** Warning accuracy has decreased! Continuing search in case
of local maxima. ****" << endl;
            }

            cout << "On level " << i << " , the best feature subset was ";
            print_set(current_features);
            cout << " . Accuracy was " << fixed << setprecision(3) << (best_accuracy*100)
<< "%\n" << endl;

            //      Output accuracy to file
            ofstream accuracy_file("./large_file_accuracy_cpp.txt", ios_base::app);
            accuracy_file << fixed << setprecision(3) << (best_accuracy*100) << "\n";
            accuracy_file.close();
        }

        cout << "Finished search! The best feature subset is ";
        print_set(best_features_overall);
        cout << " , which had an accuracy of " << fixed << setprecision(3) <<
(best_accuracy_overall*100) << "% " << endl;

```

```

//      Output accuracy to file
ofstream accuracy_file("./large_file_accuracy_cpp.txt", ios_base::app);
accuracy_file << "Best set: ";
accuracy_file.close();
output_set_to_file(best_features_overall);
accuracy_file.open("./large_file_accuracy_cpp.txt", ios_base::app);
accuracy_file << " which had an accuracy of " << fixed << setprecision(3) <<
(best_accuracy_overall*100) << endl;
accuracy_file.close();
}

void backward_elimination_search(const vector<vector<double> > &data) {
//      Size of Second dimension in the 2D array
unsigned size = data[0].size();
//      This set will have our current set of features
unordered_set<unsigned> current_features;
double best_accuracy_overall = 0.0;
//      This set will have our best set of features
unordered_set<unsigned> best_features_overall;
//      Feature we would like to add to this level
unsigned feature_to_remove;
//      This will track our best accuracy so far
double best_accuracy;
//      This will track our accuracy for each cross validation
double accuracy;
//      Iterator for unordered set
unordered_set<unsigned>::const_iterator iter;

//      Initiate current_features and best_features_overall sets to have all features
for(unsigned i = 1; i < size; i++) {
    current_features.insert(i);
    best_features_overall.insert(i);
}

//      Skip first column because the data is just the class label.
for(unsigned i = 1; i < size; i++) {

    feature_to_remove = 0;
    best_accuracy = 0.0;

    cout << "On level " << i << " of the search tree" << endl;
    for(unsigned k = 1; k < size; k++) {
        //      Check if feature has been removed already
        iter = current_features.find(k);
        //      If iter is not end, that means feature is in the set
    }
}

```

```

        if(iter != current_features.end()) {
            accuracy = leave_one_out_cross_validation(data, current_features,
k, "bes");

            cout << "\tConsidering removing feature " << k << " with " <<
fixed << setprecision(3) << (accuracy*100) << "% accuracy." << endl;

            if(accuracy > best_accuracy) {
                best_accuracy = accuracy;
                feature_to_remove = k;
            }
        }

        current_features.erase(feature_to_remove);
        cout << "\tRemoved feature " << feature_to_remove << endl;

        if(best_accuracy > best_accuracy_overall) {
            best_accuracy_overall = best_accuracy;
            best_features_overall = current_features;
        }
        else{
            cout << "***** Warning accuracy has decreased! Continuing search in case
of local maxima. *****" << endl;
        }

        cout << "On level " << i << " , the best feature subset was ";
        print_set(current_features);
        cout << " . Accuracy was " << fixed << setprecision(3) << (best_accuracy*100)
<< "%\n" << endl;

        //      Output accuracy to file
        ofstream accuracy_file("./large_file_accuracy_cpp.txt", ios_base::app);
        accuracy_file << fixed << setprecision(3) << (best_accuracy*100) << "\n";
        accuracy_file.close();
    }

    cout << "Finished search! The best feature subset is ";
    print_set(best_features_overall);
    cout << " , which had an accuracy of " << fixed << setprecision(3) <<
(best_accuracy_overall*100) << "%" << endl;

