

Computer Organization

AND

Assembly Language (CMP-223)

~Assignment - 01B~

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Problem 1:

$(41A7)_{16}$

Binary:

$$(41A7)_{16} = (4 \times 16^3) + (1 \times 16^2) + (10 \times 16^1) + (7 \times 16^0)$$

$$= 16384 + 256 + 160 + 7$$

$$= (16807)_{10}$$

Now

$(0100000110100111)_2$

Decimal:

$$= (1607)_{10}$$

Octal:

$(100\bar{0}\bar{0} \ \bar{1}\bar{1}0 \ \bar{1}\bar{0}0 \ \bar{1}\bar{1}1)_2$

$(4 \ 0 \ 6 \ 4 \ 7)_8$

$$\begin{array}{r}
 2 | 16807 \\
 2 | 8403-1 \\
 2 | 4201-1 \\
 2 | 2100-1 \\
 2 | 1050-0 \\
 2 | 525-0 \\
 2 | 262-1 \\
 2 | 131-0 \\
 2 | 65-1 \\
 2 | 32-1 \\
 2 | 16-0 \\
 2 | 8-0 \\
 2 | 4-0 \\
 2 | 2-0 \\
 \hline
 & 1-0
 \end{array}$$

Note: As the number is +ve (it's using signed value), so it'll be same for 2's, 1's and Signed magnitude methods.

Problem-02:-

In signed magnitude method,
MSB is reserved for sign and
remaining bits are used for magnitude. It
works well for representing +ve and -ve
integers (although the two os are bothersome).

But it doesn't work well in computation.

It produces undesired results while
subtraction (addition of +ve and -ve numbers).

For example:

$$\begin{array}{r} (13) \rightarrow 1101 \\ + (-6) \quad \underline{\quad 1110 \quad} \\ 7 \quad \underline{111011} \rightarrow \text{which isn't correct} \\ \text{answers.} \end{array}$$

So we need a separate hardware
for subtraction in signed magnitude.

1s and 2s complement

methods don't require any
additional hardware for subtraction.

But 1s complement method

has two different representations
for zero. (+ve 0: 0000)
and (-ve 0: 1111). So this
produce some undesire results.

```
#include <stdio.h>
```

```
#include <limits.h> // A Library that have
```

```
int main() { // macros for data types limits.
```

```
    printf("Signed char minimum=%d\n", SCHAR_MIN);
```

```
    printf("Signed char maximum=%d\n", SCHAR_MAX);
```

```
    printf("Unsigned char maximum=%d\n", UCHAR_MAX);
```

```
    printf("Signed short minimum=%d\n", SHRT_MIN);
```

```
    printf("Signed short maximum=%d\n", SHRT_MAX);
```

```
    printf("Unsigned short maximum=%d\n", USHORT_MAX);
```

```
    printf("Signed int minimum=%d\n", INT_MIN);
```

```
    printf("Signed int maximum=%d\n", INT_MAX);
```

```
    printf("Unsigned int maximum=%d\n", UINT_MAX);
```

```
    printf("Long signed minimum=%ld\n", LONG_MIN);
```

```
    printf("Signed Long maximum=%ld\n", LONG_MAX);
```

```
    printf("Unsigned Long maximum=%ld\n", ULONG_MAX);
```

```
    printf("Signed Long Long min=%lld\n", LLONG_MIN);
```

```
    printf("Signed Long Long max=%lld\n", LLONG_MAX);
```

```
    printf("Unsigned Long Long max=%llu\n", ULLONG_MAX);
```

```
return 0;
```

```
}
```

Yes, the value that can a variable hold depends on hardware. It depends on word size or register size of the machine.

For example in C/C++ size of long-int is 4-byte in 32-bit machine. While it is of 8-byte in 64-bit machine. The compile is restricted with register size of installed OS (32-bit or 64-bit).

Problem 04:

a) 2's complement: (signed)

$$-(2^{15}) \text{ to } 2^{15} - 1$$

$$-32768 \text{ to } 32767$$

Unsigned :-

$$0 \text{ to } 2^{16}$$

$$0 \text{ to } 65536$$

b) 1's complement: (signed.)

c) also to signed magnitude:-

$$-(2^{15} - 1) \text{ to } (2^{15} - 1)$$

$$-32767 \text{ to } 32767$$

Problem 05:-

a) $0x86 + 0x84$

$$(86)_{16} \rightarrow (1000\ 0110)_2$$

$$(84)_{16} \rightarrow (1000\ 0100)_2$$

$$\boxed{1} 0000\ 1010$$

As carry in and carry out from
MSB is different so this is \downarrow overflow.

Carry Flag = 1

negative

Overflow flag = 1

b) $0x7E + 0x70$

$$\begin{array}{r} 7E \\ \longrightarrow \\ \boxed{0111\ 0000} \\ + 70 \\ \hline \textcircled{0} 11101110 \end{array}$$

As carry in and carry out are different, There is overflow.

Carry flag = 0

Overflow flag = 1

c) $0xF6 + 0x7E$

$$\begin{array}{r} F6 \\ \longrightarrow \\ \boxed{1111\ 0110} \\ + 7E \\ \hline \textcircled{1} 0111\ 0100 \end{array}$$

As carry in and carry out are same so their is no overflow.

Carry flag = 1

Overflow flag = 0

Problem 06:

```
#include <stdio.h>
```

```
#include <limits.h>
```

```
int main()
```

```
    int n1;
```

```
    unsigned int n2;
```

```
    n1 = INT_MAX; // stored maximum value
```

```
    n1 += 1 // Added 1 to test overflow
```

```
    printf("n1 = %.d\n", n1);
```

```
    n2 = UINT_MAX // stored max unsigned
```

```
    n2 += 1 // To test overflow
```

```
    printf("n2 = %u\n", n2);
```

```
    return 0;
```

```
}
```

In C/C++, when overflow occurs,
it will wrap around the
minimum value. For signed numbers,
it will start from -ve value.

For example, int has 2147483647
max value. When we add 1
to it, it will become -2147483648

which is the minimum value of signed int.

And it will become 0, if there is unsigned int.

However, C/C++ ~~—~~ does not produce any error or warning for overflow.

In some programming languages like Python and Ruby, they detect the overflow and allocate larger size memory to prevent data from losing. SWIFT language produces error if we didn't tell comput what to do in case of overflow.

Problem 07:-

Integer overflow vulnerabilities are occurred when a value is moved into a variable type too small to hold it.

One example is "Downcasting" from a long (which uses 64 bits) to an int (which uses 16 or 32 bits). This is accomplished by cutting the value down to a small enough size that it fits in the small value. If any of the bits that are dropped are non-zero, then the value suddenly becomes a lot smaller.

Basically, underflow term is closely related to floating point numbers. But, specifically for integers, integer underflow happen when a value becomes too small to fit. When this occurs, the value wraps around from

the minimum value that can be stored to the maximum.

Integer overflow and underflow vulnerabilities are useful to hack in a number of ways. The main reason for this is that these vulnerabilities can invalidate checks made to protect against other classes of vulnerabilities.

For example, a buffer overflow vulnerability is created when a developer fails to check the length of user-controlled input before placing it in a preallocated memory buffer.

Another application of integer overflow and underflow is defeating checks to determine if a value meets certain criteria, like ensuring that an account has a certain minimum balance before initiating a withdrawal.

Integer overflow and underflow vulnerabilities are caused by misuse of variable type conversions. Protecting against these vulnerabilities is fairly simple:

- ↳ use a language with dynamic variable typing (like python).
- ↳ Make sure that variable types are explicitly specified and the correct type for the job.

Problem 08: Unicode

Unicode Standard is a character coding system designed to support the worldwide interchange processing and display of the written texts of the diverse languages and technical disciplines of the modern world. In addition, it supports classical and historical texts of many written languages. It afford simplicity and consistency of ASCII, even correspond characters are same.

Some common encoding formats used by Unicode are

UTF-8, UTF-16, UTF-32

and several other encodings are in use. These are common implementation used now-a-days.

Windows uses UTF-16LE

for all things Unicode (except for `MultiByteToWideChar()` and

WideCharToMultiByte(), which support UTF-7, UTF-8, and UTF-16, amongst other characters installed in the OS).

In Linux, the most general list of world characters is usually encoded in UTF-8.

In Mac OS, Simrodo 3.31 uses default formate which is UTF-16, it can convert over 100 encodings to and from unicode (UTF-8 and big and little endian UTF-16).

Problem # 09:

The concept of floating point binary numbers were introduced in the mid 1950s. There was no uniformity in the formats used to represent floating point numbers and programs were not portable from one manufacturer's computer to another.

So a standards committee was formed by the Institute of Electrical and Electronics Engineers (IEEE) to standardize how floating point binary numbers would be represented in computers. In addition, the standard specified uniformity in rounding numbers, treating exception conditions such as

attempting to divide by 0, and representation of 0 and infinity (∞).

Part - ii expo-Bais | E-bits | D-bits | E-min | E-max

a) 32-bit $2^7 - 1 = 127$ | 8 | 23 | -126 | +127

b) 64-bit $2^{10} - 1 = 1023$ | 11 | 52 | -1022 | +1023

c) 128-bit $2^{14} - 1 = 16383$ | 15 | 112 | -16382 | +16383

d) 256-bit $2^{18} - 1 = 262143$ | 19 | 236 | -262142 | +262143

Problem 10:

For flexibility to choose whether they required more +ve or more -ve exponent numbers,

IEE designers used biased notation.

Moreover in basic notation, the exponents are in lexical order and allow easy comparison of Floating Point numbers.