    //      Output accuracy to file
    ofstream accuracy_file("./large_file_accuracy_cpp.txt", ios_base::app);
    accuracy_file << "Best set: ";
    accuracy_file.close();
    output_set_to_file(best_features_overall);

```

```

        accuracy_file.open("./large_file_accuracy_cpp.txt", ios_base::app);
        accuracy_file << " which had an accuracy of " << fixed << setprecision(3) <<
(best_accuracy_overall*100) << endl;
        accuracy_file.close();
    }

```

```

vector<double> relevant_features_data(const vector<double> &data, const
unordered_set<unsigned> &set_features) {
    vector<double> rel_features;
    unsigned feature;

    for(unordered_set<unsigned>::iterator iter = set_features.begin(); iter !=
set_features.end(); iter++) {
        feature = *iter;
        rel_features.push_back(data[feature]);
    }

    return rel_features;
}

```

```

double euclidean_distance(const vector<double> a, const vector<double> b) {
    double sum = 0.0;
    unsigned size = 0;
    double diff = 0.0;

    if(a.size() == b.size()) {
        size = a.size();
    }
    else {
        cout << "Error: Sizes of array are not the same...exiting" << endl;
        exit(0);
    }

    // Calculate the difference and raise to power of 2
    for(unsigned i = 0; i < size; i++) {
        diff = a[i] - b[i];
        sum += diff*diff;
    }

    return sqrt(sum);
}

```

```

double leave_one_out_cross_validation(const vector<vector<double> > &data, const
unordered_set<unsigned> &current_features, unsigned k, string alg) {

```



```

//      Size of first dimension in the 2D array
unsigned size = data.size();
unsigned num_correctly_classified = 0;
//      Copy our current_features and add the k feature we want to add into our
test_features set
unordered_set<unsigned> test_features = current_features;
vector<double> object_to_classify;
double label_object_to_classify = 0.0;
//      Calculated distance
double distance = 0.0;
//      Nearest neighbor values
vector<double> nn_object;
double nn_dist = 0.0, nn_label = 0.0;
unsigned nn_loc = 0;
//      Accuracy we will be returning
double accuracy = 0;

if(alg == "fss"){
    test_features.insert(k);
}
else{
    test_features.erase(k);
}

for(unsigned i = 0; i < size; i++){
    object_to_classify = relevant_features_data(data[i], test_features);
    label_object_to_classify = data[i][0];

    //      Nearest neighbor distance and location will initially be infinity
    nn_dist = numeric_limits<double>::max();
    nn_loc = numeric_limits<double>::max();

    //      Try to find the nearest neighbor to our object to classify by checking every
data point
    for(unsigned k = 0; k < size; k++) {
        //      We should skip over the data point that is our object to classify
        if(k != i) {
            nn_object = relevant_features_data(data[k], test_features);
            //      Euclidean distance
            distance = euclidean_distance(object_to_classify, nn_object);

            if(distance < nn_dist) {
                nn_dist = distance;
                nn_loc = k;
                nn_label = data[nn_loc][0];
            }
        }
    }
}

```

```

        }
    }

    //      If we classify objects correctly increment num_correctly_classified
    if(label_object_to_classify == nn_label) {
        num_correctly_classified++;
    }
}

accuracy = (double)num_correctly_classified/((double)size;

return accuracy;

}

void print_set(const unordered_set<unsigned> &set) {
    unsigned feature = 0;

    cout << "{ ";
    for(unordered_set<unsigned>::iterator iter = set.begin(); iter != set.end(); iter++) {
        feature = *iter;
        cout << feature << " ";
    }
    cout << "}";
}

void output_set_to_file(const unordered_set<unsigned> &set) {
    unsigned feature = 0;
    ofstream file("./large_file_accuracy_cpp.txt", ios_base::app);

    file << "{ ";
    for(unordered_set<unsigned>::iterator iter = set.begin(); iter != set.end(); iter++) {
        feature = *iter;
        file << feature << " ";
    }
    file << "}";
    file.close();
}

```