If 14 bits are used to store the exponent, the biasing will be:

$$2^{14-1} = 2^{13}$$

$$= 8192 - 1 = 8191$$

And Range of exponent will be:

$$\text{EXP: } 1682 - 8192 = 8191$$

$$\text{Range: } \pm (2^{-13}) \times 2^{+8191}$$

$$= \pm 5.251761 \times 10^{+2431}$$

Problem 11:

Exponent in IEEE-754 is placed before mantissa so that comparison of floating point number is easily performed. The base exponent are in lexical order. In this way, for biased exponent it's simple to compare values. While in 2's complement, it's hard to compare the numbers because of negative and positive values.

Problem 12:

a) $(75.07539)_8$

Binary = $(1001011.00010011010011001)_2$

Normalizing:

$$(1.00101100010011010011001 \times 2^6)$$

Adding Biasing to exponent:

$$6 + 127 = 133 = 1000101$$

Sign Bit = 0

Now

$$\begin{array}{r} 01000010100101100010011010011001 \\ \hline \end{array}$$

$$(01000010100101100010011010011010)_2$$

↓ 1FE-754 Binary

$$\hookrightarrow (4296259A)_{16}$$

b) $(-128.25508)_{10}$

Binary = $-(1000000.010000010100110011)_2$

Normalizing = $(1.00000000100000010100110011 \times 2^3)_2$

Adding Biasing to exponent:-

$$7 + 127 = 134 = 10000110$$

sign - Bit = 1

$$\underline{10000110\ 00000000100000101001011}$$

$$\underline{1\ 10000110\ 00000000100\ 00010100101}$$

Problem 13:

$$(41A42.B43)_{16}$$

Binary:

$$(0100\ 0001\ 10\ \underline{1}0\ 0100\ 0010\ 1011\ 0100\ 0011)_2$$

Now

$$(0\ 100\ 00011\ 0100\ 1000010\ 10110100\ 0011)$$

$$\text{Exponent} = 100000_2 = (131)_{10}$$

$$\text{Removing biasing} = 131 - 127 = 4$$

$$\text{Sign} = 0$$

So

$$1.01001000010101101000011 \times 2^4$$

$$10100.1000010101101000011$$

$$20.(1 \times 2^{-1} + 1 \times 2^{-6} + 1 \times 2^{-8} + 1 \times 2^{-10} + 1 \times 2^{-11} + 1 \times 10^{-13} + 1 \times 10^{-78})$$

$$= 20.05211238861$$

Problem 14:-

```
#include <stdio.h>
#include <float.h>
int main(){
    printf("Precision of float = +- (%.e)\n", FLT_MIN);
    printf("Range of float = +- (%.e)\n", FLT_MAX);
    printf("Precision of double = +- (%.e)\n", DBL_MIN);
    printf("Range of double = +- (%.e)\n", DBL_MAX);
    printf("Precision of long double = +- (%.e)\n", LDBL_MIN);
    printf("Range of long double = +- (%.e)\n", LDBL_MAX);
    return 0;
}
```

In C/C++:

float = single precision

double = double precision

long double = quadruple precision.

Problem 15:

```
#include <stdio.h>
#include <float.h>
int main(){
    float n = FLT_MAX;
    n *= 1.5; // To check overflow
    printf("n = %.e\n", n);
    n = FLT_MIN;
    n /= 1e20; // To check underflow
    printf("n = %.e\n", n);
```

Floating point imprecision:

Floating point imprecision stems from the problem of trying to store numbers like $\frac{1}{10}$ or (0.10) in a computer with binary number system with a finite amount of zero numbers. In other words we can say recurring numbers.

Problem 16:

sign	Expo	Mantissa
+/- 0 = [0/1] 00000000 000000000000000000000000000000		

sign	Expo	Mantissa
+ (0) = [0/1] 1111111 000000000000000000000000000000		

Problem 17:i) Addition:

$$a = 01000010 00000000 01001100 01011001$$

$$b = 01000100 00100000 00000101 11010110$$

Now $a \rightarrow$ sign = 0

$$\text{expo} = 10000100 = 132$$

after biasing removed - $132 - 127 = 5$

$$\text{Mantissa} = [1.000000001001100 01011001 \times 2^5]$$

Similarly $b \rightarrow$ sign = 0

$$\text{expo} = 10001000 = 136$$

after biasing removed - $136 - 127 = 9$

$$\text{So } [1.01100000000011010110 \times 2^9]$$

For addition \rightarrow normalizing a:

$$0.000100000010011000100 \times 2^9$$

$$+ \frac{1.011000000000101110110 \times 2^9}{1.0111000000001010010101 \times 2^9}$$

Now moving back to IEEE-754.

$$a_1 + 127 = 136 = 10001000$$

so 1010001000011000000001010011011

or $0x44380A9B$

Subtraction:

As b is ~~greatly~~ greater than a:

so $b - a$:

$$1.011\overrightarrow{0}000000001011101\overleftarrow{0} \times 2^9$$

$$- 0.0010000000010011000101 \times 2^9$$

$$\underline{1.010100000000100010001 \times 2^9}$$

again moving back to IEEE-754

$$a_1 + 127 = 136 = 10001000$$

so

100010000101000000000000100010001

or $0xC4280111$